Subsystem correlations in Coulomb breakup reactions of ⁶He

Yuma Kikuchi (Hokkaido University)

Collaborators: T. Myo, M. Takashina, K. Kato and K. Ikeda

Two-neutron halo nuclei

• Exotic neutron pair – di-neutron

Spatially-correlated neutron pair was suggested over twenty years ago.



Coulomb breakup reactions

To probe the di-neutron correlations experimentally

- Some experiments were performed to investigate the Coulomb breakup reactions of halo nuclei.
 - For ⁶He
 - GSI and MSU data are available.

T. Aumann et al., PRC**59**(1999), 1252. J. Wang et al., PRC**65**(2002), 034306.

• For ¹¹Li

• MSU, RIKEN and GSI data are available.

K. Ieki et al., PRL70(1993), 730.
S. Shimoura et al., PLB348(1995), 29.
M. Zinser et al., NPA619(1997), 151.

T. Nakamura et al., PRL96(2006), 252502.

Coulomb breakup reactions

Observed data in Coulomb breakups

The low-lying peak is observed in the Coulomb breakups.



Di-neutron as n-n subsystem correlation

Di-neutron as the correlation of the n-n subsystems

- It is essential to analyze the observables as a function of energy of the n-n subsystem.
- Recently, some data were reanalyzed with respect to the subsystem correlations.
 - For ⁶He
 - Subsystem energy distributions of the breakup cross section

L.V. Chulkov et al., NPA759(2005), 23. S.N. Ershov et al., PRC74(2006), 014603.

• For ¹¹Li

Dalitz plot of E1 transition strength

T. Nakamura, DREB07 oral presentation and etc.

Motivation

To extract the di-neutron from the observables

 We estimate the E1 strength distribution with respect to the energies of the subsystems and investigate which subsystem correlation is important in the Coulomb breakups.

• To do:

• We need the description of the three-body scattering state, which is capable of investigating the subsystem correlations.

Approach based on the Lippmann-Schwinger Eq.

$$|\Psi^{(+)}(\mathbf{k},\mathbf{K})\rangle = |\mathbf{k},\mathbf{K}\rangle + \lim_{\varepsilon \to 0} \frac{1}{E - \hat{H} + i\varepsilon} \hat{V}|\mathbf{k},\mathbf{K}\rangle$$

- We start with the formal solutions of LS Eq.
- The formal solution is expressed by an asymptotic solution, which is an eigenstate of momenta of decaying particles.

Complex-scaled Green's function

A.T. Kruppa et al., PRC75(2007), 044602.

$$\mathcal{G}^{\theta}(E;\boldsymbol{\xi},\boldsymbol{\xi}') = \left\langle \boldsymbol{\xi} \left| \frac{1}{E - \hat{H}^{\theta}} \right| \boldsymbol{\xi}' \right\rangle = \sum_{i} \frac{\chi_{i}^{\theta}(\boldsymbol{\xi}) \tilde{\chi}_{i}^{\theta}(\boldsymbol{\xi}')}{E - E_{i}^{\theta}} \right\rangle$$

- Eigenstates in CSM have complex energy, and their imaginary parts shows the boundary conditions of each states.
- Using such eigenstates, we can include the boundary conditions in the Green's function.



Complex-scaled solutions of LS Eq. (CSLS)

$$\Psi^{(+)}(\mathbf{k},\mathbf{K})\rangle = |\mathbf{k},\mathbf{K}\rangle + \sum_{i} U^{-1}(\theta)|\chi_{i}^{\theta}\rangle \frac{1}{E - E_{i}^{\theta}} \langle \tilde{\chi}_{i}^{\theta}|U(\theta)\hat{V}|\mathbf{k},\mathbf{K}\rangle$$

The advantages in CSLS
 We can easily apply CSLS to the complicated systems.
 We can decompose the observables into the contribution of the direct breakups and the one of the sequential decays.

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- The advantages in CSLS
 - We can easily apply CSLS to the complicated systems.
 - The Green's function can be found by solving with the L² basis functions.
 - OCM, Coupled-channel method and other theoretical models can be applied in solving the eigenstates.

A.T. Kruppa et al., PRC75(2007), 044602.

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Direct breakups into non-resonant cont. Sequential decays via χ^{θ}_{i}

The advantages in CSLS

- We can decompose the observables into the contribution of the direct breakups and the one of the sequential decays.
 - We can easily switch on and off the decaying channels by including and excluding the eigenstates belonging to the selected decay modes.

Coulomb breakup cross section in CSLS

• The obtained cross section for ⁶He breakups

 Our result well reproduces the observed trend in the Coulomb breakup cross section.



Subsystem correlations in ⁶He

Two-dimensional energy distributions of E1 strength

$$\frac{dB(E1)}{d\varepsilon_1 d\varepsilon_2} = \iint d\mathbf{k} d\mathbf{K} \frac{dB(E1)}{d\mathbf{k} d\mathbf{K}} \delta\left(\varepsilon_1 - \frac{\hbar^2 k^2}{2\mu}\right) \delta\left(\varepsilon_2 - \frac{\hbar^2 K^2}{2M}\right)$$

Momentum distributions

$$\frac{dB(E1)}{d\mathbf{k}d\mathbf{K}} = \frac{1}{2J_{\text{g.s.}}+1} \left| \langle \Psi^{(+)}(\mathbf{k},\mathbf{K}) || \hat{O}(E1) || \Phi_{\text{g.s.}} \rangle \right|^2$$

Matrix elements

$$\begin{split} \langle \Phi_{\rm g.s.} | \hat{O}^{\dagger}(E1) | \mathbf{k}, \mathbf{K} \rangle \\ + \sum_{i} \langle \Phi_{\rm g.s.} | \hat{O}^{\dagger}(E1) U^{-1}(\theta) | \chi_{i}^{\theta} \rangle \frac{1}{E - E_{i}^{\theta}} \langle \tilde{\chi}_{i}^{\theta} | U(\theta) \hat{V} | \mathbf{k}, \mathbf{K} \rangle \end{split}$$

Correlations of ⁵He subsystem

• E1 strength with respect to ⁵He systems

- The distribution show the clear peak at 0.7 MeV of ⁵He subsystem energy.
 - \rightarrow ⁵He(3/2⁻) is important!!
- This is a consistent result with our previous work.



Correlation of n-n subsystem

• E1 strength with respect to n-n subsystem

- Strength is concentrated on the axis of $E_{nn}=0$.
- This result indicates the contribution of the virtual state of n-n system is important in the Coulomb breakups of ⁶He.



r, l

Which subsystem is important?

• E1 transition w/ and w/o the sequential decays

• We switch off the sequential process via ⁵He+n or/and α +2n.



 Contributions of both the ⁵He and 2n subsystems are important in the Coulomb breakup.

Summary

- We investigate the subsystems correlations by calculating the 2D distributions of the E1 strength.
 - We calculate the 2D distribution of the E1 strength using CSLS.
 - The two-neutron correlation in the Coulomb breakups is found as the virtual state of the n-n subsystem.
 - The correlations not only of the ⁵He, but also of the n-n subsystems are important to reproduce the observed low-lying peak in the observed cross section.