

# 高分解能測定における 高品質ビームへの期待

**Yoshitaka FUJITA (Osaka Univ.)**

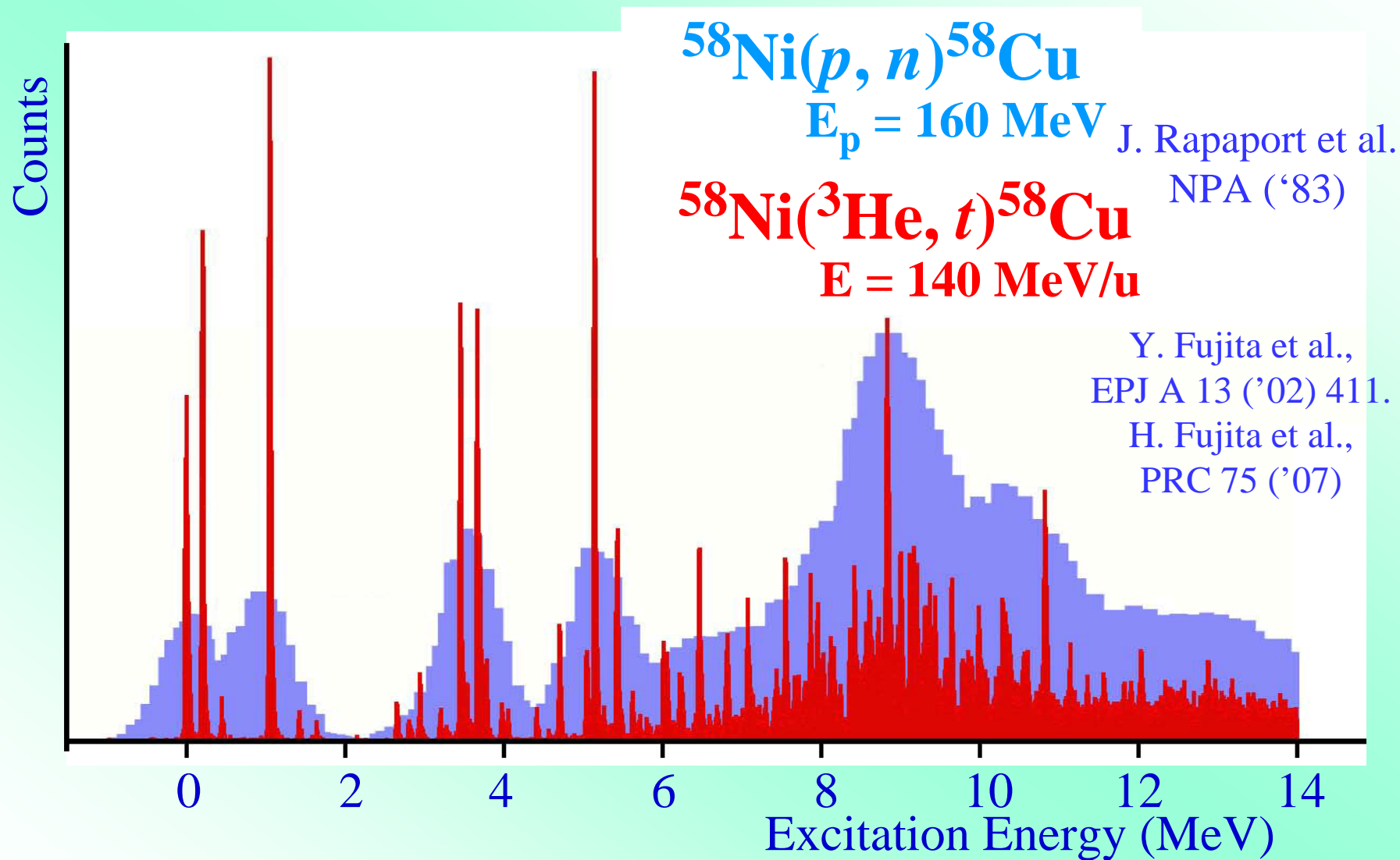
**RCNP** 入射サイクロトロン更新で展開される新しい研究

**2007 Feb. 19-20**

**RCNPでの高分解能研究と関連して**

\*\*\*High Resolution Experiment

# Comparison of (p, n) and ( $^3\text{He}, t$ ) spectra



# RCNP Ring Cyclotron

Good quality  $^3\text{He}$  beam (140 MeV/nucleon)

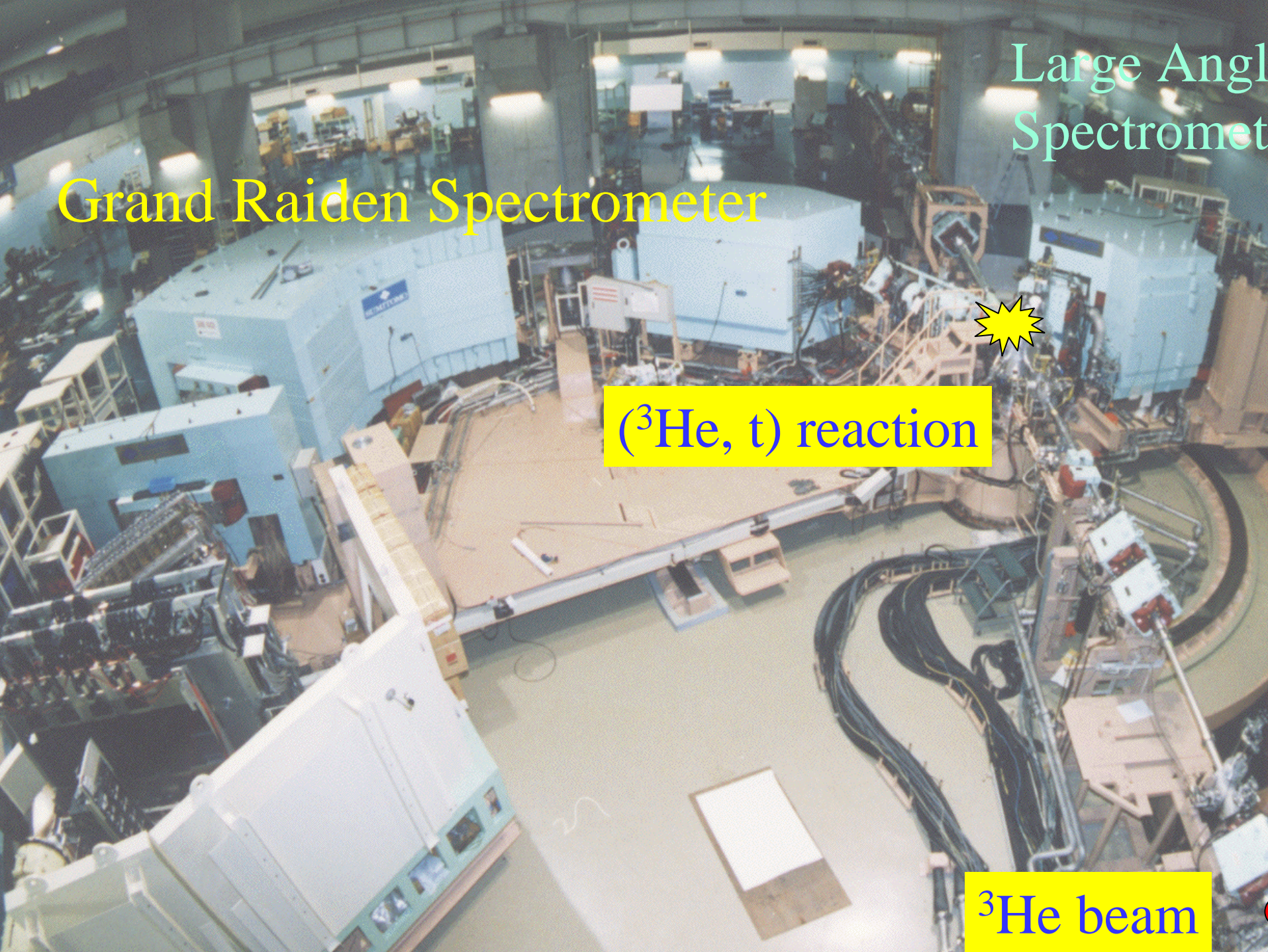


Large Angle  
Spectrometer

Grand Raiden Spectrometer

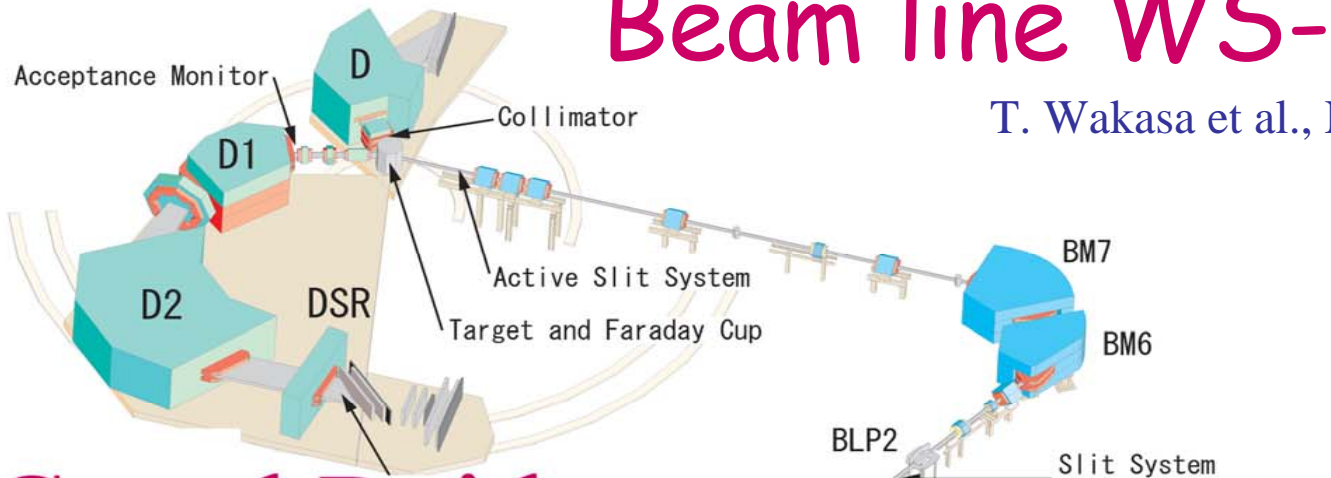
$(^3\text{He}, t)$  reaction

$^3\text{He}$  beam



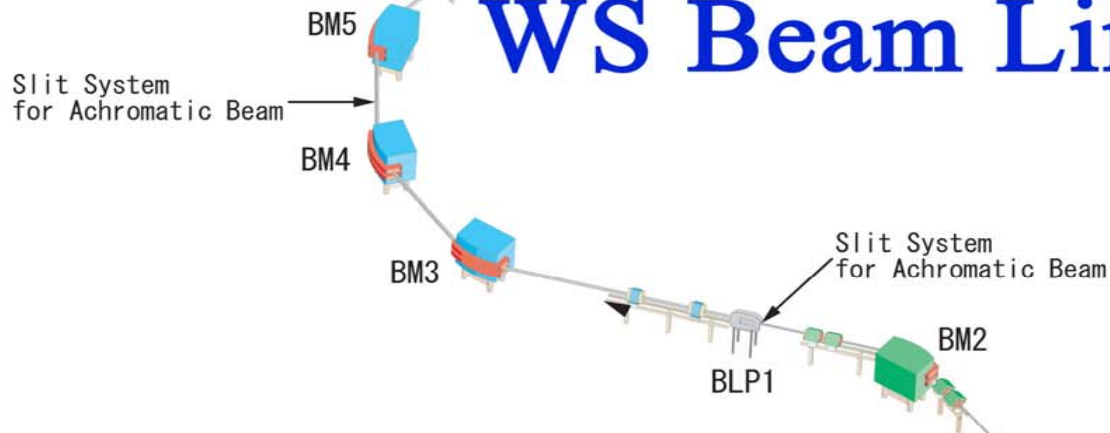
# Beam line WS-course

T. Wakasa et al., NIM A482 ('02) 79.

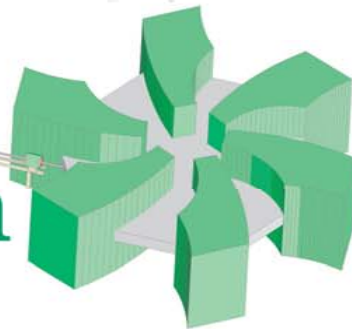


## Grand Raiden

## WS Beam Line



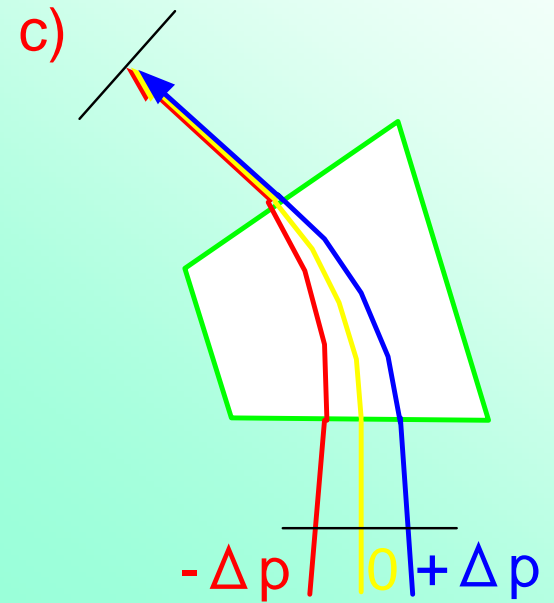
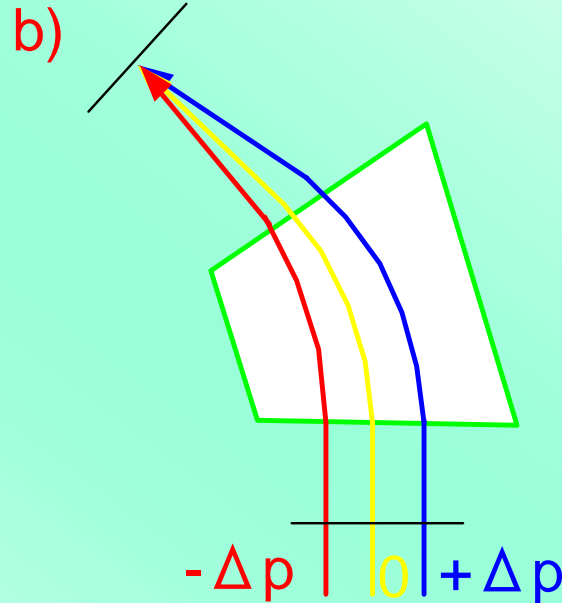
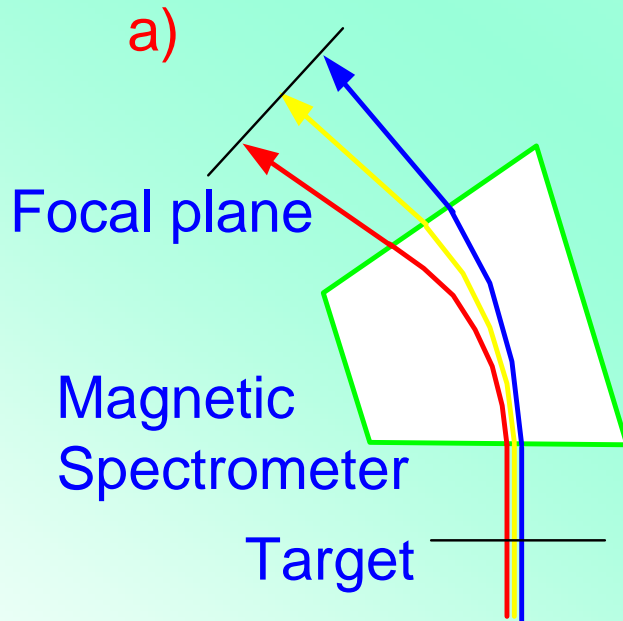
## Ring Cyclotron



# Matching Techniques

Y. Fujita et al., N.I.M. B 126 (1997) 274.

H. Fujita et al., N.I.M. A 484 (2002) 17.



*Achromatic beam transportation*

$\Delta E \sim 200$  keV  
for 140MeV/u<sup>3</sup>He beam

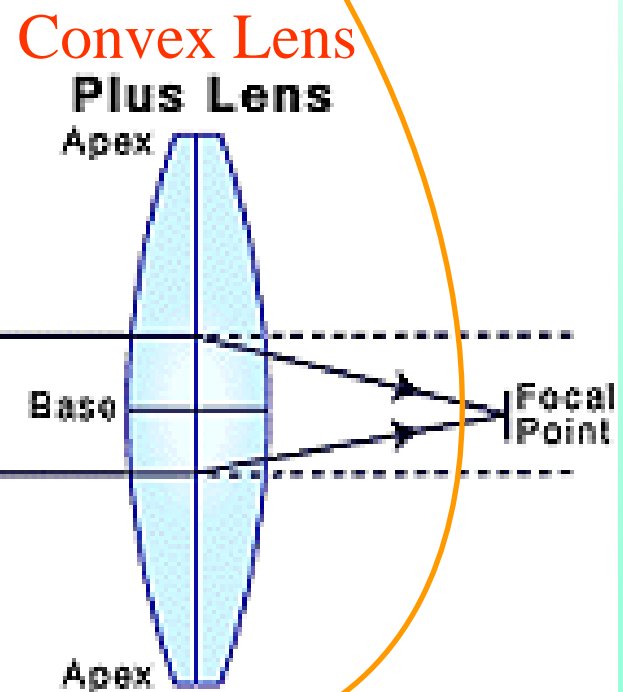
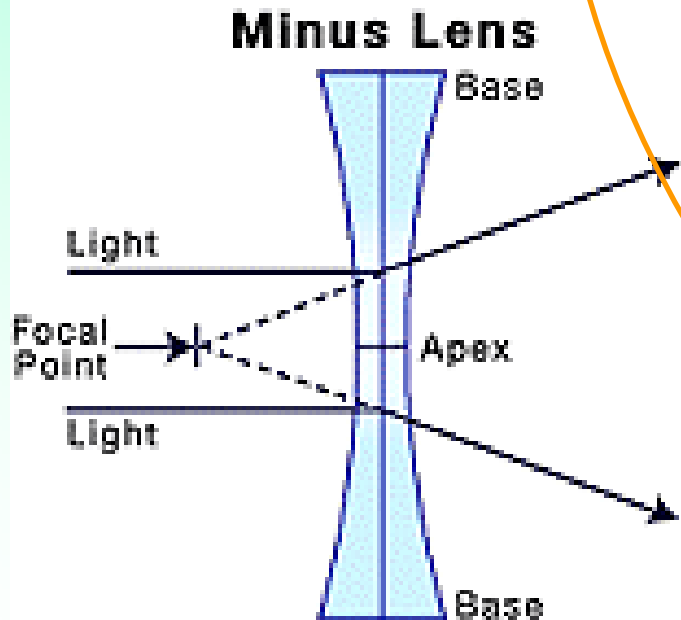
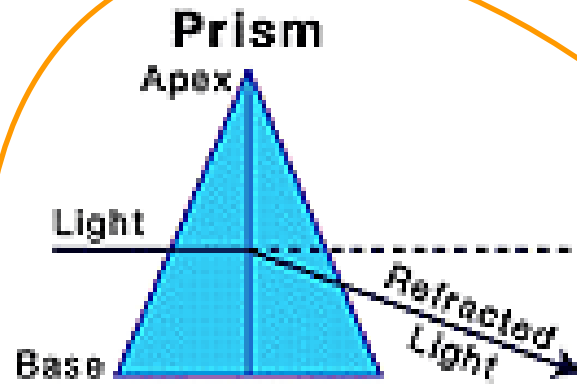
*Lateral dispersion matching*

$\Delta E \sim 35$  keV  
Horiz. angle resolution  
 $\Delta\theta_{sc} > 15$  mrad

*Angular dispersion matching*

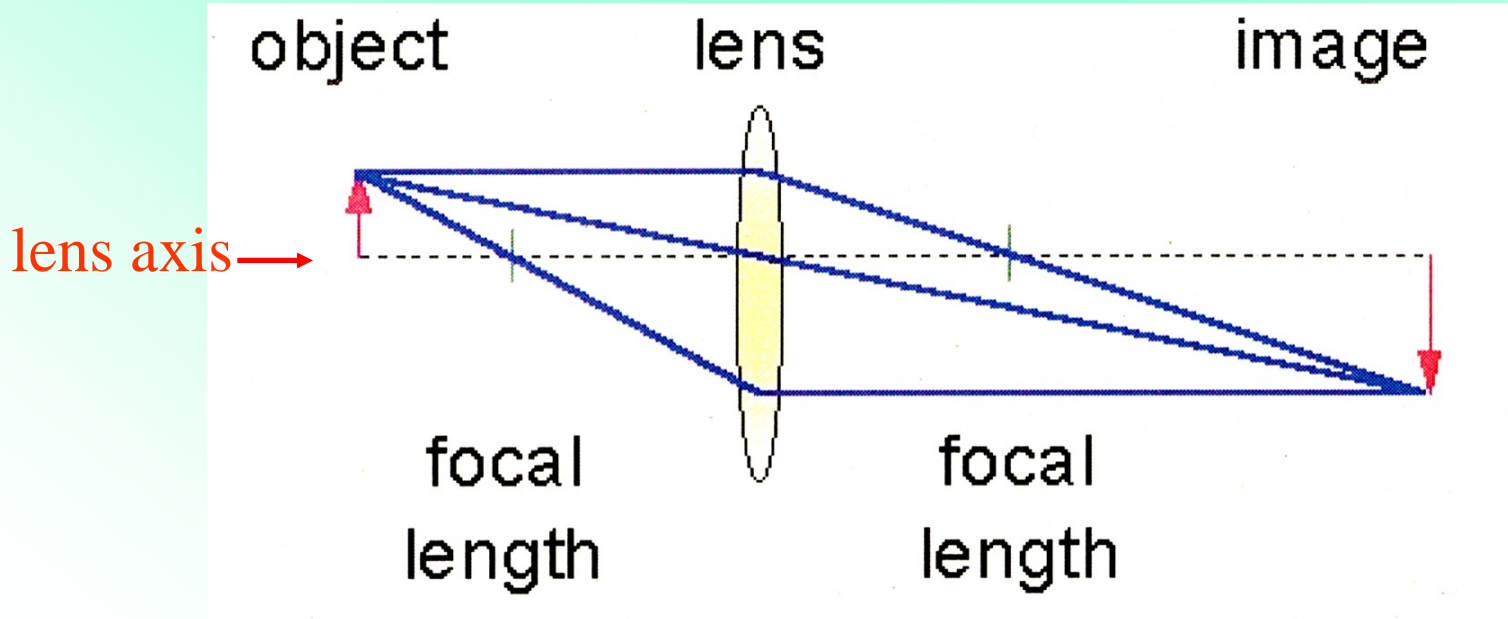
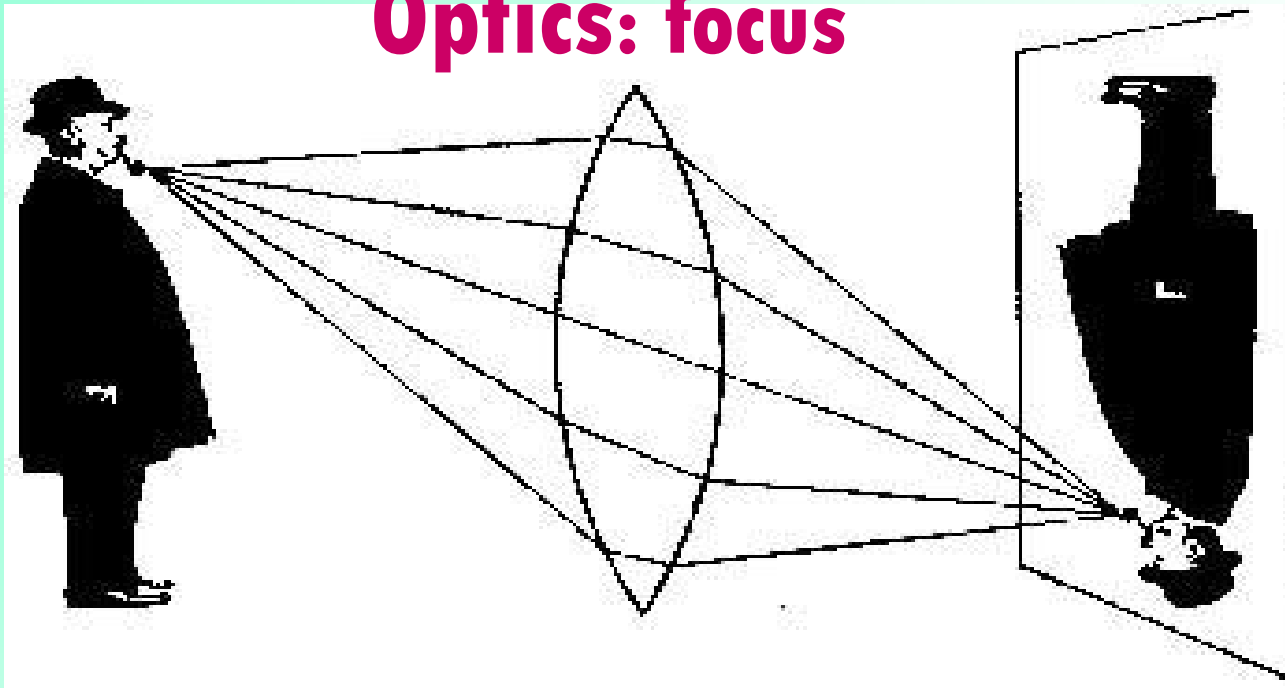
$\Delta\theta_{sc} \sim 5$  mrad

# Magnet = convex Lens + Prism

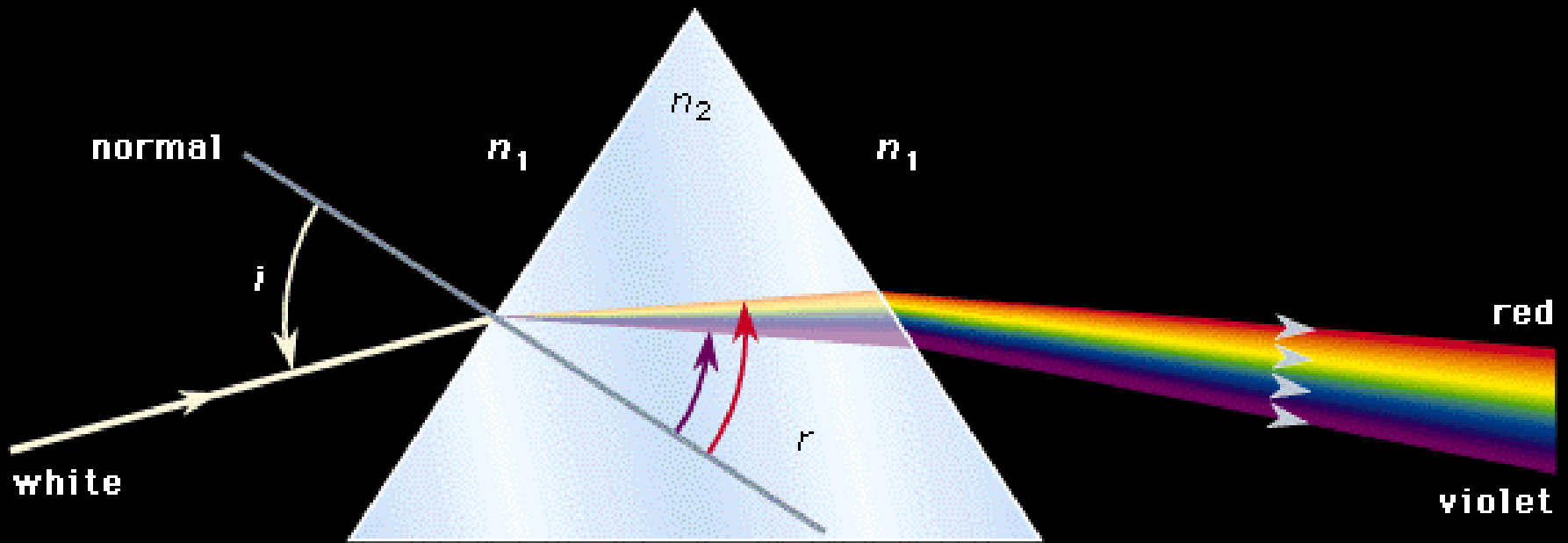




# Optics: focus



# Prism

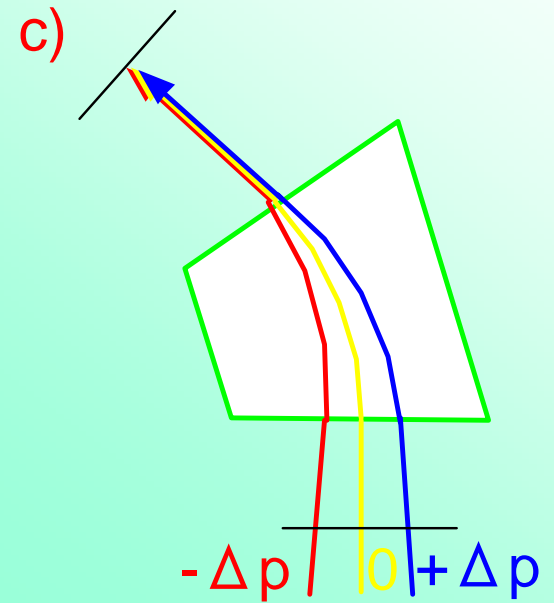
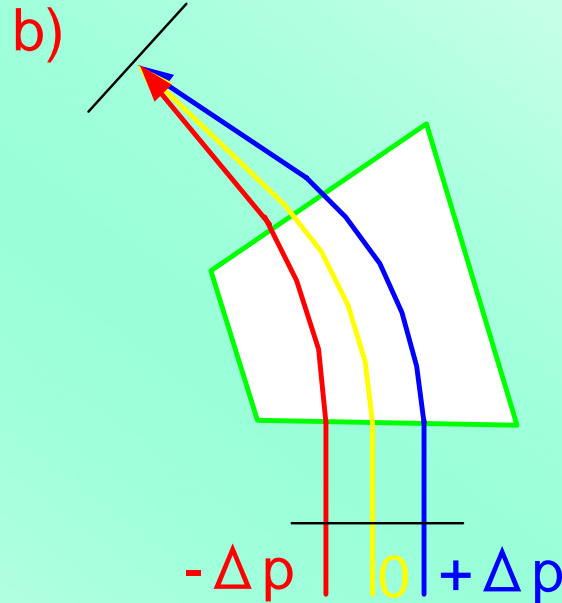
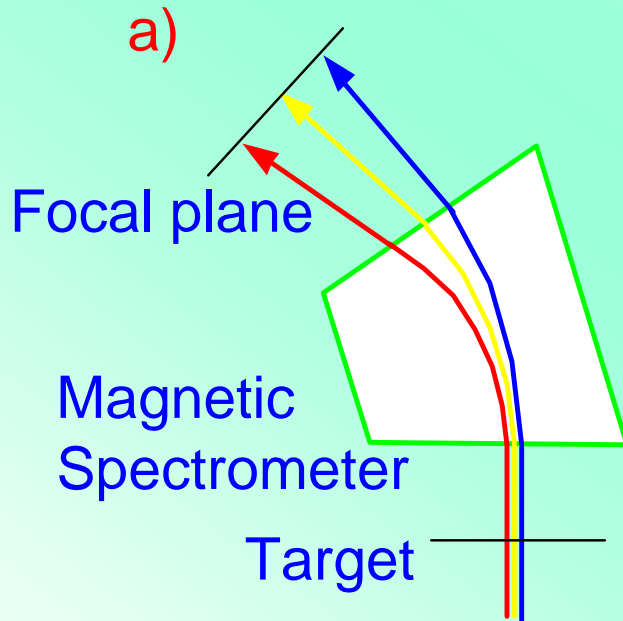


The angles  $i$  and  $r$  that the rays make with the normal are the angles of incidence and refraction. Because  $n_2$  depends upon wavelength, the incident white ray separates into its constituent colours upon refraction, with deviation of the red ray the least and the violet ray the most.

# Matching Techniques

Y. Fujita et al., N.I.M. B 126 (1997) 274.

H. Fujita et al., N.I.M. A 484 (2002) 17.



*Achromatic beam transportation*

$\Delta E \sim 200$  keV  
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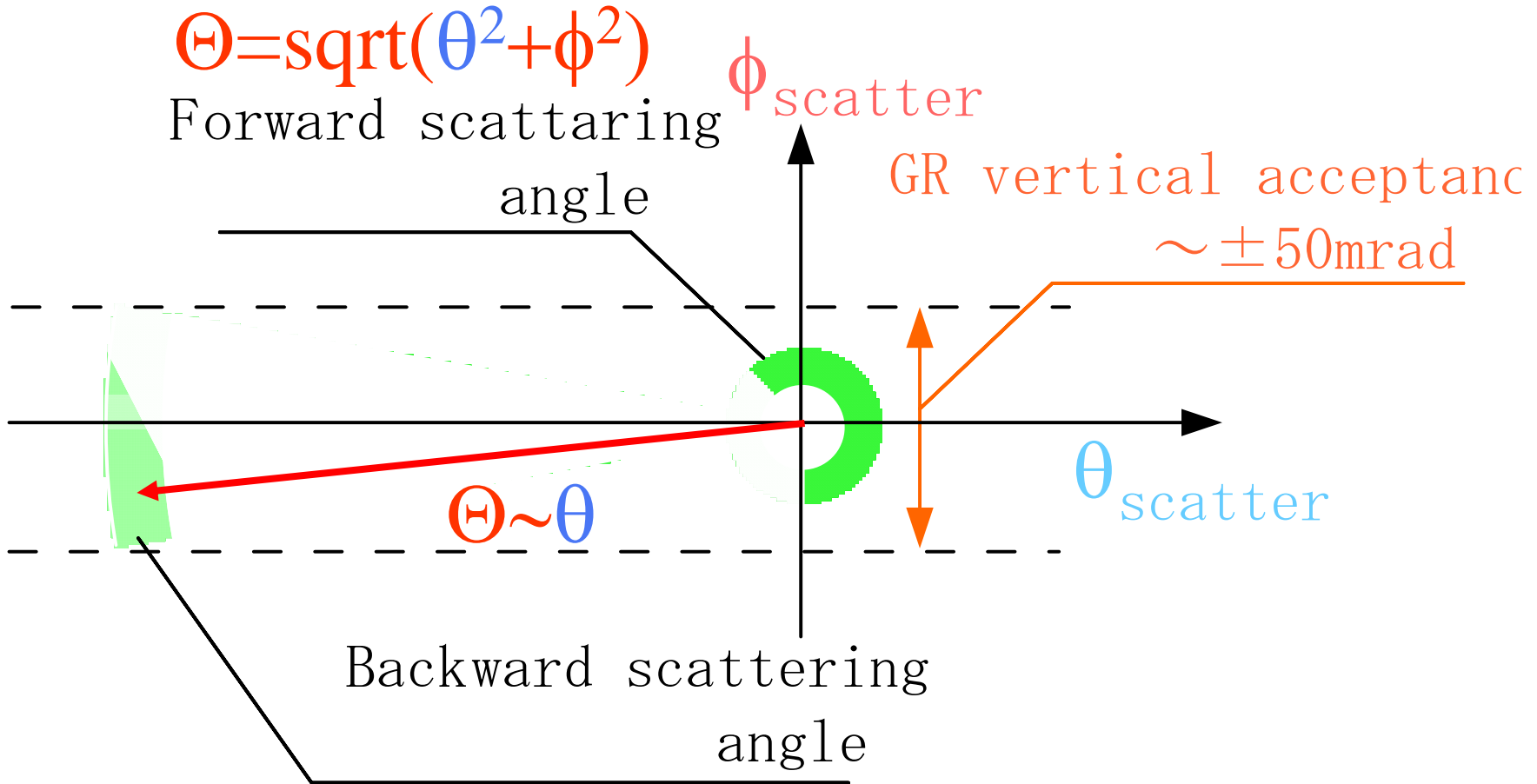
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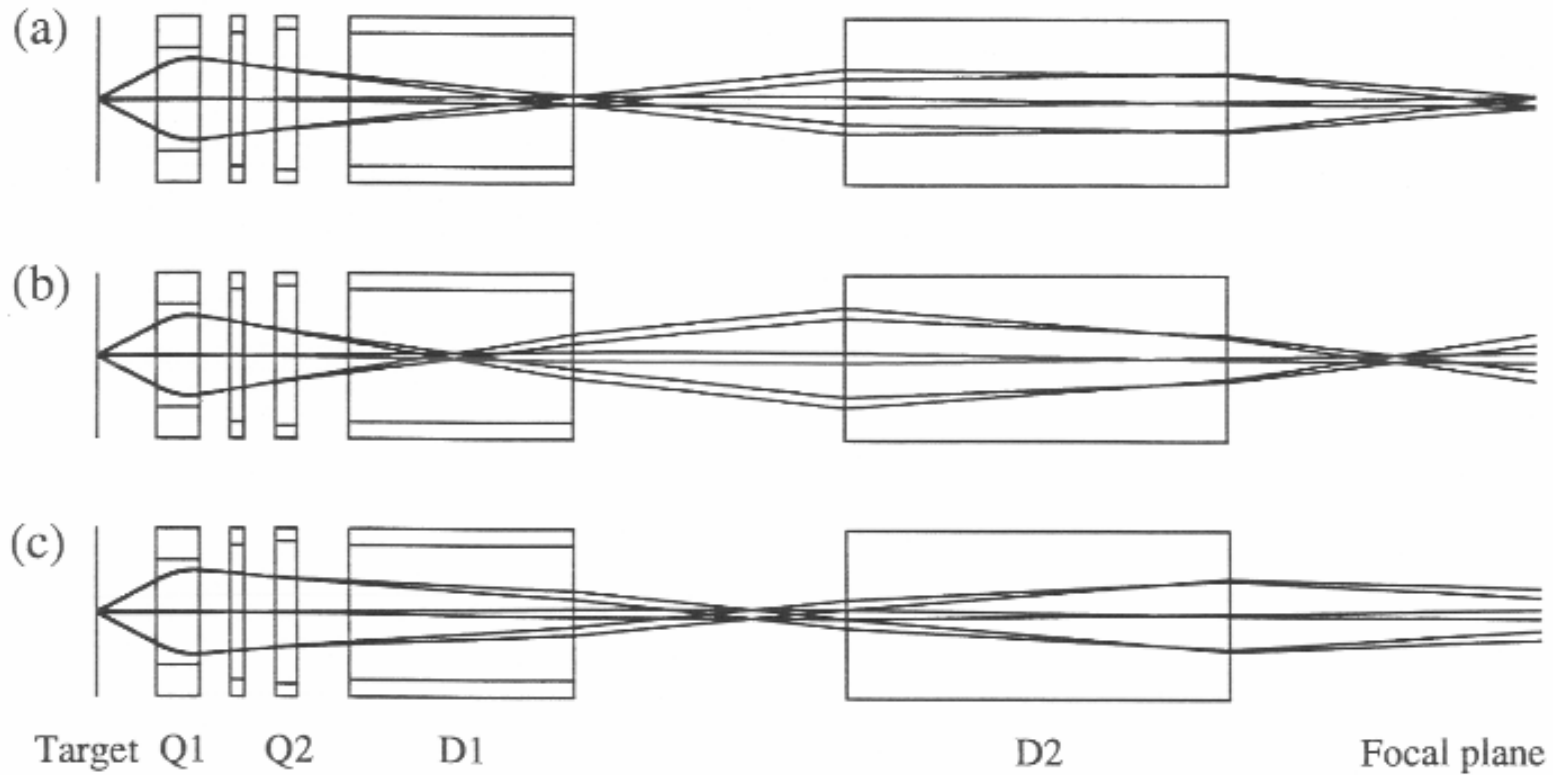
*Angular dispersion matching*

$\Delta\theta_{sc} \sim 5$  mrad

# Importance of Vertical Scattering Angle at 0°



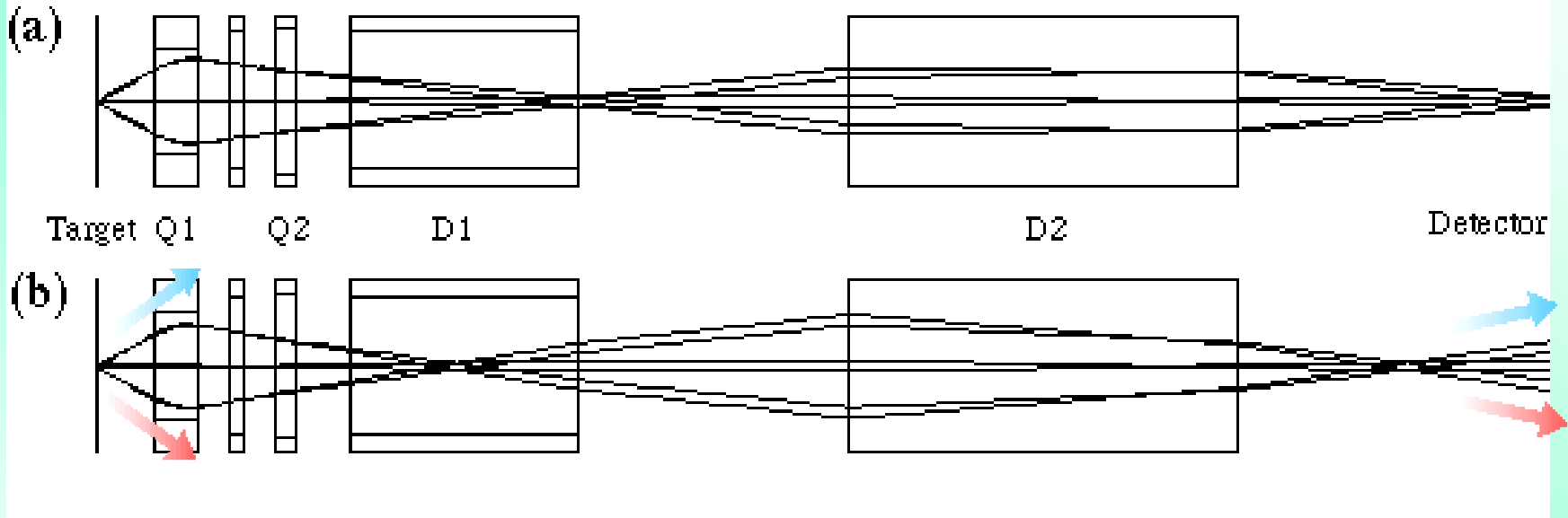
# Off-focus Mode in Vertical Direction



# Over-focus Mode of Grand Raiden

H.Fujita et al., Nucl. Instr. Meth. A 469 (2001) 55.

## Vertical orbits of scattered particles in Grand Raiden



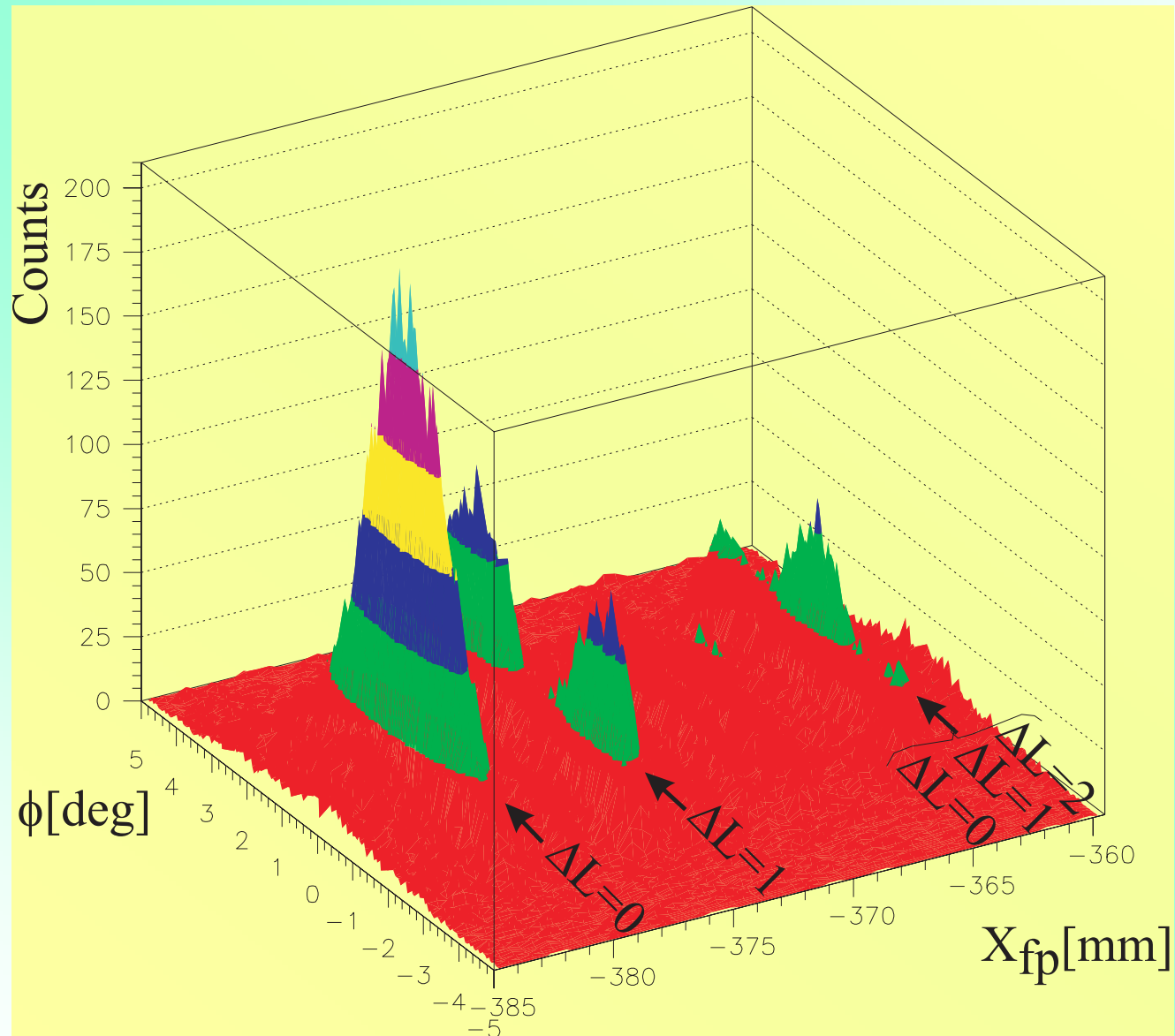
(a) ... Normal vertical point-to-point mode

(b) ... "Over-focus mode" for precise vertical scattering angle measurement

\*Vertical scattering angle is measured from vertical position at the focal plane  $y_{fp}$  (not from  $\phi_{fp}$ )

# Identification of GT transitions

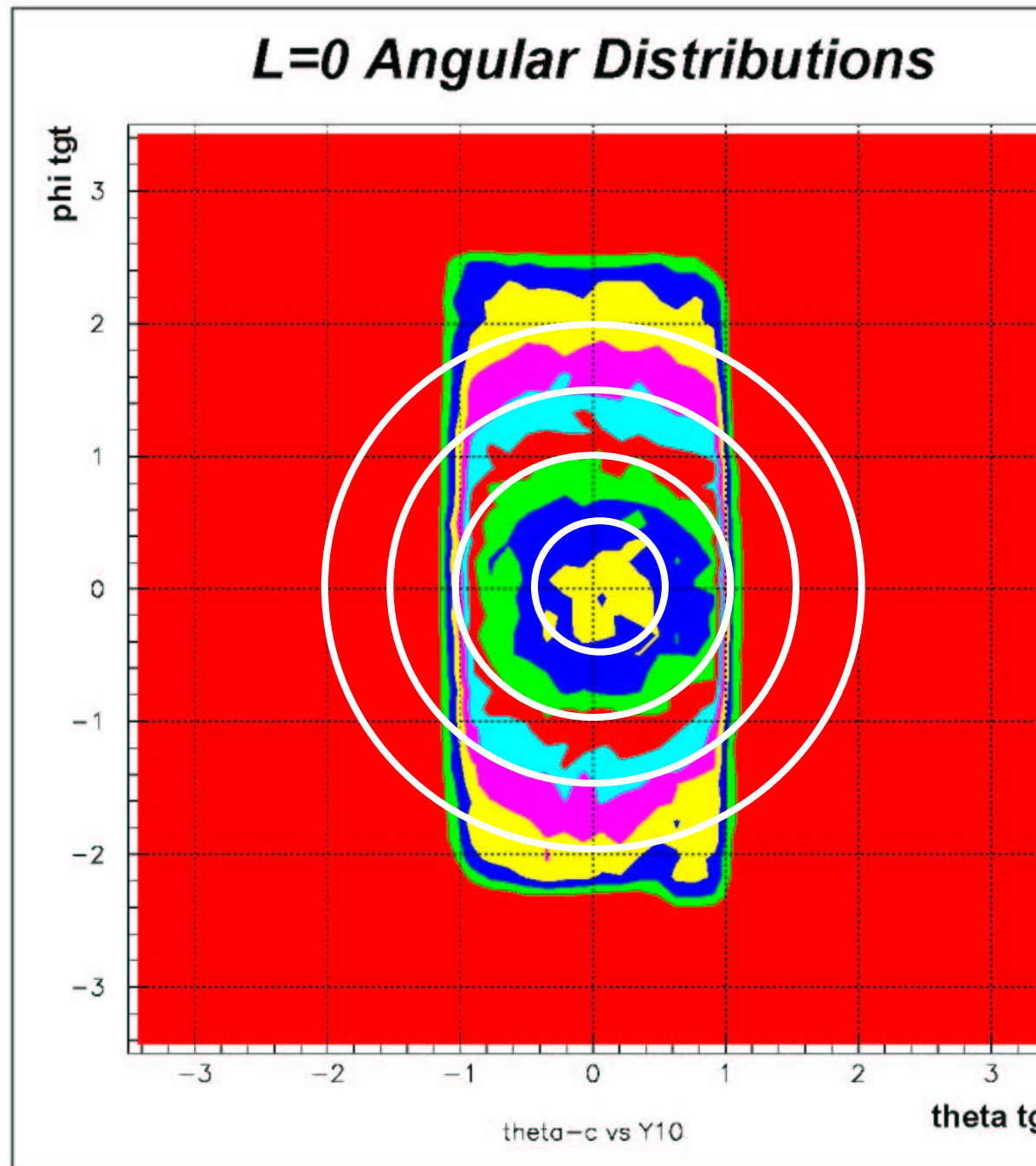
-Angular distributions for different  $\Delta L$ -



# Contour Map within the Acceptance

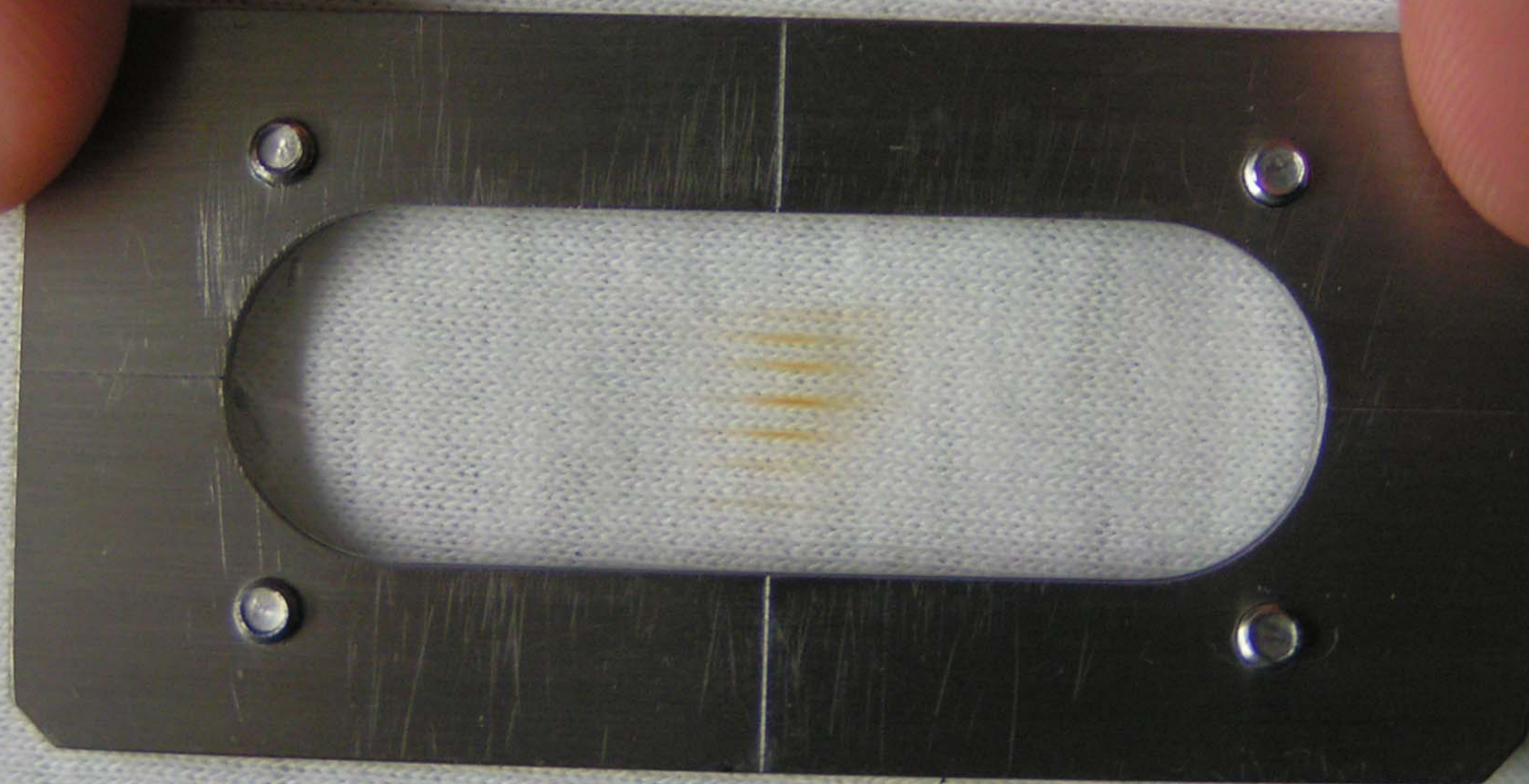
Concentric L=0 angular  
distribution around 0°

$$\Theta = \sqrt{\theta^2 + \phi^2}$$

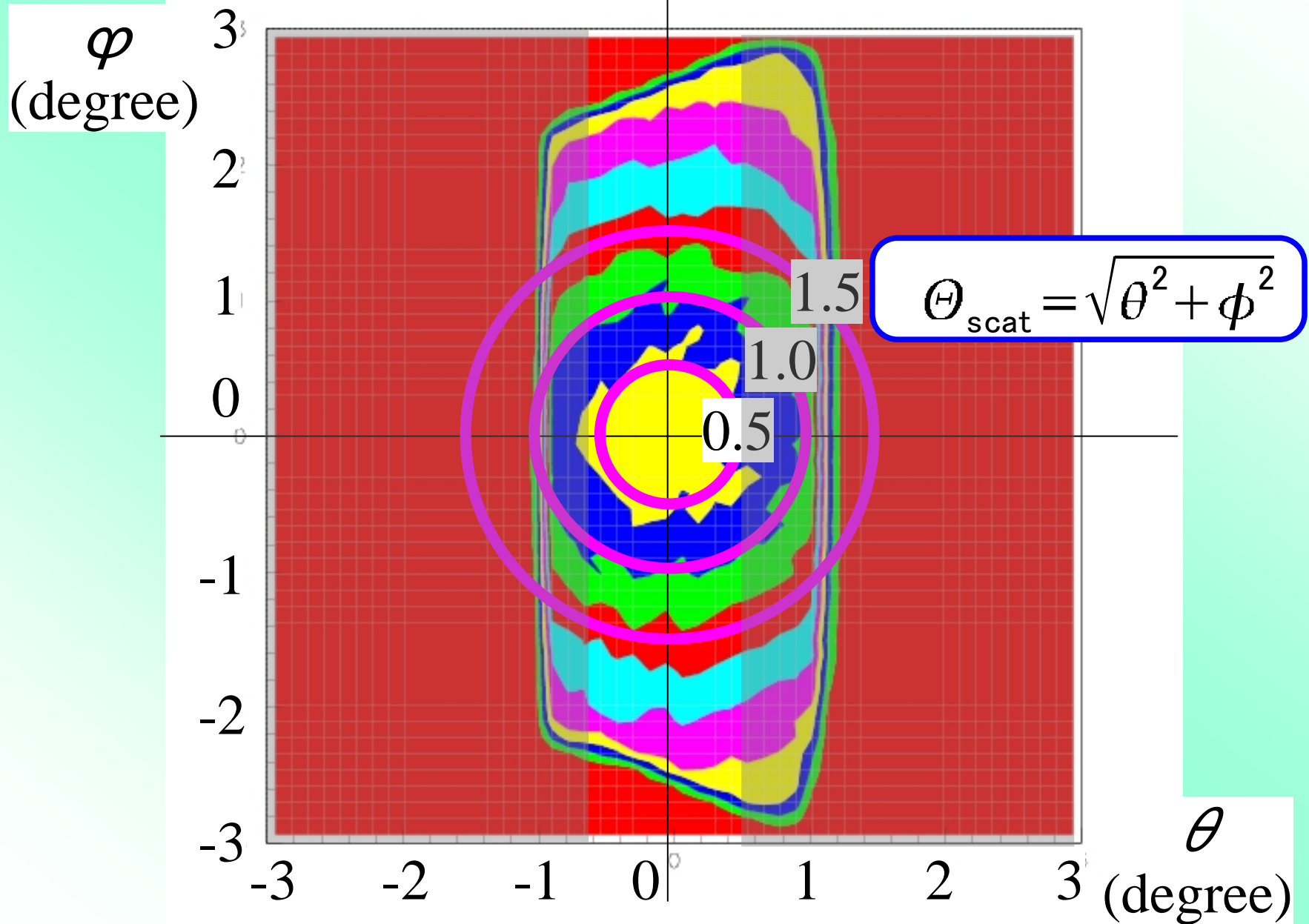




# Beam spot size under Dispersion Matching



# Angular distribution



# Dispersion Matching is possible ...

**\*\*Dispersion matching is the idea of 1<sup>st</sup> order\*\***

- \* Only when the beam emittance is “moderate”
  - multi-component beam is not allowed
  - multi-turn beam is not allowed
- \* Only when the beam energy spread is “moderate”
  - energy reduction factor  $\sim 5$
  - distortion of angular distribution in relation to the acceptance of the Spectrometer

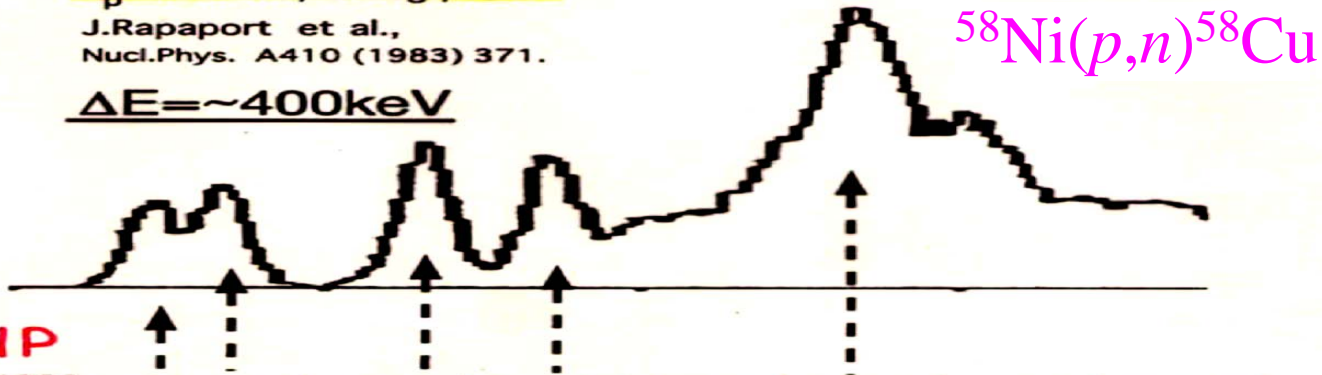


**Beam Quality of the Injector is Crucial !**  
**(RING is a “Booster”)**

**Evolution of Resolution  
in Charge-Exchange Reactions  
at Intermediate Energies**

IUCF

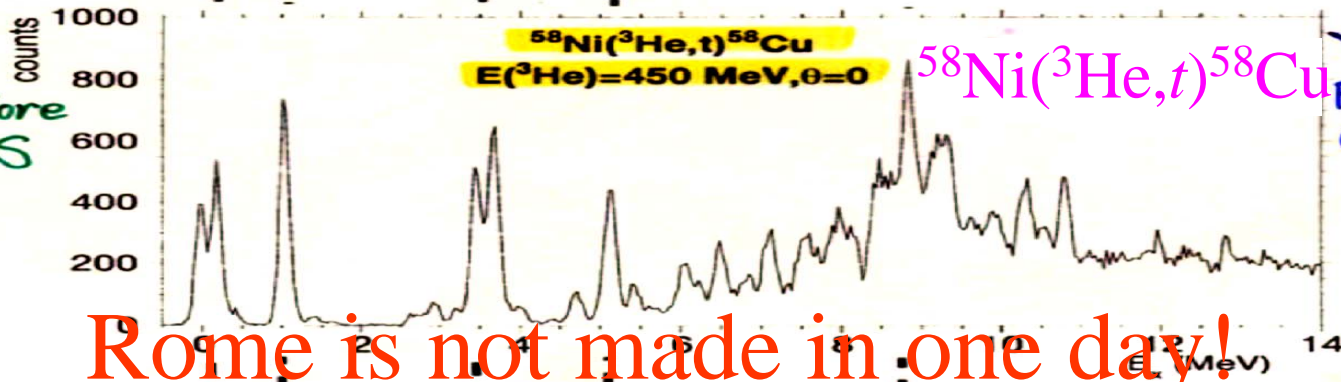
$^{58}\text{Ni}(p,n)$   
 $E_p = 160\text{MeV}$ , 0-deg., IUCF  
 J.Rapaport et al.,  
 Nucl.Phys. A410 (1983) 371.  
 $\Delta E = \sim 400\text{keV}$



$^{58}\text{Ni}(p,n)^{58}\text{Cu}$

RCNP

before  
WS



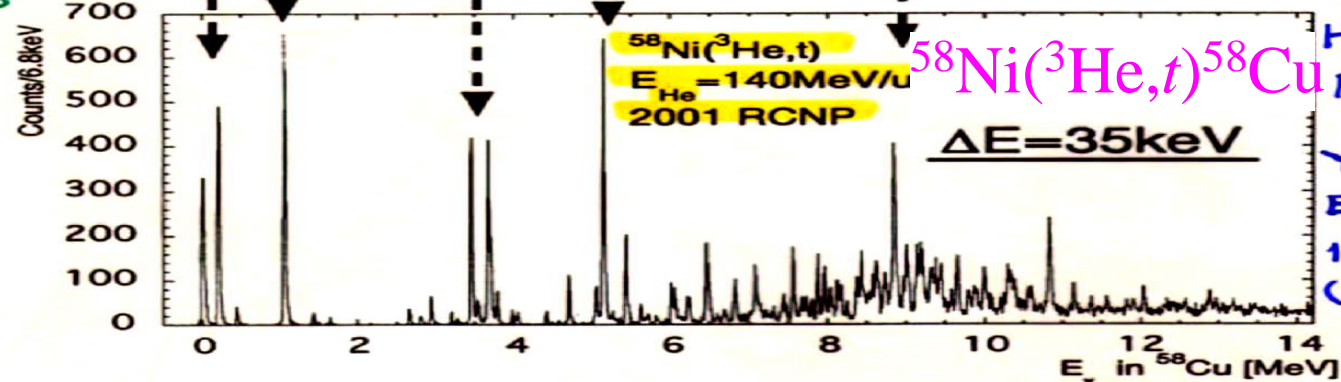
$^{58}\text{Ni}(^3\text{He},t)^{58}\text{Cu}$   
 $E(^3\text{He}) = 450\text{ MeV}, \theta = 0$

$^{58}\text{Ni}(^3\text{He},t)^{58}\text{Cu}$

Y.Fujita et al.  
 Phys. Lett. B365  
 (1996) 29

Rome is not made in one day!

WS



$^{58}\text{Ni}(^3\text{He},t)$   
 $E_{\text{He}} = 140\text{MeV/u}$   
 2001 RCNP

$^{58}\text{Ni}(^3\text{He},t)^{58}\text{Cu}$

$\Delta E = 35\text{keV}$

H.Fujita et al.  
 PhD thesis

Y.Fujita et al.  
 Euro. Phys. J. A  
 13 (2002) 411  
 ( $E_x \leq 8\text{ MeV}$ )

# RIKEN vs. RCNP

## Facility

RI beam facility

Various short-lived nuclei  
cocktail beam

Dirty beam (high intensity!)  
large emittance  
large energy spread

Stable beam facility

-smaller chance-  
single beam

High quality beam (lower intensity)  
small emittance  
small energy spread

## Experiment

Inverse kinematics

Invariant-mass Spectroscopy

Partial decay measurements

$\gamma$ : Doppler shift

particle decay

Extension in  $T_z$  axis

Normal kinematics

Singles measurement

Total decay width + partial

no effect from Doppler shift

Extension to higher T (higher Ex)

\*\*\*Isospin Symmetry

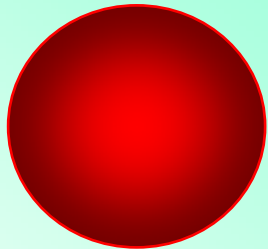
# Nucleon & Coin



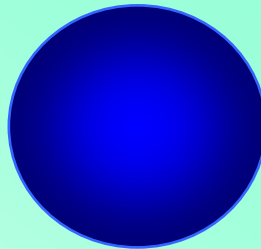
back

front

= Coin



proton



neutron

= Nucleon

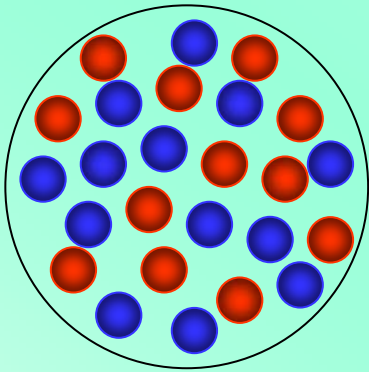
similar mass  
nearly the same interaction

$T_z = -1/2$

$T_z = 1/2$

isospin  $T = 1/2$

# Isospin of a Nucleus



$A$   
 $N$   $Z$

$$T_z = (1/2)N + (-1/2)Z$$

\*z-component: conserved

The size of a vector should be larger than its z-component!

$$T = \text{or } > |T_z|$$

*ex.*  $^{26}\text{Mg}$  ( $Z=12$ ,  $N=14$ ) :  $T_z = +1$ ,  $T = 1, 2, \dots$

$^{26}\text{Al}$  ( $Z=13$ ,  $N=13$ ) :  $T_z = 0$ ,  $T = 0, 1, 2, \dots$

$^{27}\text{Si}$  ( $Z=14$ ,  $N=12$ ) :  $T_z = -1$ ,  $T = 1, 2, \dots$

Isospin Analogous Structure is expected over same mass  $A$  nuclei (isobars)!



# Transitions in real & isospin space (T=1)

Symmetry Transitions from T=1 Nuclei

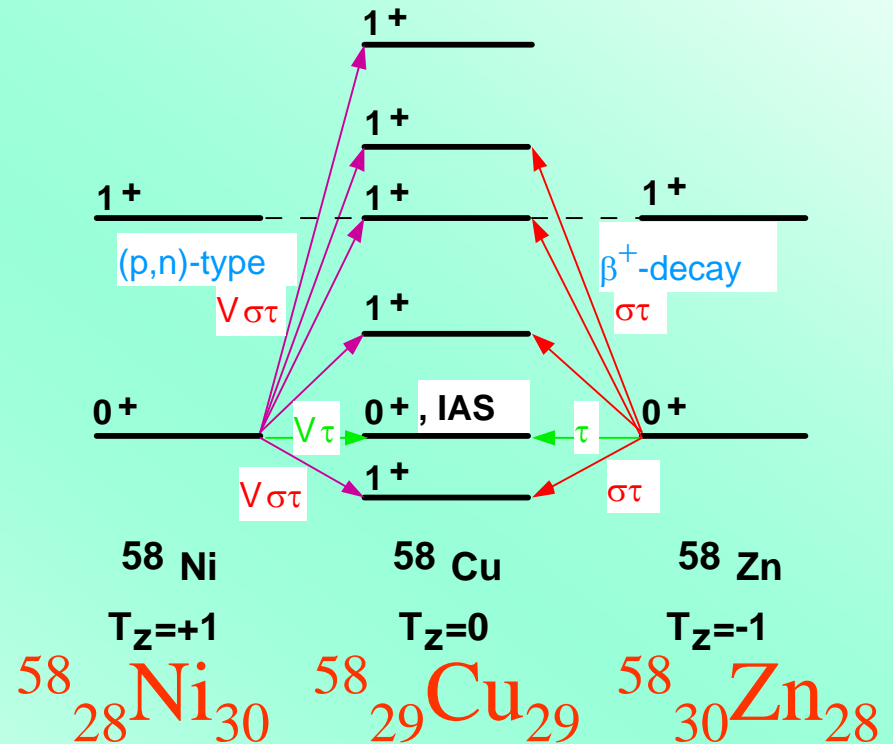
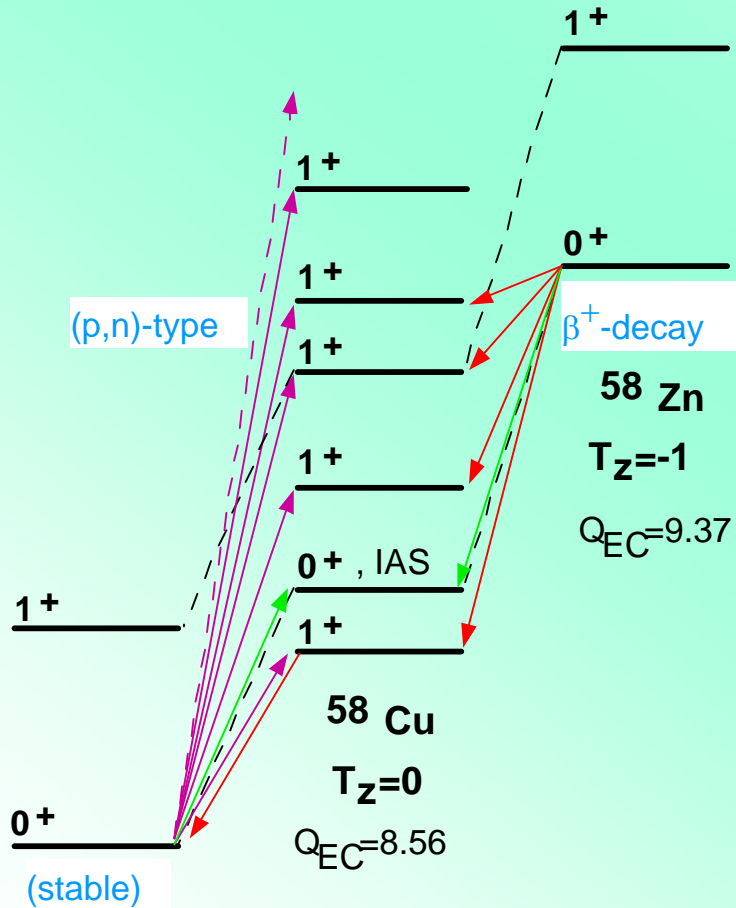
$T_z=+1 \rightarrow T_z=0 \leftarrow T_z=-1$

(in real energy space)

Symmetry Transitions from T=1 Nuclei

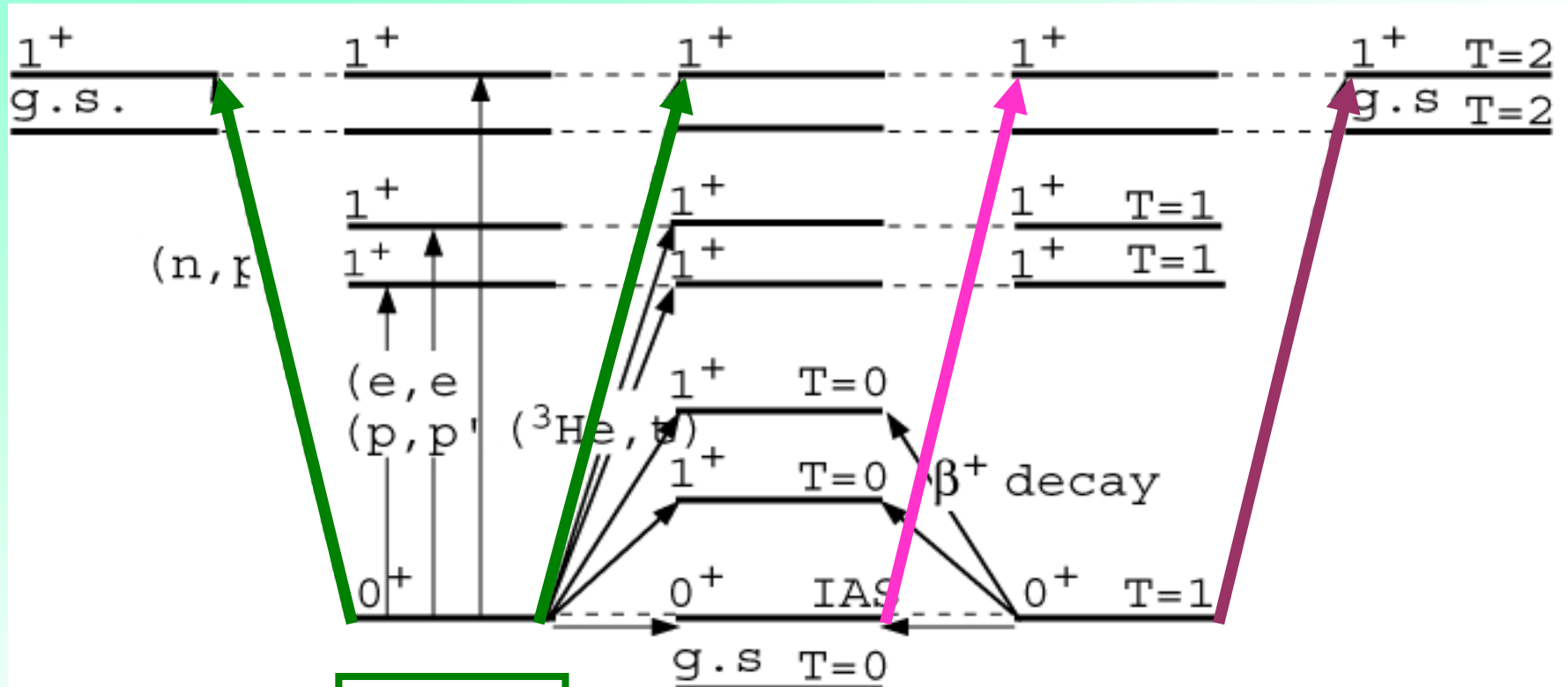
$T_z=+1 \rightarrow T_z=0 \leftarrow T_z=-1$

(in isospin symmetry space\*)



\*after the correction of Coulomb displacement energy

# T=1 and T=2 Symmetry



$^{26}\text{Na}$

$^{50}\text{V}$

$^{58}\text{Co}$

$T_z = +2$

$^{26}\text{Mg}$

$^{50}\text{Cr}$

$^{58}\text{Ni}$

$T_z = +1$

stable

$^{26}\text{Al}$

$^{50}\text{Mn}$

$^{58}\text{Cu}$

$T_z = 0$

$^{26}\text{Si}$

$^{50}\text{Fe}$

$^{58}\text{Zn}$

$T_z = -1$

$^{26}\text{P}$

$^{50}\text{Co}$

$^{58}\text{Ga}$

$T_z = -2$

# \*\*Comparison of CE and IE reactions\*\*

T identification  
on the basis of Isospin Symmetry

# B(GT) & B(M1) : Similarity & Difference

GT operator

$$\mathbf{O}_{GT\pm} = \mp \frac{1}{\sqrt{2}} \sum_{j=1}^A (\boldsymbol{\sigma}_j \tau_j^{\pm})$$

GT transition strength

$$B(\text{GT}) = \frac{1}{2J_i+1} \frac{1}{2} \frac{C_{\text{GT}}^2}{2I_f+1} [M_{\text{GT}}(\sigma\tau)]^2 \quad \text{IV Spin}$$

M1 operator

$$\boldsymbol{\mu} = \left\{ \sum_{j=1}^A \begin{matrix} 0.5 & 0.88 \\ (g_l^{\text{IS}} \mathbf{l}_j + g_s^{\text{IS}} \mathbf{s}_j) \end{matrix} - \sum_{j=1}^A \begin{matrix} 0.5 & 4.7 \\ (g_l^{\text{IV}} \mathbf{l}_j + g_s^{\text{IV}} \mathbf{s}_j) \tau_{zj} \end{matrix} \right\} \mu_N$$

M1 transition strength

$$B(\text{M1}) = \frac{1}{2J_i+1} \frac{3}{4\pi} \mu_N^2 \left[ \left( g_l^{\text{IS}} M_{\text{M1}}(l) + g_s^{\text{IS}} \frac{1}{2} M_{\text{M1}}(\sigma) \right) \right. \text{IS} \\ \left. - \frac{C_{\text{M1}}}{\sqrt{2I_f+1}} \left( g_l^{\text{IV}} M_{\text{M1}}(l\tau) + g_s^{\text{IV}} \frac{1}{2} M_{\text{M1}}(\sigma\tau) \right) \right]^2 \text{IV}$$

Meson Exchange

Currents

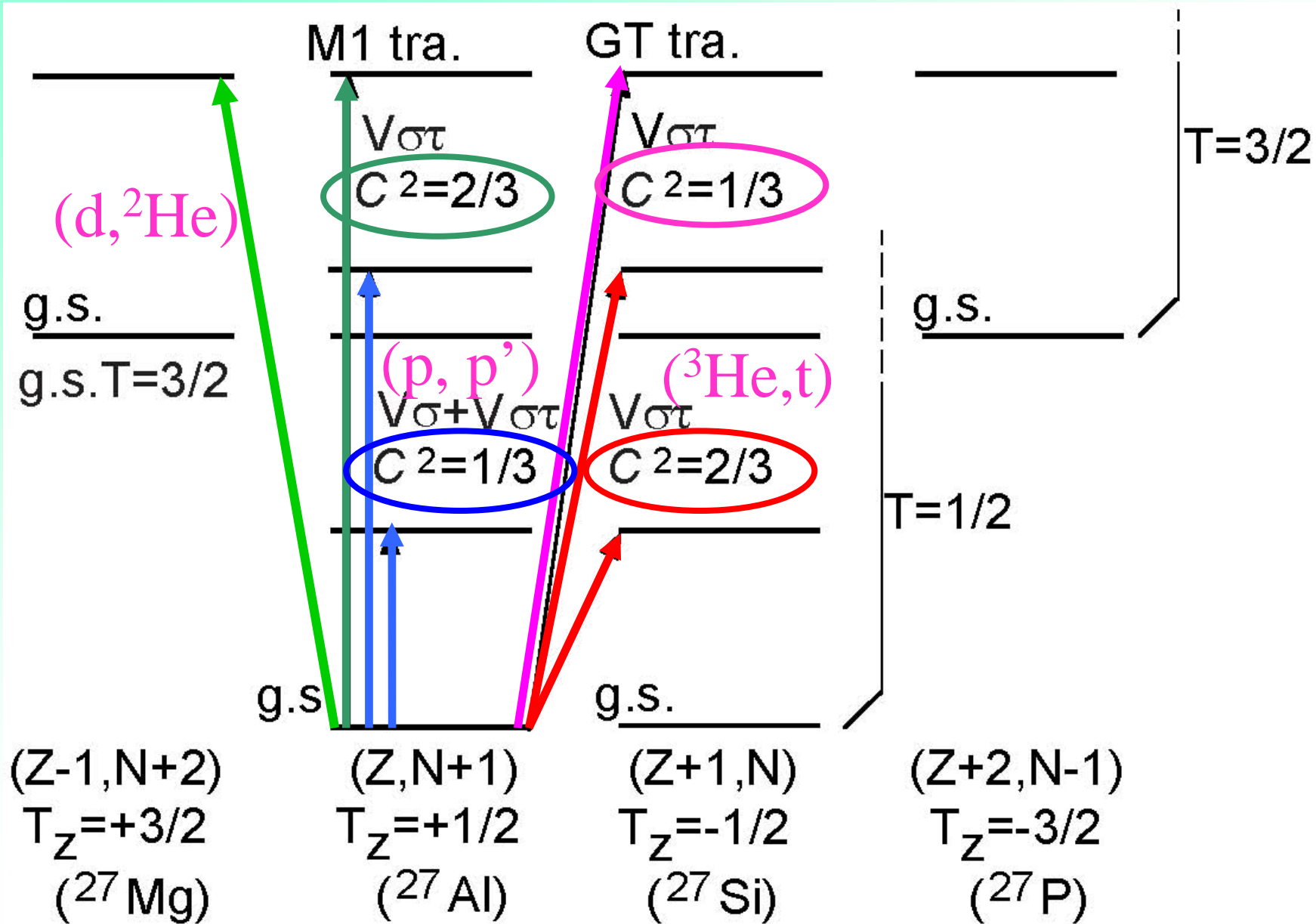
$$[M_{\text{M1}}(\sigma\tau)]^2 = R_{\text{MEC}} [M_{\text{GT}}(\sigma\tau)]^2$$

Orbital

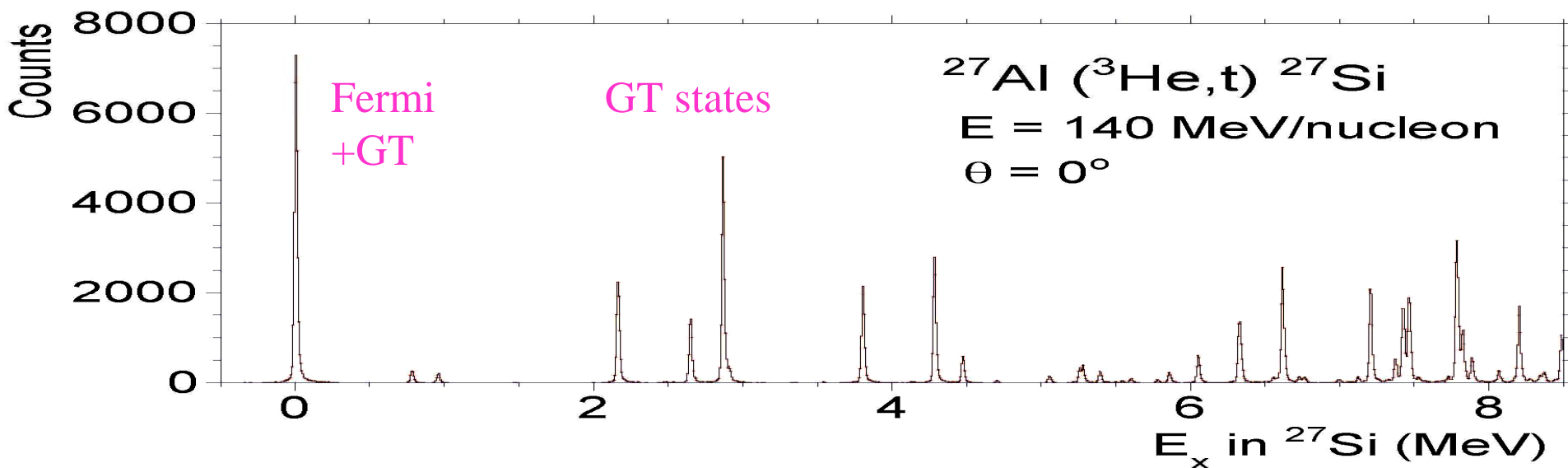
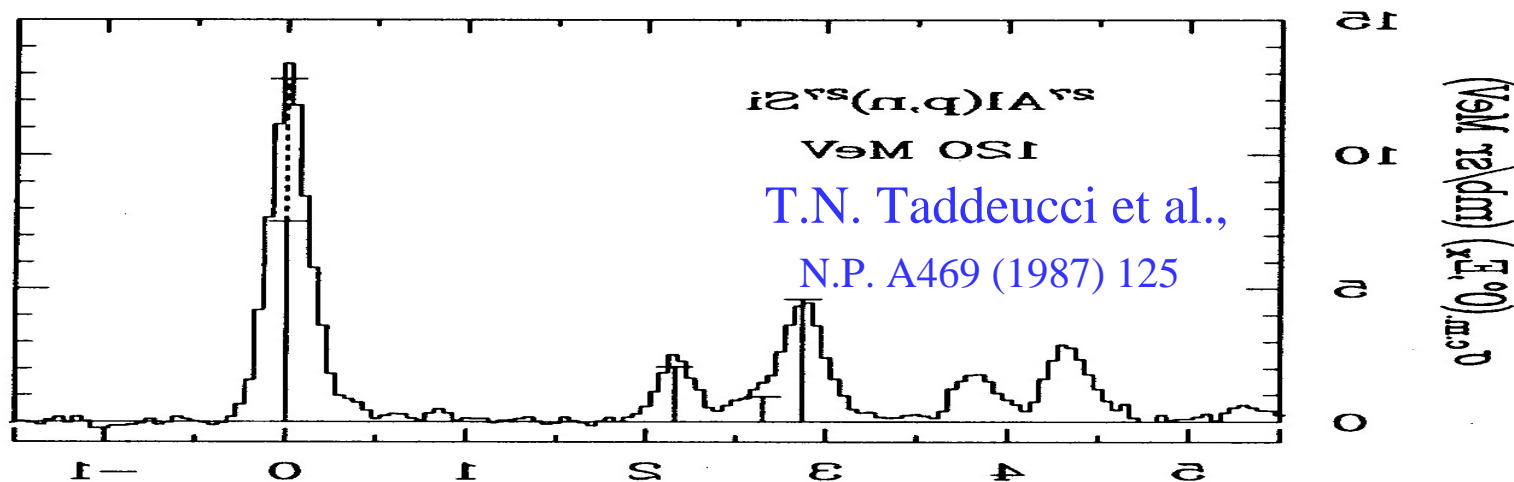
Spin (main term)

$$R_{\text{MEC}} \sim 1.25$$

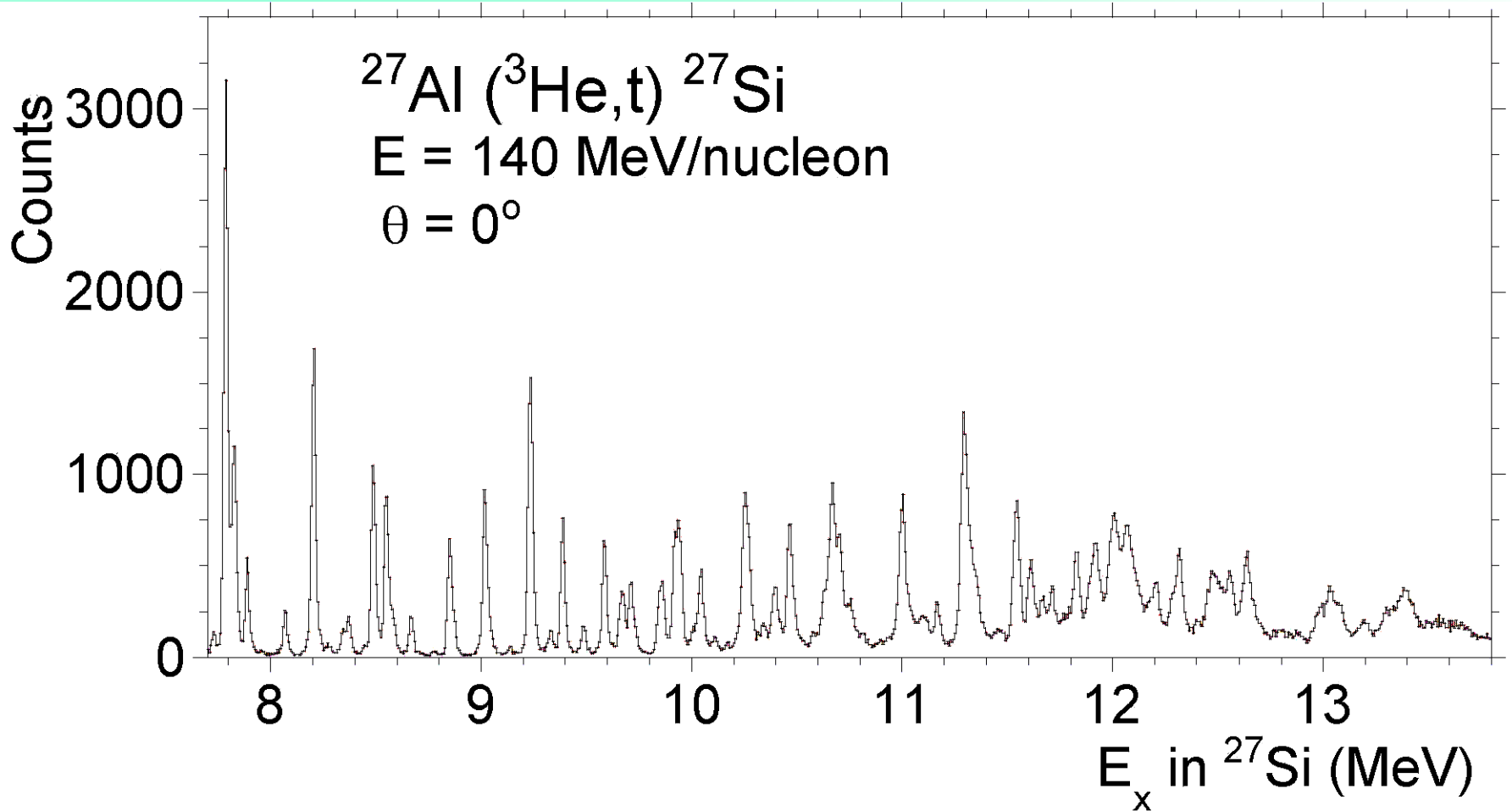
# T=1/2 & 3/2 Symmetry



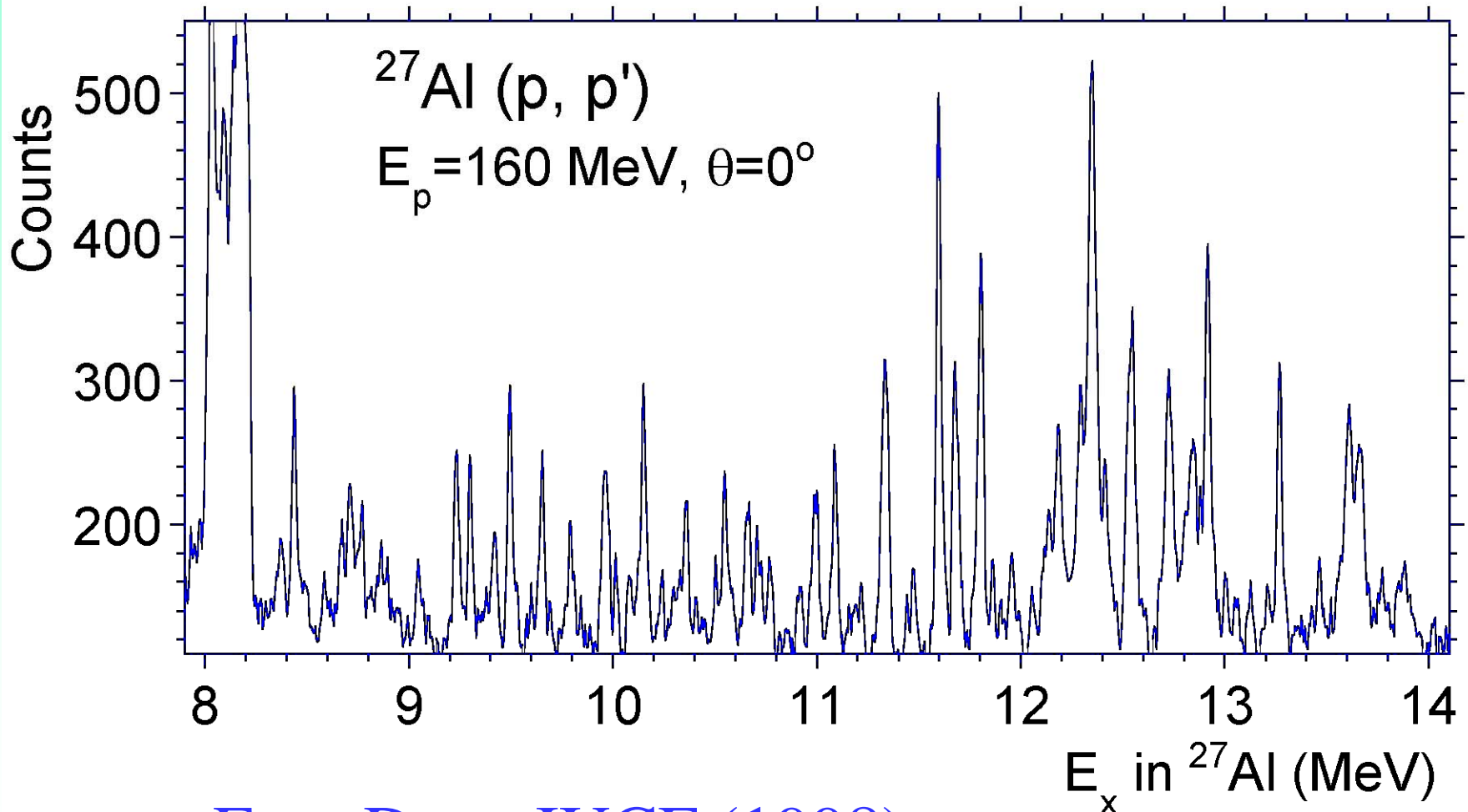
# Comparison: $^{27}\text{Al}(p,n)$ and $^{27}\text{Al}(^3\text{He},t)$



# $^{27}\text{Al}({}^3\text{He},t)$ spectrum ( $E_x > 8$ MeV)



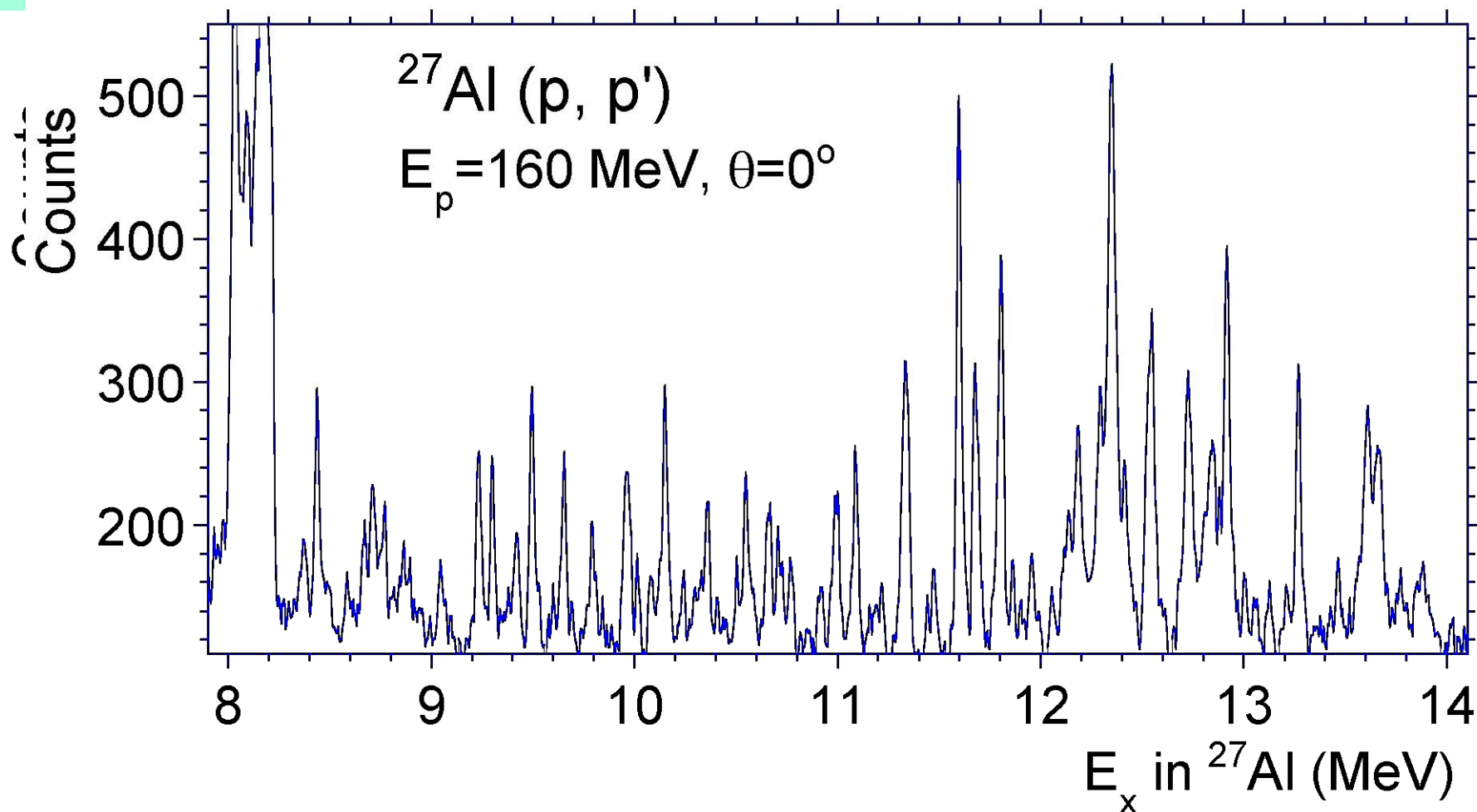
# $^{27}\text{Al}(p, p')$ spectrum ( $E_x > 8 \text{ MeV}$ )



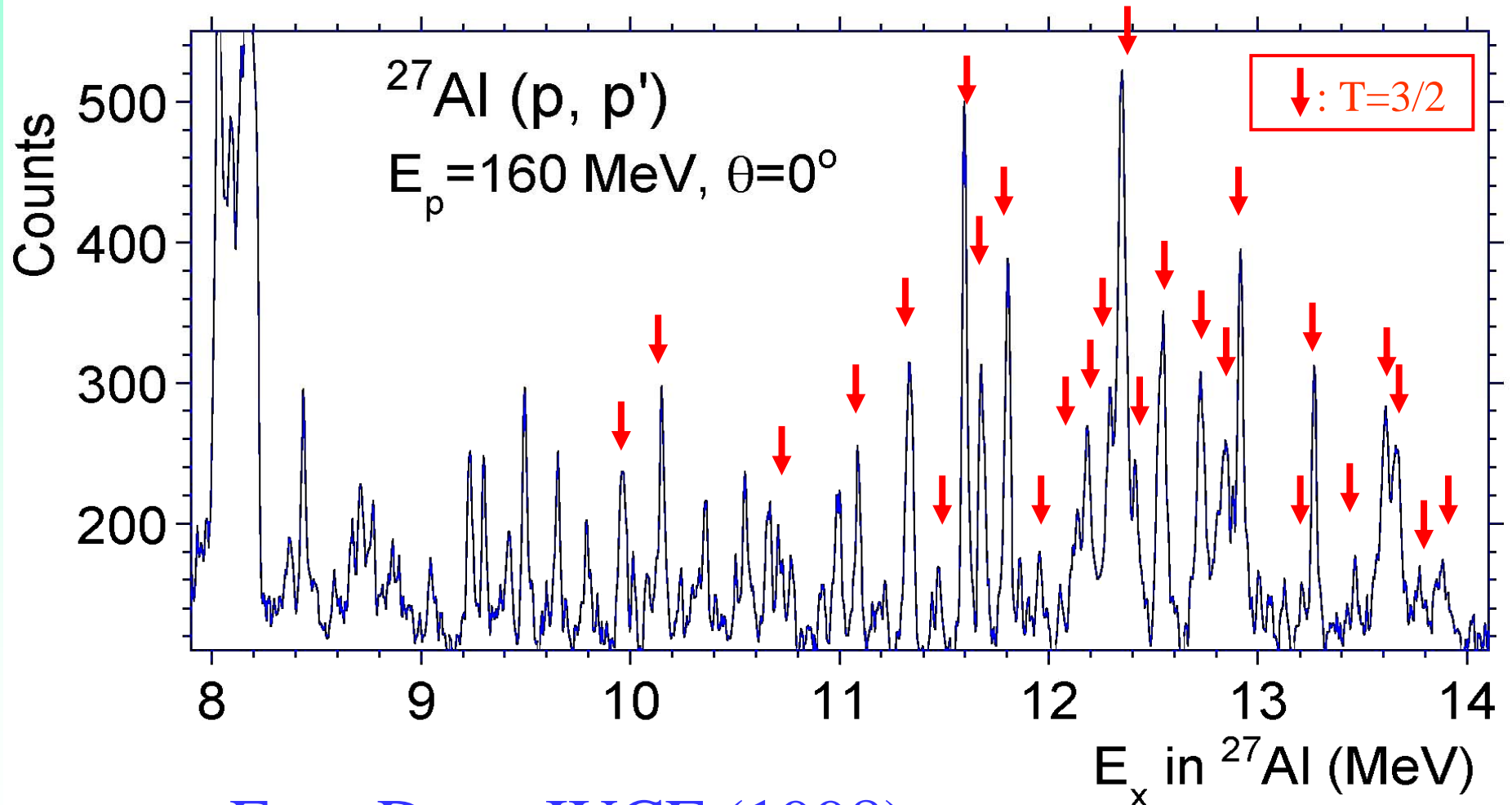
Exp. Data: IUCF (1998)



# Comp.: $^{27}\text{Al}(^3\text{He},t)$ and $^{27}\text{Al}(p,p')$ spectra

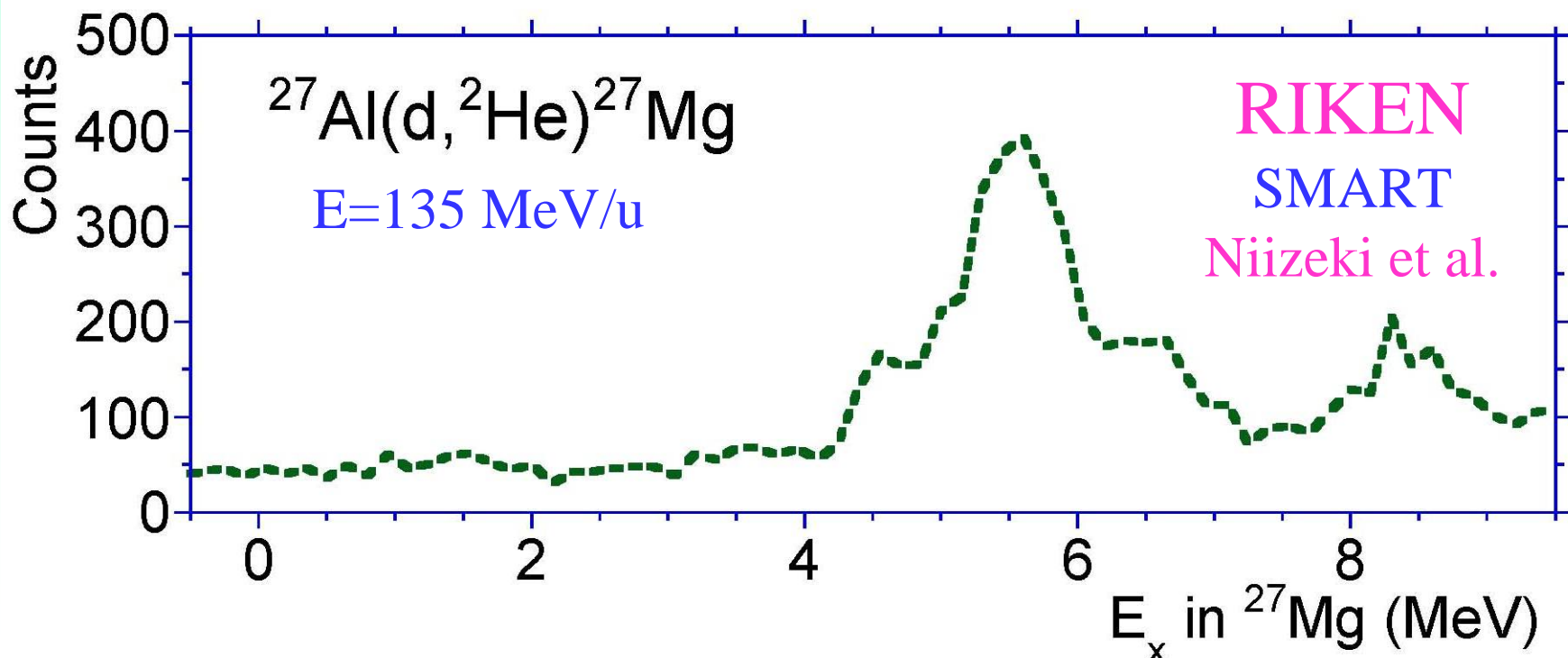
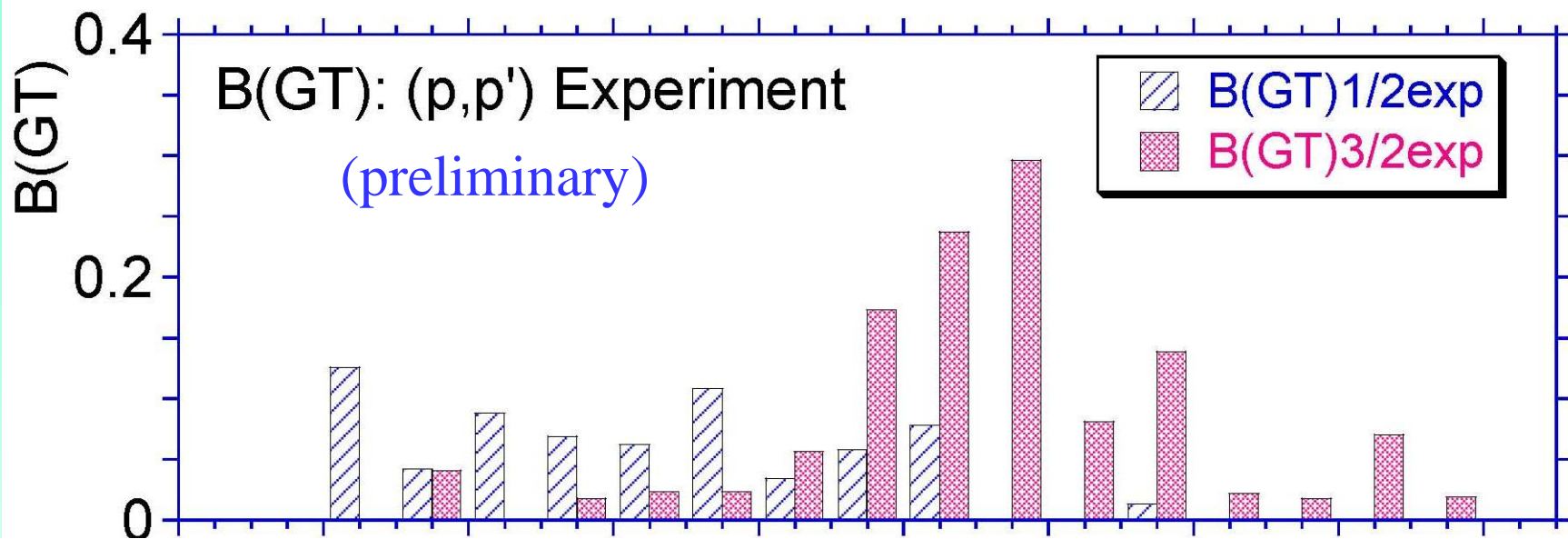


# $^{27}\text{Al}(p, p')$ spectrum ( $E_x > 8 \text{ MeV}$ )



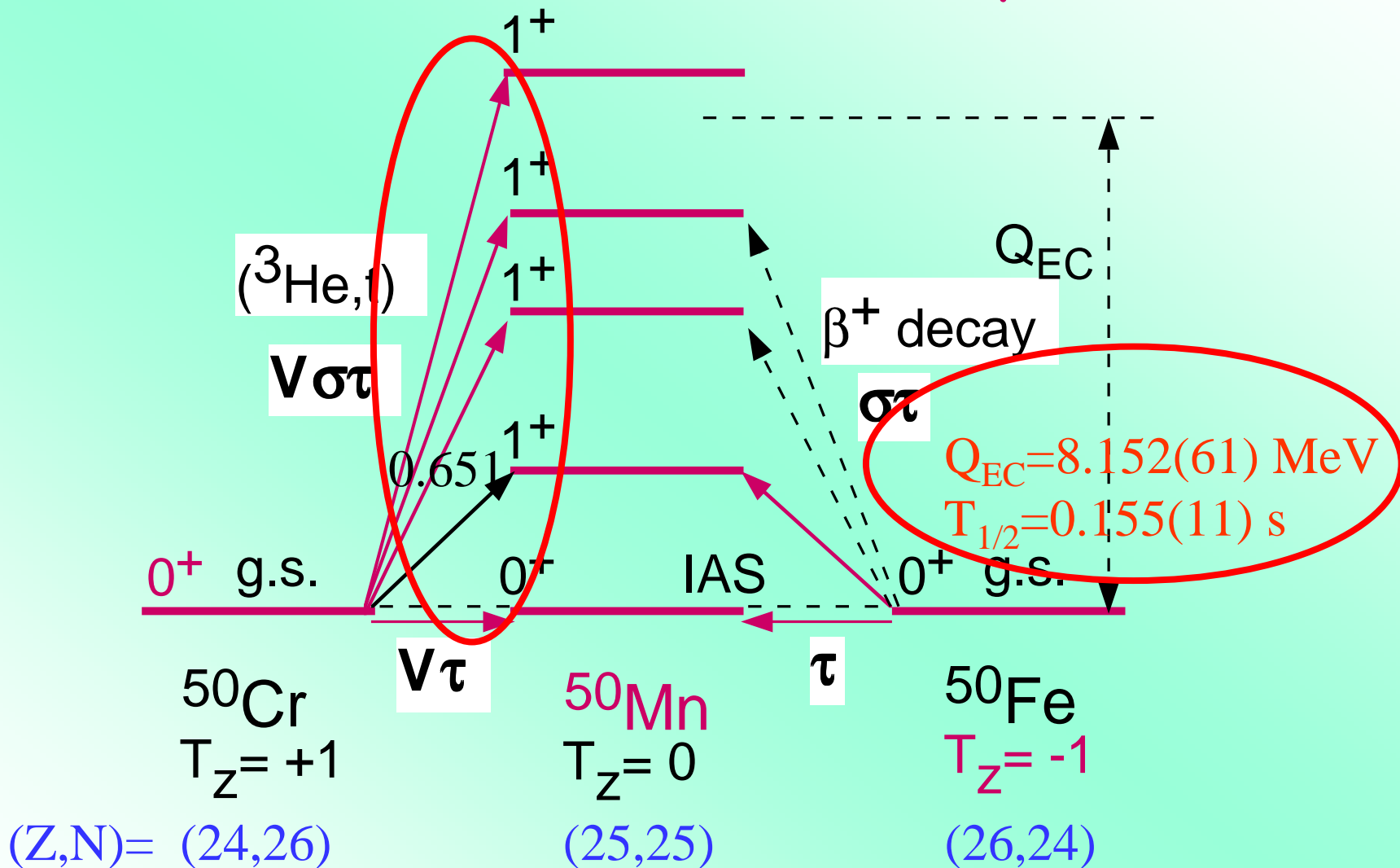
Exp. Data: IUCF (1998)

# T=3/2 strengths & Comp. with (d,<sup>2</sup>He)

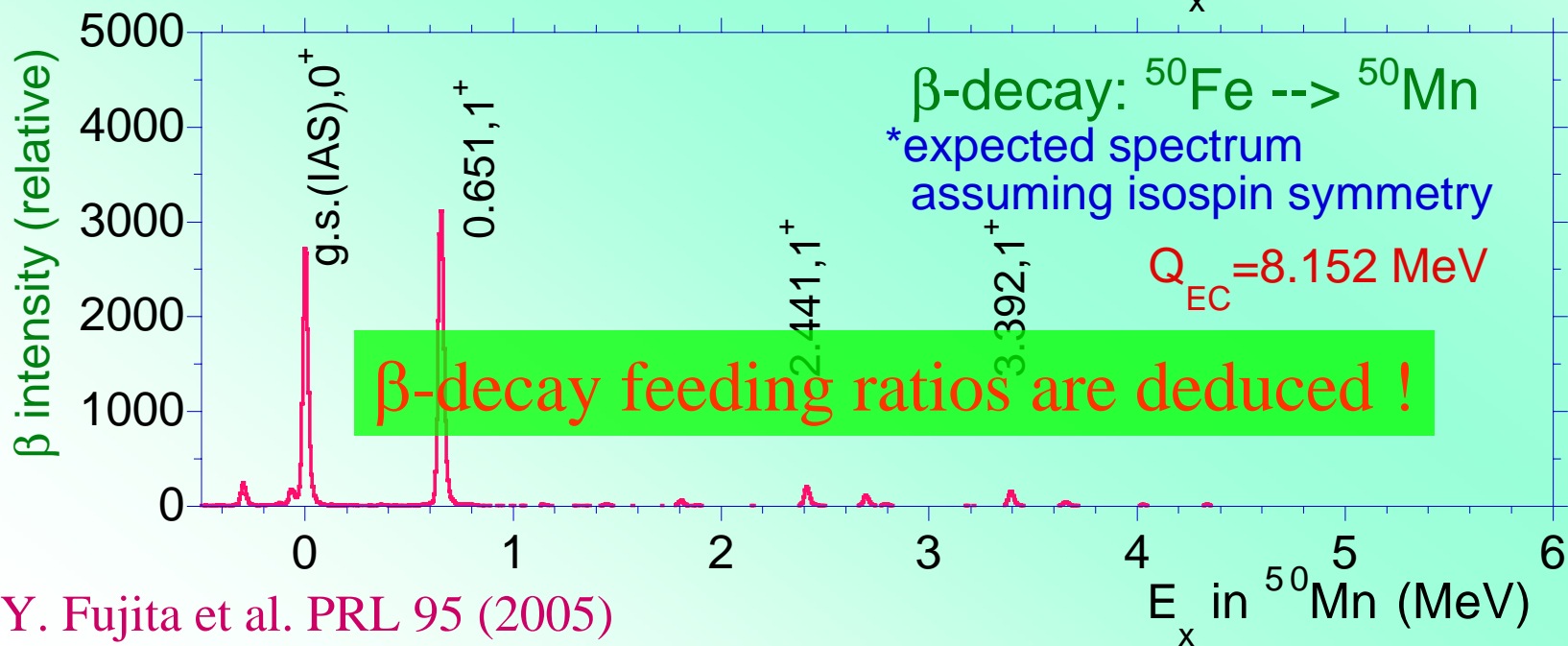
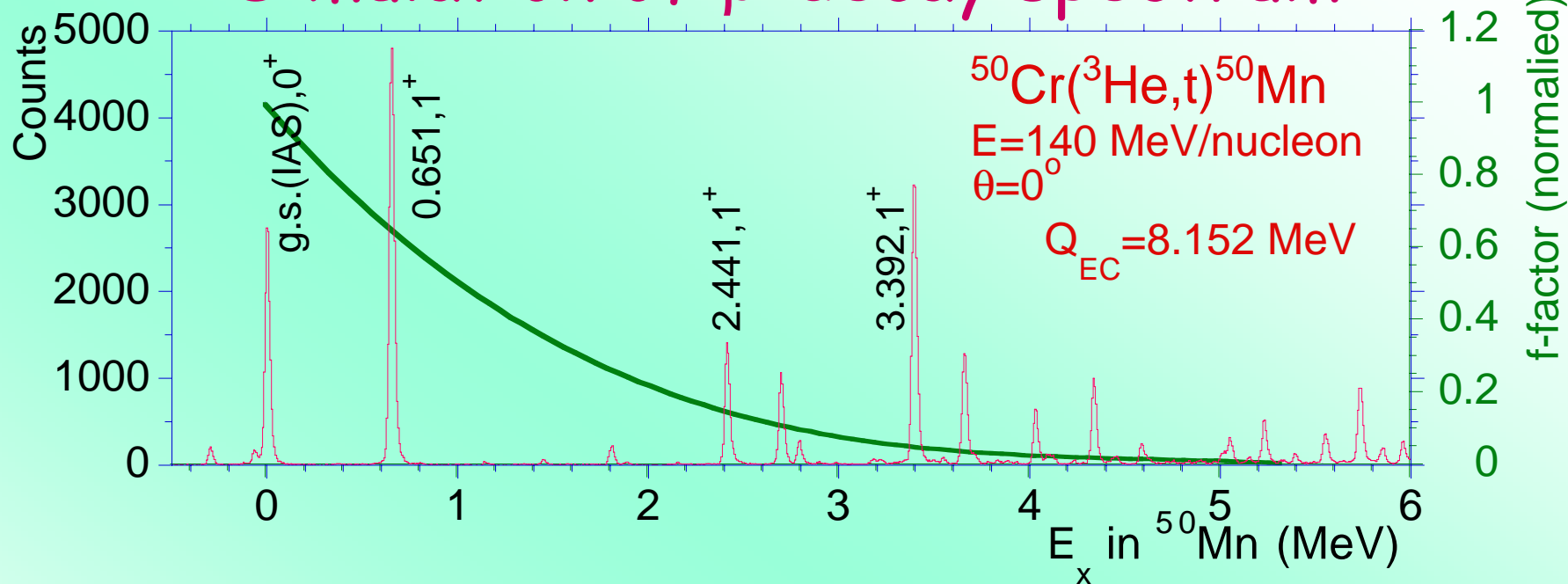


\*\*Reconstruction of  $\beta$  decay from ( ${}^3\text{He}, t$ )  
---assuming isospin symmetry ---

# Isospin Symmetry Transitions:



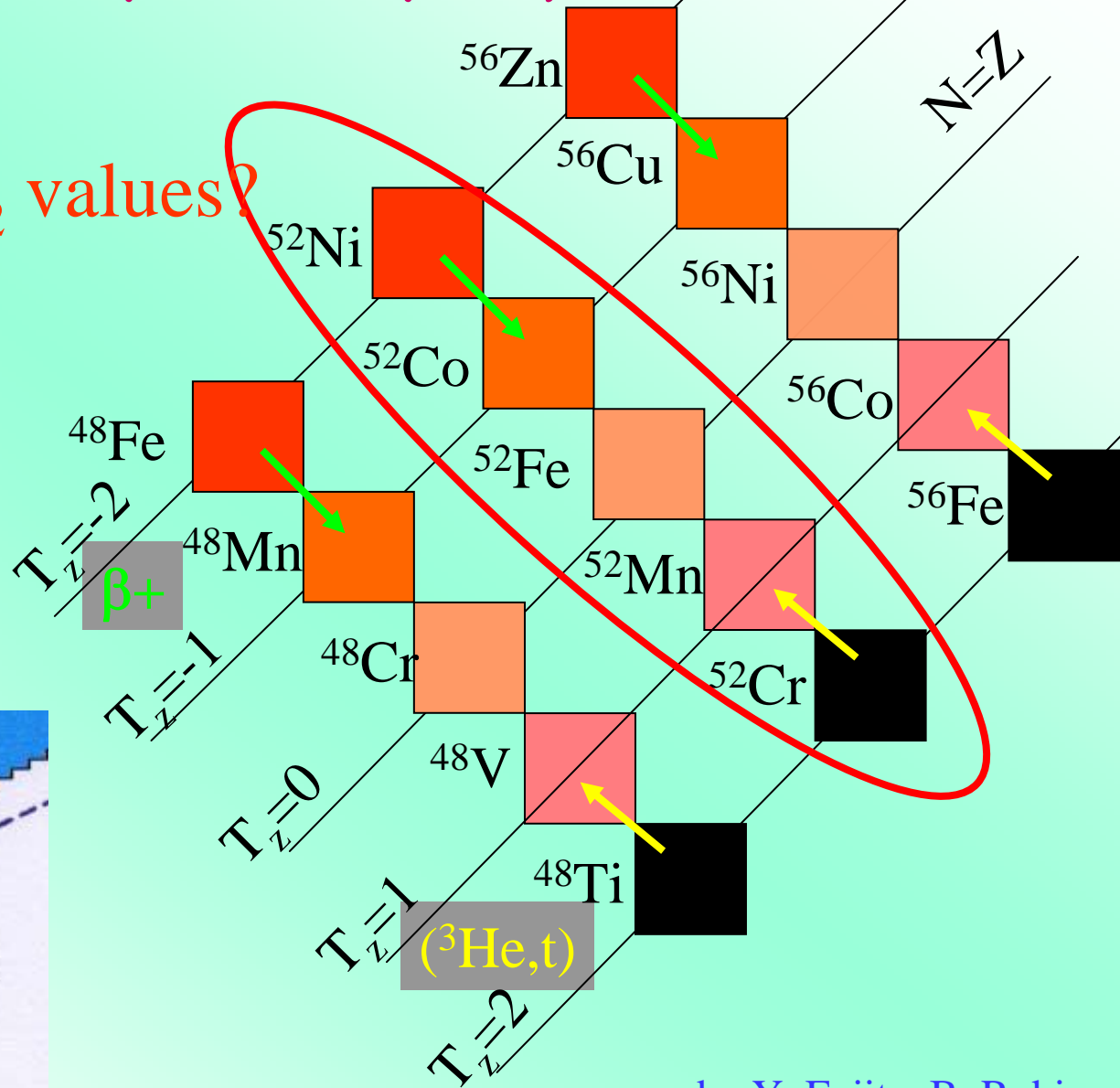
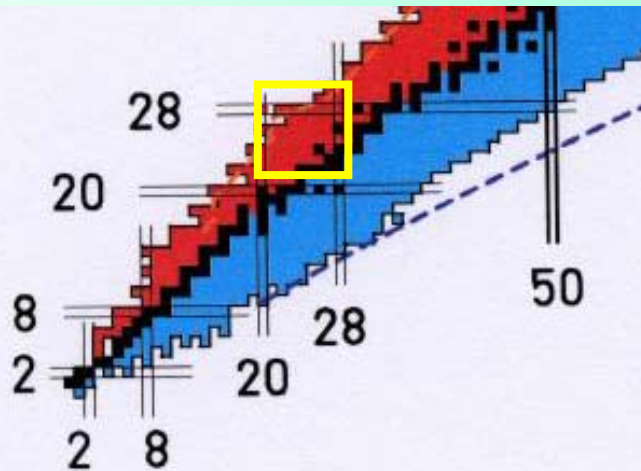
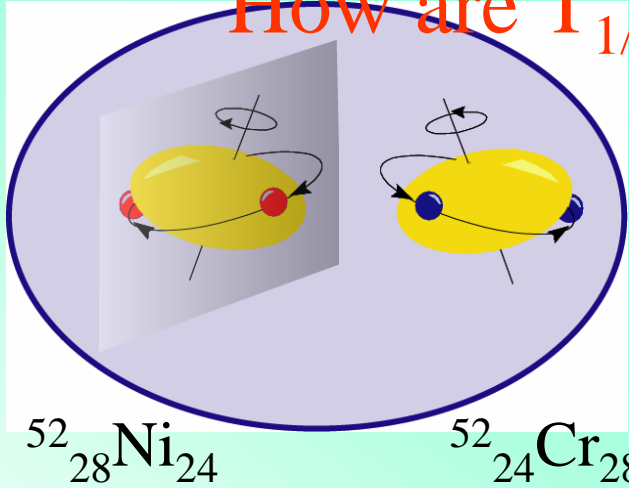
# Simulation of $\beta$ -decay spectrum



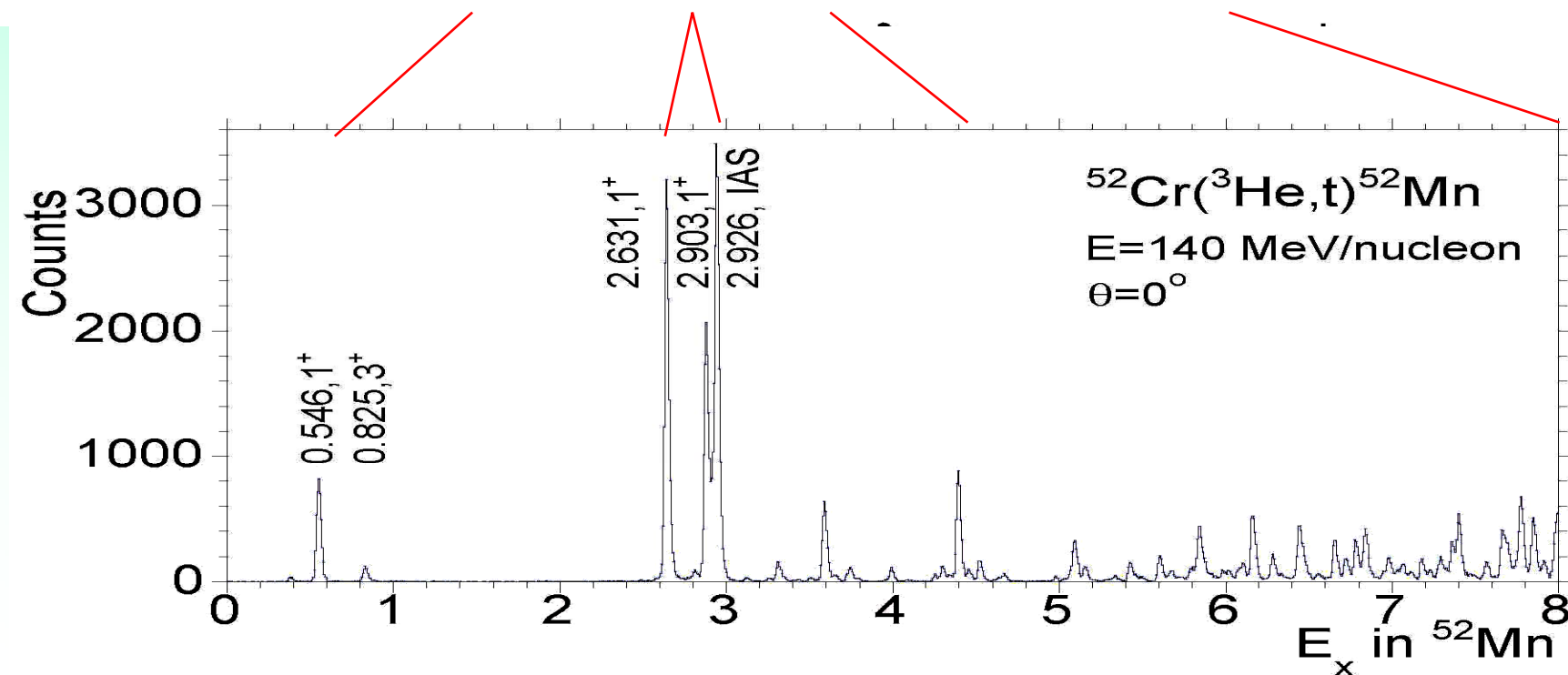
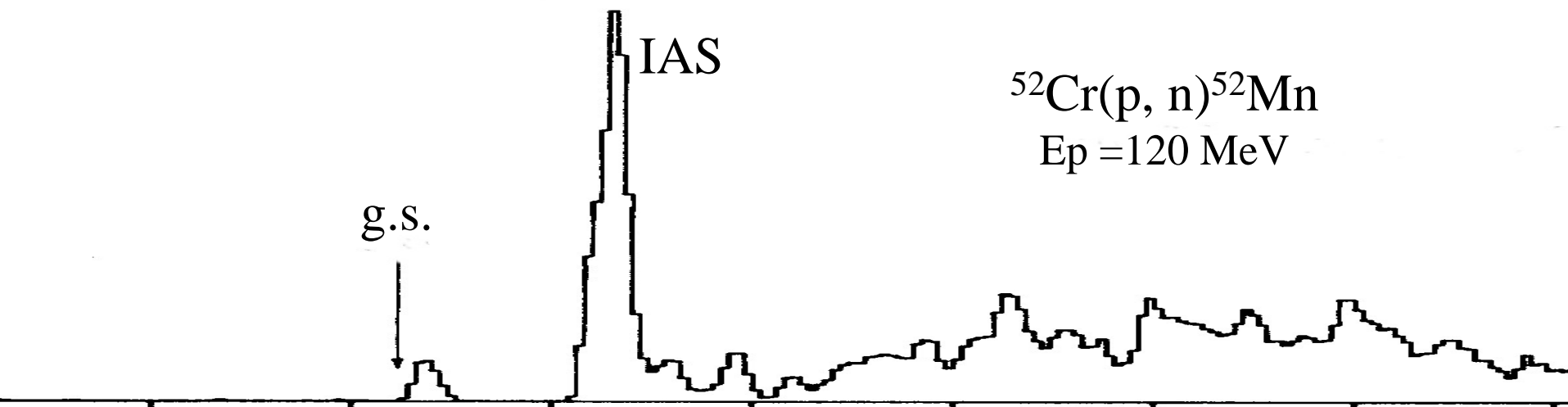
# T = 2 Isospin Symmetry in *pf*-shell Nuclei

## Mirror nuclei

How are  $T_{1/2}$  values?



# Comparison: (p, n) and ( $^3\text{He}, t$ )





# $\beta$ -decay Half-life $T_{1/2}$

-via reconstruction of  $\beta$ -decay spectrum-

$$\frac{1}{T_{1/2}} = \frac{1}{t_{Fermi}} + \sum_{i=GT} \frac{1}{t_i}$$

$$B(F) = N - Z$$

*Feedings*  $\propto 1/t_i$

abs.  $B(GT)$  distribution  
from ( ${}^3\text{He}, t$ )

# $^{52}\text{Ni}$ $\beta$ -decay Half-life $T_{1/2}$

$$\frac{1}{T_{1/2}} = \frac{1}{t_{Fermi}} + \sum_{i=GT} \frac{1}{t_i}$$

$$B(F) = N - Z$$

Isospin symmetry estimation

$T_{1/2} \sim 38$  (4) ms (preliminary)

$\beta$ -decay exp. (GANIL '06 B. Blank et al.)

$T_{1/2} = 40.8$  (30) ms

SM cal. (PRC 57, 2316, '98)

$T_{1/2} = 50$  ms

Mass formula (T. Tachibana et al.)

$T_{1/2} = 35$  ms

*Feedings*  $\propto 1/t_i$

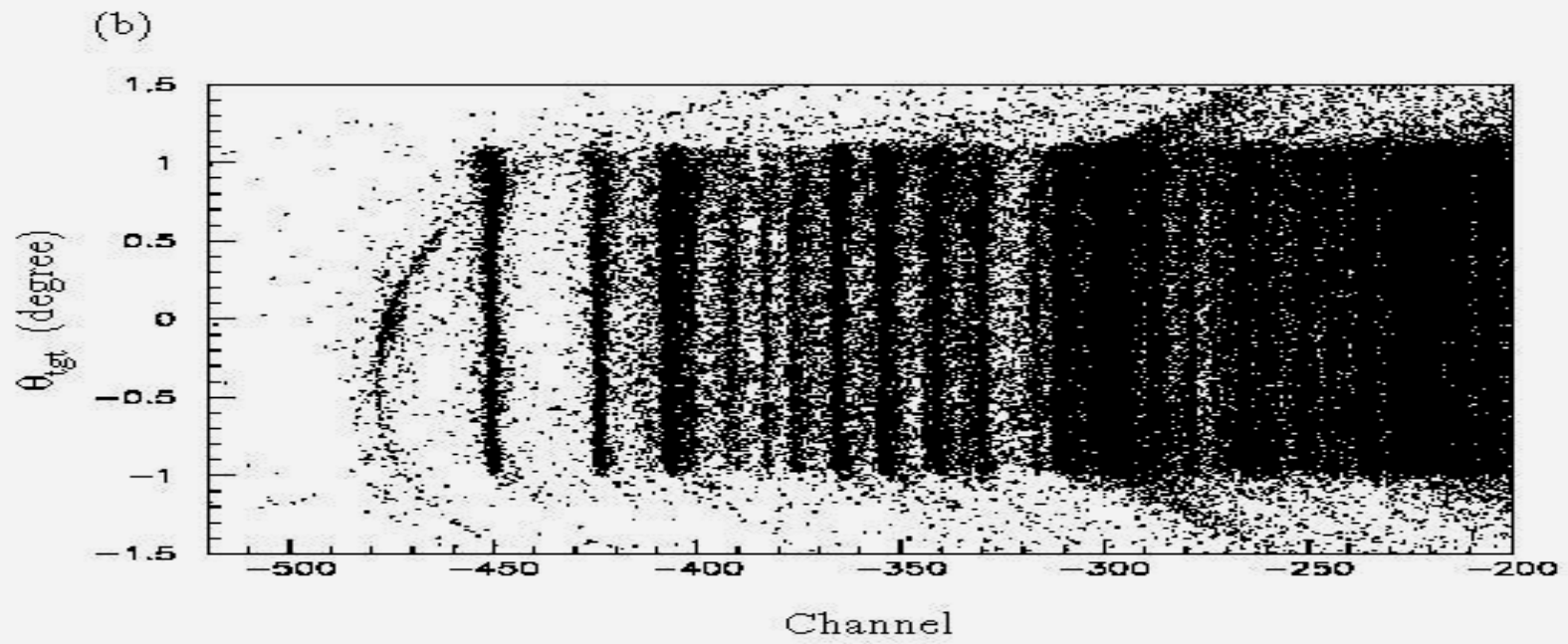
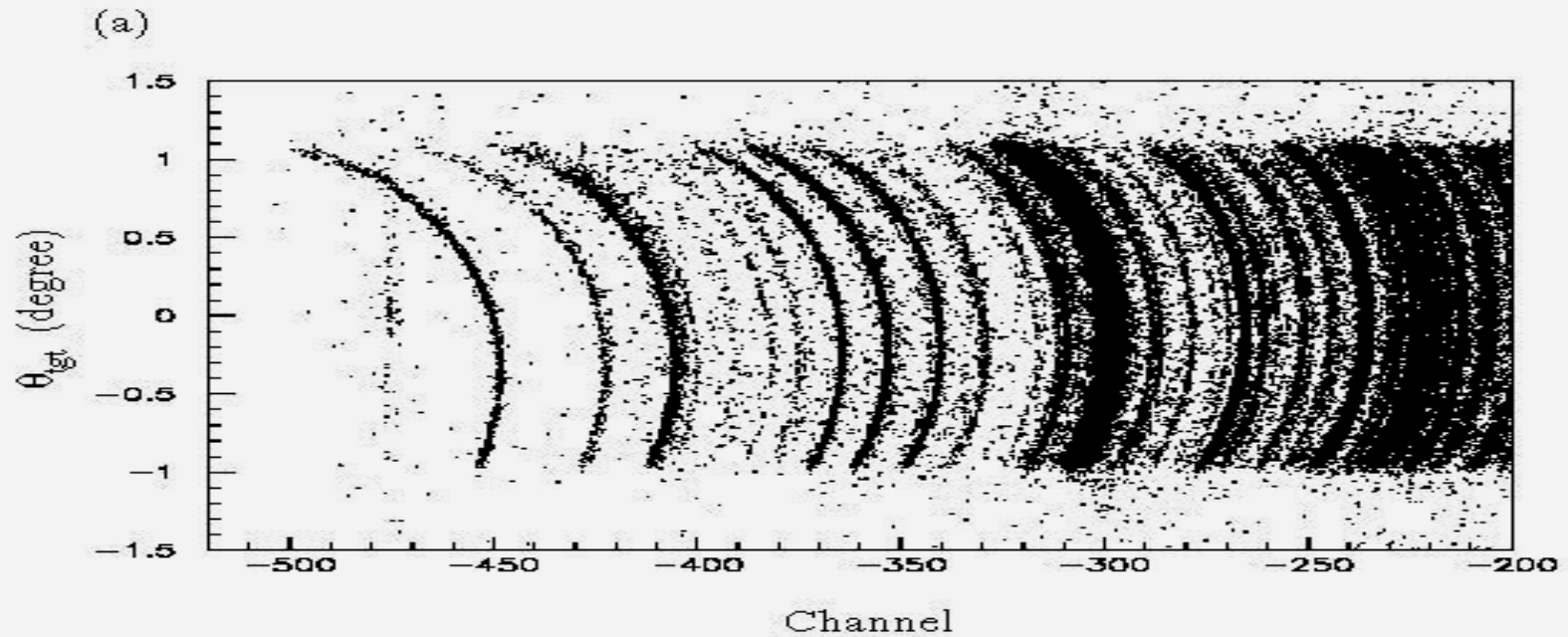
Uncertainty of the Q-value

should still be reduced!

abs.  $B(GT)$  distribution  
from  $^{52}\text{Cr}(^3\text{He}, t)$

$Q_{EC} = 11.898(44)$  MeV

# Effect of 2<sup>nd</sup> order aberrations



# Summary Words

## ★ High Resolution

$(^3\text{He},t)$  reaction : one order better resolution than in a  $(p,n)$  reaction  
Inelastic Scatterings  $(p,p')$ ,  $(^3\text{He},^3\text{He}')$  : less back ground  
→ RCNP is “THE” leading facility in the world

## ★ Angular Distribution Measurement in Dispersive Mode

## ★ Polarization Related Measurements in Dispersive Mode (using pol. $p$ , pol. $^3\text{He}$ , ...)

→ Various New Steps toward the “Higher Quality Measurements and Physics” are foreseen !