# Experimental study on inflation of the $2_{2}^{+}$state in ${ }^{12} \mathbf{C}$ 

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The $0_{2}^{+}$state in ${ }^{12} \mathrm{C}$, which is called the Hoyle state, is known to have spatially well-developed $3 \alpha$ cluster structure. It is considered that the radius of the Hoyle state is $2-3$ times larger than that of the ground state, and thus, the Hoyle state is much more dilute than usual states. This is different from the well-known fact that the nuclear density is saturated and independent of the kind of nuclei. Therefore, we should experimentaly determine the radius of the Hoyle state.

However, it is not easy to measure radii of excited states. Although it is naively expected that the nuclear radius reflects on the diffraction pattern of the angular distribution of the scattering cross section, the diffraction pattern in inelastic scattering is related to the density distributions of not only the excited state but also the ground state. The relationship between the angular distribution of the cross section and the radius of the excited state is not trivial.

Recently, M. Ito proposed to measure the inelastic scattering for the $2_{2}^{+}$state in ${ }^{12} \mathrm{C}$ instead of the Hoyle state [1]. M. Ito pointed out that the angular distribution of the cross section for the $\Delta L=0$ transition is not sensitive to the radius of the excited state but that for the $\Delta L=2$ transition has a certain sensitivity. The $2_{2}^{+}$ state is the rotational excited state of the Hoyle state and is considered to have the large radius like the Hoyle state. The $3 \alpha$ resonating-group method (RGM) calculation [2] suggests that the radii of the $2_{2}^{+}$state and the Hoyle state are 4.0 fm and 3.5 fm , respectively, while that of the ground state is as small as 2.4 fm .

The experiment was carried out at the W course in Research Center for Nuclear Physics (RCNP), Osaka University. A proton beam at 53.3 MeV bombarded the ${ }^{12} \mathrm{C}$ target with a thickness of $2.8 \mathrm{mg} / \mathrm{cm}^{2}$, and the scattered protons were analyzed by the Raiden spectrometer [3]. We measured the differential cross sections of the elastic proton scattering and inelastic proton scattering exciting the $2_{1}^{+}, 0_{2}^{+}$, and $3_{1}^{-}$states in ${ }^{12} \mathrm{C}$.


Figure 1: Excitation-energy spectrum of ${ }^{12} \mathrm{C}\left(\mathrm{p}, \mathrm{p}^{\prime}\right)$ at $\theta_{\text {Lab }}=15.0^{\circ}$. The dashed, dotted, and dashdotted lines show the fitting result for the sum of the $2_{2}^{+}$and $0_{3}^{+}$states, the $1_{1}^{-}$state, and the $3_{1}^{-}$state, respectively, while the solid line is the sum of these four states.


Figure 2: Sum of the measured cross section of the $2_{2}^{+}$and $0_{3}^{+}$states compared with the theoretical calculation (see text).

These $0_{3}^{+}$and $2_{2}^{+}$states around $E_{x}=10 \mathrm{MeV}$ in ${ }^{12} \mathrm{C}$ are broad states, and thus they overlap each other in the excitation-energy spectrum as shown in Fig. 1. Therefore, it is difficult to separately determine the respective differential cross sections. We fit the excitation-energy spectra in $E_{x}=9.17-10.14 \mathrm{MeV}$ assuming the narrow peak due to the $3_{1}^{-}$state and the broad bumps due to the $2_{2}^{+}$and $0_{3}^{+}$states. The dashed, dotted, and dash-dotted lines in Fig. 1 show the fitting result for the sum of the $2_{2}^{+}$and $0_{3}^{+}$states, the $1_{1}^{-}$state, and the $3_{1}^{-}$ state, respectively, while the solid line is the sum of these four states. The measured cross sections for the sum of the $2_{2}^{+}$and $0_{3}^{+}$states were compared with the theoretical calculation in Fig. 2. The transition densities for the $2_{2}^{+}$and $0_{3}^{+}$states used in the calculation were taken from the $3 \alpha$ RGM calculation [2]. The black and blue solid lines show the calculated cross sections of the $2_{2}^{+}$and $0_{3}^{+}$states, while the red solid line is the sum of the
$2_{2}^{+}$and $0_{3}^{+}$states. The calculated cross sections of the $2_{2}^{+}$and $0_{3}^{+}$states were normalized to fit the experimental data. As shown in Fig. 2, the theoretical calculation does not reproduce the experiment at the backward angles. We also performed another calculation assuming that the radius of the $2^{+}$state is small ( 2.54 fm ) as shown by the dashed lines in Fig. 2. The angular distribution for the smaller radius shifts to the forward angles opposite to the experiment, but the calculation does not still reproduce the experiment.

In the previous measurement of the ${ }^{12} \mathrm{C}\left(\alpha, \alpha^{\prime}\right)$ reaction, the theoretical calculation using the $3 \alpha$ RGM wave function reasonably explained the experiment [4]. The reason of this discrepancy between the ( $p, p^{\prime}$ ) and ( $\alpha, \alpha^{\prime}$ ) reactions are still unknown. Further investigation of this discrepancy is strongly desired.

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