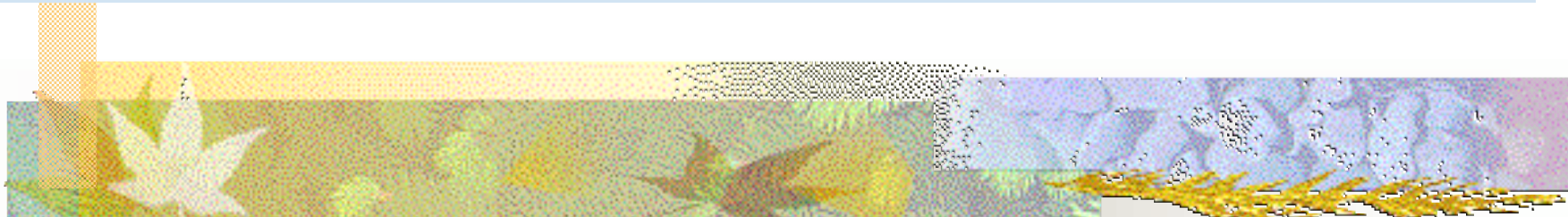


Magnetic moments of the $N(1535)$ resonance in the chiral unitary model



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Motivations

- **Experiments**

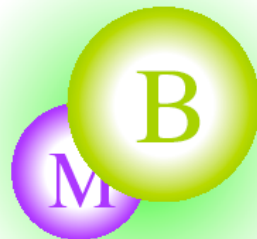
Recent developments of the experimental technique enable us to measure the **magnetic moments of the excited baryons**.

- **Application of the chiral unitary model**

Chiral unitary model

Flavor SU(3) meson-baryon scatterings (s-wave)

$J^P = 1/2^-$
Resonances



Chiral symmetry

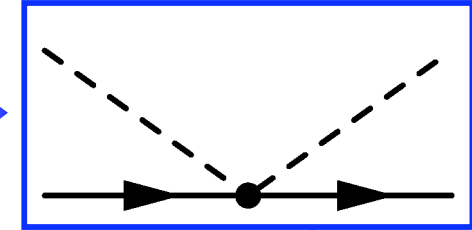
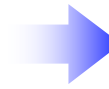
Unitarity of S-matrix

Investigation of the resonance structure

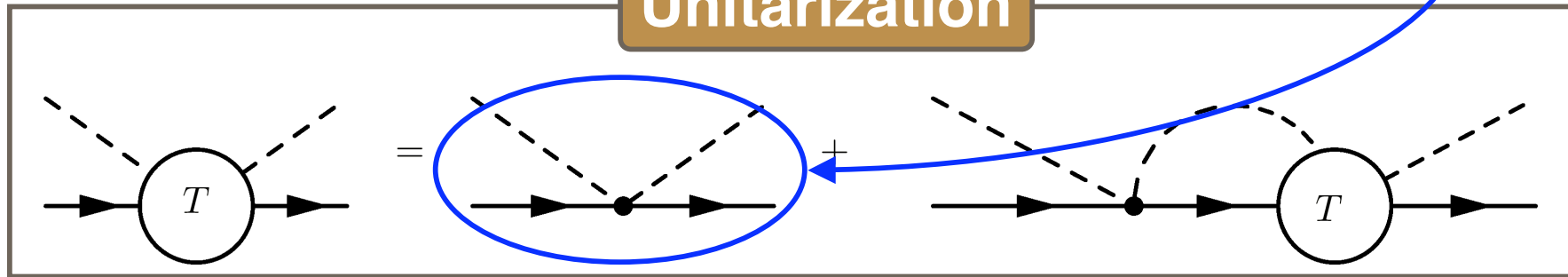
Framework of the chiral unitary model

Chiral perturbation theory

$$\mathcal{L}_{WT} = \frac{1}{4f^2} \text{Tr}(\bar{B}i\gamma^\mu[(\Phi\partial_\mu\Phi - \partial_\mu\Phi\Phi), B])$$

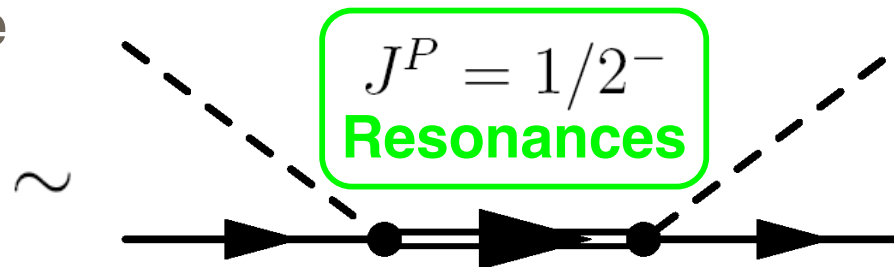


Unitarization



$$T_{ij}(\sqrt{s}) \sim \frac{g_i g_j}{\sqrt{s} - M_R + i\Gamma_R/2} + T_{ij}^{BG}$$

Generated resonances are expressed as the poles of the T-matrix.



The N(1535) resonance in the chiral unitary model

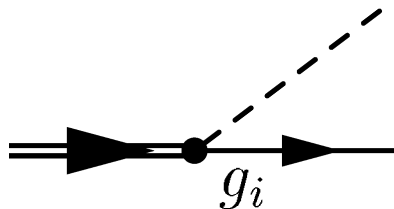
$Q = 0$	$\pi^0 n$	πp	ηn	$K^0 \Lambda$	$K^0 \Sigma^0$	$K^+ \Sigma^-$
$Q = 1$	$\pi^0 p$	$\pi^\pm n$	ηp	$K^+ \Lambda$	$K^+ \Sigma^0$	$K^0 \Sigma^\pm$

Position of the pole

$$z_{n^*} = 1536 - 37i \text{ [MeV]}$$

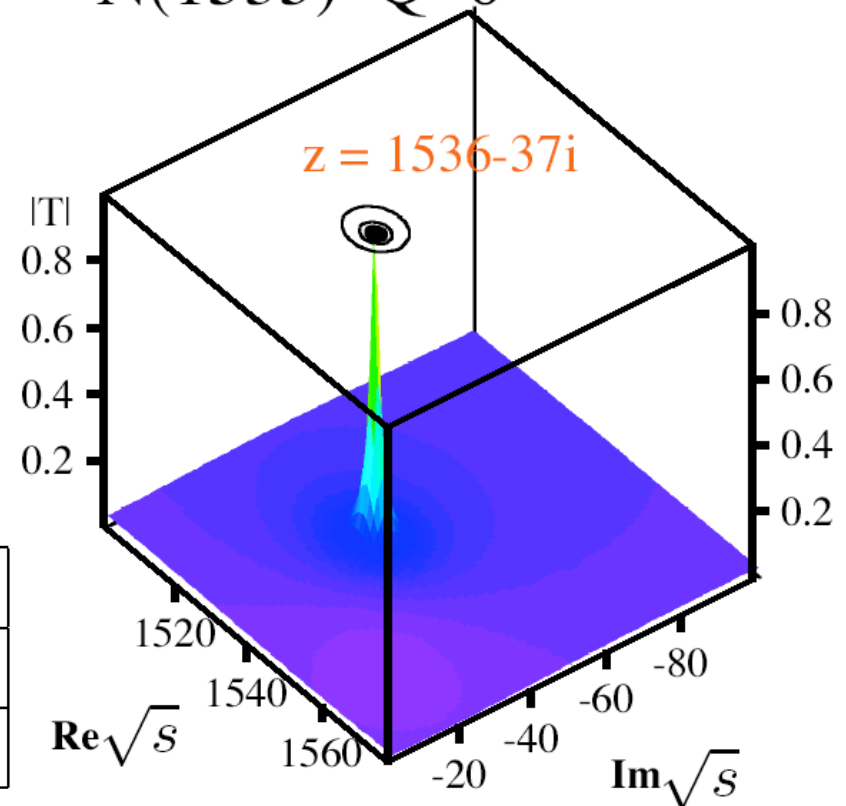
$$z_{p^*} = 1531 - 36i \text{ [MeV]}$$

Coupling strengths

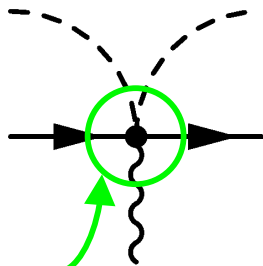
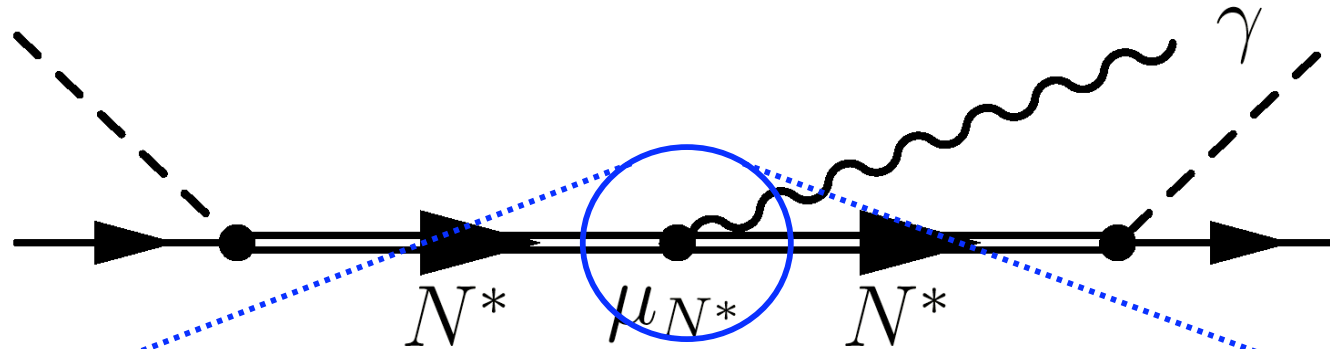


	$ g_{\pi N} ^2$	$ g_{\eta N} ^2$	$ g_{K\Lambda} ^2$	$ g_{K\Sigma} ^2$
n^*	0.623	2.30	1.93	7.29
p^*	0.619	2.35	1.88	7.37

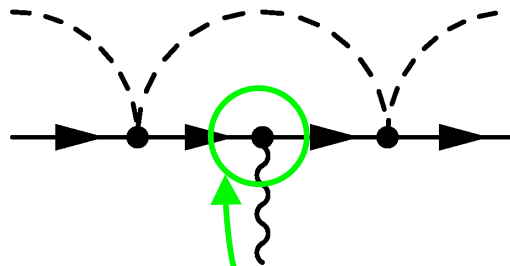
N(1535) Q=0



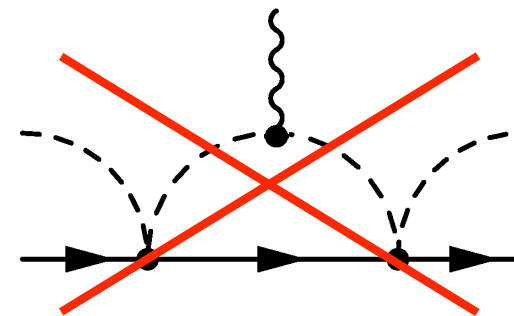
Photon coupling diagrams



ChPT



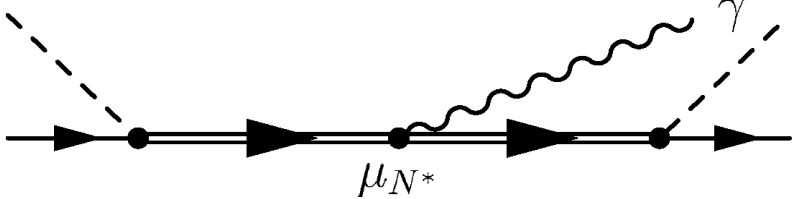
\square of ground state baryons




do not contribute

Two ways to extract μ_{N^*}

Evaluation of the magnetic moments

$$\begin{aligned}
 -i\tilde{t}_{ij}(\sqrt{s}) &= \text{Diagram} \times \left(\frac{e}{2M_p} (\boldsymbol{\sigma} \times \mathbf{q}) \cdot \boldsymbol{\epsilon} \right)^{-1} \\
 &\sim g_i \left(\frac{1}{\sqrt{s} - M_{N^*} + i\Gamma_{N^*}/2} \right) \mu_{N^*} \left(\frac{1}{\sqrt{s} - M_{N^*} + i\Gamma_{N^*}/2} \right) g_j
 \end{aligned}$$


$$\begin{aligned}
 T_{ij}(\sqrt{s}) &= \text{Diagram} \\
 &\sim \frac{g_i g_j}{\sqrt{s} - M_{N^*} + i\Gamma_{N^*}/2}
 \end{aligned}$$


Real axis

$$\mu_R(\sqrt{s}) = \frac{-i\tilde{t}_{ij}(\sqrt{s})}{\frac{\partial}{\partial \sqrt{s}} T_{ij}(\sqrt{s})},$$

Complex plane

$$\mu_C(z_R) = \lim_{z \rightarrow z_R} (z - z_R) \frac{-i\tilde{t}_{ij}(z)}{T_{ij}(z)}$$

Real axis and complex plane

Real axis

- **Sign : O.K.**
- Channel dependence
➔ strong coupling
- \sqrt{s} dependence
➔ around resonance
- **Ambiguities**

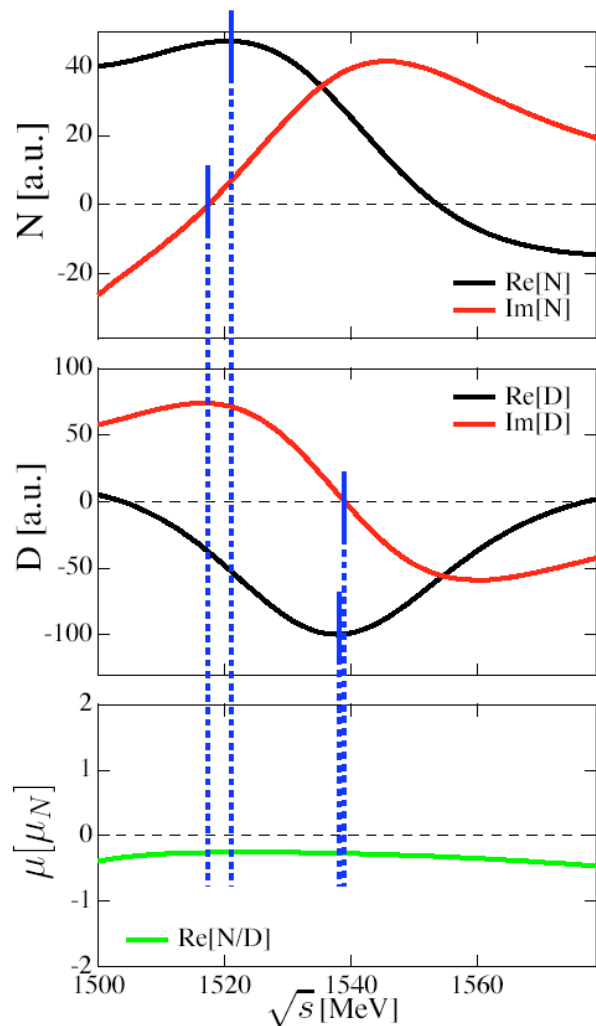
Complex plane

- **No background**
Complex value
↓
Complex phase
↓
• **Sign : X**

Strategy : combine both the results

Results on the real axis.

$K\Sigma \ K\Sigma \ (Q=0)$

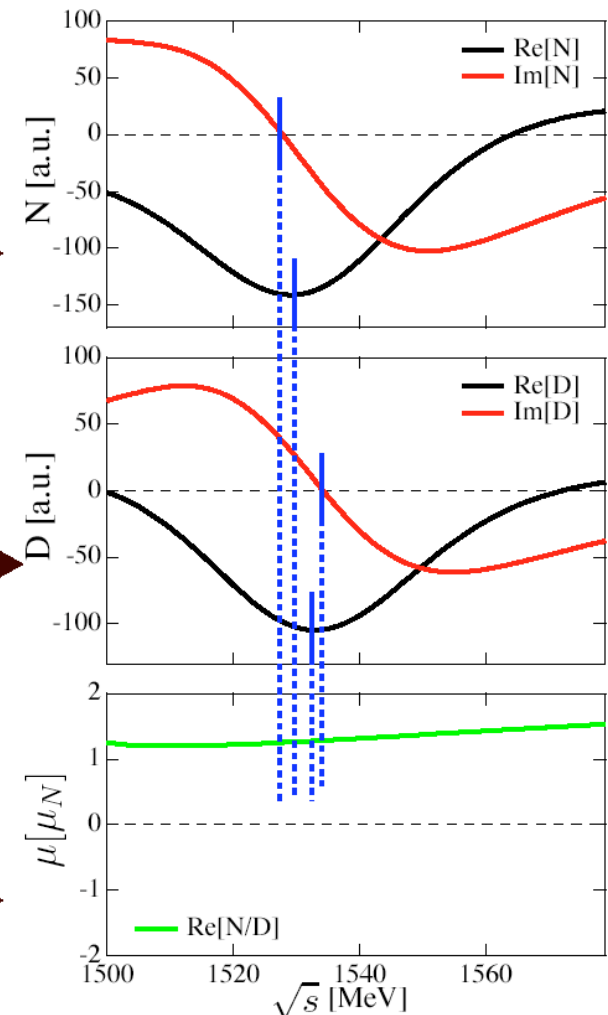


← **opposite signs** →

← **almost same**
(isospin symmetry) →

← **opposite signs** →

$K\Sigma \ K\Sigma \ (Q=1)$


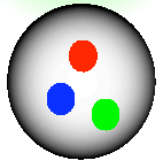


Results in the complex plane (channel independent).

$$|\mu_{n^*}| \sim 0.248 \mu_N, \quad |\mu_{p^*}| \sim 1.13 \mu_N.$$

Conclusion

We calculate the **magnetic moments of the N(1535) resonance** using the chiral unitary model.

	$n^* [\mu_N]$	$p^* [\mu_N]$	picture
ChU model	-0.25	1.13	
Quark model	-1.28	1.89	

The **absolute values** of the present results differ from those of the quark model, especially in n^* .

➡ **pictures of the excited states?**

This point will be checked when experimental data are available.