

Photoproduction of K^* for the study of $\Lambda(1405)$



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Motivation : Two poles?

There are two poles of the scattering amplitude around nominal $\Lambda(1405)$ energy region.

- Cloudy bag model
(1990)

J. Fink, *et al.*, PRC41, 2720

- Chiral unitary model
(2001~)

J. A. Oller, *et al.*, PLB500, 263

E. Oset, *et al.*, PLB527, 99

D. Jido, *et al.*, PRC66, 025203

T. Hyodo, *et al.*, PRC68, 018201

T. Hyodo, *et al.*, PTP, in press

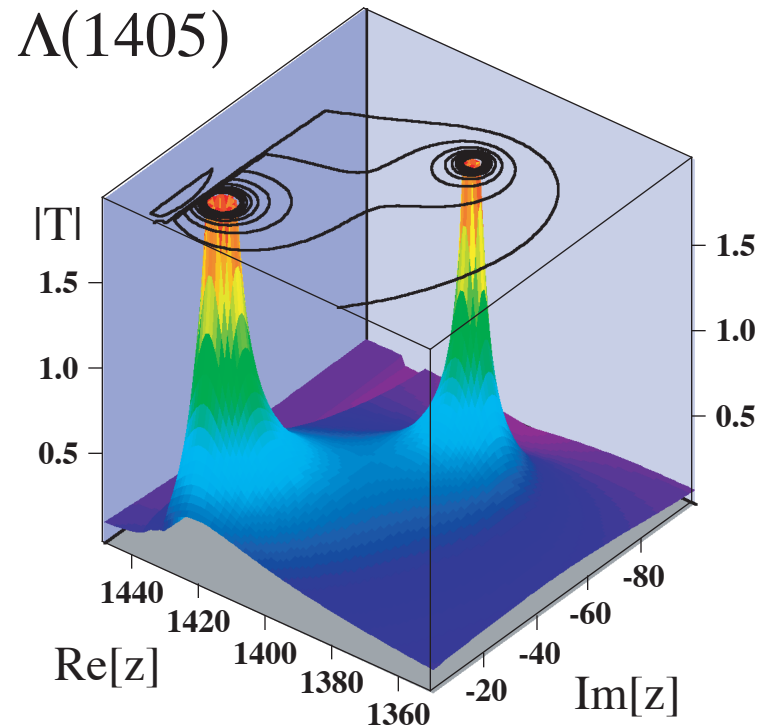
C. Garcia-Recio, *et al.*, PRD67, 076009

D. Jido, *et al.*, NPA725, 181

T. Hyodo, *et al.*, PRC68, 065203

C. Garcia-Recio, *et al.*, PLB582, 49

$\Lambda(1405) : J^P = 1/2^-, I = 0$



ChU model, T. Hyodo

Chiral unitary model

Flavor SU(3) meson-baryon scatterings (s-wave)

Chiral symmetry

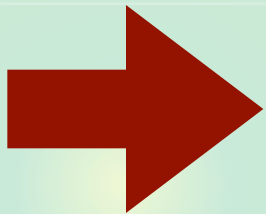
**Low energy
behavior**



Unitarity of S-matrix

**Non-perturbative
resummation**

**Dynamical
generation**



$J^P = 1/2^-$ resonances

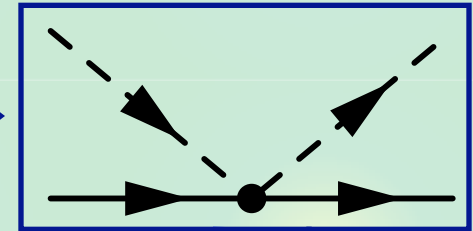
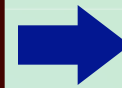
$\Lambda(1405), \Lambda(1670),$
 $\Sigma(1620), \Xi(1620),$
 $N(1535)$



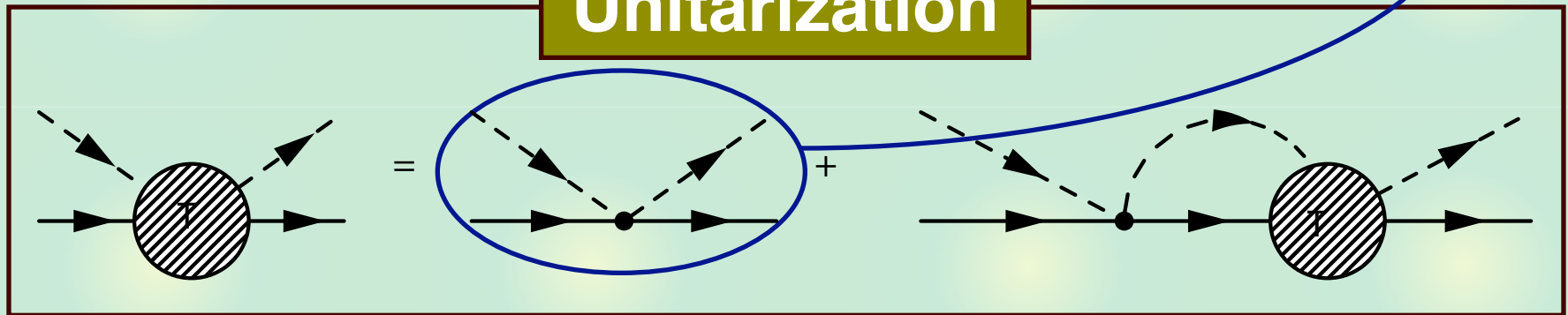
Framework of the chiral unitary model

Chiral perturbation theory

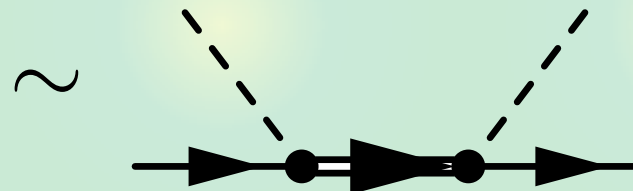
$$\mathcal{L}_{WT} = \frac{1}{4f^2} \text{Tr}(\bar{B}i\gamma^\mu[(\Phi\partial_\mu\Phi - \partial_\mu\Phi\Phi), B])$$



Unitarization



$$T_{ij}(\sqrt{s}) \sim \frac{g_i g_j}{\sqrt{s} - M_R + i\Gamma_R/2} + T_{ij}^{BG}$$



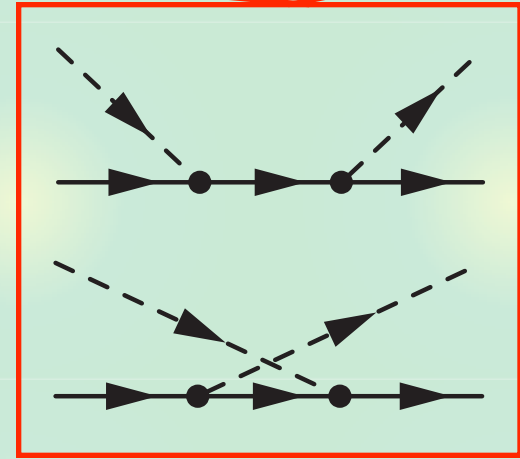
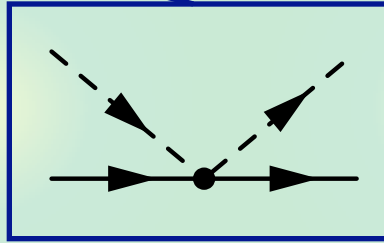
ChPT Lagrangian

$$\mathcal{L}^{(1)} = \text{Tr} \left(\bar{B}(i\not{D} - M_0)B - D(\bar{B}\gamma^\mu\gamma_5\{A_\mu, B\}) - F(\bar{B}\gamma^\mu\gamma_5[A_\mu, B]) \right)$$

$$\mathcal{D}_\mu B = \partial_\mu B + i[V_\mu, B]$$

$$\xi(\Phi) = \exp\{i\Phi/\sqrt{2}f\}$$

$$D + F = g_A$$



$$B = \begin{pmatrix} \frac{1}{\sqrt{2}}\Sigma^0 + \frac{1}{\sqrt{6}}\Lambda & \Sigma^+ & p \\ \Sigma^- & -\frac{1}{\sqrt{2}}\Sigma^0 + \frac{1}{\sqrt{6}}\Lambda & n \\ \Xi^- & \Xi^0 & -\frac{2}{\sqrt{6}}\Lambda \end{pmatrix} \quad \Phi = \begin{pmatrix} \frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta & \pi^+ & K^+ \\ \pi^- & -\frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta & K^0 \\ K^- & \bar{K}^0 & -\frac{2}{\sqrt{6}}\eta \end{pmatrix}$$

$$\underline{V}_\mu = -\frac{i}{2}(\xi^\dagger\partial_\mu\xi + \xi\partial_\mu\xi^\dagger) = \frac{i}{4f^2}(\underline{\Phi\partial_\mu\Phi} - \partial_\mu\underline{\Phi\Phi}) + \dots$$

$$\underline{A}_\mu = -\frac{i}{2}(\xi^\dagger\partial_\mu\xi - \xi\partial_\mu\xi^\dagger) = -\frac{1}{f}\underline{\partial_\mu\Phi} + \dots$$

Several treatments

N. Kaiser, P. B. Siegel and W. Weise, NPA594, 325, PLB362, 23 (1995)

(HB)ChPT p^2 , Form factor (channel dep.)

S = -1,0, $\Lambda(1405)$, N(1535)

E. Oset and A. Ramos, NPA635, 99 (1998)

WT term, 3-momentum cutoff (channel indep.)

S = -1, $\Lambda(1405)$

J. A. Oller and U. G. Meissner, PLB500, 263 (2001)

ChPT p , dimensional reg. (channel indep.)

S = -1, $\Lambda(1405)$

Analytic solution for BS eq.

-> pole structure in complex plane

Several treatments

E. Oset, A. Ramos and C. Bennhold, PLB527, 99 (2002)

T. Inoue, E. Oset, and M. J. Vicente Vacas, PRC 65, 035204 (2002)

A. Ramos, E. Oset and C. Bennhold, PRL 89, 252001 (2002)

WT term, dimensional reg. (channel dep.)

$\Lambda(1405)$, $\Lambda(1670)$, $\Sigma(1620)$, $N(1535)$, $\Xi(1620)$

Scattering observables, $S = -1, 0$, analytic

M. F. M. Lutz and E. Kolomeitsev, NPA700, 193 (2002)

ChPT p^3 , Optimal reno. (channel indep.)

Scattering observables, Numerical solution

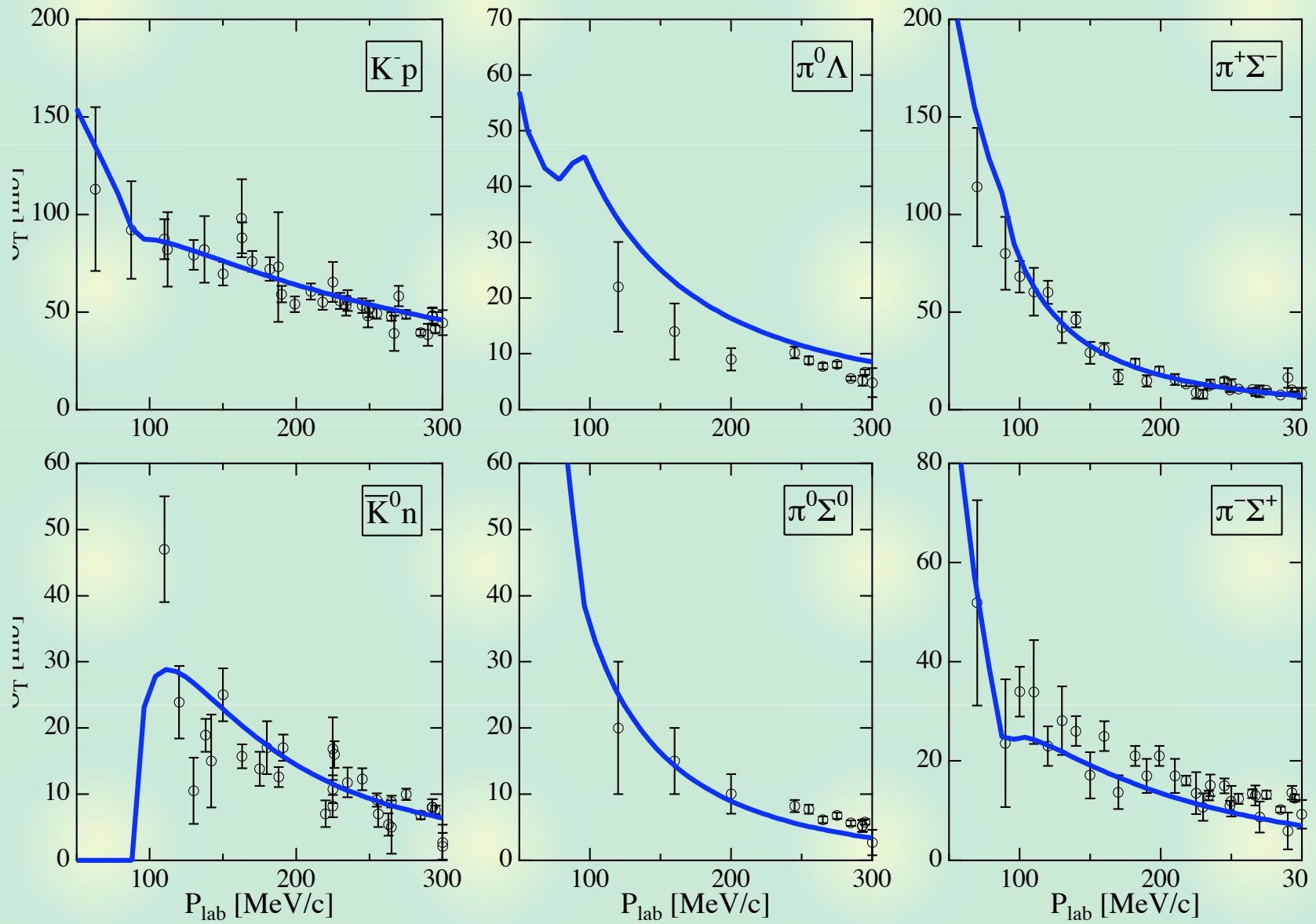
C. Garcia-Recio, M. F. M. Lutz and J. Nieves, PLB582, 49 (2004)

WT term, Optimal reno. (channel indep.)

$\Lambda(1405)$, $\Lambda(1670)$, $\Sigma(1620)$, $N(1535)$, $\Xi(1620)$, $\Xi(1690)$

Scattering observables?

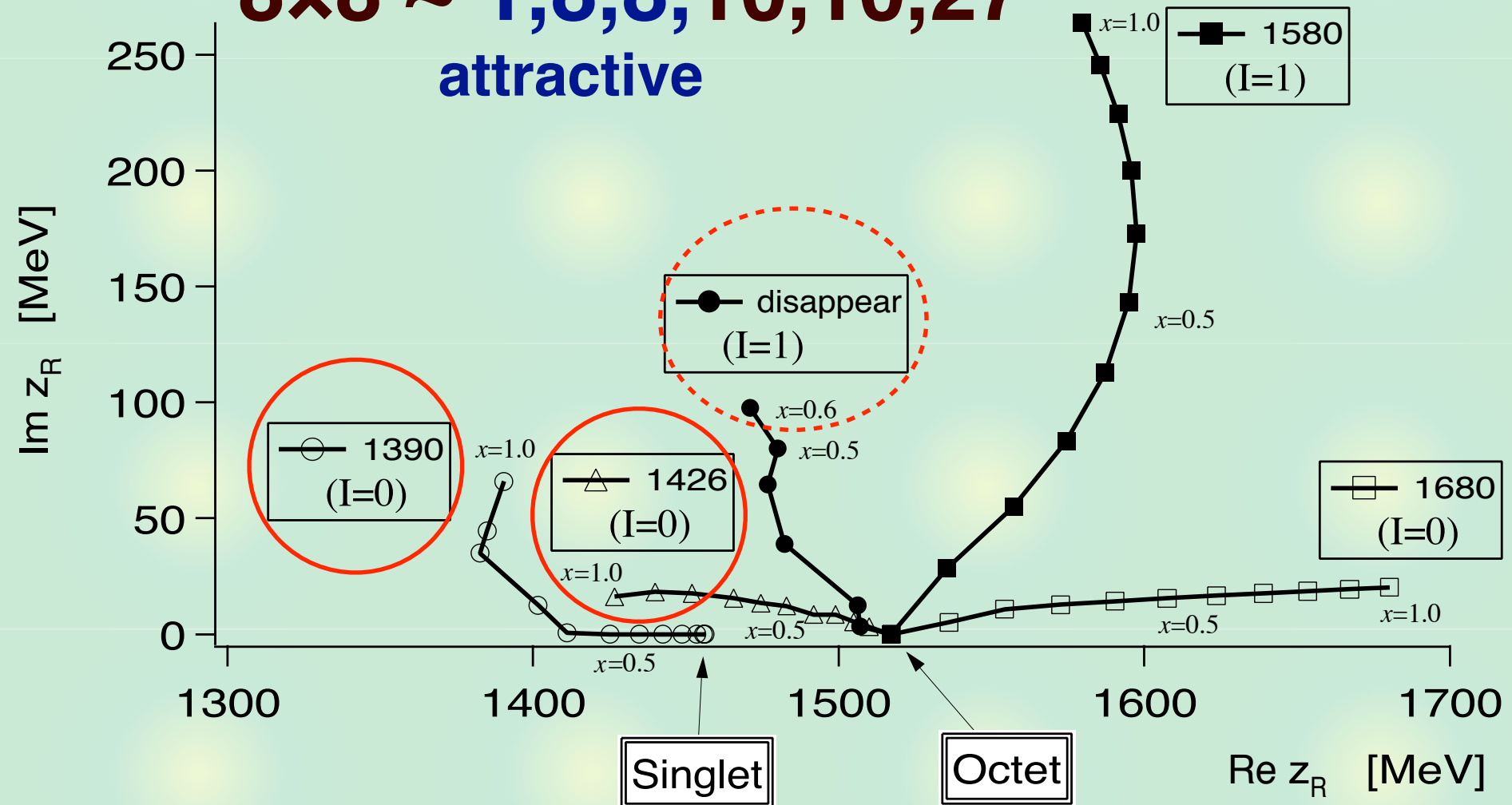
Total cross sections of K-p scattering



T. Hyodo, et al., Phys. Rev. C 68, 018201 (2003)

Trajectories of the poles with SU(3) breaking ($S = -1$)

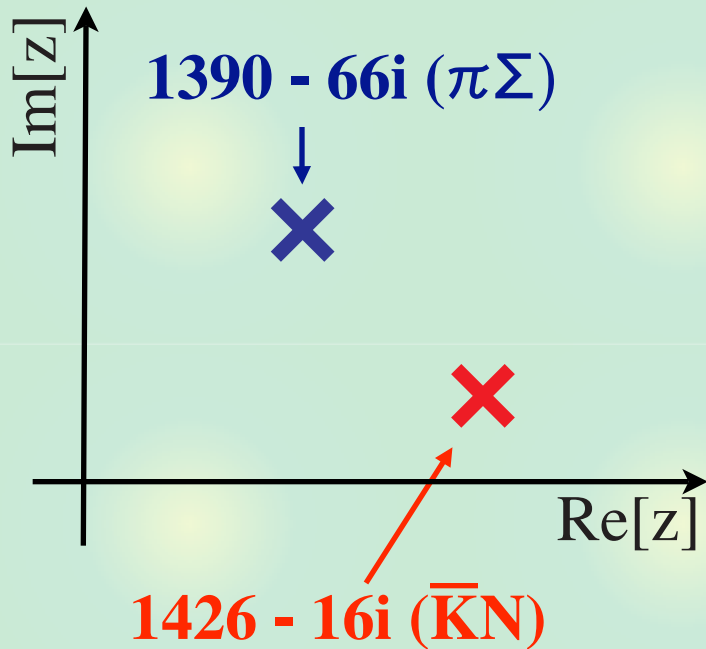
$8 \times 8 \sim 1, 8, 8, 10, \overline{10}, 27$
attractive



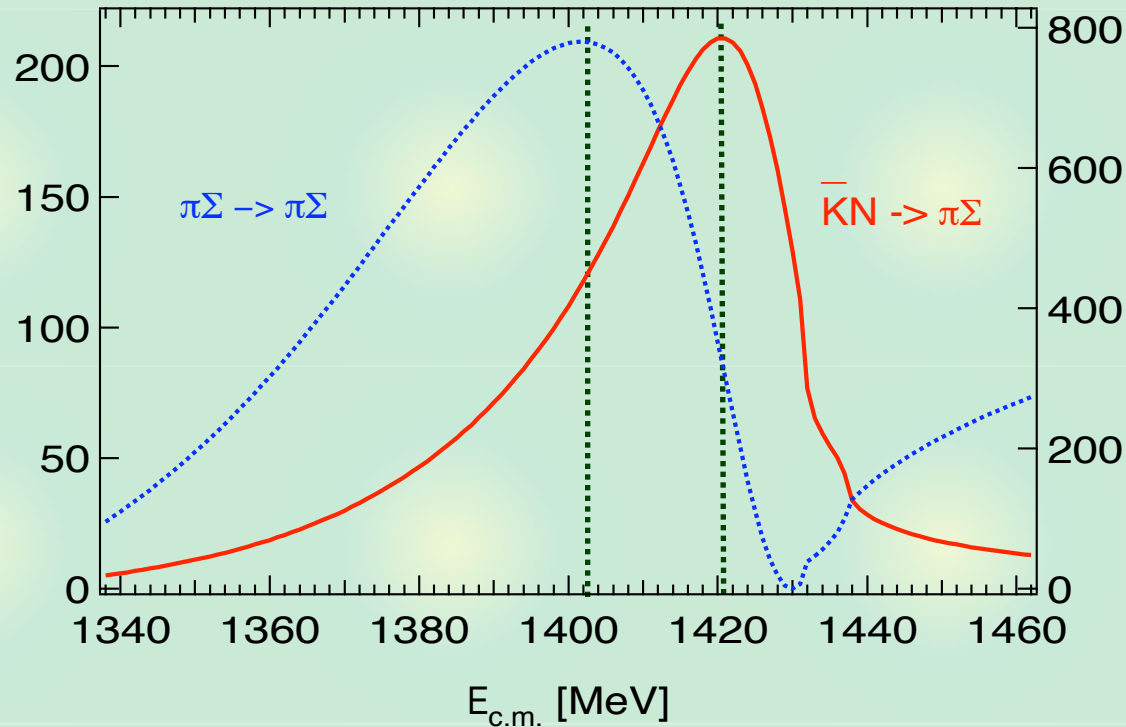
D. Jido, et al., Nucl. Phys. A 723, 205 (2003)

$\Lambda(1405)$ in the chiral unitary model

position of poles



$\pi\Sigma$ mass distribution



$$\frac{d\sigma}{dM_I} = C |t_{\pi\Sigma \rightarrow \pi\Sigma}|^2 p_{CM} \quad \longrightarrow \quad \frac{d\sigma}{dM_I} = \left| \sum_i C_i t_{i \rightarrow \pi\Sigma} \right|^2 p_{CM}$$

D. Jido, et al., Nucl. Phys. A 723, 205 (2003)

Photoproduction of K^* and $\Lambda(1405)$

In order to study

★ $S = -1, l = 0, s\text{-wave} : \Lambda(1405)$

★ two poles?

★ $1426 - 16i : \bar{K}N$

★ $1390 - 66i : \pi\Sigma$

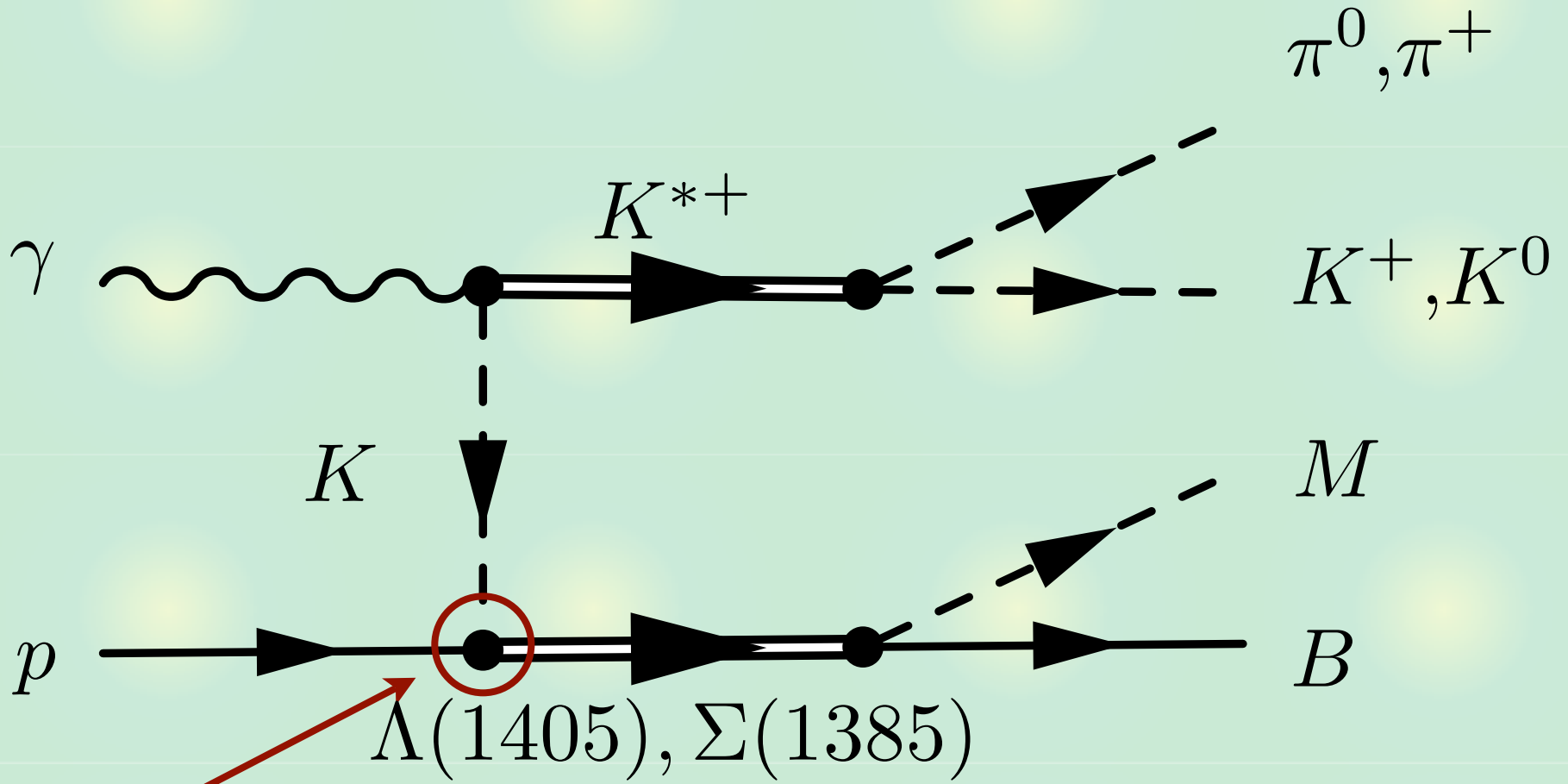
★ $S = -1, l = 1, s\text{-wave}$

★ pole?

we calculate

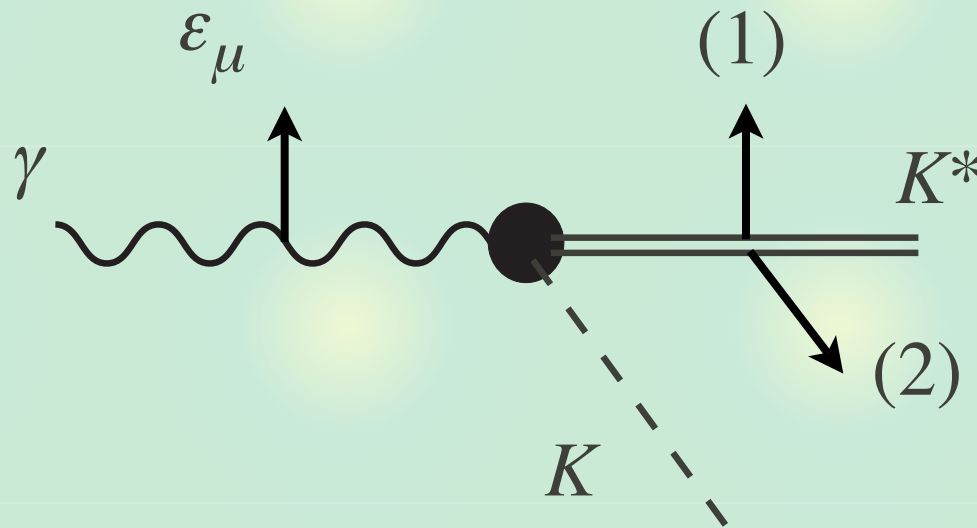
$$\gamma p \longrightarrow K^* \Lambda(1405)$$

Photoproduction of K^* and $\Lambda(1405)$



Only K^-p channel appears at the initial stage
Higher energy pole ??

Advantage of this reaction



$$(1) \quad \epsilon_\mu(K^*) \parallel \epsilon_\mu(\gamma) : J^P = \text{natural}$$

$$(2) \quad \epsilon_\mu(K^*) \perp \epsilon_\mu(\gamma) : J^P = \text{unnatural}$$

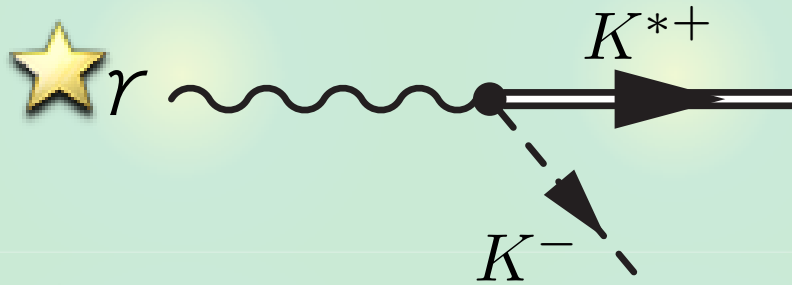
With polarized photon beam, the exchanged particle can be identified.

Clear mechanism

Effective interaction for meson part

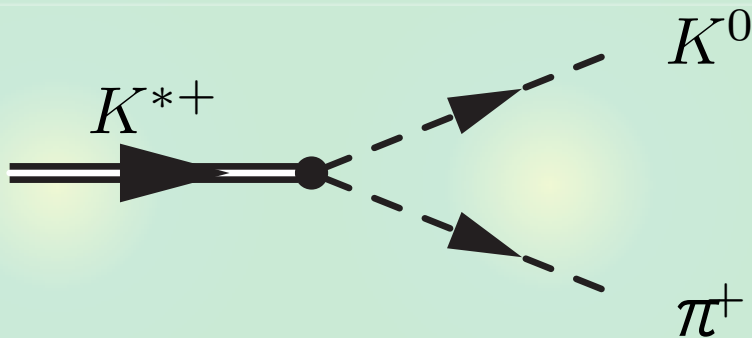
★ $\gamma K K^*$ coupling

$$\mathcal{L}_{K^* K \gamma} = g_{K^* K \gamma} \epsilon^{\mu\nu\alpha\beta} \partial_\mu A_\nu (\partial_\alpha K_\beta^{*-} K^+ + \partial_\alpha \bar{K}_\beta^{*0} K^0) + \text{h.c.}$$

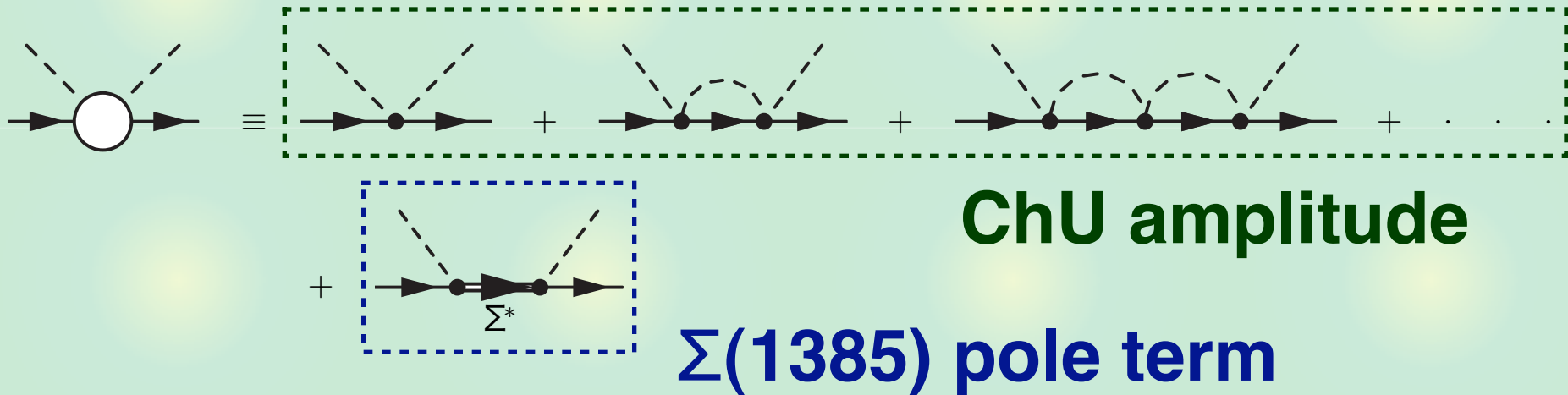


★ VPP coupling

$$\mathcal{L}_{VPP} = -\frac{ig_{VPP}}{\sqrt{2}} \text{Tr}(V^\mu [\partial_\mu P, P])$$



Effective interaction for baryon part



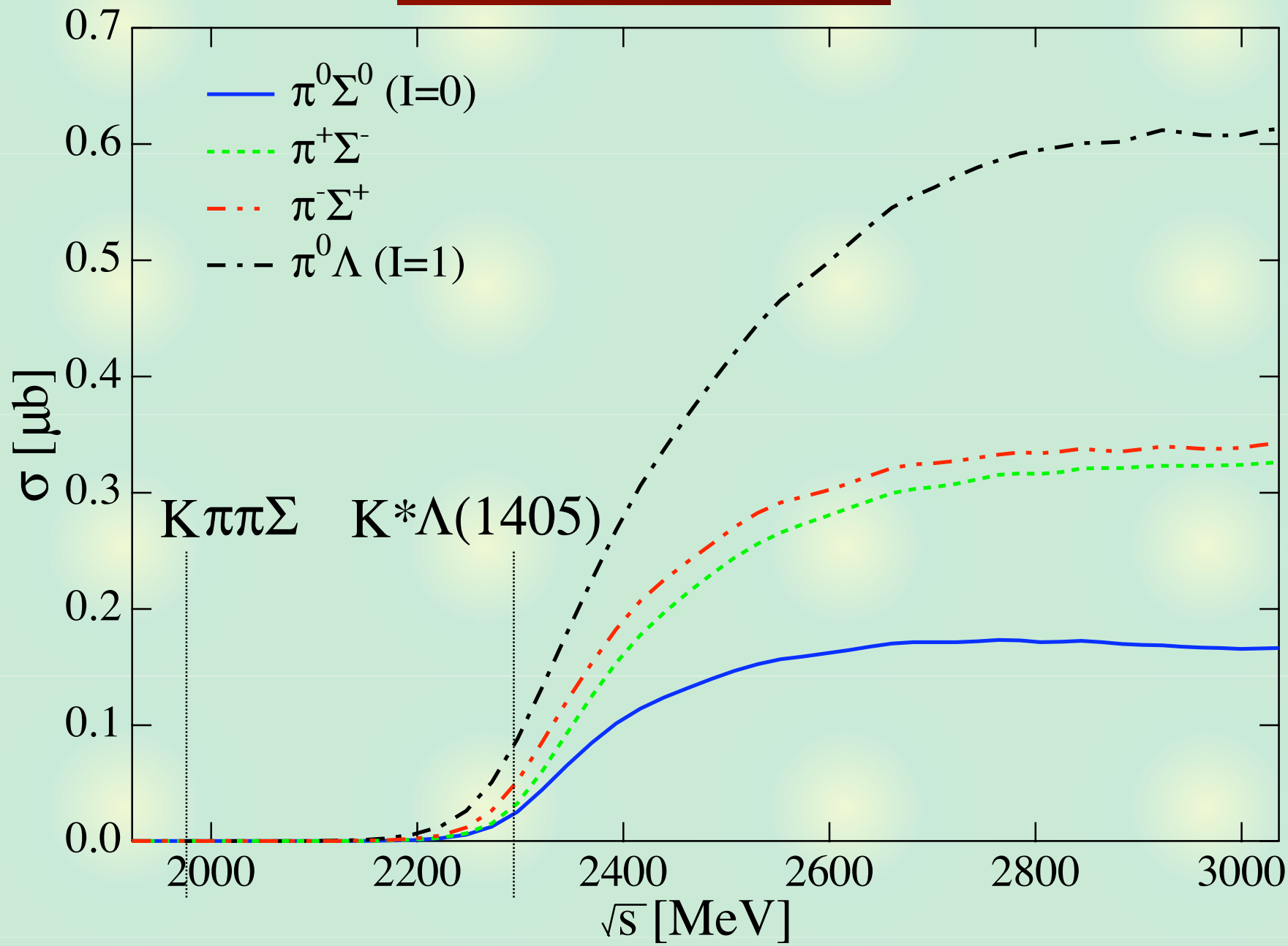
★ **$\Sigma(1385)$ MB coupling**

★
$$-it_{\Sigma^* i} = c_i \frac{12}{5} \frac{D + F}{2f} \mathbf{S} \cdot \mathbf{k}_i$$

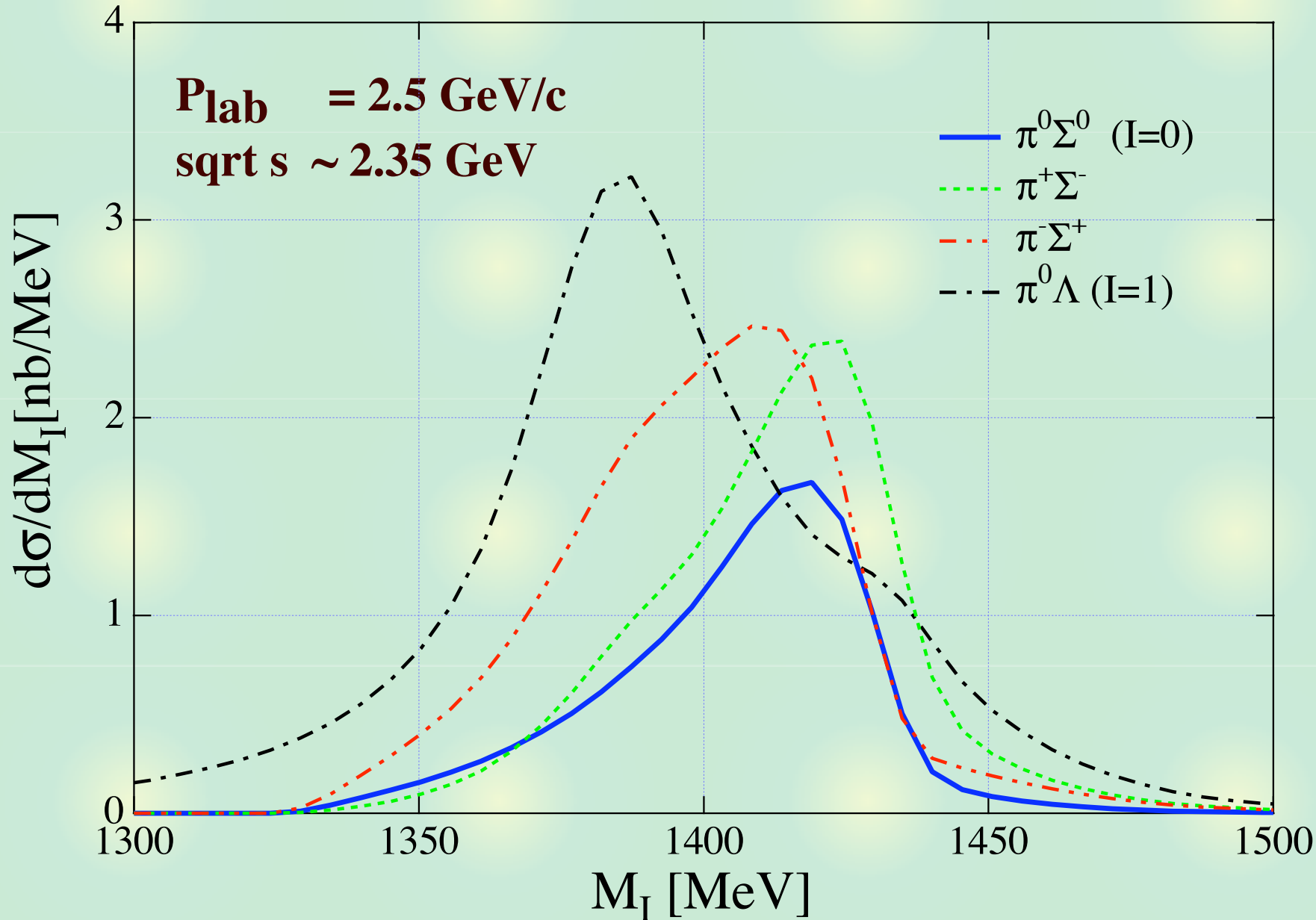
★ **form factor**

$$F_f(k_1) = \frac{\Lambda^2 - m_K^2}{\Lambda^2 - (k_1)^2}$$

Total cross sections



Invariant mass distributions



Isospin decomposition of $\pi\Sigma$ states

Since initial state is KN, we neglect the $l=2$.

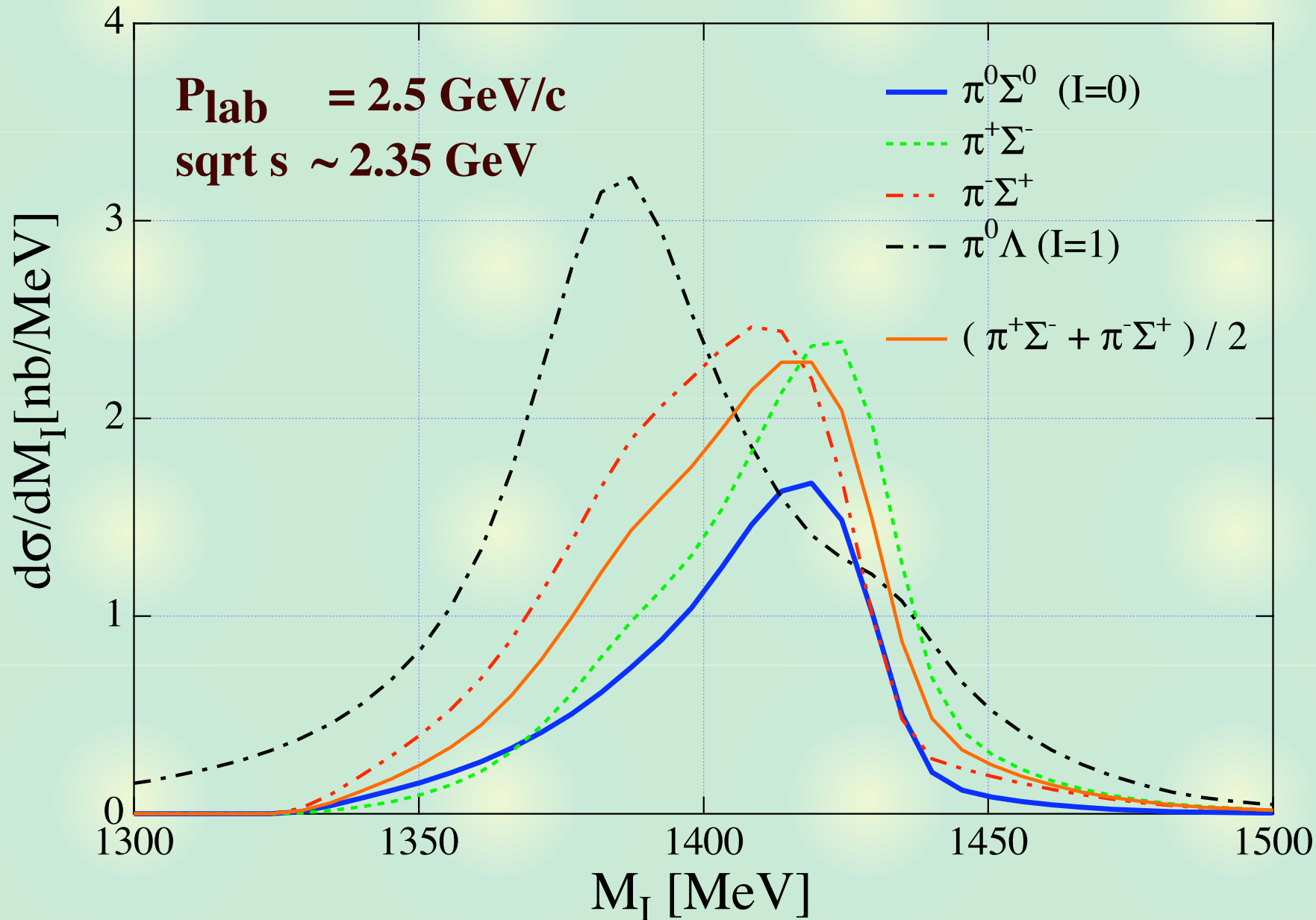
$$\frac{d\sigma(\pi^0\Sigma^0)}{dM_I} \propto \frac{1}{3} |T^{(0)}|^2$$

- **Pure $l=0$ amplitude**

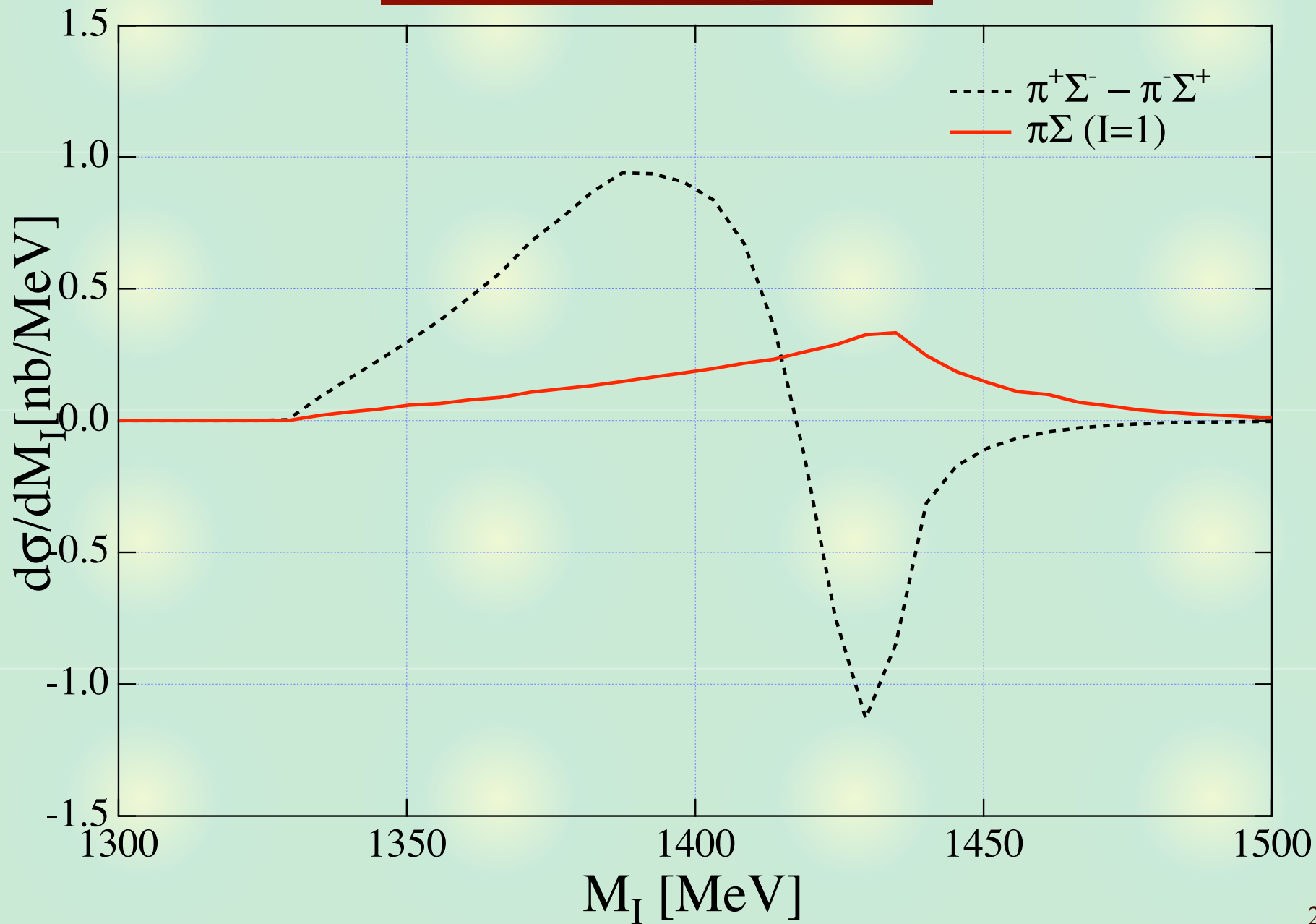
$$\frac{d\sigma(\pi^\pm\Sigma^\mp)}{dM_I} \propto \frac{1}{3} |T^{(0)}|^2 + \frac{1}{2} |T^{(1)}|^2 \pm \frac{2}{\sqrt{6}} \text{Re}(T^{(0)}T^{(1)*})$$

- **Difference among charged states**
 - > when summed up, this term vanishes
- **No p-wave contribution**
 - > $l=1$ s-wave amplitude

Invariant mass distributions 2



I=1, s-wave amplitude



Summary and conclusions 1

We study the **structure of $\Lambda(1405)$** using the chiral unitary model.


There are **two poles** of the scattering amplitude around nominal $\Lambda(1405)$.



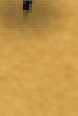
Pole 1 (1426–16i) : strongly couples to $\bar{K}N$ state

Pole 2 (1390–66i) : strongly couples to $\pi\Sigma$ state

By observing the **charged $\pi\Sigma$ states** in the $\gamma p \rightarrow K^* \Lambda(1405)$ reaction, it is possible to isolate the **higher energy pole**.

Summary and conclusions 2

 If we observe **neutral $\pi\Sigma$ state**, clear **$l=0$ distribution** is obtained.



 Combining three **$\pi\Sigma$ states**, we can also study the **s-wave $l=1$ amplitude**, where the existence of another pole is argued.

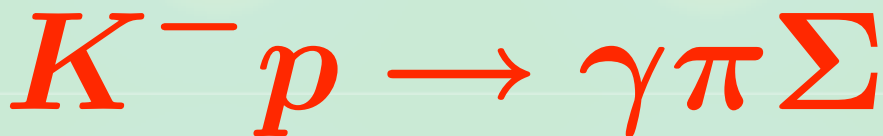
[T. H., A. Hosaka, E. Oset, M. J. Vicente Vacas, PLB593, 75 \(2004\)](#)

<http://www.rcnp.osaka-u.ac.jp/~hyodo/>

Appendix : other processes



J.C. Nacher, *et al.*, PLB445, 55



J.C. Nacher, *et al.*, PLB461, 299

