

第2回実証的原子核物理学 (Feb. 22th-23th, 2012 at RCNP)

高エネルギー重イオン散乱における 核反応ダイナミクスの分析

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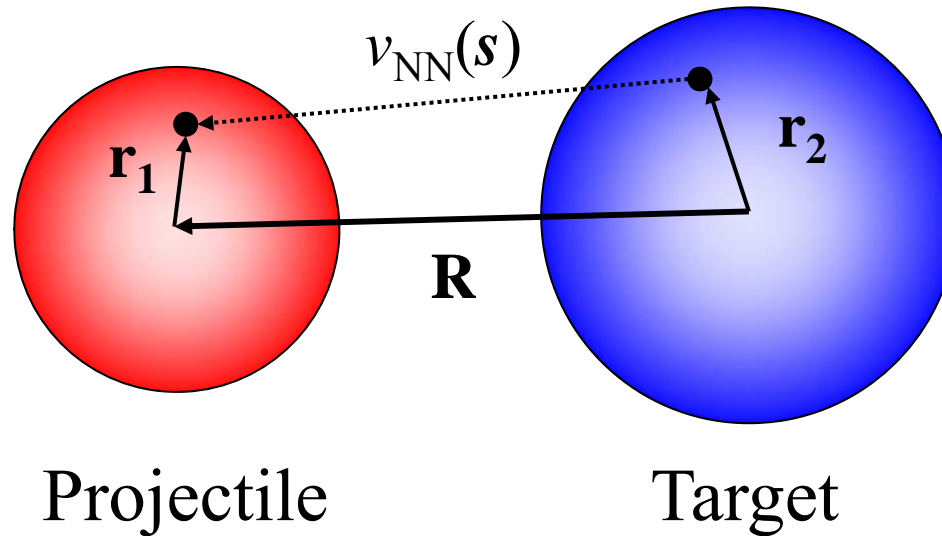
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Double-Folding Model (DFM)



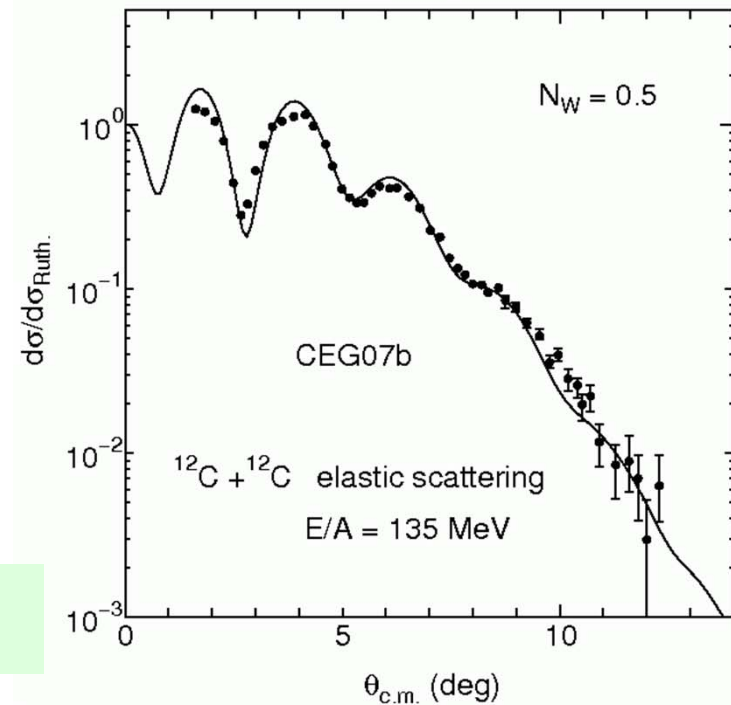
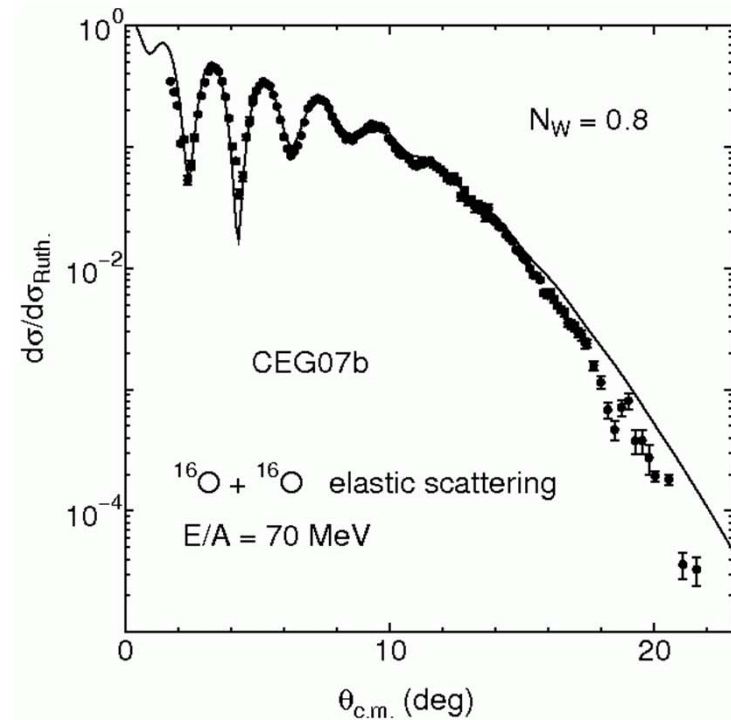
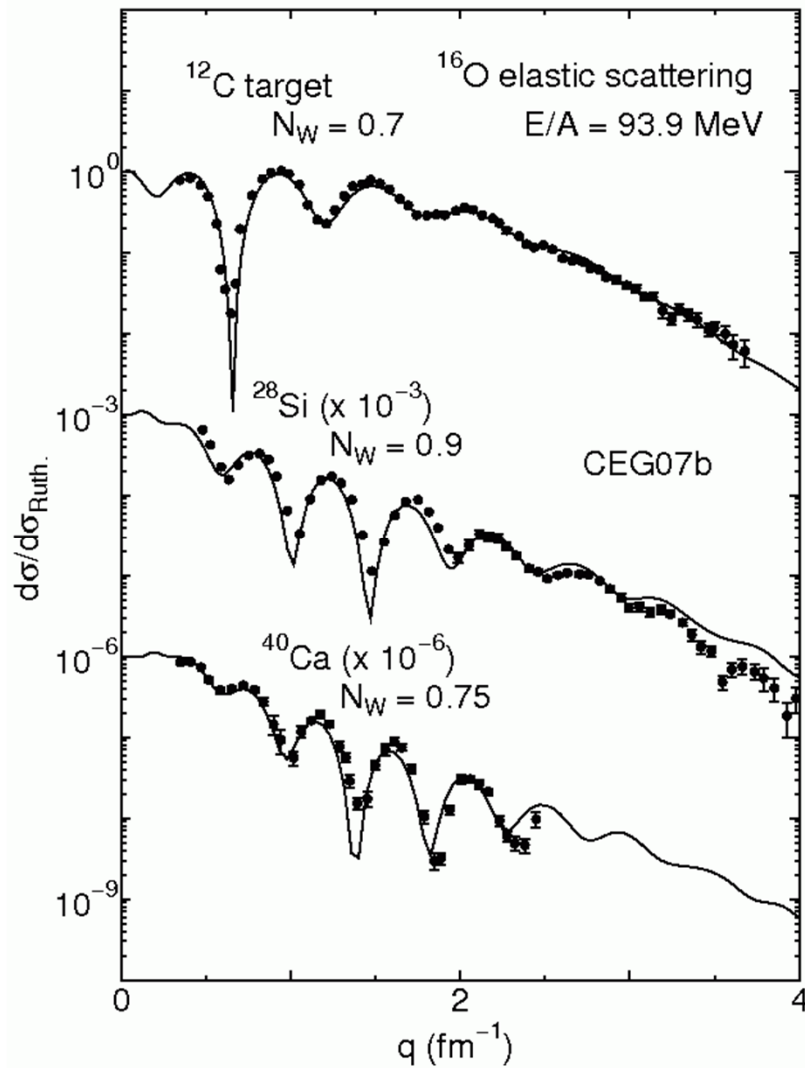
$$U_{DF}(\mathbf{R}) = \int \rho_1(\mathbf{r}_1) \rho_2(\mathbf{r}_2) v_{NN}(\mathbf{s}; \rho, E) d\mathbf{r}_1 d\mathbf{r}_2$$

nucleon density

complex G -matrix interaction
(CEG07)

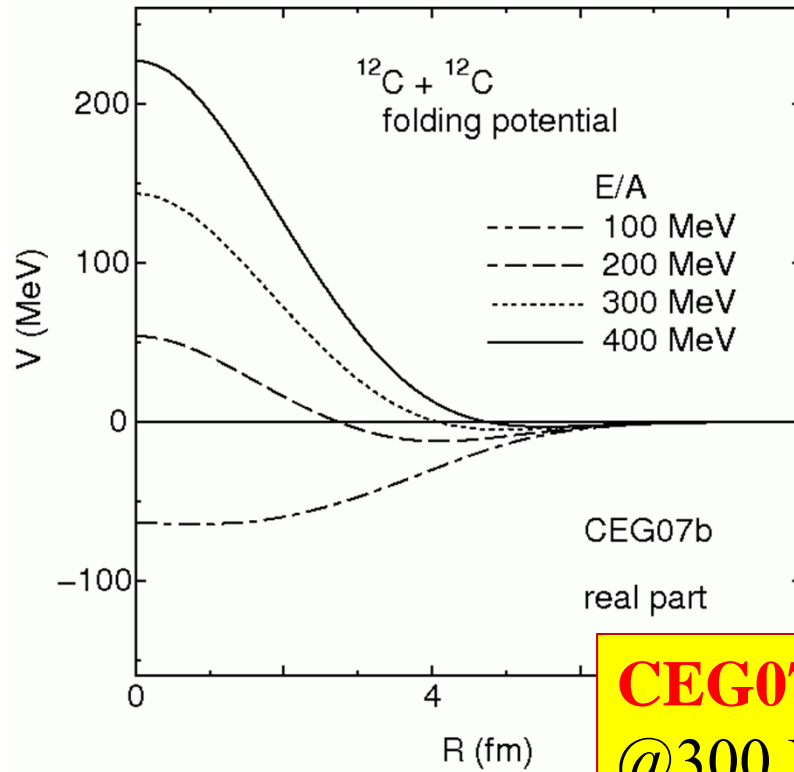
*T. Furumoto, Y. Sakuragi and Y. Yamamoto,
(Phys. Rev. C.79 (2009) 011601(R)), ibid. 80 (2009) 044614)*

Heavy-ion elastic scattering



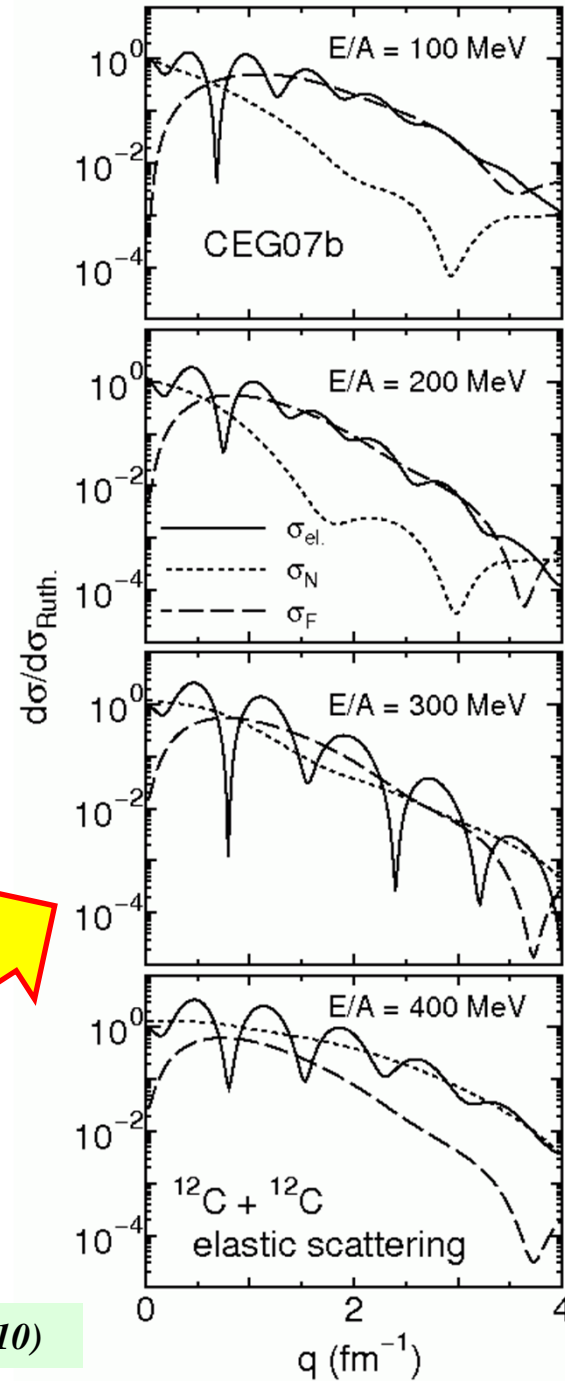
T. Furumoto, Y. Sakuragi and Y. Yamamoto,
(*Phys. Rev. C.79 (2009) 011601(R)*), *ibid. 80 (2009) 044614*)

Prediction of repulsive potential for Heavy-ion High-energy scattering



CEG07b
@300 MeV/u

The strong interference appears.



Microscopic Coupled Channel (MCC) with CEG07

Coupled Channel equation

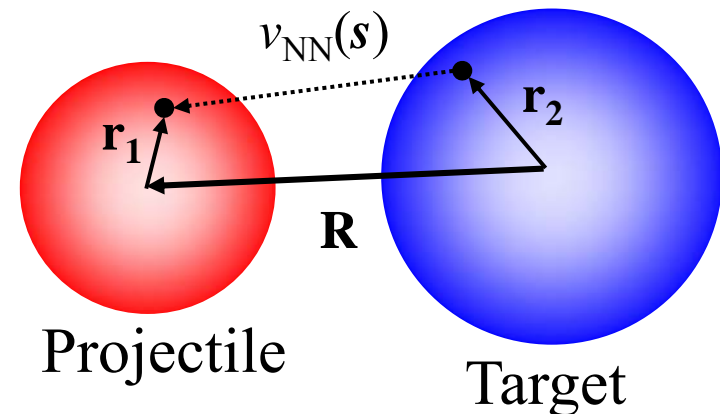
$$\left[T_R + U_{\alpha\alpha}(\mathbf{R}) - E_\alpha \right] \chi_\alpha(\mathbf{R}) = - \sum_{\beta \neq \alpha}^N U_{\alpha\beta}(\mathbf{R}) \chi_\beta(\mathbf{R})$$

The diagonal and coupling potentials are derived from microscopic view point.

$$U_{\alpha\beta}(\mathbf{R}) = \int \underbrace{\rho_{ik}^{(P)}(\mathbf{r}_1)}_{\text{transition density}} \underbrace{\rho_{jl}^{(T)}(\mathbf{r}_2)}_{\text{CEG07}} v_{NN}(\mathbf{s}; \rho, E) d\mathbf{r}_1 d\mathbf{r}_2$$

Transition density

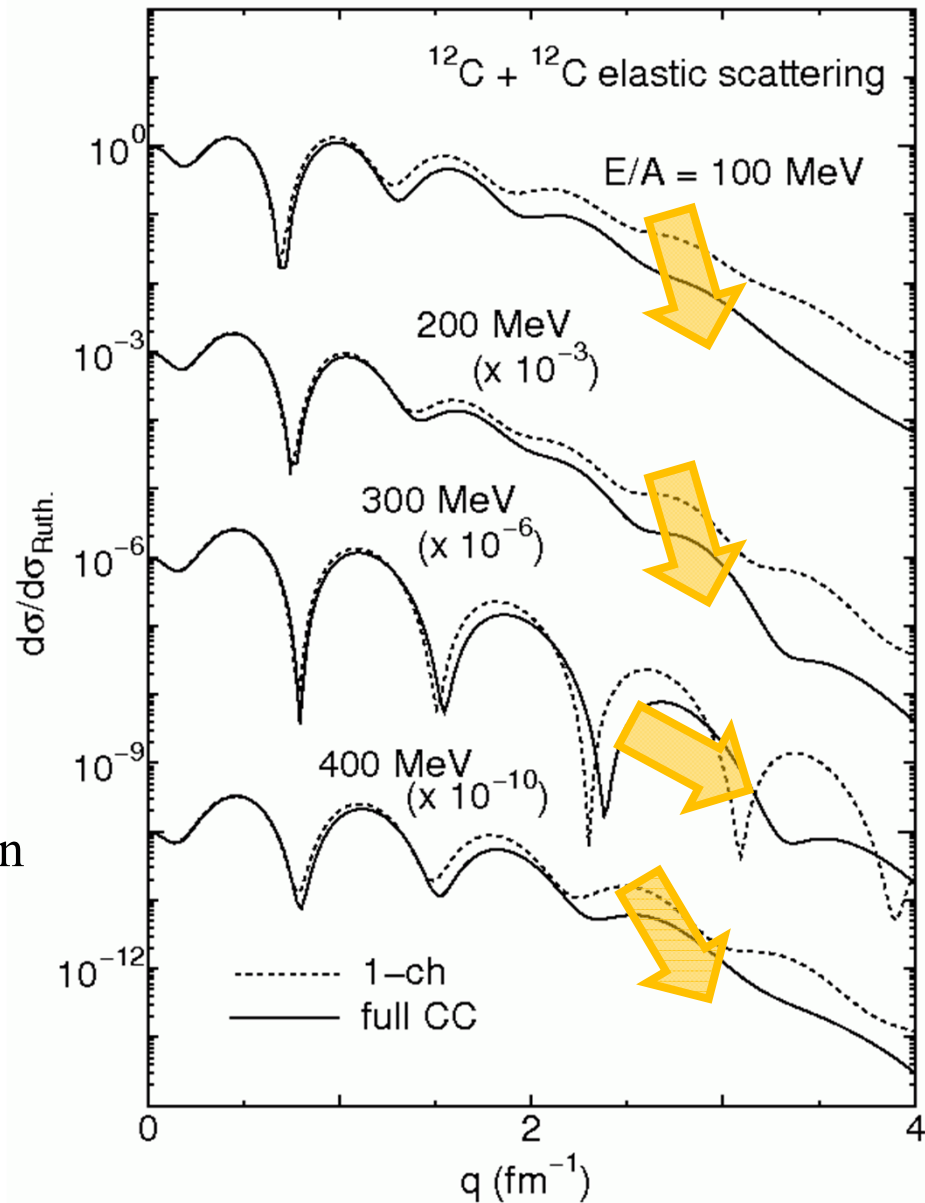
$$\underline{\rho_{ik}}(\mathbf{r}) = \langle \varphi_i(\xi) | \sum_i \delta(\mathbf{r}_i - \mathbf{r}) | \varphi_k(\xi) \rangle$$



*Dynamic coupling effect
on
high-energy heavy-ion
elastic scatterings*

The effect is clearly seen!

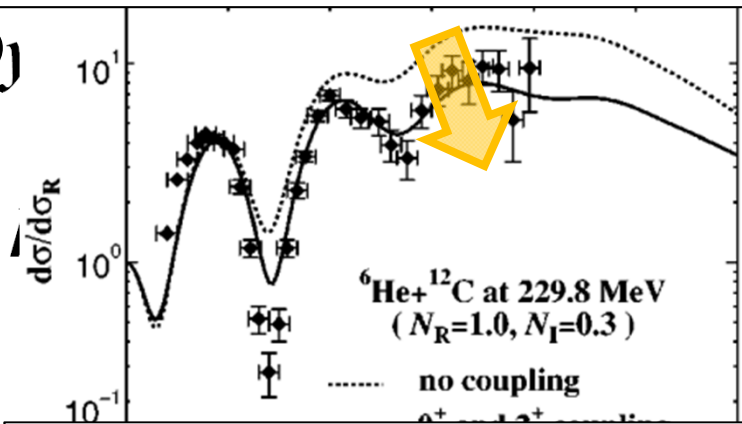
1. Backward cross section comes down
2. Diffraction pattern goes backward



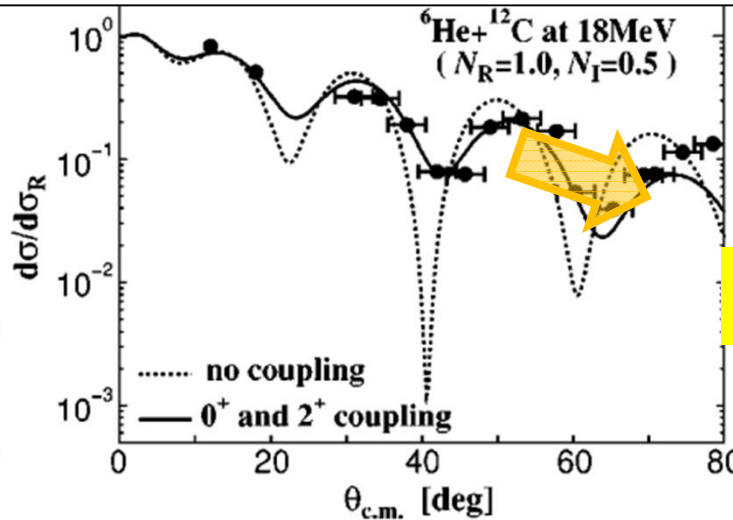
T. Furumoto and Y. Sakuragi, in preparation

1. Backward cross section comes down

D_j

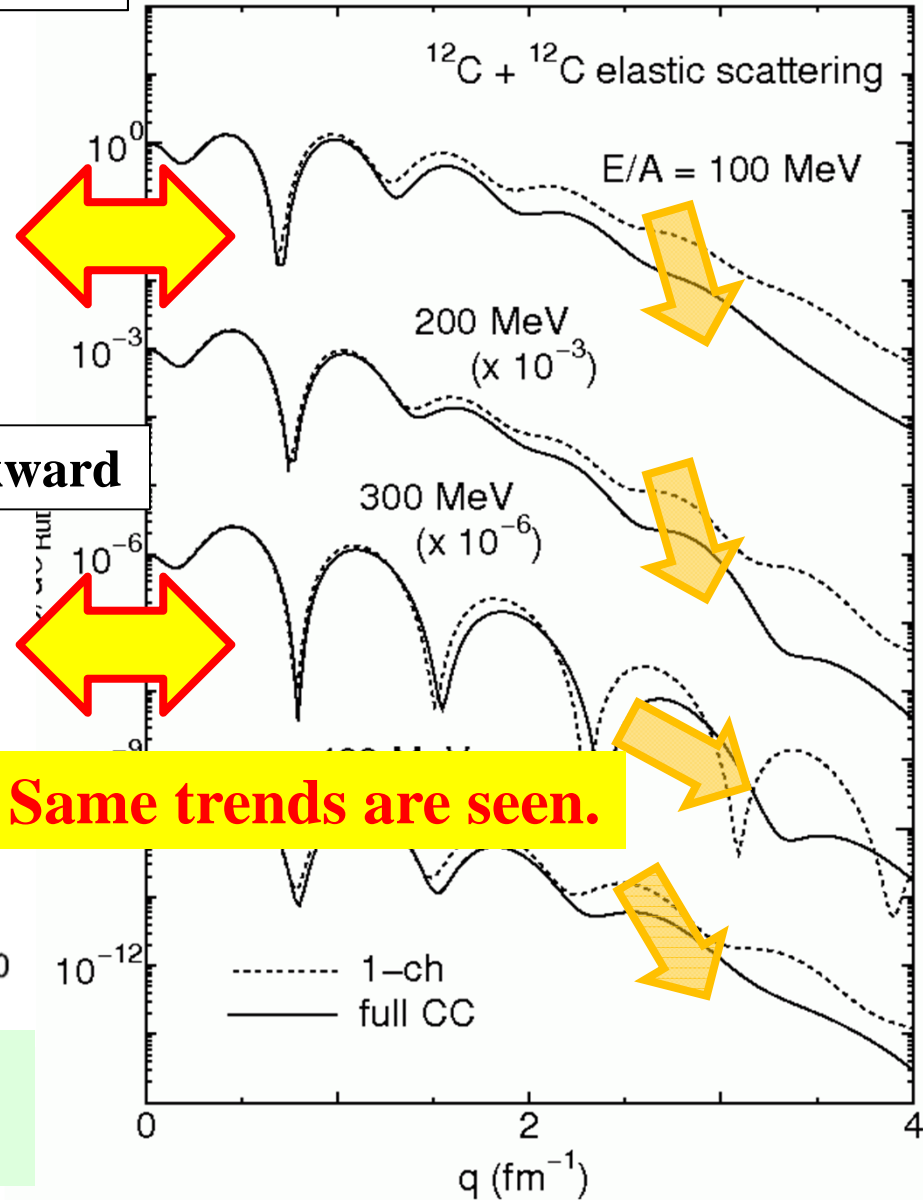


2. Diffraction pattern goes backward



1. E

2. E




Same trends are seen.

*T. Matsumoto, E. Hiyama, K. Ogata, Y. Iseri,
M. Kamimura, S. Chiba, and M. Yahiro,
(Phys. Rev. C.70 (2004) 061601(R))*

T. Furumoto and Y. Sakuragi, in preparation

Dynamical polarization potential (DPP)

Coupled Channel equation



$$\left[T_R + U_{\alpha\alpha}(\mathbf{R}) - E_\alpha \right] \chi_\alpha(\mathbf{R}) = - \sum_{\beta \neq \alpha}^N U_{\alpha\beta}(\mathbf{R}) \chi_\beta(\mathbf{R})$$
$$\left[T_R + U_{\alpha\alpha}(\mathbf{R}) + \sum_{\beta \neq \alpha}^N U_{\alpha\beta}(\mathbf{R}) \left(\chi_\beta(\mathbf{R}) / \chi_\alpha(\mathbf{R}) \right) - E_\alpha \right] \chi_\alpha(\mathbf{R}) = 0$$

Coupling effect

Dynamical polarization potential (DPP)

$$\Delta U_{DPP}(\mathbf{R}) = \sum_{\beta \neq \alpha}^N U_{\alpha\beta}(\mathbf{R}) \left(\chi_\beta(\mathbf{R}) / \chi_\alpha(\mathbf{R}) \right)$$

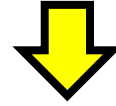
By partial wave expansion


$$\Delta U_{DPP}^{(J)}(R) = \sum_{\beta \neq \alpha}^N U_{\alpha\beta}(R) \left(\chi_\beta^{(J)}(R) / \chi_\alpha^{(J)}(R) \right)$$

Coupled Channel equation

$$\left[T_R + U_{\alpha\alpha}(\mathbf{R}) + \sum_{\beta \neq \alpha} U_{\alpha\beta}(\mathbf{R}) \left(\chi_{\beta}(\mathbf{R}) / \chi_{\alpha}(\mathbf{R}) \right) - E_{\alpha} \right] \chi_{\alpha}(\mathbf{R}) = 0$$

Dynamical polarization potential



$$\begin{aligned} \Delta U_{DPP}(\mathbf{R}) &= \sum_{\beta \neq \alpha} U_{\alpha\beta}(\mathbf{R}) \left(\chi_{\beta}(\mathbf{R}) / \chi_{\alpha}(\mathbf{R}) \right) \\ &= \sum_{\beta \neq \alpha} U_{\alpha\beta}(\mathbf{R}) \int G_{\beta}^{(+)}(\mathbf{R}, \mathbf{R}') U_{\beta\alpha}(\mathbf{R}') \chi_{\alpha}(\mathbf{R}') d\mathbf{R}' / \chi_{\alpha}(\mathbf{R}) \\ &\quad \left(G_{\beta}^{(+)} = \frac{1}{E_{\beta} - T_{\beta} - U_{\beta\beta} + i\varepsilon} \right) \end{aligned}$$

Here, we assume that $U_{\alpha\beta}(\mathbf{R}) = (N_R + iN_I)V_{\alpha\beta}(\mathbf{R})$

$$\Delta U_{DPP}(\mathbf{R}) = (N_R + iN_I)^2 \sum_{\beta \neq \alpha} V_{\alpha\beta}(\mathbf{R}) \int G_{\beta}^{(+)}(\mathbf{R}, \mathbf{R}') V_{\beta\alpha}(\mathbf{R}') \chi_{\alpha}(\mathbf{R}') d\mathbf{R}' / \chi_{\alpha}(\mathbf{R})$$

$$\begin{aligned}
\Delta U_{DPP}(\mathbf{R}) &= (N_R + iN_I)^2 \sum_{\beta \neq \alpha} V_{\alpha\beta}(\mathbf{R}) \int G_{\beta}^{(+)}(\mathbf{R}, \mathbf{R}') V_{\beta\alpha}(\mathbf{R}') \chi_{\alpha}(\mathbf{R}') d\mathbf{R}' / \chi_{\alpha}(\mathbf{R}) \\
&= (N_R + iN_I)^2 (\Delta u + i\Delta w) \\
&= \underbrace{(N_R^2 - N_I^2) \Delta u - 2N_R N_I \Delta w}_{\text{Real part}} + i \underbrace{\{2N_R N_I \Delta u + (N_R^2 - N_I^2) \Delta w\}}_{\text{Imaginary part}}
\end{aligned}$$

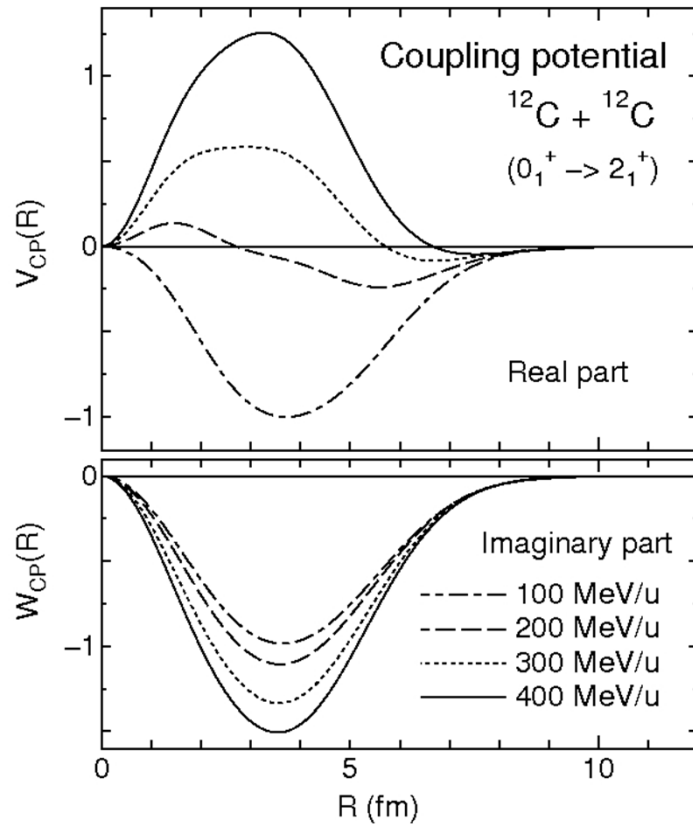
$$\begin{aligned}
\Delta u + i\Delta w &= \sum_{\beta \neq \alpha} V_{\alpha\beta}(\mathbf{R}) \int G_{\beta}^{(+)}(\mathbf{R}, \mathbf{R}') V_{\beta\alpha}(\mathbf{R}') \chi_{\alpha}(\mathbf{R}') d\mathbf{R}' / \chi_{\alpha}(\mathbf{R}) \\
&\approx -\frac{ik}{8\pi E_{c.m.}} \sum_{\beta \neq \alpha} \sum_{\lambda} f_{\alpha\beta}^{(\lambda)}(R) \int_0^{\infty} dq q j_{\lambda}(qR) \int_0^{\infty} dx x^2 f_{\beta\alpha}^{(\lambda)}(x) j_{\lambda}(qx)
\end{aligned}$$

K.-I. Kubo and P.E. Hodgson, Nucl. Phys. A366 (1981) 320

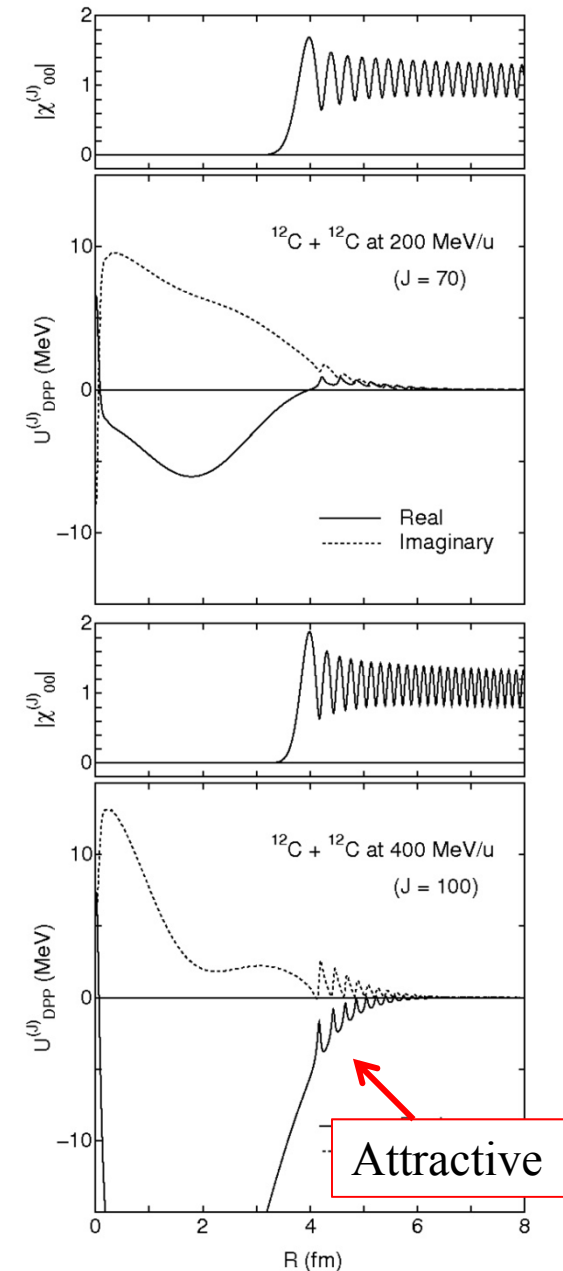
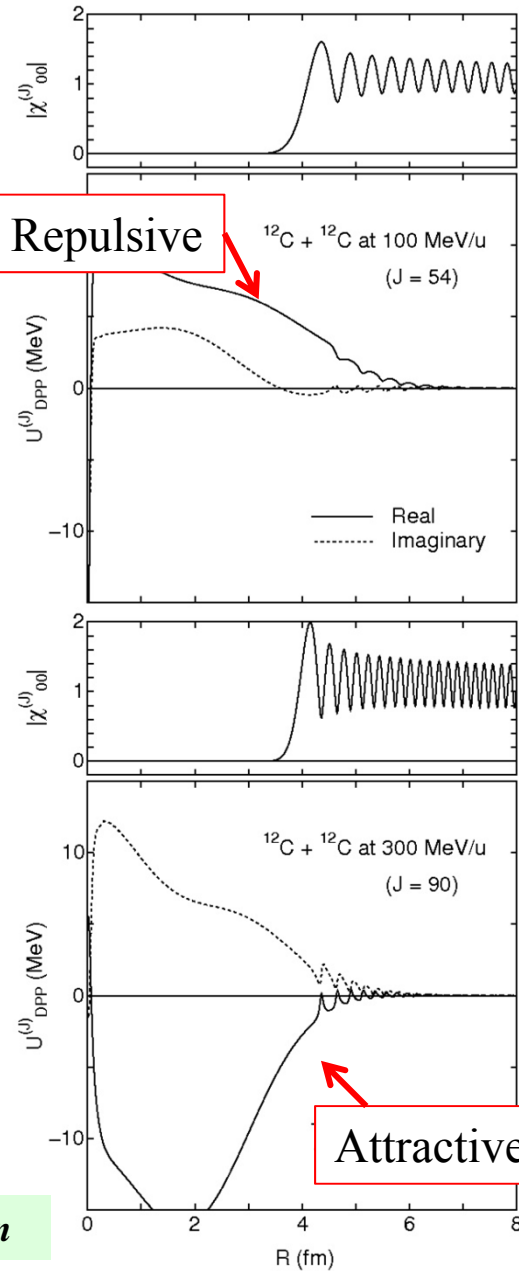
$$\text{If } f_{\beta\alpha}^{(\lambda)} \text{ is real, } \begin{cases} \Delta u = 0 \\ \Delta w < 0 \end{cases}$$

Dynamical polarization potential (DPP)

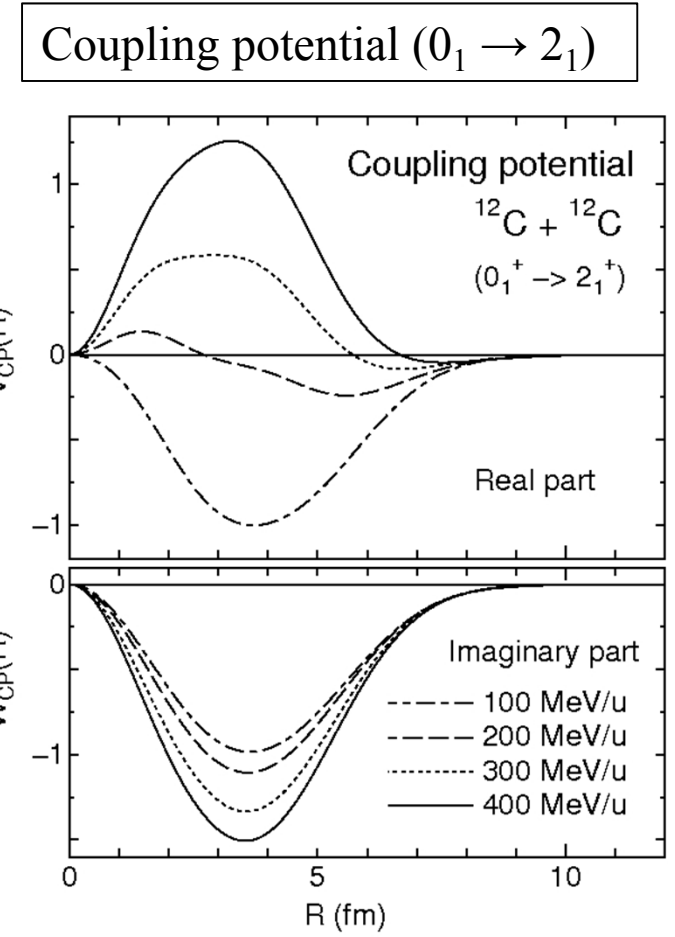
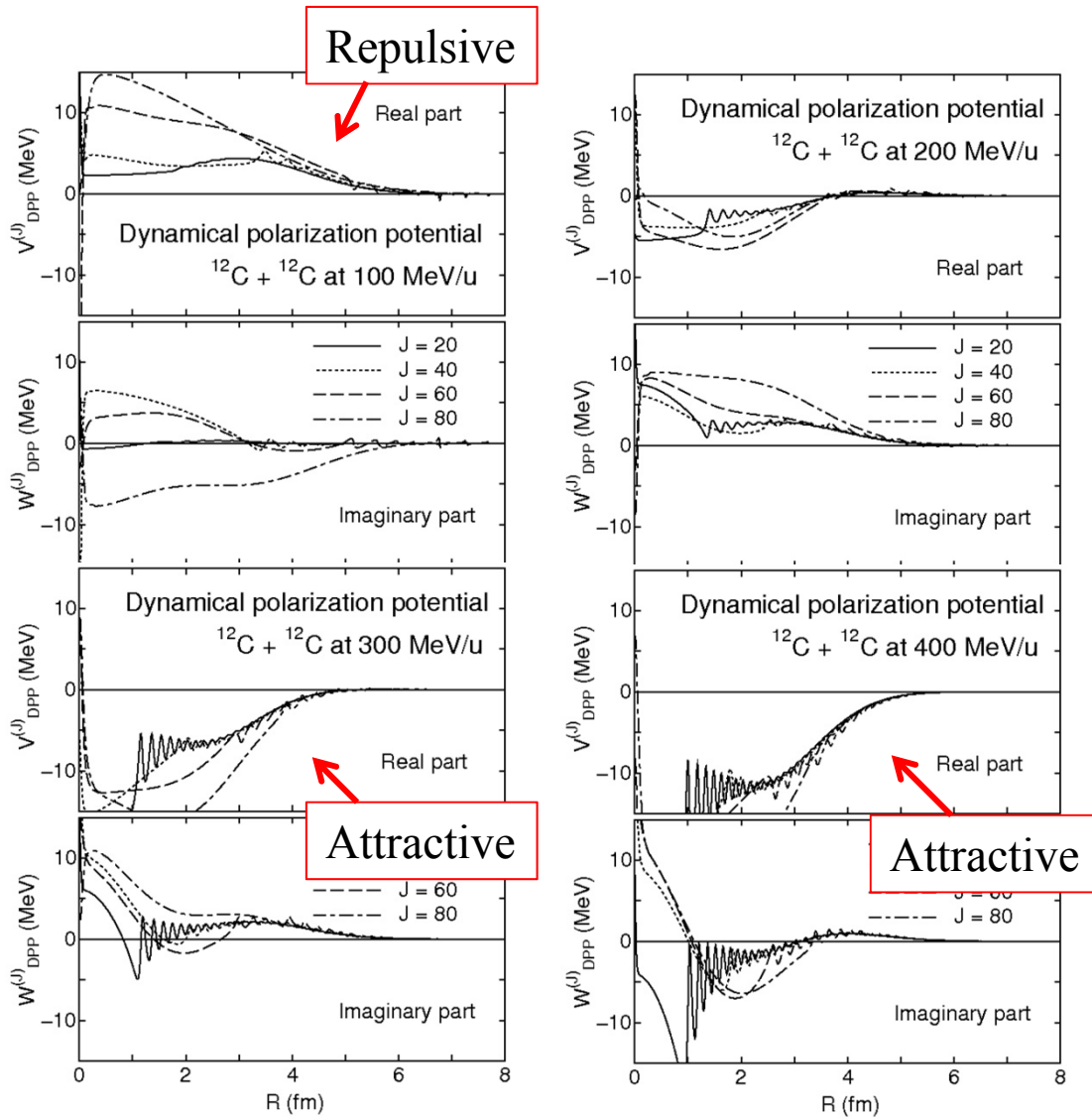
Coupling potential ($0_1 \rightarrow 2_1$)



Repulsive



Dynamical polarization potential (DPP) *for high-energy heavy-ion systems*



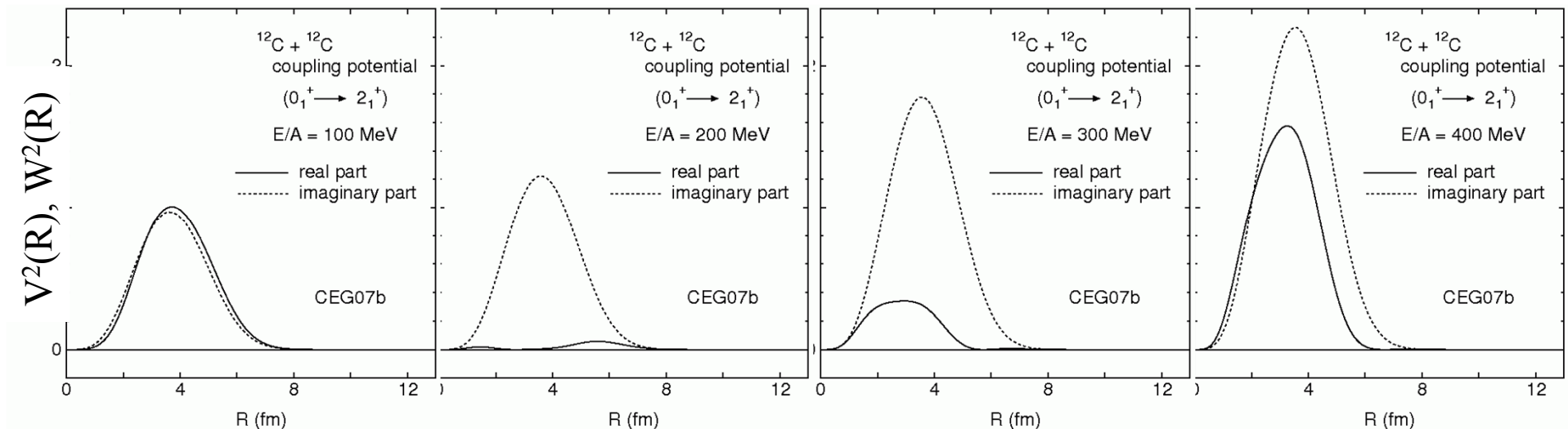
Role of imaginary part of coupling potential

- Complex coupling gives the large dynamical coupling effect.
- Coupling potential is derived as

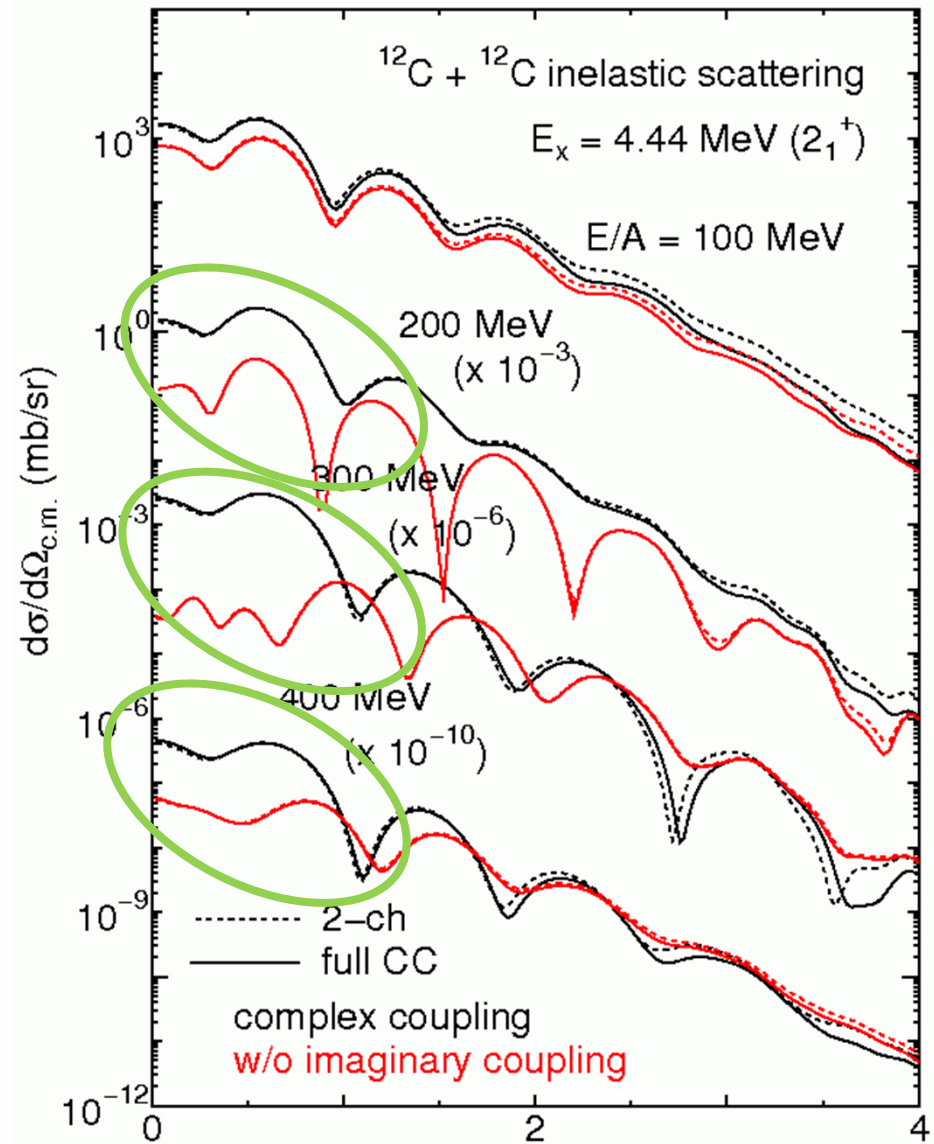
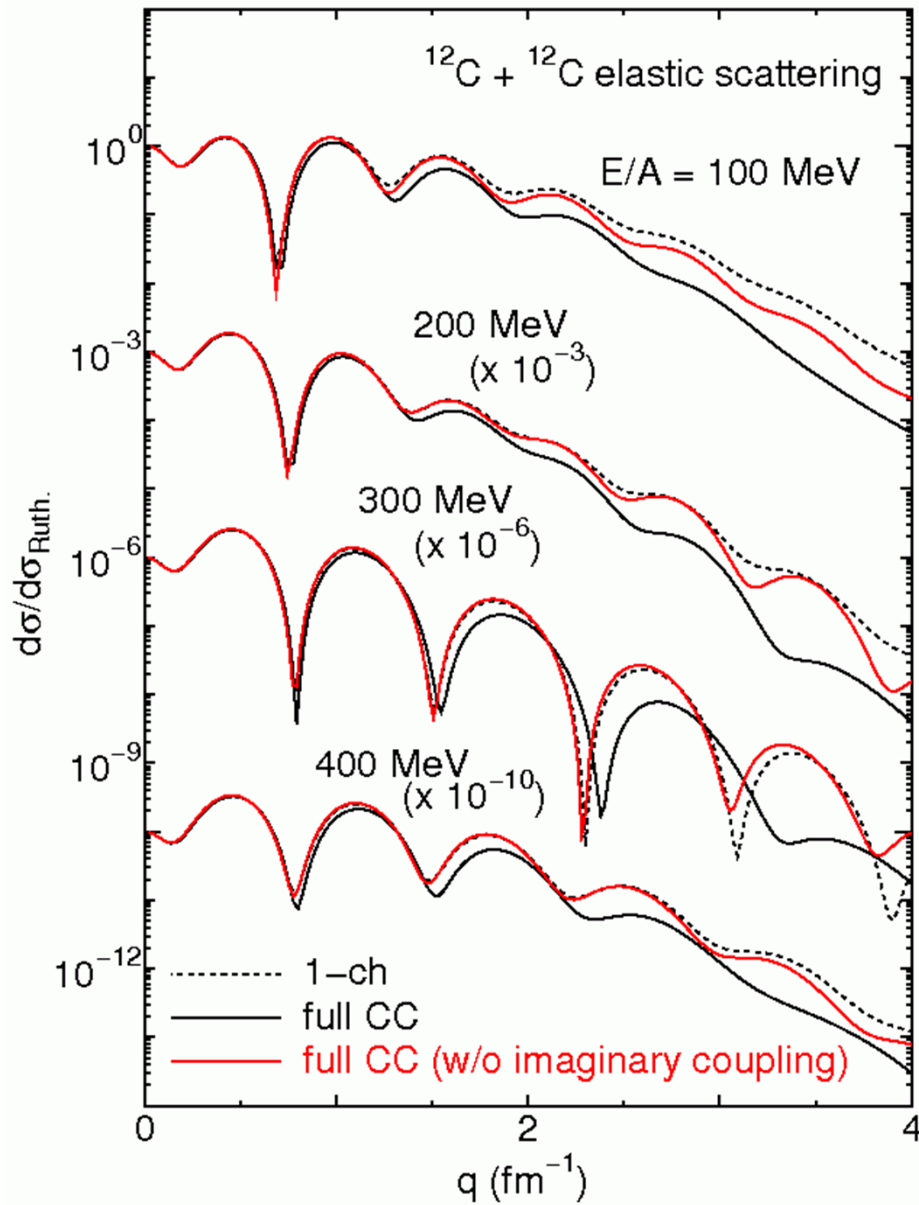
$$U_{\alpha\beta}(\mathbf{R}) = \int \rho_{ik}^{(P)}(\mathbf{r}_1) \rho_{jl}^{(T)}(\mathbf{r}_2) v_{NN}(\mathbf{s}; \rho, E) d\mathbf{r}_1 d\mathbf{r}_2$$

transition density **CEG07**

At high energies, the imaginary part of coupling potential becomes larger than the real part

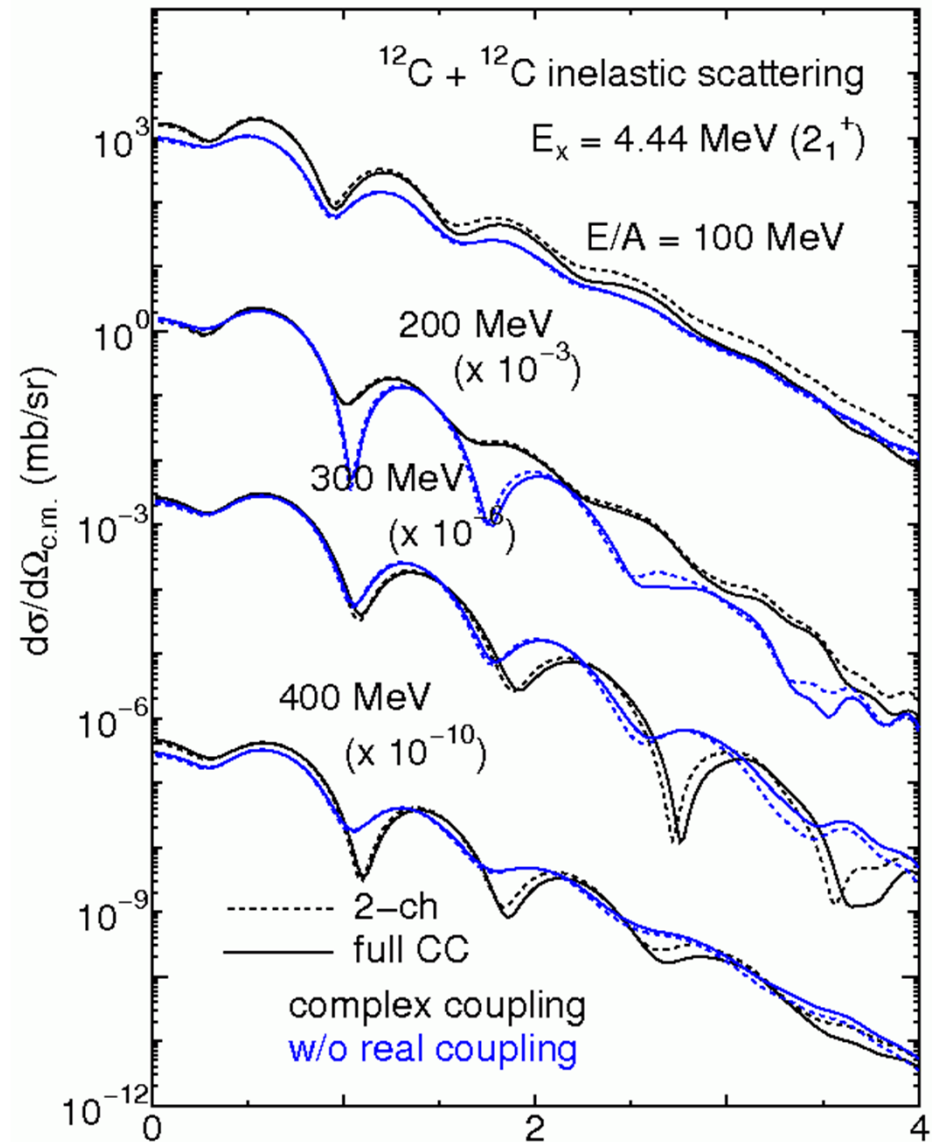
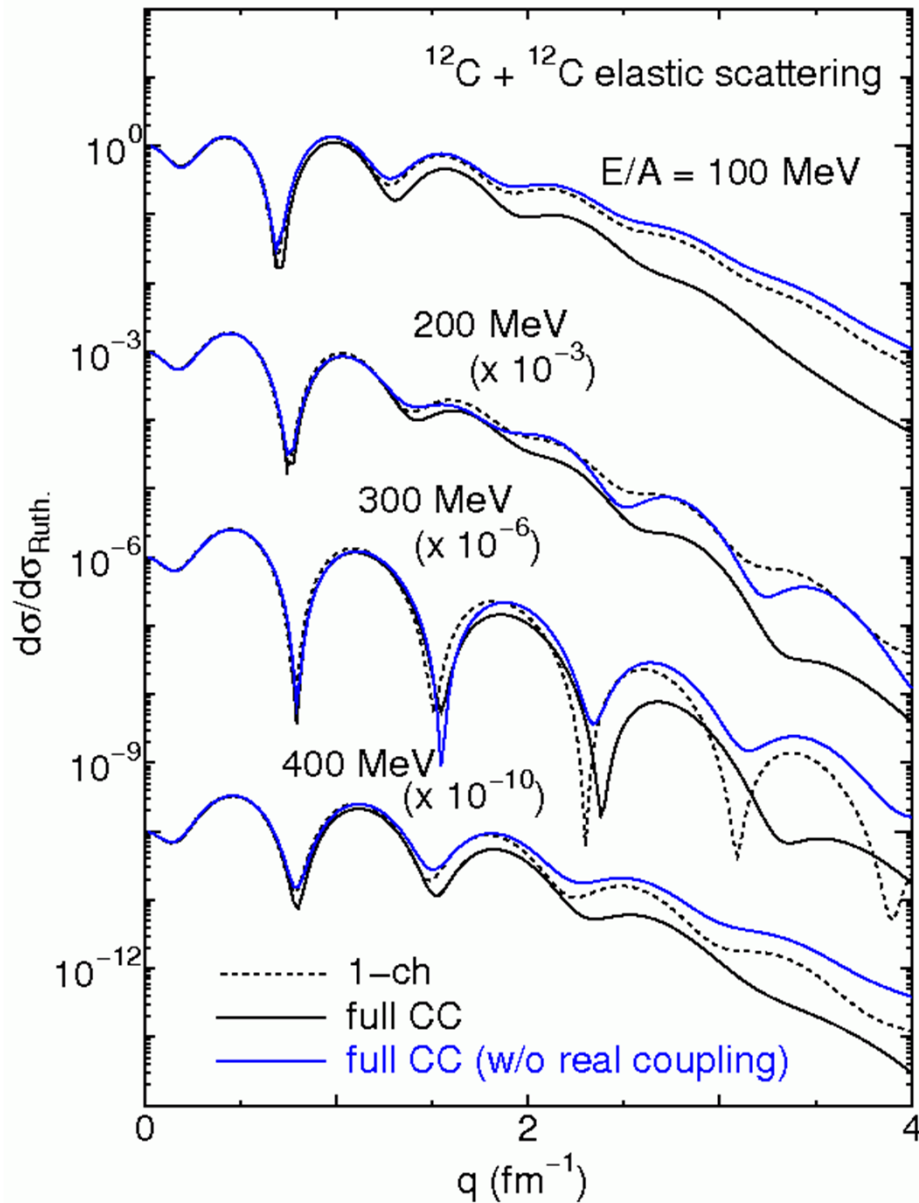


Effect of imaginary part of coupling potential



T. Furumoto and Y. Sakuragi, in preparation

Effect of real part of coupling potential



T. Furumoto and Y. Sakuragi, in preparation

