

テンソル最適化シェルモデルによる s-pシェル核構造

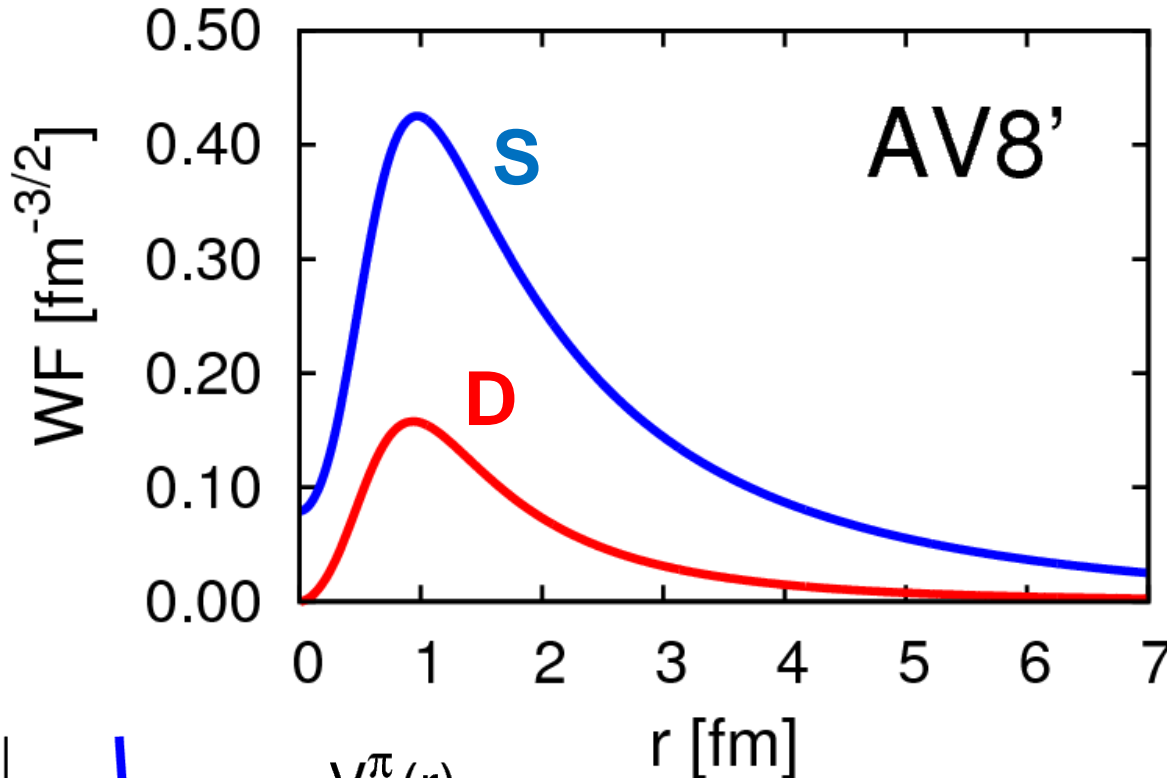
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大阪工業大学



Purpose & Outline

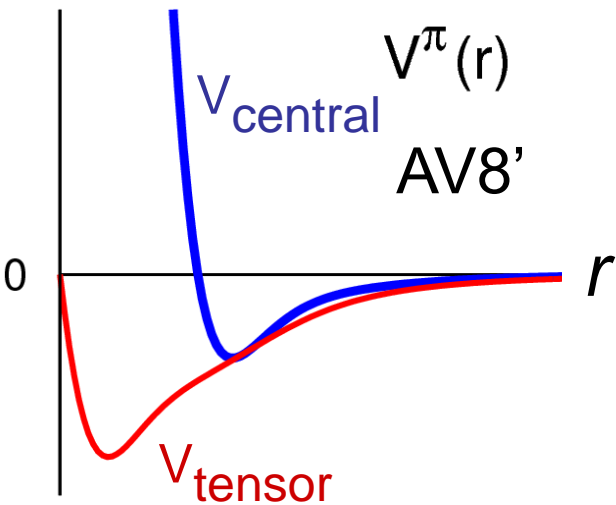
- **Role of V_{tensor}** in the nuclear structure **by describing strong tensor correlation explicitly.**
- Tensor Optimized Shell Model (**TOSM**) to describe tensor correlation.
- Unitary Correlation Operator Method (**UCOM**) to describe short-range correlation.
- **TOSM+UCOM** to He & Li isotopes with V_{bare}
- Halo formation in ^{11}Li
 - Coexistence of tensor and pairing correlations

Deuteron properties & tensor force



Energy	-2.24 MeV
Kinetic	19.88
Central	-4.46
Tensor	-16.64
LS	-1.02
P(L=2)	5.77%
Radius	1.96 fm

$R_m(s) = 2.00$ fm
 $R_m(d) = 1.22$ fm



d-wave is
“spatially compact”
 (high momentum)

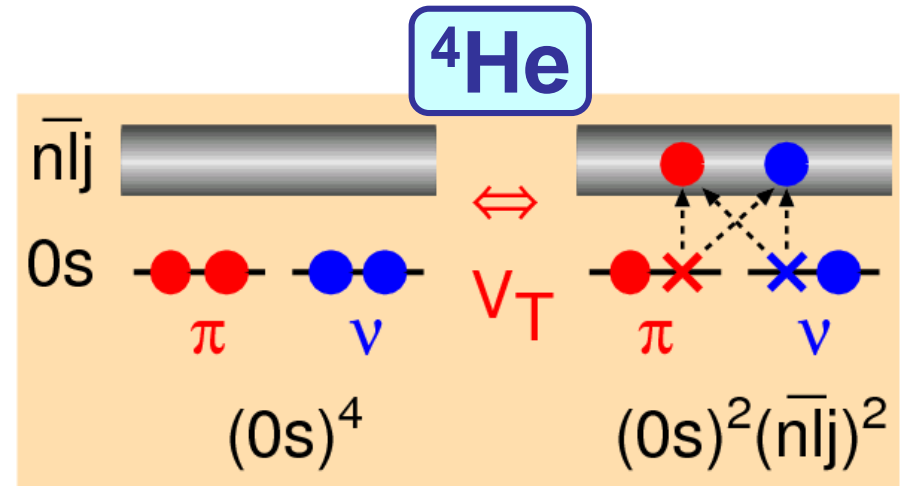
Tensor-optimized shell model (TOSM)

TM, Sugimoto, Kato, Toki, Ikeda PTP117(2007)257

- Configuration mixing within **2p2h excitations** with high- L orbits.

TM et al., PTP113(2005)

TM et al., PTP117(2007)



- Length parameters such as b_{0s} , b_{0p} , ... are optimized **independently**, or **superposed by many Gaussian bases**.
 - **Spatial shrinkage** of **D-wave** as seen in deuteron
 - HF by Sugimoto et al.(NPA740) / Akaishi (NPA738)
 - RMF by Ogawa et al.(PRC73), AMD by Dote et al.(PTP115)
- Satisfy few-body results with Minnesota central force (${}^{4,6}\text{He}_4$)

Hamiltonian and variational equations in TOSM

$$H = \sum_{i=1}^A t_i - T_G + \sum_{i<j}^A v_{ij},$$

(0p0h+1p1h+2p2h)

$$\Phi(A) = \sum_k C_k \cdot \psi_k(A)$$

$\psi_k(A)$: shell model type configuration with mass number A

Particle state: Gaussian expansion for each orbit

$$\varphi_{lj}^n(\mathbf{r}) = \sum_{m=1}^N C_{lj,m}^n \cdot \phi_{lj,m}(\mathbf{r}) \quad \phi_{lj,m}(\mathbf{r}) = N_l(b_{lj,m}) \cdot r^l e^{-\left(r/b_{lj,m}\right)^2} \left[Y_l(\hat{\mathbf{r}}), \chi_{1/2}^\sigma \right]_j$$

$$\langle \varphi_{lj}^n | \varphi_{lj}^{n'} \rangle = \delta_{n,n'}$$

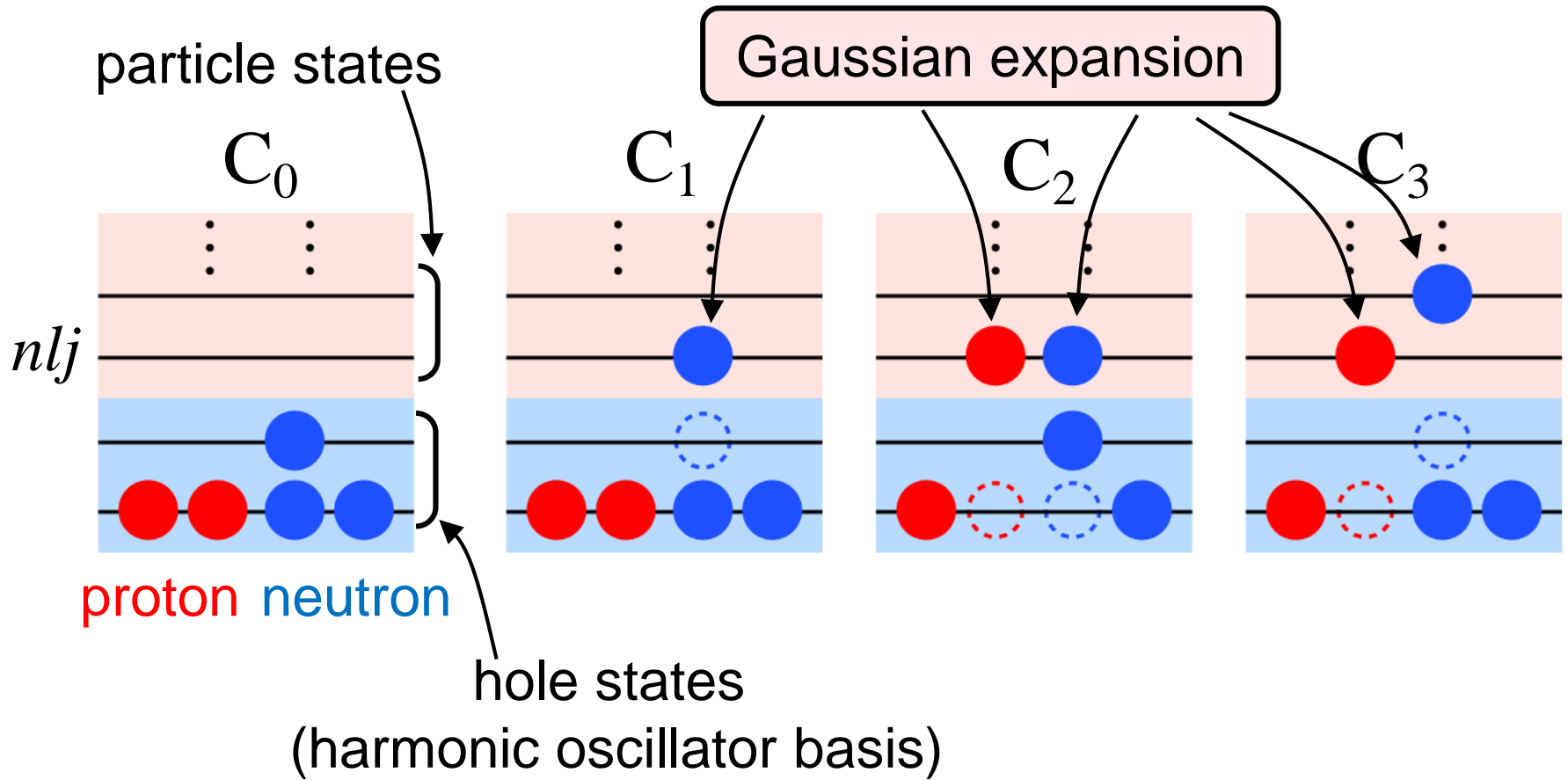
Gaussian basis function

$$\frac{\partial \langle H - E \rangle}{\partial C_k} = 0, \quad \frac{\partial \langle H - E \rangle}{\partial b_{lj,m}} = 0$$

TOSM code : p -shell region

c.m. excitation is excluded by Lawson's method

Configurations in TOSM



Application to Hypernuclei by Umeya (NIT)
to investigate ΛN - ΣN coupling

Unitary Correlation Operator Method

(short-range part)

$$\Psi_{\text{corr.}} = \mathbf{C} \cdot \Phi_{\text{uncorr.}}$$

TOSM

short-range correlator

$$\mathbf{C}^\dagger = \mathbf{C}^{-1} \quad (\text{Unitary trans.})$$

$$H\Psi = E\Psi \rightarrow \mathbf{C}^\dagger H\mathbf{C}\Phi \equiv H\Phi = E\Phi$$

Bare Hamiltonian

Shift operator depending on the relative distance

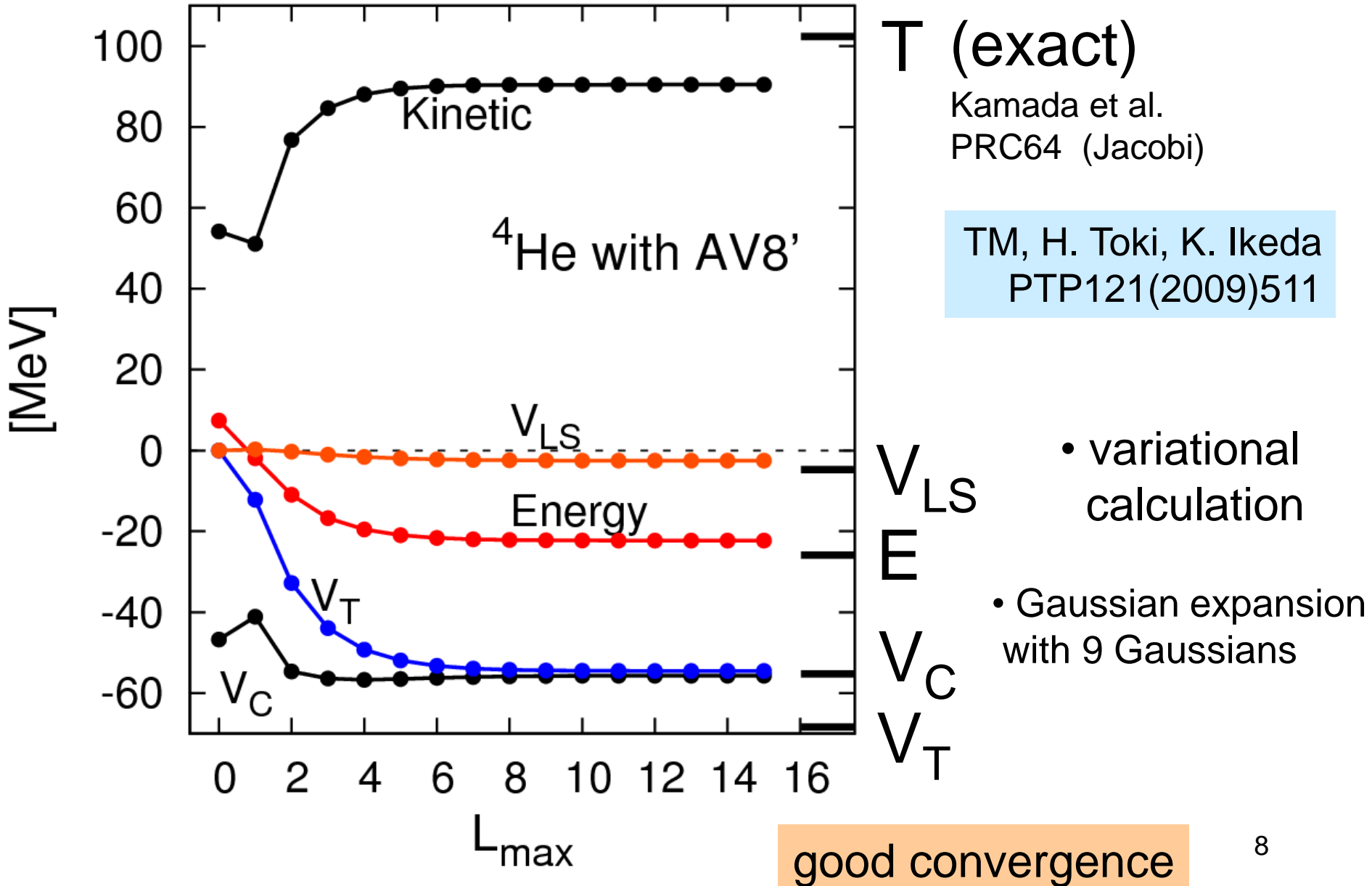
$$\mathbf{C} = \exp\left(-i \sum_{i < j} g_{ij}\right), \quad g_{ij} = \frac{1}{2} \left\{ \underline{p_r s(r_{ij})} + \underline{s(r_{ij}) p_r} \right\} \quad \vec{p} = \vec{p}_r + \vec{p}_\Omega$$

Amount of shift, variationally determined.

$$\mathbf{C}^\dagger r \mathbf{C} \simeq r + s(r) + \frac{1}{2} s(r) s'(r) \dots$$

2-body cluster expansion

^4He in TOSM + S-wave UCOM

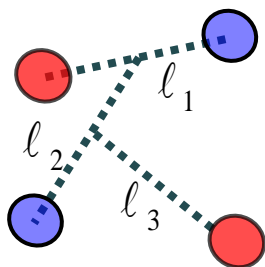


Tensor Optimized Few-body Model

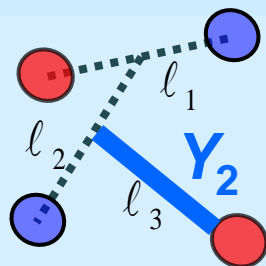
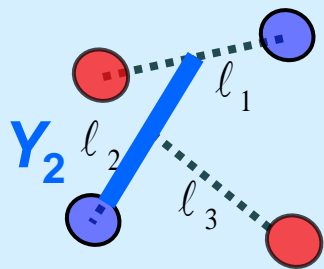
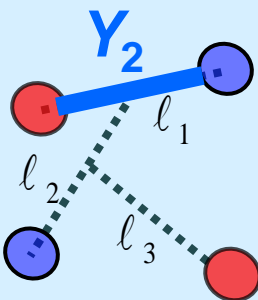
堀井ら
(RCNP)

- Same as TOSM concept
- Correlated Gaussian basis + Global vector used in SVM

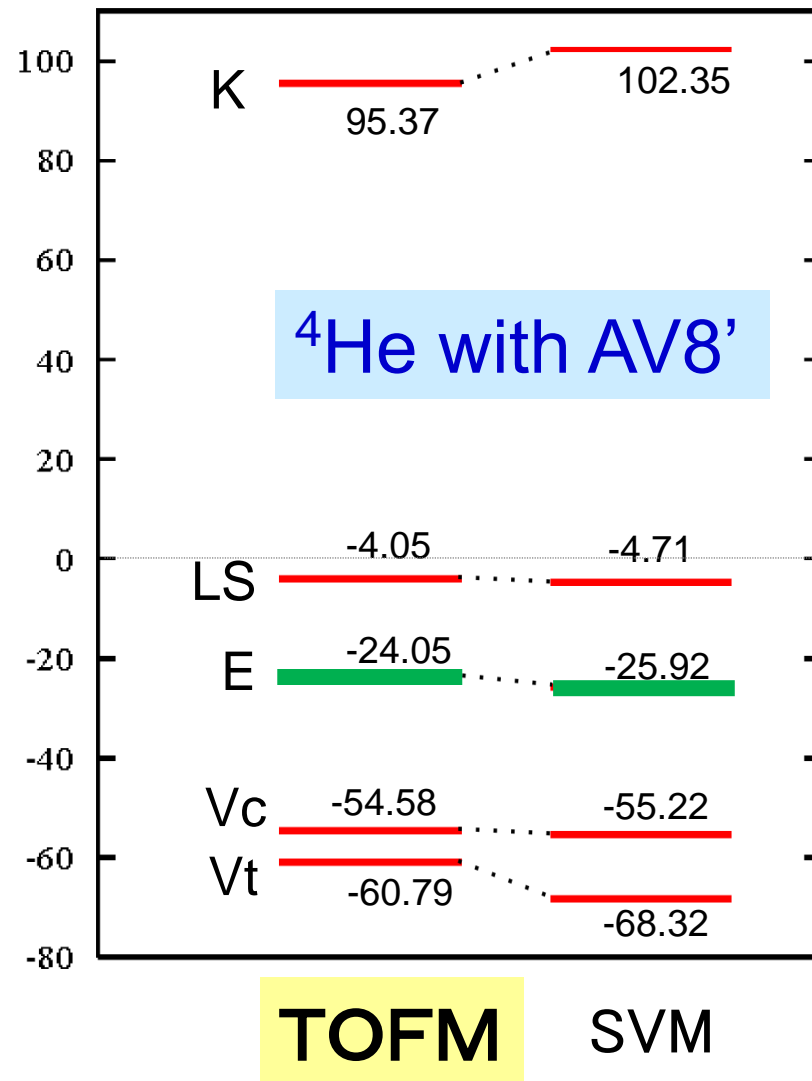
S-wave ($L=0$)



D-wave ($L=2$)



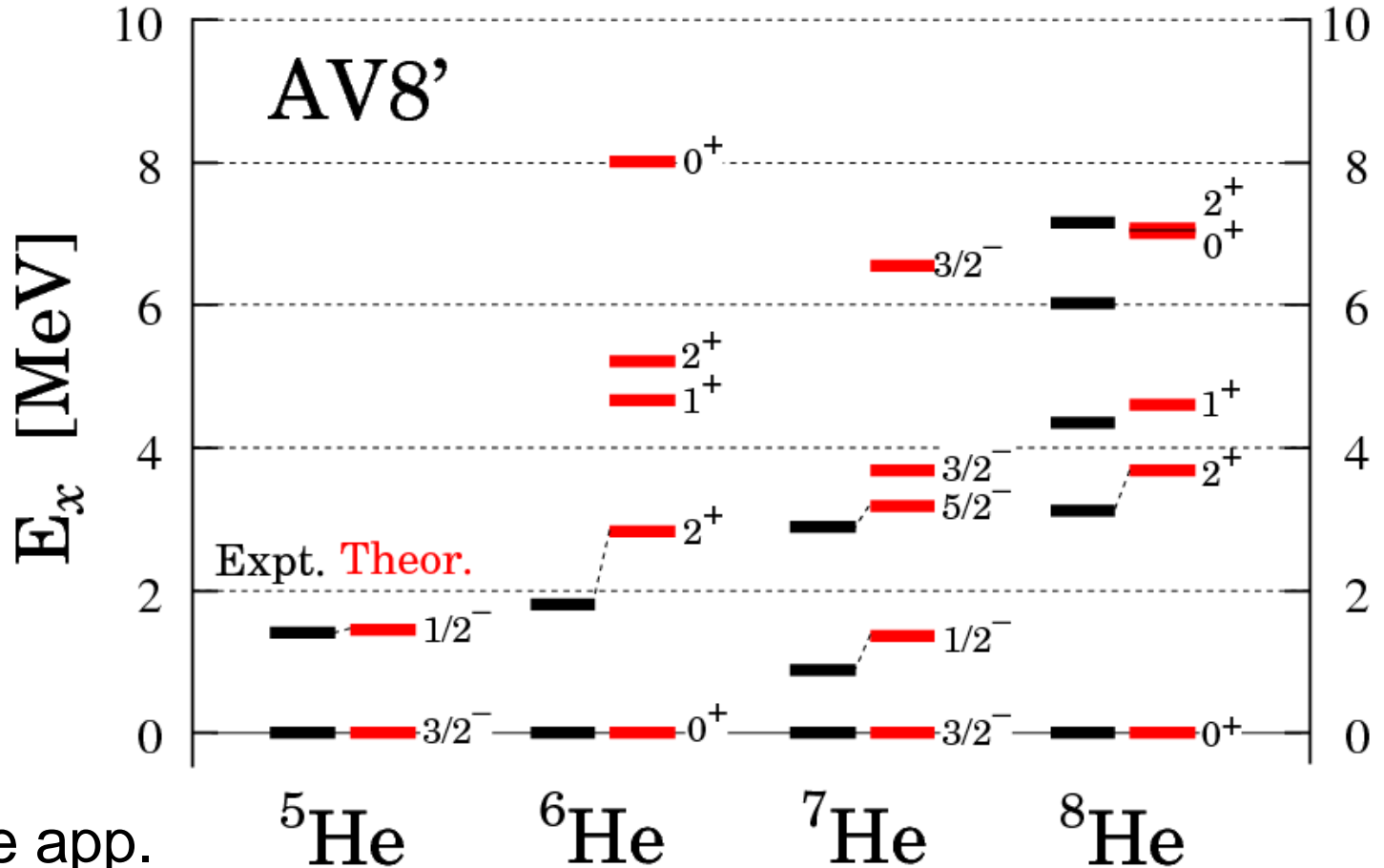
Energy [MeV]



$4\text{-}8\text{He}$ with TOSM+UCOM

- Excitation energies in MeV

TM, A. Umeya, H. Toki, K. Ikeda
PRC84 (2011) 034315

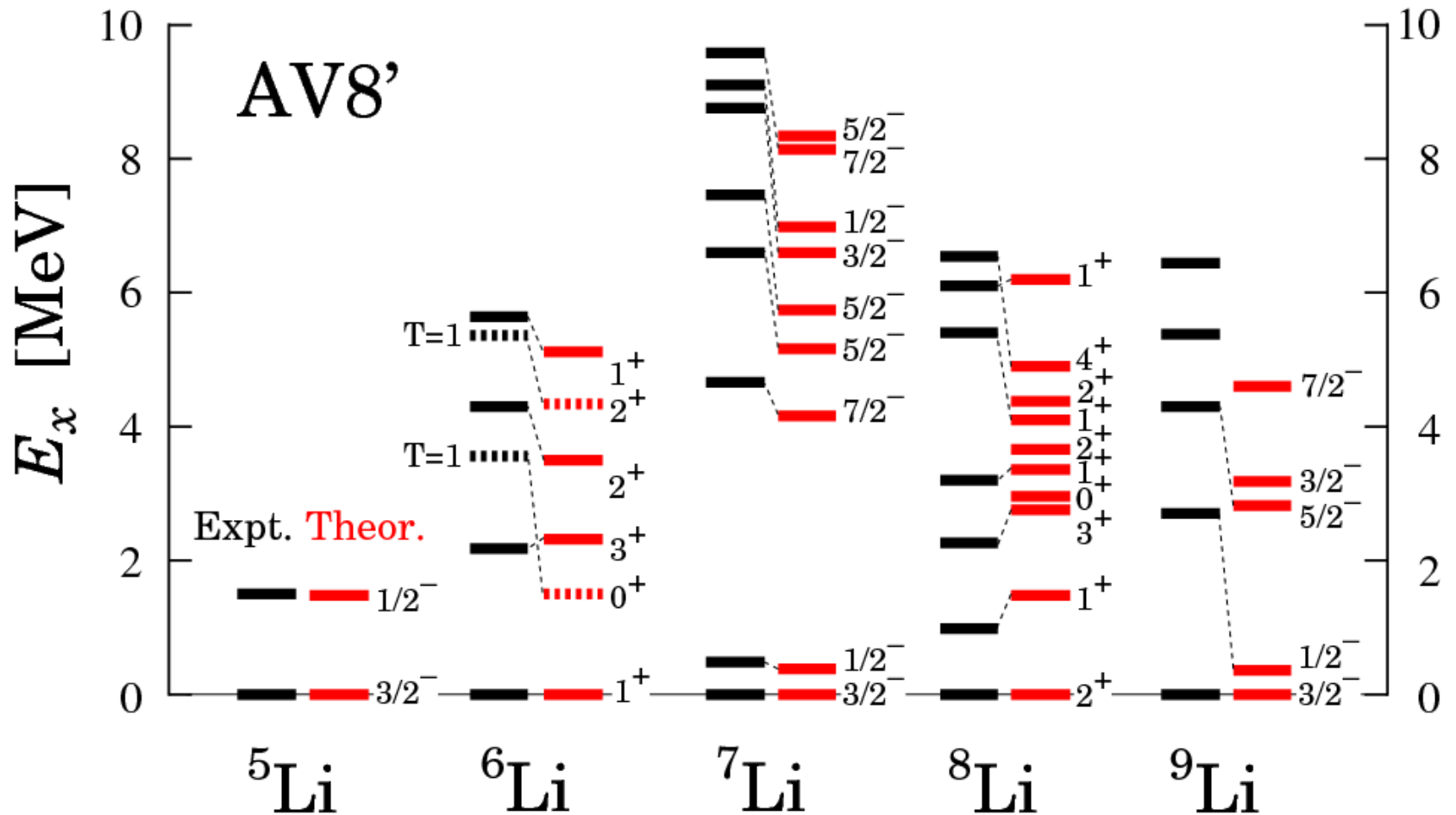


- Bound state app.
- No continuum
- No V_{NNN}

Excitation energy spectra are reproduced well

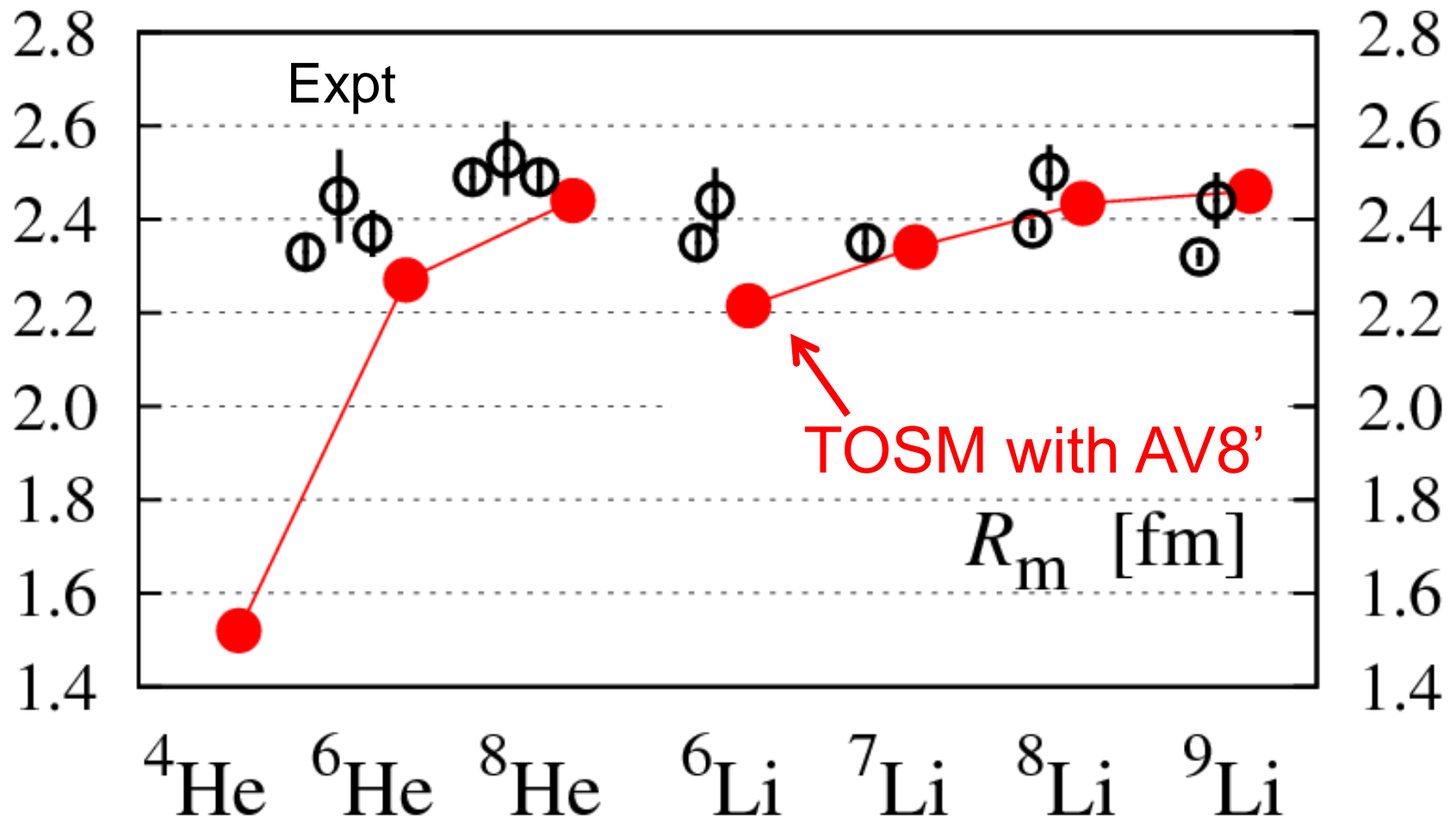
${}^5\text{-}{}^9\text{Li}$ with TOSM+UCOM

- Excitation energies in MeV



- Excitation energy spectra are reproduced well

Matter radius of He & Li isotopes



Halo

Skin

A. Dobrovolsky, NPA 766(2006)1

G. D. Alkhazov et al., PRL78('97)2313

I. Tanihata et al., PLB289('92)261

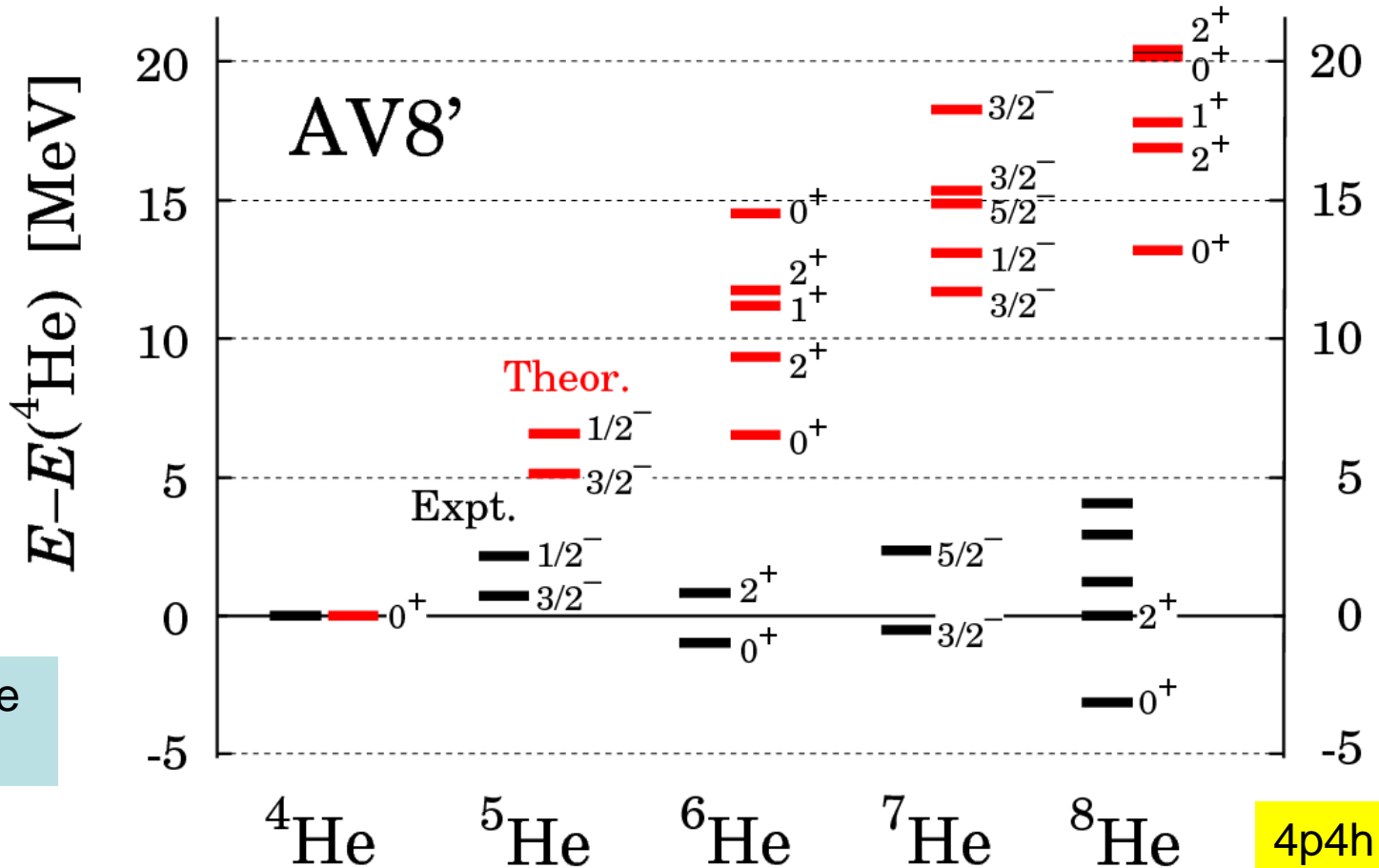
P. Mueller et al., PRL99(2007)252501

O. A. Kiselev et al., EPJA 25, Suppl. 1('05)215.

$^4\text{-}^8\text{He}$ with TOSM+UCOM

TM, A. Umeya, H. Toki, K. Ikeda
PRC84 (2011) 034315

- Difference from ^4He in MeV



~6 MeV in ^8He
using GFMC

- No V_{NNN}
- No continuum

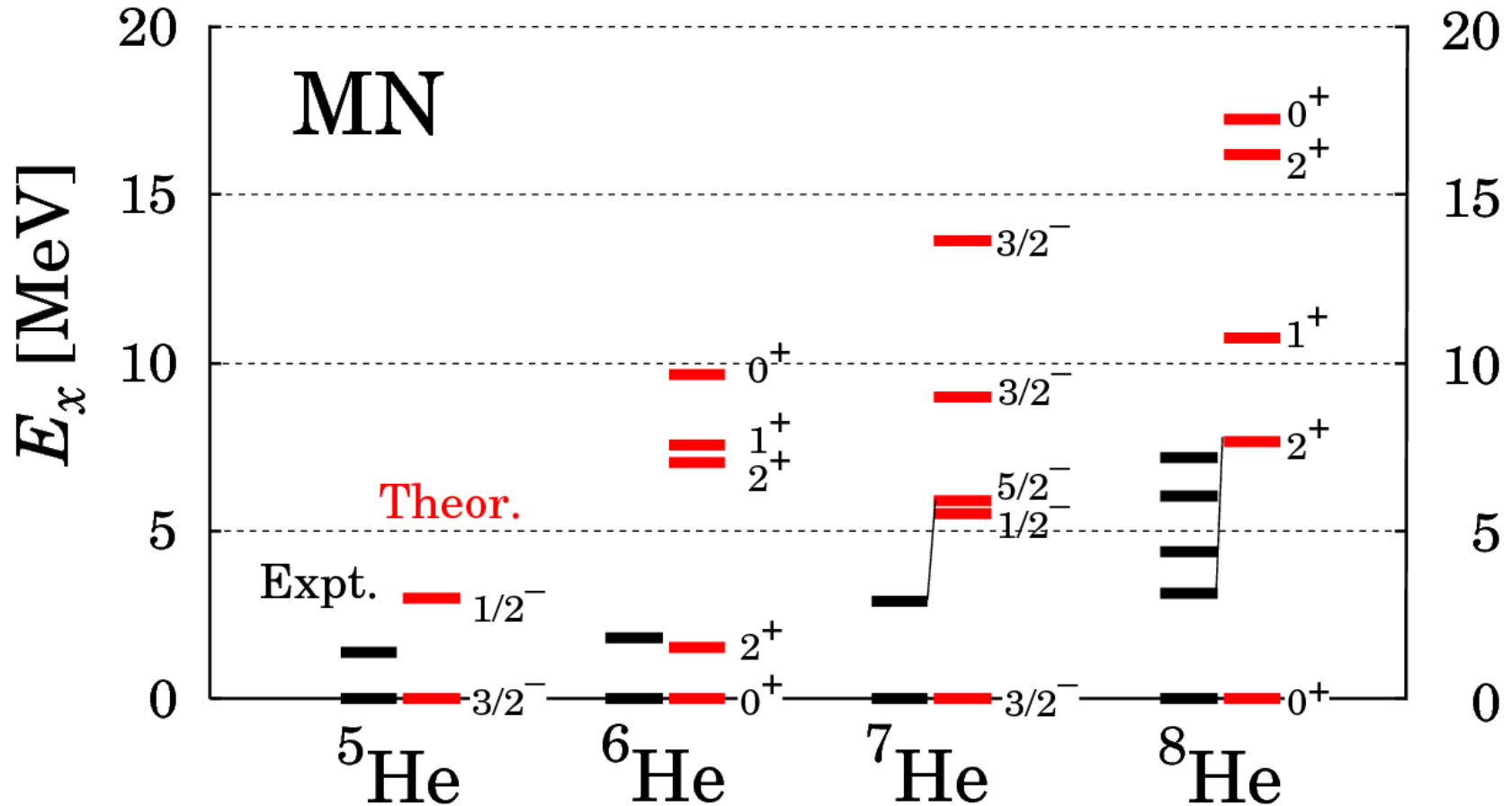
~7 MeV in ^8He using Cluster model (PLB691(2010)150, TM et al.)

4p4h
in TOSM

$4\text{-}8\text{He}$ with TOSM

Minnesota force
(Central+LS)

- Excitation energies in MeV



Configurations of ${}^4\text{He}$ with AV8'

$(0s_{1/2})^4$	83.0 %
$(0s_{1/2})^{-2}_{JT}(p_{1/2})^2_{JT}$ $JT=10$	2.6
$JT=01$	0.1
$(0s_{1/2})^{-2}_{10}(1s_{1/2})(d_{3/2})_{10}$	2.3
$(0s_{1/2})^{-2}_{10}(p_{3/2})(f_{5/2})_{10}$	1.9
Radius [fm]	1.54

TM, H. Toki, K. Ikeda
PTP121(2009)511

• deuteron correlation
with $(J, T)=(1, 0)$

Cf. R.Schiavilla et al. (VMC)
PRL98(2007)132501
R. Subedi et al. (JLab)
Science320(2008)1476

${}^{12}\text{C}(e, e' pN)$

S.C.Simpson, J.A.Tostevin
PRC83(2011)014605

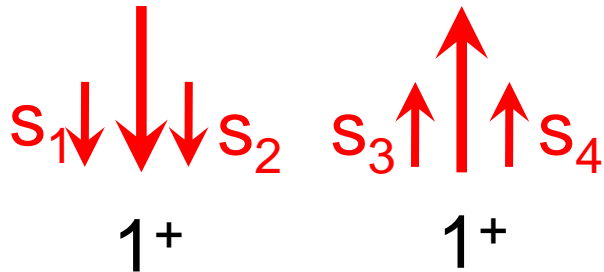
${}^{12}\text{C} \rightarrow {}^{10}\text{B} + pn$

- ${}^4\text{He}$ contains $p_{1/2}$ of “ **pn -pair**”
– Same feature in ${}^5\text{He}$ - ${}^8\text{He}$ ground state

Selectivity of the tensor coupling in ${}^4\text{He}$

$$0p0h : (0s)_{00}^4 \\ \supset (0s)_{10}^2 (0s)_{10}^2$$

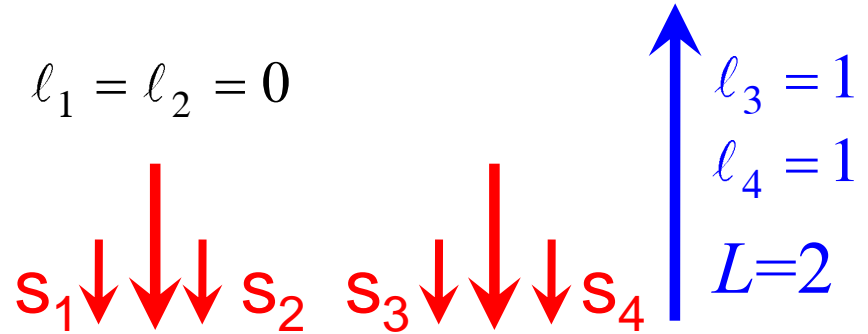
$$l_1 = l_2 = l_3 = l_4 = 0$$



V_T

$$2p2h : (0s)_{10}^2 (0p_{1/2})_{10}^2$$

$$l_1 = l_2 = 0$$



$$2p2h : (0s)_{10}^2 [(1s)(0d_{3/2})]_{10}$$

$$l_1 = l_2 = 0$$

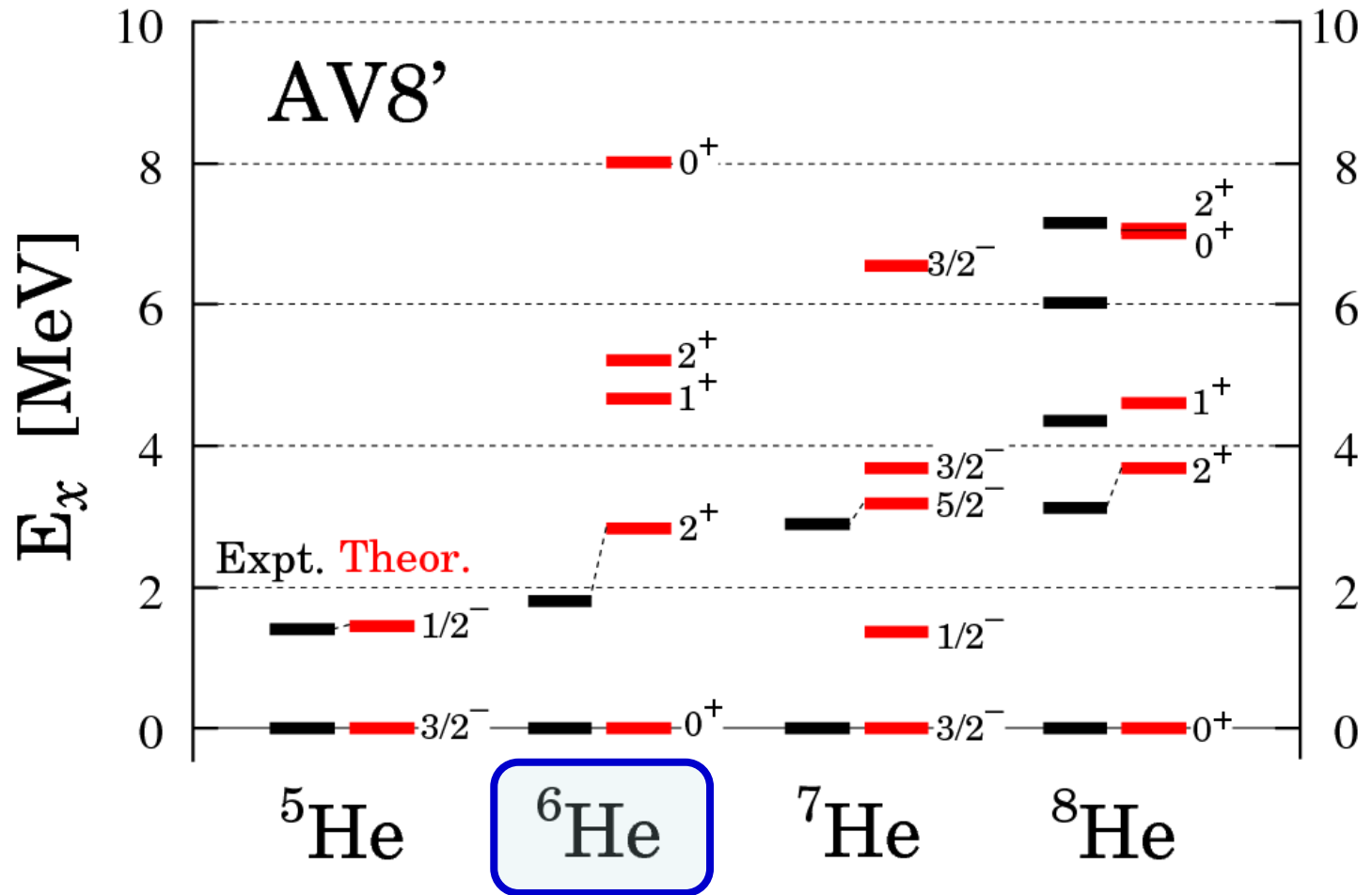


Selectivity of
tensor operator

$$\Delta L=2, \quad \Delta S=2$$

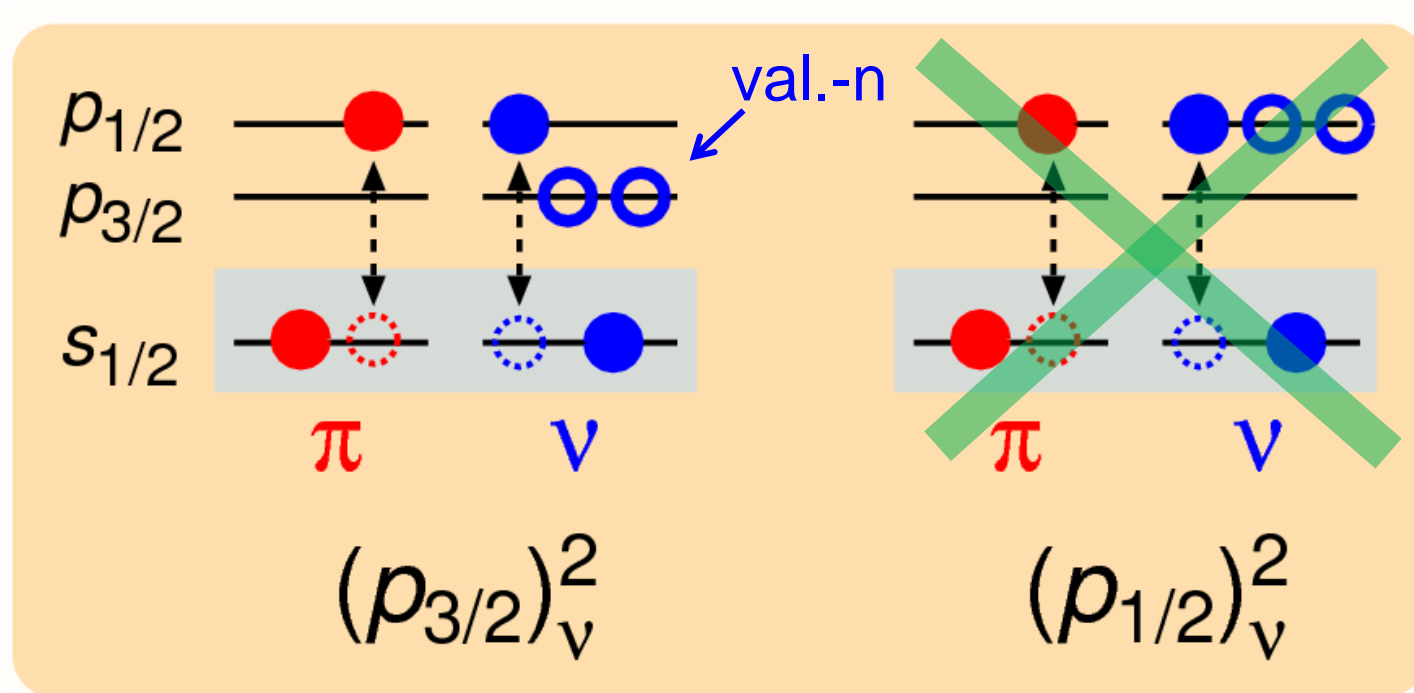
$^4\text{-}^8\text{He}$ with TOSM+UCOM

- Excitation energies in MeV



- No V_{NNN}
- No continuum
- Excitation energy spectra are reproduced well

Tensor correlation in ${}^6\text{He}$



Ground state

halo state (0^+)

Excited state

↑
Tensor correlation is **suppressed**
due to Pauli-Blocking

${}^6\text{He}$: Hamiltonian component in TOSM

- Difference from ${}^4\text{He}$ in MeV

${}^6\text{He}$	0^+_1	0^+_2
n^2 config	$(p_{3/2})^2$	$(p_{1/2})^2$

$$b_{\text{hole}} = 1.5 \text{ fm}$$

$$\hbar\omega = 18.4 \text{ MeV}$$

(hole)

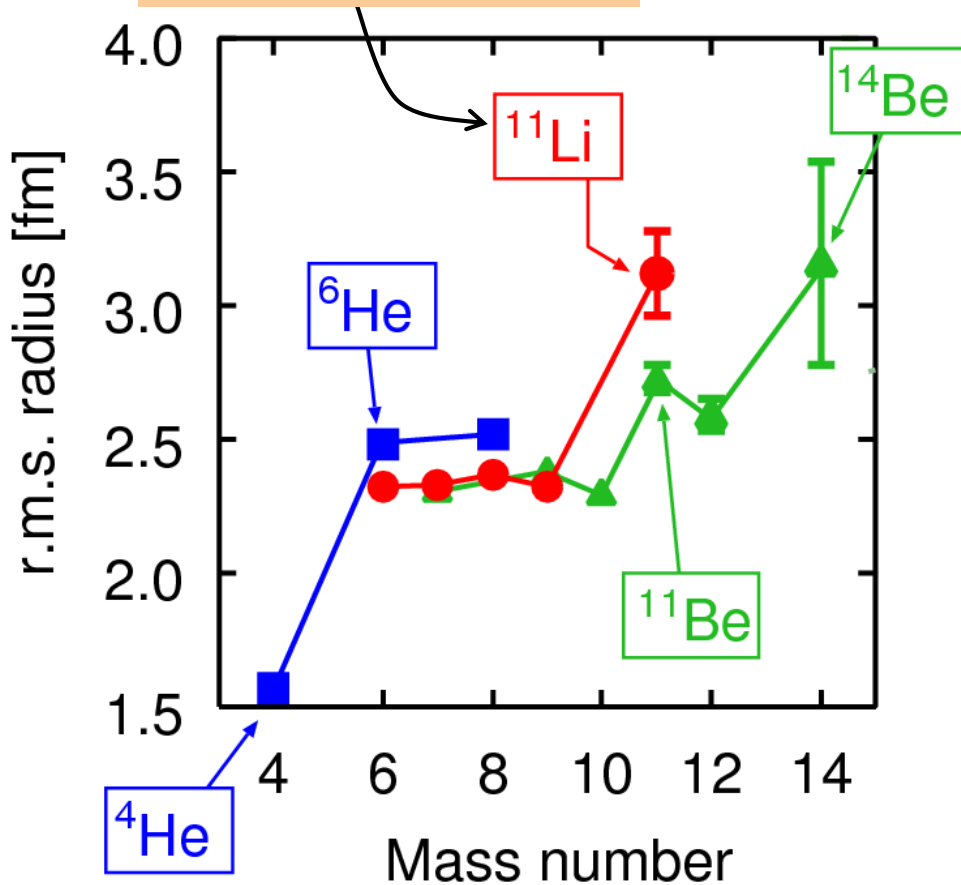
same trend
in ${}^5\text{-}{}^8\text{He}$

LS splitting
energy in ${}^5\text{He}$

- Terasawa, Arima PTP23 ('60)
- Nagata, Sasakawa, Sawada, Tamagaki, PTP22('59)
- Myo, Kato, Ikeda, PTP113 ('05)

Characteristics of Li-isotopes

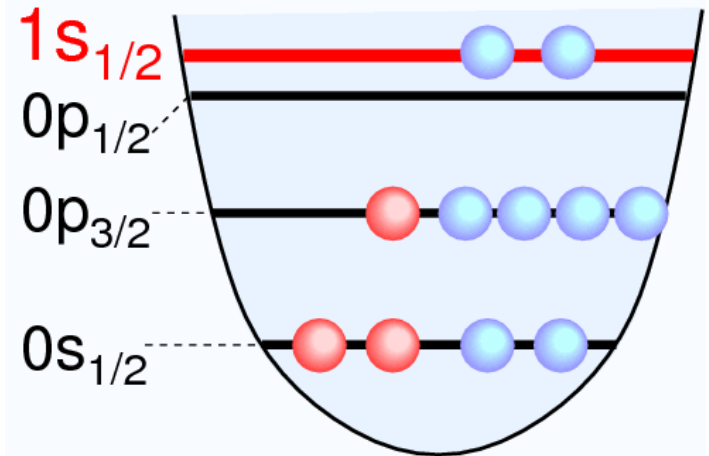
Halo structure



Tanihata et al., PRL55(1985)2676.
PLB206(1998)592.

✓ Breaking of magicity N=8

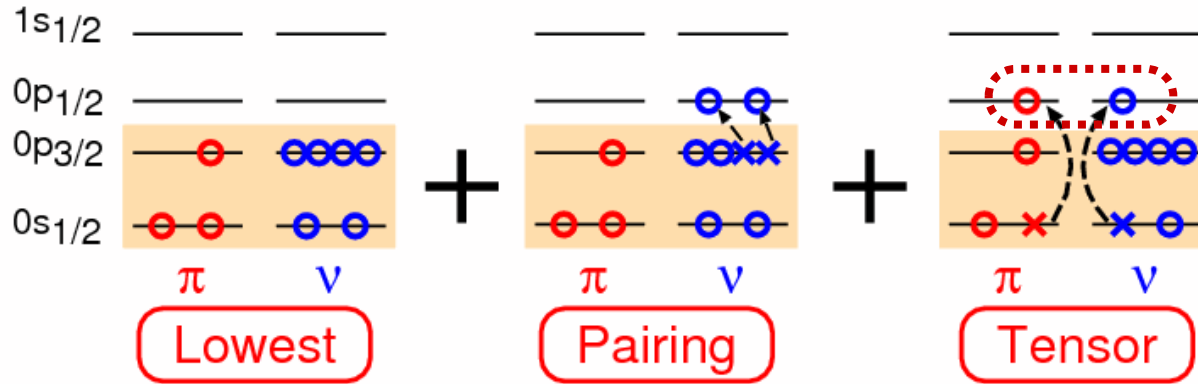
- $^{10-11}\text{Li}$, $^{11-12}\text{Be}$
- ^{11}Li ... $(1s)^2 \sim 50\%$.
(Expt by Simon et al., PRL83)
- **Mechanism is unclear**



^{11}Li

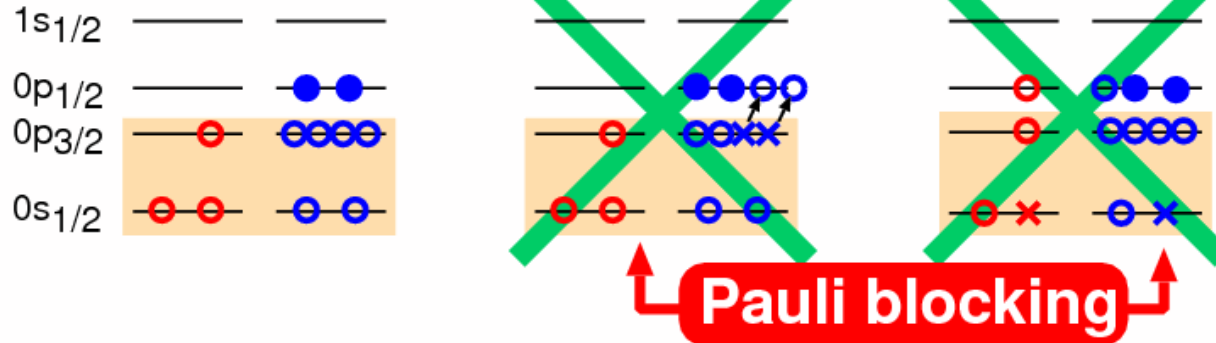
Expected effects of pairing and tensor correlations in ^{11}Li

^9Li
GS



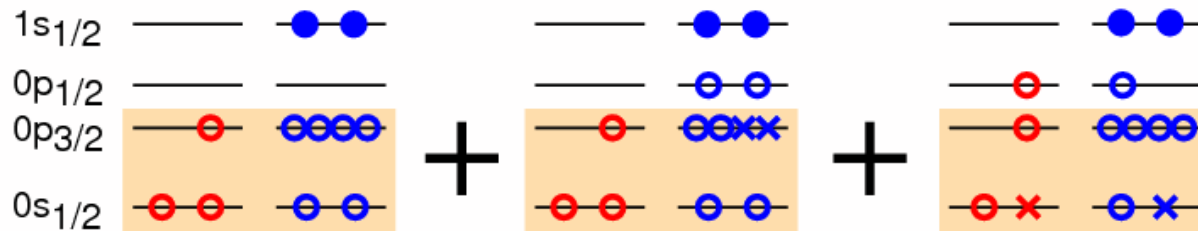
High-momentum

^{11}Li
(p^2)



energy loss

^{11}Li
(s^2)



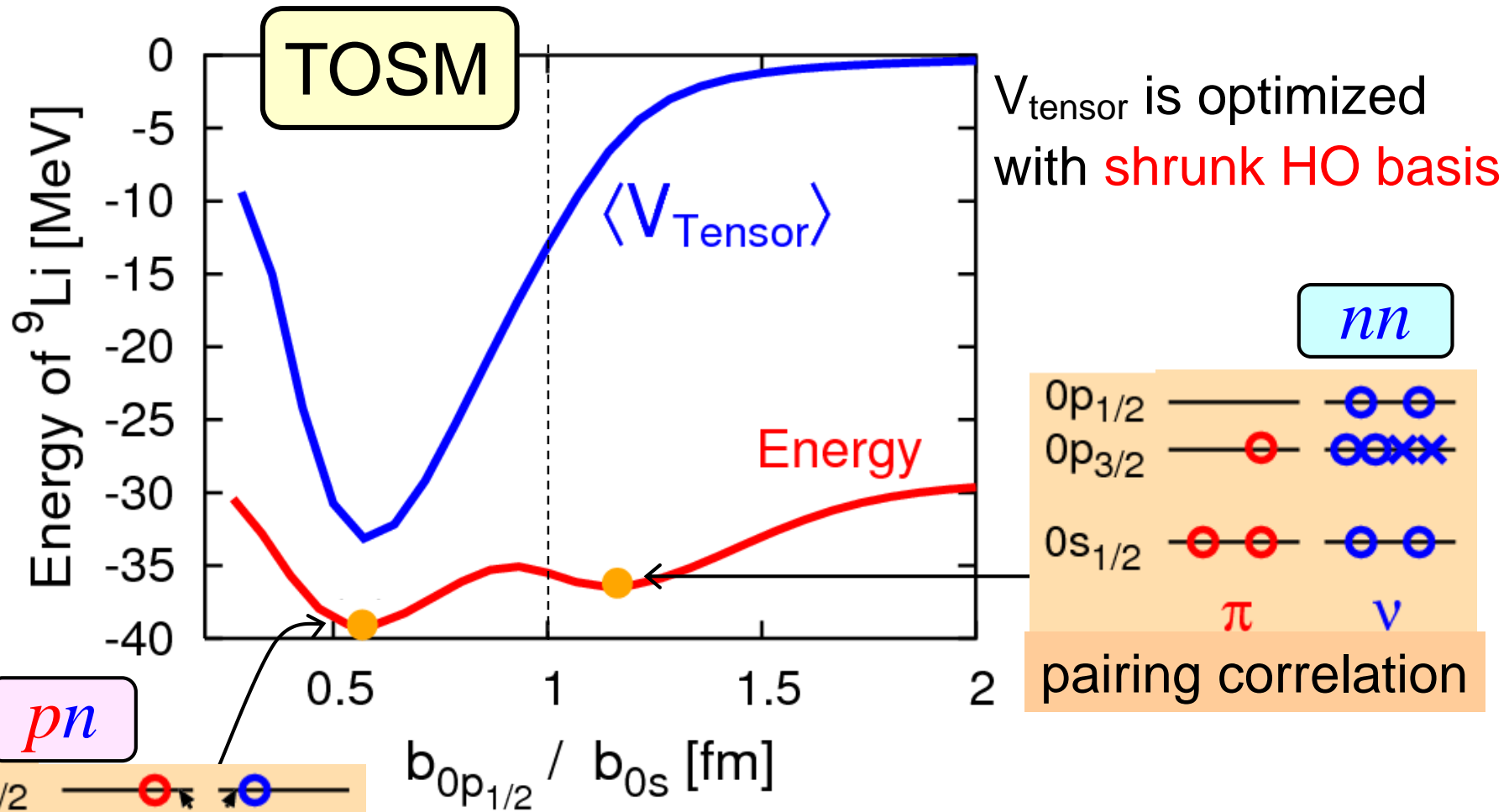
energy gain

increase ($1s$)²

Pairing-blocking :

K.Kato,T.Yamada,K.Ikeda,PTP101('99)119, Masui,S.Aoyama,TM,K.Kato,K.Ikeda,NPA673('00)207.
 TM,S.Aoyama,K.Kato,K.Ikeda,PTP108('02)133, H.Sagawa,B.A.Brown,H.Esbensen,PLB309('93)1.

Energy surface for b -parameter in ${}^9\text{Li}$



Dominant part of the tensor correlation

cf. 1st order (residual interaction): T. Otsuka et al.
PRL95(2005)232502.

^{11}Li in coupled $^9\text{Li}+n+n$ model

- System is solved based on RGM

$$H(^{11}\text{Li}) = H(^9\text{Li}) + H_{nn} \quad \Phi(^{11}\text{Li}) = \mathcal{A} \left\{ \sum_{i=1}^N \psi_i(^9\text{Li}) \cdot \chi_i(nn) \right\}$$

$$\sum_{i=1}^N \left\langle \psi_j(^9\text{Li}) \left| H(^{11}\text{Li}) - E \right| \mathcal{A} \left\{ \psi_i(^9\text{Li}) \cdot \chi_i(nn) \right\} \right\rangle = 0$$

$\psi_i(^9\text{Li})$: **shell model type configuration** \rightarrow **TOSM**

- Orthogonality Condition Model (OCM) is applied.

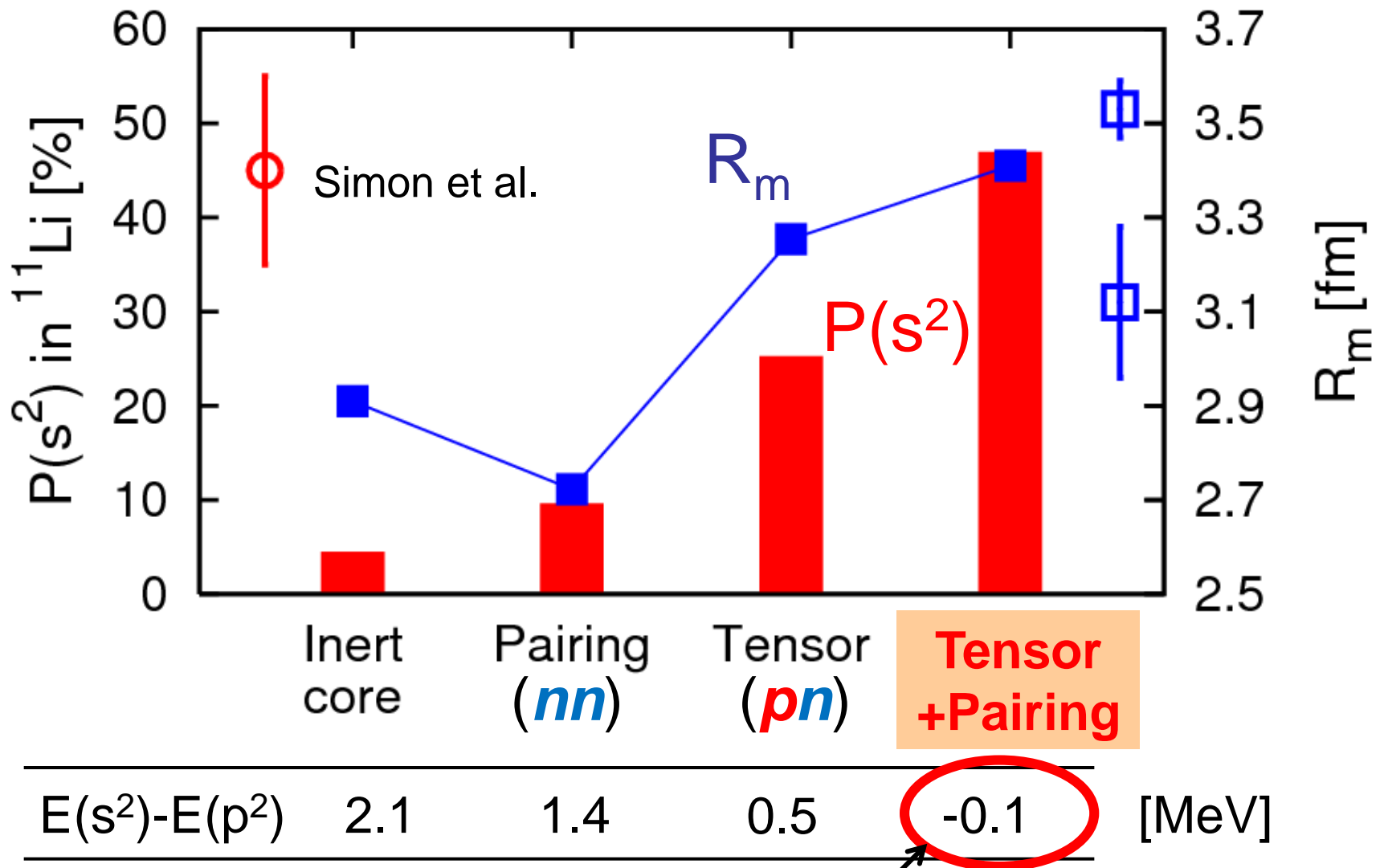
$$\sum_{i=1}^N \left[H_{ij} (^9\text{Li}) + (T_1 + T_2 + V_{c1} + V_{c2} + V_{12}) \cdot \delta_{ij} \right] \chi_j(nn) = E \chi_i(nn)$$

$$H_{ij} (^9\text{Li}) = \langle \psi_i | H(^9\text{Li}) | \psi_j \rangle : \text{Hamiltonian for } ^9\text{Li}$$

$$\chi(nn) = \mathcal{A} \{ \phi_1 \phi_2 \} : \text{few-body method with Gaussian expansion}$$

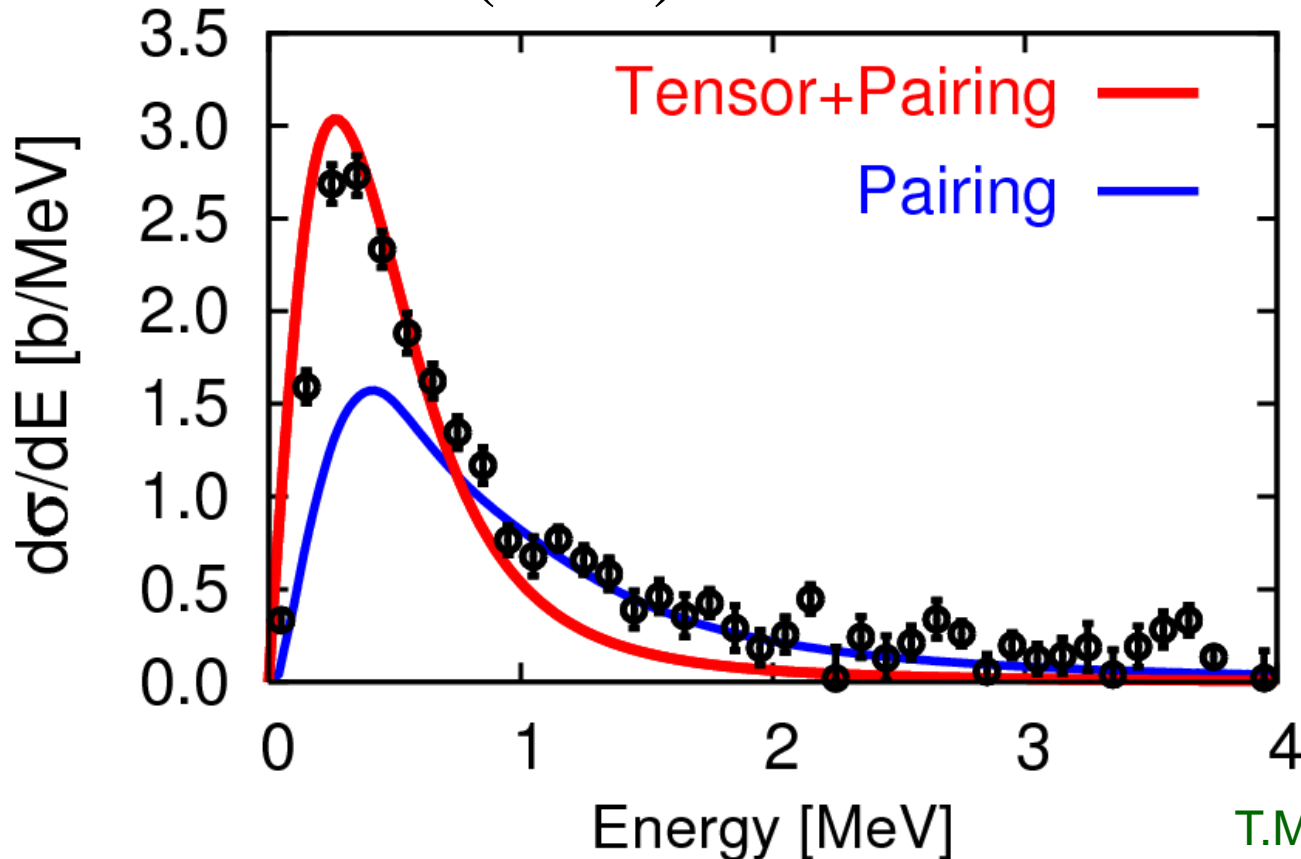
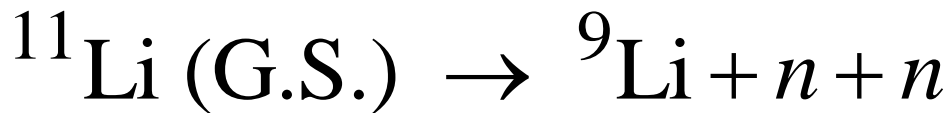
$$\langle \phi_i | \phi_\alpha \rangle = 0, \{ \phi_\alpha \in ^9\text{Li} \} : \text{Orthogonality to the Pauli-forbidden states}^{23}$$

^{11}Li G.S. properties ($S_{2n}=0.31$ MeV)



Pairing correlation couples $(0p)^2$ and $(1s)^2$ for last $2n$

Coulomb breakup strength of ^{11}Li



No three-body resonance

E1 strength by using the Green's function method +Complex scaling method +Equivalent photon method (TM et al., PRC63('01))

T.Myo, K.Kato, H.Toki, K.Ikeda
PRC76(2007)024305

- Expt: T. Nakamura et al. , PRL96,252502(2006)
- Energy resolution with $\sqrt{E} = 0.17$ MeV.

Summary

- **TOSM+UCOM** with bare nuclear force.
- ${}^4\text{He}$ contains “ **pn -pair of $p_{1/2}$** ” than $p_{3/2}$.
- **He isotopes with $p_{3/2}$** has large contributions of V_{tensor} & Kinetic energy than **those with $p_{1/2}$** .
- **Halo formation in ${}^{11}\text{Li}$** with tensor and pairing correlations.

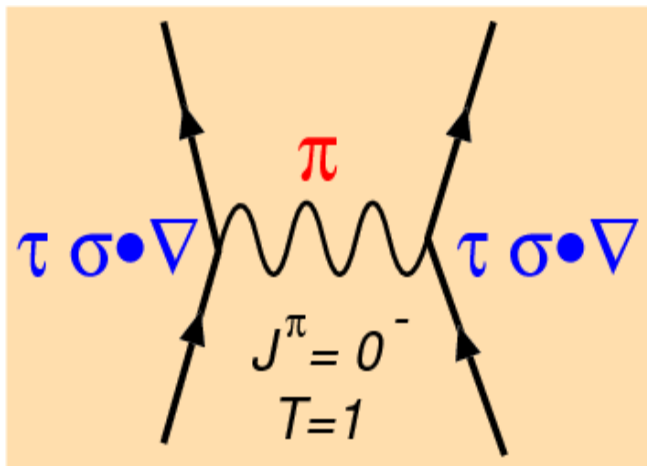
Review Di-neutron clustering and deuteron-like tensor correlation in nuclear structure focusing on ${}^{11}\text{Li}$

K. Ikeda, T. Myo, K. Kato and H. Toki
Springer, Lecture Notes in Physics 818 (2010)
“**Clusters in Nuclei**” Vol.1, 165-221.

Pion exchange interaction vs. V_{tensor}

$$3(\vec{\sigma}_1 \cdot \hat{q})(\vec{\sigma}_2 \cdot \hat{q}) \frac{q^2}{m^2 + q^2} = (\vec{\sigma}_1 \cdot \vec{\sigma}_2) \frac{q^2}{m^2 + q^2} + S_{12} \frac{q^2}{m^2 + q^2}$$

$$= (\vec{\sigma}_1 \cdot \vec{\sigma}_2) \left[\frac{m^2 + q^2}{m^2 + q^2} - \frac{m^2}{m^2 + q^2} \right] + S_{12} \frac{q^2}{m^2 + q^2}$$



Tensor operator

$$S_{12} = 3(\vec{\sigma}_1 \cdot \hat{q})(\vec{\sigma}_2 \cdot \hat{q}) - (\vec{\sigma}_1 \cdot \vec{\sigma}_2)$$

Delta interaction

Yukawa interaction

Involve large momentum

- V_{tensor} produces the high momentum component. 27

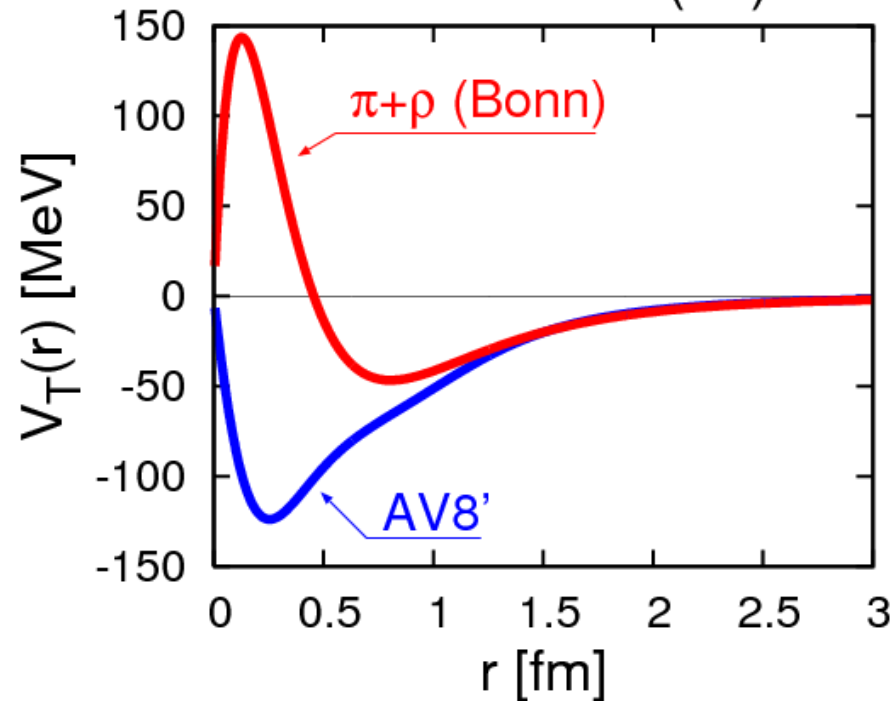
Property of the tensor force

$$F(r) = r^2 \cdot \phi_{0s}(r, b_{0s}) \cdot V_T(r) \cdot \phi_{0d}(r, b_d)$$

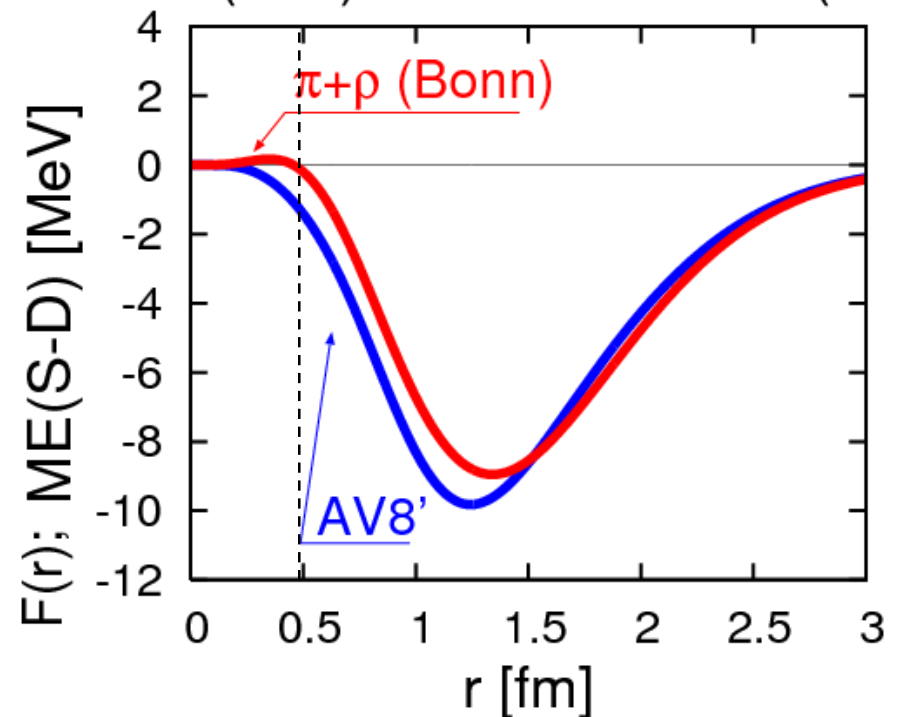
$$b_s = 1.4 \cdot \sqrt{2} \text{ [fm]} \quad b_d = b_s / 2$$

$$V_{\text{tensor}} = V_T(r) \cdot S_{12}$$

Tensor Force (3E)



ME(S-D) of Tensor Force (3E)



- Centrifugal potential (1 GeV @ 0.5 fm) pushes away the L=2 wave function.