

Tensor-optimized shell model with bare interaction for light nuclei

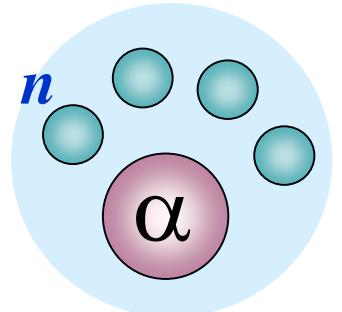
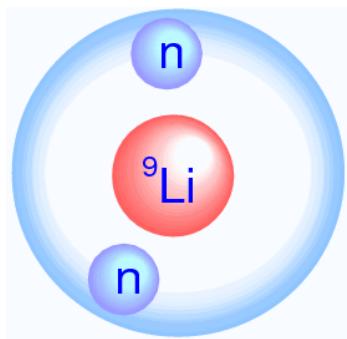
Takayuki MYO 明 孝之
Osaka Institute of Technology
大阪工業大学



In collaboration with Atsushi UMEYA (Nippon Inst. Tech.)
Hiroshi TOKI, Kaori Horii (RCNP)
Kiyomi IKEDA (RIKEN)

Scientific activities with Prof. Kiyoshi Kato

- 1996-1998: Master course in Hokkaido Univ.
 - Strength function using complex scaling method (CSM)
- 1999-2002: Doctor course in Hokkaido Univ.
 - Coulomb breakups of halo nuclei, ${}^6\text{He}$, ${}^{11}\text{Li}$, ${}^{11}\text{Be}$, ... with CSM
 - Pairing correlation in halo nuclei
- 2003-2007: Researcher in RCNP (Toki, Ikeda)
 - Role of tensor force (pion) in light nuclei with tensor-optimized shell model (TOSM)
 - He isotopes, LS splitting, halo formation in ${}^{11}\text{Li}$
- 2008- : Osaka Institute of Technology
 - Tensor correlation in nuclei with “TOSM+UCOM using bare NN interaction”.
 - Multi particle resonances up to five-body system in unstable nuclei (${}^8\text{He}$ as ${}^4\text{He}+4\text{n}$, ${}^8\text{C}$ as ${}^4\text{He}+4\text{p}$)

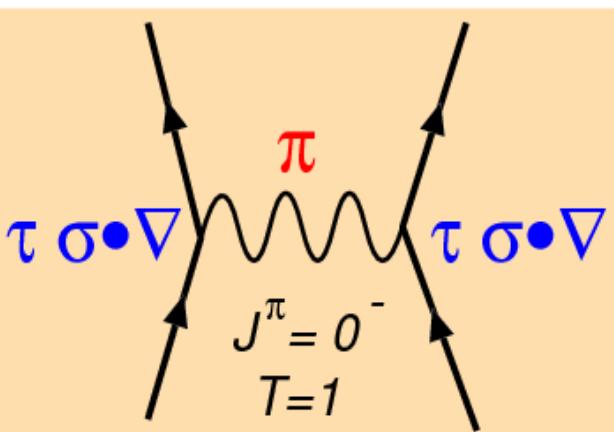


Outline

- **Role of V_{tensor} (V_π)** in the nuclear structure by describing strong tensor correlation explicitly.
- Tensor Optimized Shell Model (**TOSM**) to describe tensor correlation.
- Unitary Correlation Operator Method (**UCOM**) to describe short-range correlation.
- **TOSM+UCOM** to He & Li isotopes with V_{bare}

TM, A. Umeya, H. Toki, K. Ikeda, PRC84 (2011) 034315
TM, A. Umeya, H. Toki, K. Ikeda, PRC86 (2012) 024318

Pion exchange interaction vs. V_{tensor}

$$3(\vec{\sigma}_1 \cdot \hat{q})(\vec{\sigma}_2 \cdot \hat{q}) \frac{q^2}{m^2 + q^2} = (\vec{\sigma}_1 \cdot \vec{\sigma}_2) \frac{q^2}{m^2 + q^2} + S_{12} \frac{q^2}{m^2 + q^2}$$
$$= (\vec{\sigma}_1 \cdot \vec{\sigma}_2) \left[\frac{m^2 + q^2}{m^2 + q^2} - \frac{m^2}{m^2 + q^2} \right] + S_{12} \frac{q^2}{m^2 + q^2}$$


Delta interaction

Yukawa interaction

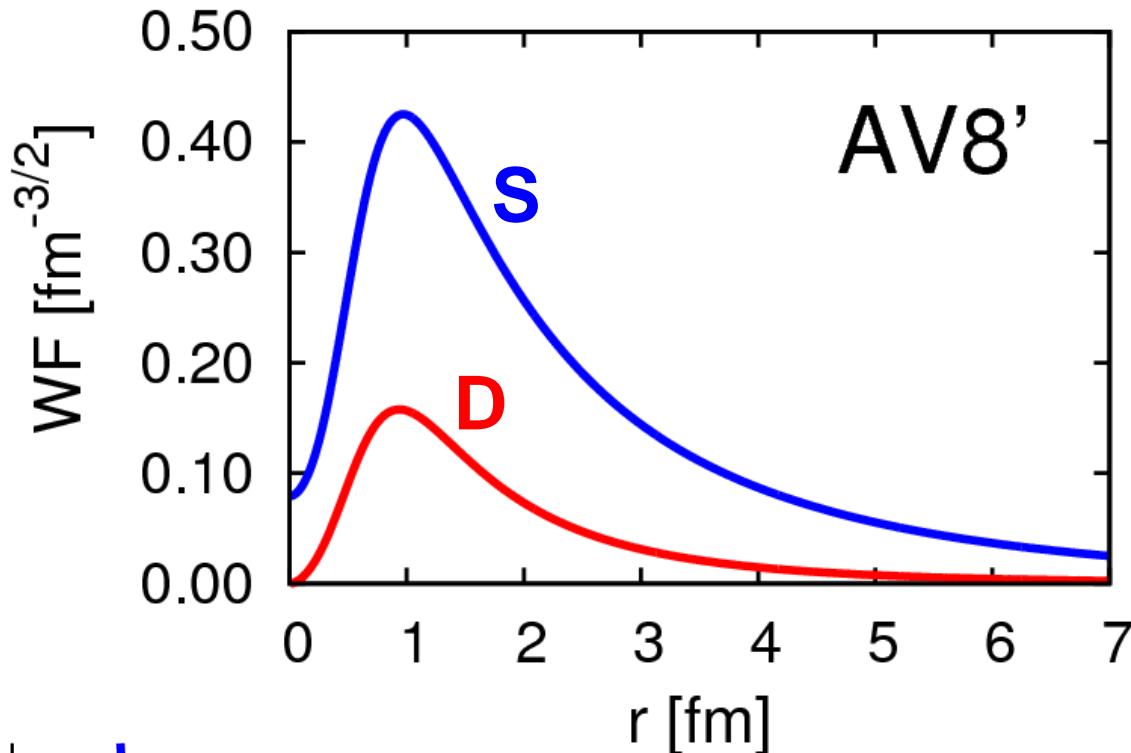
Involve large momentum

Tensor operator

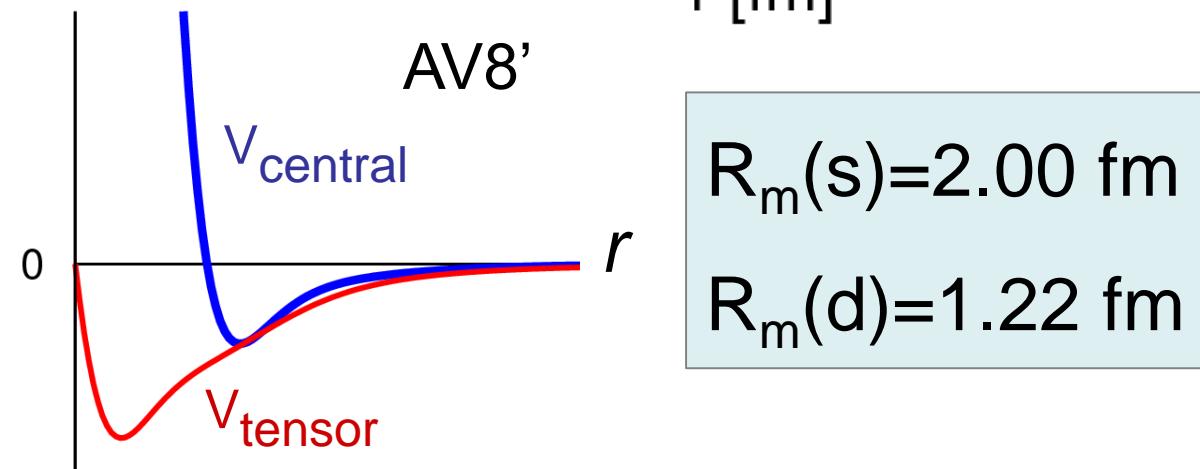
$$S_{12} = 3(\vec{\sigma}_1 \cdot \hat{q})(\vec{\sigma}_2 \cdot \hat{q}) - (\vec{\sigma}_1 \cdot \vec{\sigma}_2)$$

- V_{tensor} produces the high momentum component. 4

Deuteron & tensor force



Energy	-2.24 MeV
Kinetic	19.88
Central	-4.46
Tensor	-16.64
LS	-1.02
$P(L=2)$	5.77%
Radius	1.96 fm



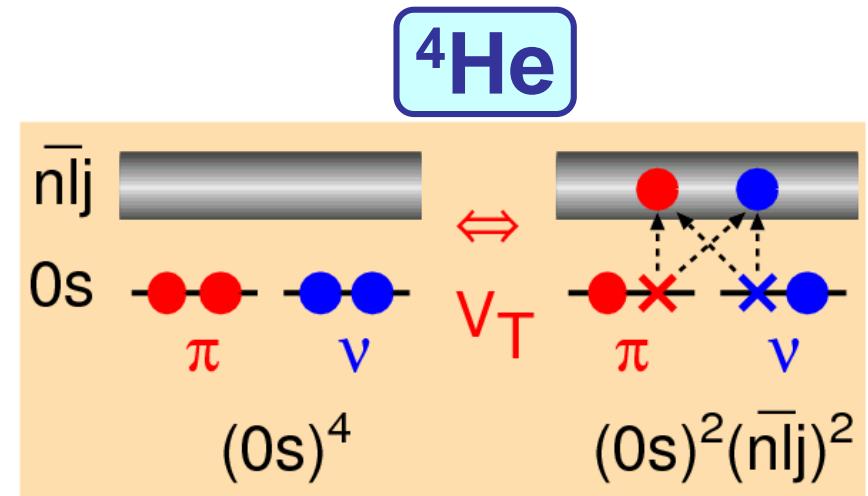
d-wave is
“spatially compact”
 (high momentum)

Tensor-optimized shell model (TOSM)

TM, Sugimoto, Kato, Toki, Ikeda PTP117(2007)257

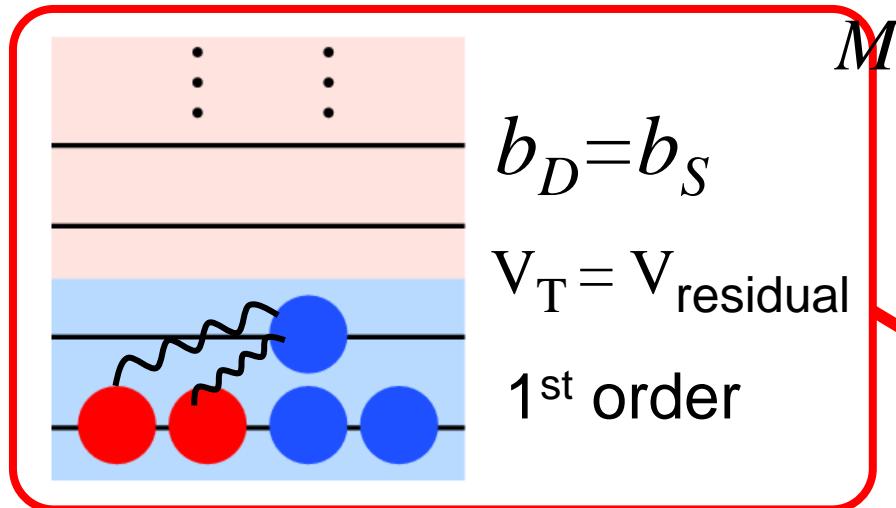
- Configuration mixing with **2p2h excitations** with high- L orbits.
- V_{tensor} is **NOT** treated as residual interactions

$$\text{cf. } \frac{V_\pi}{V_{NN}} \sim 80\% \text{ in GFMC}$$



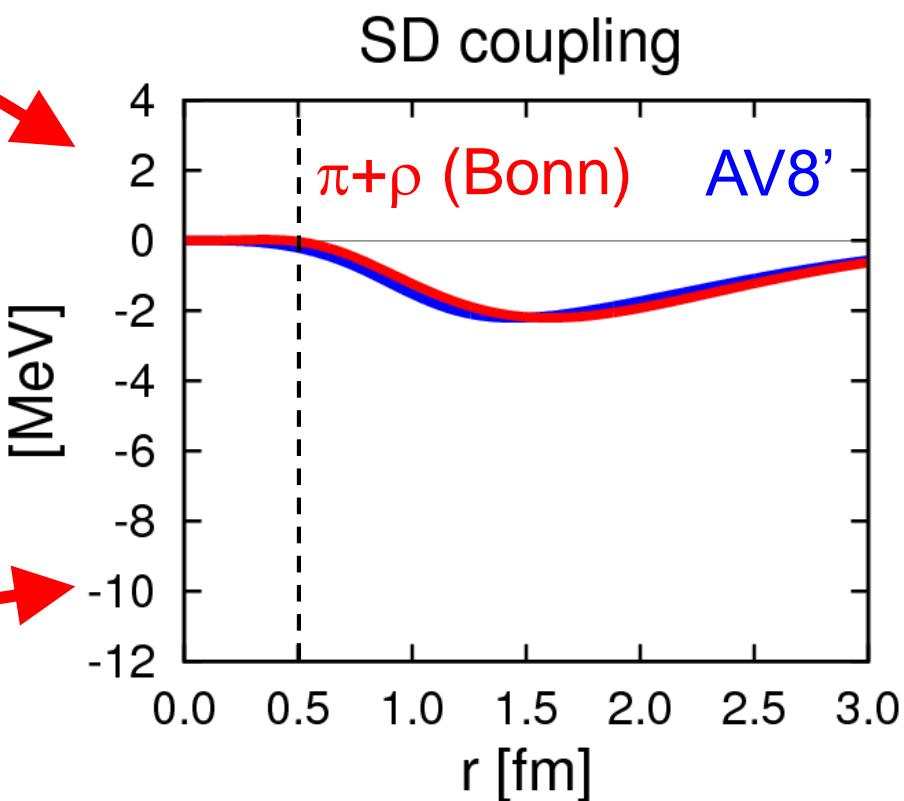
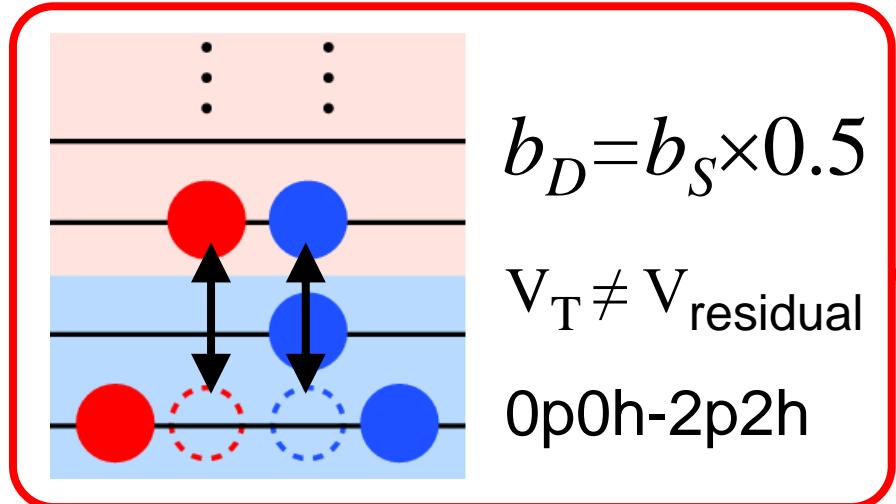
- Length parameters such as b_{0s} , b_{0p} , ... are optimized **independently**, or **superposed by many Gaussian bases**.
 - **Spatial shrinkage** of **D-wave** as seen in deuteron.
HF (Sugimoto, NPA740), RMF (Ogawa, PRC73), AMD (Dote et al., PTP115)
- Satisfy few-body results with Minnesota central force (${}^{4,6}\text{He}$)

Tensor force matrix elements



$$M_{SD}(r) = r^2 \phi_S(r, b_S) \cdot V_T(r) \cdot \phi_D(r, b_D)$$

: Integrand of Tensor ME



- Centrifugal potential (1GeV@0.5fm) pushes away the D-wave.

Effect of Tensor force in TOSM

- 1st order treatment of V_T  HF state
 - Spin-saturated nuclei : $\langle 0 | V_T | 0 \rangle = 0$
 - For $N \neq Z$ nuclei : $\langle 0 | V_T | 0 \rangle \sim \text{few MeV}$
 - Effect on the energy spectra in unstable nuclei
cf. T. Otsuka et al. PRL95(2005)232502.
- In TOSM, 0p0h+1p1h+2p2h
 - In ${}^4\text{He}$, : $\langle V_T \rangle \sim 15 \text{MeV/A}$, comparable to GFMC.
 - *SD* coupling between 0p0h & 2p2h is essential
 - Describe high momentum (compact *D*-wave)
 - Break $N=8$ magic in ${}^{11}\text{Li}$. TM et al. PRC76(2007)024305
 - Experiments using (*p,d*) reaction by Ong-Tanihata Group @ RCNP, to observe high momentum nucleon.⁸

Hamiltonian and variational equations in TOSM

$$H = \sum_{i=1}^A t_i - T_G + \sum_{i < j}^A v_{ij},$$

(0p0h+1p1h+2p2h)

$$\Phi(A) = \sum_k C_k \cdot \psi_k(A)$$

Shell model type configuration
with mass number A

Particle state : Gaussian expansion for each orbit

←

$$\phi_{lj}^{n'}(\mathbf{r}) = \sum_{n=1}^N C_{lj,n}^{n'} \cdot \phi_{lj,n}(\mathbf{r}) \quad \phi_{lj,n}(\mathbf{r}) \propto r^l \exp\left[-\frac{1}{2}\left(\frac{r}{b_{lj,n}}\right)^2\right] [Y_l(\hat{\mathbf{r}}), \chi_{1/2}^\sigma]_j$$

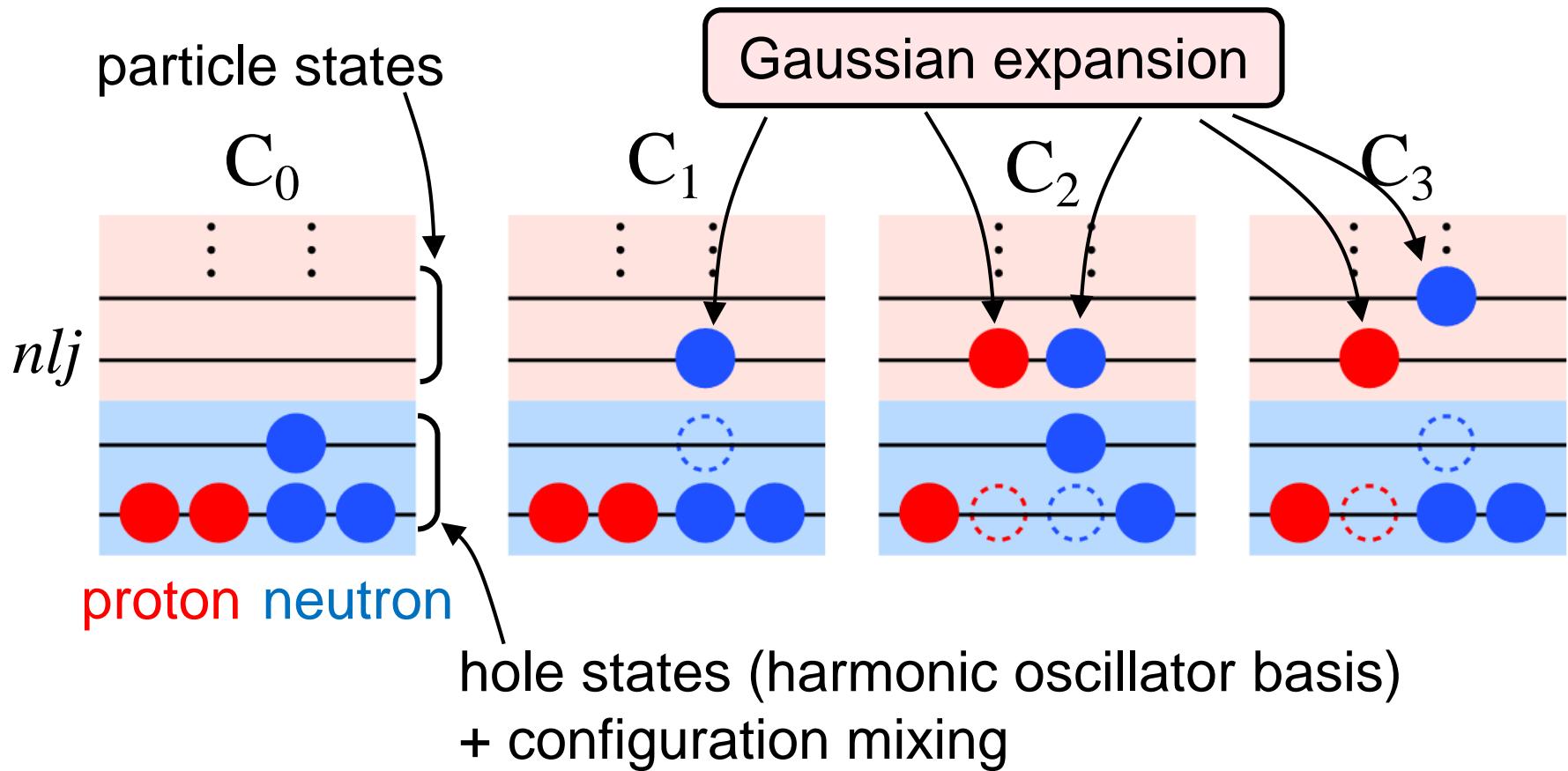
Gaussian basis function
Hiyama, Kino, Kamimura
PPNP51(2003)223

$$\langle \phi_{lj}^{n'} | \phi_{lj}^{n''} \rangle = \delta_{n', n''}$$

$$\frac{\partial \langle H - E \rangle}{\partial C_k} = 0, \quad \frac{\partial \langle H - E \rangle}{\partial b_{lj,n}} = 0$$

c.m. excitation is excluded
by Lawson's method

Configurations in TOSM



Application to Hypernuclei to investigate $\Lambda N - \Sigma N$ coupling
by **Umeya** (NIT), **Hiyama** (RIKEN)

Unitary Correlation Operator Method

$$\Psi_{\text{corr.}} = C \cdot \Phi_{\text{uncorr.}}$$

(short-range part)

TOSM

short-range correlator

$$C^\dagger = C^{-1} \quad (\text{Unitary trans.})$$

$$H\Psi = E\Psi \rightarrow C^\dagger H C \Phi \equiv \hat{H}\Phi = E\Phi$$

Bare Hamiltonian

$$C = \exp(-i \sum_{i < j} g_{ij}),$$

Shift operator depending on the relative distance

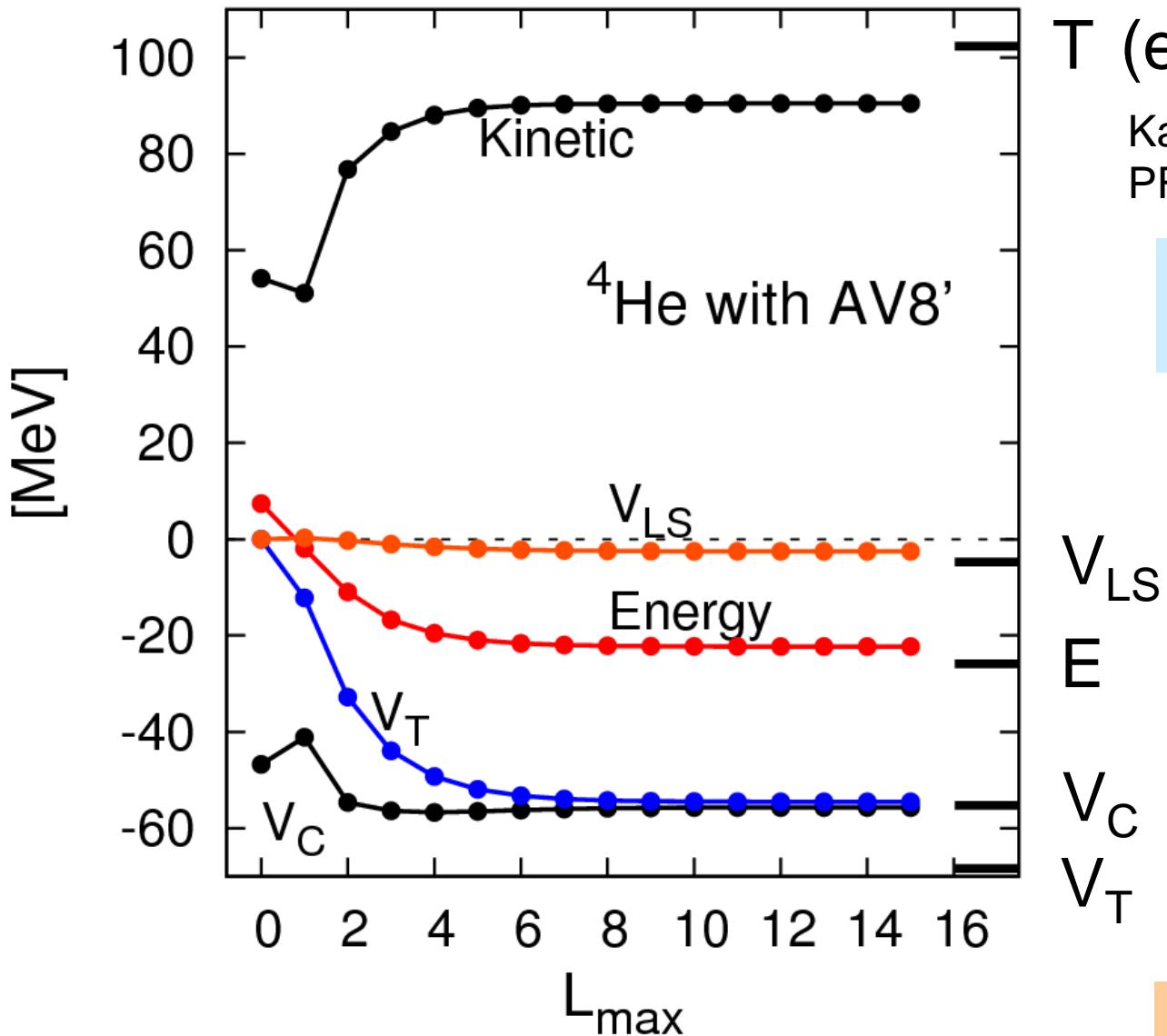
$$g_{ij} = \frac{1}{2} \left\{ p_r \underset{\overrightarrow{r}}{s(r_{ij})} + s(r_{ij}) \underset{\overrightarrow{r}}{p_r} \right\} \quad \vec{p} = \vec{p}_r + \vec{p}_\Omega$$

Amount of shift, variationally determined.

$$C^\dagger r C \simeq r + s(r) + \frac{1}{2} s(r) s'(r) \dots$$

2-body cluster expansion

^4He in TOSM + short-range UCOM



T (exact)

Kamada et al.
PRC64 (Jacobi)

TM, H. Toki, K. Ikeda
PTP121(2009)511

• variational
calculation

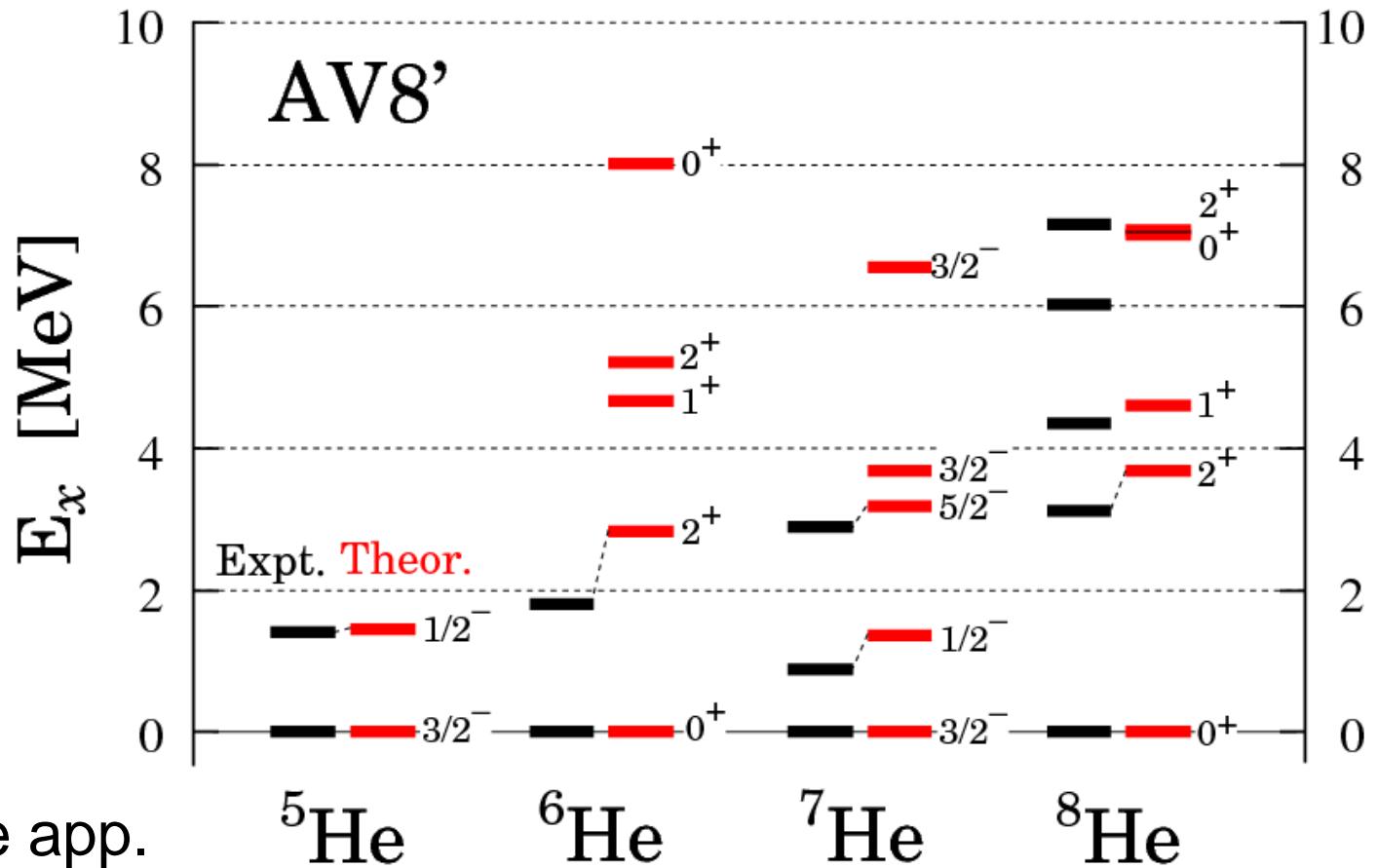
• Gaussian expansion
with 9 bases

good convergence

^{5-8}He with TOSM+UCOM

- Excitation energies in MeV

TM, A. Umeya, H. Toki, K. Ikeda
PRC84 (2011) 034315

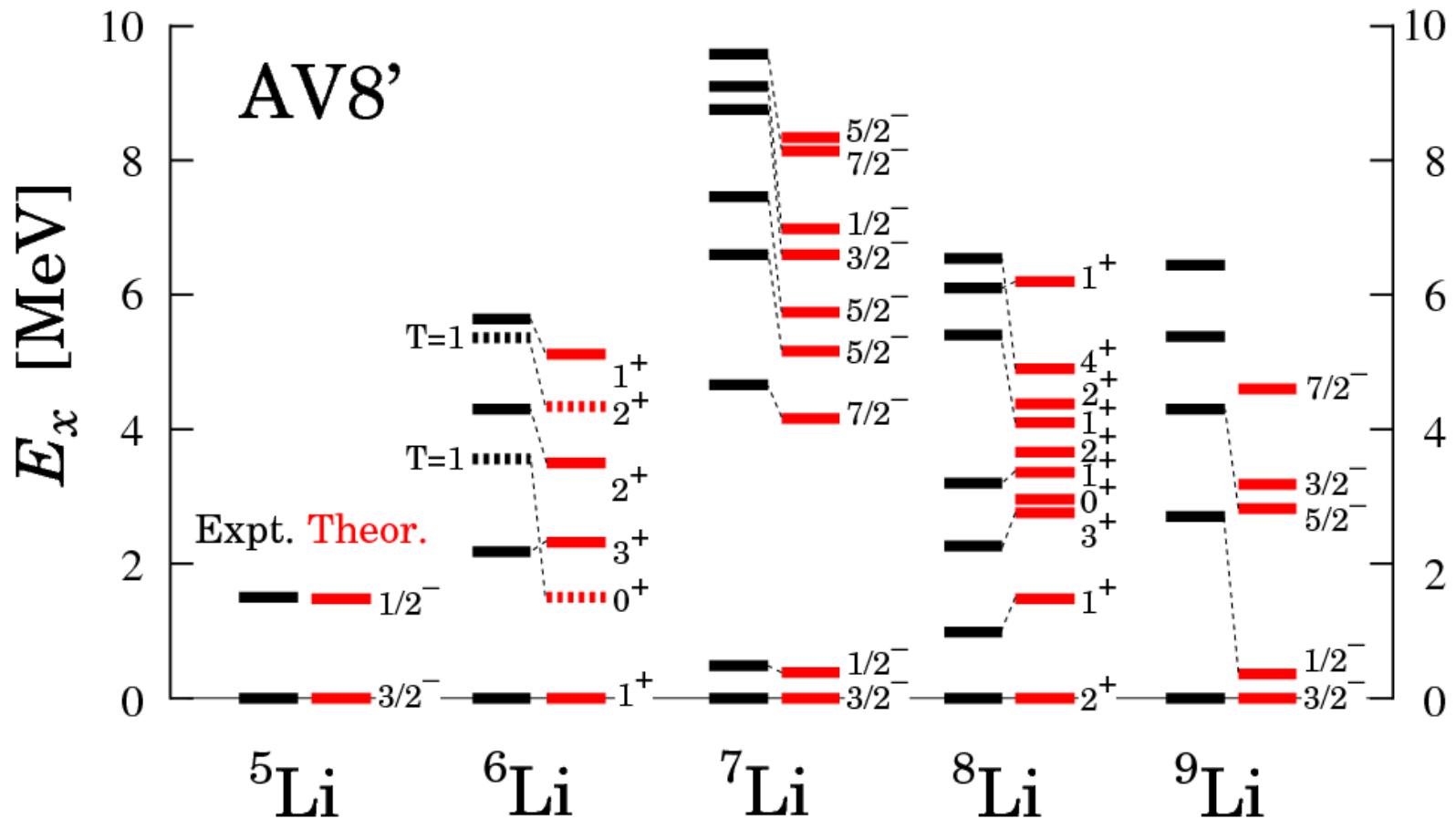


- Bound state app.
- No continuum
- No V_{NNN}
- Excitation energy spectra are reproduced well

^{5-9}Li with TOSM+UCOM

- Excitation energies in MeV

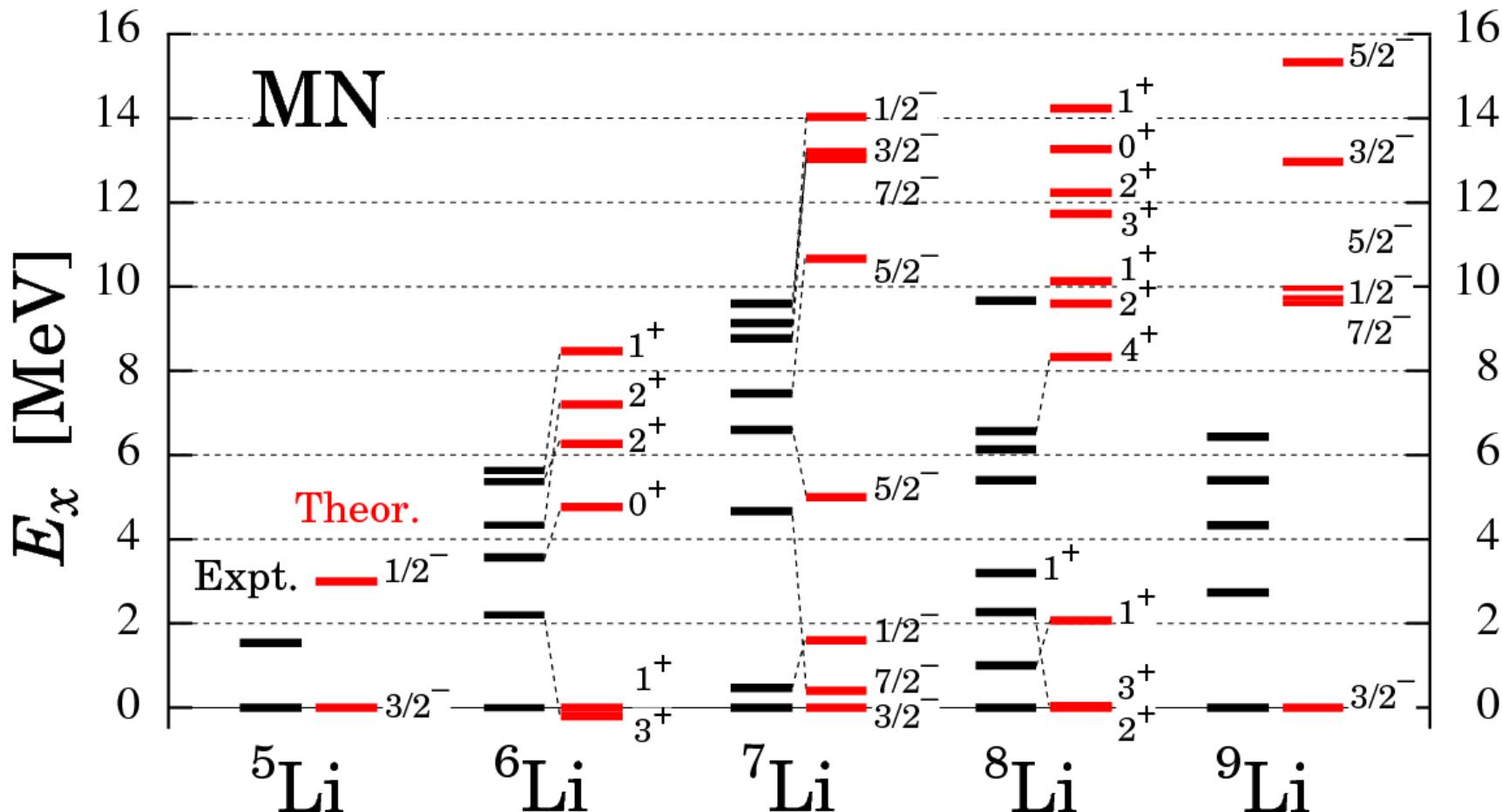
TM, A. Umeya, H. Toki, K. Ikeda
PRC86(2012) 024318



^{5-9}Li with TOSM

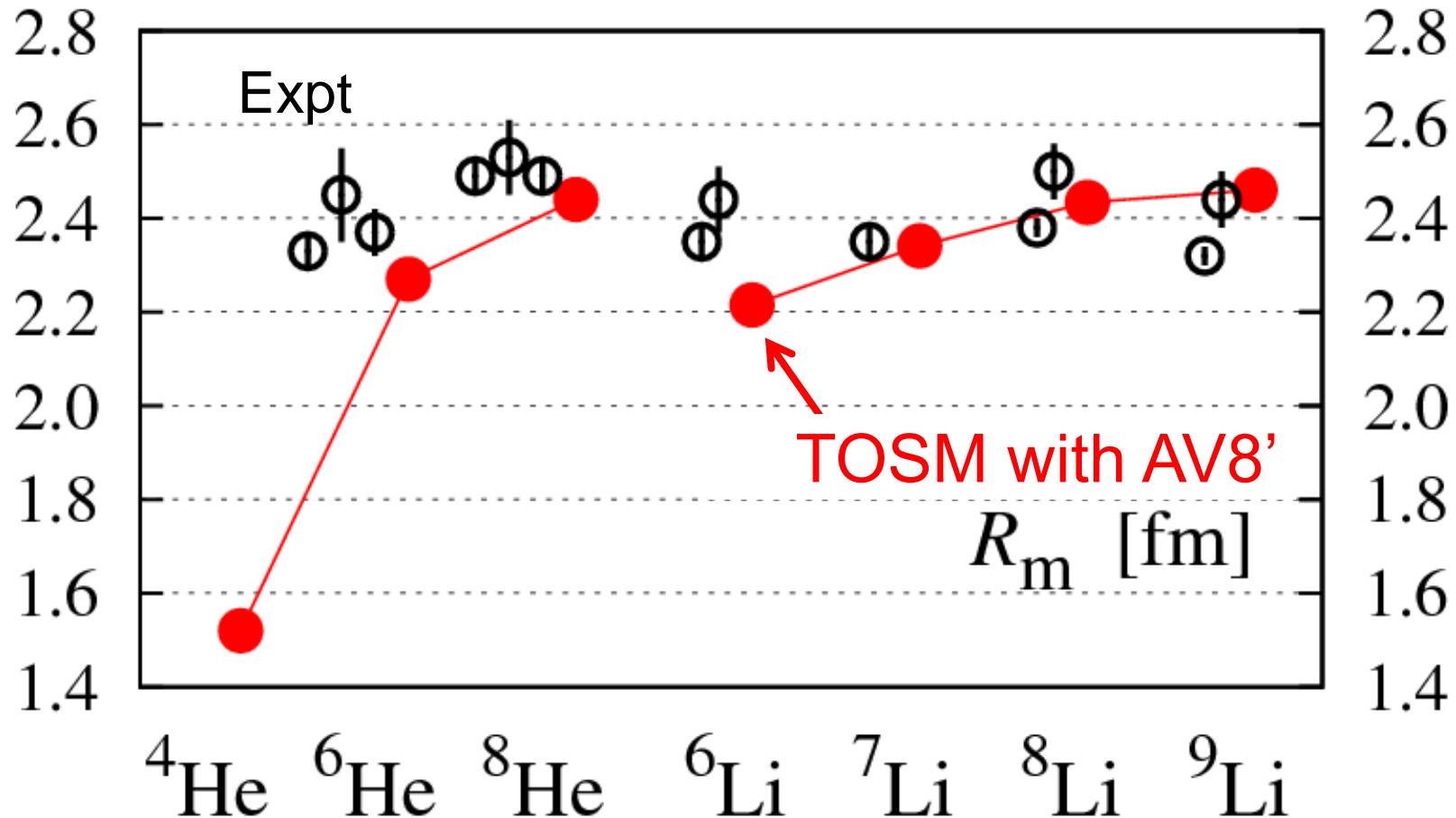
Minnesota force (Central+LS)

- Excitation energies in MeV



- Too large excitation energy

Matter radius of He & Li isotopes



I. Tanihata et al., PLB289('92)261

O. A. Kiselev et al., EPJA 25, Suppl. 1('05)215.

A. Dobrovolsky, NPA 766(2006)1

G. D. Alkhazov et al., PRL78('97)2313

P. Mueller et al., PRL99(2007)252501

Configurations of ${}^4\text{He}$ with AV8'

$(0s_{1/2})^4$	83.0 %
$(0s_{1/2})^{-2} {}_{\text{JT}}(p_{1/2})^2 {}_{\text{JT}}$ $JT=10$ $JT=01$	2.6 0.1 2.3 1.9
$(0s_{1/2})^{-2} {}_{10}(1s_{1/2})({d}_{3/2})_{10}$	
$(0s_{1/2})^{-2} {}_{10}(p_{3/2})({f}_{5/2})_{10}$	
Radius [fm]	1.54

TM, H. Toki, K. Ikeda
PTP121(2009)511

• deuteron correlation
with $(J, T)=(1, 0)$

Cf. R.Schiavilla et al. (VMC)
PRL98(2007)132501
R. Subedi et al. (JLab)
Science320(2008)1476

${}^{12}\text{C}(e, e' pN)$

S.C.Simpson, J.A.Tostevin
PRC83(2011)014605

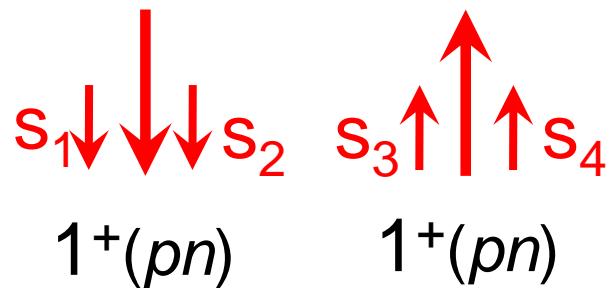
${}^{12}\text{C} \rightarrow {}^{10}\text{B} + pn$

- ${}^4\text{He}$ contains $p_{1/2}$ of “ pn -pair”
 - Same feature in ${}^5\text{He}-{}^8\text{He}$ ground state

Selectivity of the tensor coupling in ^4He

$$0\text{p}0\text{h} : (0s)_{00}^4 \supset (0s)_{10}^2 (0s)_{10}^2$$

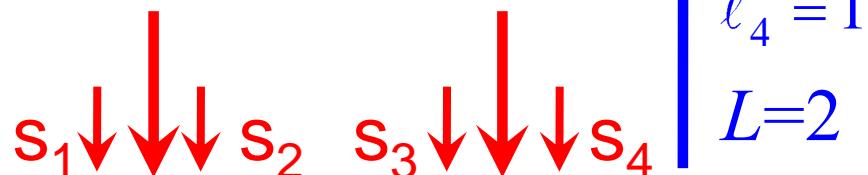
$$\ell_1 = \ell_2 = \ell_3 = \ell_4 = 0$$



Selectivity of
tensor operator
 $\Delta L=2, \Delta S=2$

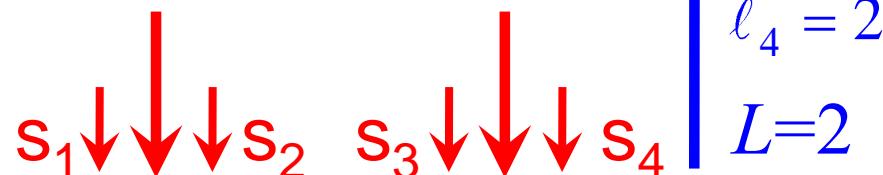
$$2\text{p}2\text{h} : (0s)_{10}^2 (0p_{1/2})_{10}^2$$

$$\ell_1 = \ell_2 = 0$$

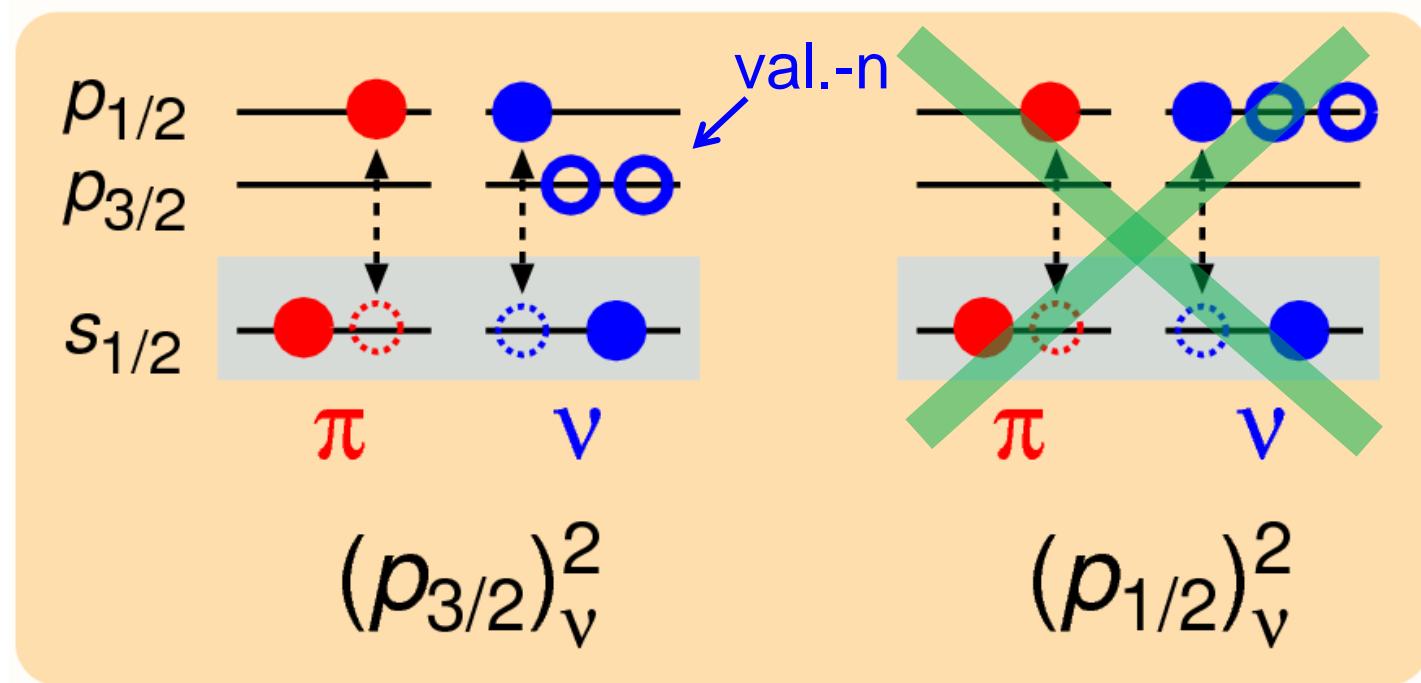


$$2\text{p}2\text{h} : (0s)_{10}^2 [(1s)(0d_{3/2})]_{10}$$

$$\ell_1 = \ell_2 = 0$$



Tensor correlation in ${}^6\text{He}$



Ground state

halo state (0^+)

Excited state

Tensor correlation is **suppressed**
due to Pauli-Blocking

^6He : Hamiltonian component in TOSM

- Difference from ^4He in MeV

^6He	0^+_1	0^+_2
n^2 config	$(p_{3/2})^2$	$(p_{1/2})^2$
$\Delta\text{Kin.}$	<u>53.0</u>	<u>34.3</u>
$\Delta\text{Central}$	-27.8	-14.1
ΔTensor	<u>-12.0</u>	<u>-0.2</u>
ΔLS	-4.0	2.1

$b_{\text{hole}}=1.5 \text{ fm}$

$\hbar\omega=18.4 \text{ MeV}$

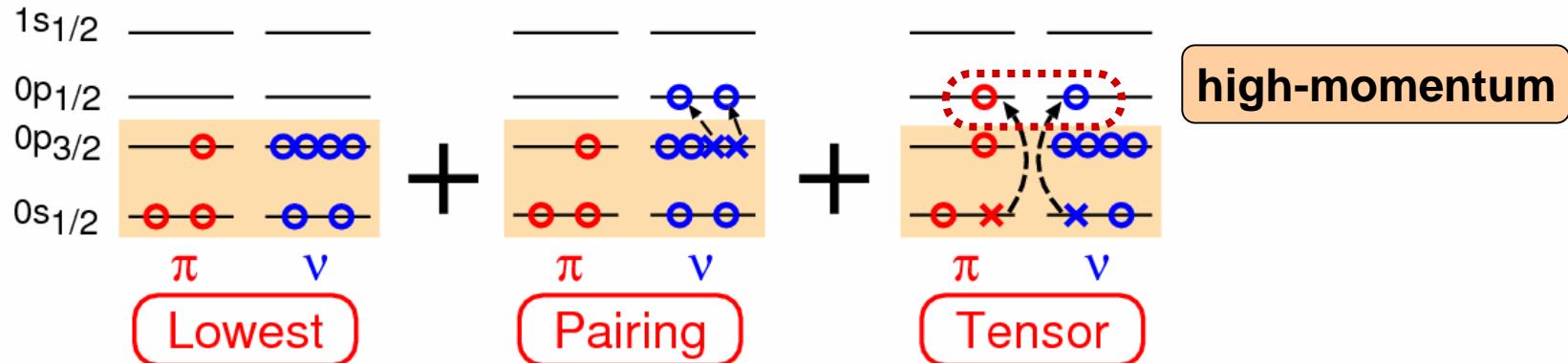
LS splitting
energy in ^6He

same trend
in ^{5-8}He , $^{10,11}\text{Li}$

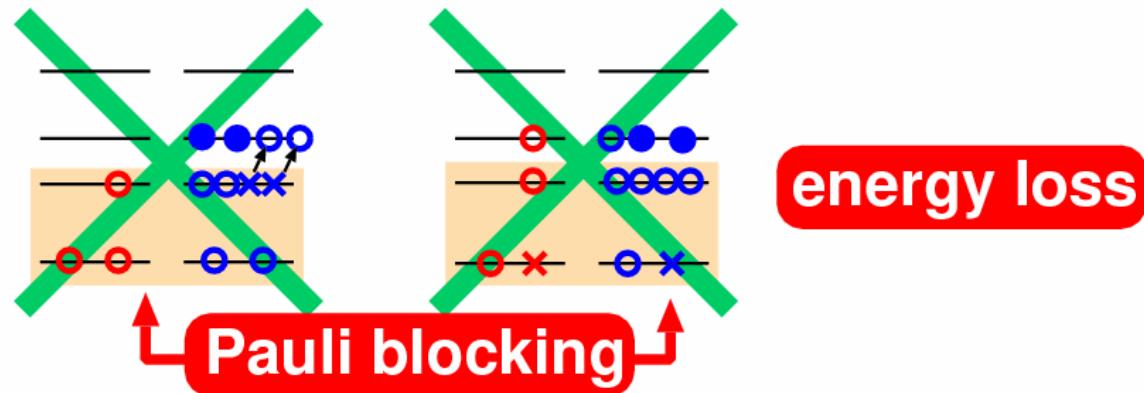
Halo formation with
large 1s-wave in ^{11}Li

Effects of tensor & pairing correlations in ^{11}Li

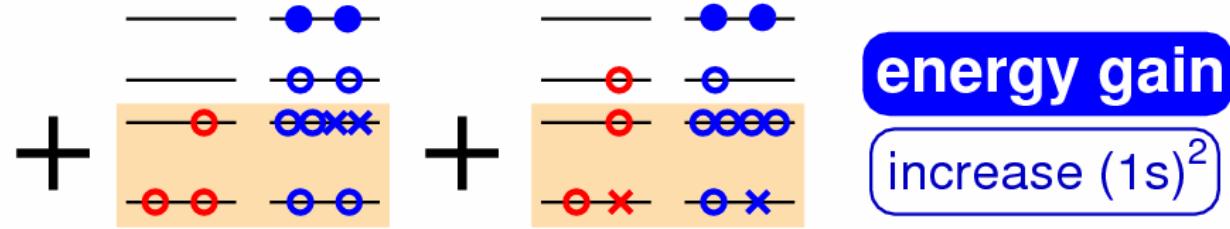
^9Li
GS



^{11}Li
(p^2)



^{11}Li
(s^2)

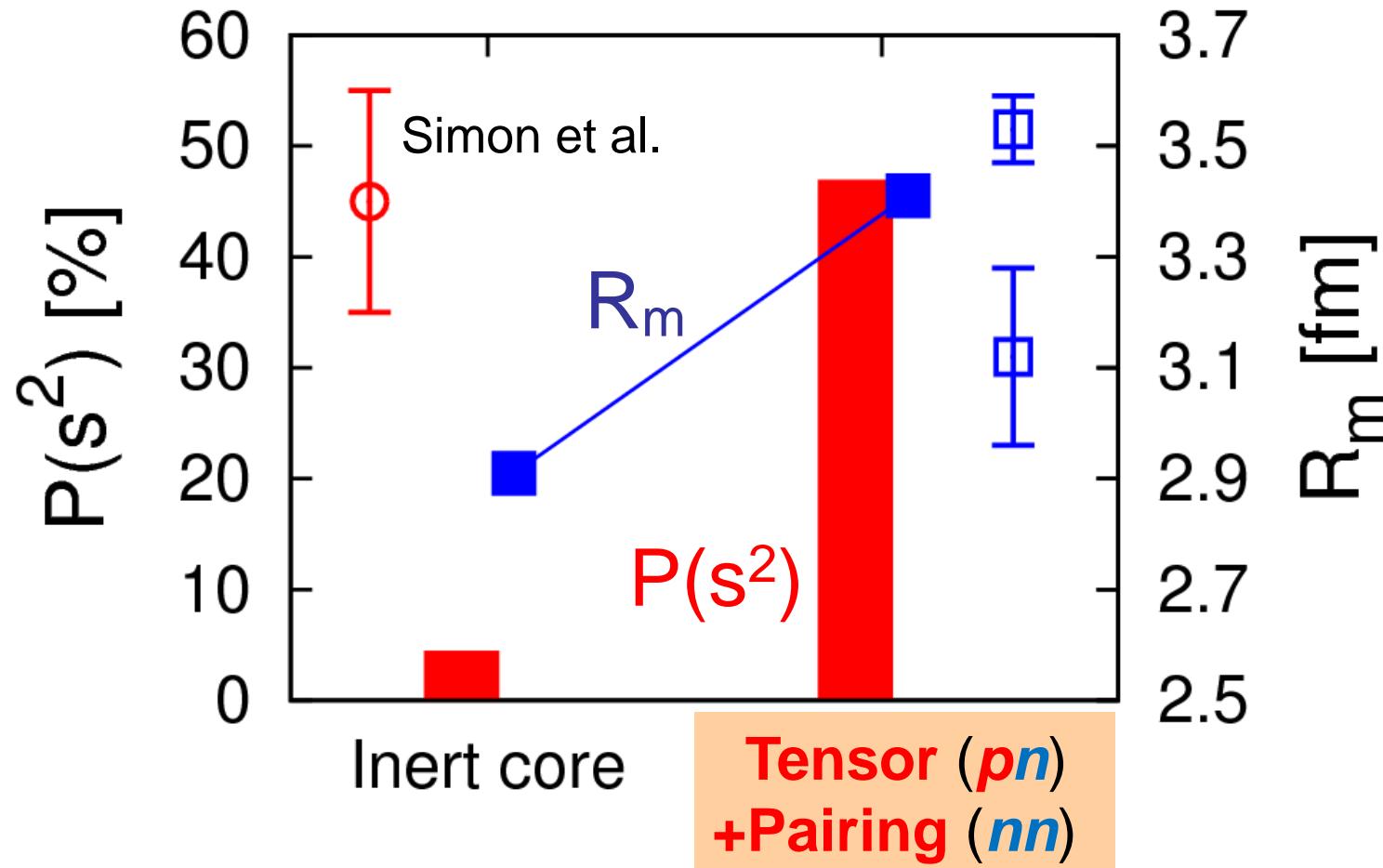


Exp ~ 50%

Pairing-blocking :

K.Kato,T.Yamada,K.Ikeda,PTP101('99)119, Masui,S.Aoyama,TM,K.Kato,K.Ikeda,NPA673('00)207.
TM,S.Aoyama,K.Kato,K.Ikeda,PTP108('02)133, H.Sagawa,B.A.Brown,H.Esbensen,PLB309('93)1.

^{11}Li properties ($S_{2n}=0.31$ MeV)



Pairing correlation between halo neutrons couples $(0p)^2$ and $(1s)^2$

TM, K.Kato, H.Toki, K.Ikeda, PRC76(2007)024305

TM, Y.Kikuchi, K.Kato, H.Toki, K.Ikeda, PTP119(2008)561

Li isotopes: Ground state configurations

	<i>p-shell Config.</i>	Weight	
<i>LS</i>	${}^6\text{Li } (1^+, T=0)$	$(0p_{1/2})(0p_{3/2})$	43% $S=1$
<i>jj</i>	${}^6\text{Li } (0^+, T=1)$	$(0p_{3/2})^2$	72% IAS of ${}^6\text{He}$
<i>jj</i>	${}^7\text{Li } (3/2^-)$	$(0p_{3/2})^3$	48%
<i>jj</i>	${}^8\text{Li } (2^+)$	$(0p_{3/2})^4$	41%
<i>jj</i>	${}^9\text{Li } (3/2^-)$	$(0p_{3/2})^5$	46%

- ${}^6\text{Li}_{\text{gs}}$... *LS* coupling → Indication of $\alpha+d$ clustering
- ${}^{7-9}\text{Li}$... *jj* coupling

Summary

- **TOSM+UCOM** using V_{bare} .
- Reproduce the excitation energy spectra.
- ${}^4\text{He}$ contains “***pn-pair of $p_{1/2}$*** ” than $p_{3/2}$.
- **He isotopes with $p_{3/2}$** has large contributions of V_{tensor} & Kinetic energy.
- ${}^6\text{Li}_{\text{gs}}$: ***LS coupling***, indication of $\alpha+d$ cluster.
- ${}^{7-9}\text{Li}$: ***jj coupling***

TM, A. Umeya, H. Toki, K. Ikeda, PRC84 (2011) 034315
TM, A. Umeya, H. Toki, K. Ikeda, PRC86 (2012) 024318