

# **Light-quark baryon spectroscopy from ANL-Osaka dynamical coupled-channels analysis**

**Hiroyuki Kamano  
(RCNP, Osaka U.)**

# Outline

## 1. $N^*$ and $\Delta^*$ spectroscopy via ANL-Osaka Dynamical Coupled-Channels (DCC) analysis of $\pi N$ , $\gamma N$ , and $eN$ reactions

→ HK, Nakamura, Lee, Sato, PRC88(2013)035209

(See also talk by Toru Sato in NSTAR2013:

[http://ific.uv.es/nucth/nstar/talks/P1\\_Sato.pdf](http://ific.uv.es/nucth/nstar/talks/P1_Sato.pdf))

## 2. $\Lambda^*$ and $\Sigma^*$ spectroscopy via ANL-Osaka DCC analysis of $K^- p$ reactions

→ HK, Nakamura, Lee, Sato, PRC90(2014)065204; in preparation.

# ANL-Osaka DCC approach to $N^*$ and $\Delta^*$

Dynamical coupled-channels model [Matsuyama, Sato, Lee, Phys. Rep. 439(2007)193]

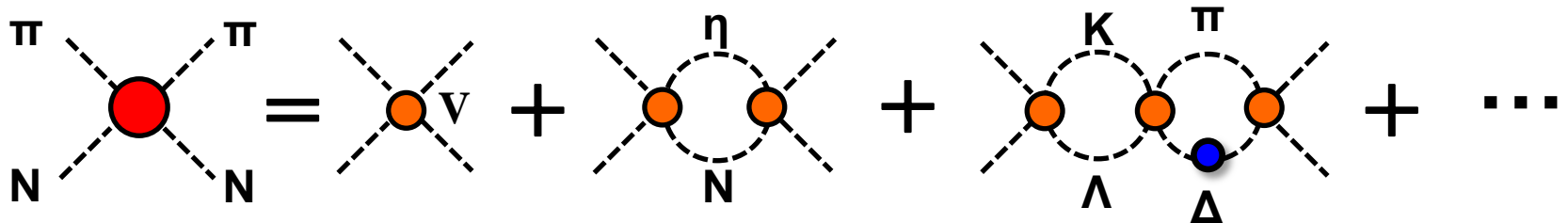
$$T_{a,b}^{(LSJ)}(p_a, p_b; E) = V_{a,b}^{(LSJ)}(p_a, p_b; E) + \underbrace{\sum_c}_{\text{CC effect}} \underbrace{\int_0^\infty q^2 dq}_{\text{off-shell effect}} V_{a,c}^{(LSJ)}(p_a, q; E) G_c(q; E) T_{c,b}^{(LSJ)}(q, p_b; E)$$

$$a, b, c = (\gamma^{(*)}N, \pi N, \eta N, \boxed{\pi\Delta, \sigma N, \rho N}, K\Lambda, K\Sigma, \dots)$$

$\pi\pi N$

- ✓ Summing up all possible transitions between reaction channels !!  
(→ satisfies **multichannel two-** and **three-body unitarity**)

e.g.)  $\pi N$  scattering



- ✓ **Momentum integral** takes into account **off-shell rescattering effects** in the intermediate processes.

# ANL-Osaka DCC approach to $N^*$ and $\Delta^*$

Dynamical coupled-channels model [Matsuyama, Sato, Lee, Phys. Rep. 439(2007)193]

$$T_{a,b}^{(LSJ)}(p_a, p_b; E) = V_{a,b}^{(LSJ)}(p_a, p_b; E) + \underbrace{\sum_c \int_0^\infty q^2 dq V_{a,c}^{(LSJ)}(p_a, q; E) G_c(q; E) T_{c,b}^{(LSJ)}(q, p_b; E)}_{\substack{\text{CC effect} \\ \text{off-shell effect}}}$$

$$a, b, c = (\gamma^{(*)}N, \pi N, \eta N, \boxed{\pi\Delta, \sigma N, \rho N}, K\Lambda, K\Sigma, \dots)$$

$\pi\pi N$

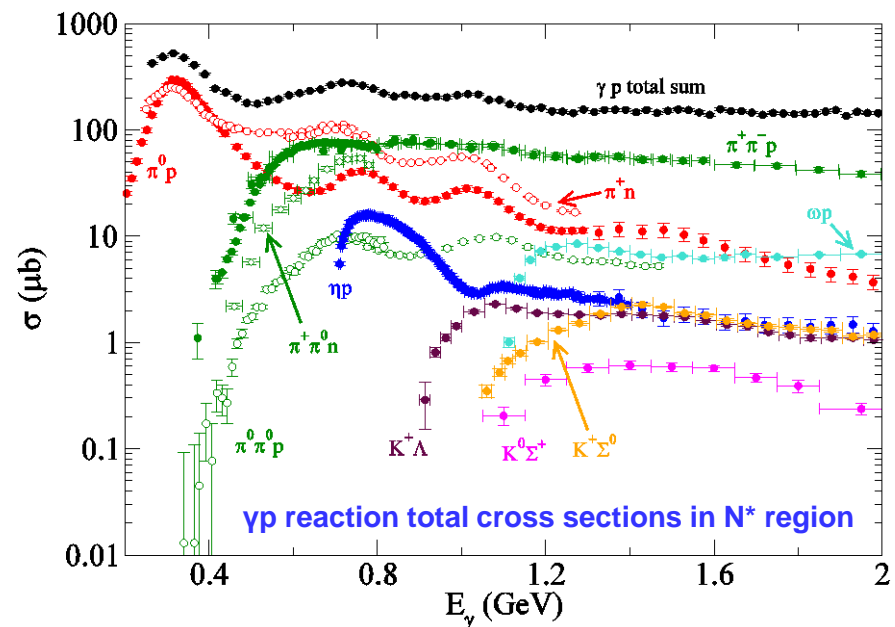
← Region our model can cover →

Latest published model:

HK, Nakamura, Lee, Sato, PRC88(2013)035209

Constructed by **simultaneous** analysis of

- $\pi N$  SAID PW amps. ( $W < 2.3$  GeV)
- $\pi\pi \rightarrow \eta N, K\Lambda, K\Sigma$  ( $W < 2.1$  GeV)
- $\gamma p \rightarrow \pi N, \eta N, K\Lambda, K\Sigma$  ( $W < 2.1$  GeV)

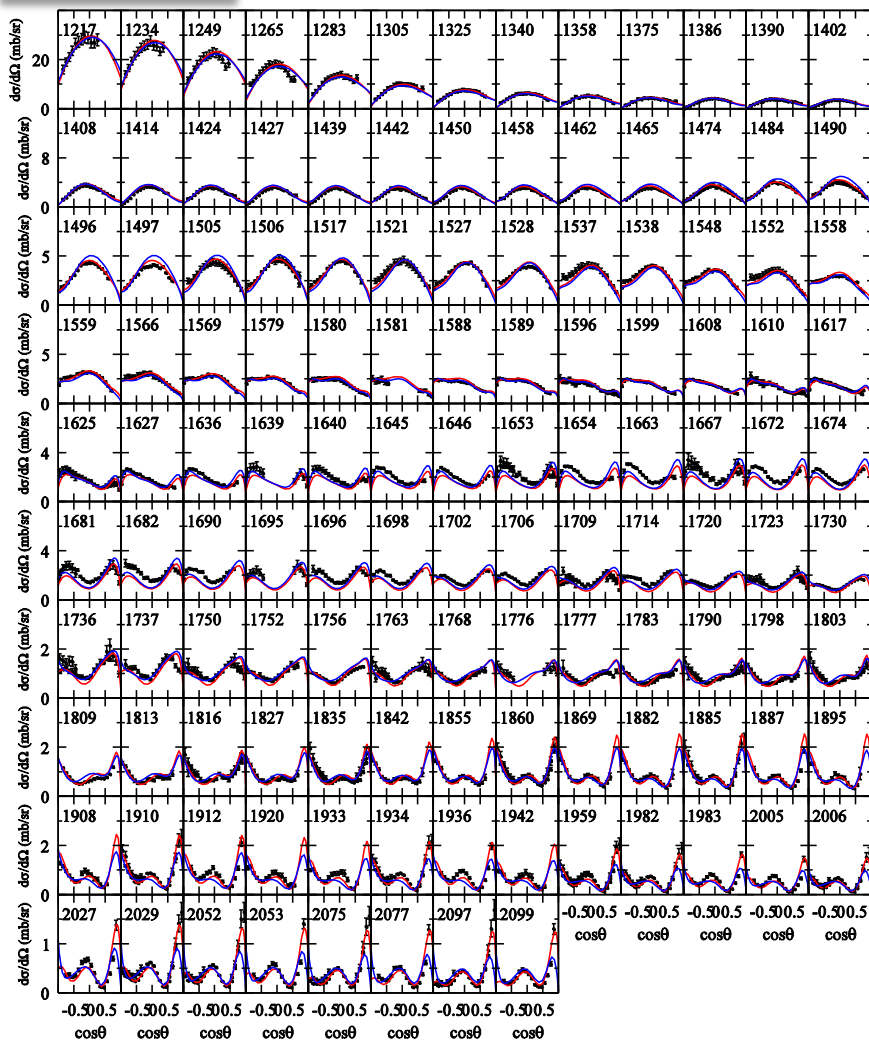


# ANL-Osaka DCC approach to $N^*$ and $\Delta^*$

HK, Nakamura, Lee, Sato, PRC88(2013)035209 (with update)

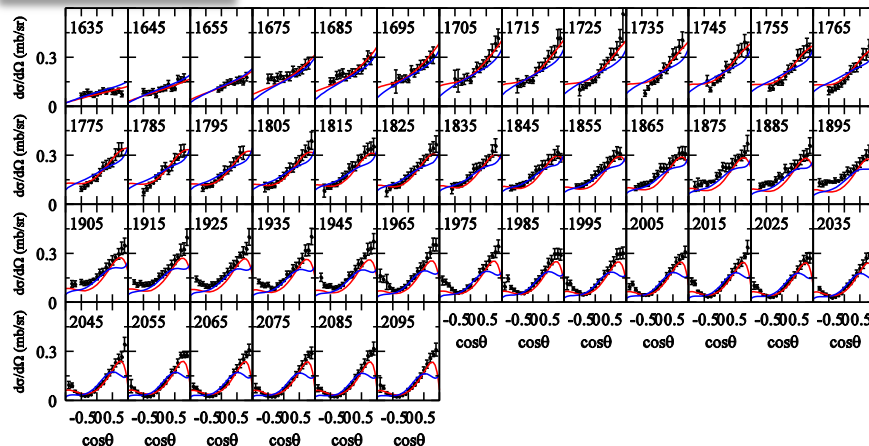
$\gamma p \rightarrow \pi^0 p$

$d\sigma/d\Omega$  for  $W < 2.1$  GeV



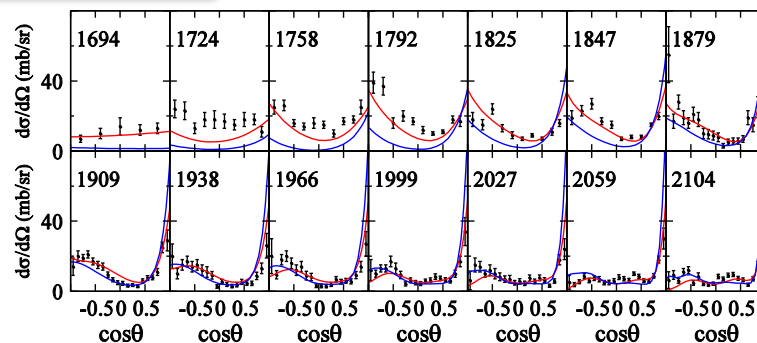
$\gamma p \rightarrow K^+ \Lambda$

$d\sigma/d\Omega$  for  $W < 2.1$  GeV



$\pi^- p \rightarrow K^0 \Sigma^0$

$d\sigma/d\Omega$  for  $W < 2.1$  GeV



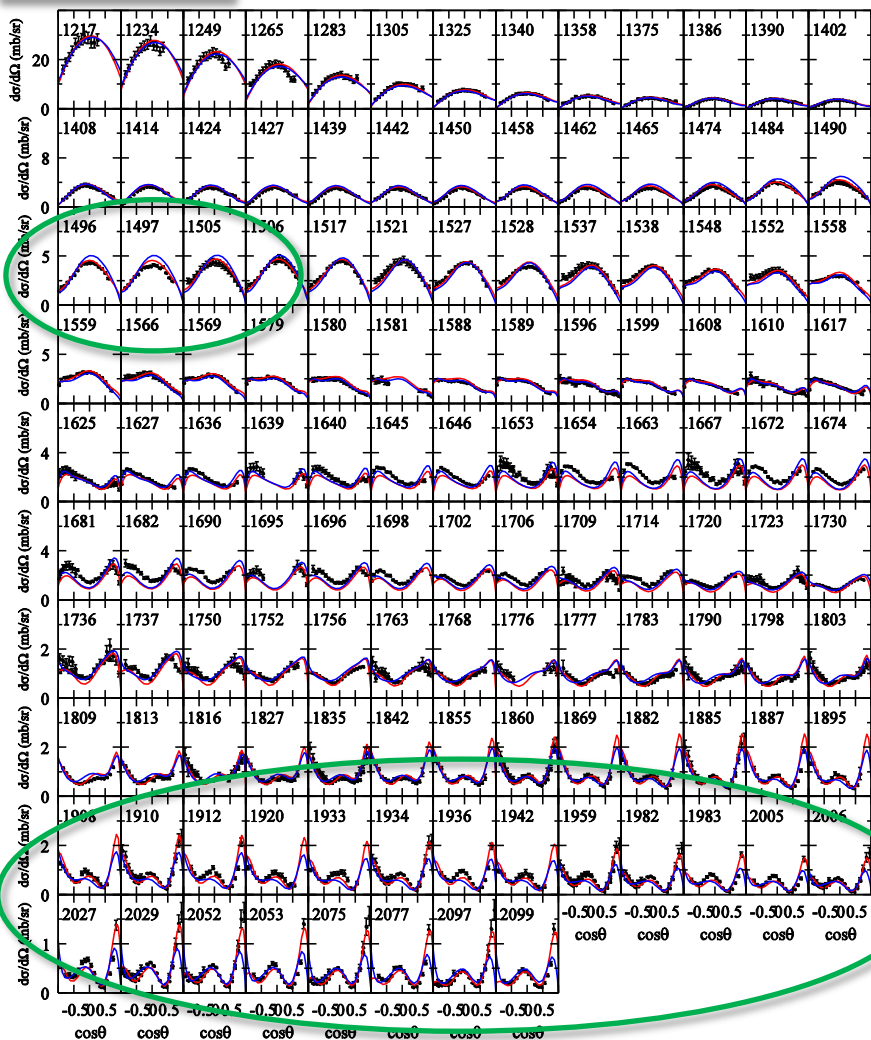
Red: minor updated ver.  
Blue: PRC88(2013)035209

# ANL-Osaka DCC approach to $N^*$ and $\Delta^*$

HK, Nakamura, Lee, Sato, PRC88(2013)035209 (with update)

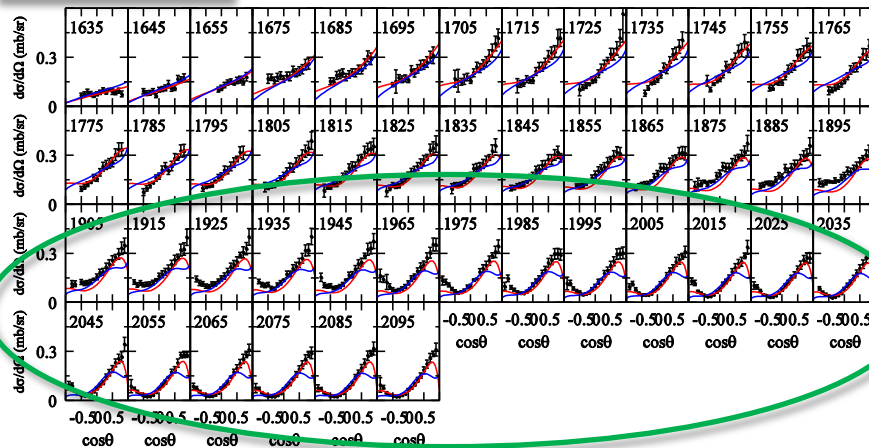
$\gamma p \rightarrow \pi^0 p$

$d\sigma/d\Omega$  for  $W < 2.1$  GeV



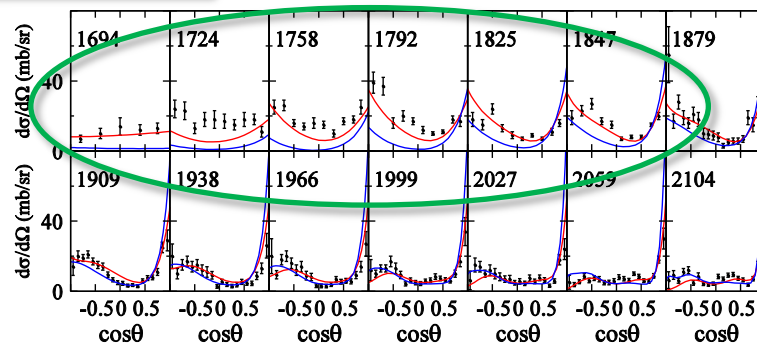
$\gamma p \rightarrow K^+ \Lambda$

$d\sigma/d\Omega$  for  $W < 2.1$  GeV



$\pi^+ p \rightarrow K^0 \Sigma^0$


$d\sigma/d\Omega$  for  $W < 2.1$  GeV

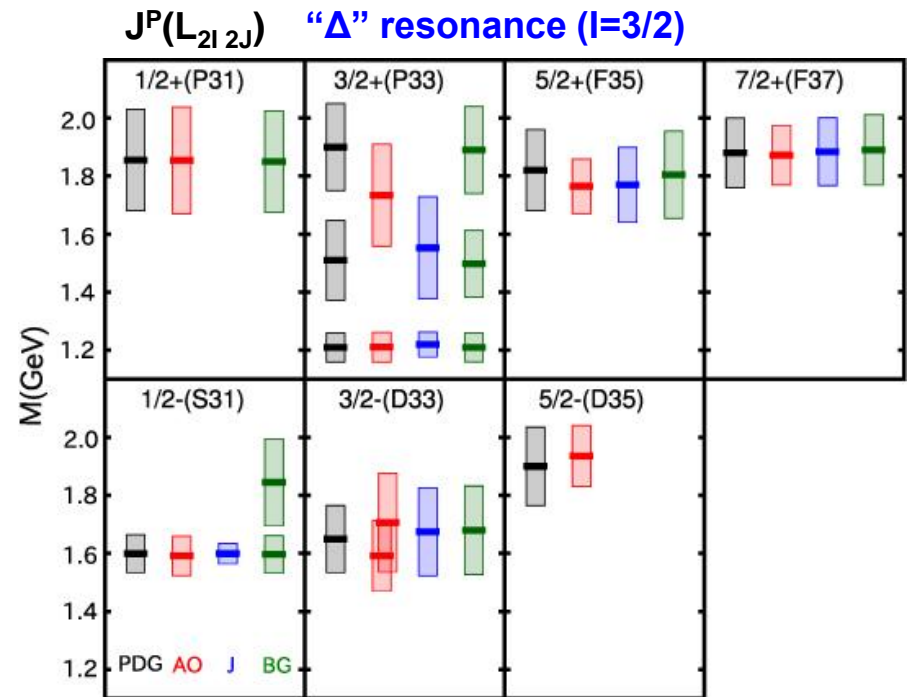
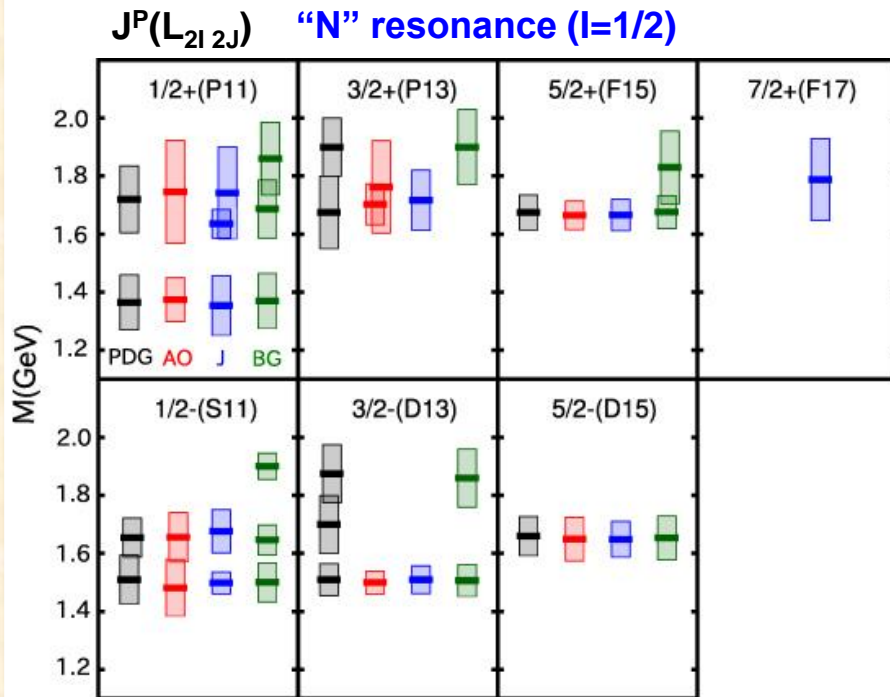


Red: minor updated ver.  
Blue: PRC88(2013)035209

# Comparison of $N^*$ & $\Delta^*$ spectrum between multichannel analyses

HK, Nakamura, Lee, Sato, PRC88 (2013) 035209

$-2\text{Im}(M_R)$  (“width”)   $\text{Re}(M_R)$   $M_R$ : Resonance pole mass (complex)



PDG:  $4^*$  &  $3^*$  states assigned by PDG2012

AO : ANL-Osaka


J : Juelich [EPJA49(2013)44]

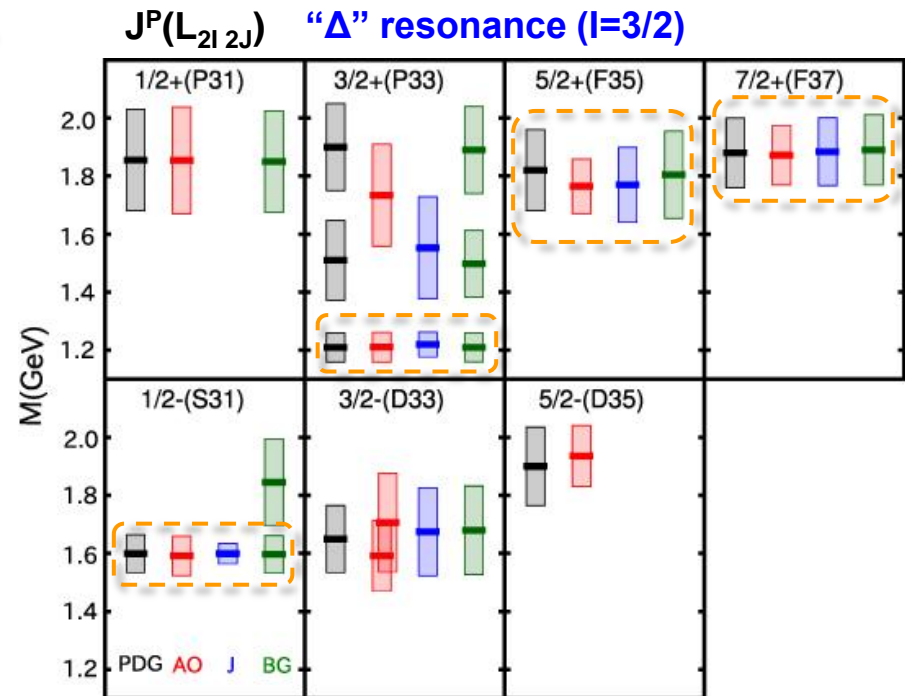
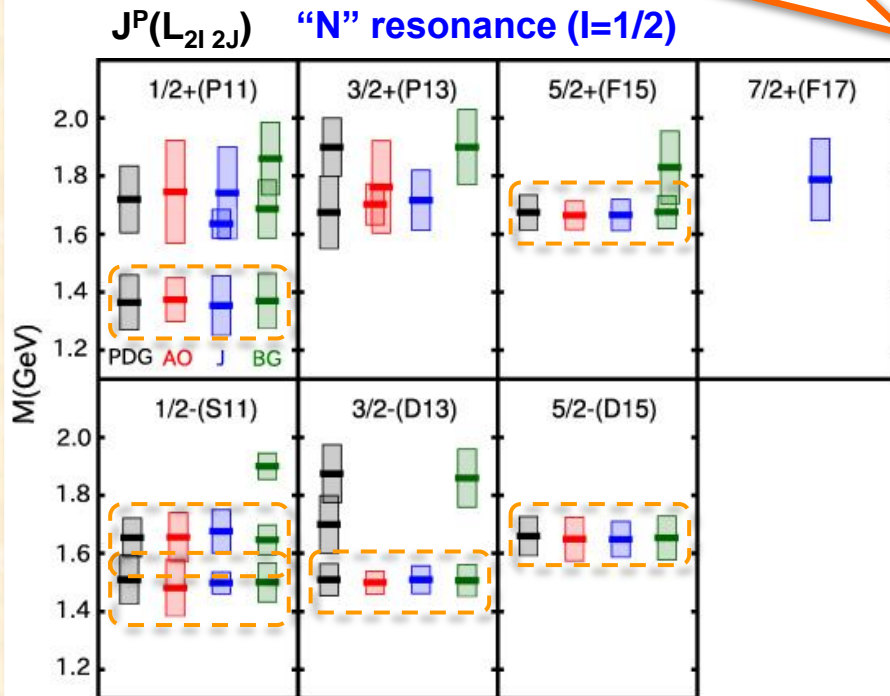
BG : Bonn-Gatchina [EPJA48(2012)5]

# Comparison of $N^*$ & $\Delta^*$ spectrum between multichannel analyses

HK, Nakamura, Lee, Sato, PRC88 (2013) 035209

Existence and mass spectrum are now well established for most low-lying resonances !!  
 (→ Next task: establish high-mass resonances)

$-2\text{Im}(M_R)$  ("width")   $\text{Re}(M_R)$   $M_R$ : Resonance pole mass (complex)



PDG: 4\* & 3\* states assigned by PDG2012

AO : ANL-Osaka

J : Juelich [EPJA49(2013)44]

BG : Bonn-Gatchina [EPJA48(2012)5]



# Necessity of inelastic reaction data for establishing high-mass $N^*$ and $\Delta^*$ spectrum

To establish the spectrum of **high-mass resonances**, inelastic reaction (particularly **double pion production**) data are highly desirable:

$\pi N, \gamma N \rightarrow \pi\pi N, K\Lambda, K\Sigma, \eta N, \eta' N, \omega N, \Phi N, \dots$

Measurements of

$\pi N \rightarrow \pi\pi N, \dots$  :

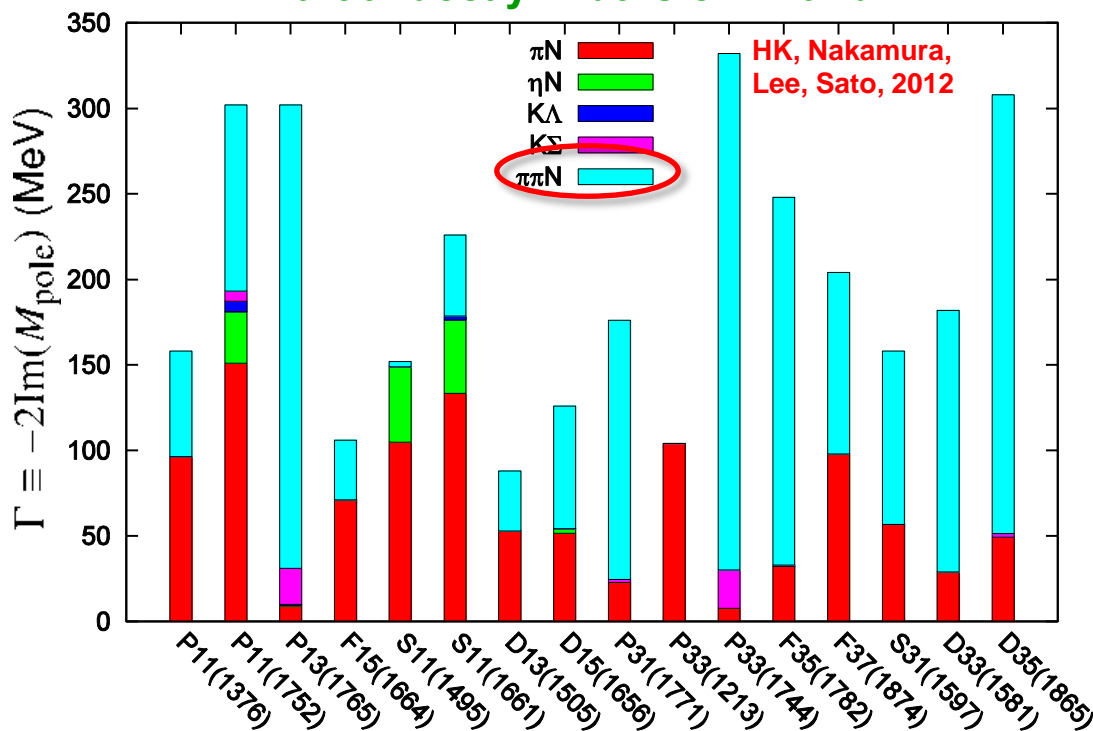
**HADES**

[→ Talk by W. Przygoda  
27th(Wed.) Plenary 27-2]

**J-PARC E45**

[→ Talk by K. Hosomi  
27th(Wed.) ParallelA 27-2]

Partial decay widths of  $N^*$  and  $\Delta^*$



# Necessity of inelastic reaction data for establishing high-mass $N^*$ and $\Delta^*$ spectrum

To establish the spectrum of **high-mass resonances**, inelastic reaction (particularly **double pion production**) data are highly desirable:

$\pi N, \gamma N \rightarrow \pi\pi N, K\Lambda, K\Sigma, \eta N, \eta' N, \omega N, \Phi N, \dots$

Measurements of

$\pi N \rightarrow \pi\pi N, \dots$  :

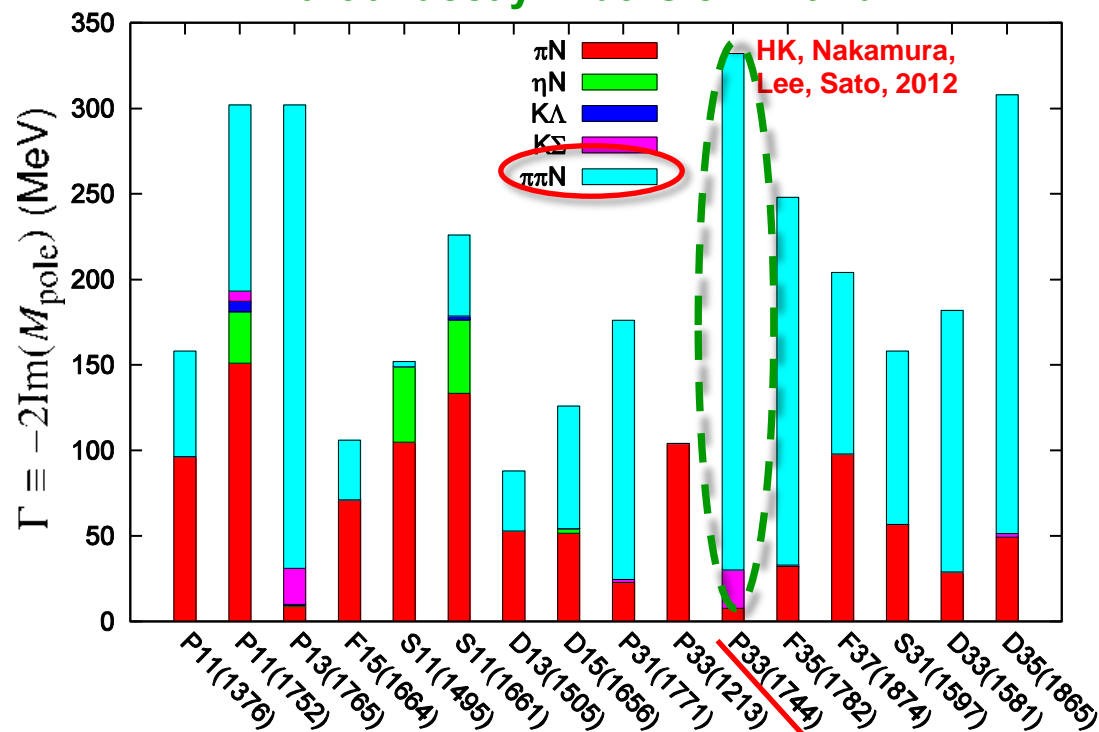
**HADES**

[→ Talk by W. Przygoda  
27th(Wed.) Plenary 27-2]

**J-PARC E45**

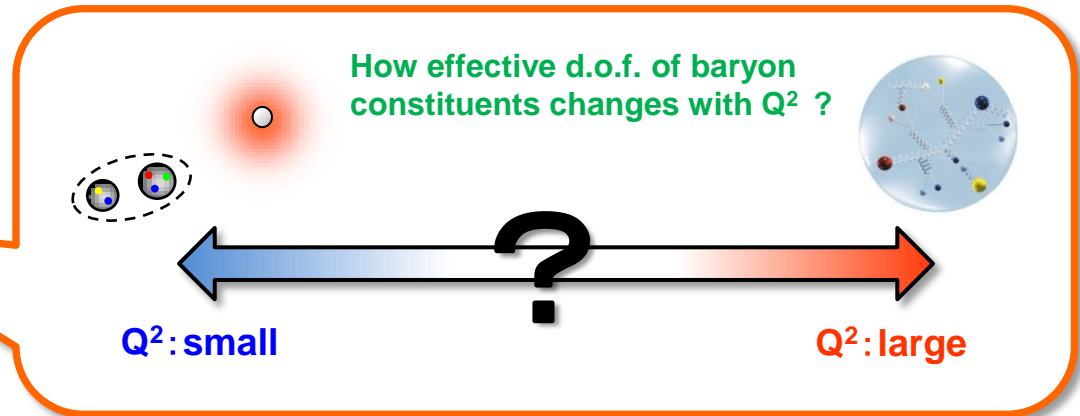
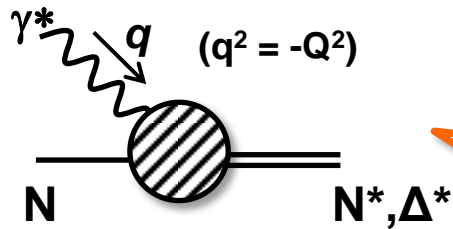
[→ Talk by K. Hosomi  
27th(Wed.) ParallelA 27-2]

Partial decay widths of  $N^*$  and  $\Delta^*$

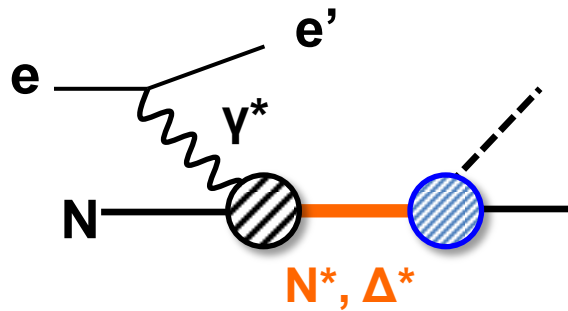


# Analysis of electroproduction reactions: Determining N-N\* e.m. transition form factors

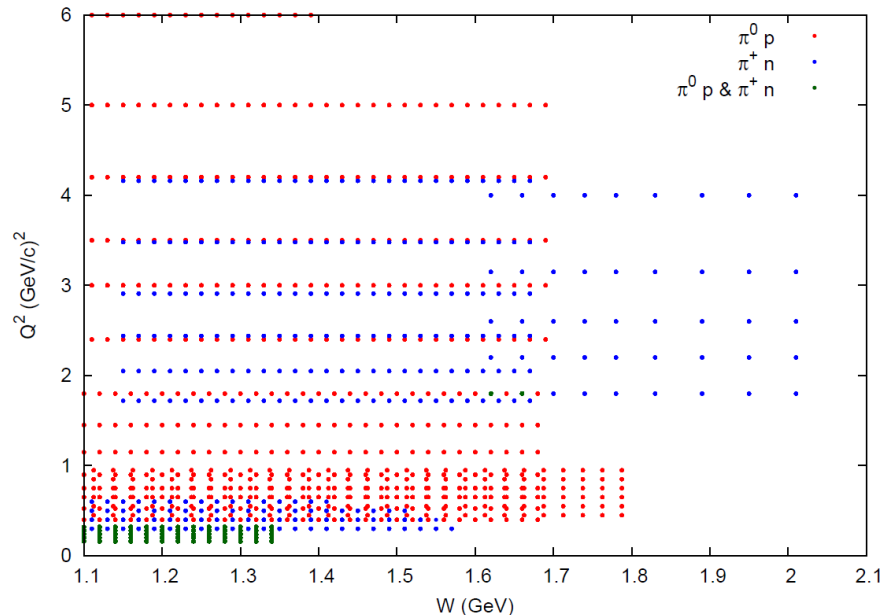
N-N\* e.m. transition form factors



Meson electro-productions:



CLAS database for  $1\pi$  electroproductions  
( $Q^2 < 6 \text{ GeV}^2$ )



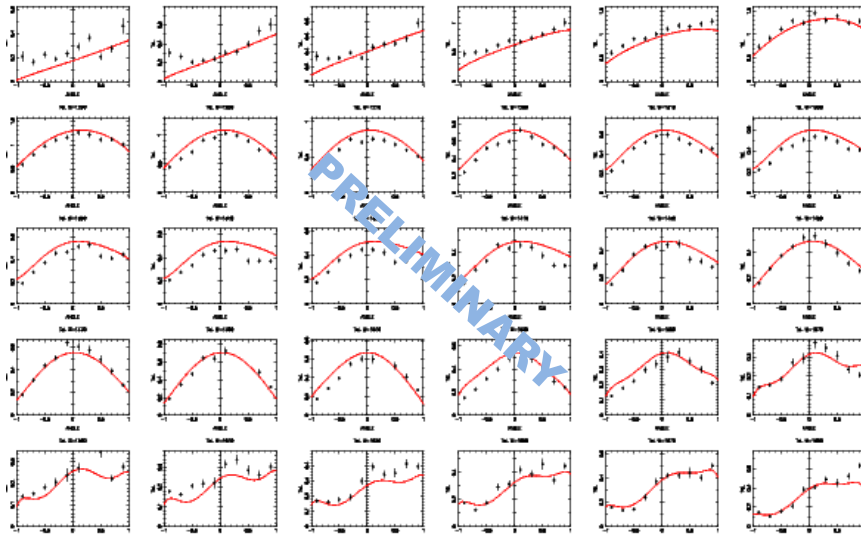
+  $K^+ \Lambda$ ,  $K^+ \Sigma^0$   
electro-  
production  
data

# Analysis of electroproduction reactions: Determining N-N\* e.m. transition form factors

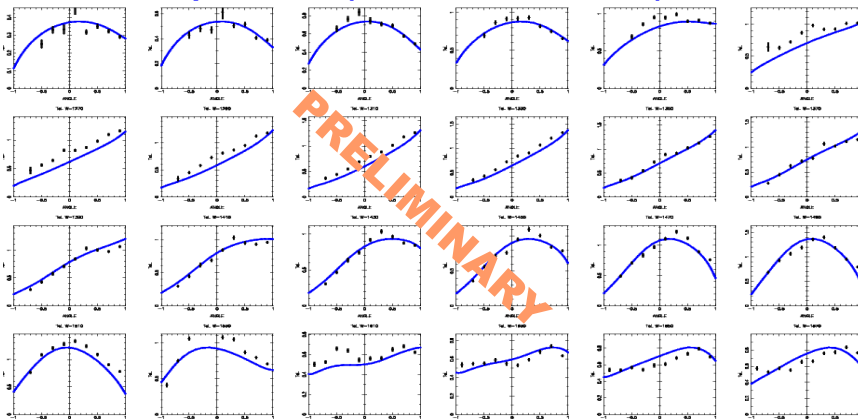
$$\sigma_T + \epsilon\sigma_L @ Q^2 = 2.42 \text{ (GeV/c)}^2$$

Structure functions  
are provided by  
K. Joo and C. Smith.

$ep \rightarrow e\pi^0 p$  ( $1.11 < W < 1.69$  GeV)



$ep \rightarrow e\pi^+ n$  ( $1.15 < W < 1.67$  GeV)



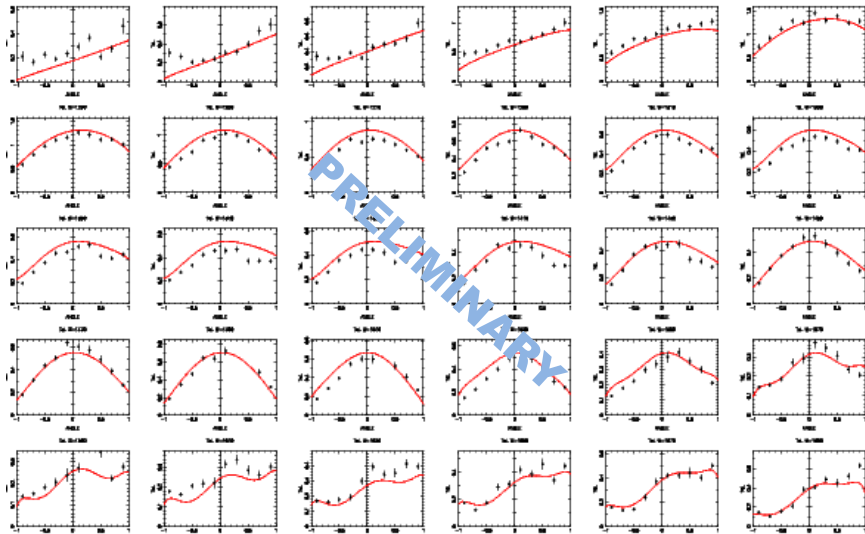
$\cos\theta$

# Analysis of electroproduction reactions: Determining N-N\* e.m. transition form factors

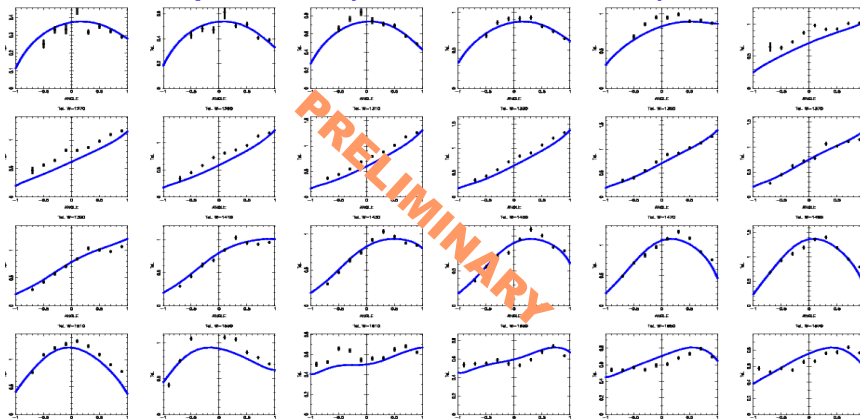
$$\sigma_T + \epsilon \sigma_L @ Q^2 = 2.42 \text{ (GeV/c)}^2$$

$ep \rightarrow e\pi^0 p$  ( $1.11 < W < 1.69$  GeV)

Structure functions  
are provided by  
K. Joo and C. Smith.

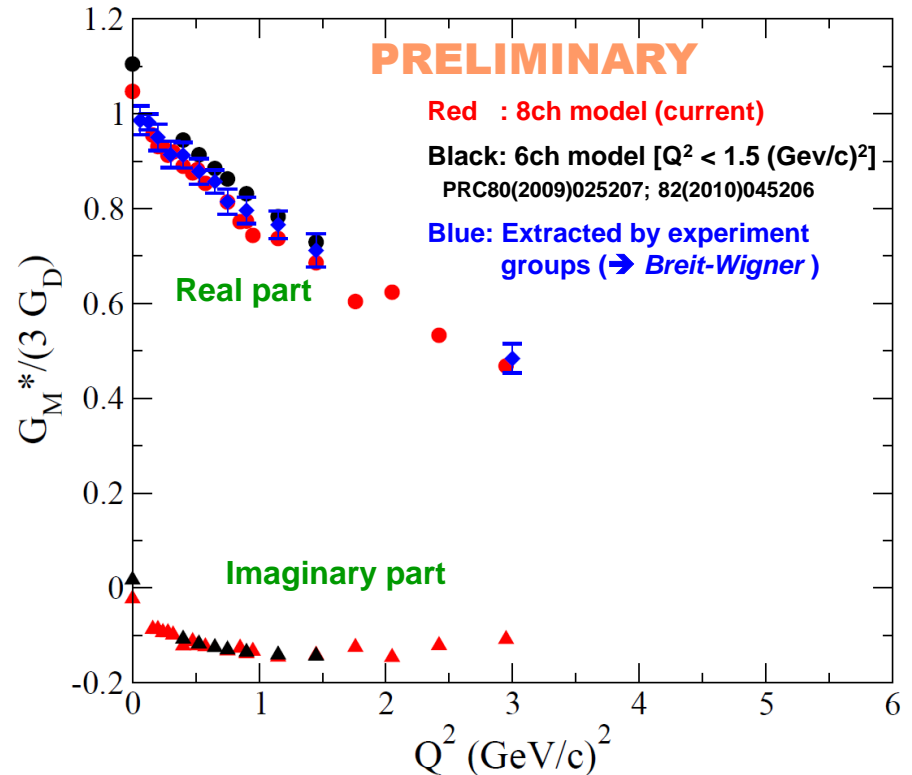


$ep \rightarrow e\pi^+ n$  ( $1.15 < W < 1.67$  GeV)



$\cos\theta$

$G_M(Q^2)$  for  $\gamma^* N \rightarrow \Delta(1^{\text{st}} \text{ P33})$  evaluated *at pole*

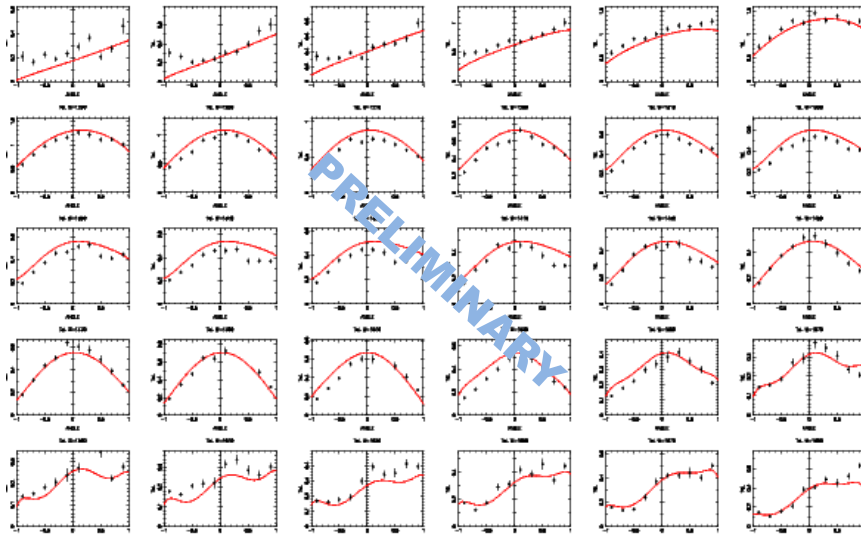


# Analysis of electroproduction reactions: Determining N-N\* e.m. transition form factors

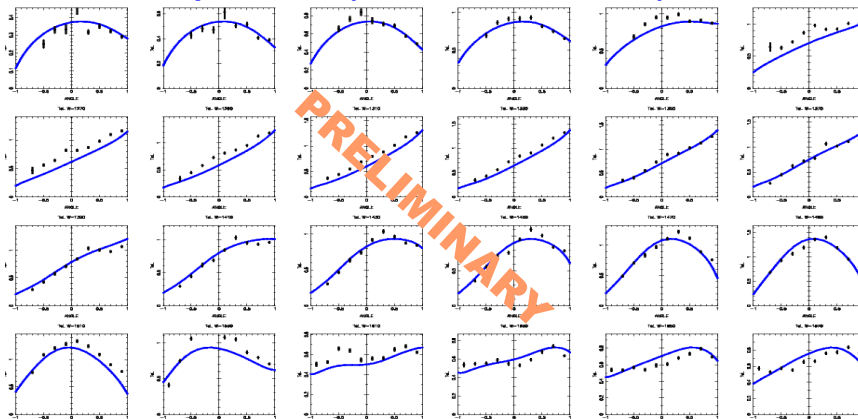
$$\sigma_T + \epsilon \sigma_L @ Q^2 = 2.42 \text{ (GeV/c)}^2$$

$ep \rightarrow e\pi^0 p$  ( $1.11 < W < 1.69$  GeV)

Structure functions  
are provided by  
K. Joo and C. Smith.

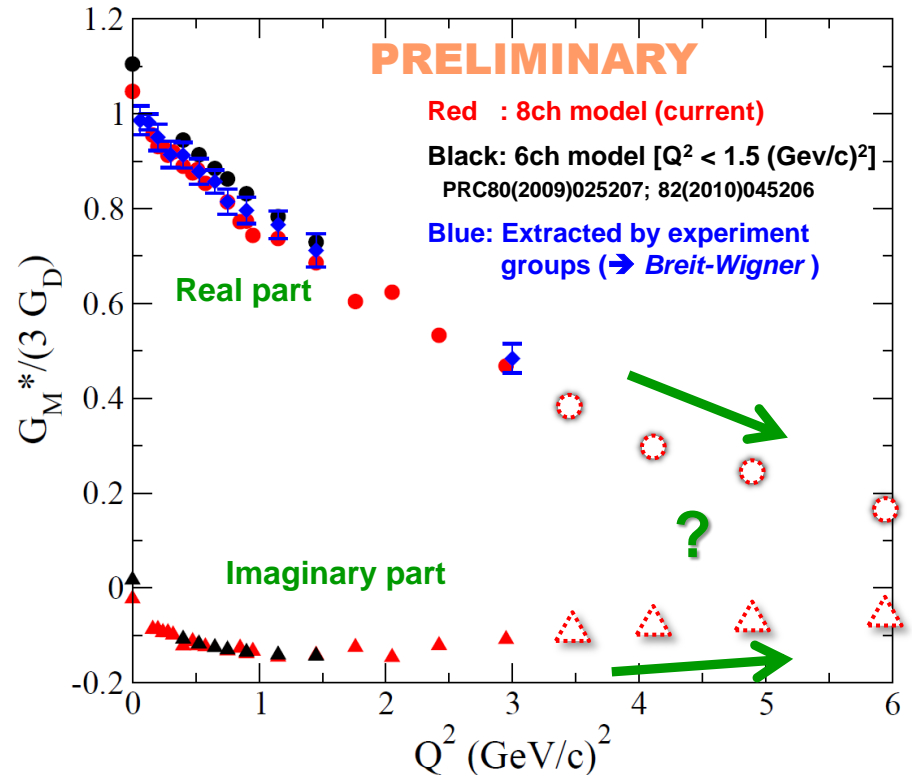


$ep \rightarrow e\pi^+ n$  ( $1.15 < W < 1.67$  GeV)



$\cos\theta$

$G_M(Q^2)$  for  $\gamma^* N \rightarrow \Delta(1^{\text{st}} \text{ P33})$  evaluated *at pole*

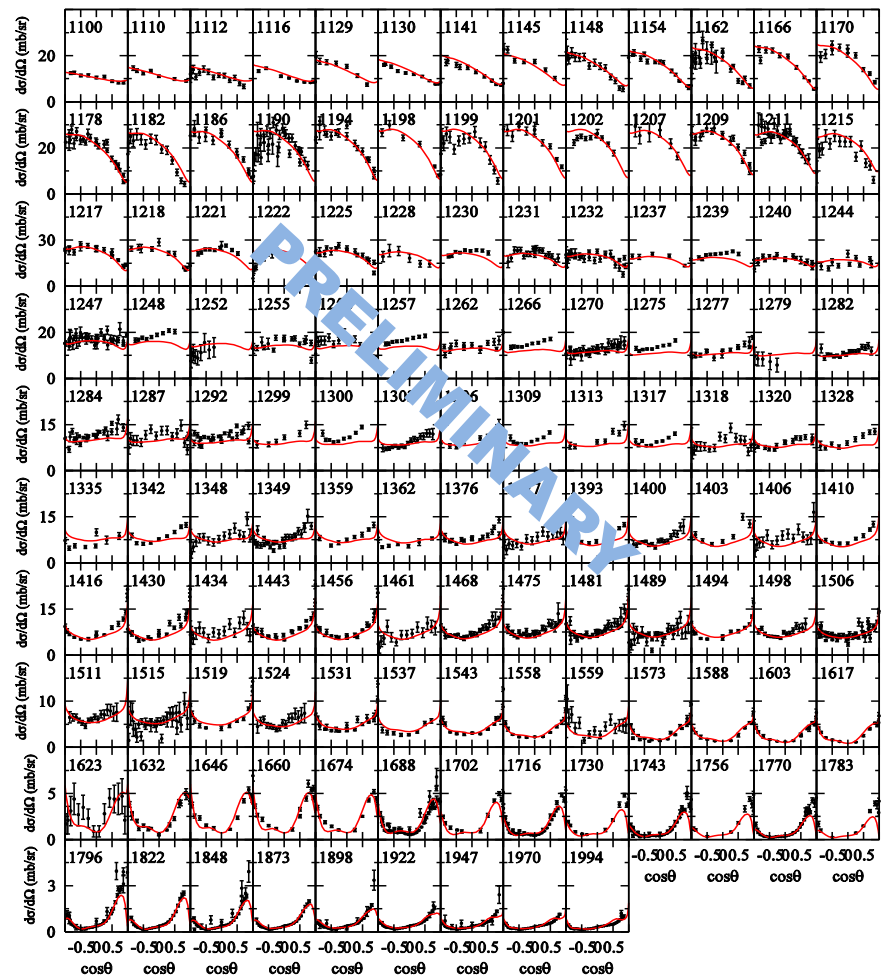


# Meson photoproductions off “neutron”

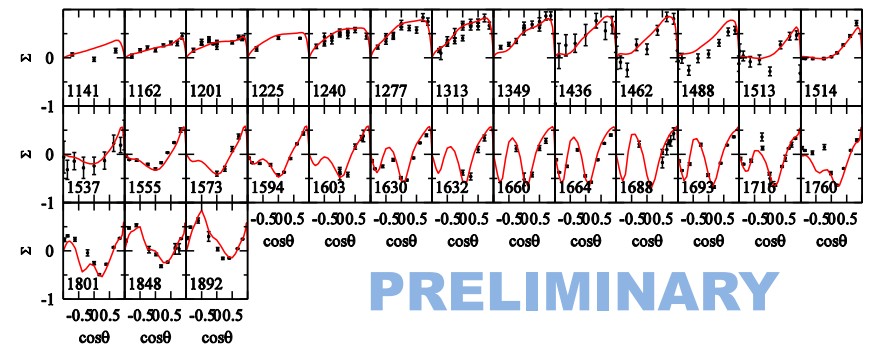
- ✓ Need for **isospin decomposition** of electromagnetic currents.
  - Necessary for applications to **NEUTRINO** reactions: **S. Nakamura, 27th (Wed) ParallelA 27-1**

$$\gamma \text{ 'n'} \rightarrow \pi \text{ p}$$

$d\sigma/d\Omega$  for  $W < 2 \text{ GeV}$



$\Sigma$  for  $1.14 < W < 1.9 \text{ GeV}$



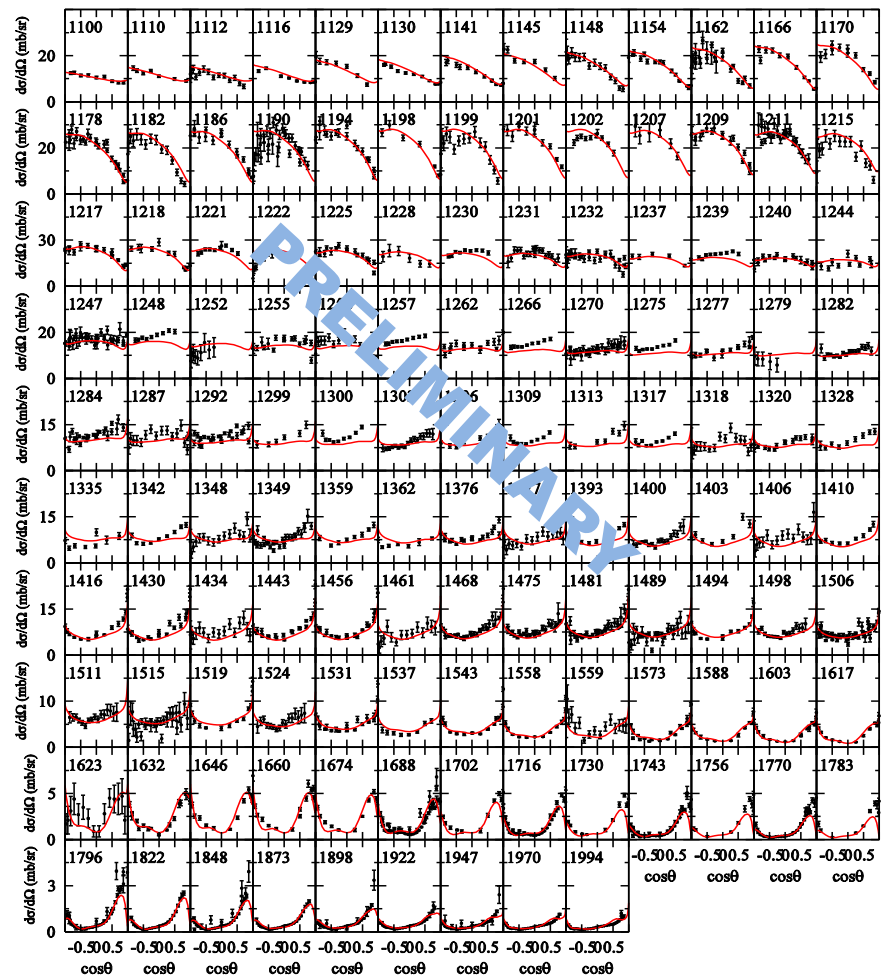
**PRELIMINARY**

# Meson photoproductions off “neutron”

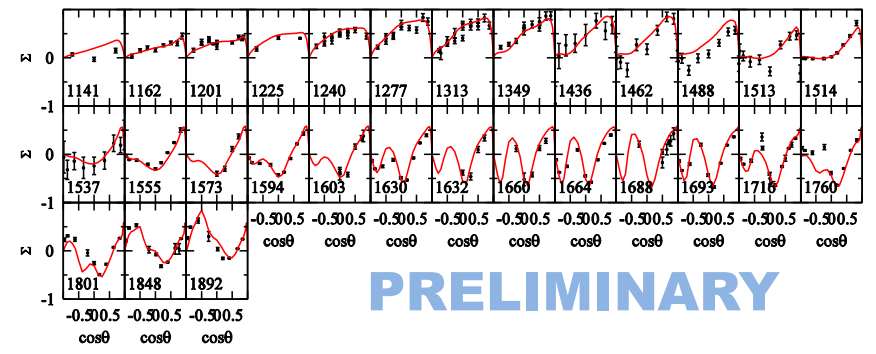
- ✓ Need for **isospin decomposition** of electromagnetic currents.
  - Necessary for applications to **NEUTRINO** reactions: **S. Nakamura, 27th (Wed) ParallelA 27-1**

$$\gamma \text{ 'n' } \rightarrow \pi \text{ p}$$

$d\sigma/d\Omega$  for  $W < 2 \text{ GeV}$



$\Sigma$  for  $1.14 < W < 1.9 \text{ GeV}$



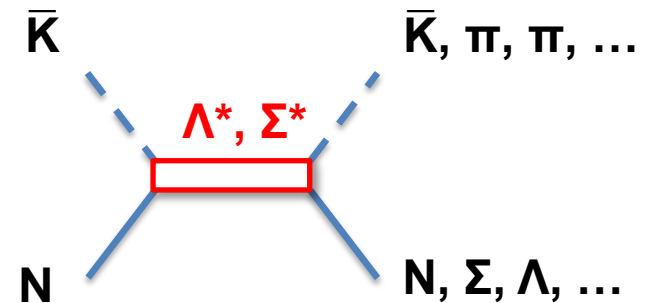
**PRELIMINARY**

**Future work:**  
 Analyze **deuteron reaction data directly**  
 to extract **single- & double-polarization**  
**observables for “neutron-target” reactions**  
 in **a fully consistent way in our approach.**



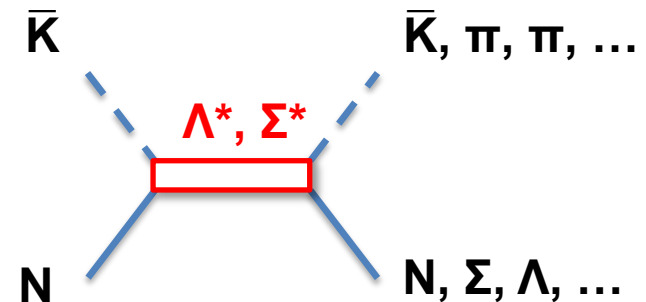
# Current situation for $Y^*$ spectroscopy

- ✓  $Y^*$  ( $= \Lambda^*, \Sigma^*$ ) resonances are much less understood than  $N^*$  and  $\Delta^*$ .
- ✓ Comprehensive & systematic PWA to extract  $Y^*$  defined by *poles of scattering amplitudes* has **only recently** been made:
  - Kent State University (KSU) group (2013, “KSU parametrization” of S-matrix)
  - Our group (2014- , dynamical approach)



# Current situation for $Y^*$ spectroscopy

- ✓  $Y^*$  ( $= \Lambda^*, \Sigma^*$ ) resonances are much less understood than  $N^*$  and  $\Delta^*$ .
- ✓ Comprehensive & systematic PWA to extract  $Y^*$  defined by *poles of scattering amplitudes* has **only recently** been made:
  - Kent State University (KSU) group (2013, “KSU parametrization” of S-matrix)
  - Our group (2014- , dynamical approach)



## What we have done so far

- ✓ Formulation of DCC approach for  $S = -1$  sector  
→ contains  $\bar{K}N, \pi\Sigma, \pi\Lambda, \eta\Lambda, K\Xi, \pi\pi\Lambda(\pi\Sigma^*), \pi\bar{K}N(\bar{K}^*N)$  channels
- ✓ Comprehensive analysis of *all* available data of  $K^- p \rightarrow \bar{K}N, \pi\Sigma, \pi\Lambda, \eta\Lambda, K\Xi$  up to  $W = 2.1$  GeV.  
[HK, Nakamura, Lee, Sato, PRC90(2014)065204]
  - Successfully determined the partial-wave amplitudes for **S, P, D, and F waves** !!
- ✓ Extraction of  $\Lambda^*$  and  $\Sigma^*$  resonance parameters defined by poles of scattering amplitudes.  
[HK, Nakamura, Lee, Sato, in preparation]

# Database of our analysis ( $W < 2.1\text{GeV}$ )

HK, Nakamura, Lee, Sato, PRC90(2014)065204

## Issues in the availability of data:

- ✓ Most data are from 60-70's.
- ✓ Kinematical coverage is rather scarce for most reactions.
- ✓ No data for spin rotations ( $\beta, R, A$ ).
- ✓ No data near the threshold for  $K^- p \rightarrow \bar{K}N, \pi\Sigma, \pi\Lambda$ .



The  $K^- p$  reaction data are far from “complete”!!

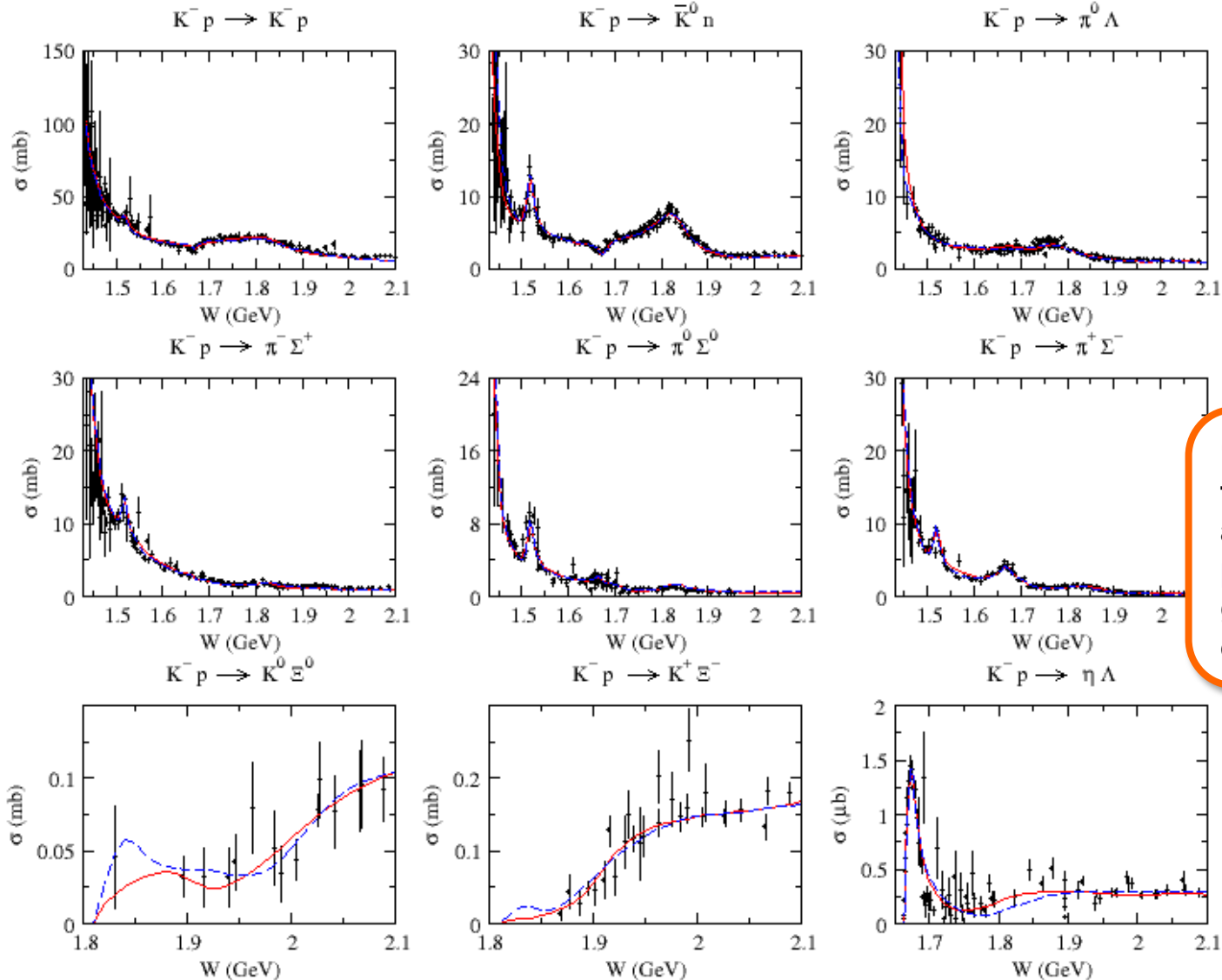
➔ Need help of hadron beam facilities !!

Reactions	Observables	Number of data	
$K^- p \rightarrow K^- p$	$d\sigma/d\Omega$	3962	} $d\sigma/d\Omega$ : 1465 MeV < W P : 1730 MeV < W $\beta, R, A$ : No data
	P	510	
	$\sigma$	253	
$K^- p \rightarrow \bar{K}^0 n$	$d\sigma/d\Omega$	2950	} $d\sigma/d\Omega$ : 1465 MeV < W P : No data $\beta, R, A$ : No data
	$\sigma$	260	
$K^- p \rightarrow \pi^- \Sigma^+$	$d\sigma/d\Omega$	1792	} $d\sigma/d\Omega$ : 1535 MeV < W P : 1535 MeV < W < 1967 MeV $\beta, R, A$ : No data
	P	418	
	$P \times d\sigma/d\Omega$	177	
	$\sigma$	173	
$K^- p \rightarrow \pi^0 \Sigma^0$	$d\sigma/d\Omega$	580	} $d\sigma/d\Omega$ : 1535 MeV < W < 1763 MeV P : 1535 MeV < W < 1696 MeV $\beta, R, A$ : No data
	P	196	
	$P \times d\sigma/d\Omega$	189	
	$\sigma$	125	
$K^- p \rightarrow \pi^+ \Sigma^-$	$d\sigma/d\Omega$	1786	} $d\sigma/d\Omega$ : 1536 MeV < W P : No data $\beta, R, A$ : No data
	$\sigma$	181	
$K^- p \rightarrow \pi^0 \Lambda$	$d\sigma/d\Omega$	2178	} $d\sigma/d\Omega$ : 1535 MeV < W P : 1535 MeV < W $\beta, R, A$ : No data
	P	693	
	$P \times d\sigma/d\Omega$	176	
	$\sigma$	207	
$K^- p \rightarrow \eta \Lambda$	$d\sigma/d\Omega$	160	} $d\sigma/d\Omega$ : 1664 MeV < W < 1696 MeV P : 1669 MeV < W < 1681 MeV $\beta, R, A$ : No data
	P	18	
	$\sigma$	78	
$K^- p \rightarrow K^0 \Xi^0$	$d\sigma/d\Omega$	33	} $d\sigma/d\Omega$ : 1970 MeV < W < 2070 MeV P : No data $\beta, R, A$ : No data
	$\sigma$	15	
$K^- p \rightarrow K^+ \Xi^-$	$d\sigma/d\Omega$	92	} $d\sigma/d\Omega$ : 1950 MeV < W < 2070 MeV P : No data $\beta, R, A$ : No data
	$\sigma$	27	
Total		17229	

# Results of the fits

## $K^- p \rightarrow MB$ total cross sections

HK, Nakamura, Lee, Sato, PRC90(2014)065204



Red: Model A

Blue: Model B

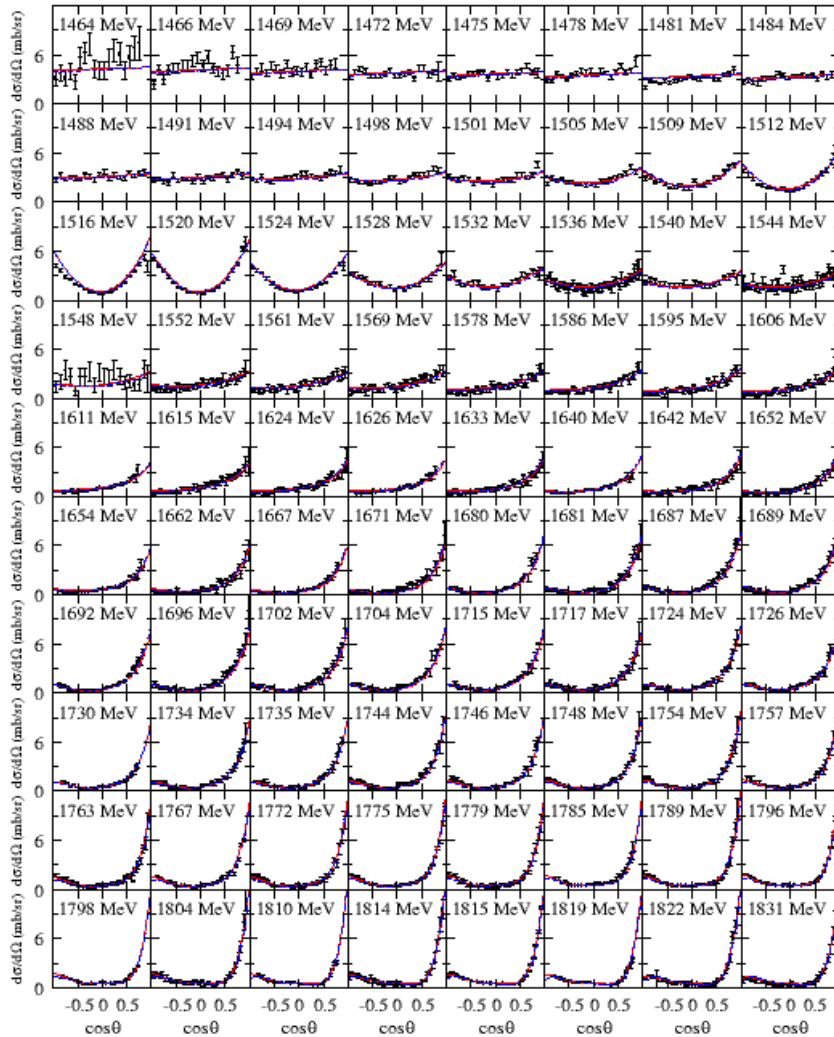
“Incompleteness” of the current database allows us to have two parameter sets that give similar quality of the fit.

# Results of the fits

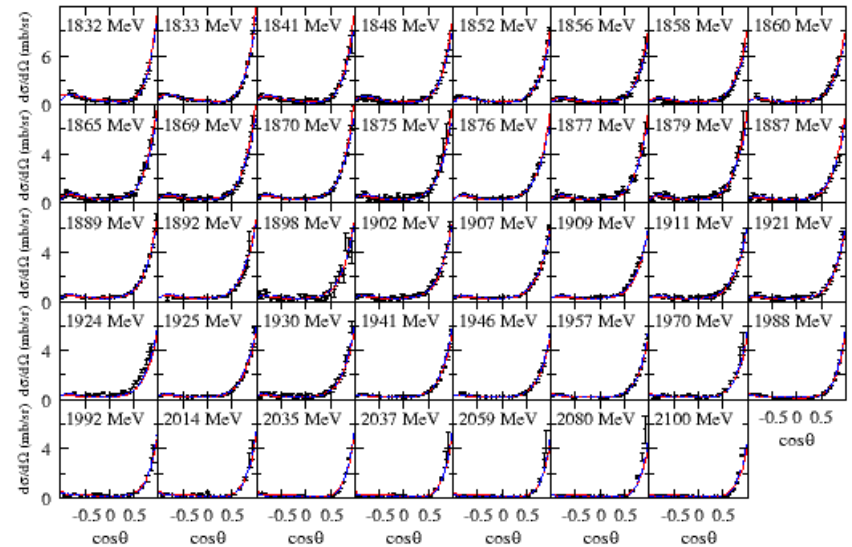
$K^- p \rightarrow K^- p$  scattering

HK, Nakamura, Lee, Sato, PRC90(2014)065204

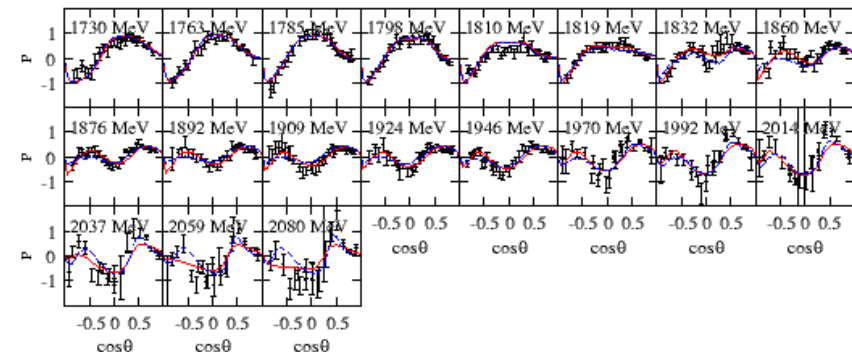
$d\sigma/d\Omega$  ( $1464 < W < 1831$  MeV)



$d\sigma/d\Omega$  ( $1832 < W < 2100$  MeV)



P



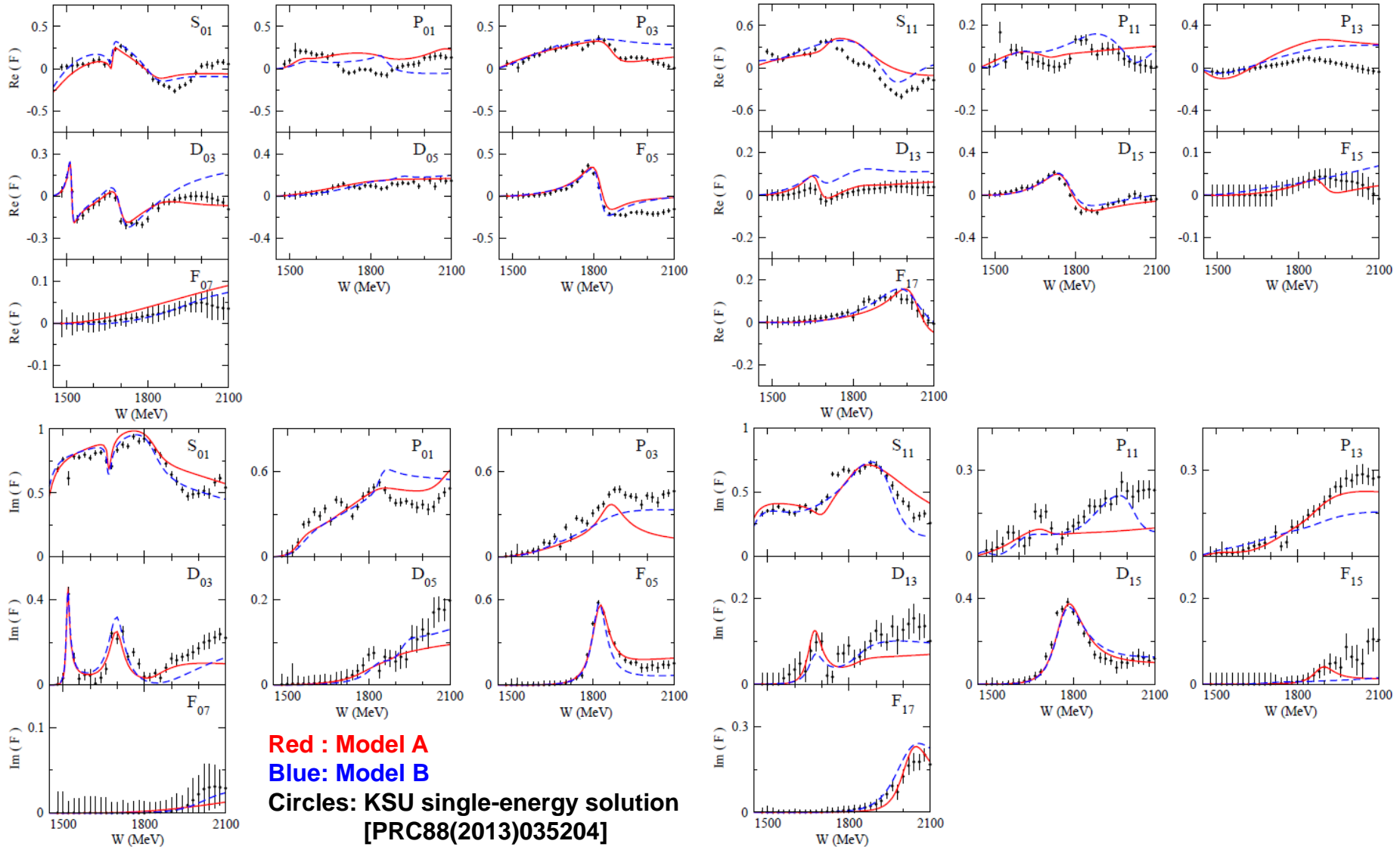
Red: Model A Blue: Model B

# Comparison of extracted partial-wave amplitudes

## Extracted $\bar{K}N$ scattering amplitudes

HK, Nakamura, Lee, Sato, PRC90(2014)065204

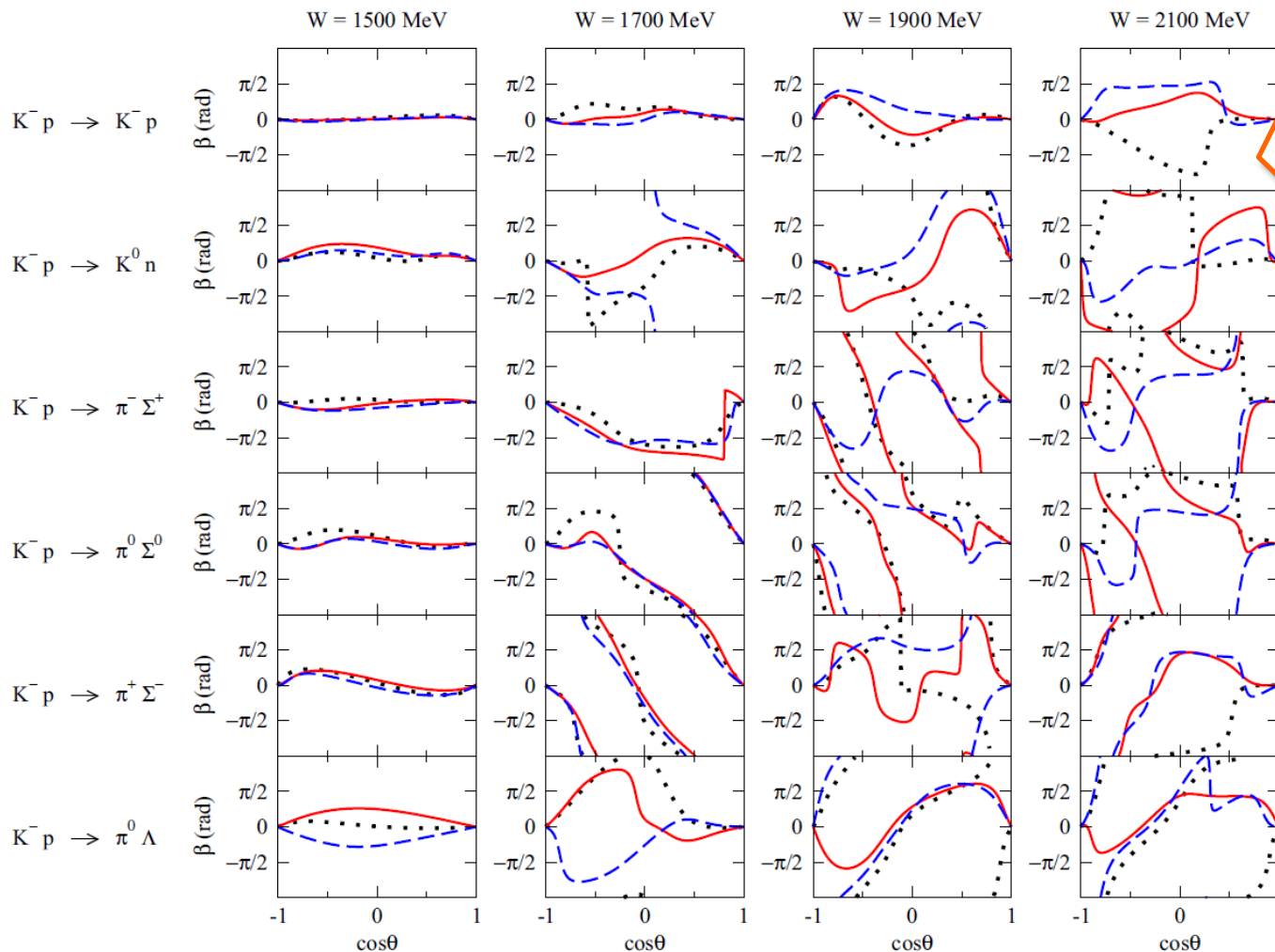
$L_{I2J}$  :  $L = S, P, \dots$  ;  $I =$  isospin;  $J =$  Total angular mom.



# Predicted spin-rotation angle $\beta$

HK, Nakamura, Lee, Sato, PRC90(2014)065204

**## Currently no data for spin-rotation angle  $\beta$**



Analysis dependence is clearly seen !!



Measurement of  $\beta$  will give strong constraints on  $Y^*$  spectrum !!

**Red: Model A**

**Blue: Model B**

**Black: KSU**

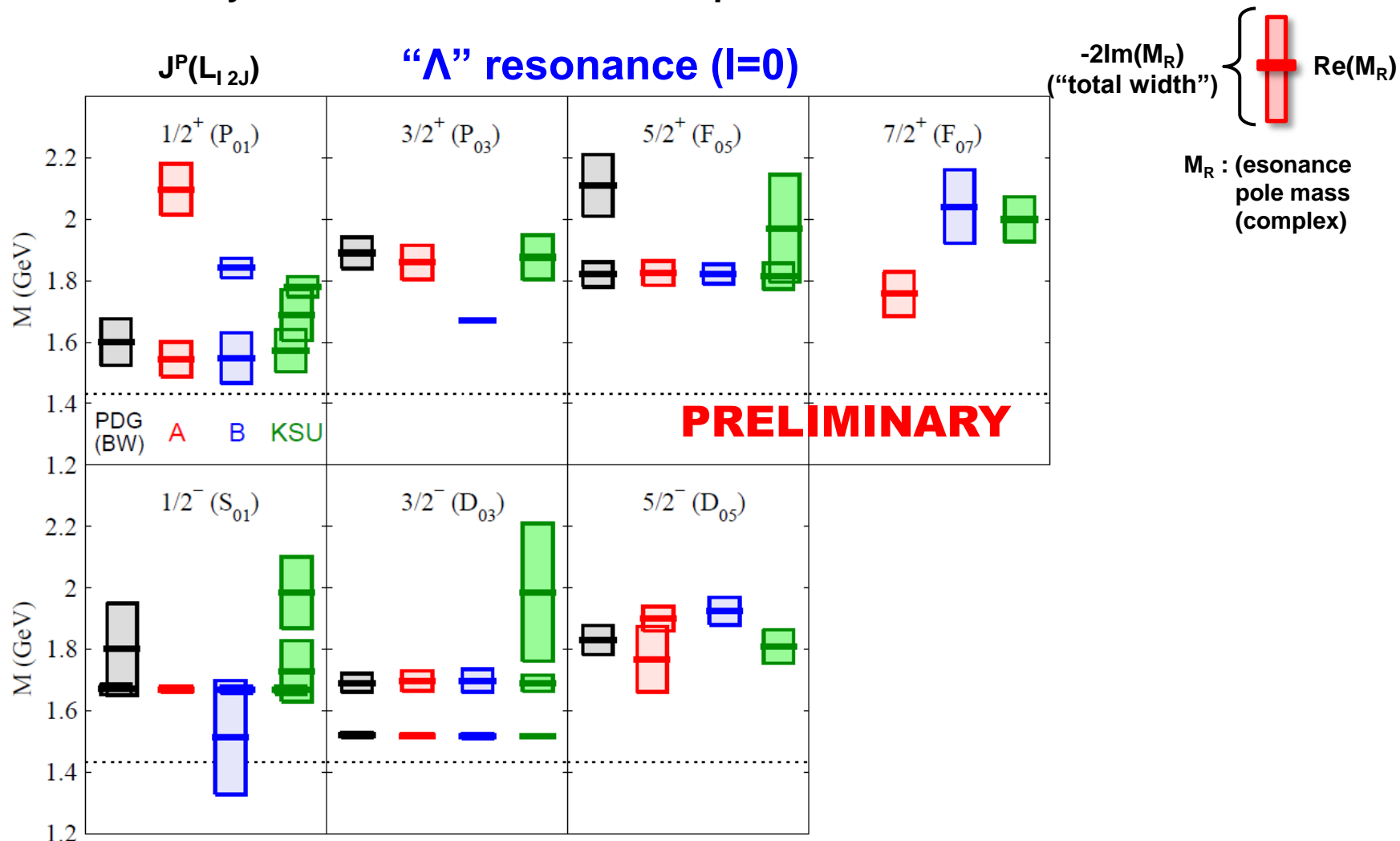
The KSU results are computed by us using their amplitudes in PRC88(2013)035204.

**## NOTE:**  
 $\beta$  is modulo  $2\pi$

# Comparison of $\Lambda^*$ spectrum between multichannel analyses

HK, Nakamura, Lee, Sato, in preparation

### Here only  $Y^*$ s above  $\bar{K}N$  threshold are presented.



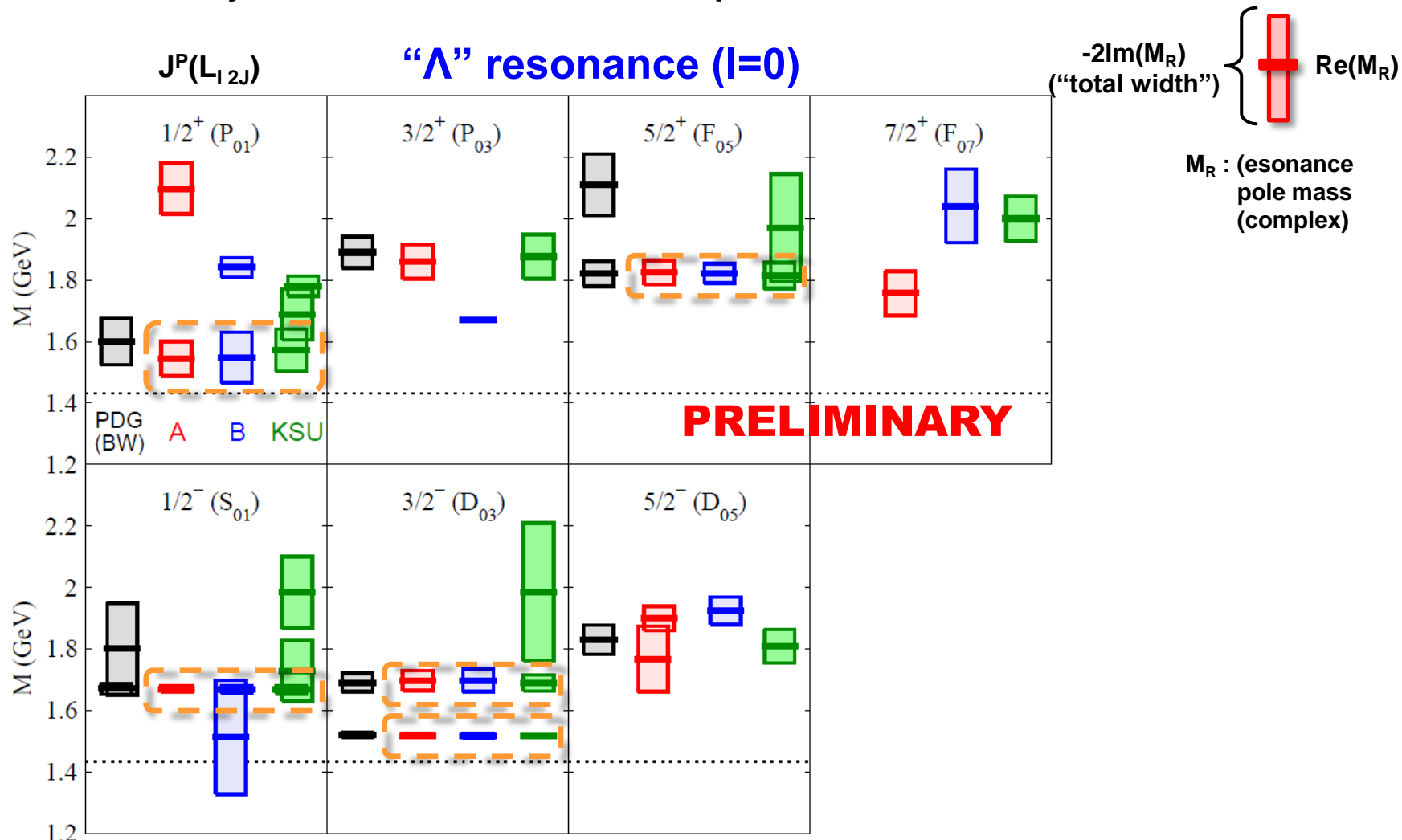
Red: Model A, Blue: Model B, Green: KSU[on-shell K-matrix,PRC88(2013)035205], Black: PDG(Breit-Wigner)



# Comparison of $\Lambda^*$ spectrum between multichannel analyses

HK, Nakamura, Lee, Sato, in preparation

### Here only  $Y^*$ s above  $\bar{K}N$  threshold are presented.

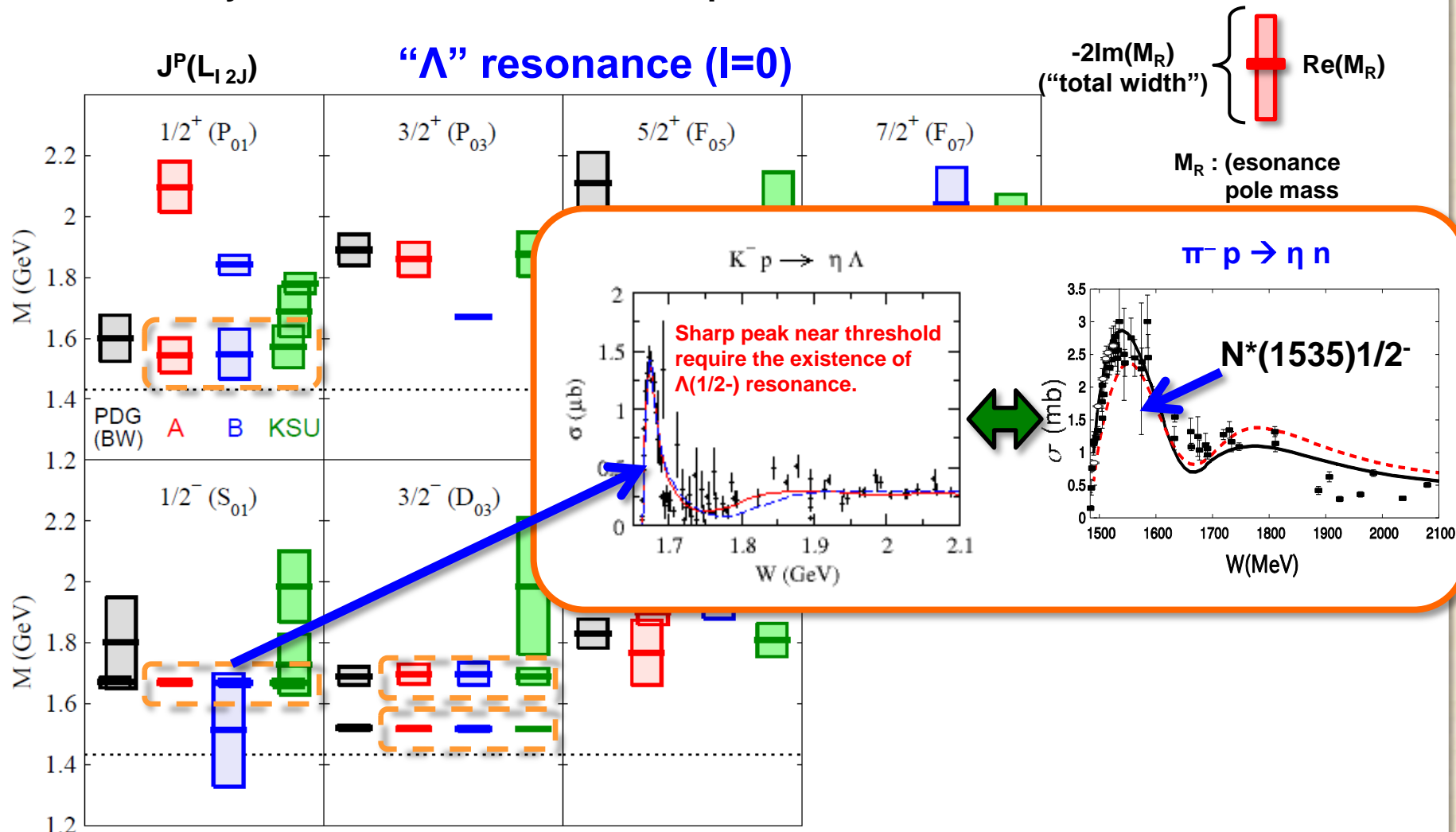


Red: Model A, Blue: Model B, Green: KSU[on-shell K-matrix,PRC88(2013)035205], Black: PDG(Breit-Wigner)

# Comparison of $\Lambda^*$ spectrum between multichannel analyses

HK, Nakamura, Lee, Sato, in preparation

### Here only  $Y^*$ s above  $\bar{K}N$  threshold are presented.

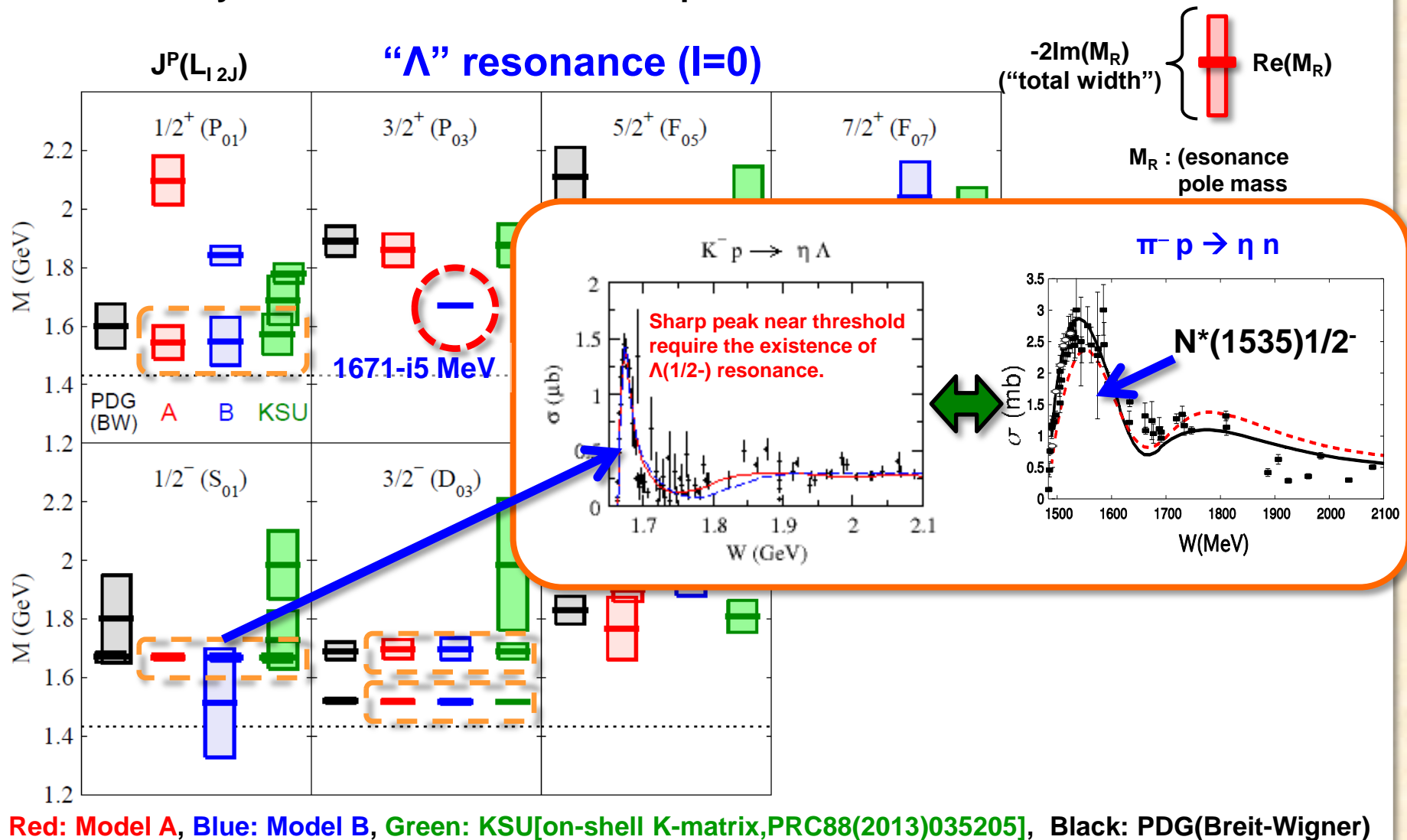


Red: Model A, Blue: Model B, Green: KSU[on-shell K-matrix,PRC88(2013)035205], Black: PDG(Breit-Wigner)

# Comparison of $\Lambda^*$ spectrum between multichannel analyses

HK, Nakamura, Lee, Sato, in preparation

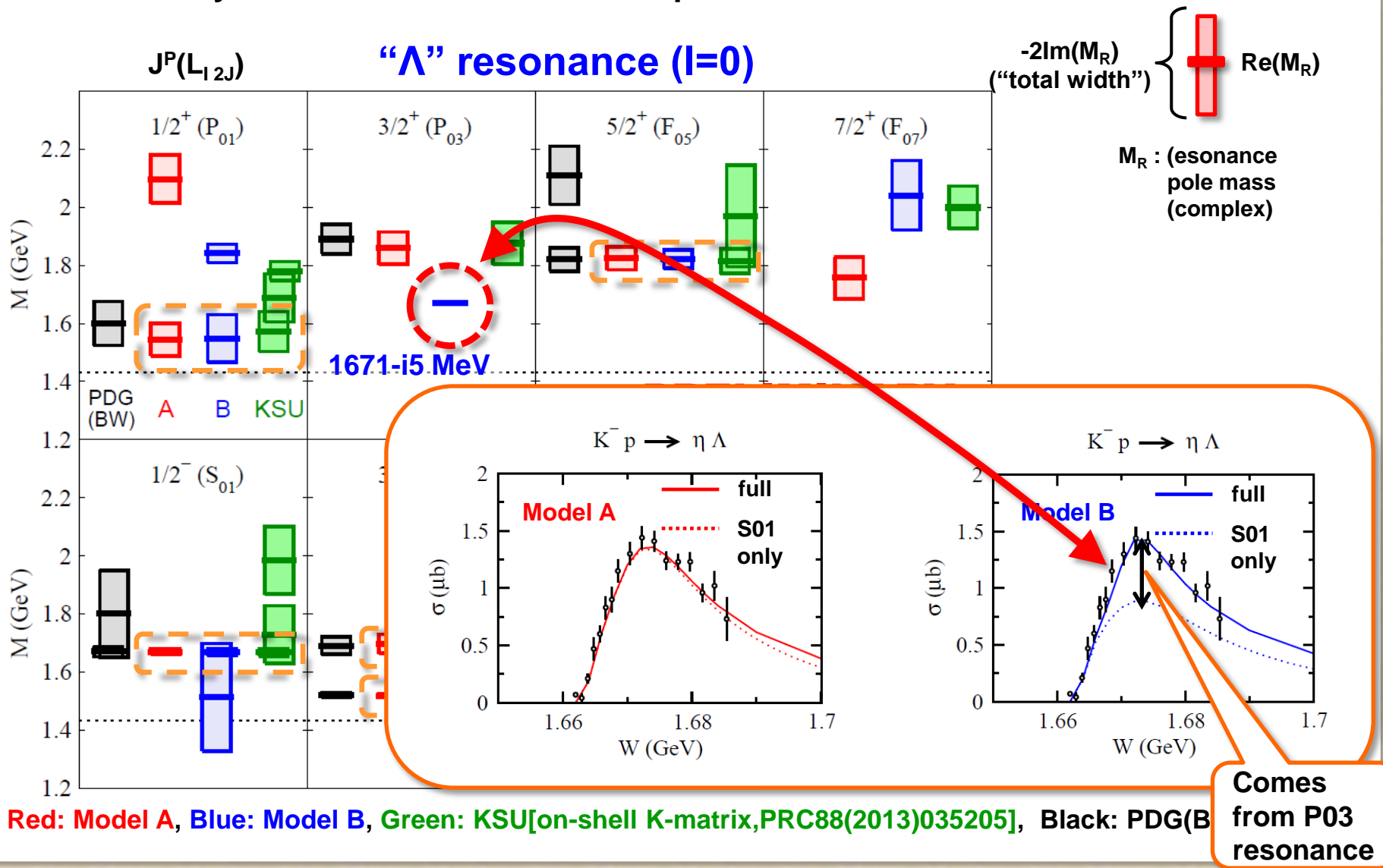
### Here only  $Y^*$ s above  $\bar{K}N$  threshold are presented.



# Comparison of $\Lambda^*$ spectrum between multichannel analyses

HK, Nakamura, Lee, Sato, in preparation

### Here only  $Y^*$ s above  $\bar{K}N$  threshold are presented.



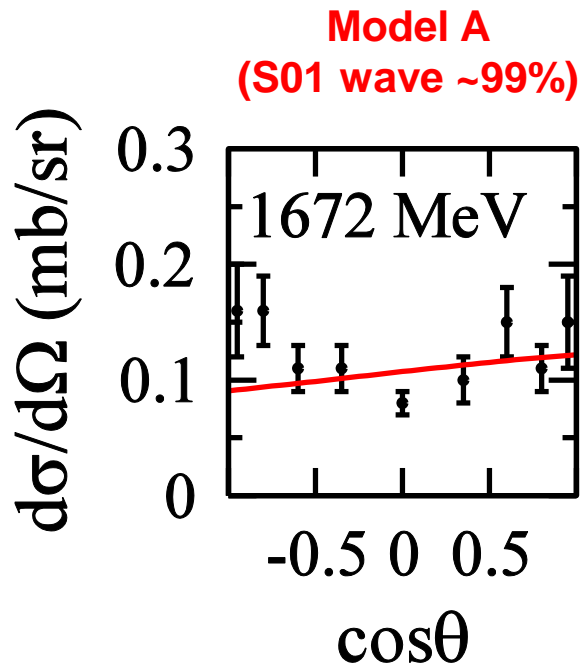
Red: Model A, Blue: Model B, Green: KSU[on-shell K-matrix,PRC88(2013)035205], Black: PDG(BW)

# P03 resonance just above the $\eta\Lambda$ threshold

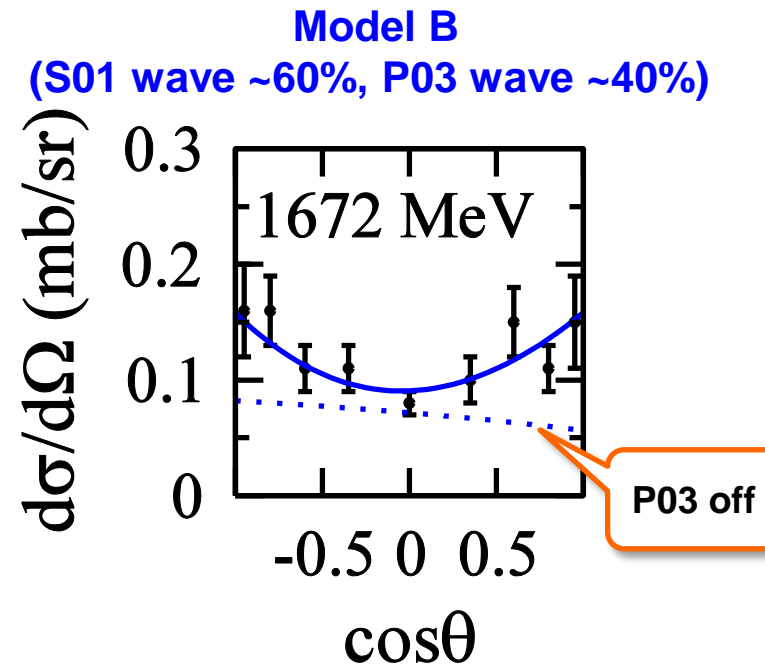
HK, Nakamura, Sato, in preparation

$d\sigma/d\Omega$  of  $K^- p \rightarrow \eta\Lambda$  @  $W=1672$  MeV (just **8 MeV** above the threshold)

- Even close to the threshold, the data show **a clear angular dependence**.



- ✓ Concave-up behavior not reproduced.

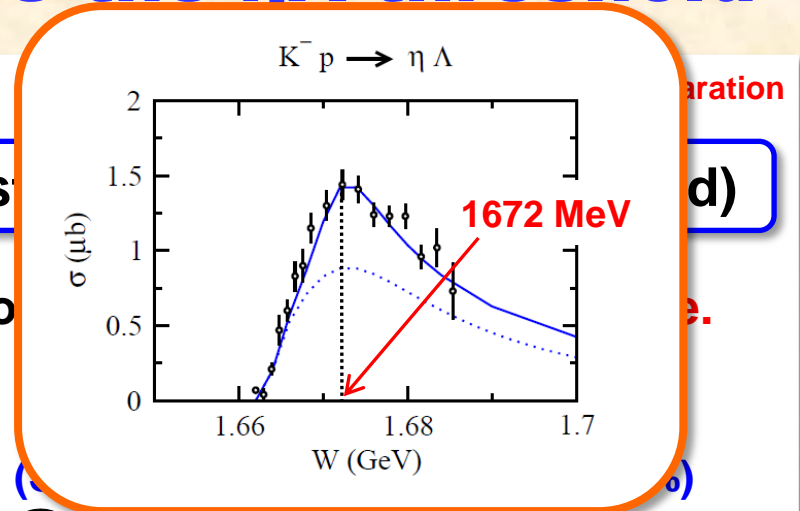


- ✓ **Narrow P03 resonance** responsible for the angular dependence !!

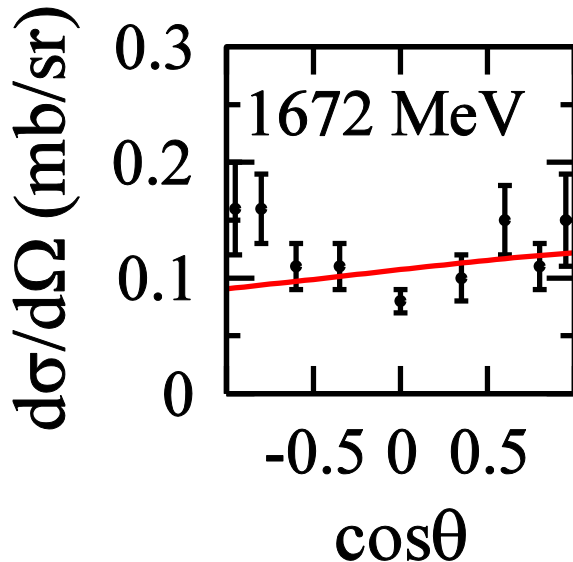
# P03 resonance just above the $n\Lambda$ threshold

$d\sigma/d\Omega$  of  $K^- p \rightarrow \eta \Lambda$  @  $W=1672$  MeV (just above threshold)

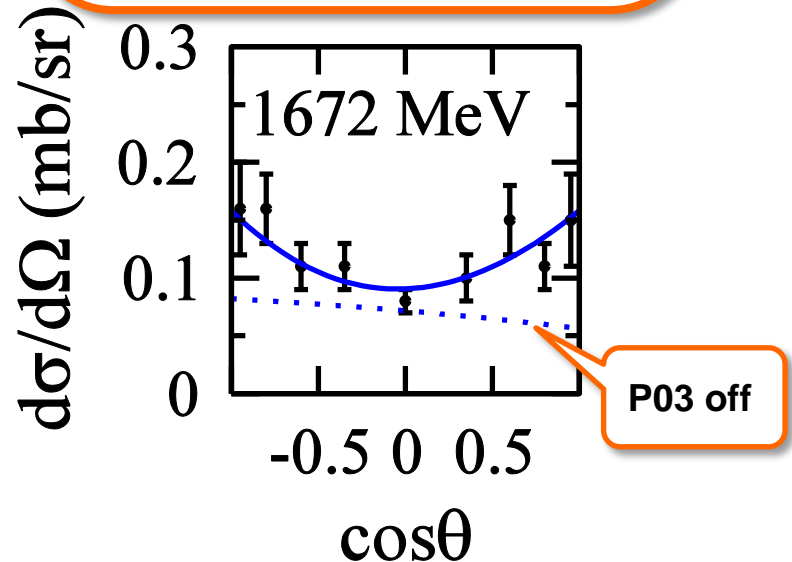
➤ Even close to the threshold, the data show a narrow resonance



**Model A**  
(S01 wave ~99%)



✓ Concave-up behavior not reproduced.



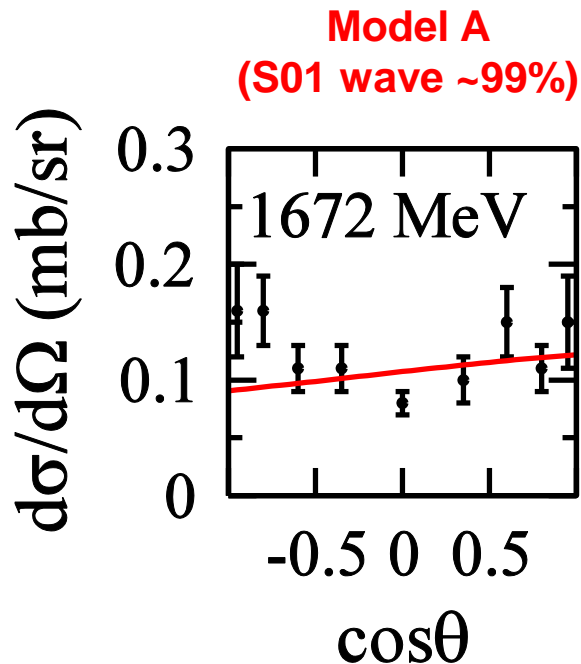
✓ **Narrow P03 resonance** responsible for the angular dependence !!

# P03 resonance just above the $\eta\Lambda$ threshold

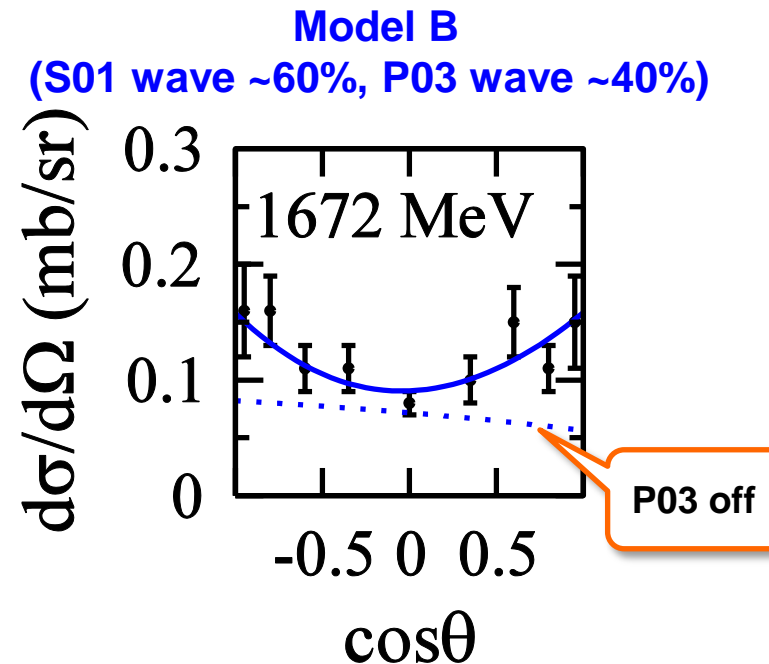
HK, Nakamura, Sato, in preparation

$d\sigma/d\Omega$  of  $K^- p \rightarrow \eta\Lambda$  @  $W=1672$  MeV (just **8 MeV** above the threshold)

- Even close to the threshold, the data show **a clear angular dependence**.



- ✓ Concave-up behavior not reproduced.



- ✓ **Narrow P03 resonance** responsible for the angular dependence !!

# Summary & ongoing/future works

## Summary

- ✓ Comprehensive PWA to extract properties of **light-quark baryons** ( $N^*$ ,  $\Delta^*$ ,  $\Lambda^*$ ,  $\Sigma^*$ ) within **Dynamical Coupled-Channels (DCC) approach**.
- ✓ **Visible analysis dependence in extracted resonance spectrum.**
  - needs more extensive meson production data (including polarization observables) from electron, photon, and hadron beam facilities.

## Ongoing/future works

- ✓ **N-N\* e.m. transition form factors to high Q<sup>2</sup>**
- ✓ **High-mass N\* and  $\Delta^*$  spectroscopy (extends channel space, inclusion of  $\pi\pi N$  data)**
- ✓ **DCC approach to deuteron target reactions**
  - Helicity amplitudes for  $\gamma$ -neutron  $\rightarrow N^*$  (need for isospin separation)
  - $Y^*$  spectroscopy below  $\bar{K}N$  threshold with  $K^- d$  reactions (J-PARC E31)
- ✓ **Applications to neutrino-induced reactions ( input for neutrino-oscillation experiments )**
  - Collaboration@J-PARC Branch of KEK Theory Center  
( <http://j-parc-th.kek.jp/html/English/e-index.html> )
- ✓ **Applications to hypernuclei & kaonic nuclei productions**

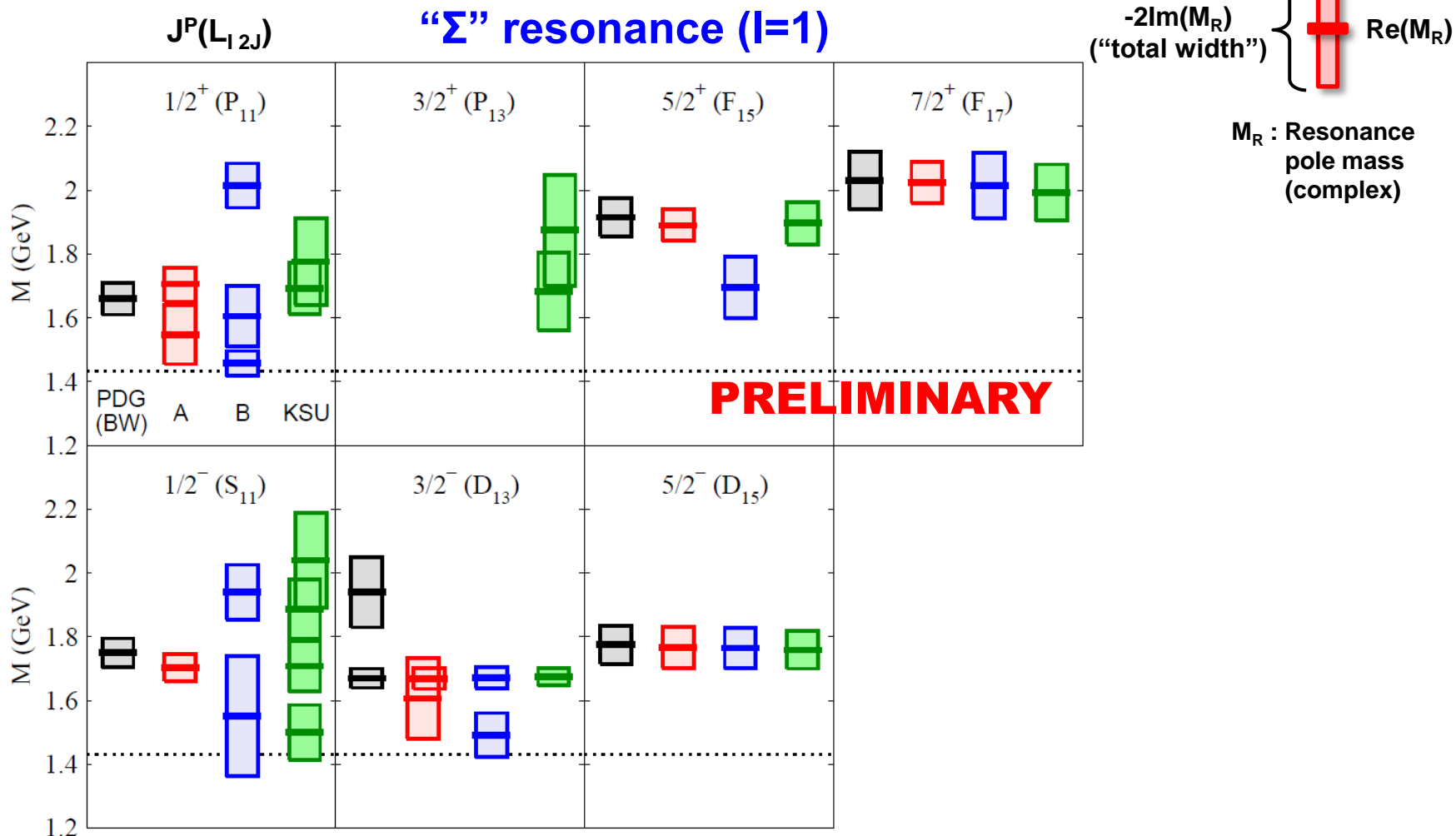


**Back up**

# Comparison of $\Sigma^*$ spectrum between multichannel analyses

HK, Nakamura, Lee, Sato, in preparation

### Here only  $Y^*$ s above  $\bar{K}N$  threshold are presented.

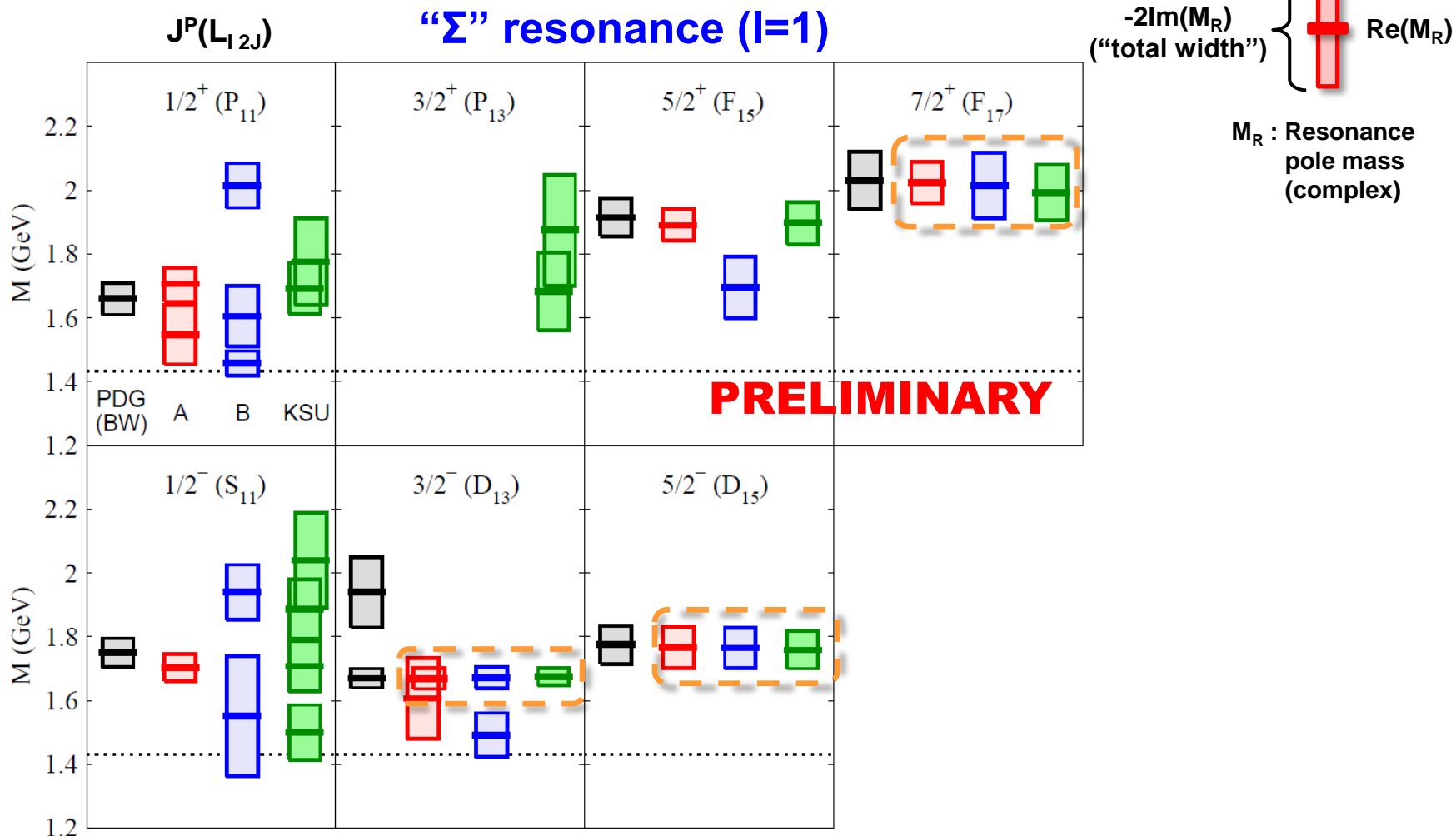


Red: Model A, Blue: Model B, Green: KSU[on-shell K-matrix,PRC88(2013)035205], Black: PDG(Breit-Wigner)

# Comparison of $\Sigma^*$ spectrum between multichannel analyses

HK, Nakamura, Lee, Sato, in preparation

### Here only  $Y^*$ s above  $\bar{K}N$  threshold are presented.

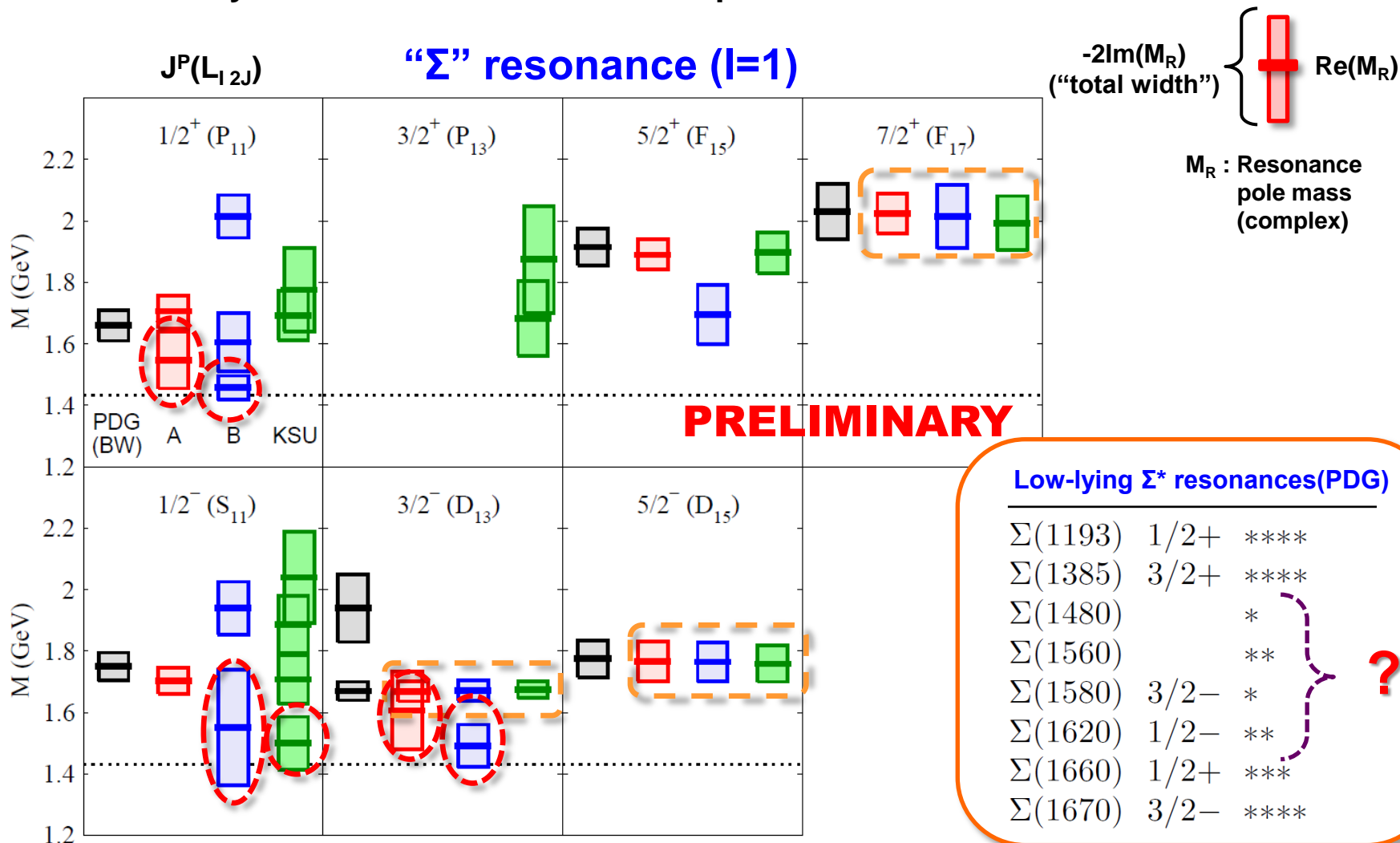


Red: Model A, Blue: Model B, Green: KSU[on-shell K-matrix,PRC88(2013)035205], Black: PDG(Breit-Wigner)

# Comparison of $\Sigma^*$ spectrum between multichannel analyses

HK, Nakamura, Lee, Sato, in preparation

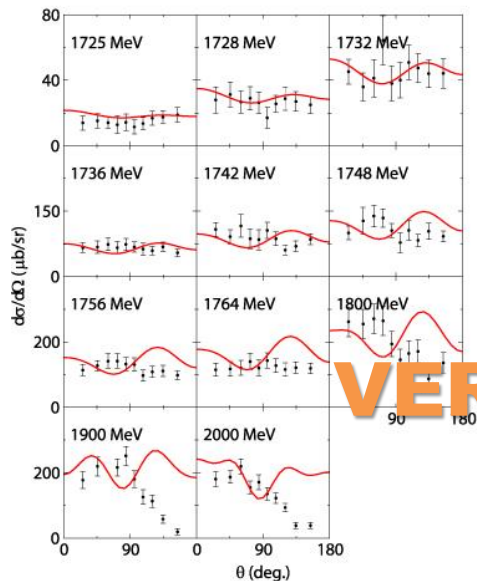
### Here only  $Y^*$ s above  $\bar{K}N$  threshold are presented.



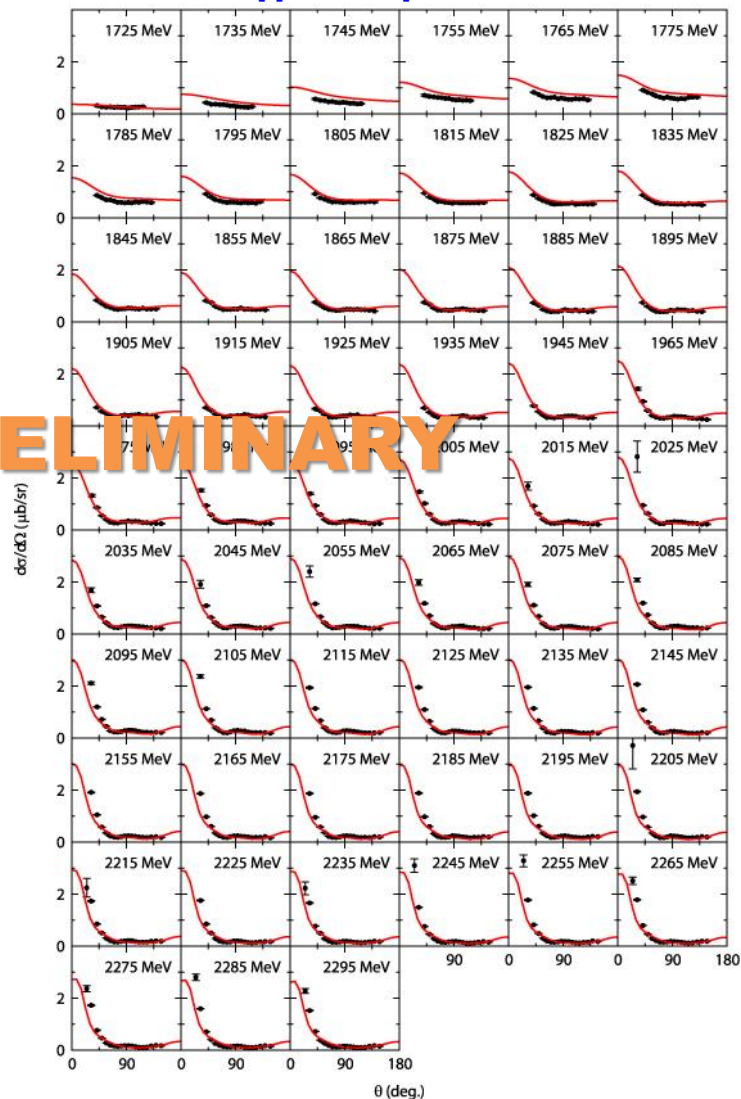
Red: Model A, Blue: Model B, Green: KSU[on-shell K-matrix,PRC88(2013)035205], Black: PDG(Breit-Wigner)

# Extending analysis of $N^*$ production within ANL-Osaka DCC approach

## $\pi p \rightarrow \omega n$ DCS



## $\gamma p \rightarrow \omega p$ DCS

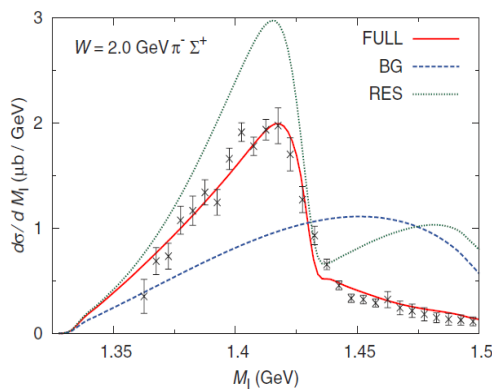
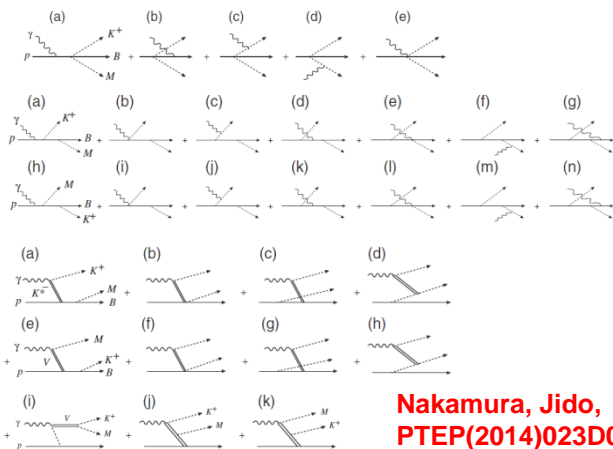


Combined analysis  
including  $\omega N$  data  
is *in progress* !!

# How we study the region below the $\bar{K}N$ threshold ?

E.g.)  $\gamma p \rightarrow K^+ \pi^- \Sigma$  @CLAS

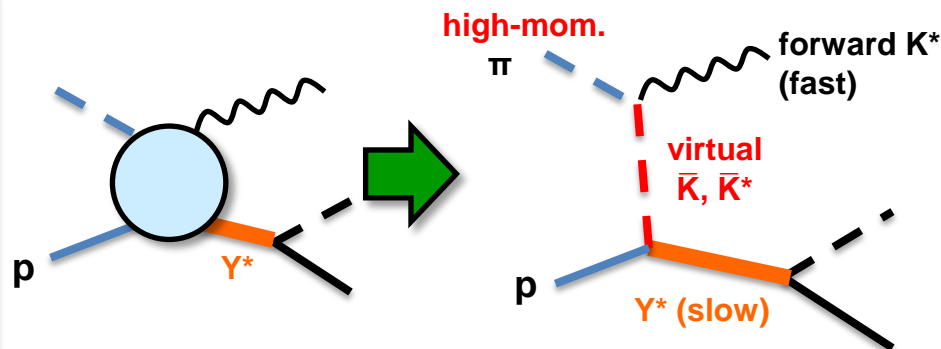
At the CLAS energy, **many production processes contribute** and sizably affect mass distributions as **backgrounds**.



**Large model dependence from complicated production processes.**

→ Makes unambiguous determination of  $\Lambda(1405)$  difficult.

Forward  $p(\pi, K^*)X$  reactions with **high-momentum pion beam** (→ J-PARC E50)



- For forward  $K^*$  (small  $t$ ), the processes are dominated by diffractive t-channel exchange processes.
- We DO have fully unitarized  $\bar{K}N \rightarrow MB$  and  $\bar{K}^*N \rightarrow MB$  half off-shell amplitudes !!
- 12 GeV JLab can do a similar measurement by replacing incident  $\pi$  by high-energy photon.

➤ Useful also for determining **low-lying  $\Sigma^*$  resonances**

**Low-lying  $\Sigma^*$  resonances(PDG)**

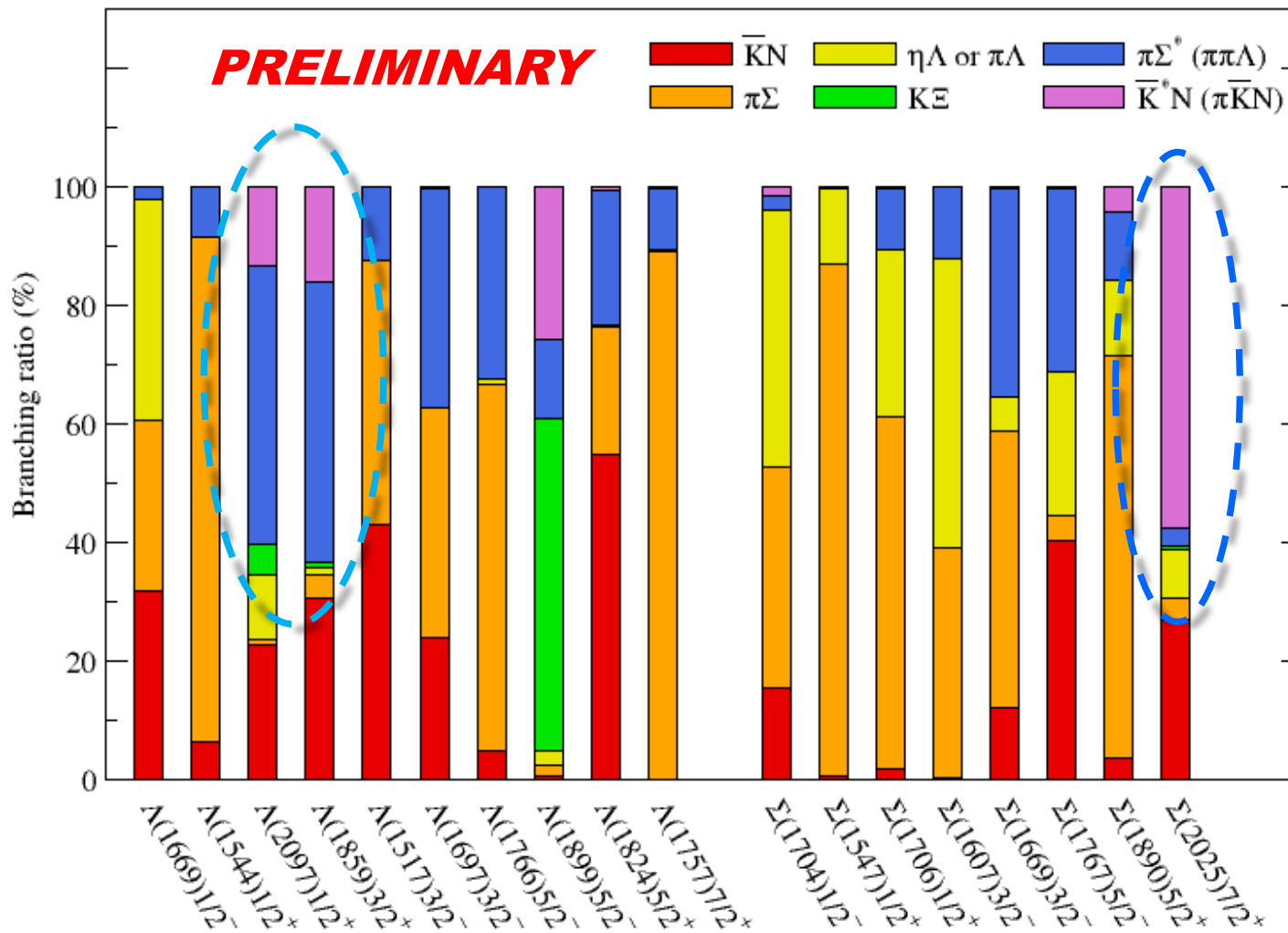
$\Sigma(1193)$	1/2+	****
$\Sigma(1385)$	3/2+	****
$\Sigma(1480)$		*
$\Sigma(1560)$		**
$\Sigma(1580)$	3/2-	*
$\Sigma(1620)$	1/2-	**
$\Sigma(1660)$	1/2+	***
$\Sigma(1670)$	3/2-	****

?

# Branching ratios

HK, Nakamura, Lee, Sato, in preparation

## Model A

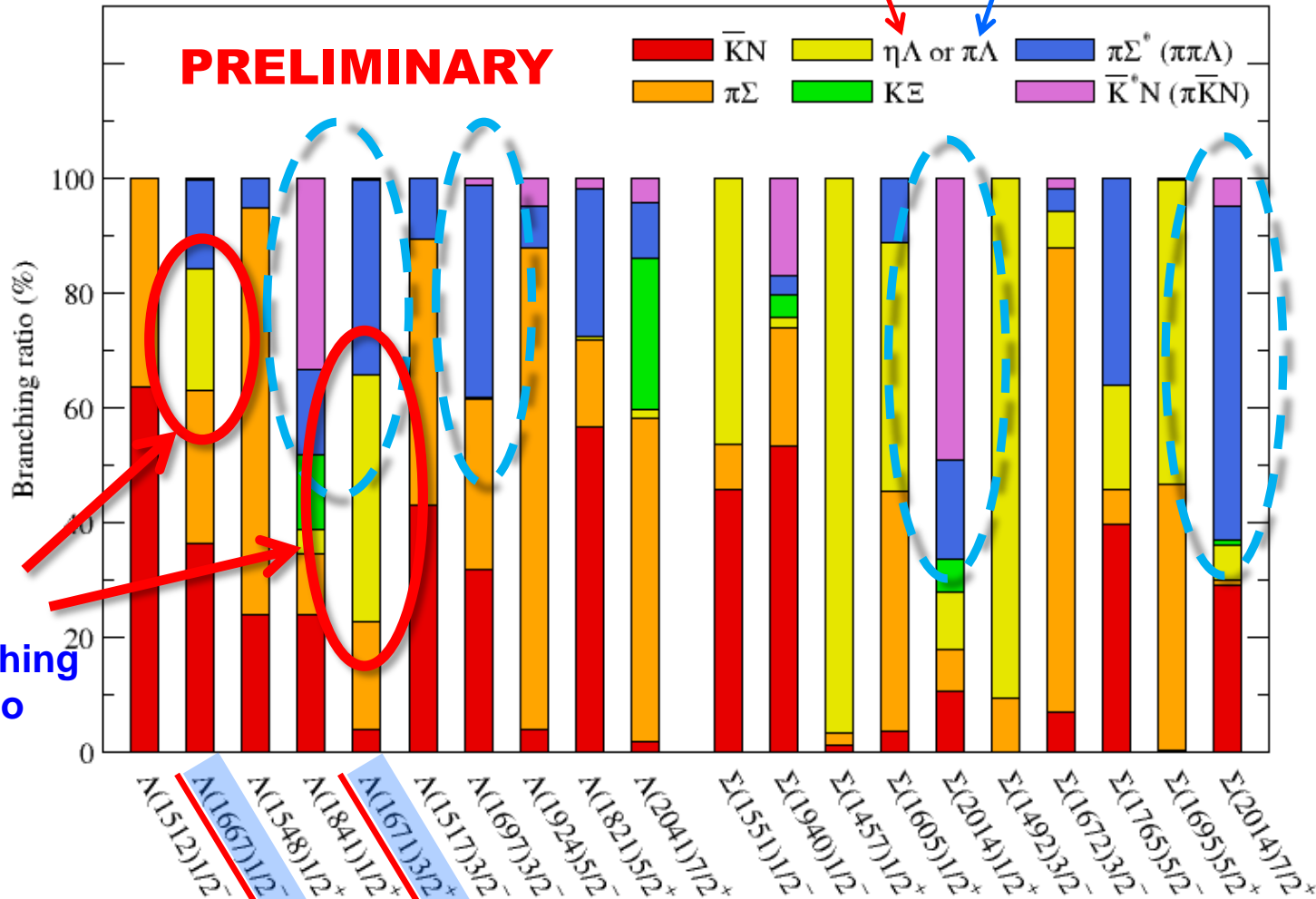
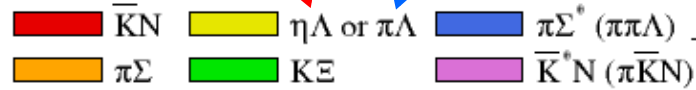


# Branching ratios

HK, Nakamura, Lee, Sato, in preparation

## Model B for $\Lambda^*$ for $\Sigma^*$

**PRELIMINARY**



Large branching ratio to  $\eta\Lambda$  !!

Resonances producing sharp peak in the  $K-p \rightarrow \eta\Lambda$  total cross section near the threshold



# Application to neutrino-induced reactions

- ✓ **Reliable neutrino reaction model** is necessary for **precise** determination of neutrino parameters from **future neutrino-oscillation experiments** (leptonic CP phase, neutrino mass hierarchy...).
- ✓ Relevant kinematical region extends over **Quasi elastic**, **Resonance**, and **DIS** regions.



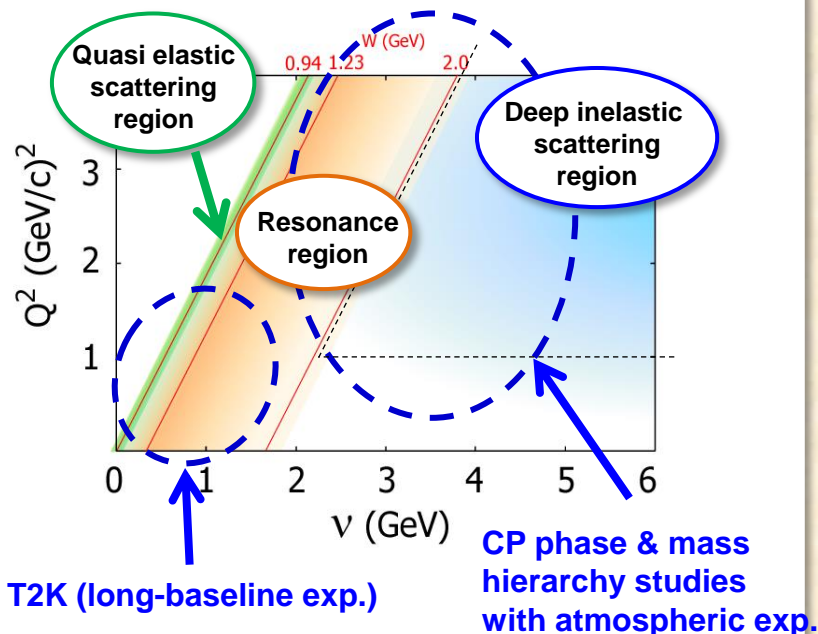
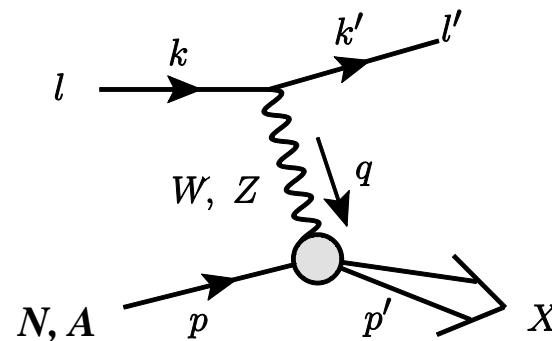
Collaboration@J-PARC Branch of KEK Theory Center  
[<http://j-parc-th.kek.jp/html/English/e-index.html>]

Y. Hayato (ICRR, U. of Tokyo), M. Hirai (Nippon Inst. Tech.)  
H. Kamano (RCNP, Osaka U.), S. Kumano (KEK)  
S. Nakamura (Osaka U.), K. Saito (Tokyo U. of Sci.)  
M. Sakuda (Okayama U.), T. Sato (Osaka U.)

[→ [arXiv:1303.6032](https://arxiv.org/abs/1303.6032)]

→ **Talk by S. Nakamura**  
**27(Wed) Parallel-A:27-1**

## Neutrino-nucleon/nucleus reactions

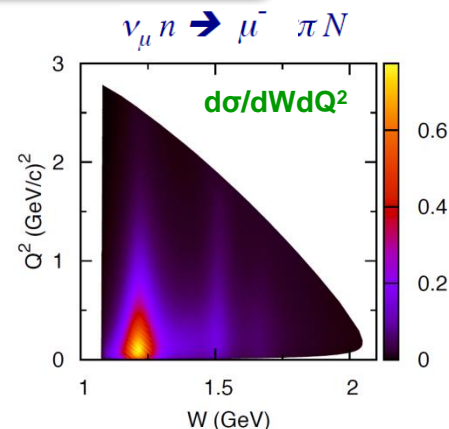
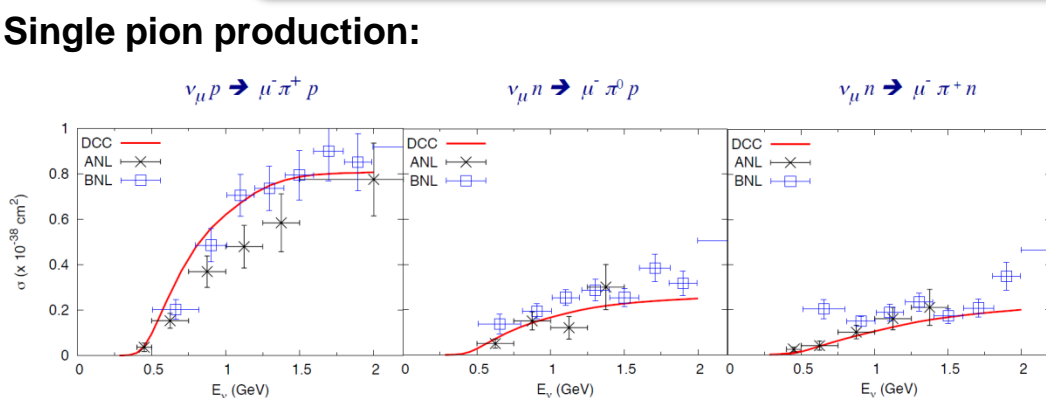


# Application to neutrino-induced reactions

Nakamura, HK, Sato, in preparation

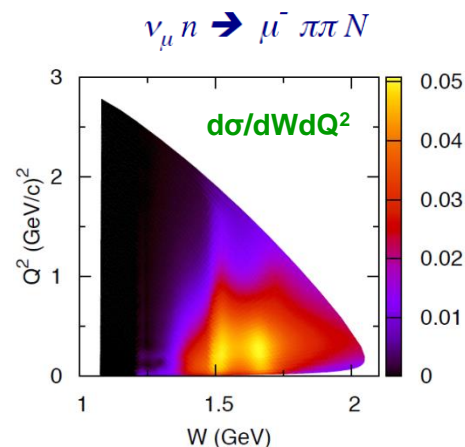
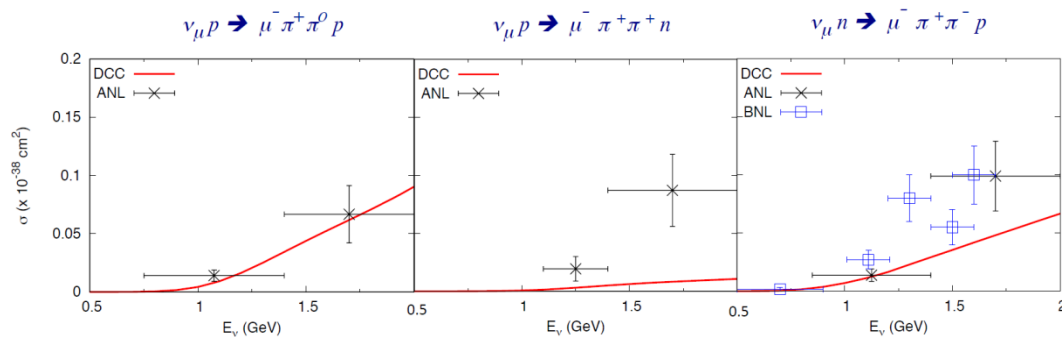
The **first-time** full coupled-channels calculation of  $\nu$ -nucleon reactions **beyond the  $\Delta(1232)$  region !!**

## ✓ Single pion production:



## ✓ Double pion production:

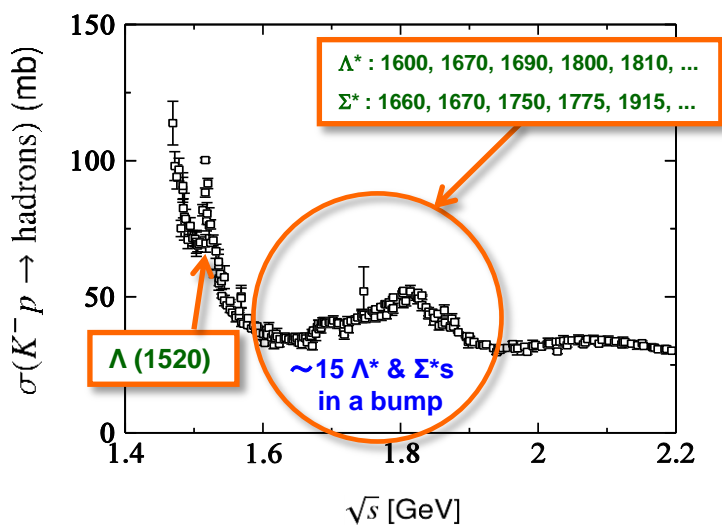
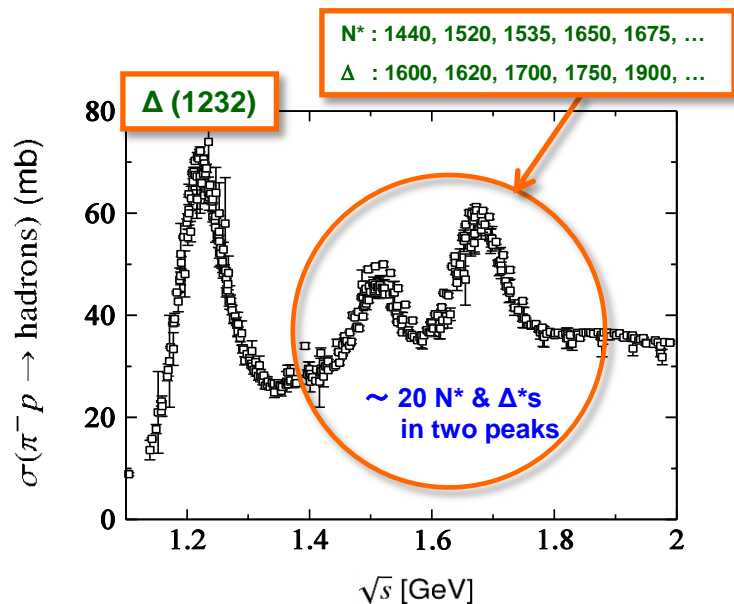
**PRELIMINARY**



##NOTE:  $Q^2$  dependence of all N-N\* axial transition form factors are currently fixed with that of N- $\Delta(1232)$  transition.

##  $\eta N$ ,  $K\Lambda$ ,  $K\Sigma$  productions can also be calculated.

# Light-quark baryon ( $N^*$ , $\Delta^*$ , $\Lambda^*$ , $\Sigma^*$ ) spectroscopy : Physics of broad & overlapping resonances



- ✓ Width:  $O(10^1-10^2)$  MeV.
- ✓ Resonances are **highly overlapping** in energy except  $\Delta(1232)$  and  $\Lambda(1520)$



- ✓ To reliably extract baryon resonances, one must do **comprehensive PWA of meson production reactions**:

- taking account of **various final states simultaneously**.
- extending **over the wide energy region**.



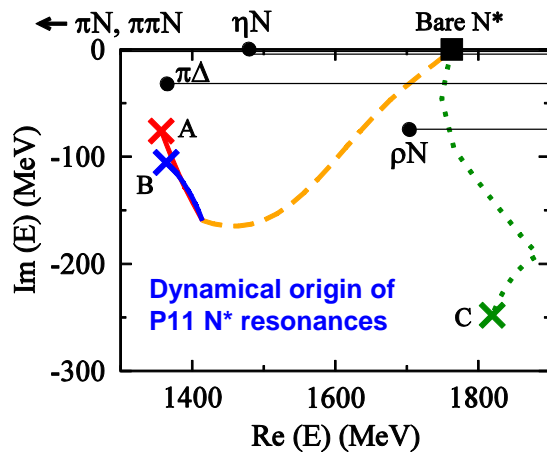
- ✓ Analysis with a theoretical framework satisfying **multichannel unitarity** is essential.



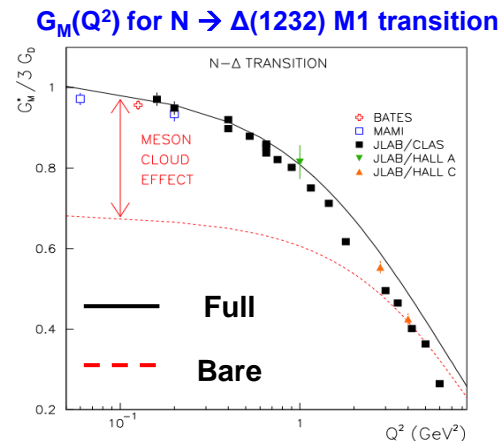
- ✓ Employ a **Dynamical Coupled-Channels (DCC)** approach for meson production reactions  
 ➔ Matsuyama, Sato, Lee, Phys. Rep. 439(2007)193

# Why DCC approach ??

- Given the lack of “complete” data, **theoretical guidance** as taken within DCC approaches (introducing model Hamiltonian etc.) will be **effective for reducing experimental uncertainties** in determining partial wave amplitude and extracting resonance parameters.
- If one wants to explore and understand the **physics** behind hadron resonances (dynamical origin and internal structure, etc.), one **needs a model** that appropriately describes the dynamics of reaction processes.



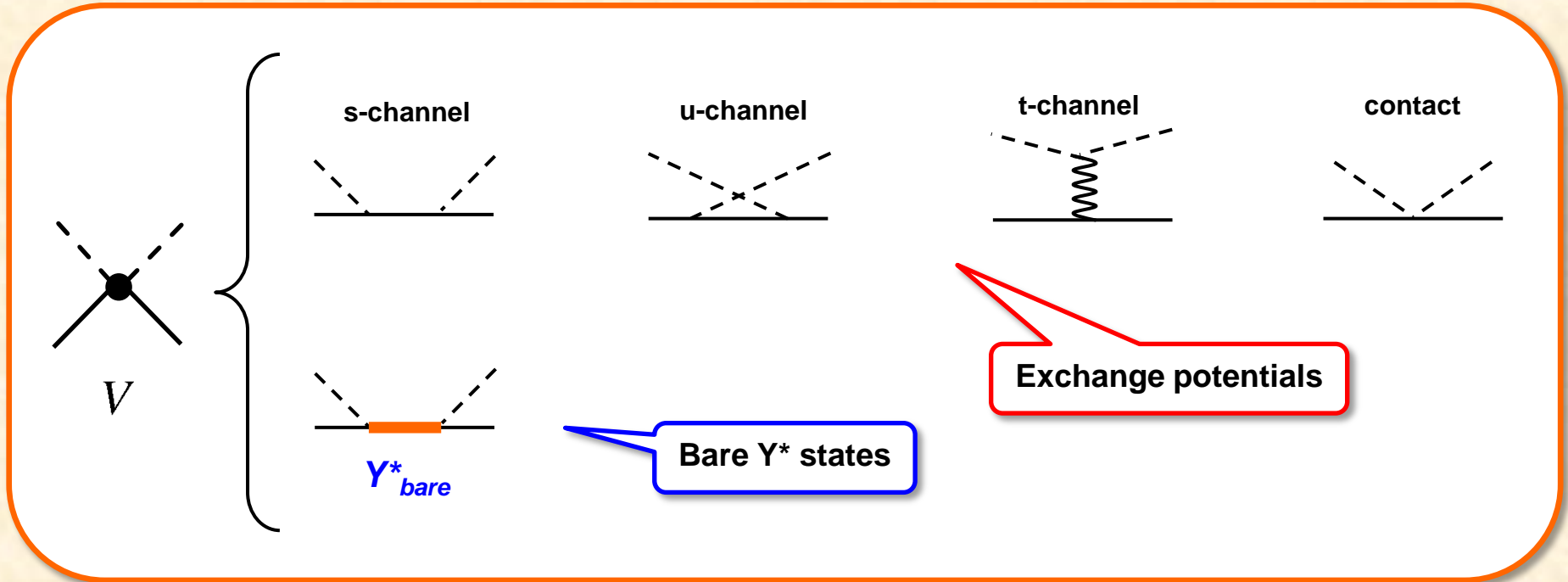
Suzuki, Julia-Diaz, HK, Lee, Matsuyama, Sato  
PRL104 065203 (2010)



Julia-Diaz, Lee, Sato, Smith PRC75 015205 (2007)

# Dynamical coupled-channels (DCC) model for $Y^*$ production reactions

HK, Nakamura, Lee, Sato, arXiv:1407.6839 (with updates)



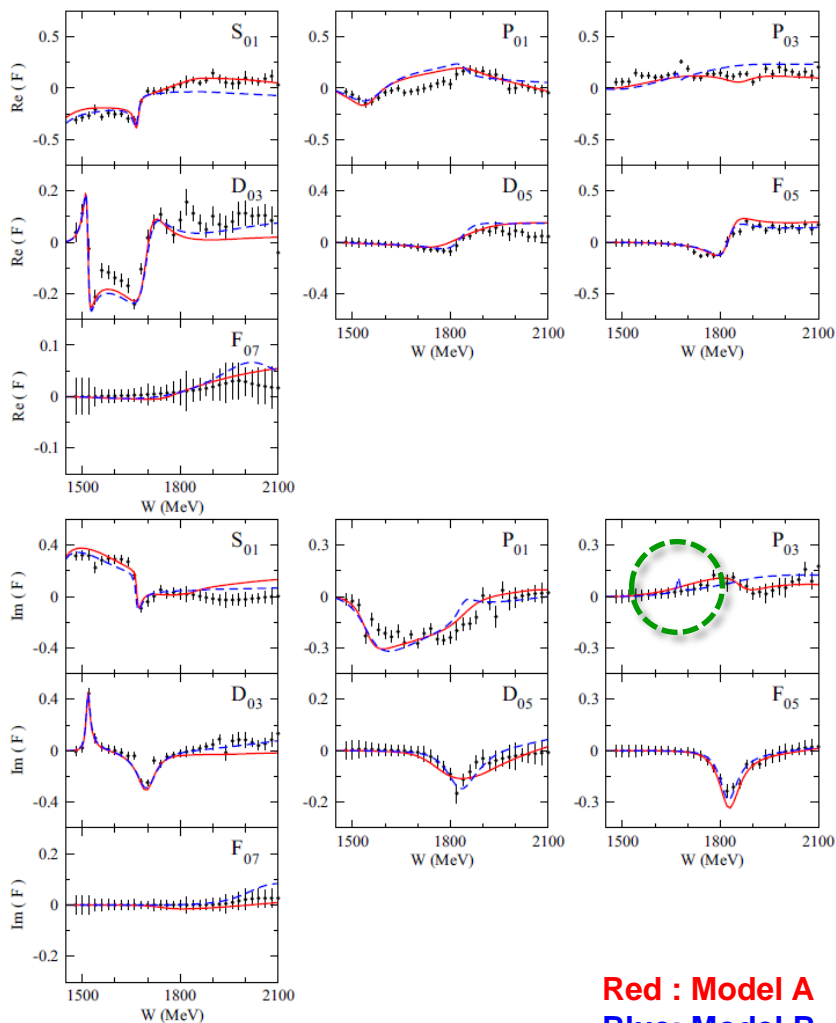
$$V_{a,b} = v_{a,b} + \sum_{Y^*} \frac{\Gamma_{Y^*,a}^\dagger \Gamma_{Y^*,b}}{E - M_{Y^*}}$$

Exchange potentials
bare  $Y^*$  states

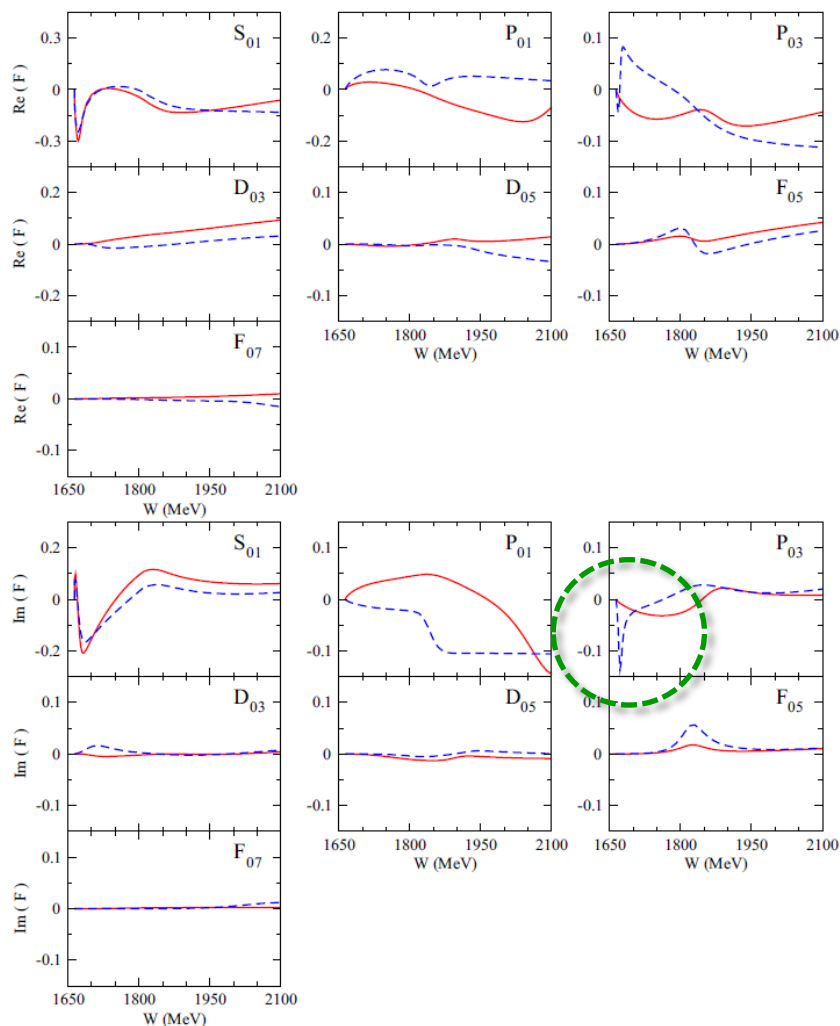
# Contribution of narrow P03 resonance to amplitudes

HK, Nakamura, Lee, Sato, PRC90(2014)065204

## Extracted $\bar{K}N \rightarrow \pi\Sigma$ amplitudes



## Extracted $\bar{K}N \rightarrow \eta\Lambda$ amplitudes

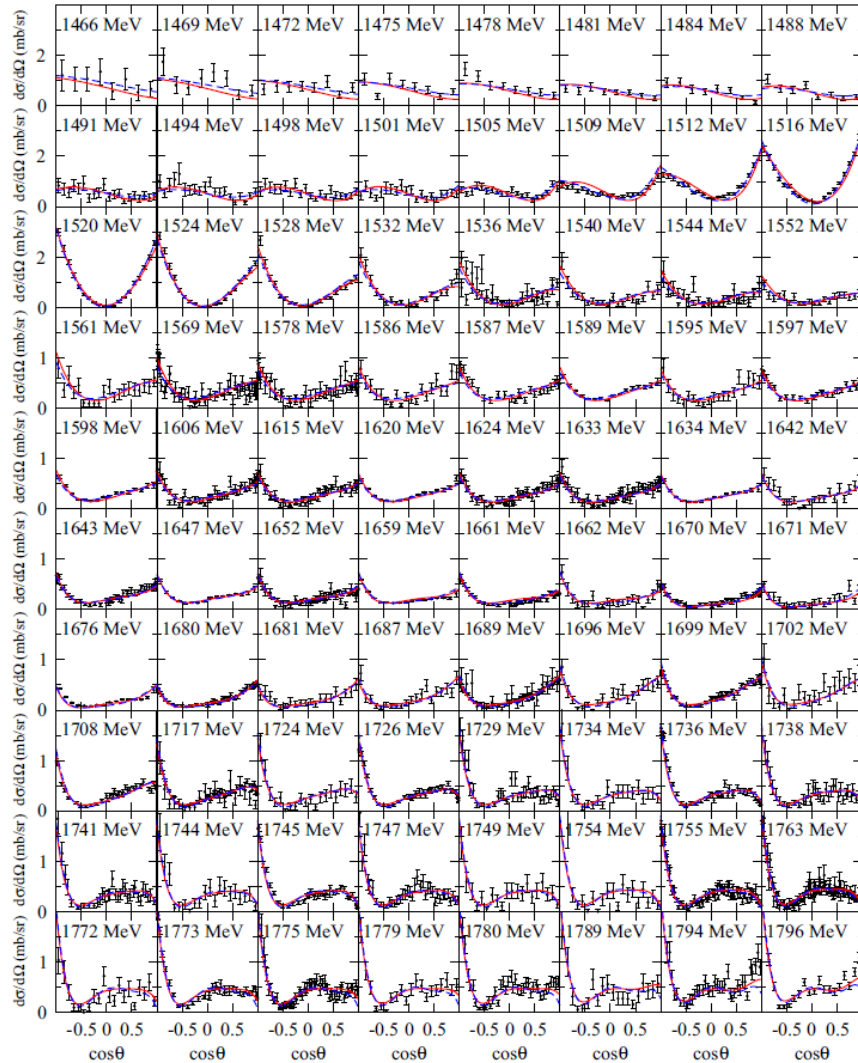


# Results of the fits

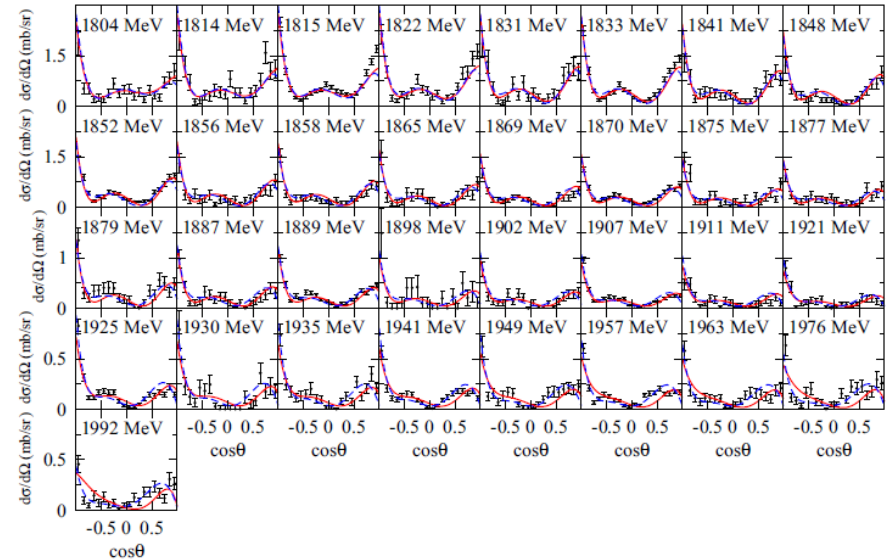
**$K^- p \rightarrow K^0 n$  reaction**

HK, Nakamura, Lee, Sato, PRC90(2014)065204

**$d\sigma/d\Omega$  ( $1466 < W < 1796$  MeV)**



**$d\sigma/d\Omega$  ( $1804 < W < 1992$  MeV)**



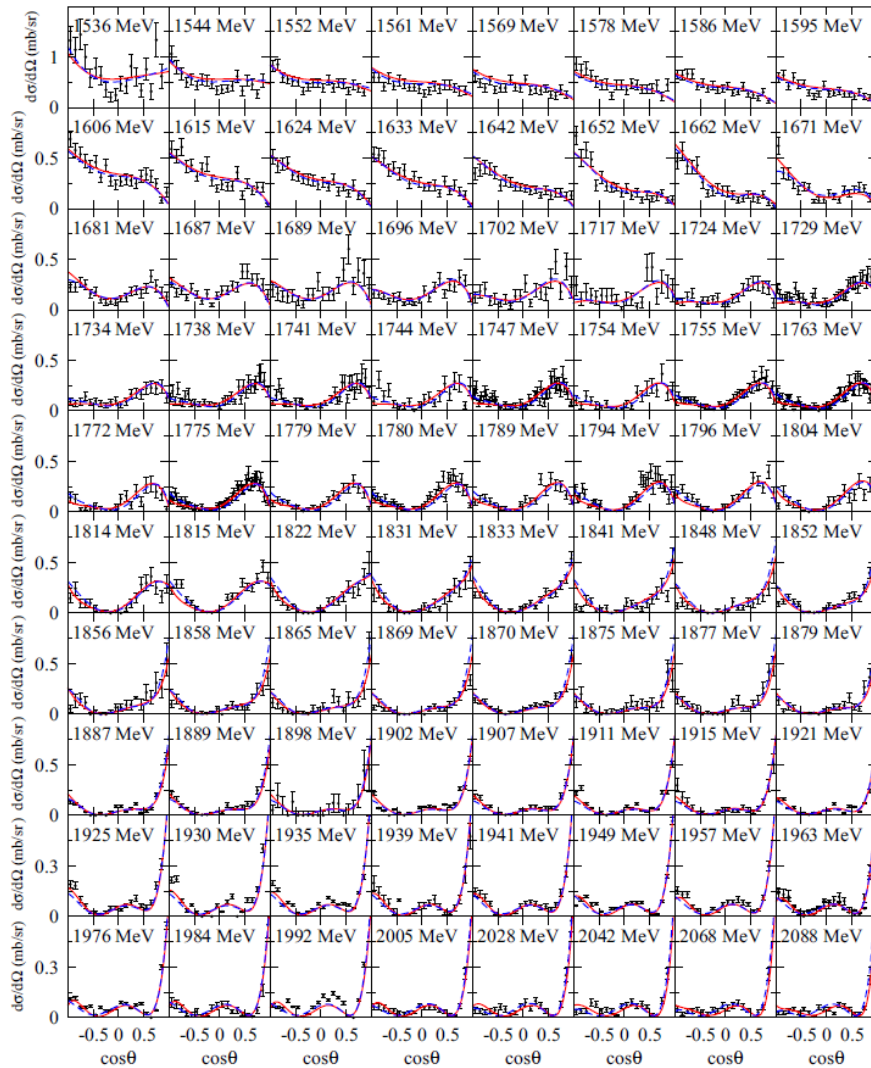
**Red: Model A Blue: Model B**

# Results of the fits

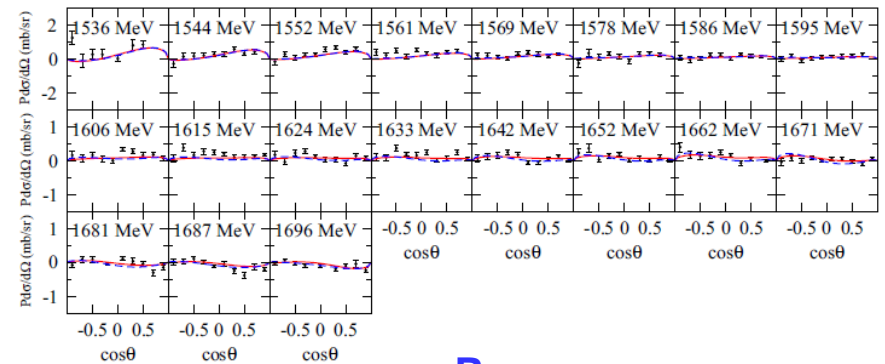
$K^- p \rightarrow \pi^- \Sigma^+$  reaction

HK, Nakamura, Lee, Sato, PRC90(2014)065204

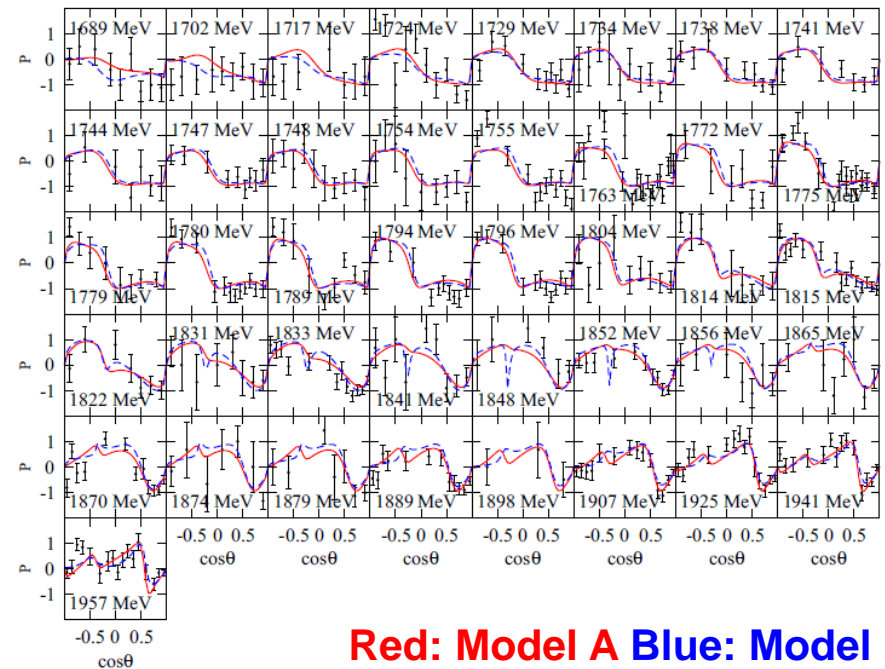
$d\sigma/d\Omega$



$P \times d\sigma/d\Omega$



$P$



Red: Model A Blue: Model B

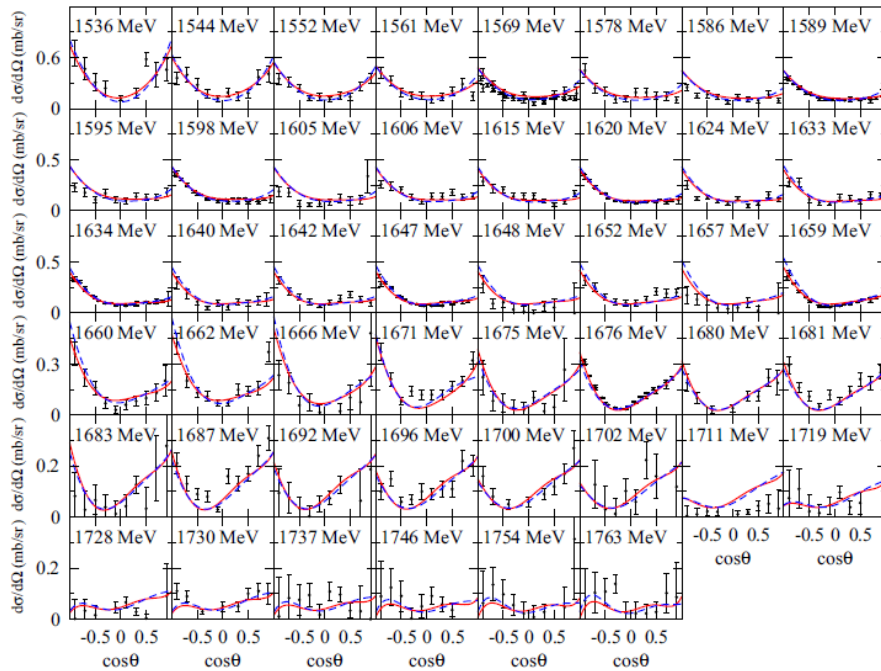


# Results of the fits

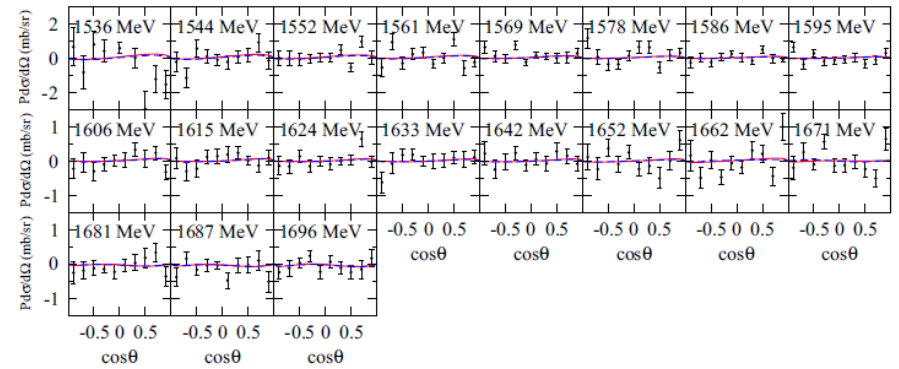
$K^- p \rightarrow \pi^0 \Sigma^0$  reaction

HK, Nakamura, Lee, Sato, PRC90(2014)065204

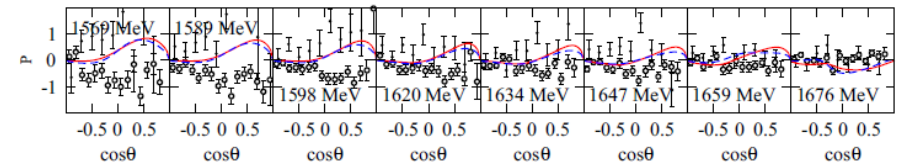
$d\sigma/d\Omega$



$P \times d\sigma/d\Omega$



$P$



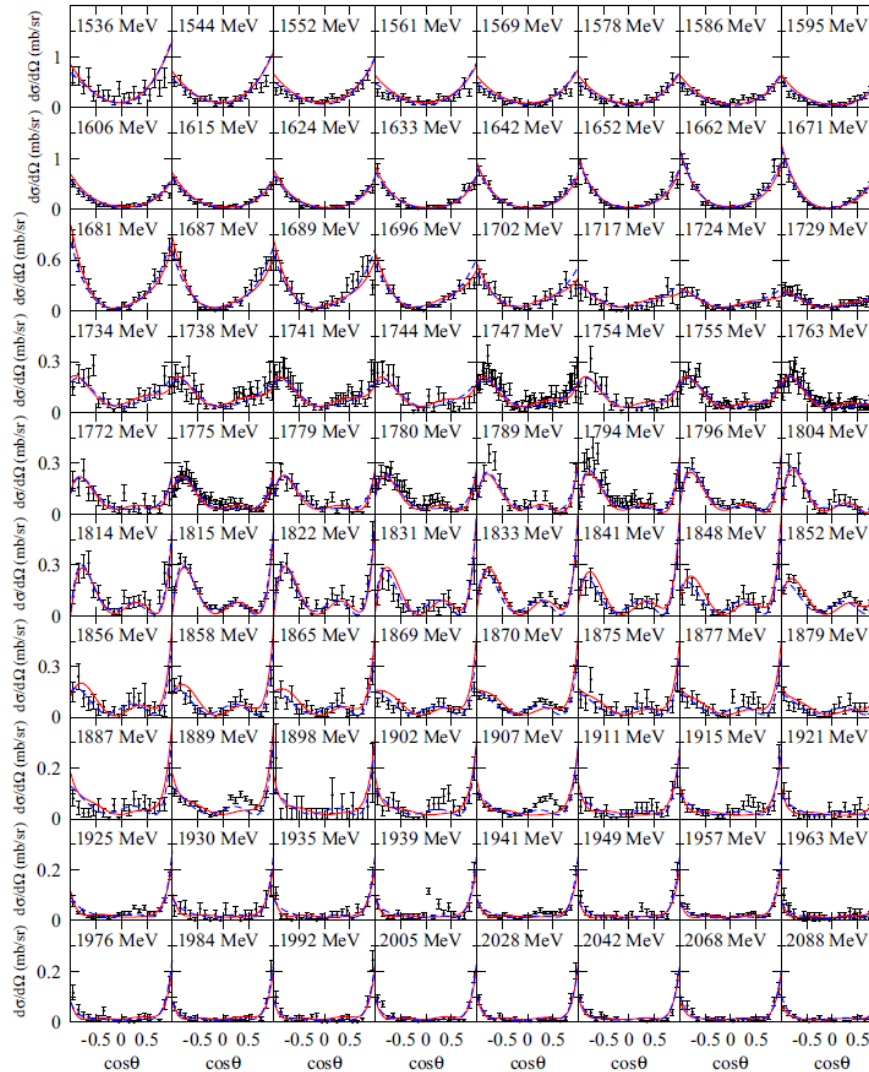
Red: Model A Blue: Model B

# Results of the fits

$K^- p \rightarrow \pi^+ \Sigma^-$  reaction

HK, Nakamura, Lee, Sato, PRC90(2014)065204

$d\sigma/d\Omega$



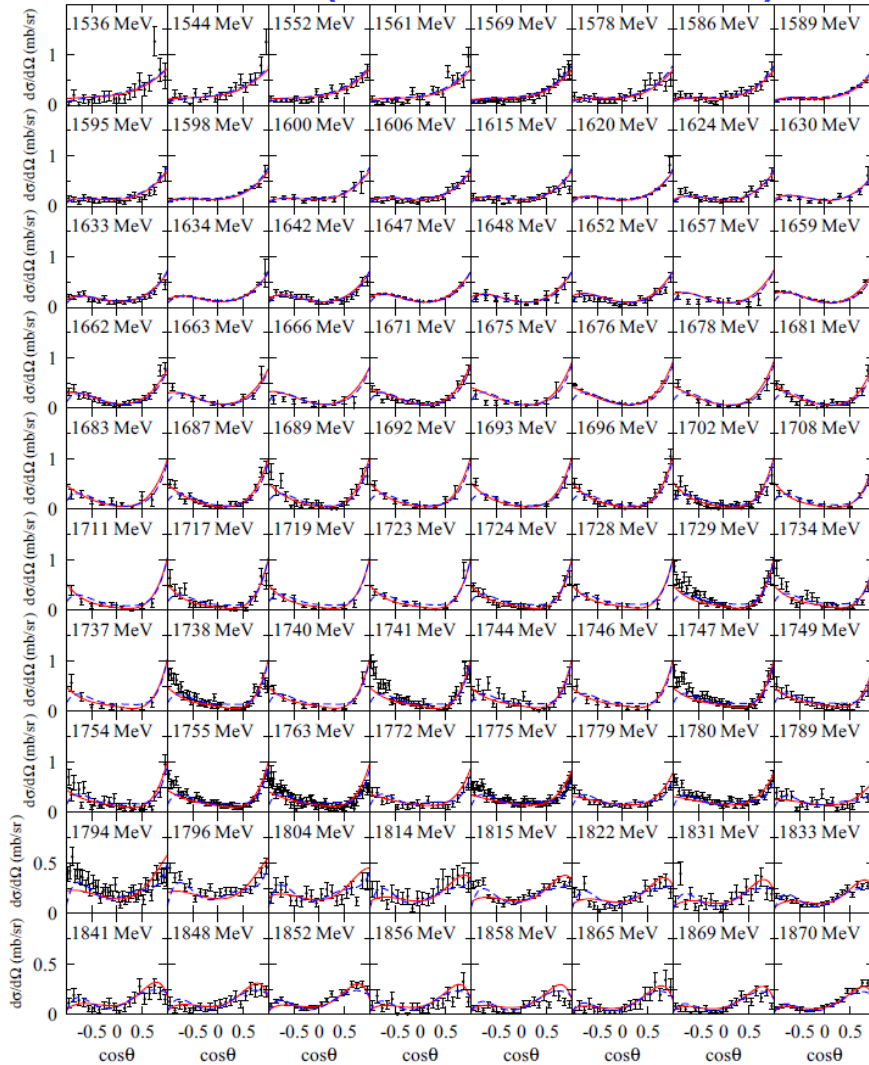
Red: Model A Blue: Model B

# Results of the fits

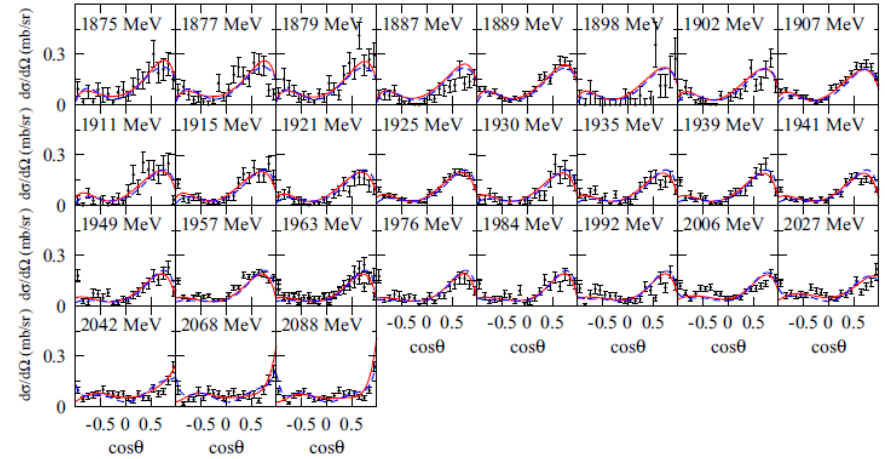
$K^- p \rightarrow \pi^0 \Lambda$  reaction

HK, Nakamura, Lee, Sato, PRC90(2014)065204

$d\sigma/d\Omega$  ( $1536 < W < 1870$  MeV)



$d\sigma/d\Omega$  ( $1875 < W < 2088$  MeV)



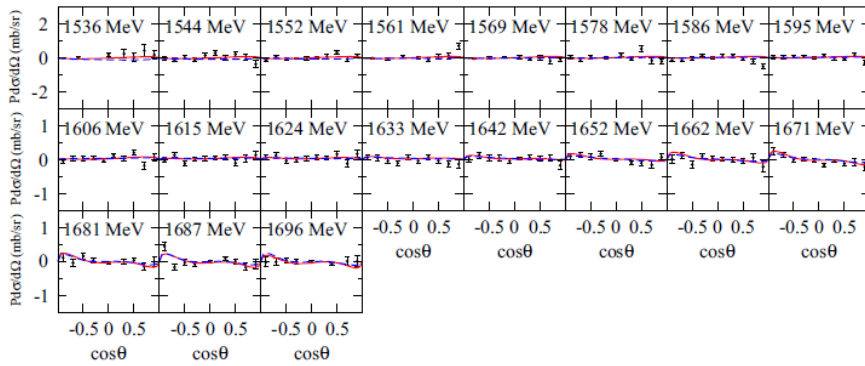
Red: Model A Blue: Model B

# Results of the fits

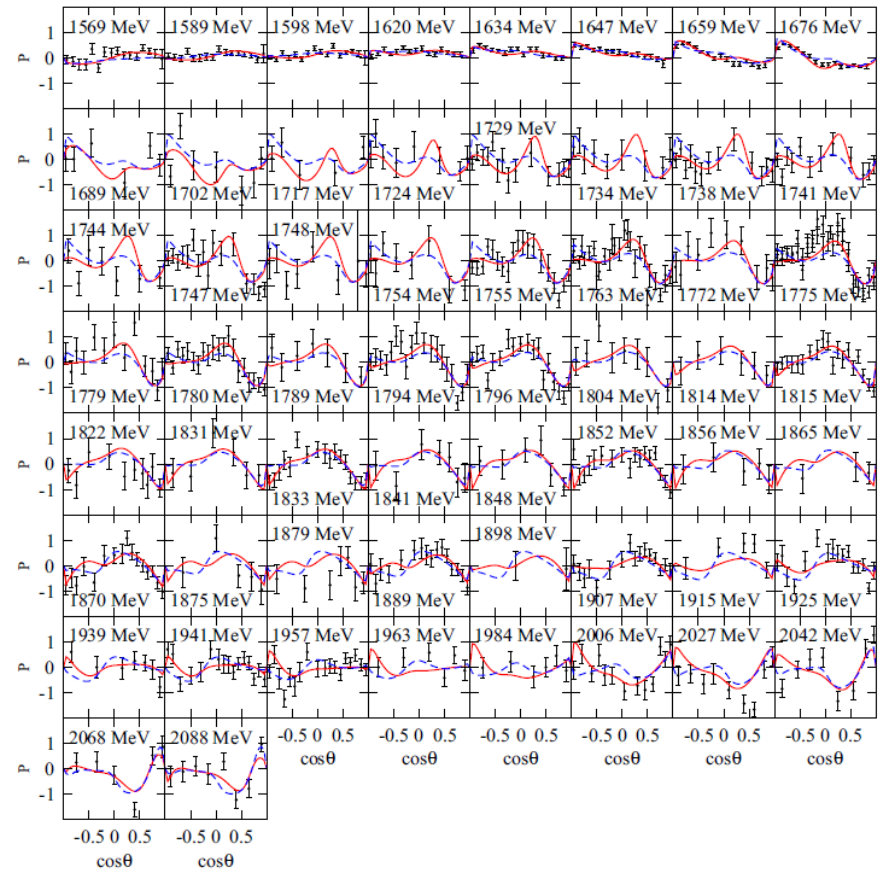
HK, Nakamura, Lee, Sato, PRC90(2014)065204

$K^- p \rightarrow \pi^0 \Lambda$  reaction (cont'd)

$P \times d\sigma/d\Omega$



P



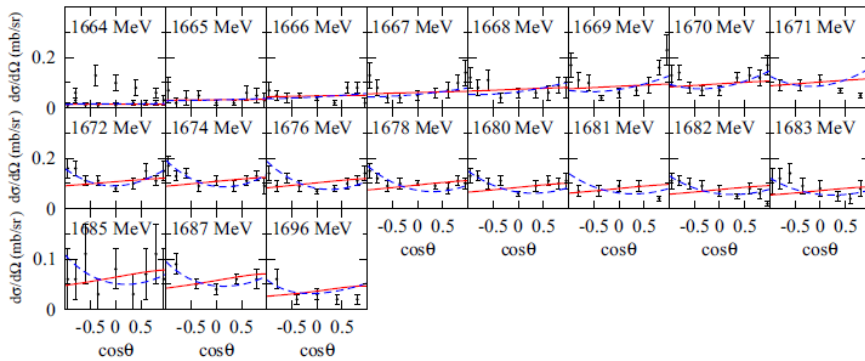
Red: Model A Blue: Model B

# Results of the fits

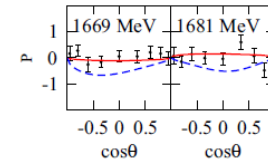
HK, Nakamura, Lee, Sato, PRC90(2014)065204

## $K^- p \rightarrow \eta \Lambda$ reaction

$d\sigma/d\Omega$

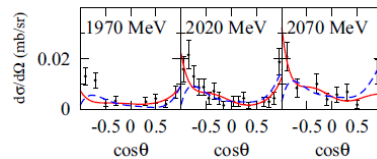


P



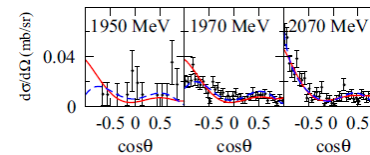
## $K^- p \rightarrow K^0 \Xi^0$ reaction

$d\sigma/d\Omega$



## $K^- p \rightarrow K^+ \Xi^-$ reaction

$d\sigma/d\Omega$



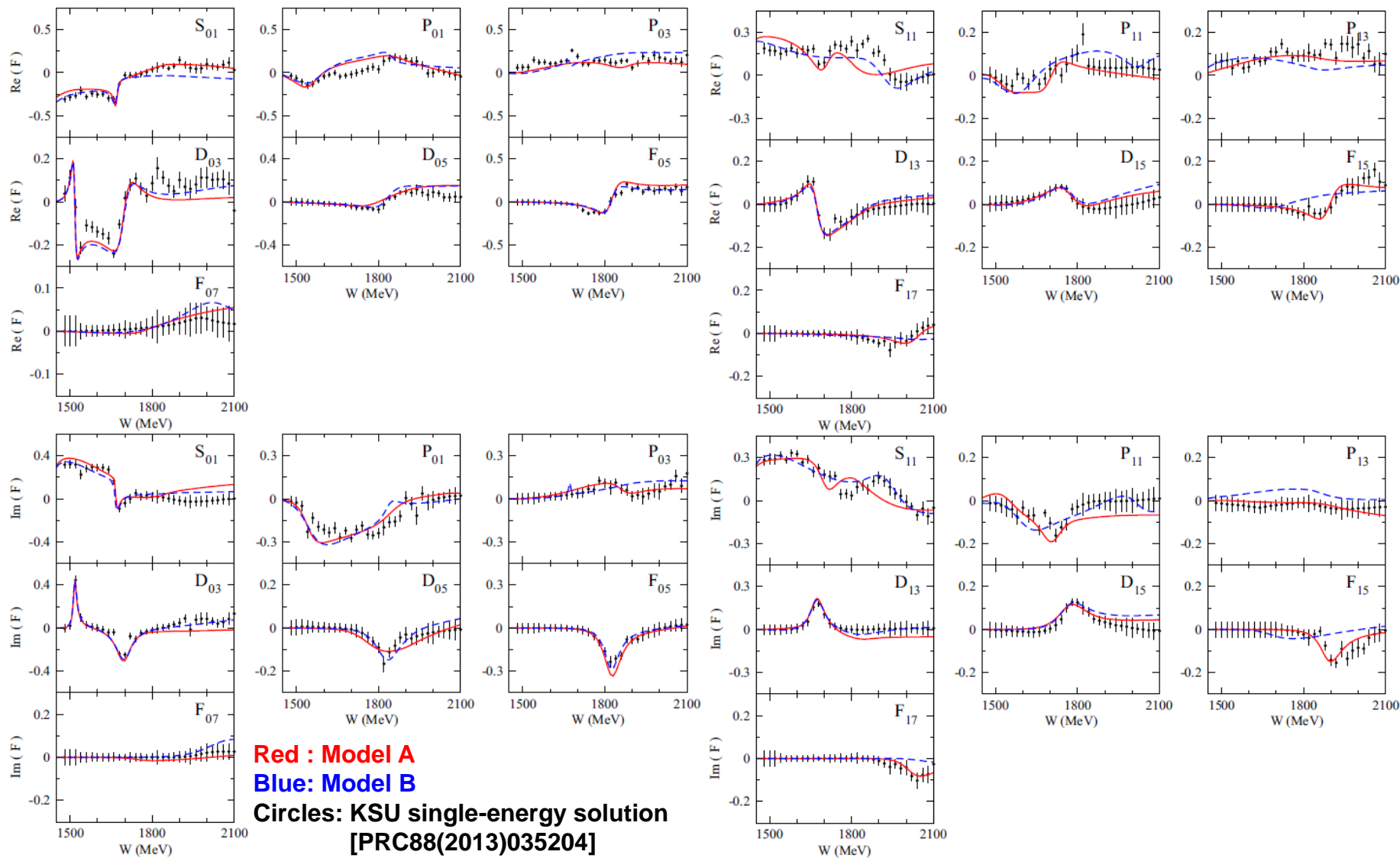
Red: Model A Blue: Model B

# Comparison of extracted partial-wave amplitudes

Extracted  $\bar{K}N \rightarrow \pi\Sigma$  amplitudes

HK, Nakamura, Lee, Sato, PRC90(2014)065204

$L_{I2J}$  :  $L = S, P, \dots$  ;  $I =$  isospin;  $J =$  Total angular mom.



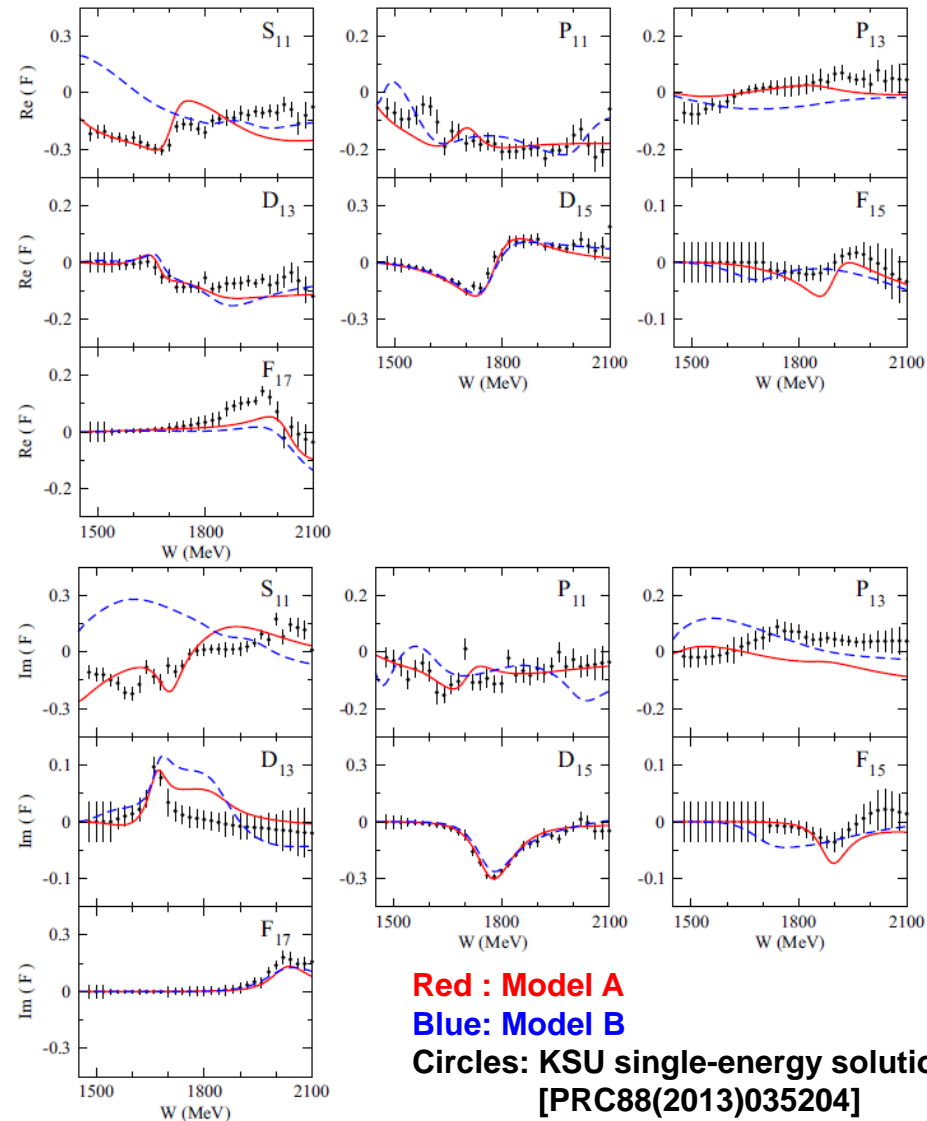
# Comparison of extracted partial-wave amplitudes

Extracted  $\bar{K}N \rightarrow \pi\Lambda$  amplitudes

HK, Nakamura, Lee, Sato, PRC90(2014)065204

$L_{12J}$  :  $L = S, P, \dots$  ;  $I =$  isospin;  $J =$  Total angular mom.

Sizable analysis dependence seen in S11 etc., even though the three analyses reproduce the available data equally well.

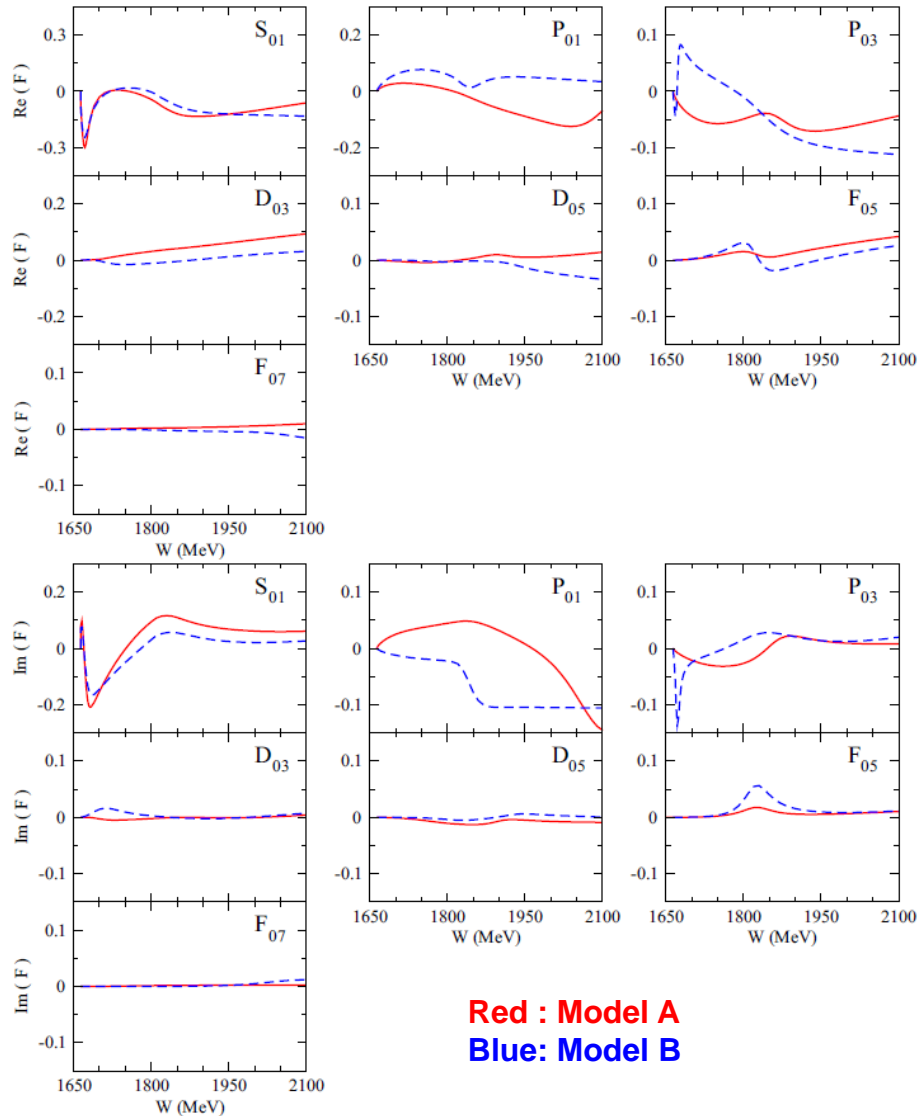


# Comparison of extracted partial-wave amplitudes

Extracted  $\bar{K}N \rightarrow \eta\Lambda$  amplitudes

HK, Nakamura, Lee, Sato, PRC90(2014)065204

$L_{I2J}$  :  $L = S, P, \dots$  ;  $I =$  isospin;  $J =$  Total angular mom.



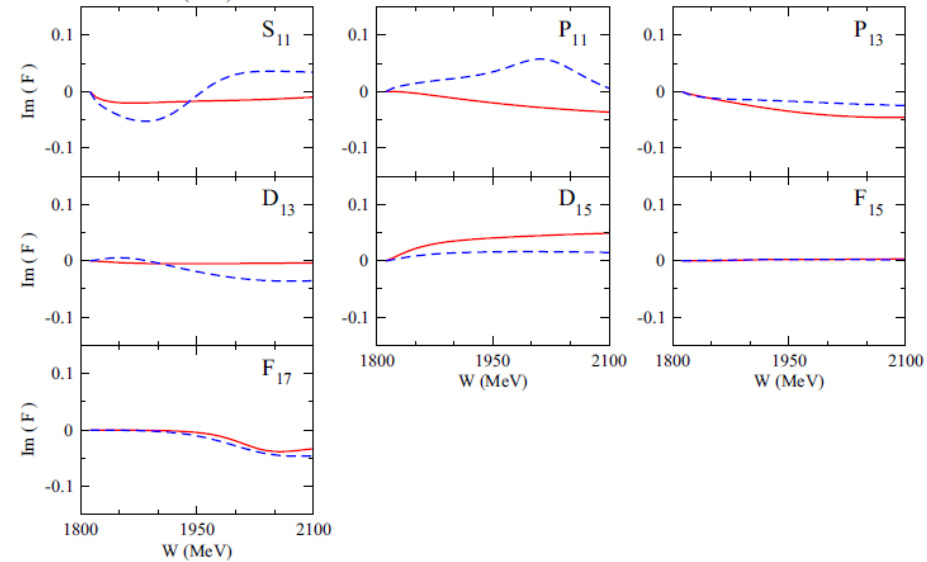
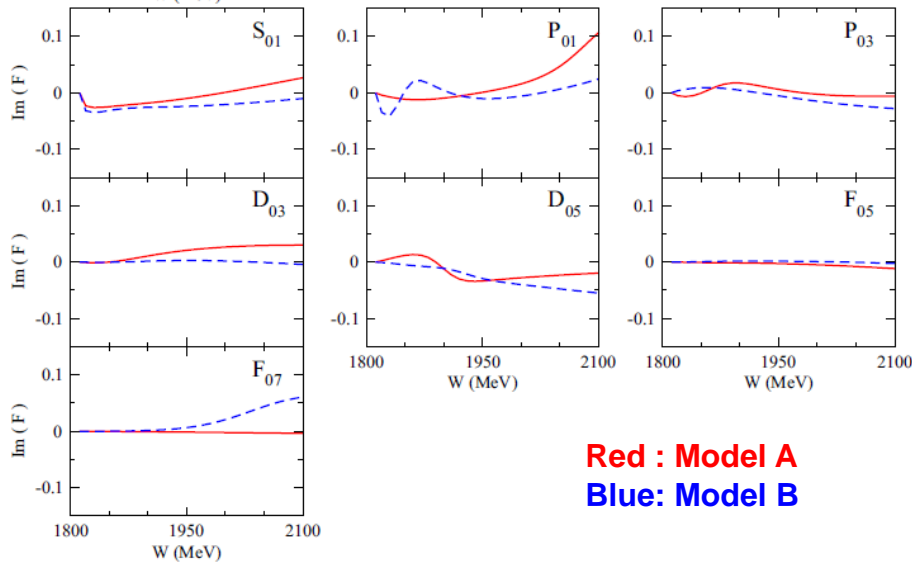
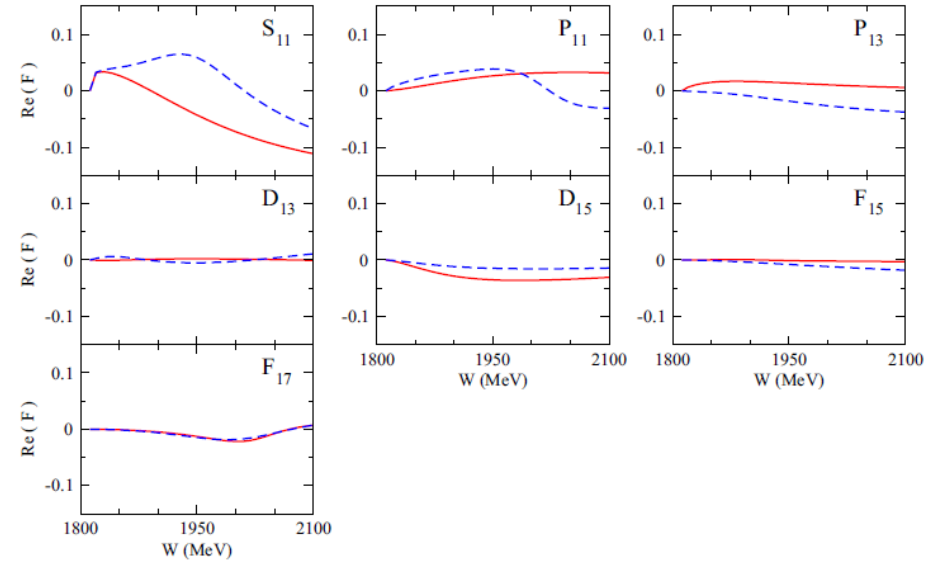
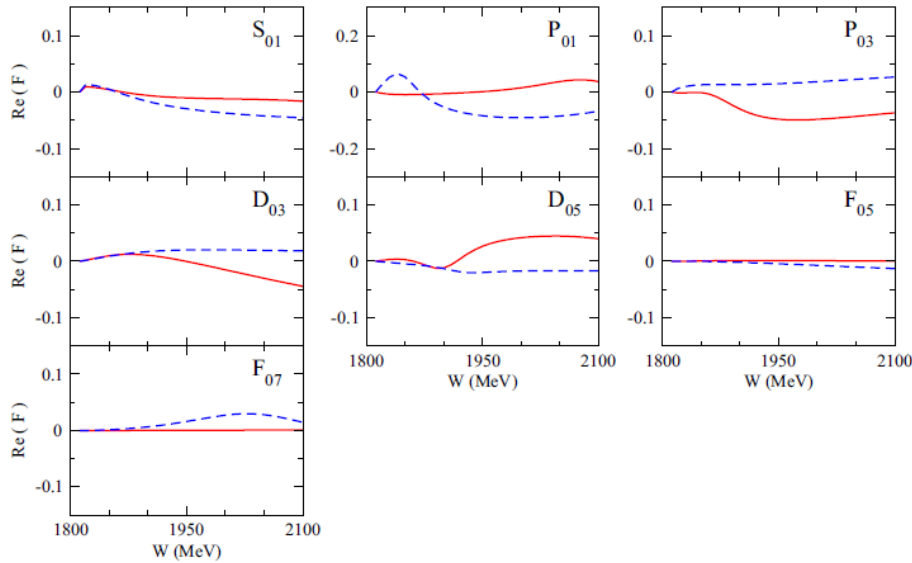


# Comparison of extracted partial-wave amplitudes

## Extracted $\bar{K}N \rightarrow K\bar{E}$ amplitudes

HK, Nakamura, Lee, Sato, PRC90(2014)065204

$L_{12J}$  :  $L = S, P, \dots$  ;  $I =$  isospin;  $J =$  Total angular mom.



Red : Model A  
Blue: Model B

# Extracted scattering lengths and effective ranges

HK, Nakamura, Lee, Sato, PRC90(2014)065204

## Scattering length and effective range

	Model A		Model B	
	$I = 0$	$I = 1$	$I = 0$	$I = 1$
$a_{\bar{K}N}$ (fm)	$-1.37 + i0.67$	$0.07 + i0.81$	$-1.62 + i1.02$	$0.33 + i0.49$
$a_{\eta\Lambda}$ (fm)	$1.35 + i0.36$	-	$0.97 + i0.51$	-
$a_{K\Xi}$ (fm)	$-0.81 + i0.14$	$-0.68 + i0.09$	$-0.89 + i0.13$	$-0.83 + i0.03$
$r_{\bar{K}N}$ (fm)	$0.67 - i0.25$	$1.01 - i0.20$	$0.74 - i0.25$	$-1.03 + i0.19$
$r_{\eta\Lambda}$ (fm)	$-5.67 - i2.24$	-	$-5.82 - i3.32$	-
$r_{K\Xi}$ (fm)	$-0.01 - i0.33$	$-0.42 - i0.49$	$0.13 - i0.20$	$-0.22 - i0.11$

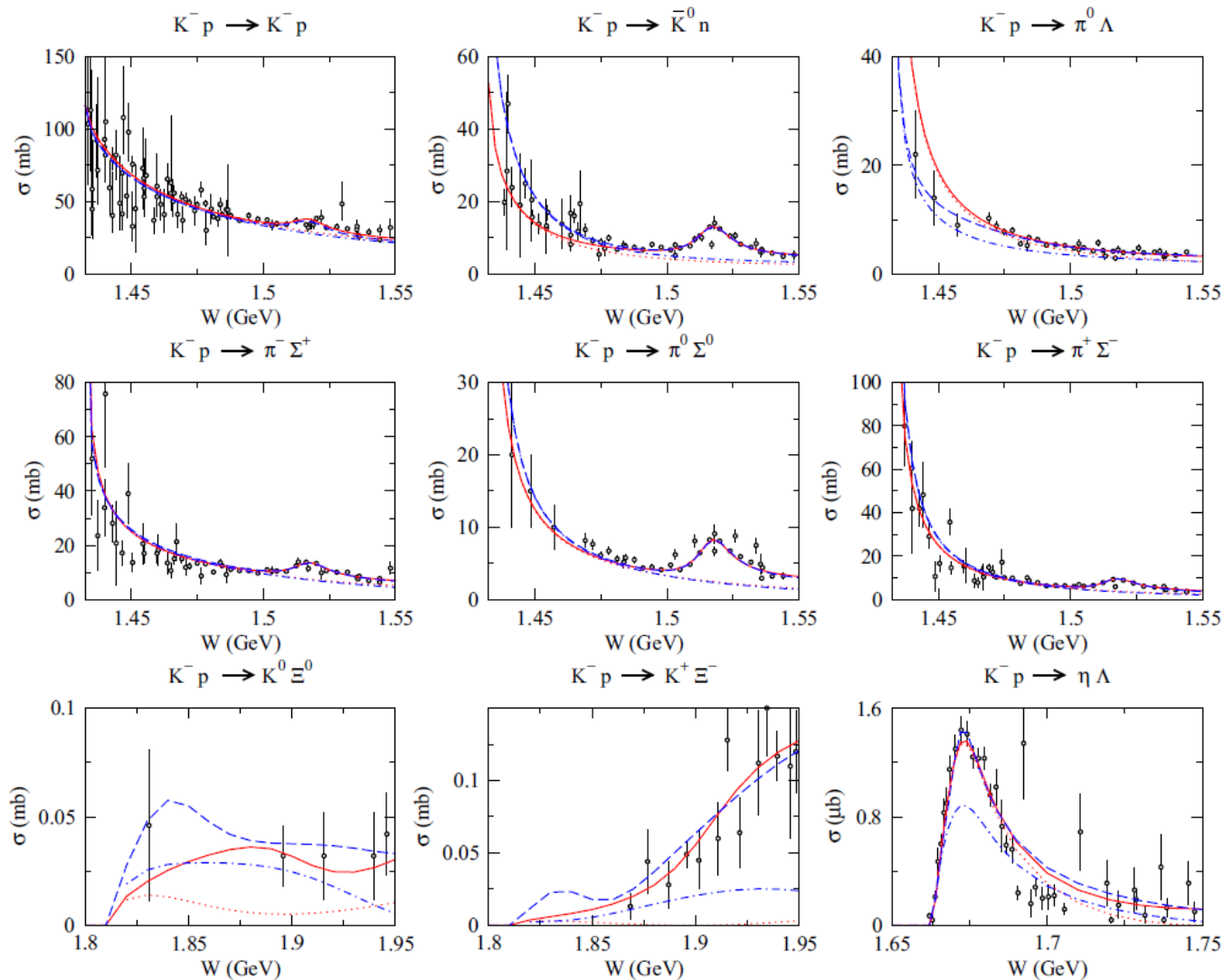
$$a_{K-p} = -0.65 + i0.74 \text{ fm (Model A)}$$

$$a_{K-p} = -0.65 + i0.76 \text{ fm (Model B)}$$

# S-wave contributions in the threshold region

$K^- p \rightarrow MB$  total cross sections

HK, Nakamura, Lee, Sato, PRC90(2014)065204



Red: Model A

Blue: Model B