



Photoproduction of the scalar mesons $f_0(980)$ and $f_0(500)$ off the nucleon

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Outline

- Motivation
- Theoretical Framework
 - Effective Lagrangian Approach
 - Coupling Constants
 - Regge Propagators
- Numerical Result
- Summary and Outlook

Motivation

- Scalar mesons
 - $I^G(J^{PC}) = 0^+(0^{++})$
 - Long-standing puzzle
 - Large decay widths
 - Interpretation of structure is not clear
 - Lack of information about the production mechanism

Motivation

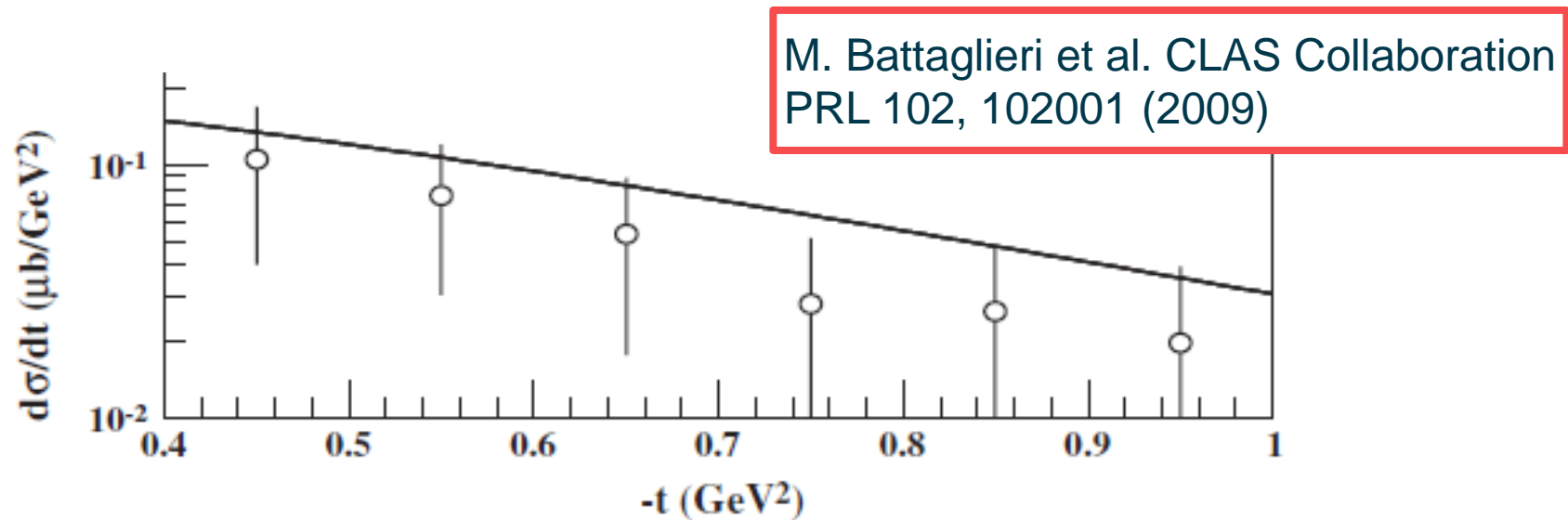
Name	Mass [MeV]	Width [MeV]	$I^G(J^{PC})$
$f_0(980)$	990	40 – 100	$0^+(0^{++})$
$f_0(500)$	400 – 550	400 – 700	$0^+(0^{++})$

- Both of them exist in $\pi\pi$ scattering

K.A. Olive et al., (Particle Data Group), Chin. Phys. **C 38**, 090001 (2014).

Motivation

- $(\pi\pi)_{s\text{-wave}}^{I=0}$ photoproduction has been reported.



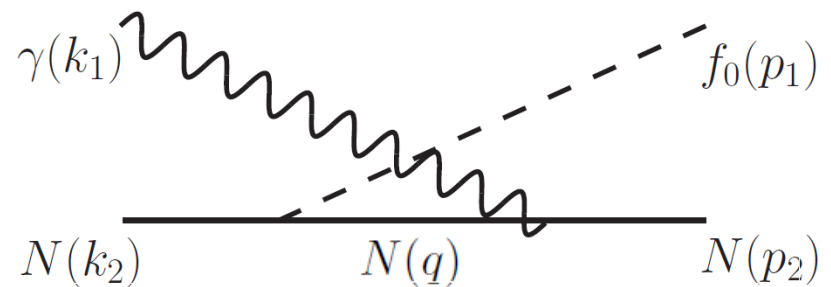
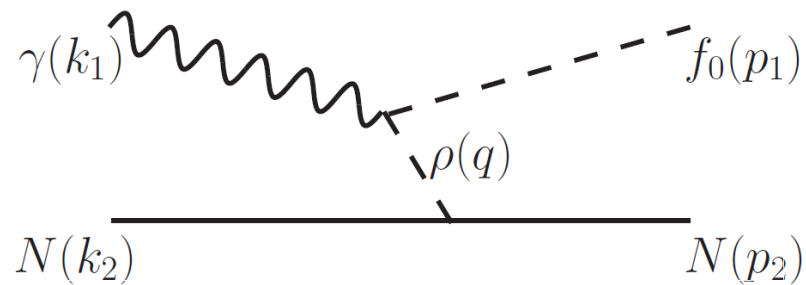
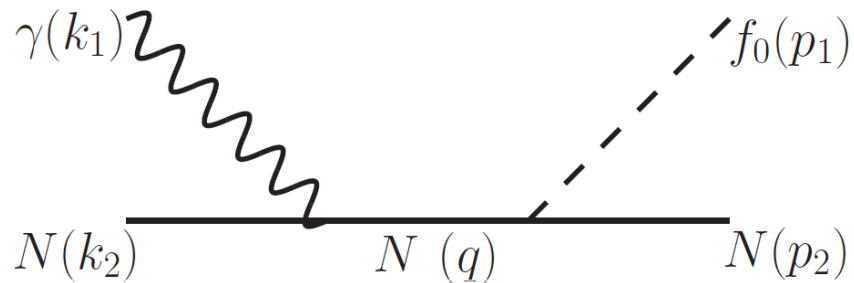
- CLAS collaboration. M. Bellis et al., Proposal to the PAC, E-06-013. at Jefferson Lab.

Theoretical Framework

- Effective Lagrangian Approach
- Coupling Constants
- Regge Propagators

Effective Lagrangians Approach

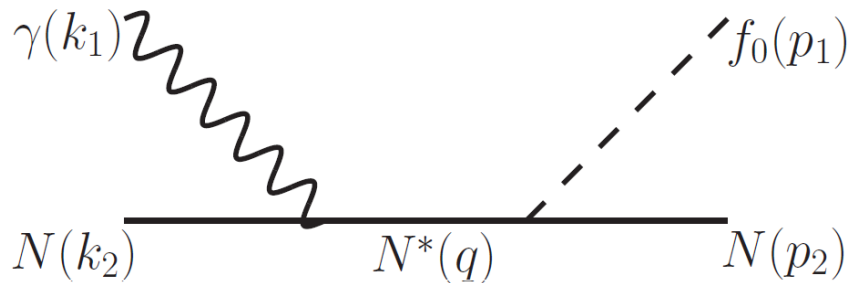
$$\gamma N \rightarrow f_0(980)N$$



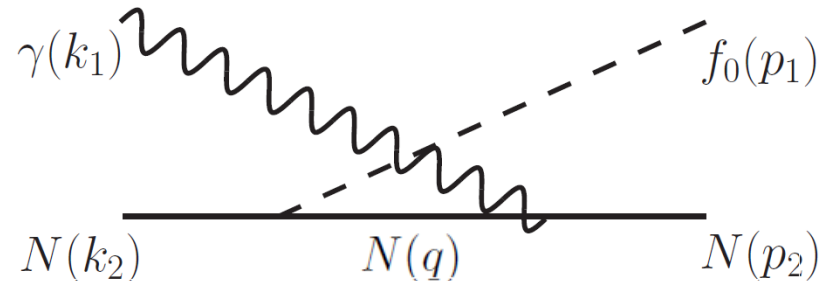
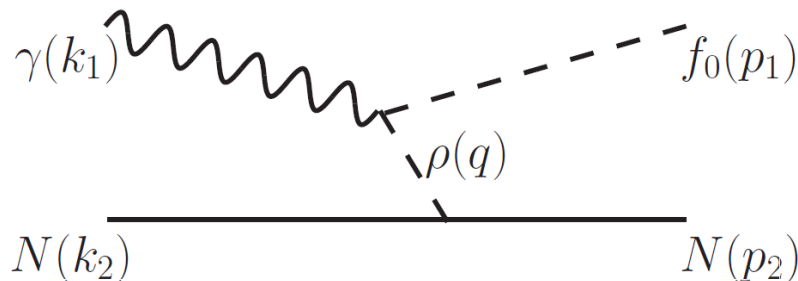
Effective Lagrangians Approach

$$\gamma N \rightarrow f_0(500) N$$

Resonance	$I(J^P)$	Status
N(1440)	$\frac{1}{2}(\frac{1}{2}^+)$	****
N(1535)	$\frac{1}{2}(\frac{1}{2}^-)$	****
N(1710)	$\frac{1}{2}(\frac{1}{2}^+)$	***



K.A. Olive et al., (Particle Data Group),
Chin. Phys. **C 38**, 090001 (2014).

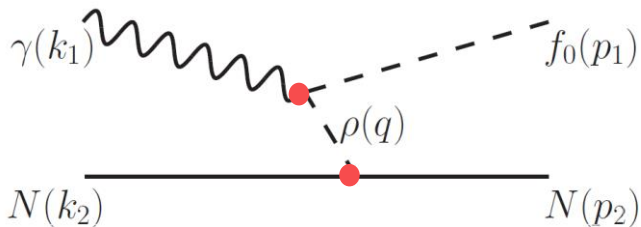


Effective Lagrangians Approach

$$\gamma N \rightarrow f_0(980)N$$

$$\gamma N \rightarrow f_0(500)N$$

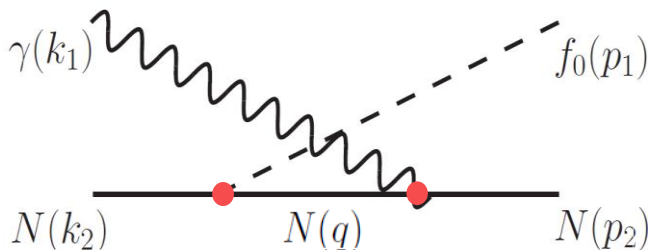
t-channel : ρ



$$\mathcal{L}_{\gamma\rho f_0} = \frac{g_{\gamma\rho f_0}}{m_\rho} [\partial_\mu A_\nu \partial^\mu \rho^\nu - \partial_\mu A_\nu \partial^\nu \rho^\mu] f_0$$

$$\mathcal{L}_{\rho NN} = -g_{\rho NN} \bar{N} \left[\gamma_\mu \rho^\mu - \frac{\kappa_\rho}{2m_N} \sigma^{\mu\nu} \partial_\nu \rho_\mu \right] N$$

u-channel : N(938)



$$\mathcal{L}_{\gamma NN} = -\bar{N} \left(e_N \gamma_\mu A^\mu - \frac{e\kappa_N}{2m_N} \sigma_{\mu\nu} \partial^\nu A^\mu \right) N$$

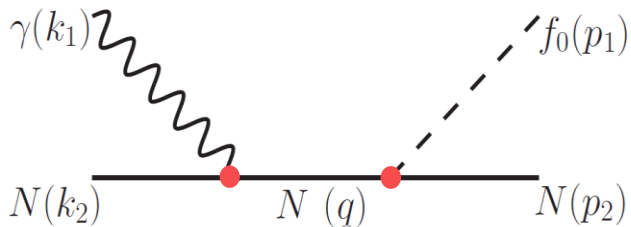
$$\mathcal{L}_{f_0 NN} = g_{f_0 NN} f_0 \bar{N} N$$

Effective Lagrangians Approach

$$\gamma N \rightarrow f_0(980) N$$

$$\gamma N \rightarrow f_0(500) N$$

s-channel : N(938)



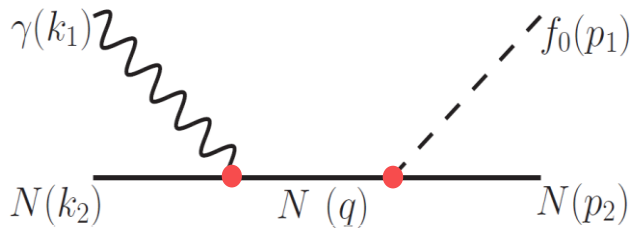
$$\mathcal{L}_{\gamma NN} = -\bar{N} \left(e_N \gamma_\mu A^\mu - \frac{e\kappa_N}{2m_N} \sigma_{\mu\nu} \partial^\nu A^\mu \right) N$$

$$\mathcal{L}_{f_0 NN} = g_{f_0 NN} f_0 \bar{N} N$$

Effective Lagrangians Approach

$$\gamma N \rightarrow f_0(500) N$$

s-channel : N(1440), N(1650), N(1710)



$$\mathcal{L}_{\gamma NN^*} \left(\frac{1^\pm}{2} \right) = \pm \frac{ef_1}{2m_N} \bar{N}^* \partial^\nu A^\mu \sigma^{\mu\nu} \Gamma^{(\mp)} N$$

$$\mathcal{L}_{f_0 NN^*} \left(\frac{1^\pm}{2} \right) = \pm g_{f_0 NN^*} f_0 \bar{N} \Gamma^{(\mp)} N^*$$

Coupling Constants

Meson vertex

Using the partial decay width

$$\Gamma = \frac{P}{8\pi m_R^2} \frac{1}{2J+1} \sum_{\lambda\gamma, s, s'} |\mathcal{M}|^2$$

$$\Gamma = \left(\text{the Breit-Wigner width of the meson} \right) \\ \times \left(\text{the branching ratio of } (\pi\pi)_{s\text{-wave}}^{I=0} \right)$$

Assumption

We only consider $(\pi\pi)_{s\text{-wave}}^{I=0}$ decay mode

Coupling Constants

$$\gamma N \rightarrow f_0(980)N$$

s- and *u*- channel

κ_p	$g_{f_0 NN}$
1.79	0.56

t- channel

κ_ρ	$g_{\rho NN}$	$g_{\gamma\rho f_0}$
6.1	3.1	0.22

B. Friman and M. Soyeur, Nucl. Phys. A 600, 477 (1996)

Coupling Constants

$$\gamma N \rightarrow f_0(500)N$$

s- channel

$$\frac{\kappa_p}{1.79} \quad \frac{g_{f_0 NN}}{5.6}$$

Name	$g_{f_0 NN^*}$
N(1440)	± 3.88166
N(1535)	± 0.962174
N(1710)	± 2.29678

t- channel

$$\frac{\kappa_\rho}{6.1} \quad \frac{g_{\rho NN}}{3.1} \quad \frac{g_{\gamma\rho f_0}}{0.25}$$

u- channel

$$\frac{\kappa_p}{1.79} \quad \frac{g_{f_0 NN}}{5.6}$$

B. Friman and M. Soyeur, Nucl. Phys. A 600, 477 (1996)
 Y. s. Oh and T. S. H. Lee, Phys. Rev. C 69, 025201 (2004)

Coupling Constants

$$\gamma N \rightarrow f_0(500)N$$

γNN vertex

Using the $R \rightarrow N\gamma$ helicity amplitude

$$A_{1/2} \left(\frac{1^\pm}{2} \right) = \mp \frac{ef_1}{2m_N} \sqrt{\frac{k_\gamma m_R}{m_N}}$$

Name	f_1
N(1440)	0.47198
N(1535)	0.803571
N(1710)	-0.237518

V. Shklyar, H. Lenske, U. Mosel, and G. Penner, Phys. Rev. C 71, 055206 (2005)

Regge Propagator

t -channel

$$\begin{aligned} D_{Regge} &= \left(\frac{s}{s_0}\right)^{\alpha_\rho(t)-1} \frac{1}{\sin[\pi\alpha_\rho(t)]} \frac{\pi\alpha'_\rho}{\Gamma[\alpha_\rho(t)]} \\ &= \left(\frac{s}{s_0}\right)^{\alpha_\rho(t)-1} \Gamma[1 - \alpha_\rho(t)] \cdot \alpha'_\rho \end{aligned}$$

u -channel

$$\begin{aligned} D_{Regge} &= \frac{\left(\frac{s}{s_0}\right)^{\alpha_N(u)-\frac{1}{2}} \pi\alpha'_N}{\Gamma[\alpha_N(u) + \frac{1}{2}] \sin\pi(\alpha_N + \frac{1}{2})} \\ &= \left(\frac{s}{s_0}\right)^{\alpha_N(u)-\frac{1}{2}} \Gamma[1 - (\alpha_N(u) + \frac{1}{2})] \alpha'_N \end{aligned}$$

Regge Trajectory

t -channel

$$\alpha_\rho(t) = 0.55 + 0.8t$$

u -channel

$$\alpha_N(u) = -0.34 + 0.98u$$

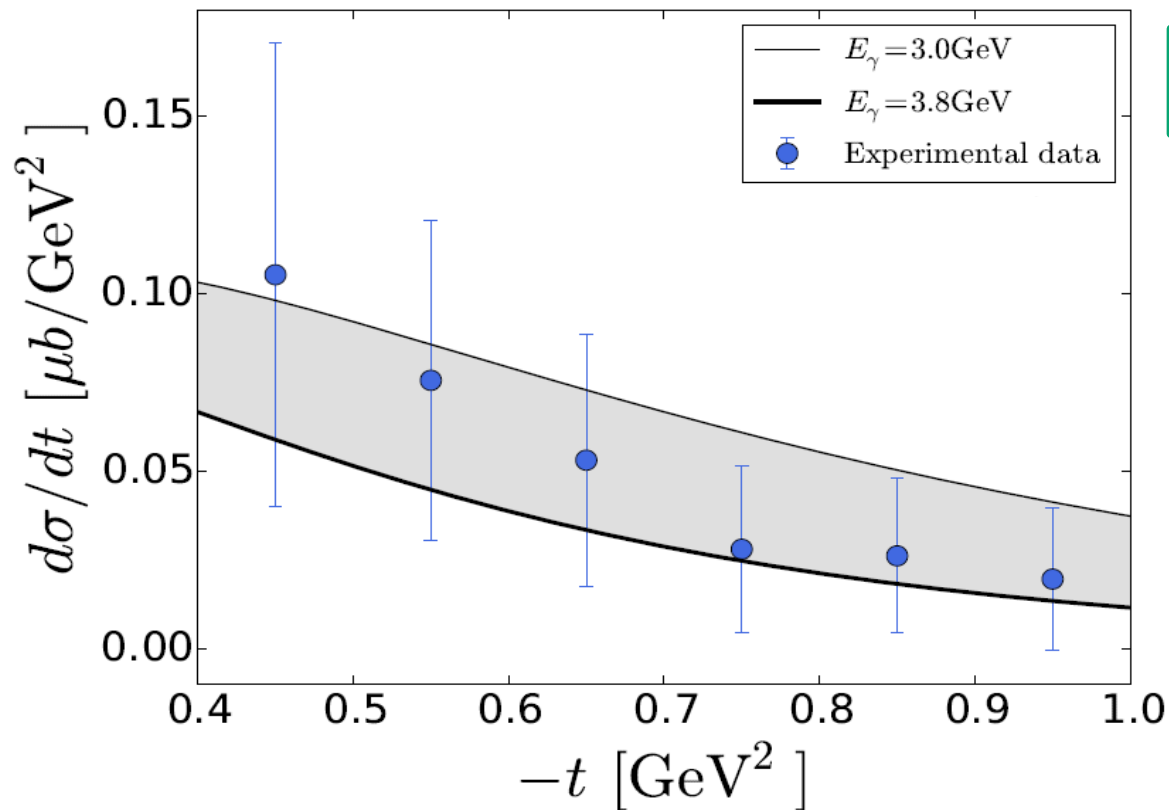
M.Guidal, J.-M Laget, M.Vanderhaeghen, Nucl. Phys. A 627, 645-678 (1997)
L. Sertorio, L.L. Wang, Phys. Rev. 178, 5 (1969)

Numerical Results

- Differential cross section of $\gamma N \rightarrow f_0(980)N$
- Total cross section of $\gamma N \rightarrow f_0(980)N$
- Differential cross section of $\gamma N \rightarrow f_0(500)N$
- Total cross section of $\gamma N \rightarrow f_0(500)N$

Differential cross section of $f_0(980)$

- To determine the cutoff and s_0 scale

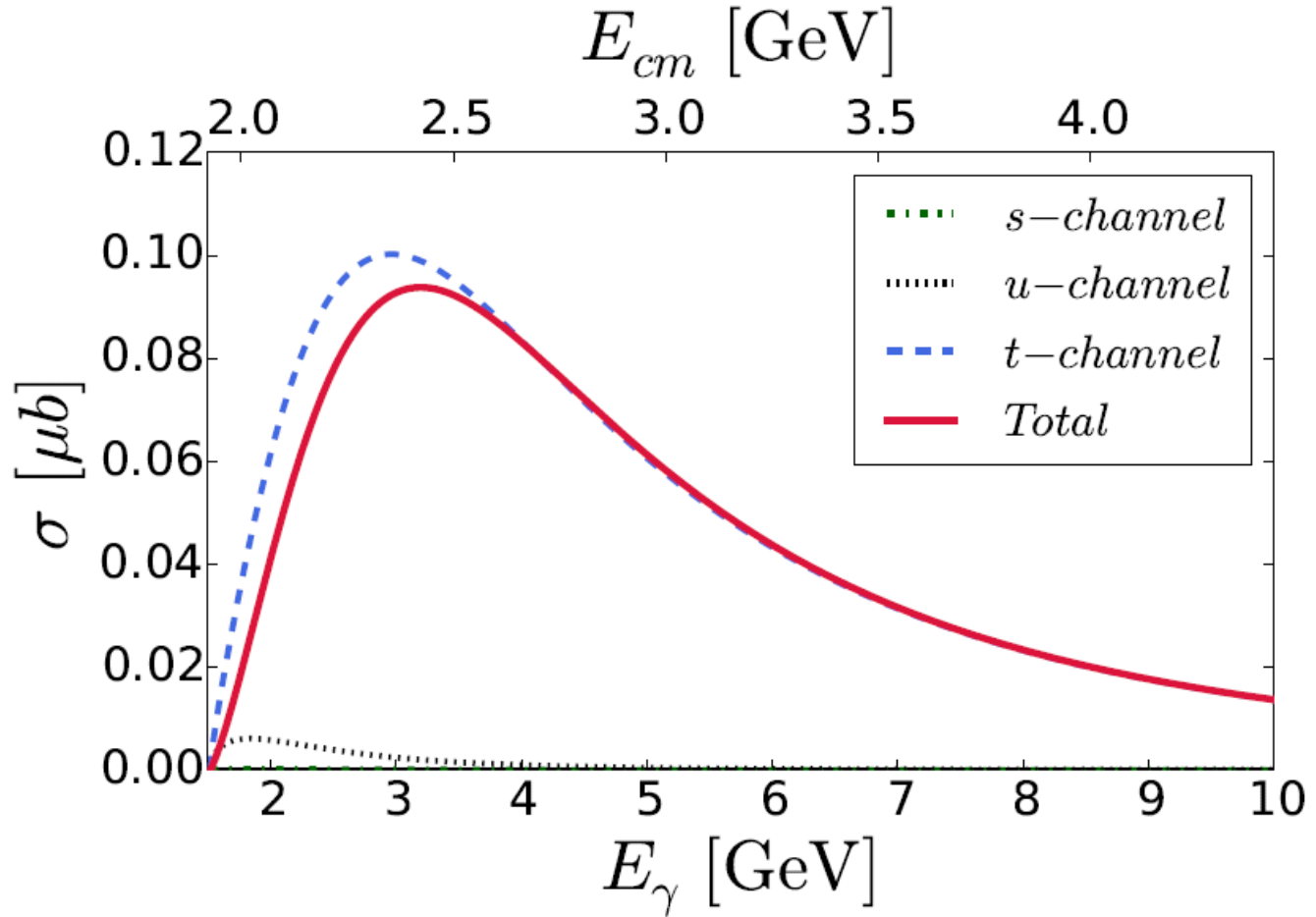


$$E_\gamma = 3.0 - 3.8 \text{ GeV}$$

$$\Lambda = 0.8 \text{ GeV}$$
$$s_0 = 1.2 \text{ GeV}^2$$

$$\frac{\Lambda^4}{\Lambda^4 + (p^2 - m_R^2)^2}$$

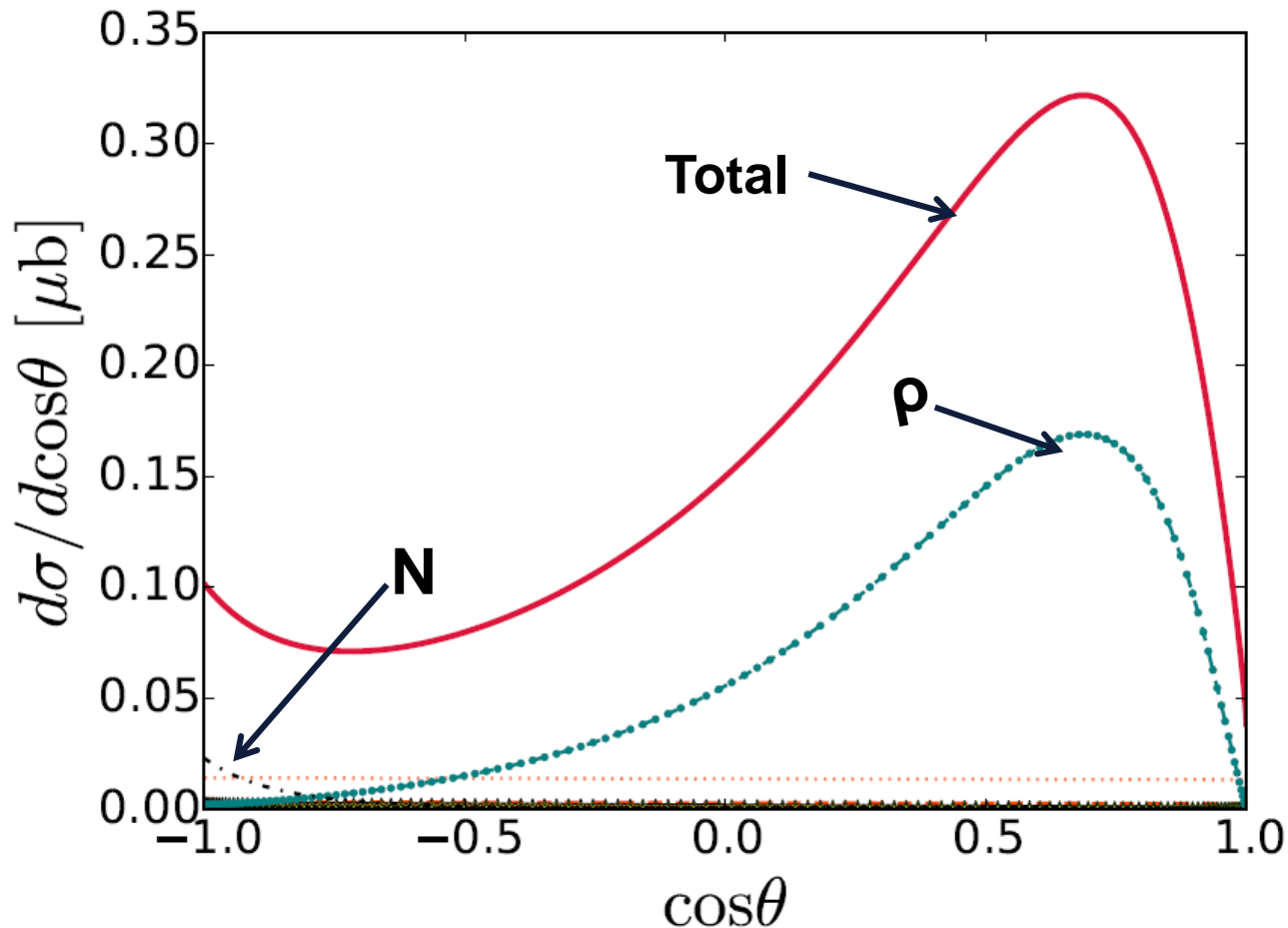
Total cross section of $f_0(980)$



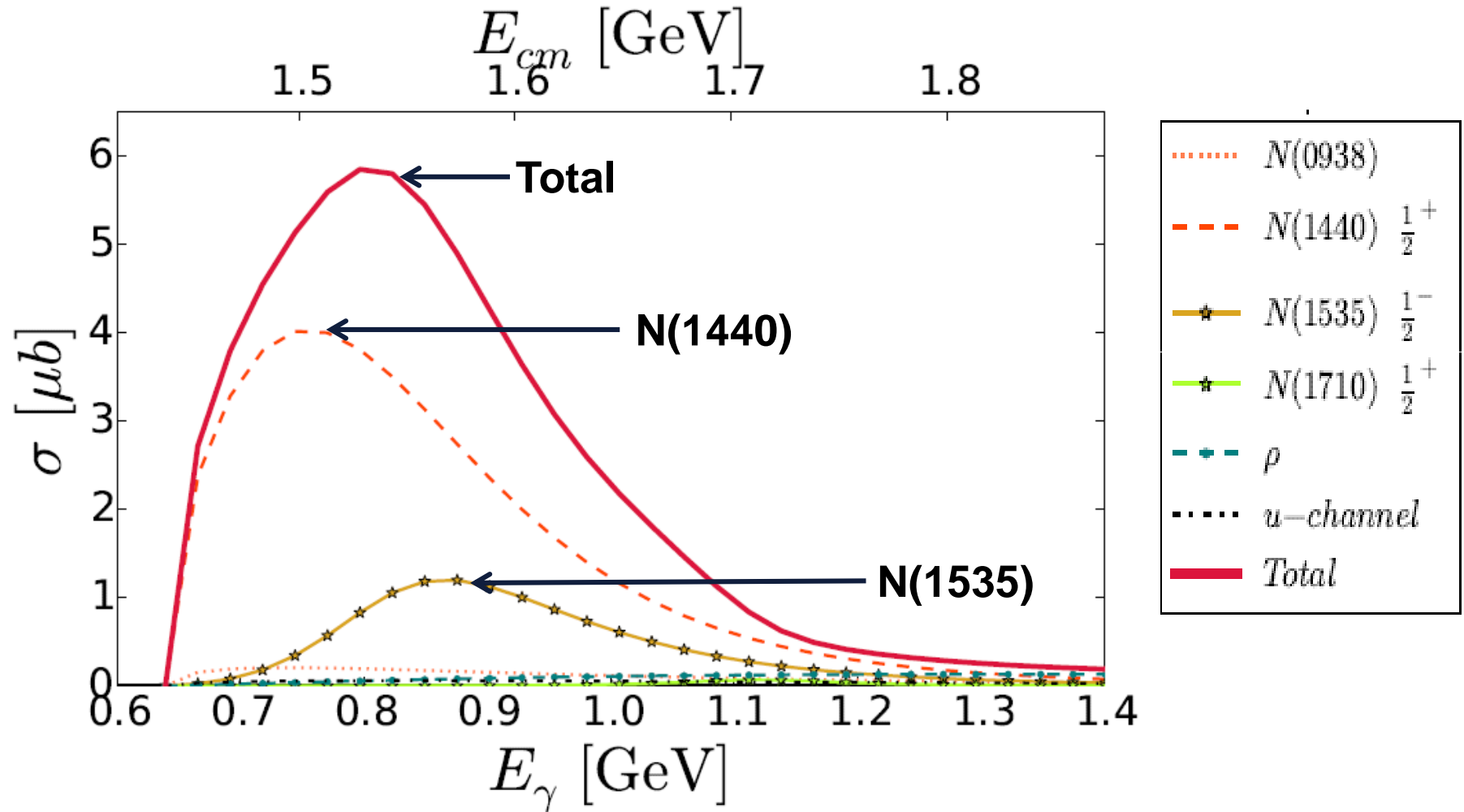
ρ -meson exchange is dominant !

Differential cross section of $f_0(500)$

$$E_\gamma = 2.0 \text{ GeV}$$



Total cross section of $f_0(500)$

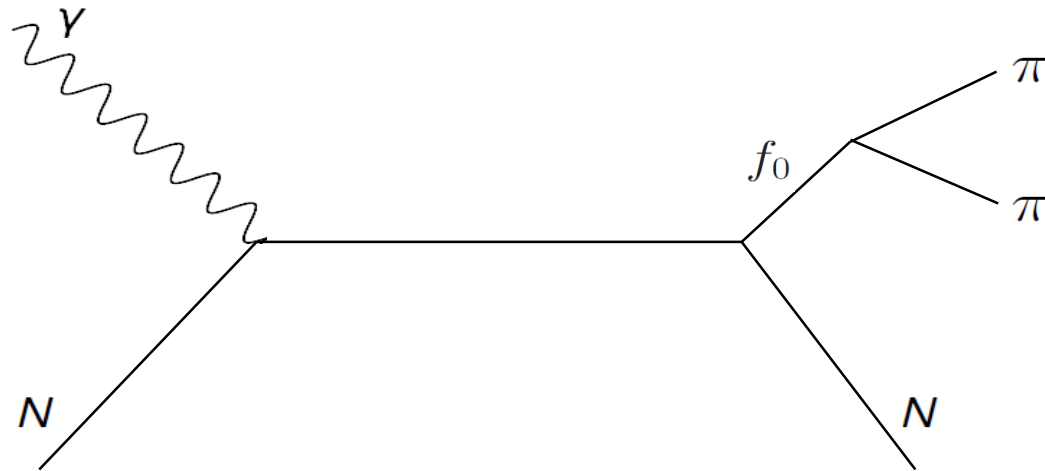


Summary

- We investigated the $f_0(980)N$ and $f_0(500)N$ photoproduction within the effective Lagrangian method.
- We took into account the contributions of nucleon resonances in $f_0(500)N$ photoproduction.
- Using the Regge approach, we consider the rho and nucleon exchange in the t - and u -channel, respectively.
- We calculated the differential cross section and the total cross section.

Outlook

- The $(\pi\pi)_{s\text{-wave}}^{I=0}$ photoproduction is under investigation with final-state interactions considered.

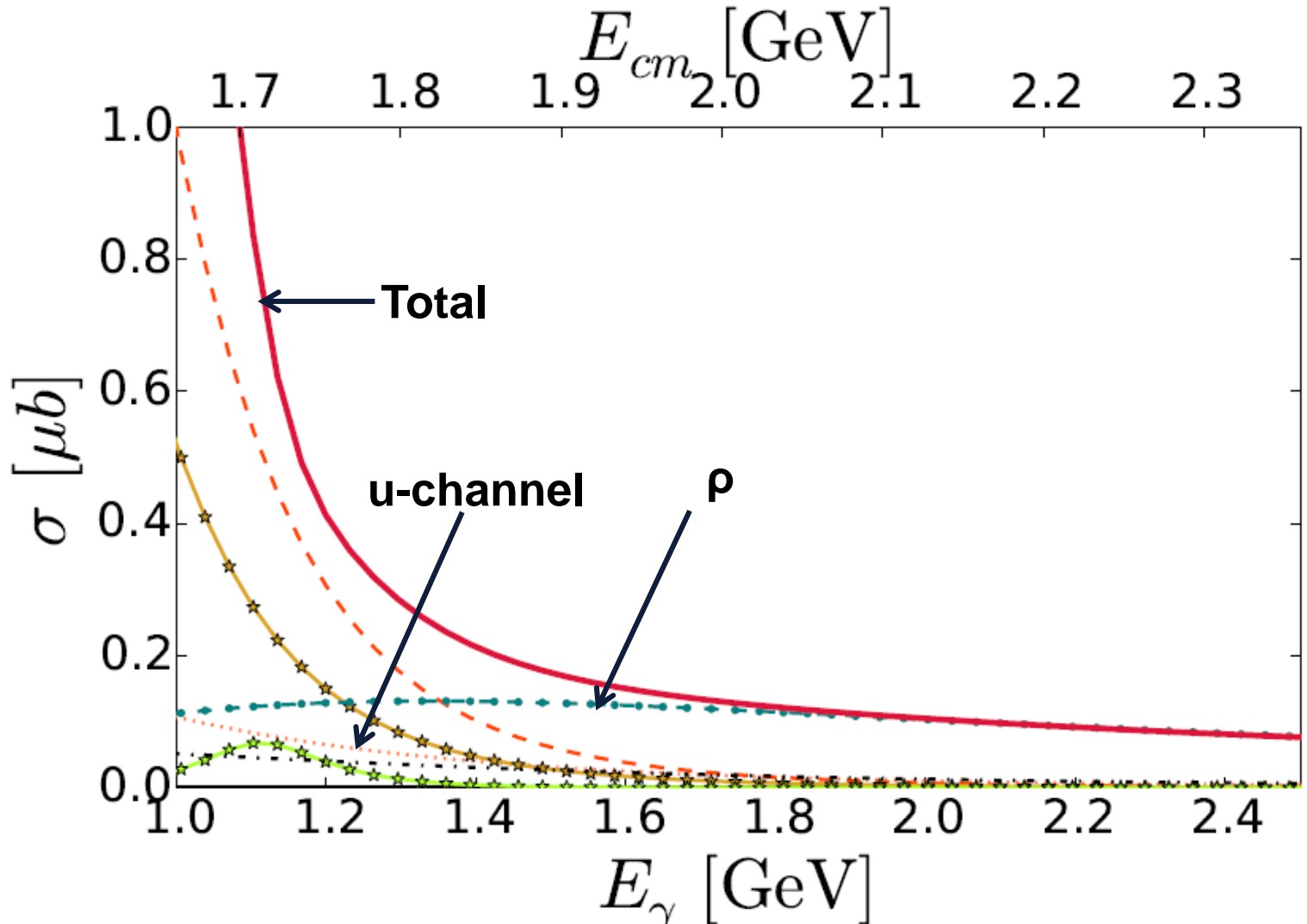




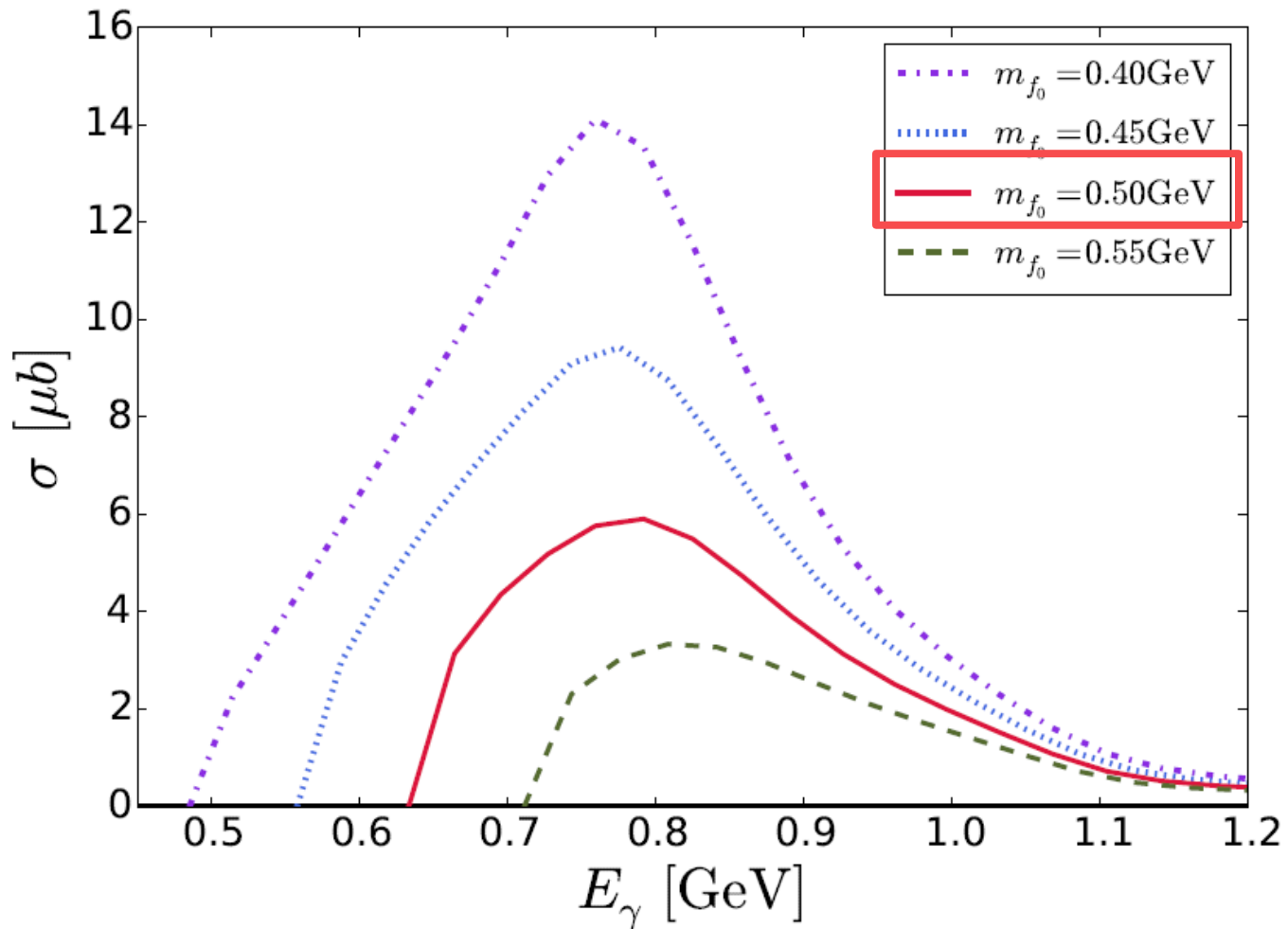
THANK YOU

Backup slides

$\gamma N \rightarrow f_0(500)N$: High energy



$\gamma N \rightarrow f_0(500)N$: Mass dependence



Resonances

Particle	spin ^{parity}	Mass [GeV]	Width [GeV]	Status	Decay mode $N(\pi\pi)_{s-wave}^{I=0}$ [%]
N(1440)	$\frac{1}{2}^+$	1.410-1.450	0.250-0.450	****	10~20
N(1535)	$\frac{1}{2}^-$	1.520-1.545	0.125-0.175	****	2 ± 1
N(1710)	$\frac{1}{2}^+$	1.680-1.740	0.050-0.250	***	10~40