

Mixing of pseudoscalar-baryon and vector-baryon in the $J^P = 1/2^-$ sector and the $N^*(1535)$ and $N^*(1650)$ resonances

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Section 1

Introduction

Approach to the nature of $N^*(1535)$ and $N^*(1650)$

- $N^*(1535)$ and $N^*(1650)$ are both well established 4-star resonances of the $J^P = 1/2^-$ sector.

¹N. Kaiser, P. B. Siegel and W. Weise, Phys. Lett. B **362**, 23 (1995)

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- The introduction of the chiral unitary techniques¹ lead to the dynamically generation of the $N^*(1535)$.
- However, in this case of the $N^*(1535)$, different cut offs or different subtraction constants² for different channels must be used.
- This was considered as a manifestation a nonnegligible component of a genuine state of $N^*(1535)$.

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Approach to the nature of $N^*(1535)$ and $N^*(1650)$

- In one work³ $N^*(1535)$ and $N^*(1650)$ are obtained with only pseudoscalar - baryon states using an offshell approach, which is in principle equivalent to having different subtraction constants in different channels.
- The $N^*(1650)$ is dynamically generated with the vector meson-baryon interaction, including the ρN channel.
- The mixture of the pseudoscalar-baryon and vector-baryon channels can remove the pathology observed by the need of different subtraction constants in different channels.

³J. Nieves and E. Ruiz Arriola, Phys. Rev. D **64**, 116008 (2001)

Section 2

Framework

Coupled channels with $J^P = 1/2^-$

The coupled channels of $N^*(1535)$ and $N^*(1650)$ used in this work are

$$\pi N, \eta N, K\Lambda, K\Sigma, \rho N \text{ and } \pi\Delta \text{ (d-wave).}$$

$PB \rightarrow PB$ transition mediated by a vector meson exchange⁴. The potential of this transition is given by

$$V_{ij} = -C_{ij} \frac{1}{4f^2} (k^0 + k'^0) \quad (1)$$

with the PB transition coefficients

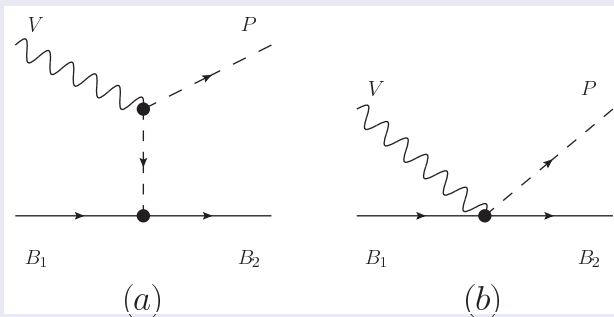
	πN	ηN	$k\Lambda$	$k\Sigma$
πN	2	0	$\frac{3}{2}$	$-\frac{1}{2}$
ηN		0	$-\frac{3}{2}$	$-\frac{3}{2}$
$K\Lambda$			0	0
$K\Sigma$				2

Table : Coefficients of PB transition with $I = 1/2$

⁴T. Inoue, E. Oset and M. J. Vicente Vacas, Phys.Rev.C**65**, 035204(2002)

Vertices of the transition diagrams

Vertices for the transition of $\rho N \rightarrow PB$ for (a) meson exchange and (b) the Kroll-Ruderman term



Vertices of the transition diagrams

Vertices for the transition of $\rho N \rightarrow PB$ with the Kroll-Ruderman term included

$$t_{\rho N(s) \rightarrow \pi N(s)} = -2\sqrt{6}g \frac{D+F}{2f} \left\{ \frac{\frac{2}{3}\vec{q}_{\pi N}^2}{(P_V + q_{\pi N})^2 - m_\pi^2} + 1 \right\} \quad (2)$$

$$t_{\rho N(s) \rightarrow \eta N(s)} = 0 \quad (3)$$

$$t_{\rho N(s) \rightarrow K\Lambda(s)} = -\frac{1}{2}\sqrt{6}g \frac{D+3F}{2f} \left\{ \frac{\frac{2}{3}\vec{q}_{K\Lambda}^2}{(P_V + q_{K\Lambda})^2 - m_K^2} + 1 \right\} \quad (4)$$

$$t_{\rho N(s) \rightarrow K\Sigma(s)} = -\frac{1}{2}\sqrt{6}g \frac{D-F}{2f} \left\{ \frac{\frac{2}{3}\vec{q}_{K\Sigma}^2}{(P_V + q_{K\Sigma})^2 - m_K^2} + 1 \right\} \quad (5)$$

The transition of $\rho N \rightarrow \pi\Delta(d)$ is introduced with

$$t_{\rho N(s) \rightarrow \pi\Delta(d)} = g \frac{2}{\sqrt{3}} \frac{f_{\pi N\Delta}}{m_\pi} \left\{ \frac{\frac{2}{3}\vec{q}^2}{(P_V + q)^2 - m_\pi^2} \right\} \quad (6)$$

The transitions involving d wave are introduced with a parameter⁵ γ for $\pi\Delta(d) \rightarrow \pi\Delta(d)$ and $\pi\Delta(d) \rightarrow \pi N(s)$.

$$t_{\pi\Delta(d) \rightarrow \pi\Delta(d)} = -\frac{\gamma_0}{m_\pi^5} q_{\pi\Delta}^4 \quad (7)$$

$$t_{\pi\Delta(d) \rightarrow \pi N(s)} = -\frac{\gamma_1}{m_\pi^3} q_{\pi\Delta}^2 \quad (8)$$

⁵As done in L. Roca, S. Sarkar, V. K. Magas, and E. Oset, Phys. Rev. C 73, 045208 (2006).

Section 3

Fitting the data

We fit eight parameters to the data⁶ of the πN scattering in S_{11} .

⁶R. A. Arndt, W. J. Briscoe, I. I. Strakovsky and R. L. Workman, Phys. Rev. C **74**, 045205 (2006)

We fit eight parameters to the data⁶ of the πN scattering in S_{11} .

- Six subtraction constants of the G function, one for each channel ($\pi N(s)$, $\eta N(s)$, $K\Lambda(s)$, $K\Sigma(s)$, $\rho N(s)$, $\pi\Delta(d)$).
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μ [MeV]	$a_{N\pi}$	$a_{N\eta}$	$a_{\Lambda K}$	$a_{\Sigma K}$	$a_{N\rho}$	$a_{\Delta\pi}$	γ_0	γ_1
M_B	-1.203	-2.208	-1.985	-0.528	-0.493	-1.379	0.595	1.47
630	-2.001	-3.006	-3.128	-1.799	-1.291	-2.720	0.595	1.47

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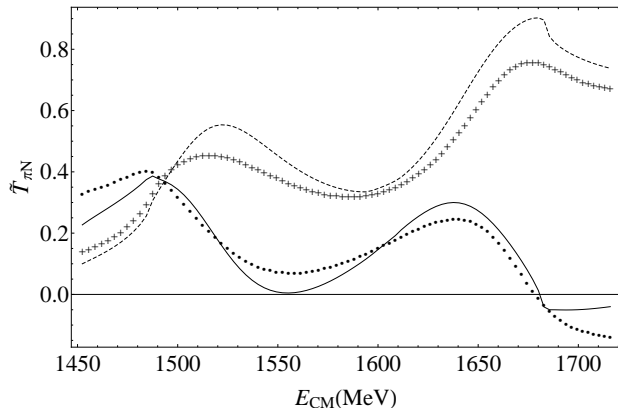
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- Where now, all the subtraction constants are of the natural size.

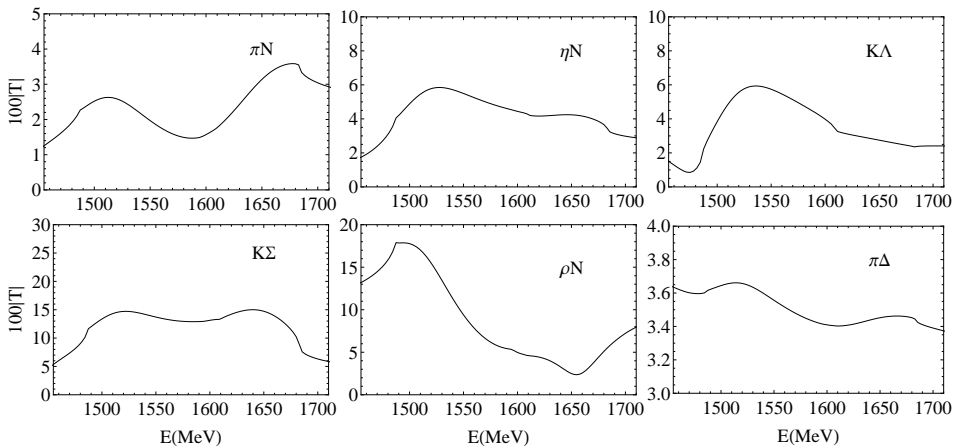
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Fitting the data



We show the real part (circles) and imaginary part (cross) of the data and the result of our fit of $\tilde{T}_{\pi N}$ for real (solid) and imaginary (dashed) parts.

Results of the $|T|^2$ matrix for the diagonal channels



Branching ratios for the $N^*(1535) J^P = 1/2^-$

$N^*(1535) J^P = 1/2^-$						
	Theory	PDG	Cutkosky ⁷	Anisovich ⁸	Vrana ⁹	Thoma ¹⁰
Re	1508.1	1490 – 1530	1510 ± 50	1501 ± 4	1525	$1508 \begin{smallmatrix} + \\ - \end{smallmatrix} \begin{smallmatrix} 10 \\ 30 \end{smallmatrix}$
2Im	90.3	90 – 250	260 ± 80	134 ± 11	102	165 ± 15
Channel	Branching Ratio [$\Gamma_i/\Gamma(\%)$]					
$N\pi$	58.6	35 – 55	50 ± 10	54 ± 5	35 ± 8	37 ± 9
$N\eta$	37.0	42 ± 10		33 ± 5	51 ± 5	40 ± 10
ΛK	0.0	-				
ΣK	0.0	-				
$N\rho$	1.0	2 ± 1			2 ± 1	
$\Delta\pi$	3.3	0 – 4		2.5 ± 1.5	1 ± 1	23 ± 8

⁷R. E. Cutkosky *et al.*, Phys. Rev. D **20**, 2839 (1979).

⁸A. V. Anisovich *et al.*, Eur. Phys. J. A **48**, 15 (2012)

⁹T. P. Vrana *et al.*, Phys. Rept. **328**, 181 (2000)

¹⁰U. Thoma *et al.*, Phys. Lett. B **659**, 87 (2008)

Branching ratios for the $N^*(1650) J^P = 1/2^-$

$N^*(1650) J^P = 1/2^-$						
	Theory	PDG	Cutkosky ¹¹	Anisovich ¹²	Vrana ¹³	Thoma ¹⁴
Re	1672.3	1640 – 1670	1640 ± 20	1647 ± 6	1663	1645 ± 15
2Im	158.2	100 – 170	150 ± 30	103 ± 8	240	187 ± 20
Channel	Branching Ratio [$\Gamma_i/\Gamma(\%)$]					
$N\pi$	58.9	50 – 90	65 ± 10	51 ± 4	74 ± 2	70 ± 15
$N\eta$	27.6	5 – 15		18 ± 4	6 ± 1	15 ± 6
ΛK	5.7	-		10 ± 5		
ΣK	0.0	-				
$N\rho$	5.6	1 ± 1			1 ± 1	
$\Delta\pi$	2.2	0 – 25		19 ± 9	2 ± 1	10 ± 5

¹¹R. E. Cutkosky *et al.*, Phys. Rev. D **20**, 2839 (1979).

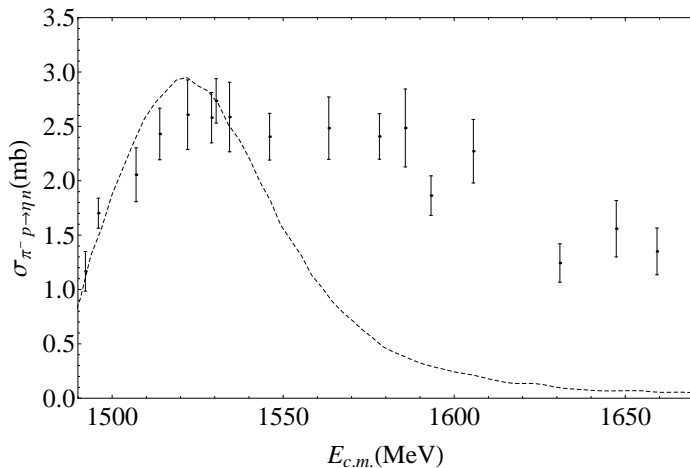
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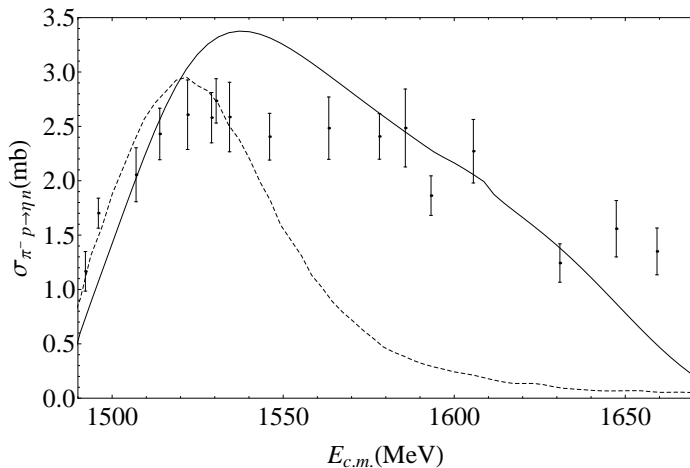
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- The important component of a genuine state in the wave function of the $N^*(1535)$ claimed in other works, can be translated now by stating that the missing components can be filled up by the ρN and $\pi\Delta$ channels.