

# 原子核の励起状態の研究から考える 今後理解したいこと

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関西核多体セミナー, 2023年8月4日, 阪大中之島センター

slide: <https://www.rcnp.osaka-u.ac.jp/~tamii> → 頁の下の方

# Outline

## Methods

spin-M1 excitation

E1 excitation

decay-coincidence

quasi-free at 0deg

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## Physics

photo-nuclear reactions

*E1* polarizability  
spin susceptibility

decay  
damping  
width  
viscosity

EoS

*n*-skin

PDR  
*E1* toroidal

*d*-like correlation  
*np*-pairing

level density  
characteristic scale

an image of

Nuclear ground states

=

mean-field like component (low-momentum)

← single particle orbit  
occupation

⊕

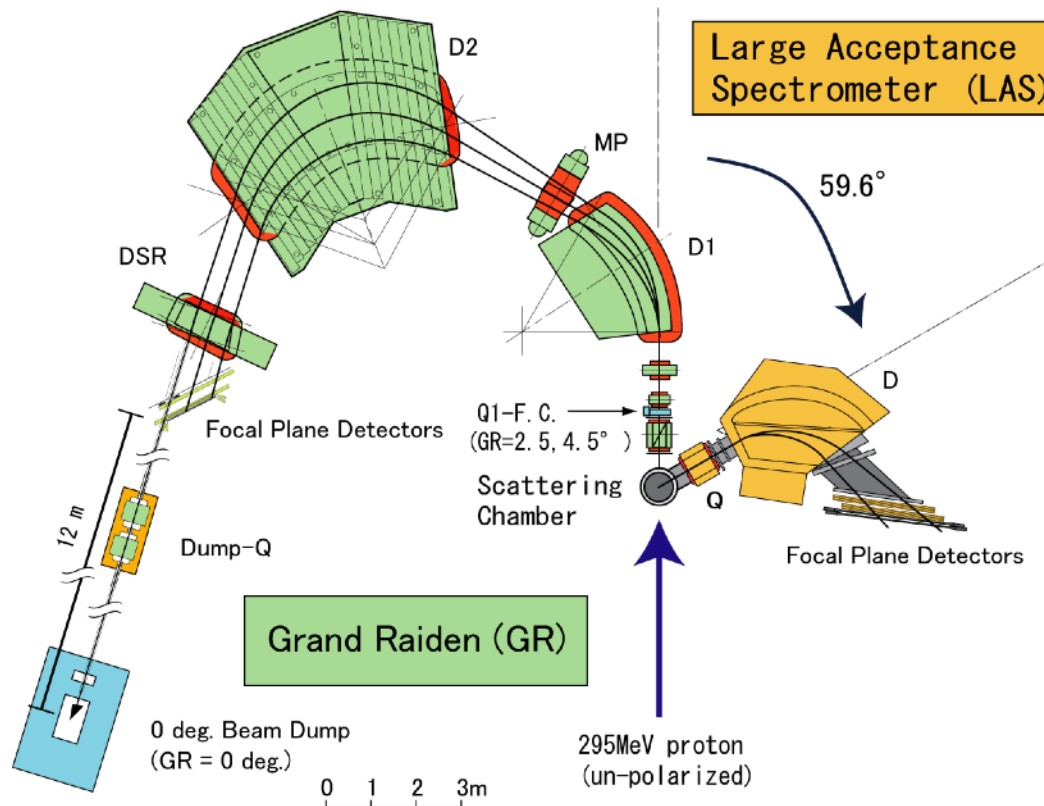
d-like correlation (inc. high-momentum)

←  $\alpha$ -cluster も含まれる

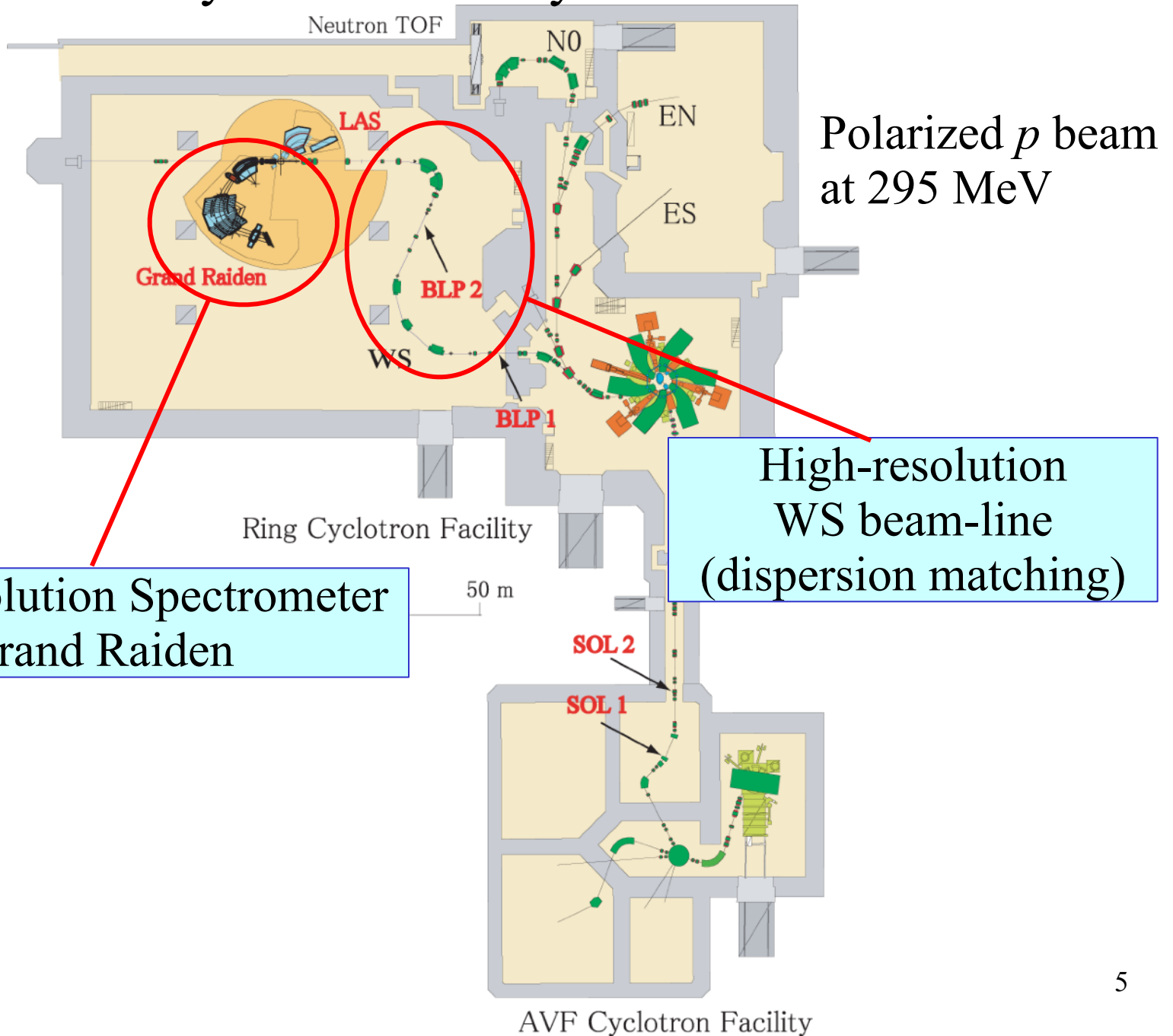
?

d-like correlation の定量的記述

# Experimental Methods Briefly

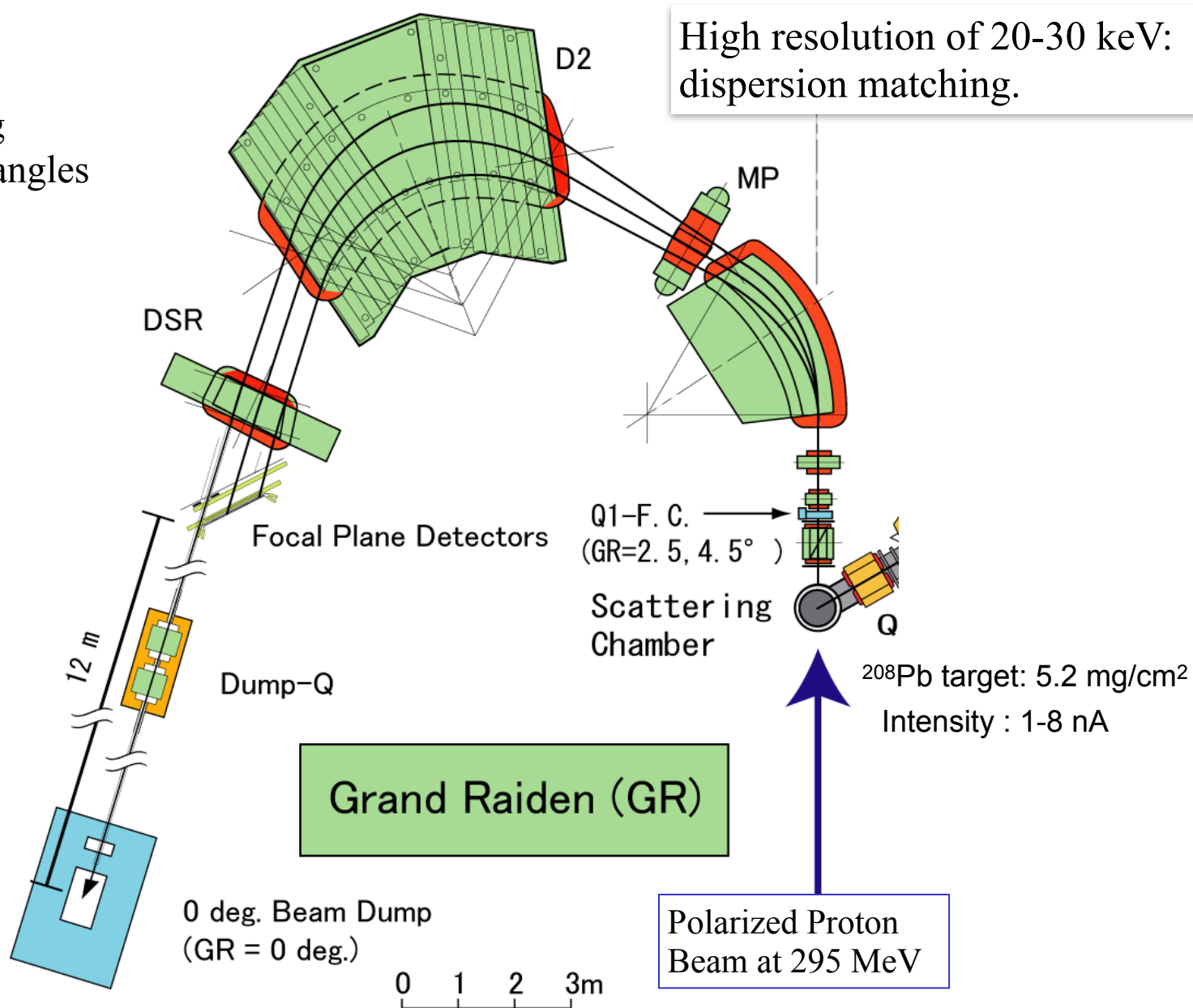


# Cyclotron Facility at RCNP



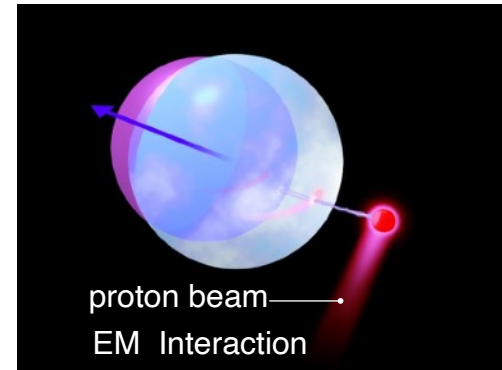
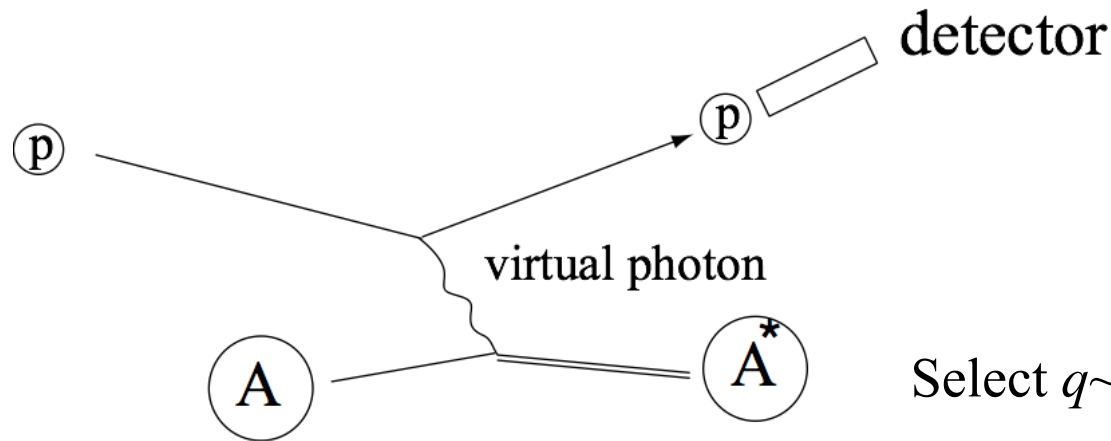
# High-Resolution Spectrometer "Grand Raiden"

Proton scattering  
at very forward angles



# Probing the E1 Response by Proton Scattering

## Missing Mass Spectroscopy by Virtual Photon Excitation



Select  $q \sim 0$  ( $\sim 0$  deg.)

- **Missing mass spectroscopy:**

Total strength is measured independently from the decaying channels.

- **Multipole decomposition** of the strength in the continuum:

Includes the contribution of unresolved small states

- **Coulomb excitation:** EM Interaction

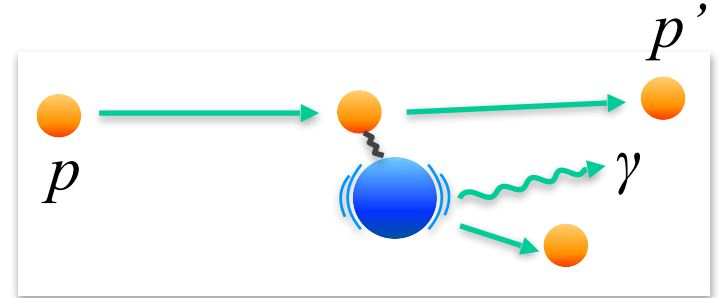
Absolute determination of the transition strength.

# Probes for the Electric Dipole Response of Nuclei

## 1. Virtual photon excitation

(Coulomb excitation)

- proton inelastic scattering at 0 deg.

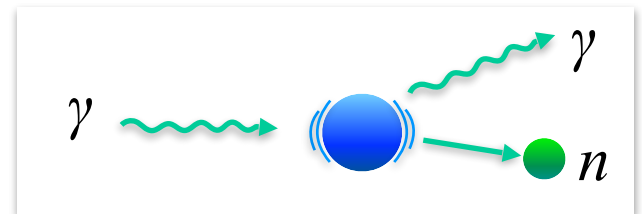


Proton beams at RCNP  
and iThemba LABS

$E_x$  distribution in one shot measurement  
total photo-absorption c.s.  
up to 32 (24) MeV at RCNP (iThemba)

## 2. Real photon absorption

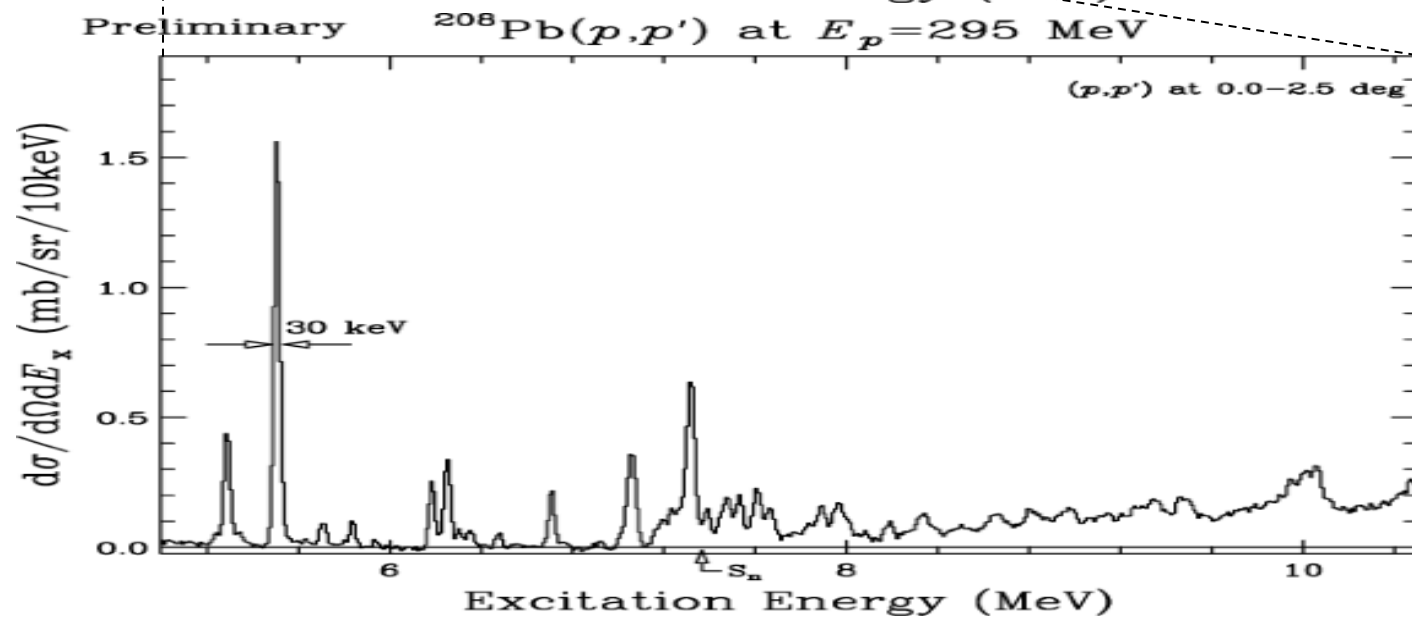
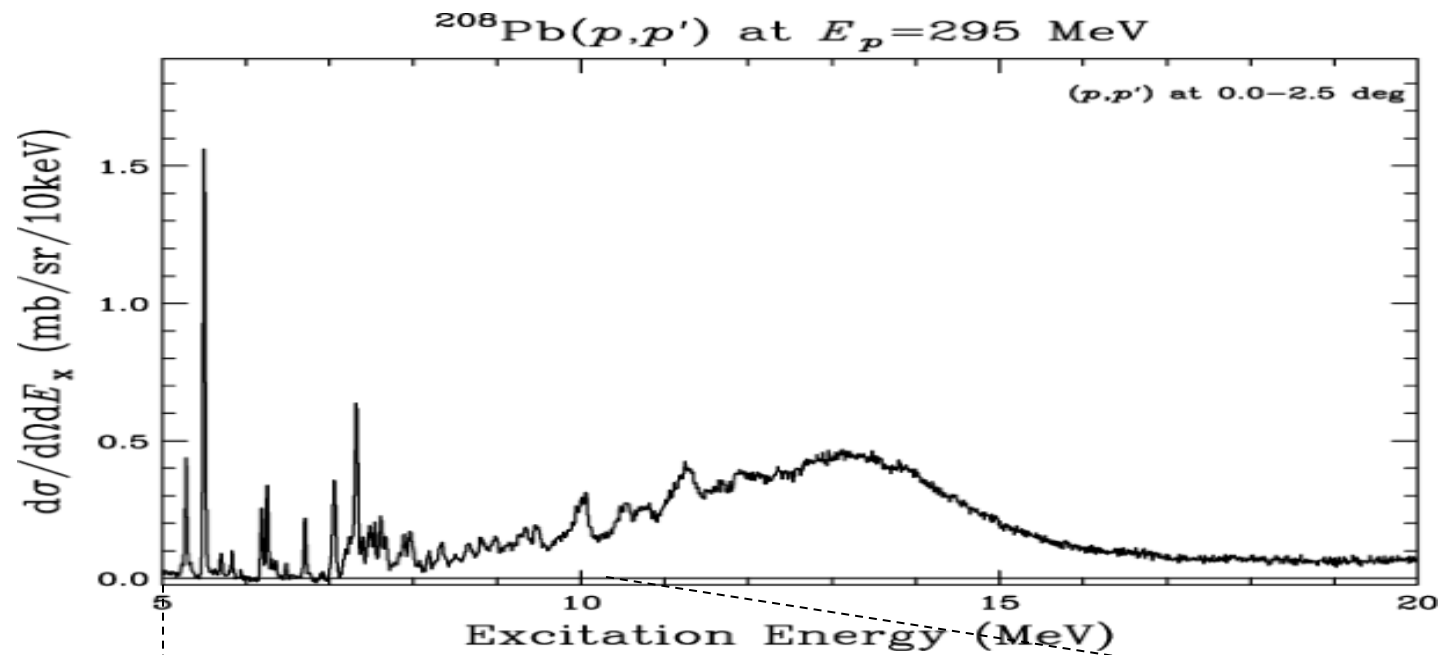
- $(\gamma, \gamma')$  Nuclear Resonance Fluorescence
- $(\gamma, n)$ ,  $(\gamma, 2n)$ ,  $(\gamma, p)$ , ... photodisintegrations



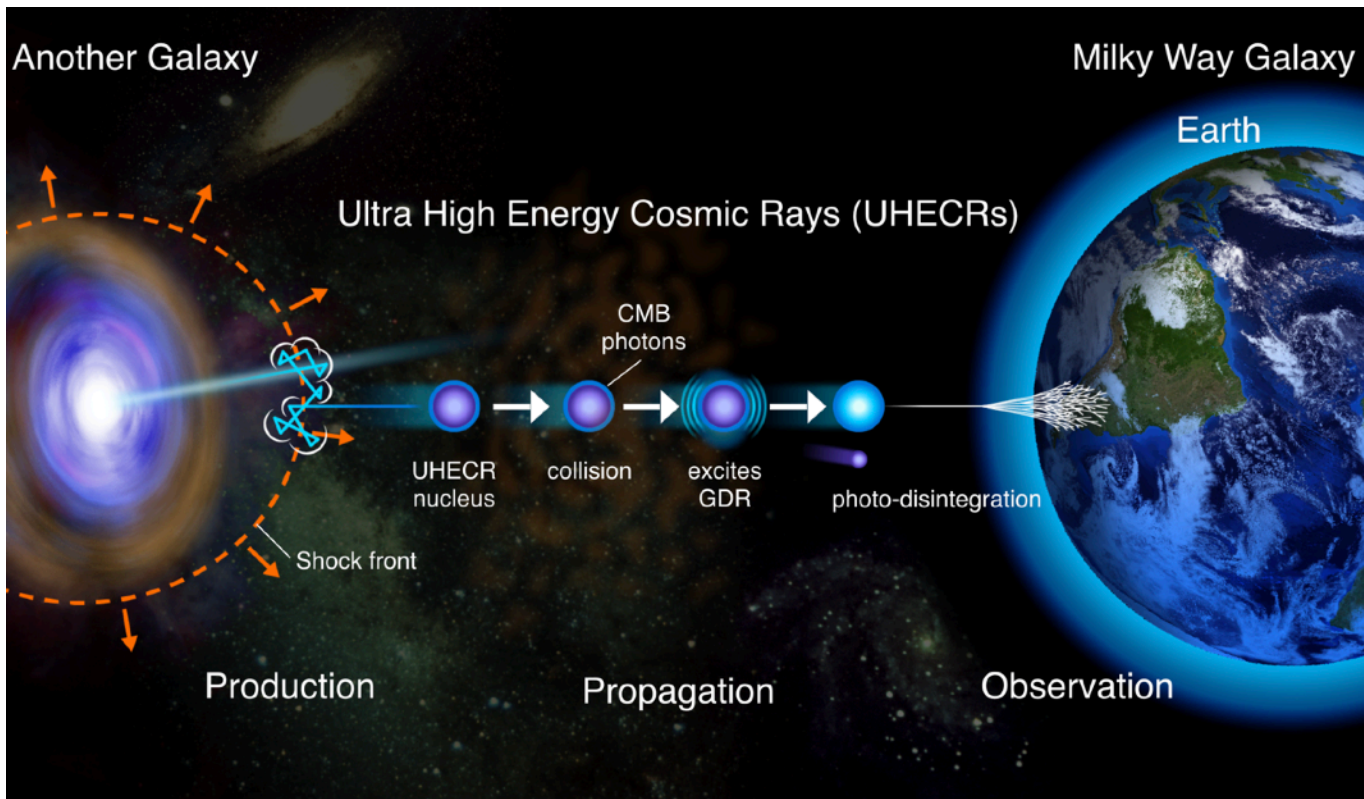
Real  $\gamma$ -beam at ELI-NP

pure EM probe  
precise absolute c.s.  
partial strength including  $n$   
up to 20 MeV at ELI-NP





# Photo-Nuclear Reaction

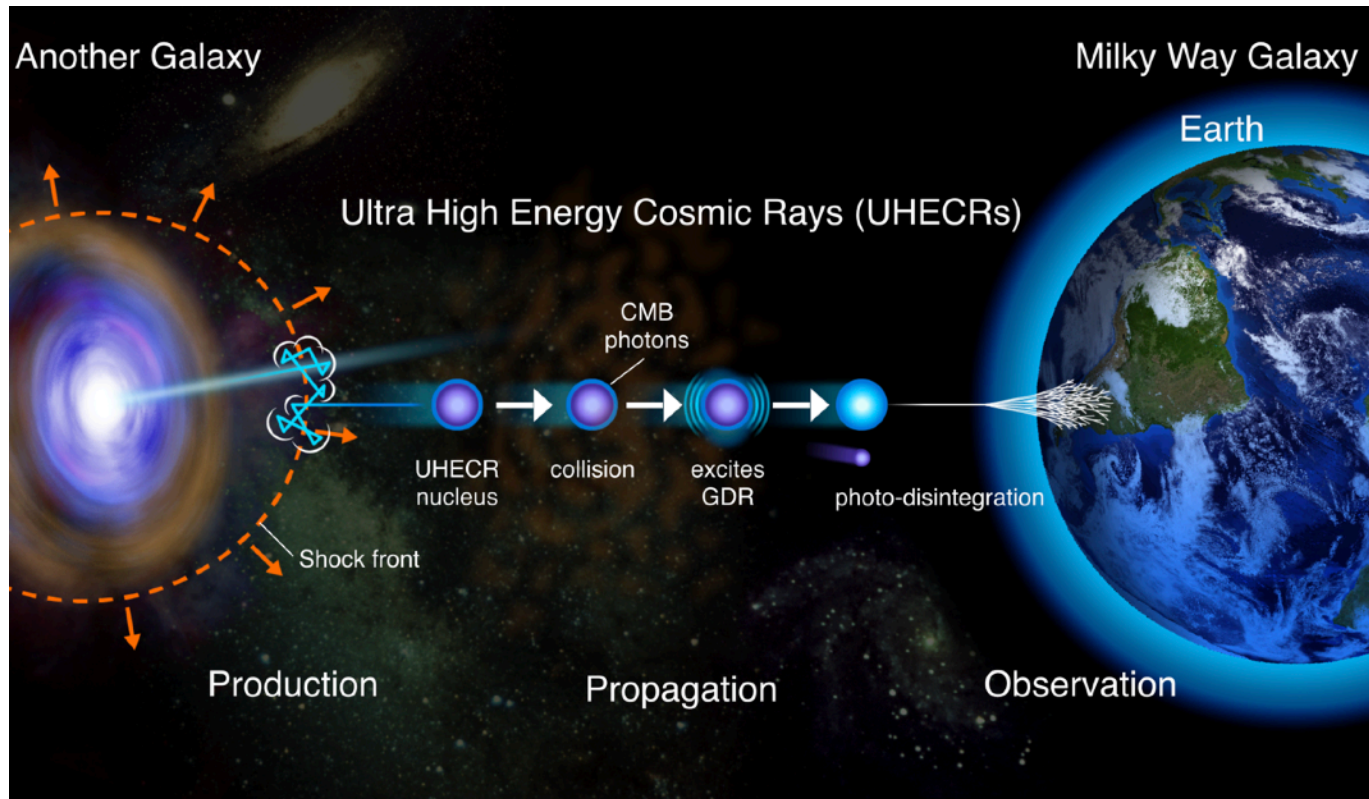


# PANDORA Project

## Photo-Absorption of Nuclei and Decay Observation for Reactions in Astrophysics

Systematic Measurement on E1 Strength Distribution and n,p, $\alpha$ , $\gamma$  decays up to A=60

inter-galactic propagation of UHECRs



# PANDORA Project

Photo-Absorption of Nuclei and Decay Observation for Reactions in Astrophysics

Systematic Measurement on E1 Strength Distribution and n,p, $\alpha$ , $\gamma$  decays up to A=60

Understanding of photo-nuclear reactions for light nuclei

- photo-absorption c.s.  $\simeq$  B(E1) distribution
- decay process

軽核の光核反応を精度よく記述したい

崩壊計算も重要

E1遷移

統計崩壊計算では不十分

# 軽い核の光核反応の記述の重要性

宇宙核物理・素粒子物理:

元素合成

超高エネルギー宇宙線のエネルギー損失過程

中性カレントニュートリノ検出: 巨大共鳴の $\gamma$ 放出、 $(n,\gamma)$ 反応

放射線遮蔽、放射線施設のdecommissioning、原子炉内の核反応

光放射化分析、非破壊検査

$\gamma$ -イメージング、CT診断、生体物質の放射線への影響

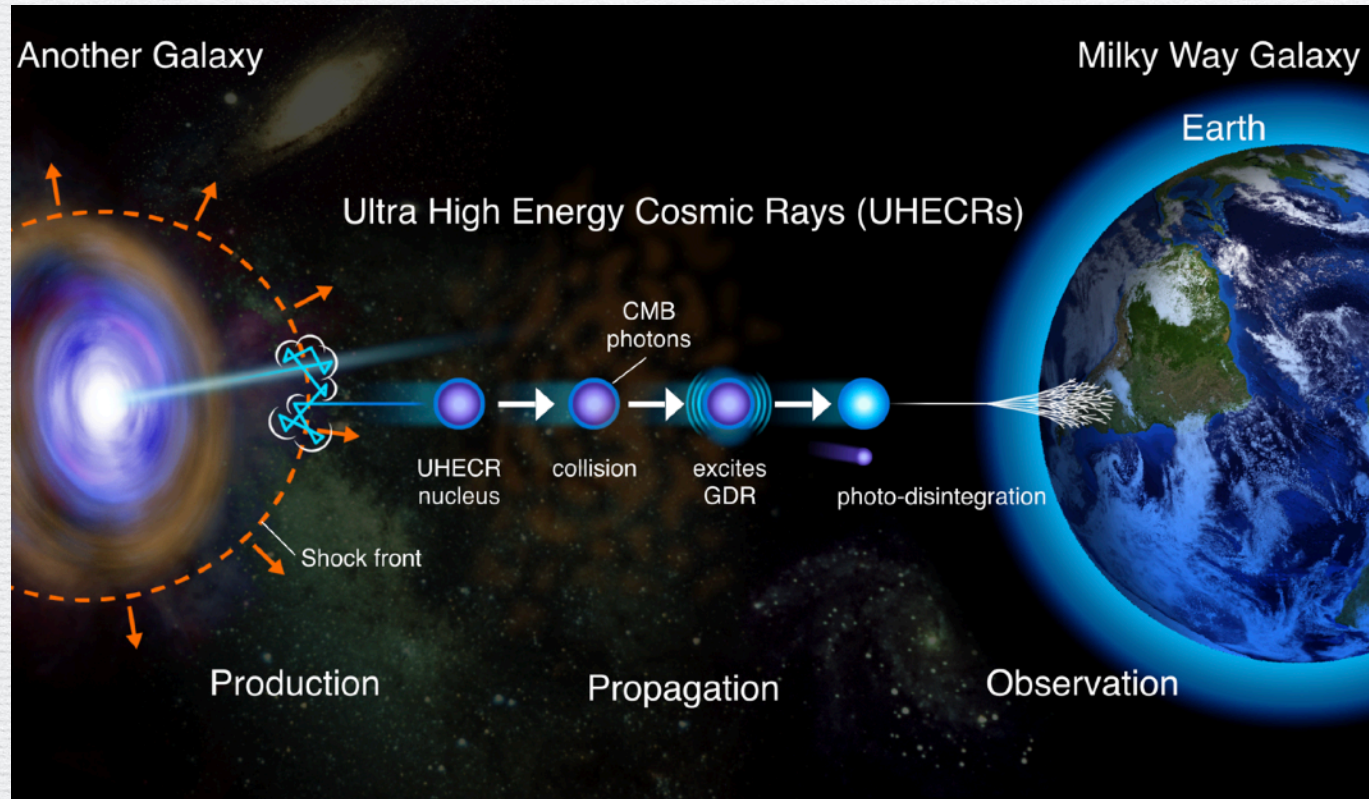
Home-Land Security、核分裂物質・爆発性物質の探査

光照射による医療用RI製造

雷雲内の核反応、ガンマ放射

宇宙の元素の99.99999%は  
A=60以下の原子核から成る

# Extragalactic Propagation of UHECR Nuclei



Cosmic Microwave Background (CMB)

WMAP  
 $T=2.73\text{ K}$

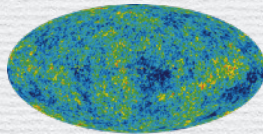
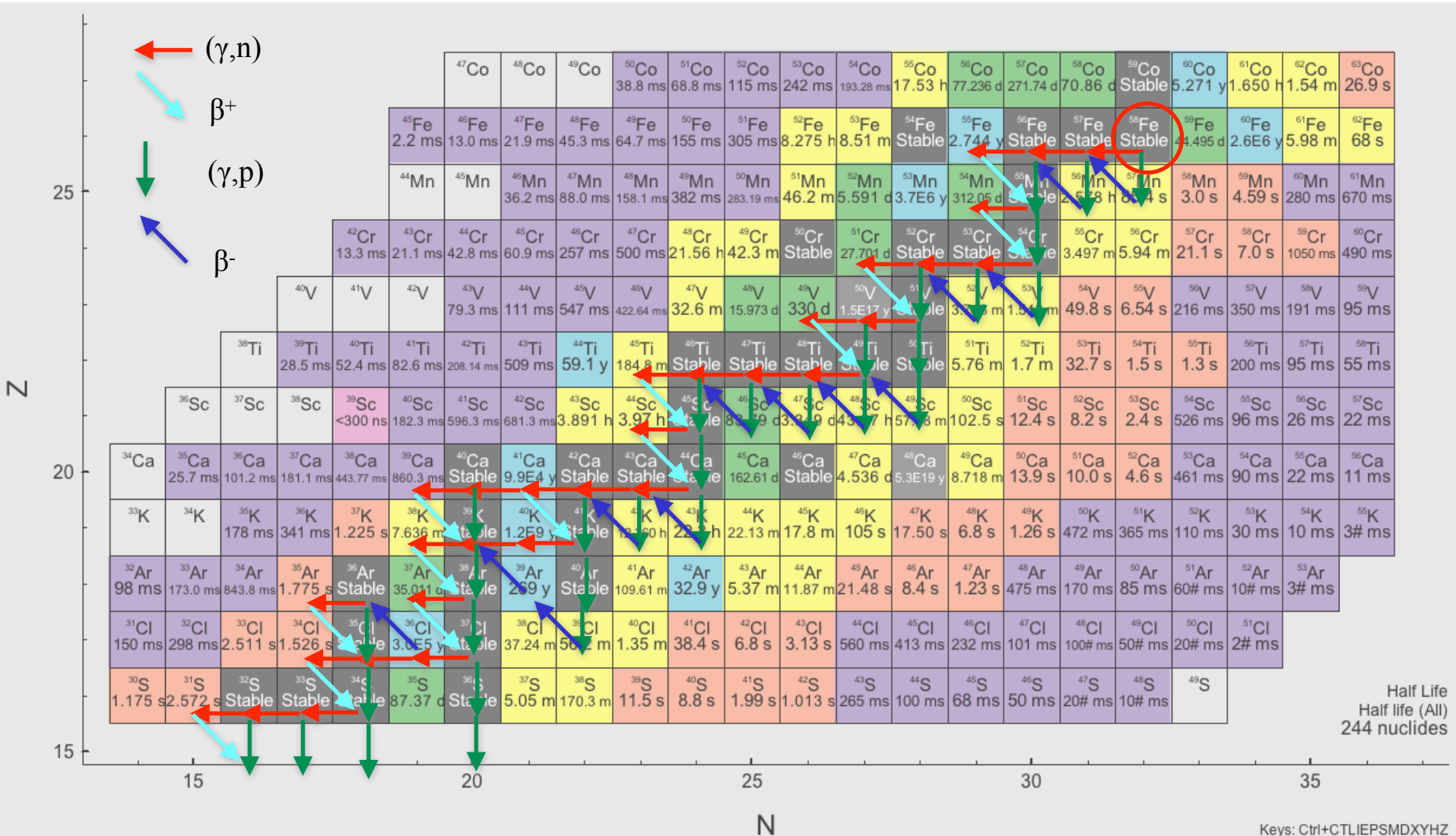


Photo-nuclear reactions determine the maximum travel distance of UHECRs nuclei and their composition/energy modification in extra-galactic propagation.



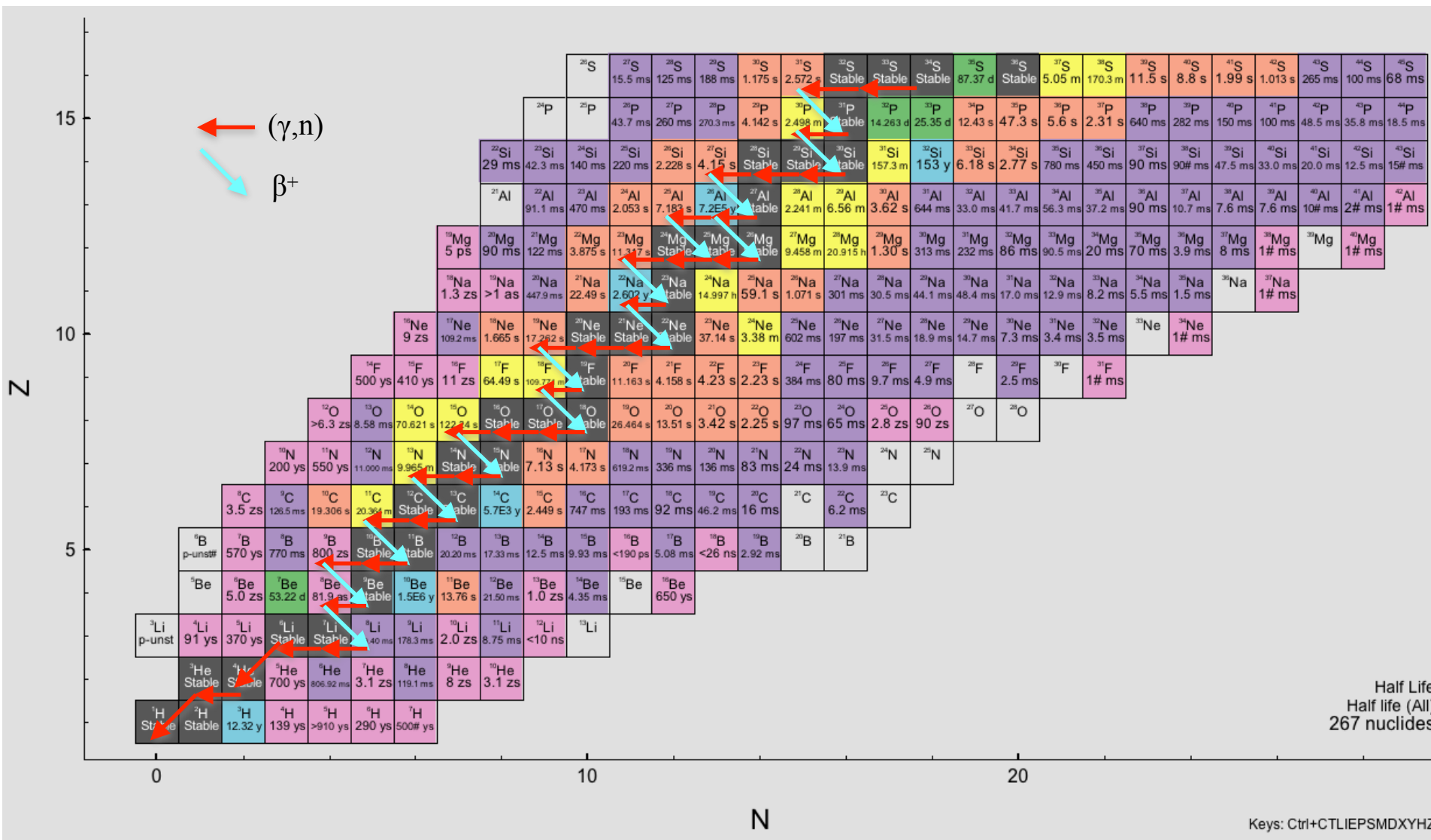
GZK cut-off

# Photo-disintegration Pass of $^{56}\text{Fe}$



$(\gamma, xn)$ ,  $(\gamma, \alpha)$  reactions also take place.  
 Several unstable nuclei also contribute.

# Photo-disintegration Pass of $^{56}\text{Fe}$





# PANDORA Project: Collaborator

## Nuclear Experiments

*Osaka Univ.*

RCNP

**A. Tamii, N. Kobayashi**, T. Sudo, M. Murata, A. Inoue, **R. Niina**, T. Kawabata, T. Furuno, S. Adachi, K. Sakanashi, K. Inaba, Y. Fujikawa, S. Okamoto

ELI-NP

*ELI-NP*

**P.-A. Söderström**, D. Balabanski, L. Capponi, A. Dhal, T. Petruse, D. Nichita, Y. Xu

iThemba LABS

*iThemba LABS, Univ. Witwatersland, Stellenbosh Univ.*

**L. Pellegri**, R. Neveling, F.D. Smit, **J.A.C. Bekker**, S. Binda, H. Jivan, T. Khumal, M. Wiedeking, P. Adsley, L.M. Donaldson, E. Sideras-Haddado, K.L. Malatji, S. Jongile, A. Netshiya

TU-Darmstadt

P. von Neumann-Cosel, N. Pietralla, J. Isaak, J. Kleemann, M. Spall

U. Milano/INFN

A. Bracco, F. Camera, F. Crespi, O. Wieland

Shanghai

H. Utsunomiya

U. Oslo

K.C.W. Li, S. Siem, ...

## Nuclear Theory

AMD

**M. Kimura, Y. Taniguchi**, H. Motoki

Large Scale  
Shell Modle

NRFT

**E. Litvinova**, P. Ring, H. Wibowo

Y. Utsuno, N. Shimizu

RPA/DFT

RPA by **T. Inakura**, QPM by **N. Tsoneva**

TALYS

**S. Goriely, E. Khan**

## UHECR Theory

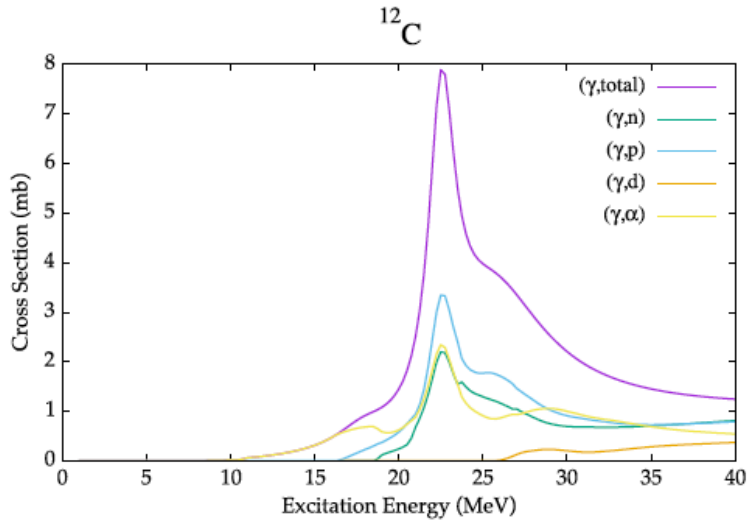
Propagation  
and production

**D. Allard**, B. Baret, I. Deloncle, J. Kiener, E. Parizot, V. Tatischeff

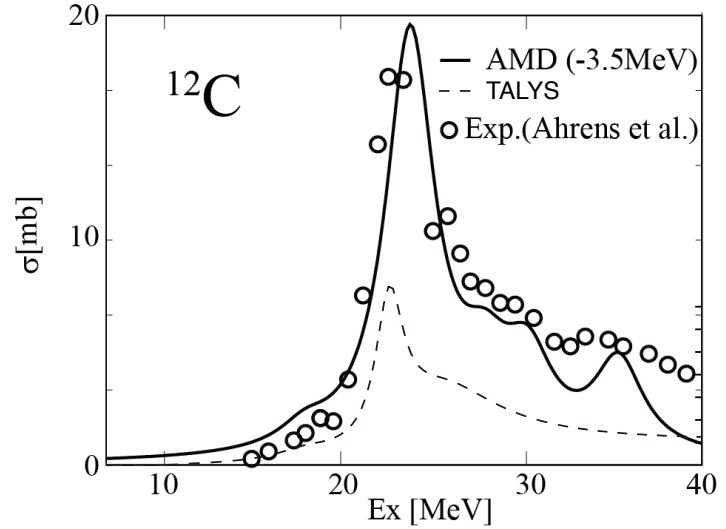
**S. Nagataki, E. Kido**, J. Oliver, H. Haoning

# Predictions

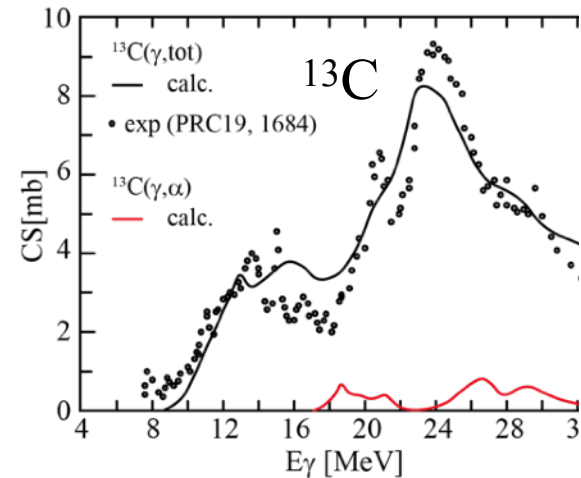
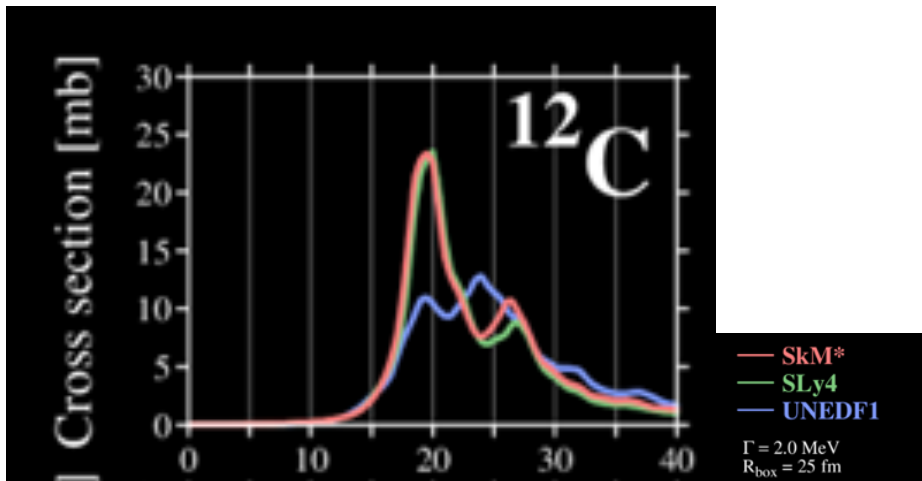
TALYS



AMD + Laplace Expansion (M. Kimura et al.,)

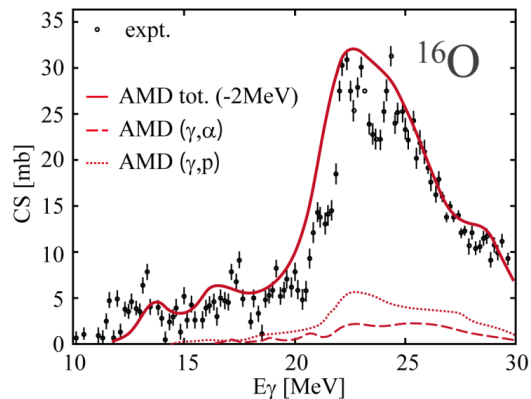
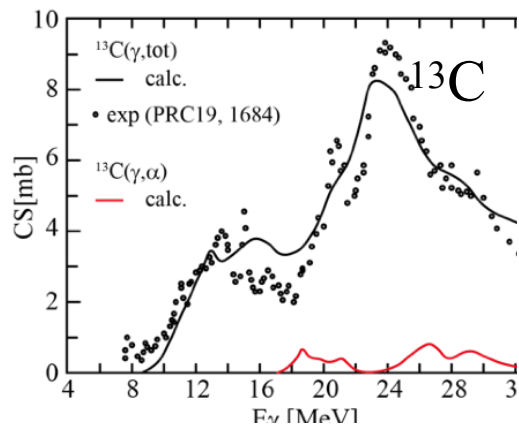


RPA (T. Inakura)



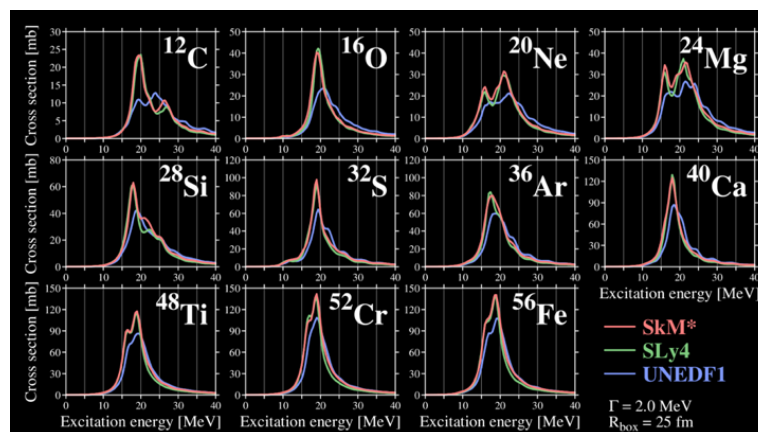
# Theoretical Model Developments

AMD + Laplace Expansion (M. Kimura et al.,)

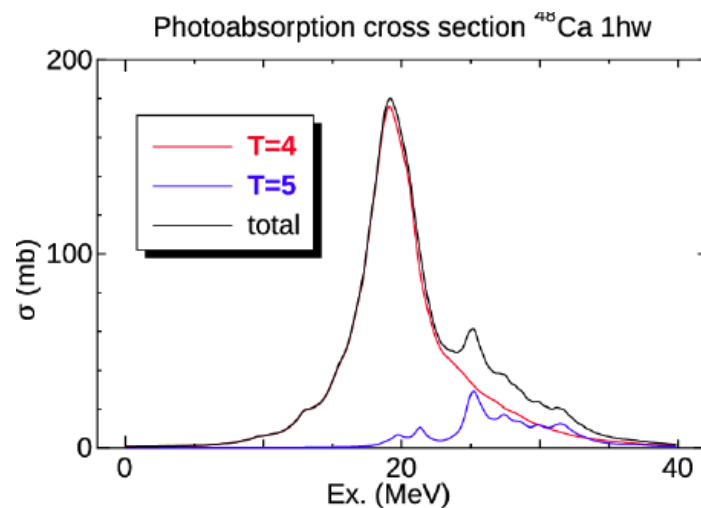


Isospin selection rule

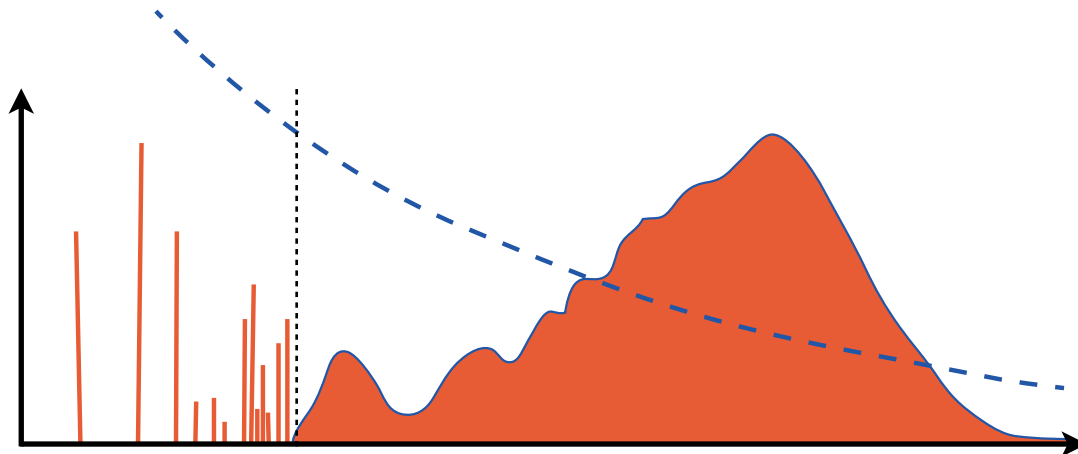
RPA by T. Inakura



N. Shimizu, Y. Utsuno, et al.,



# E1 Polarizability



# Static Electric Dipole Polarizability ( $\alpha_D$ )

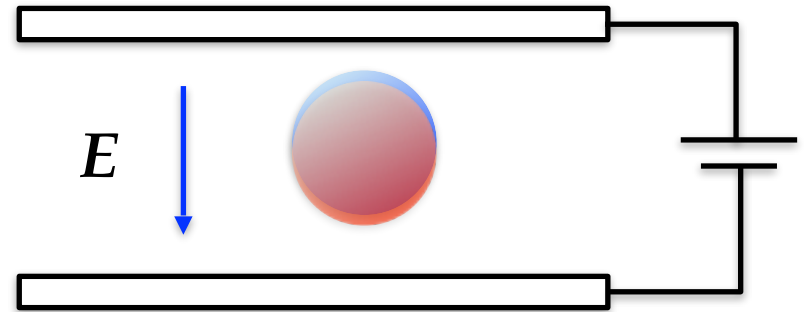
Electric dipole moment

$$p = \alpha_D \times E$$

$\alpha_D$ : electric dipole polarizability



The **restoring force** originates from the **symmetry energy**.

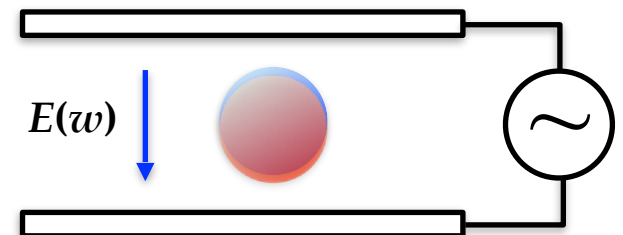


nucleus

in a static electric field  
with fixing the c.m. position

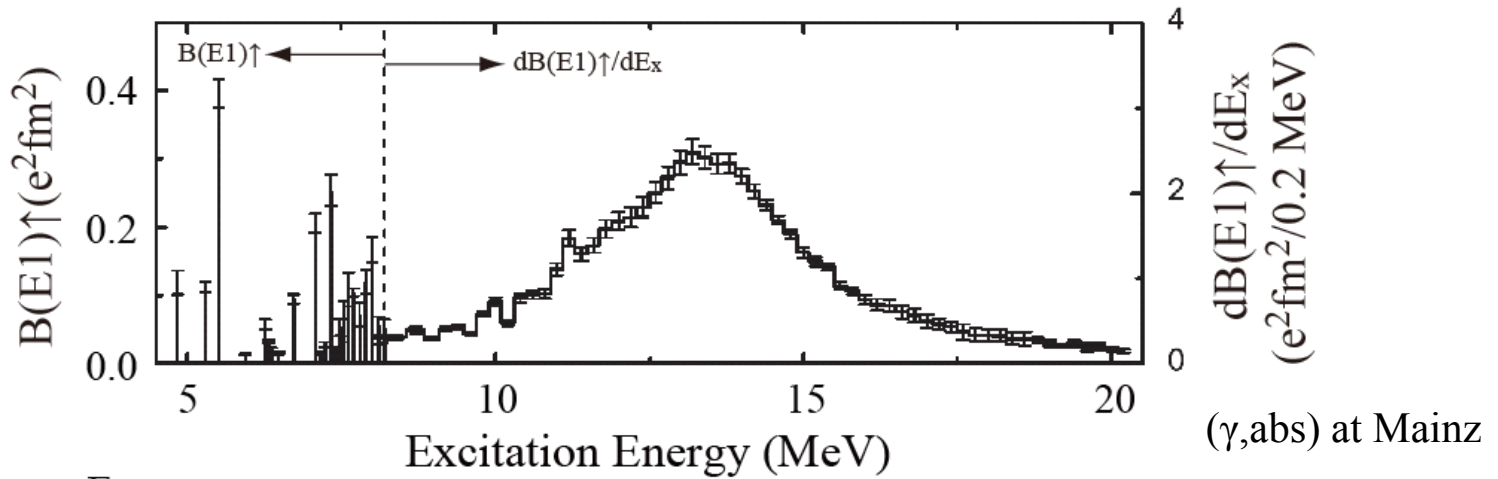
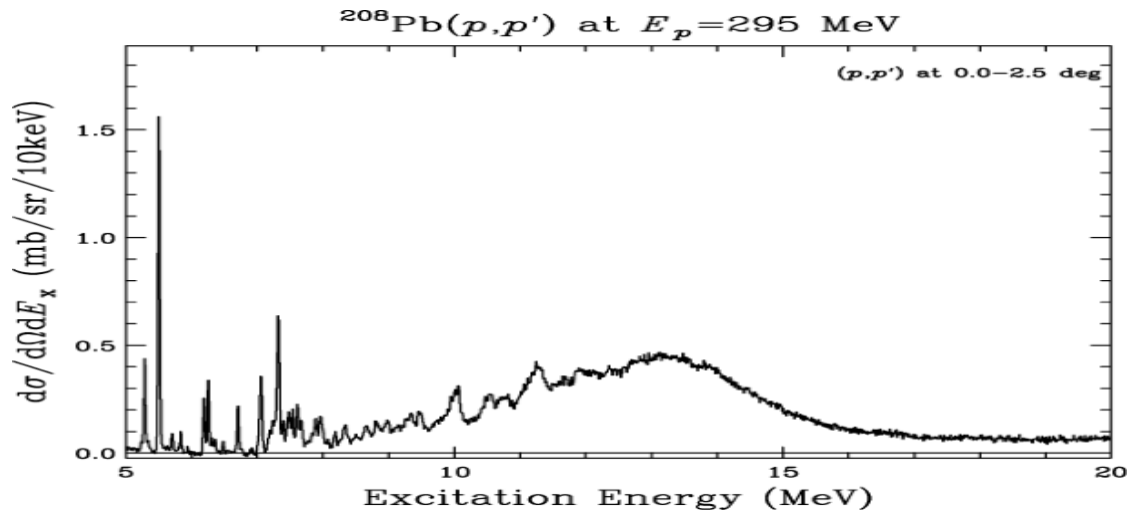
Inversely energy-weighted sum-rule of B(E1)

$$\alpha_D = \frac{8\pi e^2}{9} \int \frac{dB(E1)}{E_x}$$



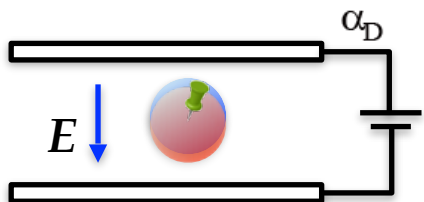
first order perturbation calc. A.B. Migdal: 1944  
dielectric theorem

# Electric Dipole Polarizability: $^{208}\text{Pb}$ , $^{120}\text{Sn}$



$E_x$  0                      10                      20                      130 MeV

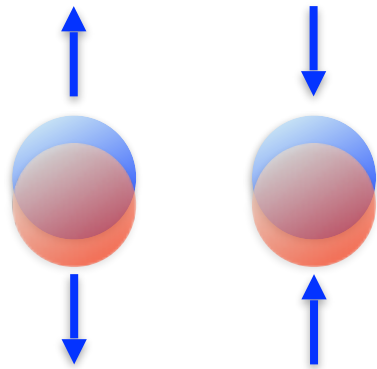
$\alpha_D$                       2.7                      16.2                      1.2  $\text{fm}^3$   
total  $20.1 \pm 0.6 \text{ fm}^3$



# Symmetry Energy (J and L parameters)

## Keys to Understand the Neutron Matter Equation of State (EOS)

Electric Force      Symmetry Energy

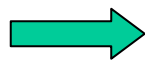


$\alpha_D$  is determined by the balance between the two.

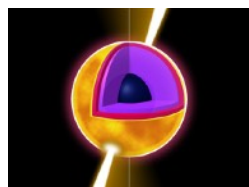
Nucleus



$Z \approx N$

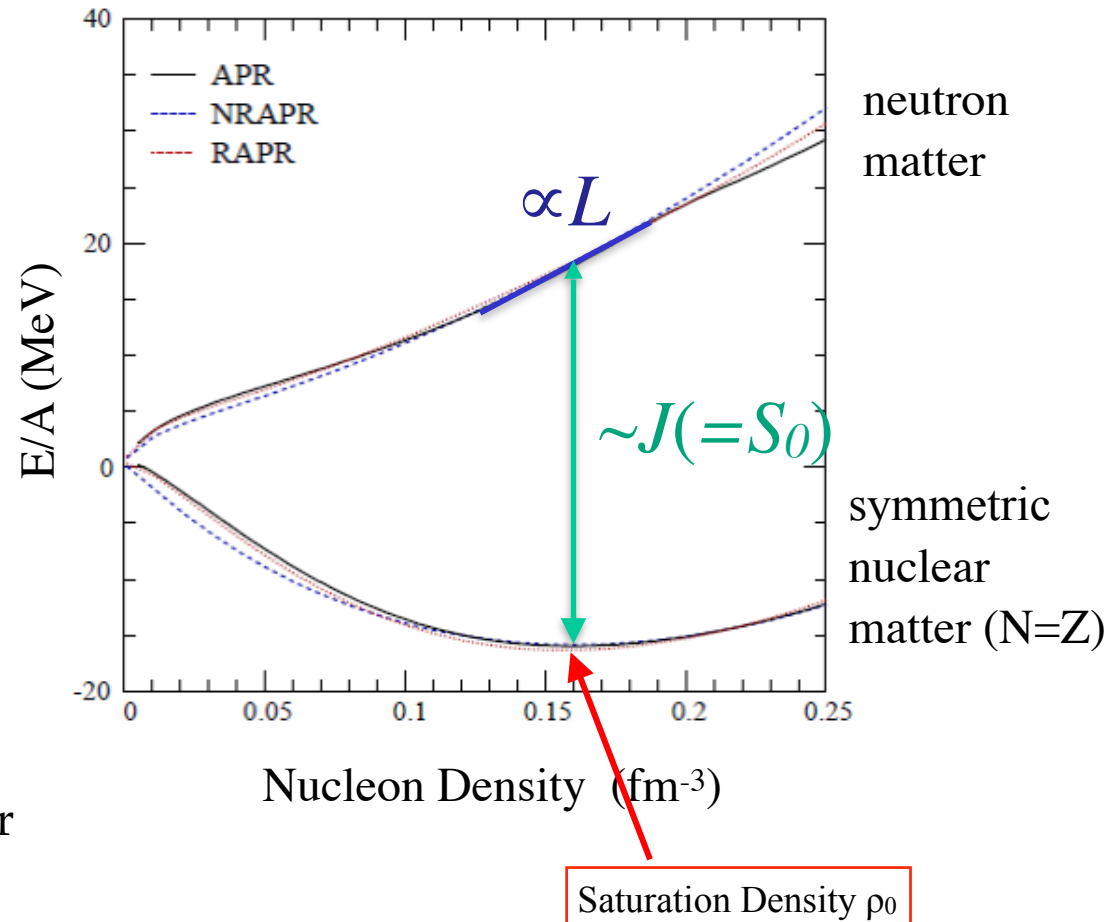


Neutron Star



$Z \ll N$

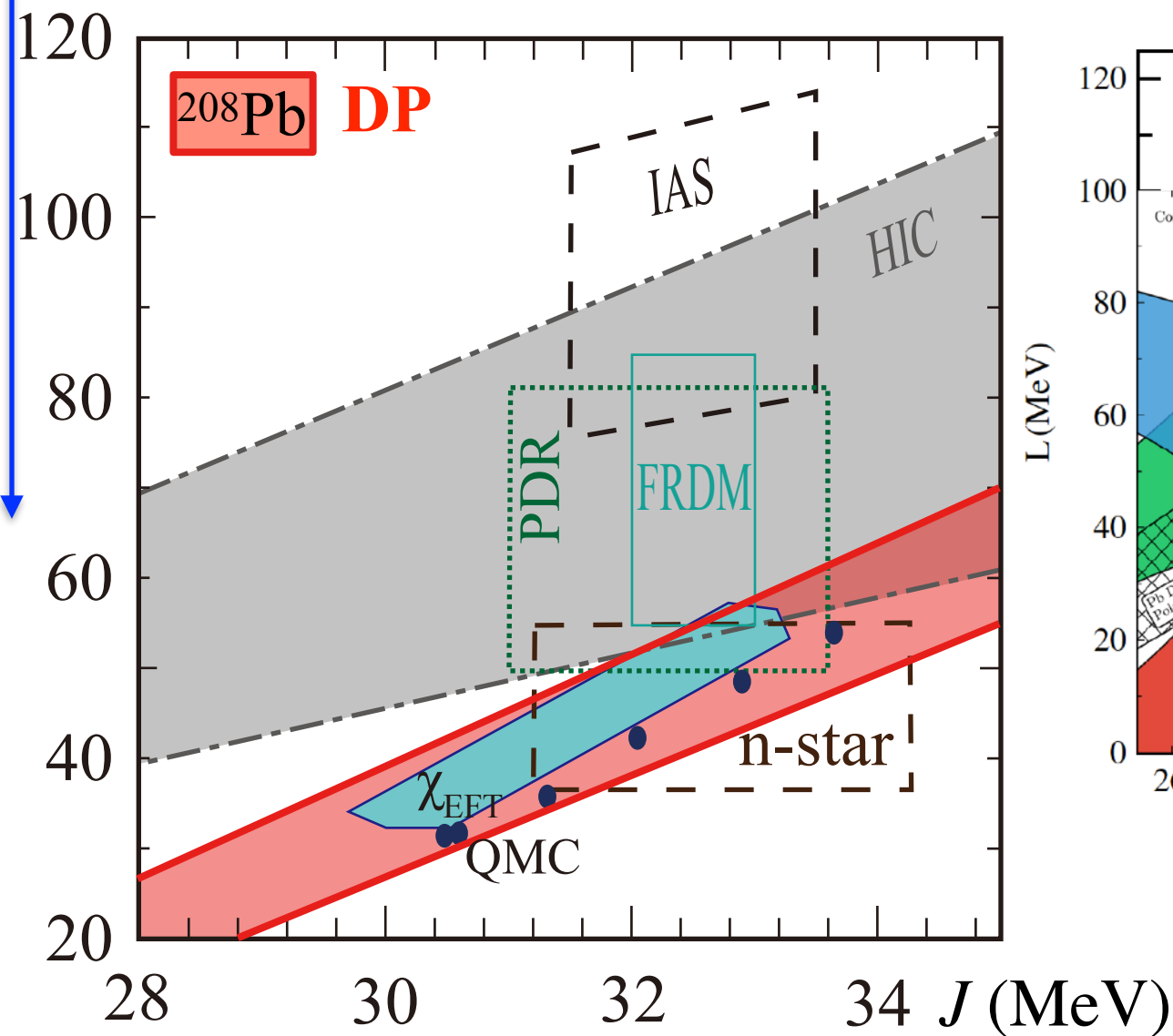
### Nuclear Equation of State



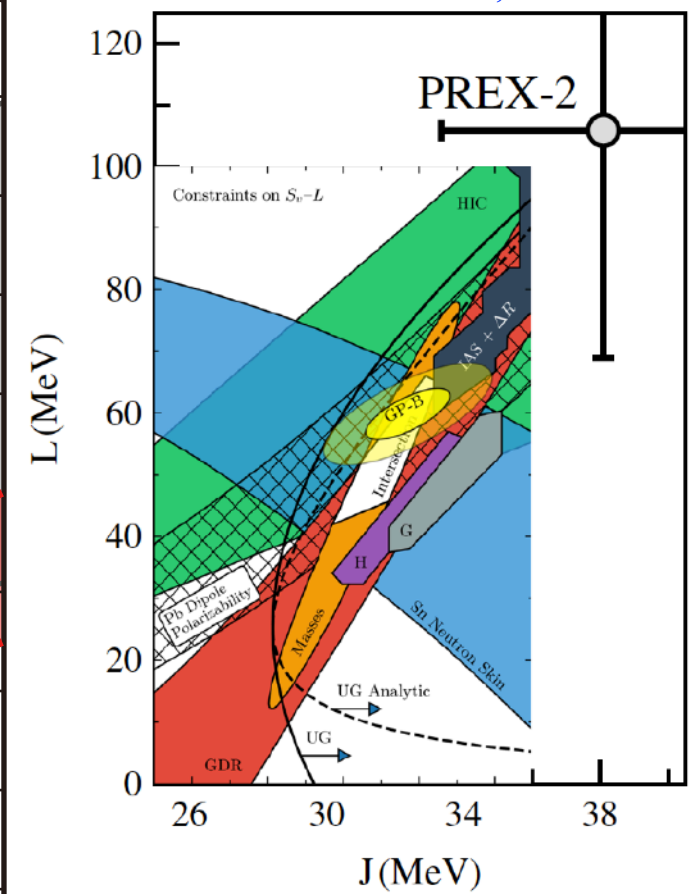
# Constraints on Symmetry Energy ( $J$ and $L$ )

$R_{\text{skin}} = R_n - R_p = (0.283 \pm 0.071) \text{ fm}$ ,  
 B.T.Reed et al., PRL2021  
**PREX-2  $106 \pm 37 \text{ MeV}$**

$L \text{ (MeV)}$



B.T.Reed et al., PRL2021



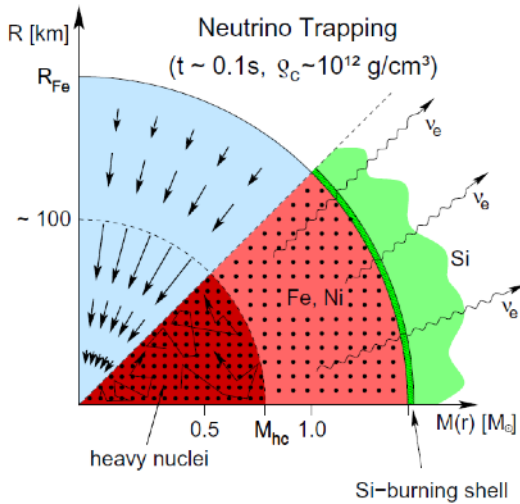
DP: Dipole Polarizability  
 208Pb AT PRL2011 24



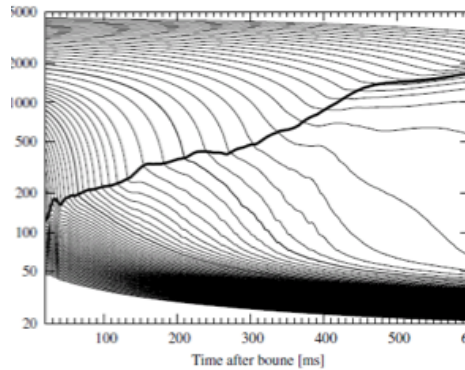
# Symmetry Energy of the Nuclear EOS

is fundamental information for stellar processes

## Core-collapse supernova

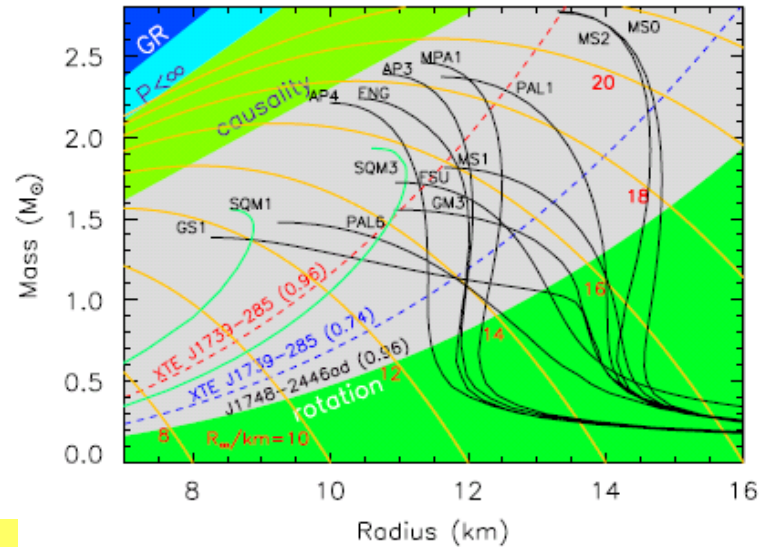


Langanke and Martinez-Pinedo



Y. Suwa et al., ApJ764, 99 (2013).

## Neutron star mass vs radius



Lattimer et al., Phys. Rep. 442, 109(2007)

## Nucleosynthesis

## Neutron star structure



## Neutron Star Merger Gravitational Wave



## Neutron star cooling

Symmetry Energyの理解: neutron-skin, n-star radius, n-star merger GW, ...

広く訴えられているので、今回は強調しない

$\rho(r, t)$

Lattimer and Prakash, Science 304, 536 (2004).



# Quasi-Deuteron Excitation Contribution

Photon absorption by a virtual deuteron in the nucleus

Needs to be subtracted for comparison with EDF calculations.

$^{208}\text{Pb}$

$$\alpha_D(^{208}\text{Pb}): 20.1 \pm 0.6 \text{ fm}^3$$

$$\text{quasi-}d: 0.51 \pm 0.15 \text{ fm}^3$$

$$\text{w/o quasi-}d: 19.6 \pm 0.6 \text{ fm}^3$$

$\sim 2.5\%$

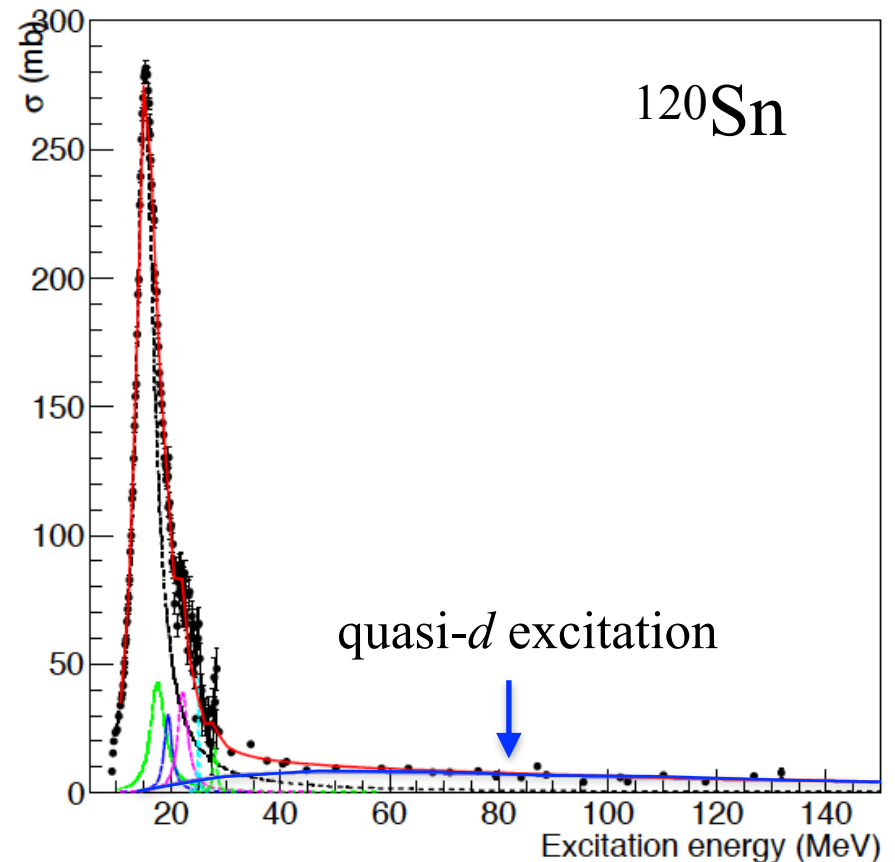
$^{120}\text{Sn}$

$$\alpha_D(^{120}\text{Sn}): 8.93 \pm 0.36 \text{ fm}^3$$

$$\text{quasi-}d: 0.34 \pm 0.08 \text{ fm}^3$$

$$\text{w/o quasi-}d: 8.59 \pm 0.37 \text{ fm}^3$$

$\sim 4\%$



quasi-deuteron excitation の理解:  
 $d$ -like correlation in nuclei

# Quasi-Deuteron Excitation Contribution

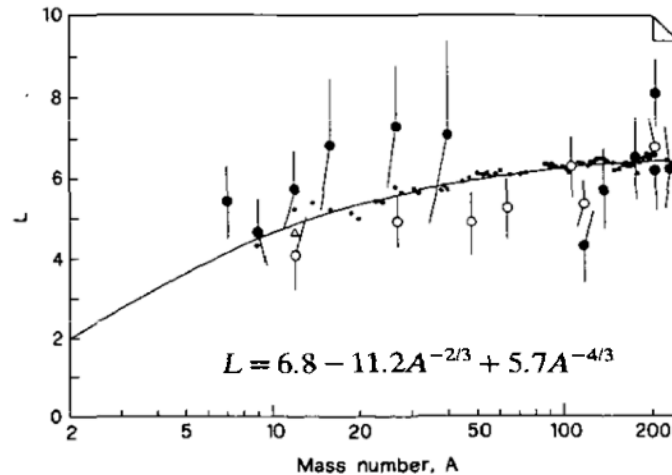
## Levinger constant

Levinger, PR84, 43(1951).

Tavares and Terranova, JPG18, 521 (1992)

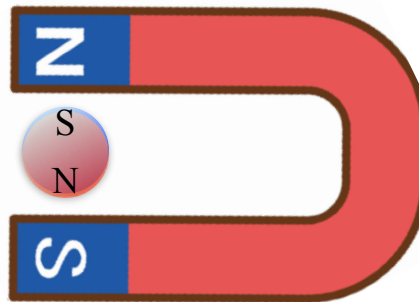
$$\sigma_{\text{qd}}^{\text{t}}(E_{\gamma}, A) = L \frac{NZ}{A} \sigma_{\text{d}}^{\text{t}}(E_{\gamma})$$

現象論的?

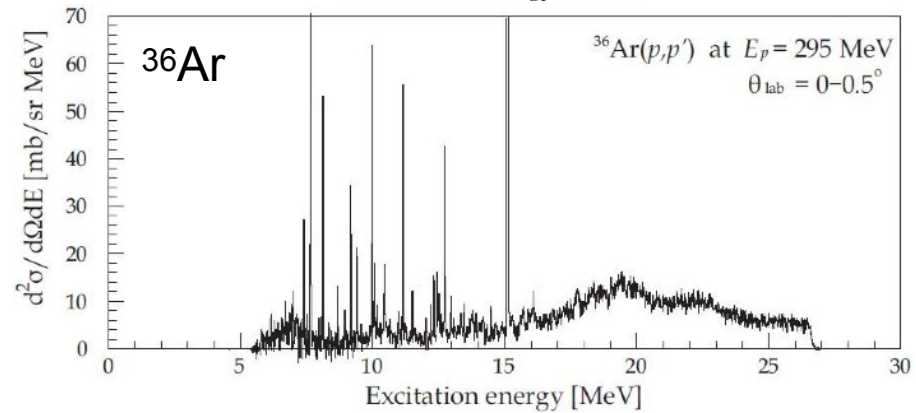
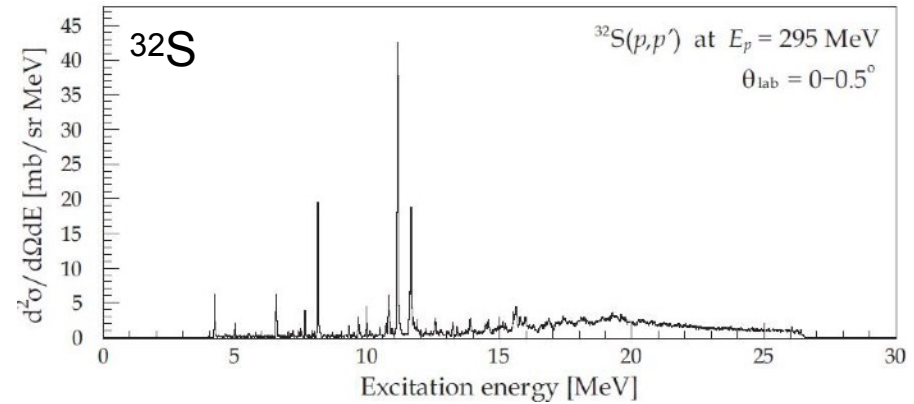
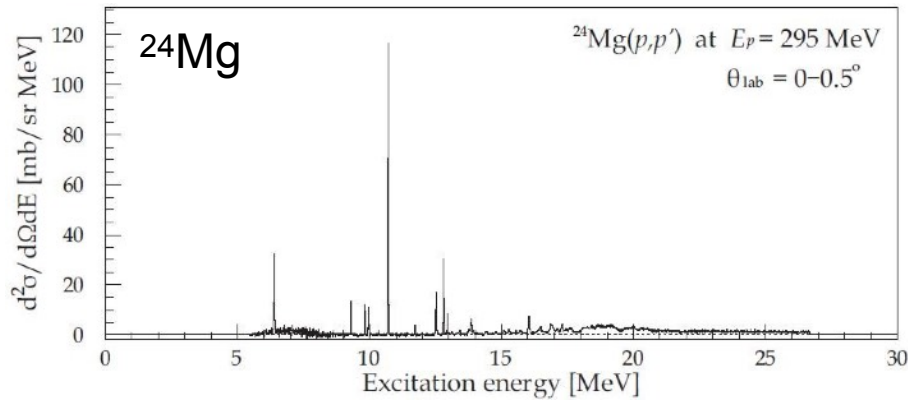
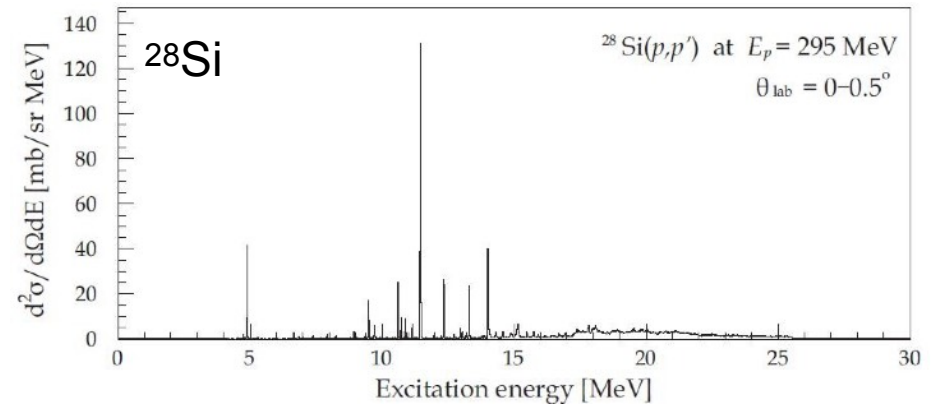
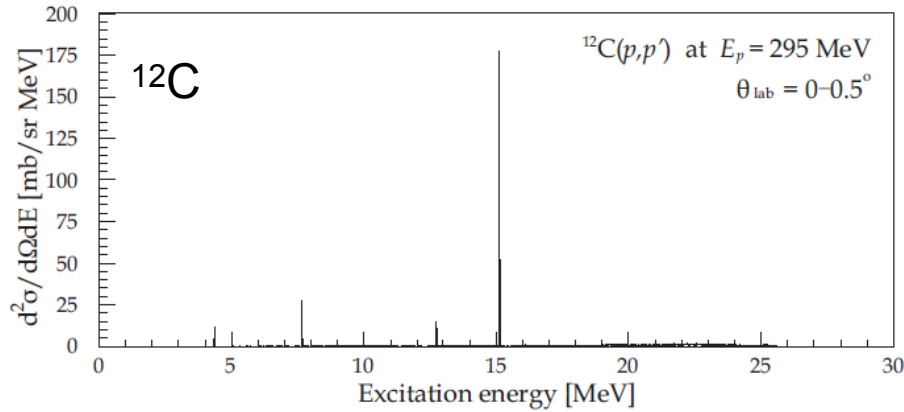


**Figure 1.** Levinger's constant  $L$  plotted against mass number  $A$ . The dots represent  $L$  values calculated according to Levinger's model as explained in the text. The line is the trend obtained by least-squares fitting of the calculated  $L$  values (equation (9)). Full circles represent  $L$  values obtained from total nuclear photoabsorption cross section data [14]. Open symbols represent  $L$  values deduced from:  $\circ$ , data by Stibunov [16];  $\triangle$ , data by Homma *et al* [17, 18].

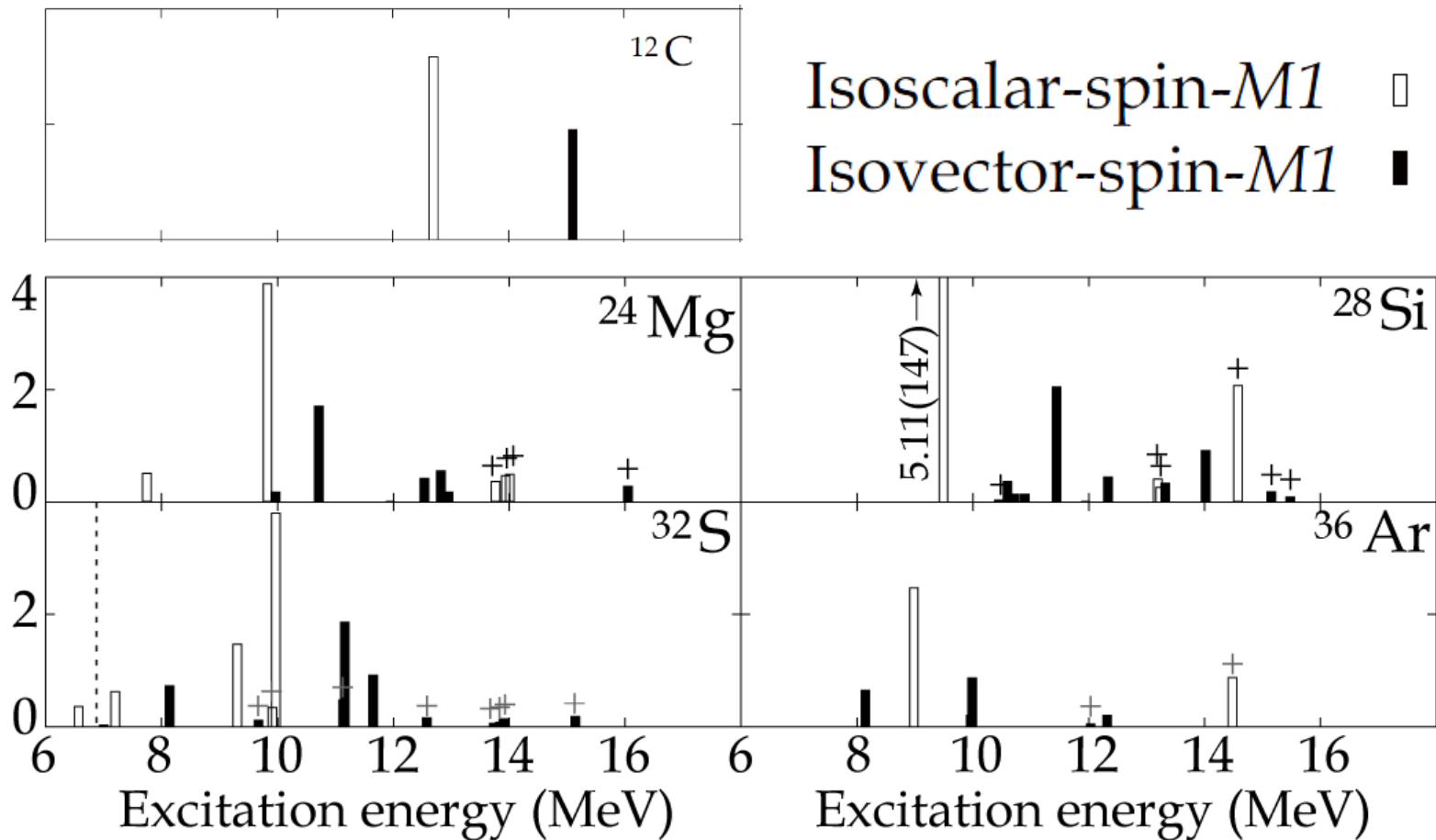
# spin-Magnetic Excitation



# Energy spectra at 0-degrees

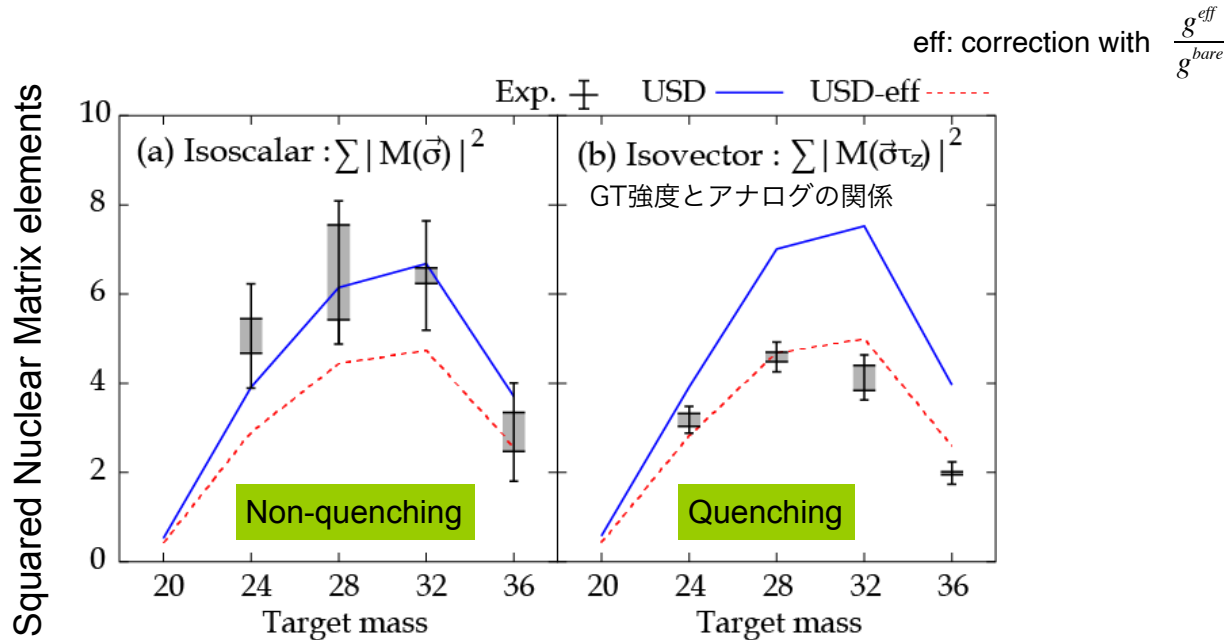


# IS / IV-spin-M1 distribution



# スピンM1遷移行列要素

H. Matsubara et al., PRL115, 102501 (2015)



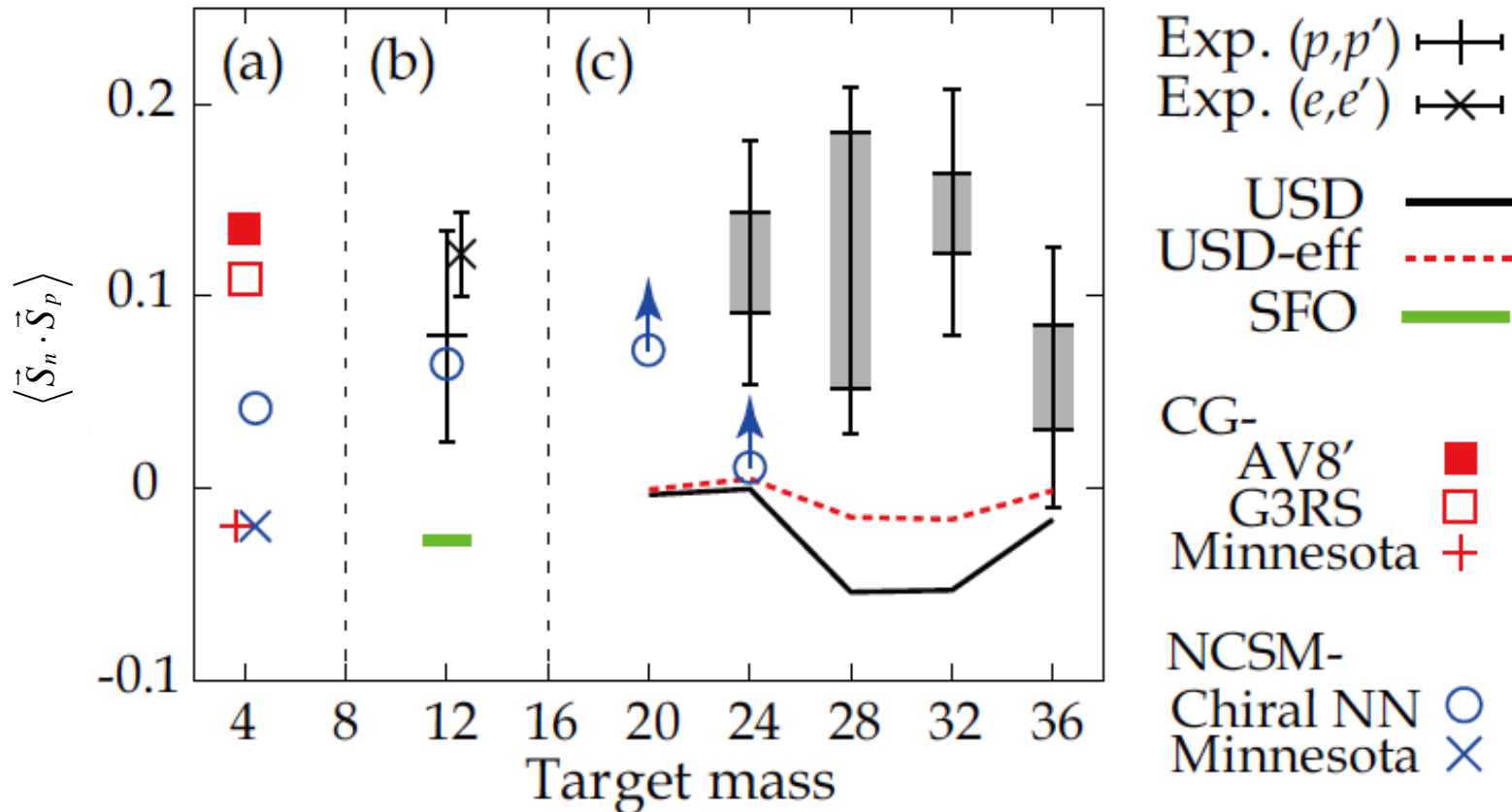
IV spin-M1遷移行列要素にquenchingがあるが  
IS spin-M1遷移行列要素にはquenchingが見られない

(IS/IV spin-M1) Quenching機構の理解

GTなど他のmultipolarity遷移も  
“ab initio” couple-cluster model etc.

# スピンM1遷移行列要素

H. Matsubara et al., PRL115, 102501 (2015)



np スピン相関関数(基底状態)

$$\langle \vec{S}_n \cdot \vec{S}_p \rangle = \frac{1}{16} \left( \sum_{\text{IS-IV}} |M(\vec{\sigma})|^2 - \sum |M(\vec{\sigma}\tau_z)|^2 \right)$$

model dependent sum-rule

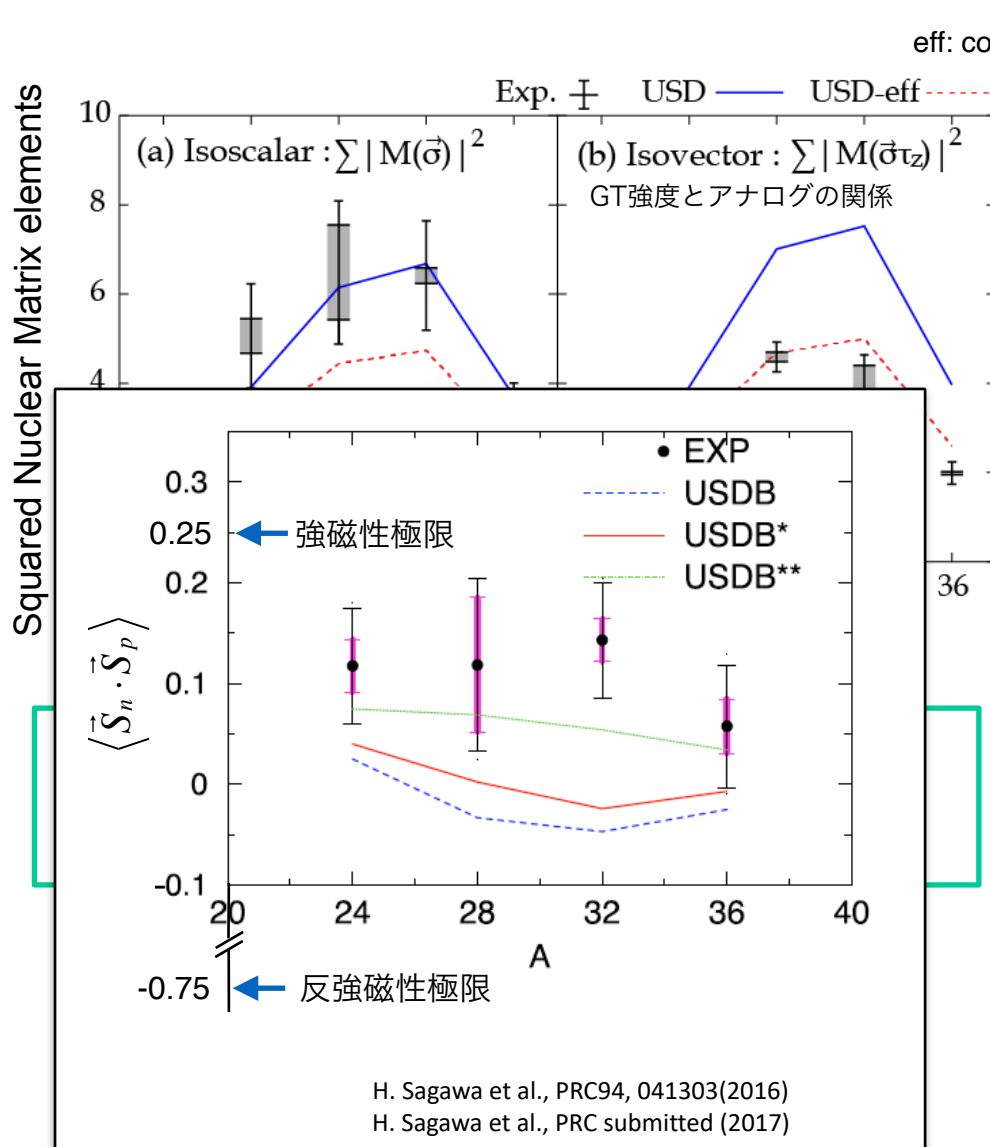
基底状態のnp-spin相関の理解

d-like correlation in nuclei



# スピンM1遷移行列要素

H. Matsubara et al., PRL115, 102501 (2015)

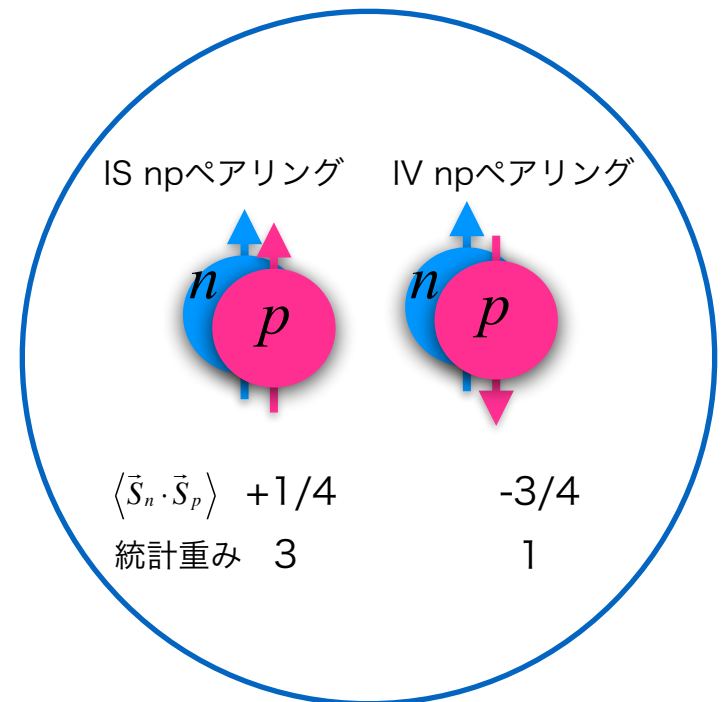


np スピン相関関数(基底状態)

$$\langle \vec{S}_n \cdot \vec{S}_p \rangle = \frac{1}{16} \left( \sum |M(\vec{\sigma})|^2 - \sum |M(\vec{\sigma}\tau_z)|^2 \right)$$

IS - IV

$> 0$



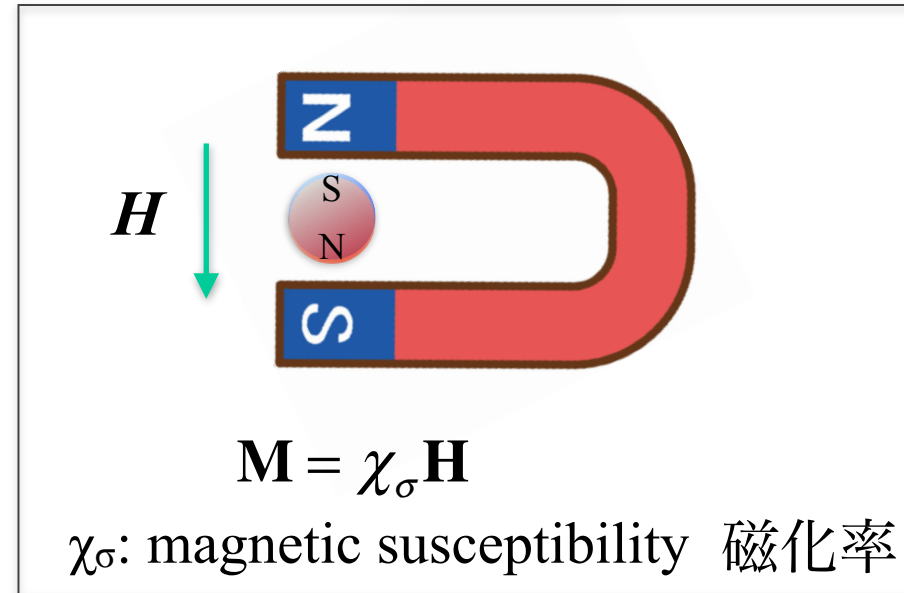
# 原子核の磁氣的応答: スピン磁化率

Magnetic dipole ( $M1$ ) operator

$$O(M1) = g_\ell^{\text{IS}} \ell + \underline{g_s^{\text{IS}} \sigma} + g_\ell^{\text{IV}} \ell \cdot \tau + \underline{g_s^{\text{IV}} \sigma \cdot \tau}$$

IS(1) and IV( $\tau$ ) terms

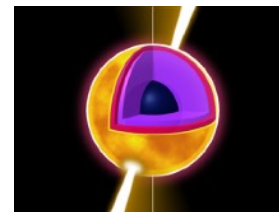
$$\chi_\sigma^{\text{spin}} = \frac{8}{3N} \sum_f \frac{1}{\omega} \left| \langle f | \sum_i \sigma_i | 0 \rangle \right|^2$$



- 核物質の磁化率のスピ成分
- 強磁場中の核物質の応答(マグネターなど)
- 超新星爆発コア中でのニュートリノ閉じ込め・透過度
- 中性子星の強磁性体状態発現の可能性

S. Fantoni et al., PRL87, 181101 (2001)

S. Reddy et al., PRC59, 2888 (1999)



マグネター  $10^{14-16}$  Gauss

核物質のスピ磁化率の理解

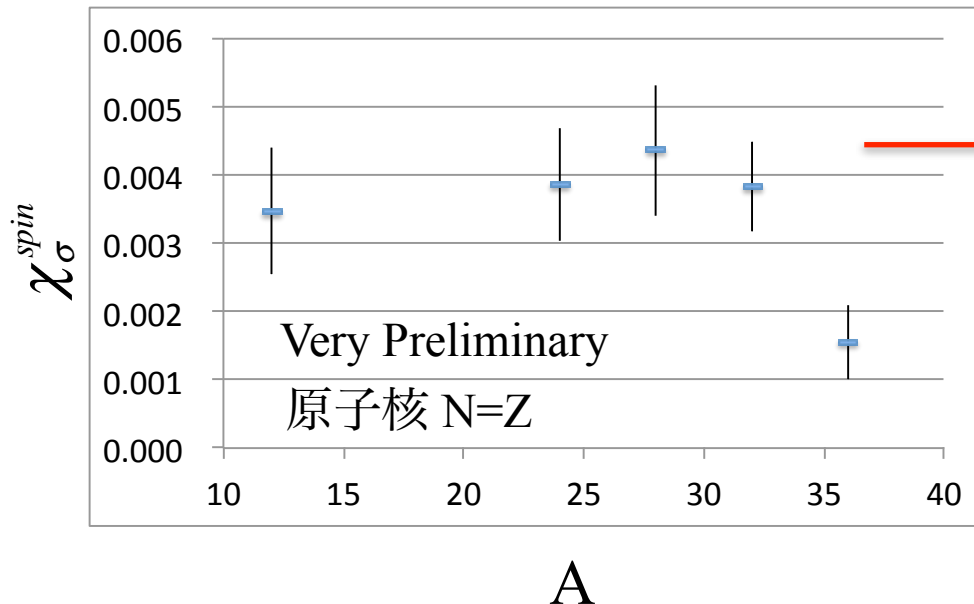
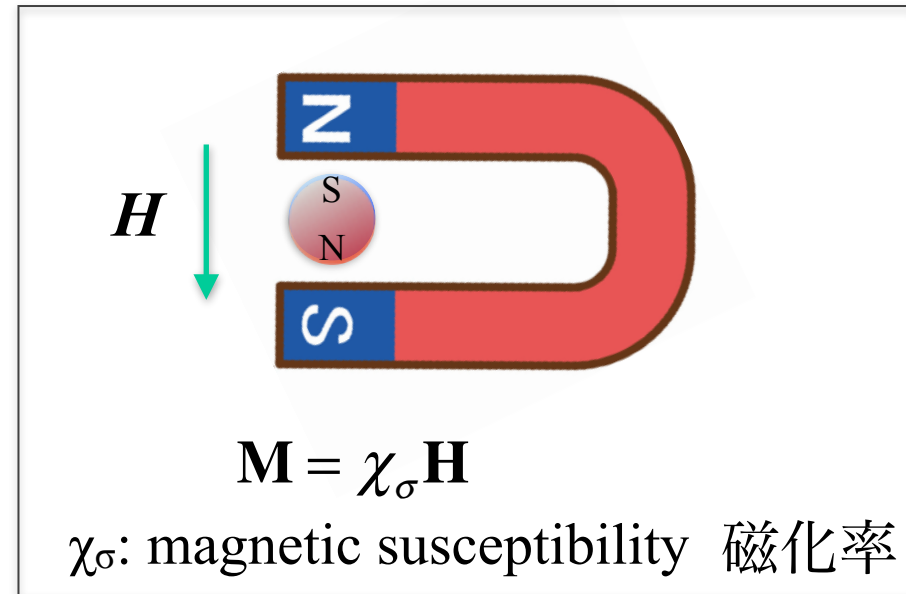
# スピン磁化率

Magnetic dipole ( $M1$ ) operator

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IS(1) and IV( $\tau$ ) terms

$$\chi_\sigma^{\text{spin}} = \frac{8}{3N} \sum_f \frac{1}{\omega} \left| \langle f | \sum_i \sigma_i | 0 \rangle \right|^2$$



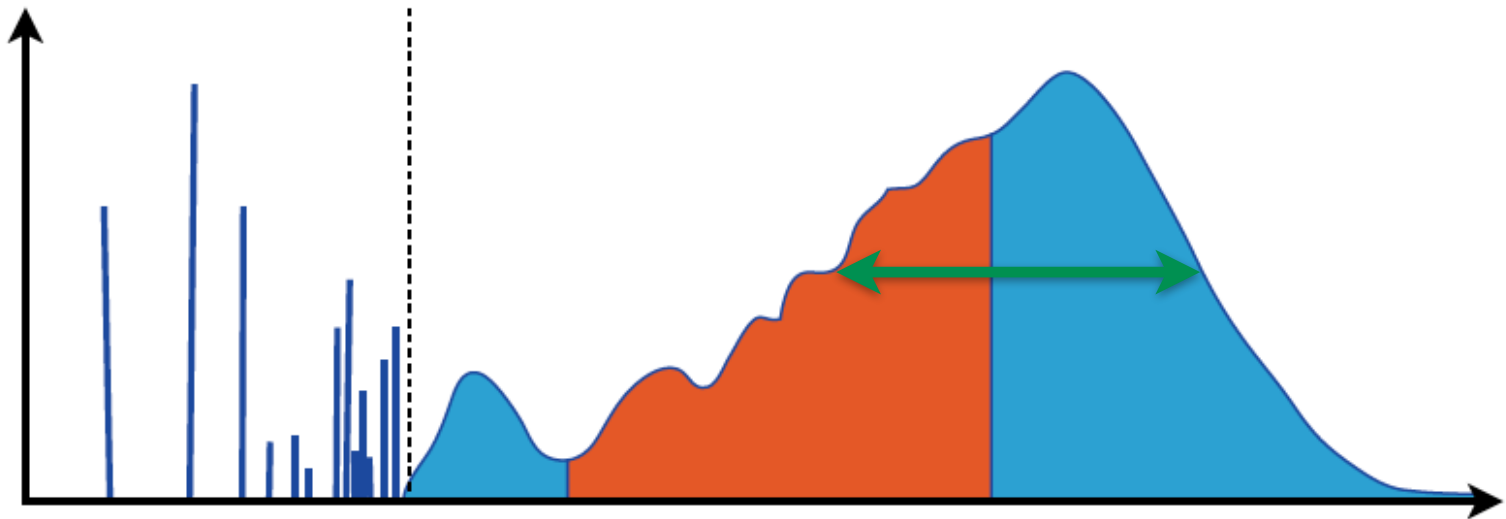
0.0044(7) MeV<sup>-1</sup> at  $\rho=0.16 \text{ fm}^{-3}$

中性子物質計算 AFDMC model

G. Shen et al., PRC87, 025802 (2013)

→ 重い原子核、同位体依存性、...

# Damping of Giant Resonances



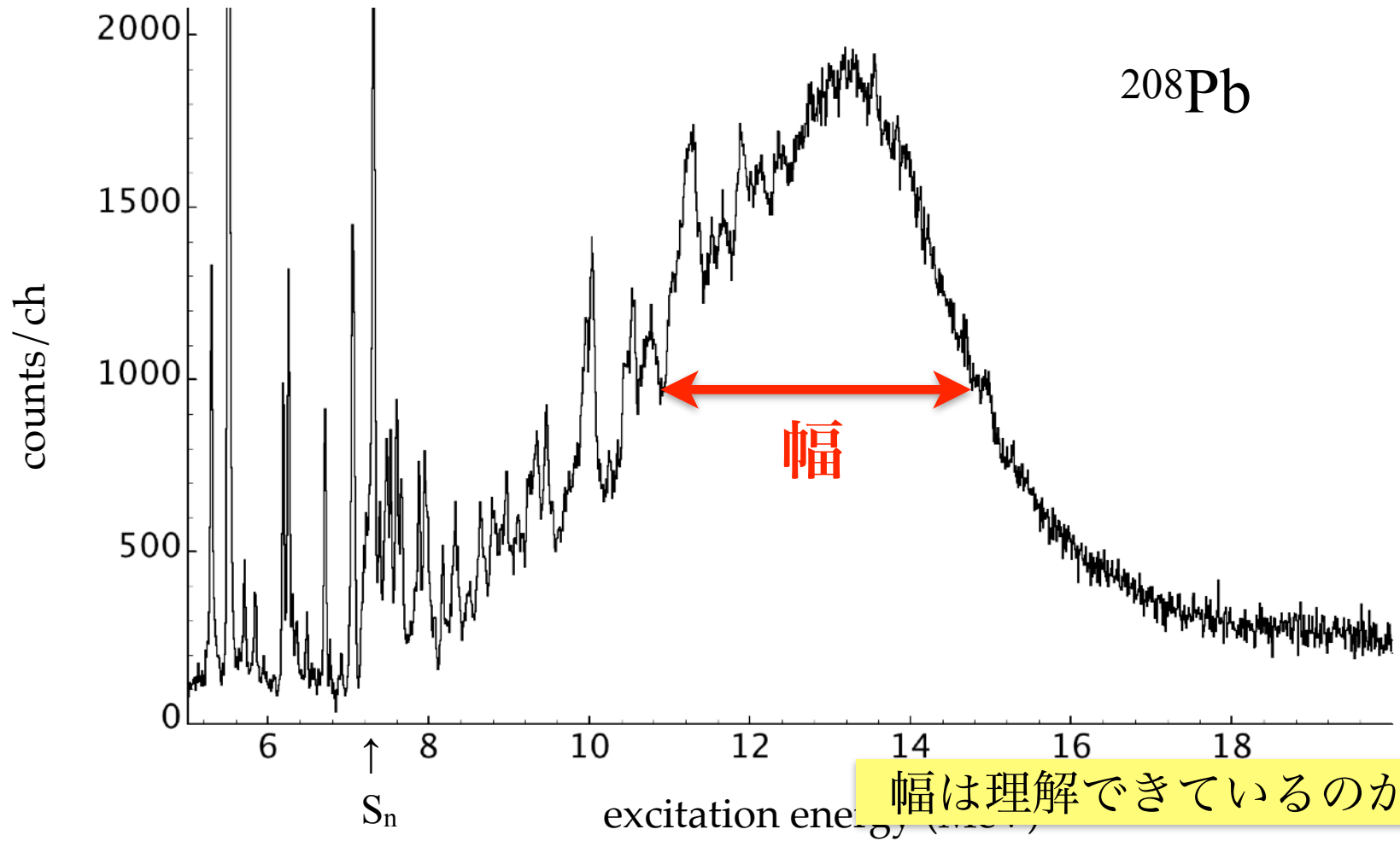
# 原子核の電気双極(E1)応答



PDR ピグミー共鳴



IVGDR 巨大双極子共鳴



幅は理解できているのか？

巨大共鳴の崩壊の記述

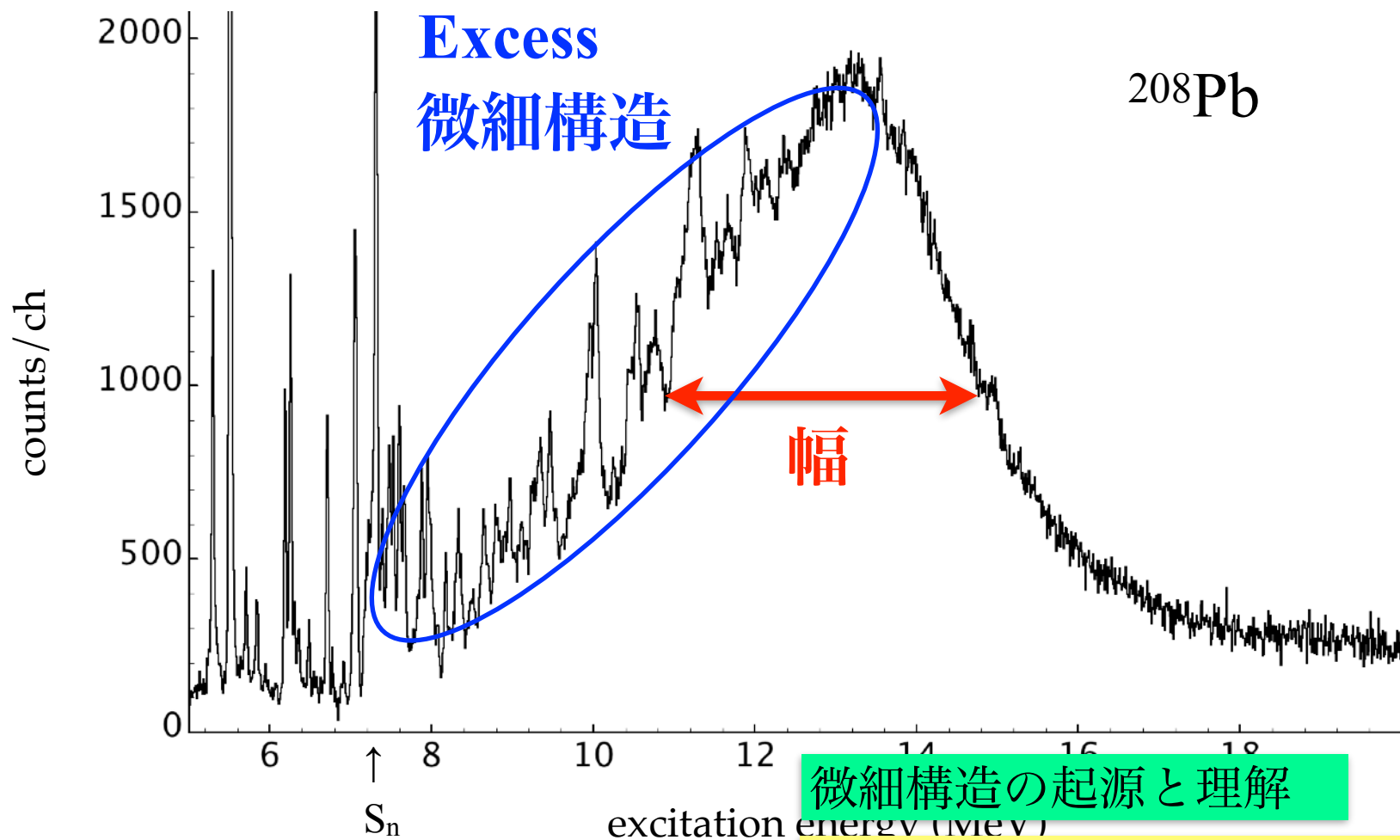
# 原子核の電気双極(E1)応答



PDR ピグミー共鳴



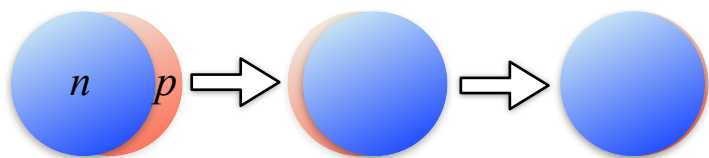
IVGDR 巨大双極子共鳴



微細構造の起源と理解

特徴的な幅を持つのではないか？

# 巨大共鳴の減衰



巨大双極子共鳴(IVGDR)

巨視的な集団運動描像

→陽子と中性子の相対双極振動

振動の減衰は、陽子中性子流体間の粘性  
によって引き起こされる

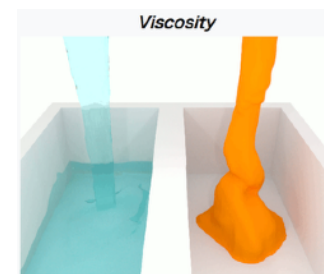
減衰（共鳴幅）の生成機構 (教科書的説明)

$$\Gamma = \Delta\Gamma + \Gamma_{\downarrow} + \Gamma_{\uparrow}$$

$\Delta\Gamma$  ランダウ減衰: 戸口状態の1p1h配位分布  
複数の1p1h共鳴モードの合成

$\Gamma_{\uparrow}$  エスケープ幅: 戸口状態からの粒子・光子放出による直接崩壊過程  
エネルギーを放出して別の状態へ遷移する

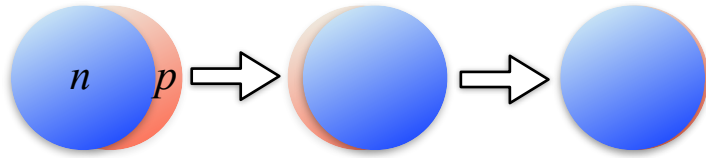
$\Gamma_{\downarrow}$  分散幅: 戸口状態からより複雑な配位(複合核) への遷移  
共鳴がコヒーレンスを失っていく過程



wikipedia



# 巨大共鳴の減衰：微視的理解



巨大双極子共鳴(IVGDR)

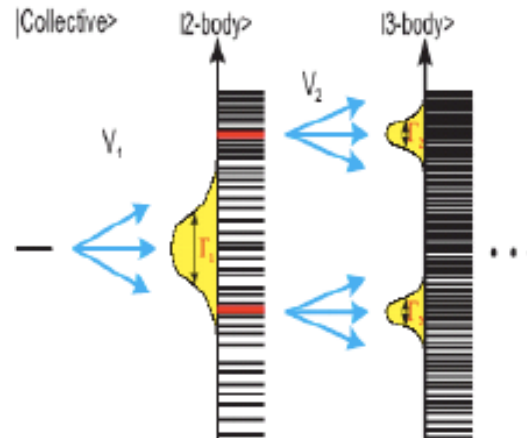
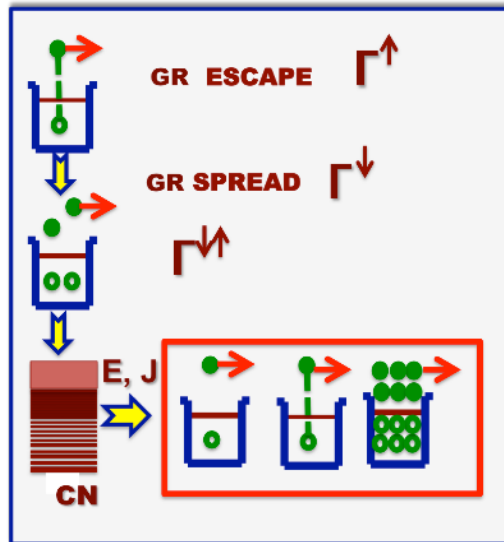
分散幅:

励起状態のW.F.

中重核の分散幅の主成分

$$|\psi\rangle = \sum_i |1p1h\rangle_i + \sum_i |1phonon + 1p1h\rangle_i + \sum_i |2p2h\rangle_i + \dots + \sum_i |CN\rangle_i$$

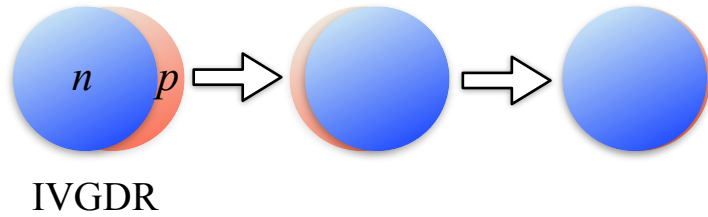
→ コヒーレンスを失うことによる減衰



total width =  $\Sigma$  partial width  
 $\propto \Sigma$  partial transition rate  
 $\propto \Sigma$  (partial life time)<sup>-1</sup>



# 巨大共鳴の減衰：実験からの観点



巨大共鳴は最終的にはエネルギーを失って別の形態へ崩壊する。

崩壊チャンネルは放出粒子（光子）とそのエネルギーによって分類される

$$\Gamma = \sum \Gamma_n + \sum \Gamma_p + \sum \Gamma_\gamma + \dots$$

実験では、各崩壊チャンネル毎に分岐比を測定することが可能

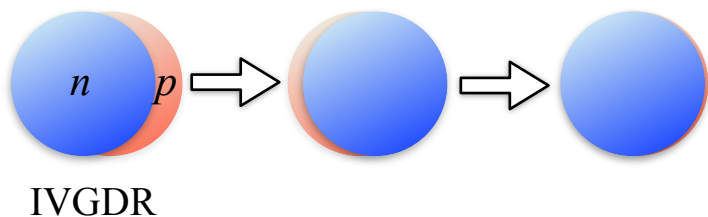
$$\text{分岐比: } b_i = \frac{\Gamma_i}{\Gamma} \quad \text{全幅: } \Gamma = \sum \Gamma_i$$

今回の研究では基底状態への $\gamma$ 崩壊に着目

$$\Gamma_{\gamma_0} \quad \text{分岐比} \sim 1\%$$

なぜか？

# 巨大共鳴の減衰



基底状態への $\gamma$ 崩壊は、基底状態からのクーロン励起の逆過程にあたる。

基底状態からのクーロン励起断面積から

- $B(E1)\uparrow$
- $B(E1)\downarrow$  (微細平衡)
- $\Gamma_{\gamma_0}$

が決まる。

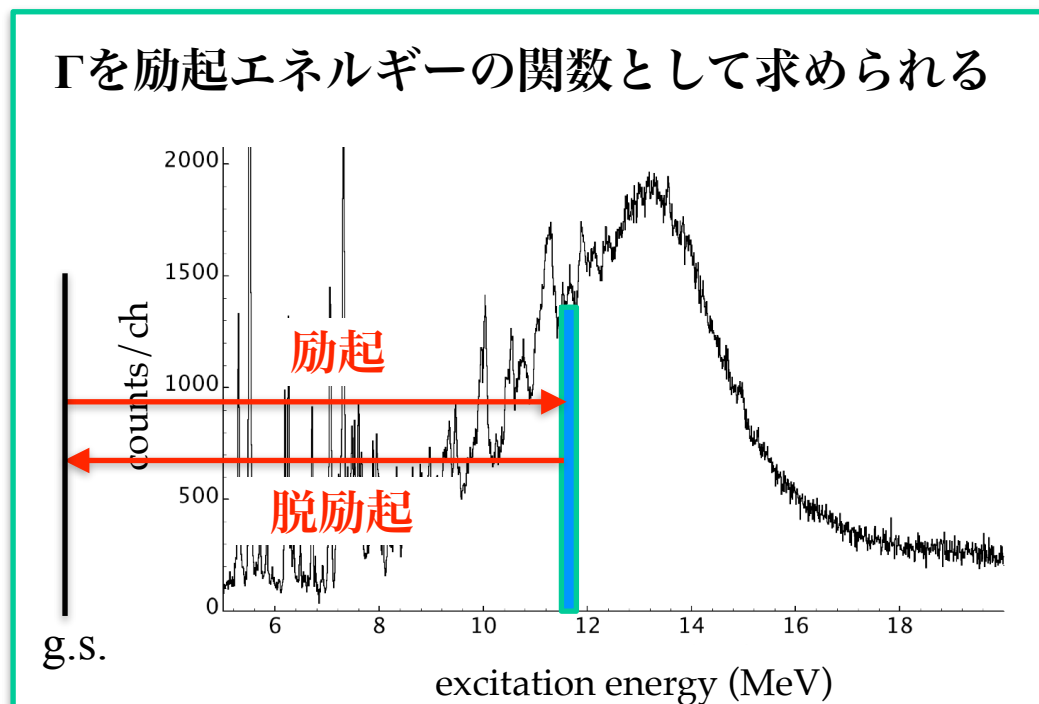
崩壊同時測定

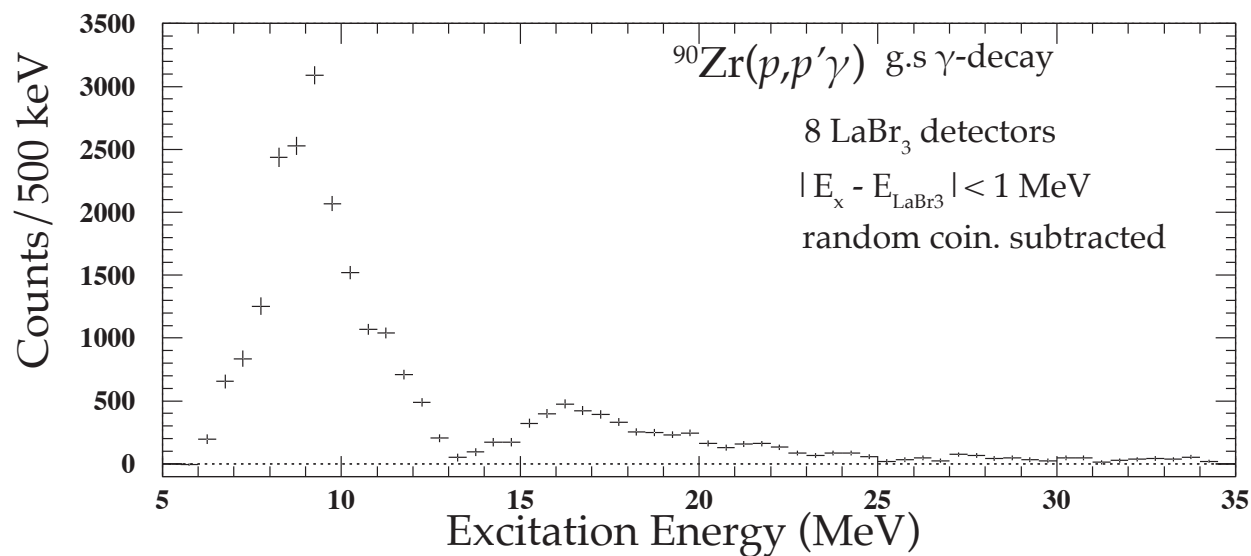
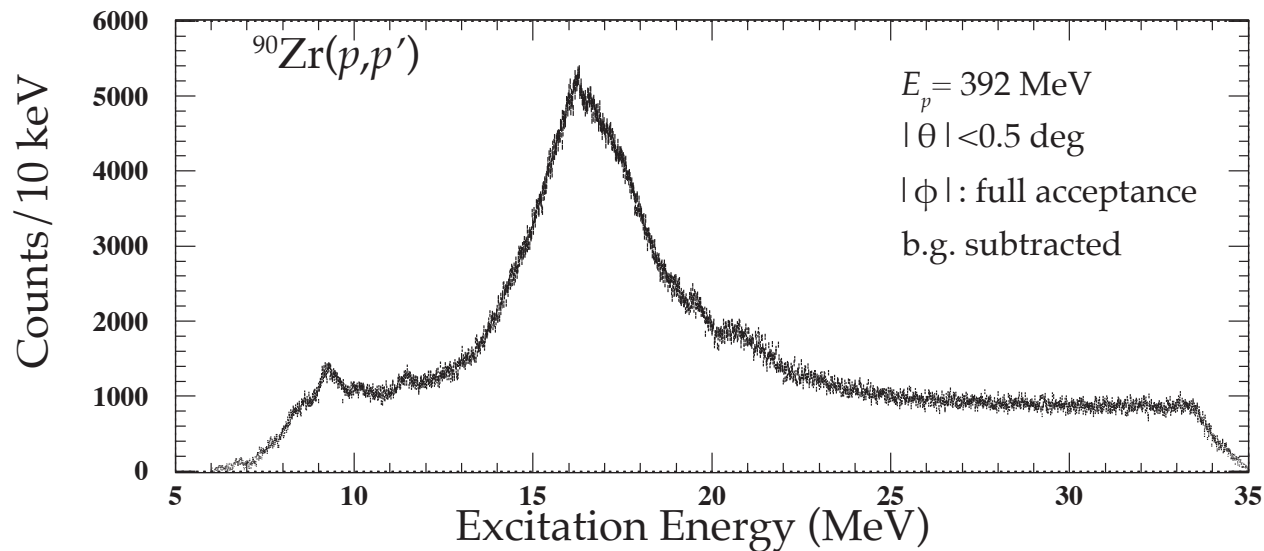
→ 分岐比  $b_{\gamma_0} = \frac{\Gamma_{\gamma_0}}{\Gamma}$

が決まる。

- $\Gamma$ が決まる

どうなる？

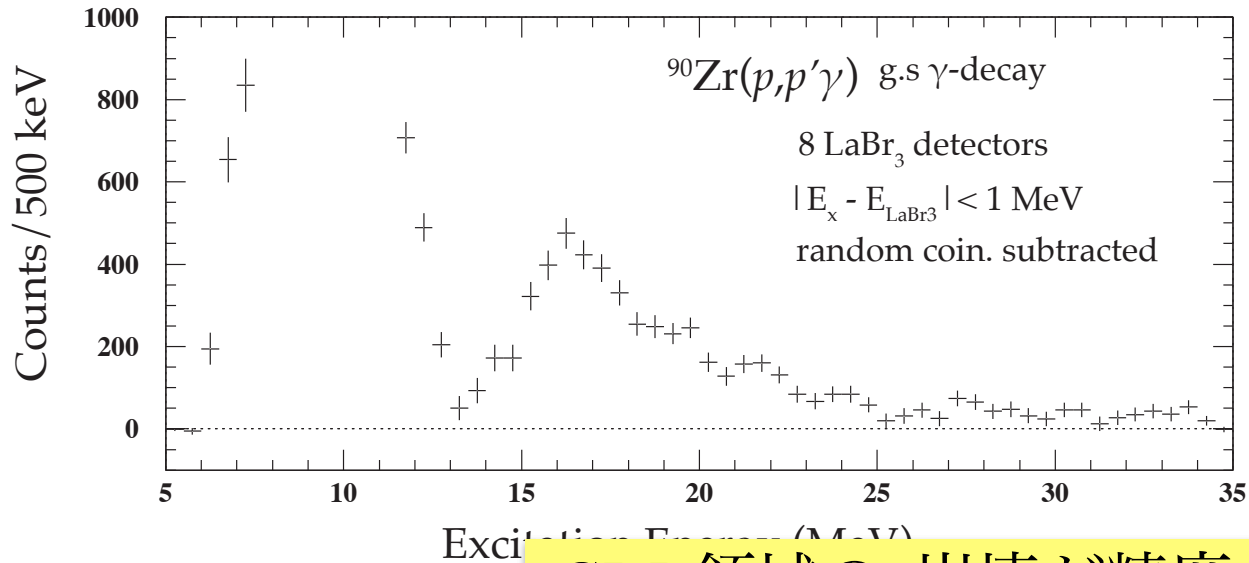
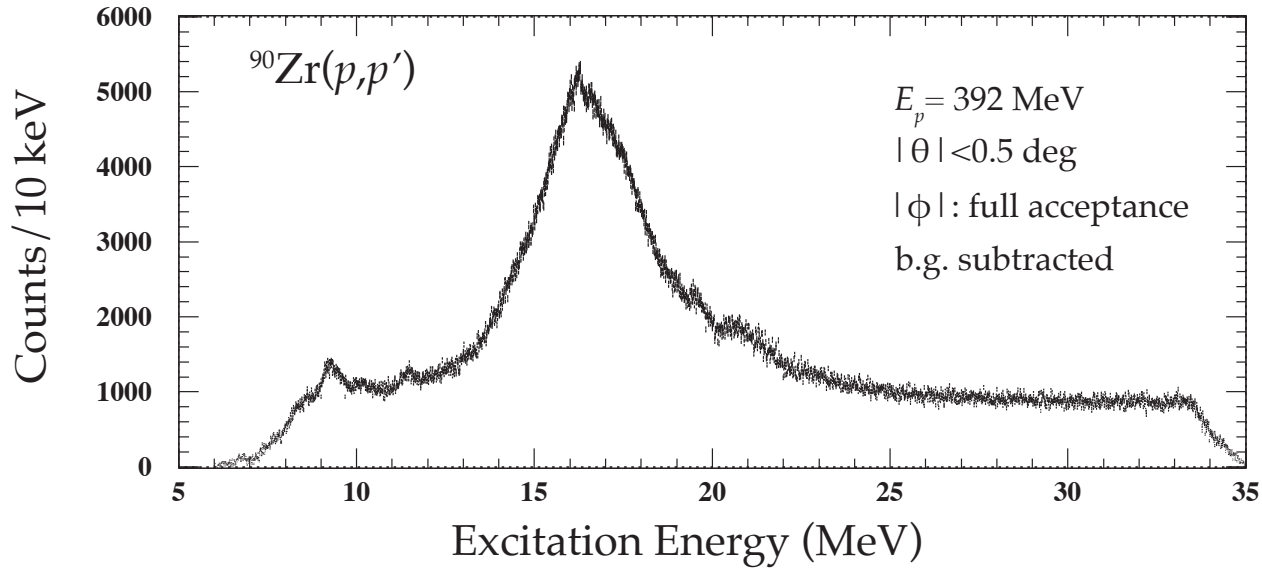




preliminary

$^{90}\text{Zr}(p,p')$  at 0 deg

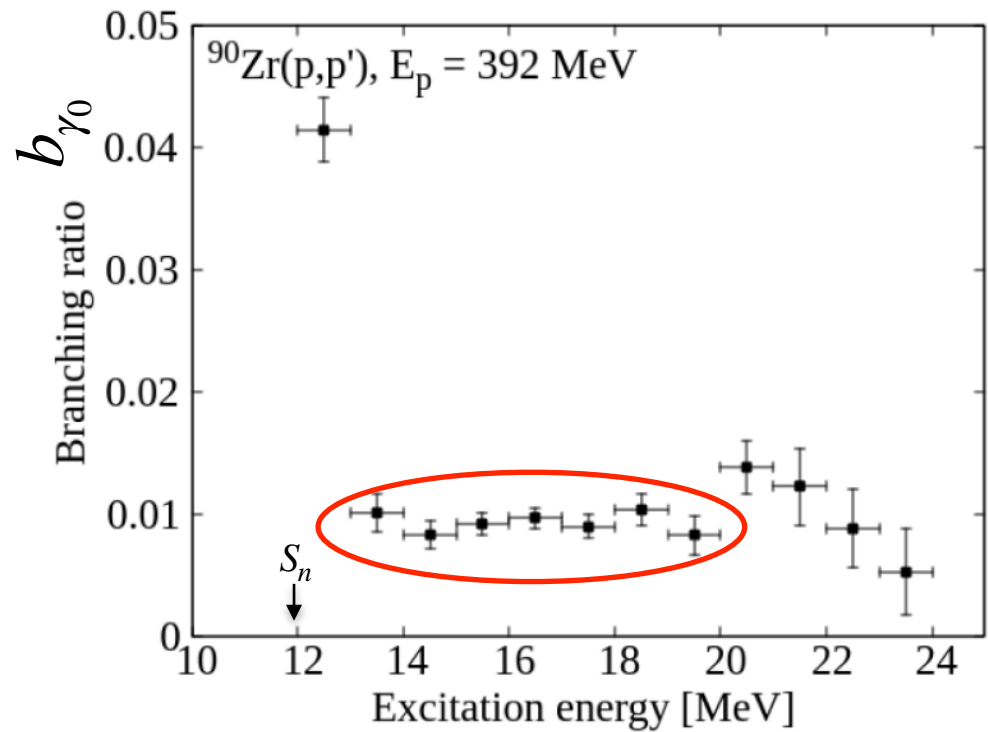
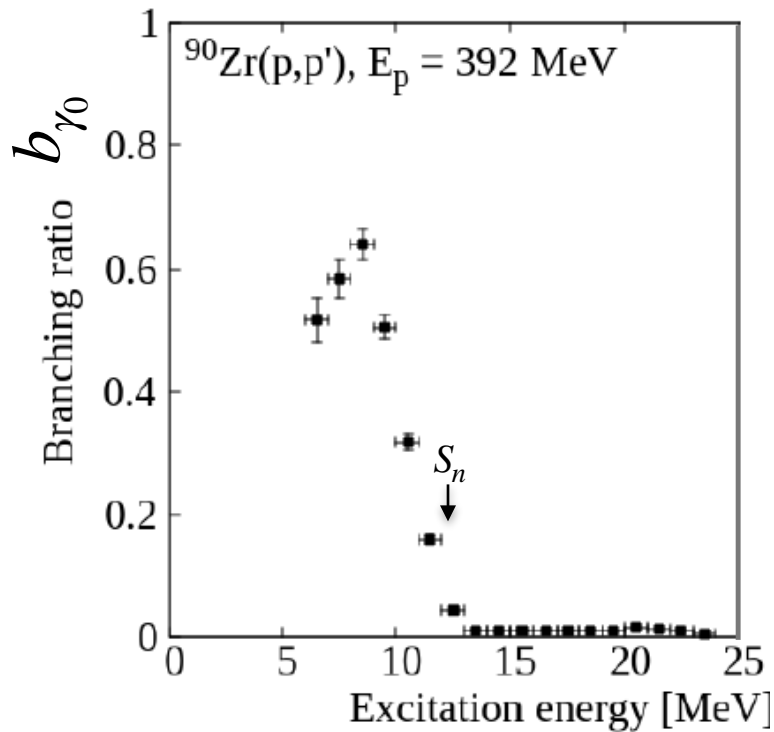
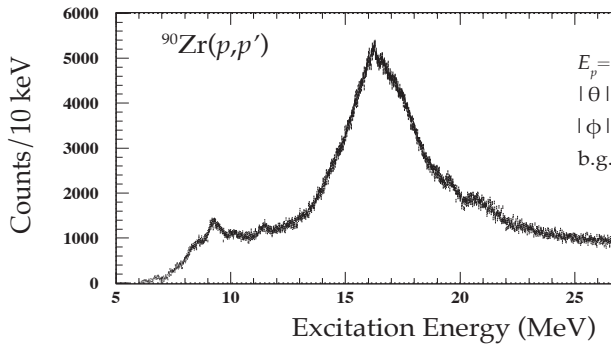
RCNP-E498  
semi-online analysis  
2018/07/27 Run #1100-1199



GDR領域の $\gamma$ 崩壊が精度よく測れた

# g.s. $\gamma$ 崩壊: 分岐比

Preliminary

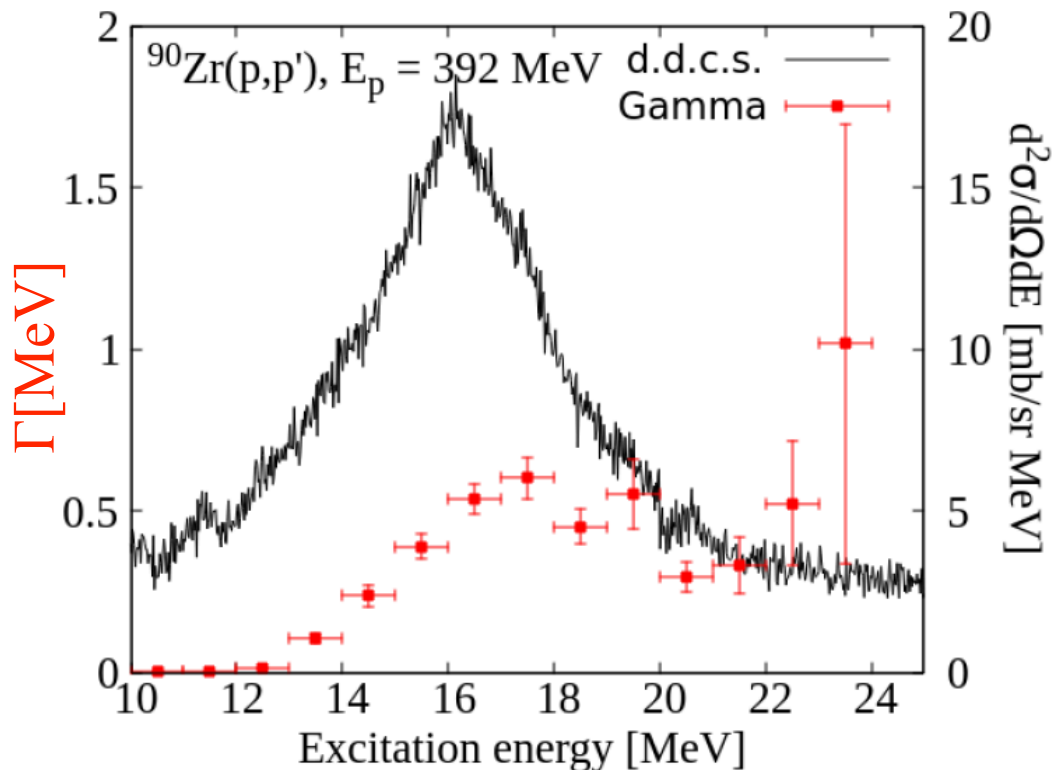


g.s. $\gamma$ 崩壊比はGDR領域でほぼフラット

# Γの励起エネルギー依存性

Preliminary

$$\Gamma = \frac{\Gamma_{\gamma_0}}{b_{\gamma_0}} \quad \Gamma_{\gamma_0} = \frac{16\pi}{9} \left( \frac{E_x}{\hbar c} \right)^3 \frac{2J_0 + 1}{2J_x + 1} B(E1) \uparrow$$



どう解釈するのか？

測られた「Γ」は  
Γなのか、Γ↑なのか？

$$\Gamma = \Delta\Gamma + \Gamma\downarrow + \Gamma\uparrow$$

「Γ」を積算した値がIVGDRの  
幅に対応するのか？

$E_x \rightarrow$ 大で、「Γ」 $\rightarrow$ 大

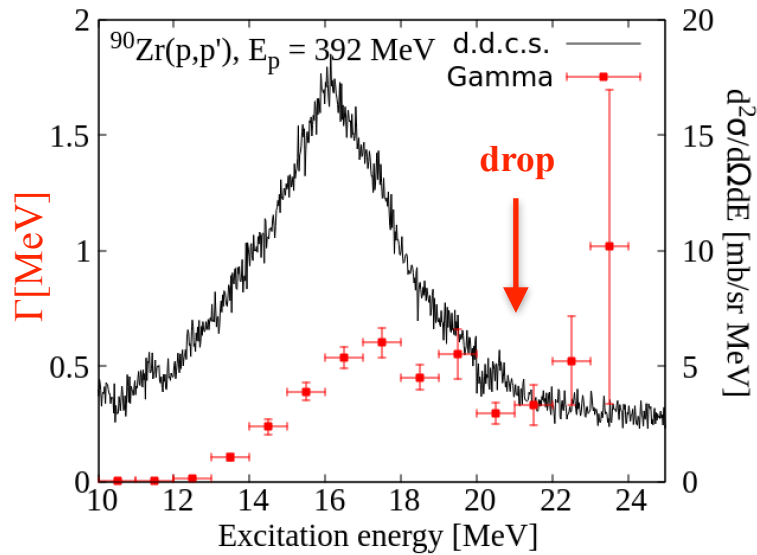
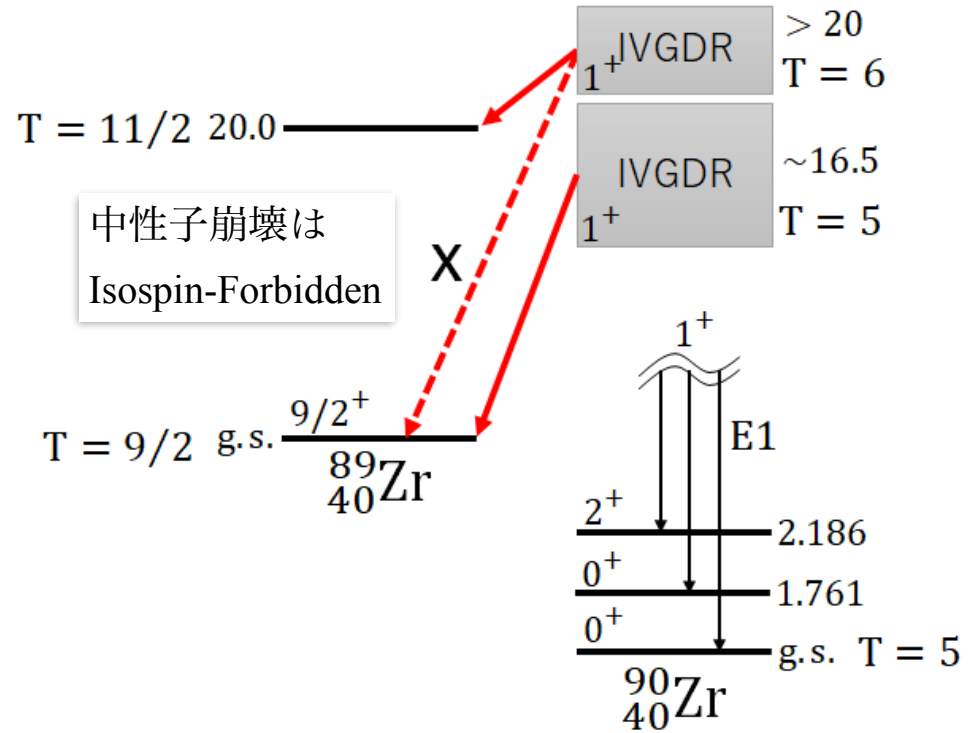
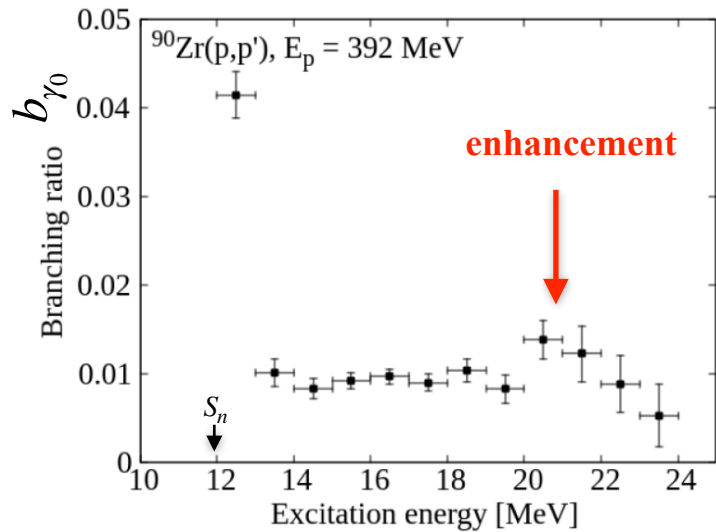
中性子崩壊の位相空間体  
積効果？

IVGDRの低 $E_x$ 側に見られ  
る微細構造に対応？

open questions...

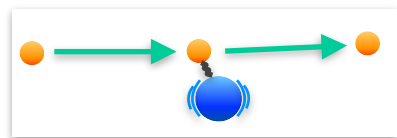
# Isospin Upper IVGDR の影響

Preliminary

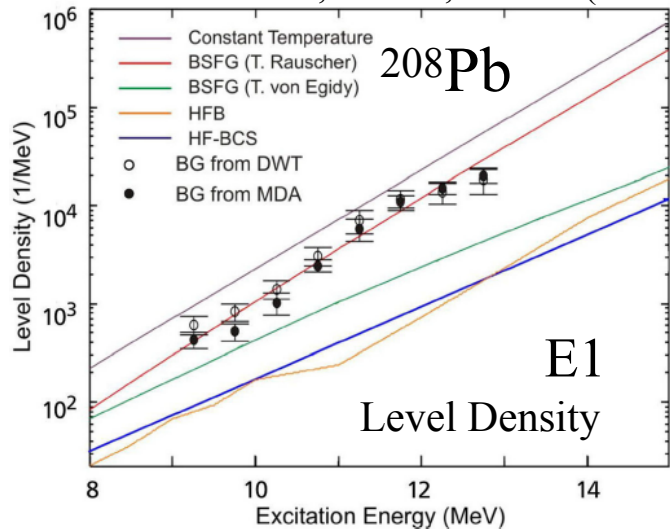


# Nuclear Level Densities

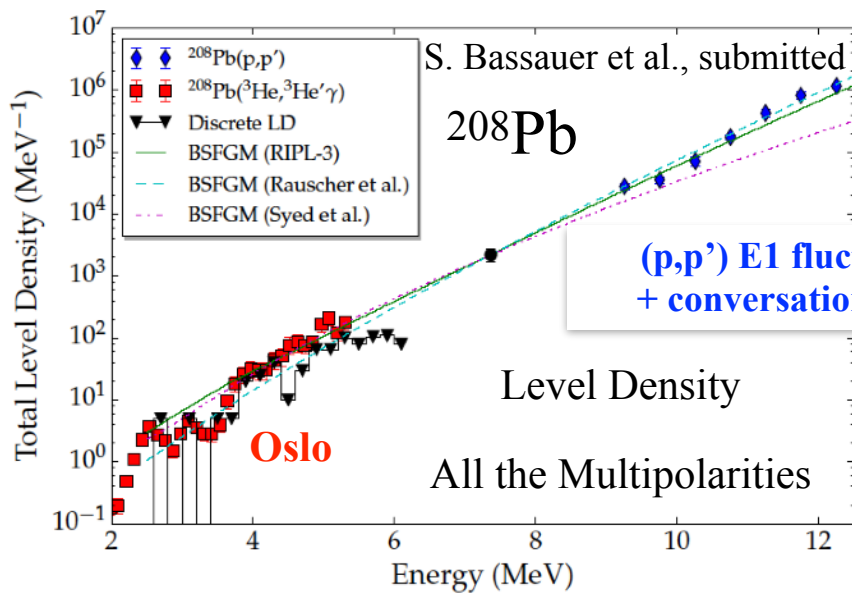
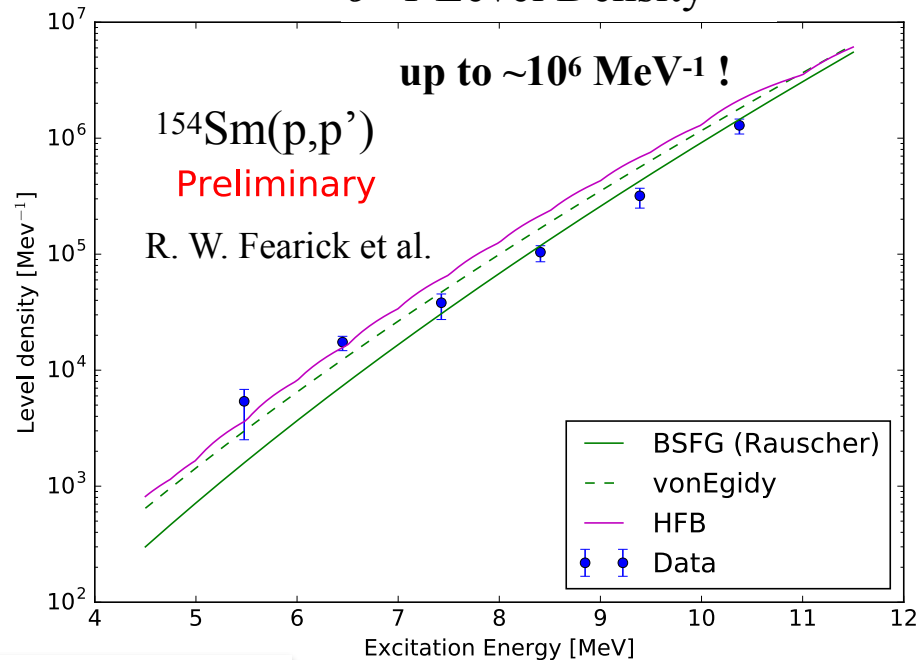
extracted by fluctuation analysis using auto-correlation function



I. Poltoratska et al., PRC89, 054322 (2014)



$J=1$  Level Density

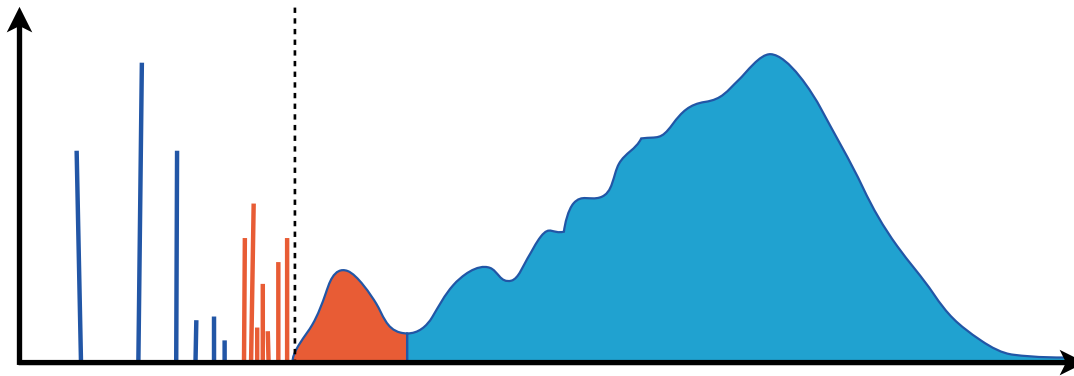


**(p,p') E1 fluctuation analysis  
+ conversion to total (theo.)**

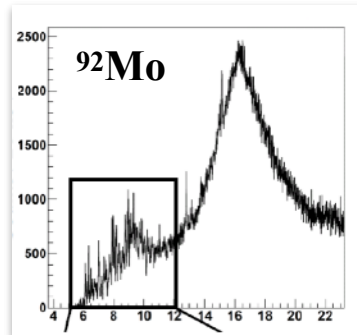
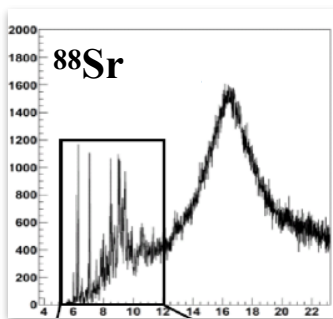
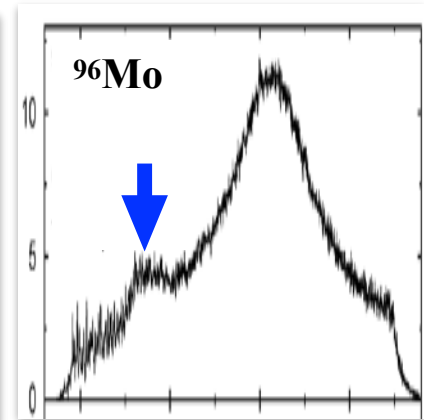
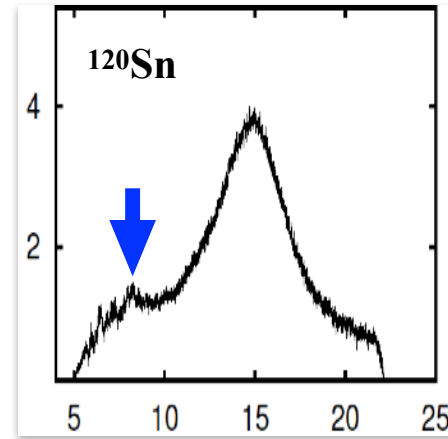
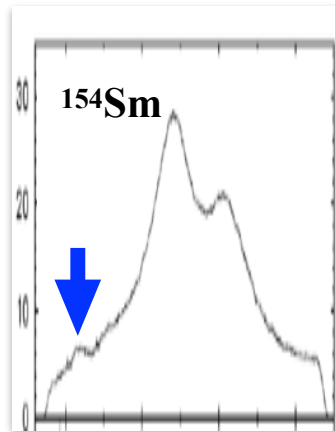
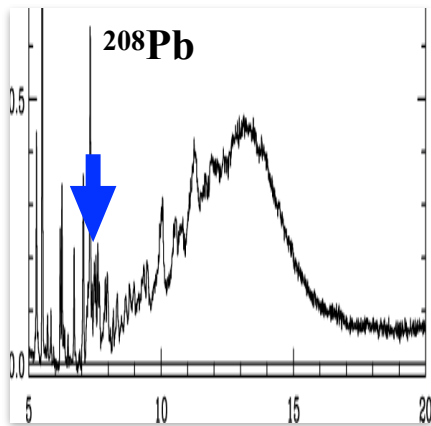
準位密度の定量的記述



# Pygmy Dipole Resonance

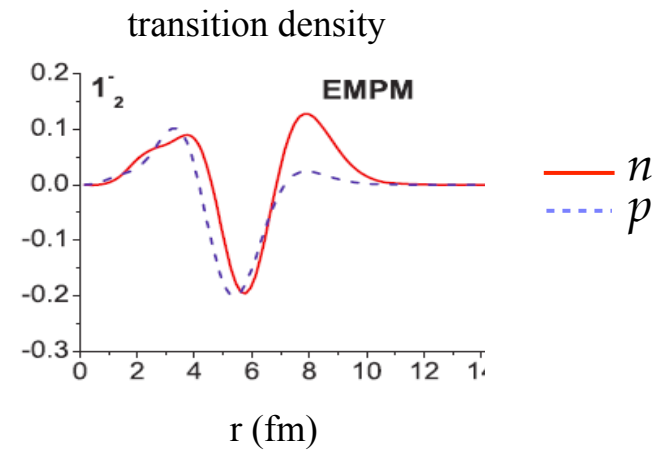


# Universal Existence of PDR in Nuclei with $A > \sim 90$ ?



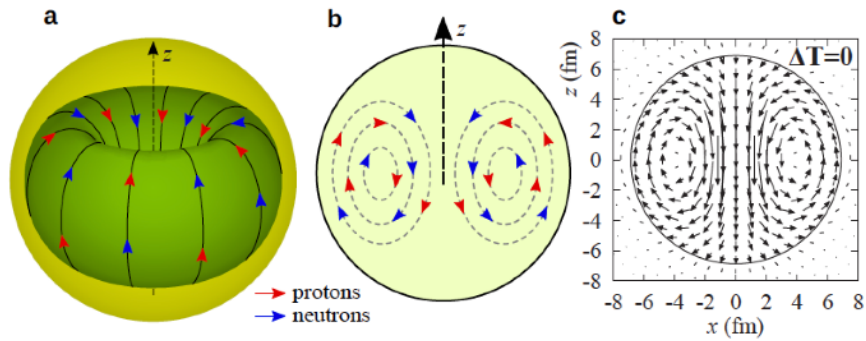
There must be a common reason of the existence.

# Pygmy Dipole Resonance (PDR)



How is the relation to the IS-E1 mode?

How is the relation to the E1 toroidal mode?



( $e, e'$ ) transverse excitation?

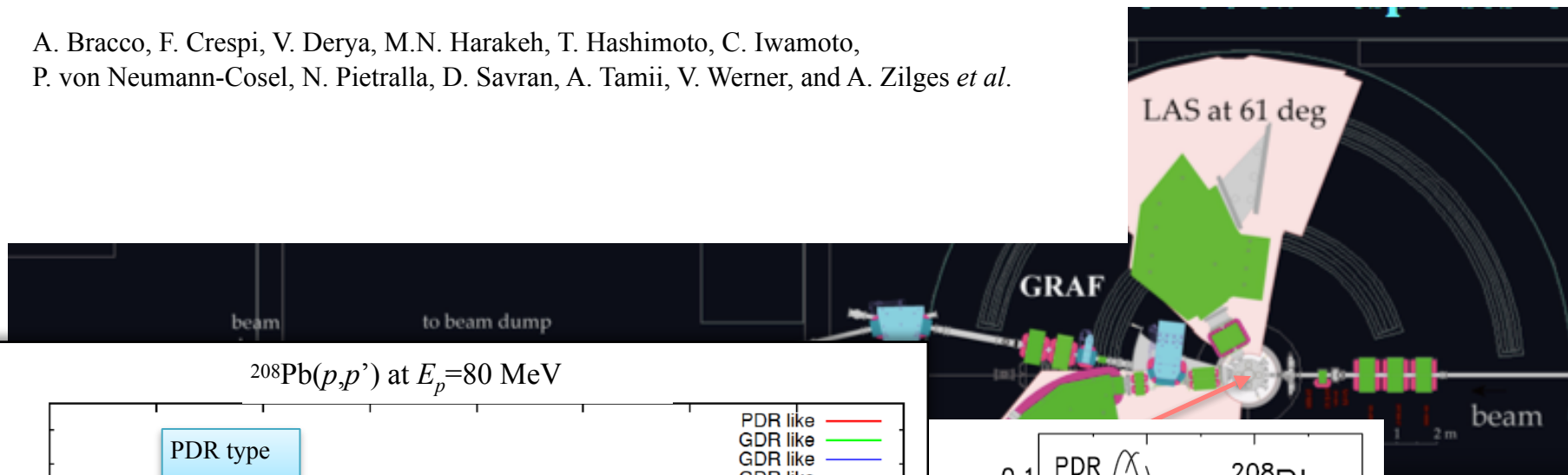
What is the signature of PDR?

PDRの実験的証拠は何か?

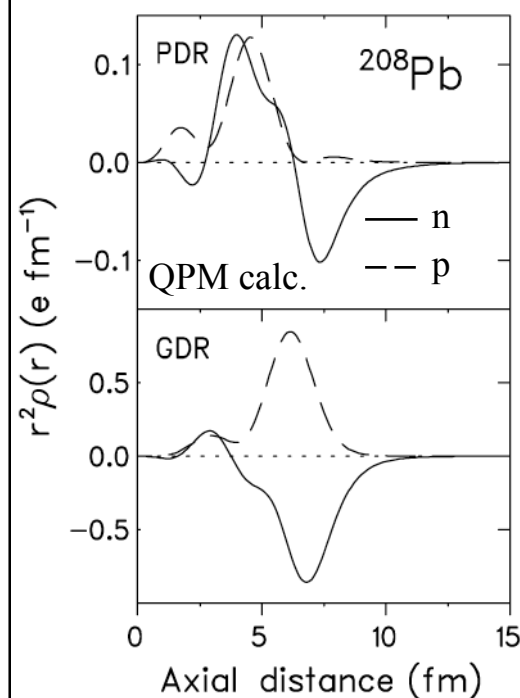
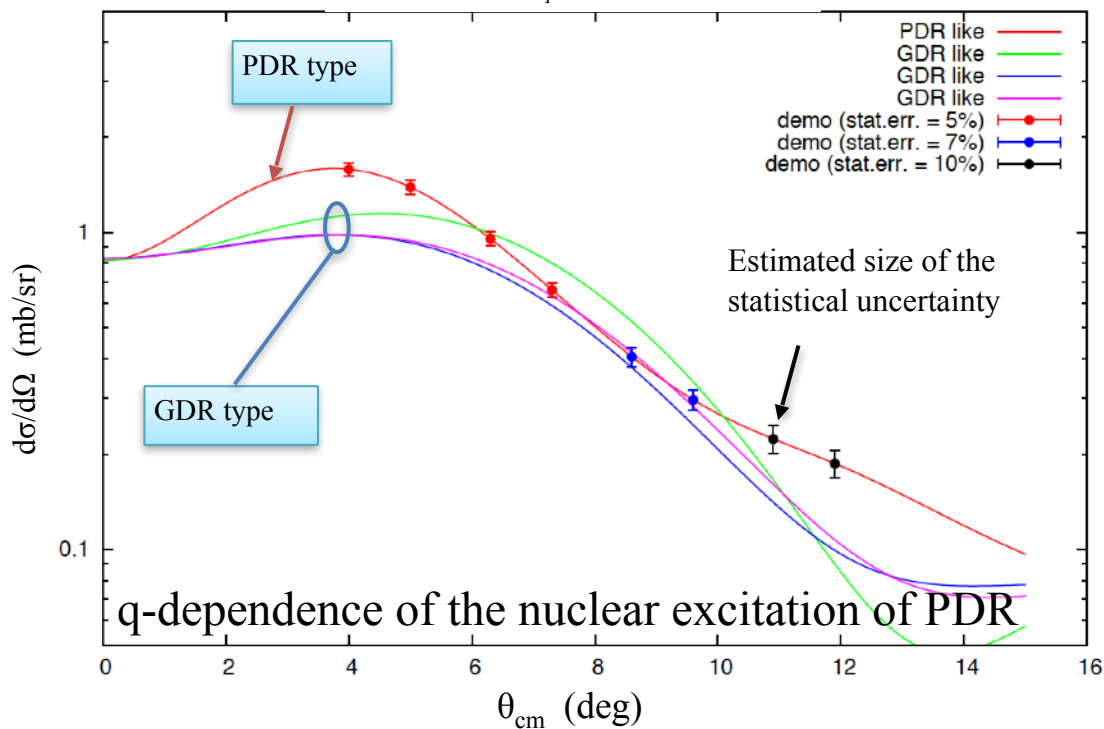
# (p,p $\gamma$ ) in CAGRA+GR Campaign

## Structure of the PDR \*1

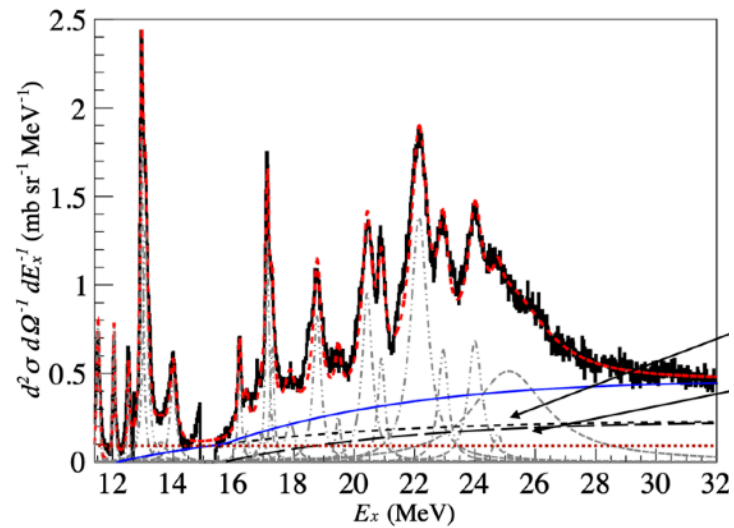
A. Bracco, F. Crespi, V. Derya, M.N. Harakeh, T. Hashimoto, C. Iwamoto,  
P. von Neumann-Cosel, N. Pietralla, D. Savran, A. Tamii, V. Werner, and A. Zilges *et al.*



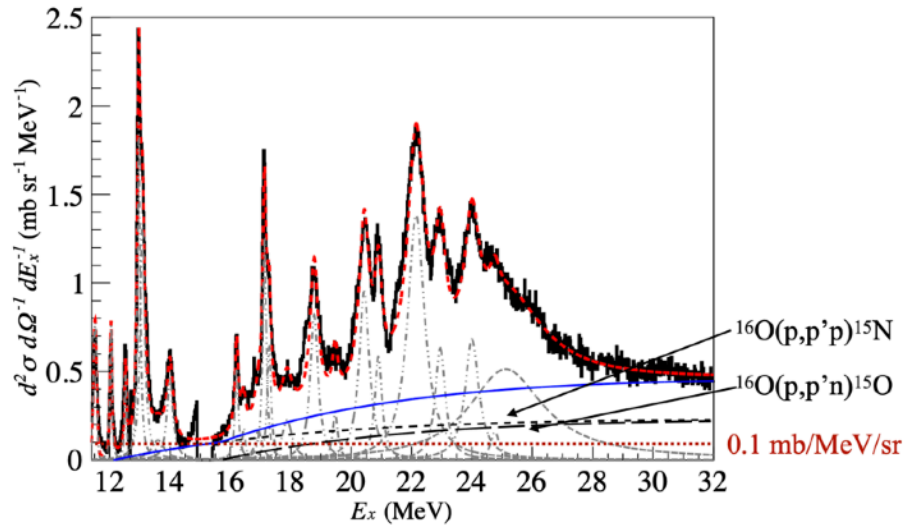
$^{208}\text{Pb}(p,p')$  at  $E_p=80$  MeV



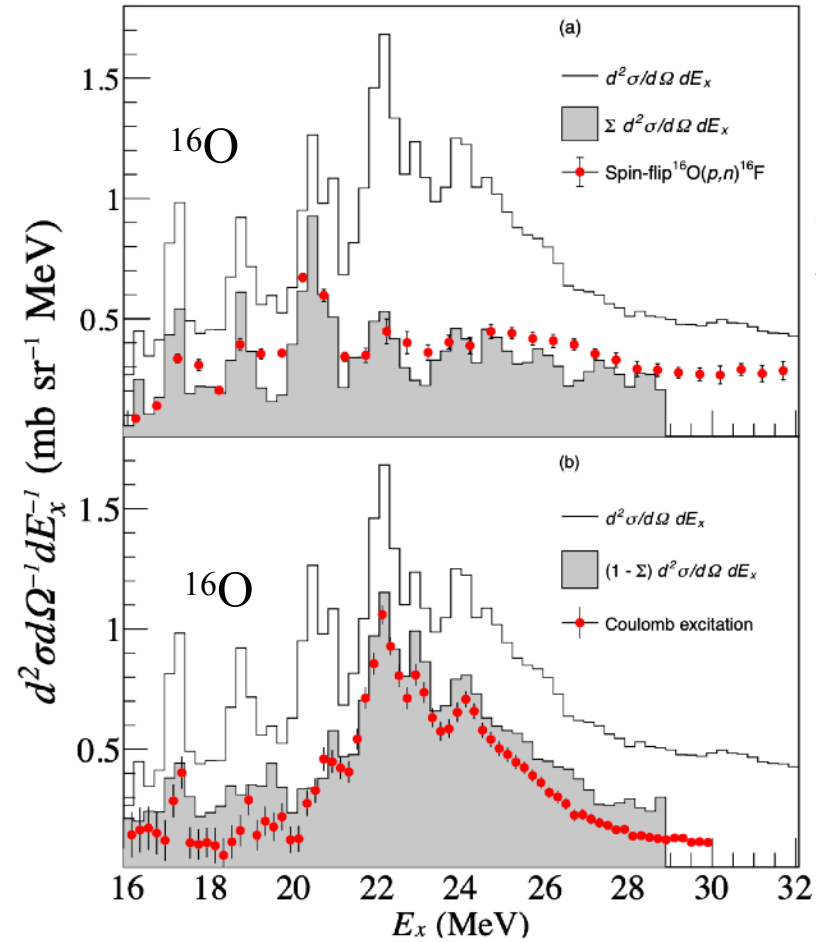
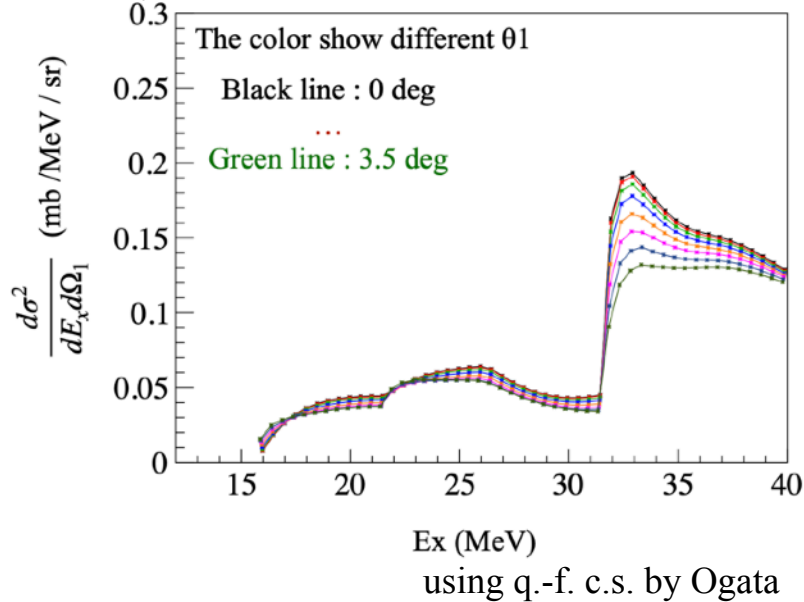
# Quasi-free Scattering at 0-deg



# Quasi-free scattering c.s. at 0-deg



Preliminary



0度準弾性散乱の定量的記述

Sudo et al.,

spin-flip-probability taken from Kawabata et al.,

description of d-like correlation in nuclei would be important for describing quasi-free scattering c.s. at 0-deg?

# Summary

RCNP Grand Raidenでの陽子散乱を使ったこれまでの実験から、理解したいことをピックアップしてお話しました。

- d-like 相関の定量的記述
- 軽核の光核反応の記述: 光吸収+崩壊計算
- quasi-deuteron excitationの理解
- (IS/IV spin-M1)クエンチング機構の理解
- 基底状態の $np$ -spin相関の理解
- 核物質のスピン磁化率の理解
- 巨大共鳴の崩壊の記述
- GDRの微細構造の起源と理解
- 準位密度の定量的・現象論的でない記述
- PDR機構の実験的証拠は何か?
- 0度準弾性散乱の定量的記述

*Thank you for your attention!*