



High-resolution Study of Gamow-Teller Transitions in the $^{46,47,48}\text{Ti}(^3\text{He},t)^{46,47,48}\text{V}$ Reactions

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Outline

- The importance of Gamow-Teller (GT) transitions
- Main features of Gamow-Teller (GT) / Fermi (F) transitions
- Transition probabilities: $B(\text{GT})$, $B(\text{F})$
- Measuring $B(\text{GT})$ s : beta-decay and charge exchange reactions
- High resolution $(^3\text{He}, t)$ experiments at RCNP :
 $^{46,47,48}\text{Ti}(^3\text{He}, t)^{46,47,48}\text{V}$
- Results
- Conclusions

Why are GT transitions important?

Gamow-Teller (GT) transitions are the most common weak interaction processes.

Good Probe to Study some Key questions in Nuclear Structure.

-Because of their simple character

Astrophysical Interest

- At the core collapse stage of type II supernovae, Gamow-Teller (GT) transitions in pf-shell nuclei play an important role *

* K. Langanke et al, Rev. Mod. Phys. **75**, 819 (2003).

The main features of GT transitions

GT transitions are governed by the $\sigma\tau$ operator.

The $\sigma\tau$ operator has no spatial component \rightarrow transitions between states with similar spatial shapes are favoured.

They are of isovector (IV) nature.

Allowed GT transitions $\Delta T = 1$, $\Delta S = 1$ and $\Delta L = 0$, they also have $\Delta J = 1$ and no parity change.

Isospin quantum number T plays an important role:

$T=T_0$ states are connected with T_{0-1} , T_0 and T_{0+1} states

They can be studied either in β decay (weak interaction) or in Charge Exchange (strong interaction) reactions.

The main features of F transitions

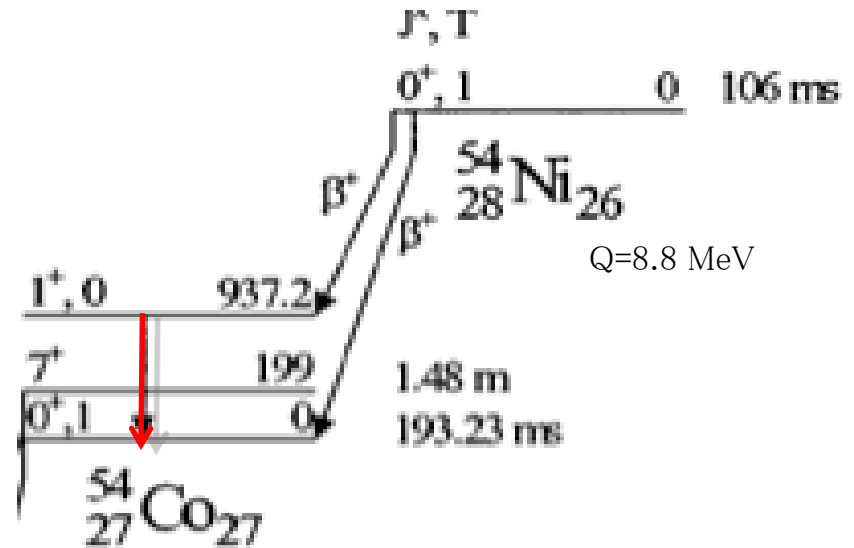
Fermi transitions are due to the τ operator. Hence only a single state (Isobaric Analog State, IAS) is populated in the final nucleus.

They are of isoscalar (IS) nature with $\Delta T = 1$, $\Delta S = 0$ and $\Delta L = 0$, they also have $\Delta J = 0$ and no parity change.

They can be studied either in β decay (weak interaction) or in Charge Exchange (strong interaction) reactions.

Measuring $B(\text{GT})_{\text{s-I}}$

β -decay studies:



The most direct information on $B(\text{GT})$
A weak interaction process,

The accessible excitation energy is limited by the decay Q -value.

Measuring B(GT)s-(II)

Charge-exchange Reactions:

Strong interaction process

GT strengths B(GT) can reliably be mapped up to higher excitations if a “standard B(GT) value” from decay is available.

An approximate proportionality between measured cross sections and

B(GT) values has been established in (p,n) reactions.

at incident beam energies > 100 MeV/u at the scattering angle 0°

$$\frac{d\sigma(0^\circ)_{GT}}{d\Omega} \approx \hat{\sigma}_{GT} \cdot B(GT)$$

*T.N. Taddeucci et. al., NPA469 (1987) 125

E. Ganioglu, IIS T15, Osaka

$(^3\text{He}, t)$ type CE reactions

46Fe	47Fe	48Fe	49Fe	50Fe	51Fe	52Fe	53Fe	54Fe
45Mn	46Mn	47Mn	48Mn	49Mn	50Mn	51Mn	52Mn	53Mn
44Cr	45Cr	46Cr	47Cr	48Cr	49Cr	50Cr	51Cr	52Cr
43V	44V	45V	46V	47V	48V	49V	50V	51V
42Ti	43Ti	44Ti	45Ti	46Ti	47Ti	48Ti	49Ti	50Ti
41Sc	42Sc	43Sc	44Sc	45Sc	46Sc	47Sc	48Sc	49Sc
40Ca	41Ca	42Ca	43Ca	44Ca	45Ca	46Ca	47Ca	48Ca
39K	40K	41K	42K	43K	44K	45K	46K	47K

$^{46}\text{Ti} \rightarrow 0.92 \text{ mg/cm}^2$

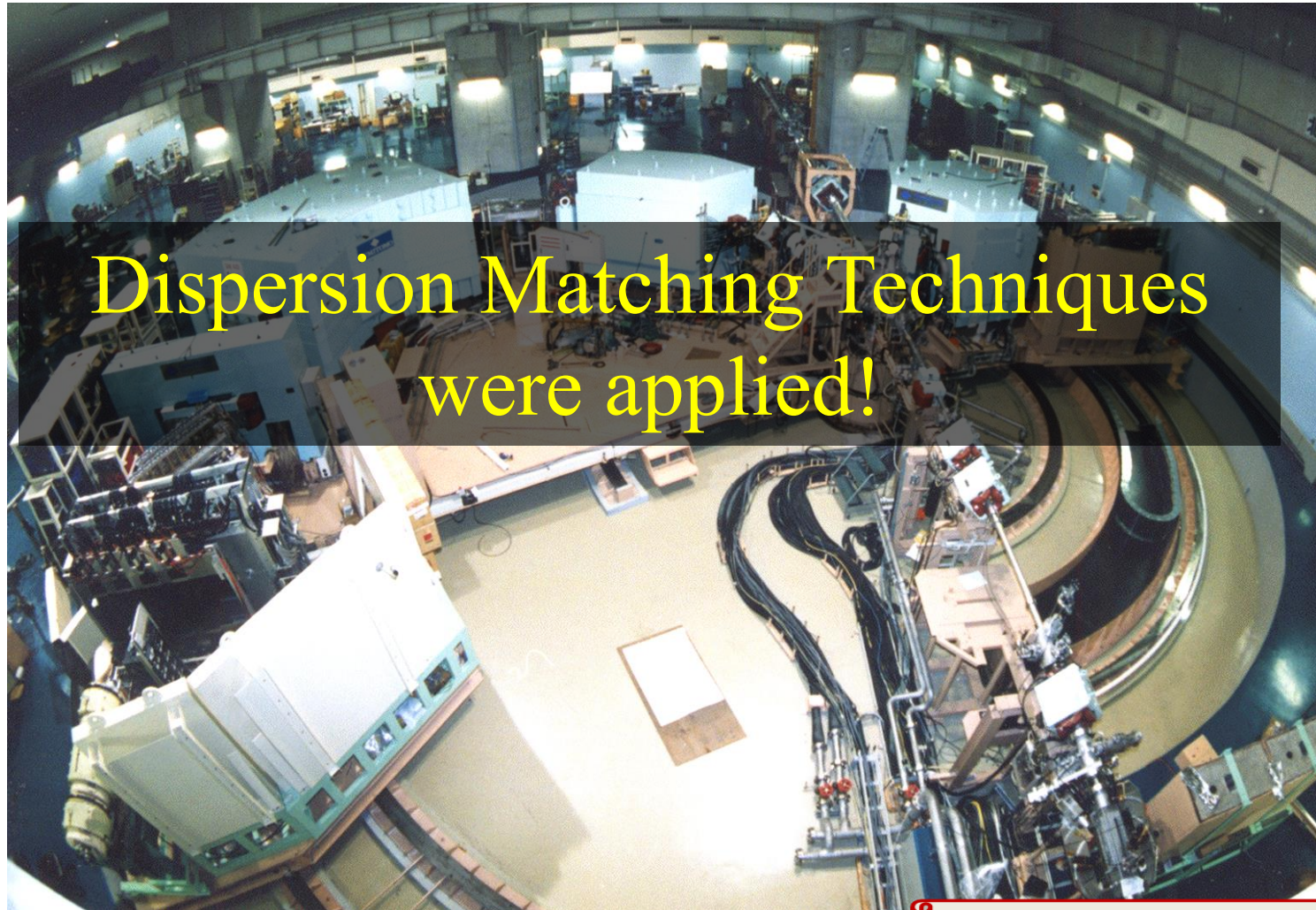
$^{47}\text{Ti} \rightarrow 0.85 \text{ mg/cm}^2$

$^{48}\text{Ti} \rightarrow 0.50 \text{ mg/cm}^2$

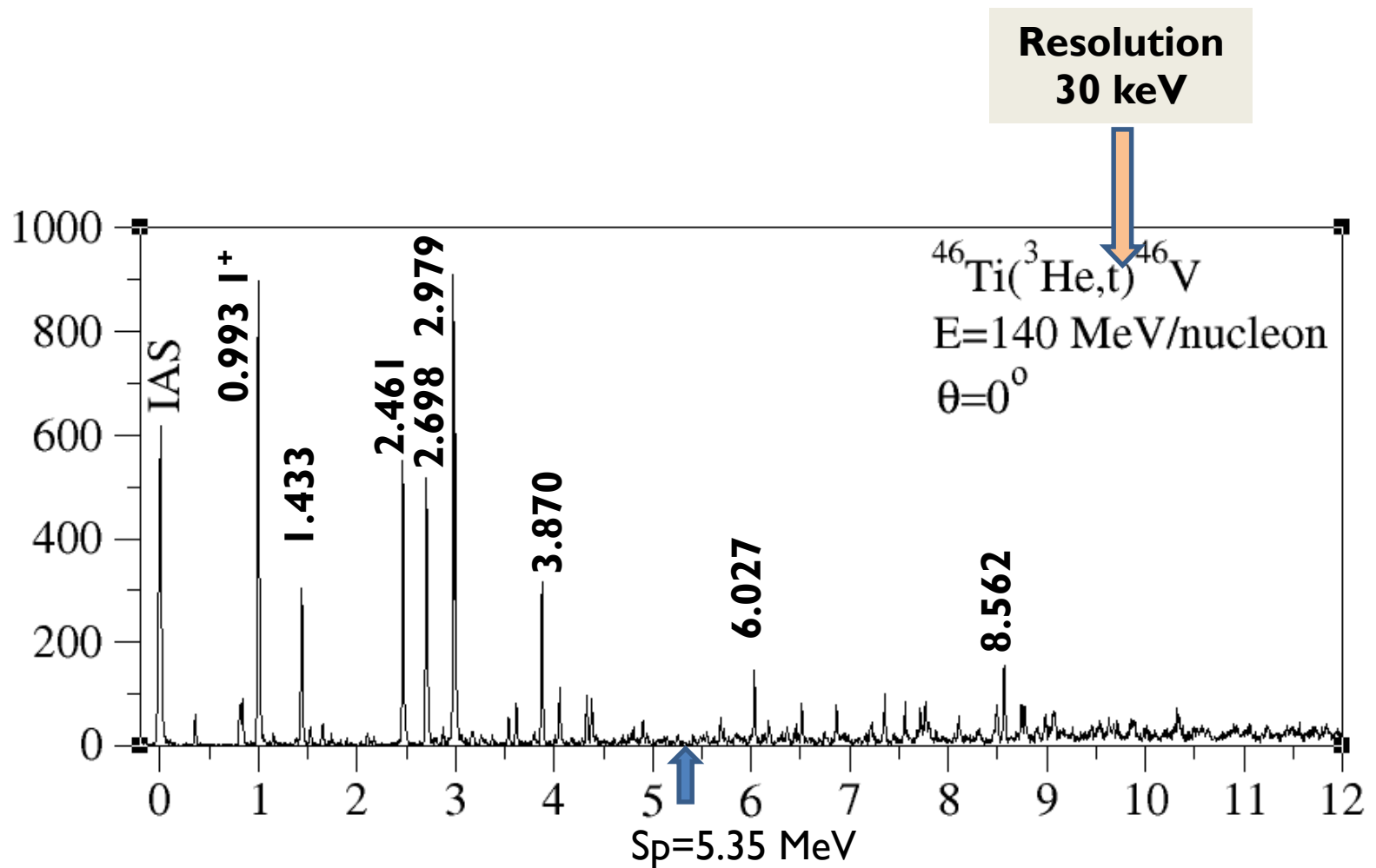
@ 140 MeV/n

$N=Z$

Research Center for Nuclear Physics (RCNP)

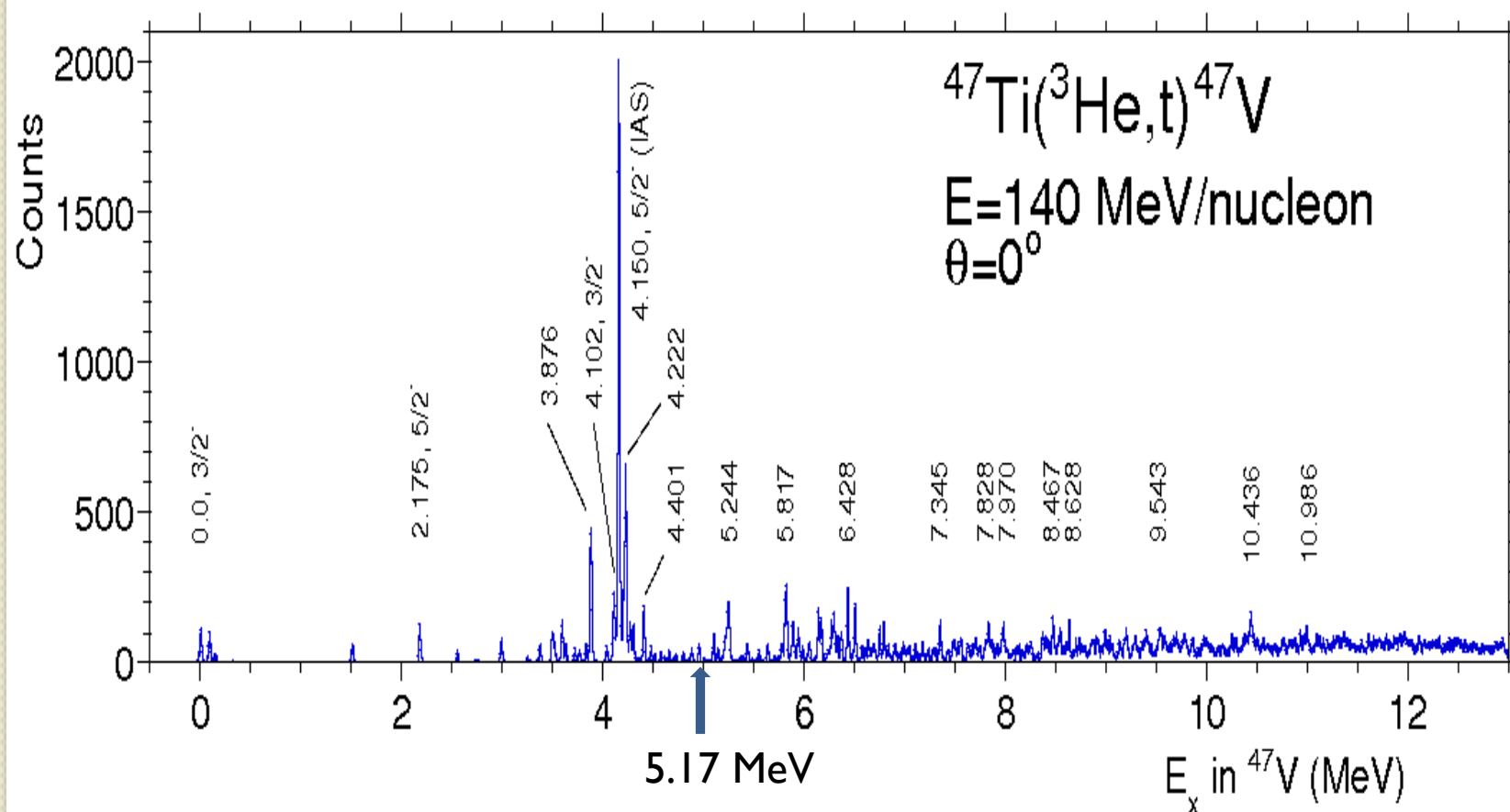


T. Wakasa et al., NIM A482 ('02) 79.



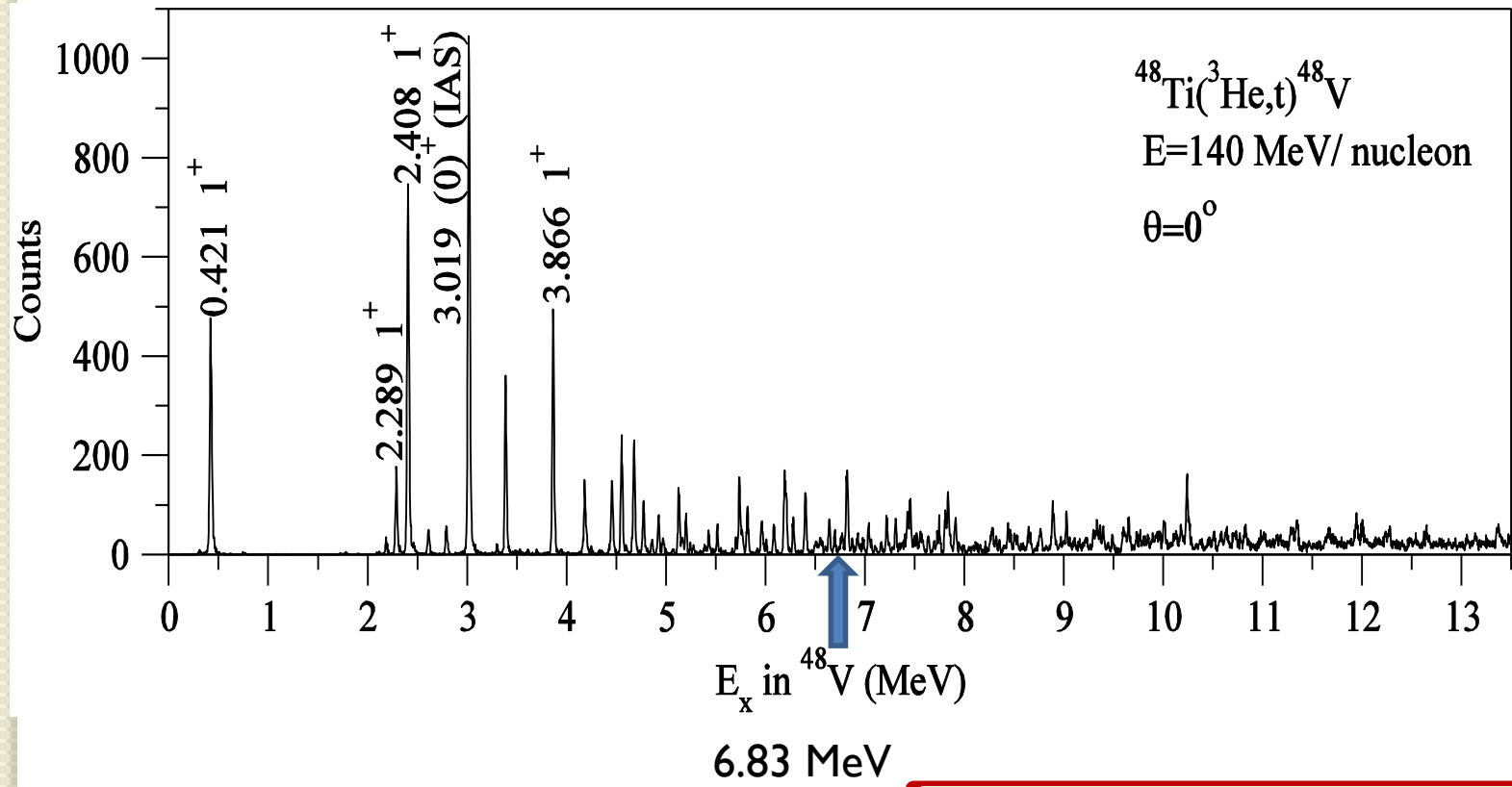
- Adachi T. et. al., Physical Review C 73, 02431 (2006). (Up to 6 MeV)
- Dogan M. et al., MSc Thesis, Istanbul University, 2014, publication – in preparation

**Resolution
20 keV**



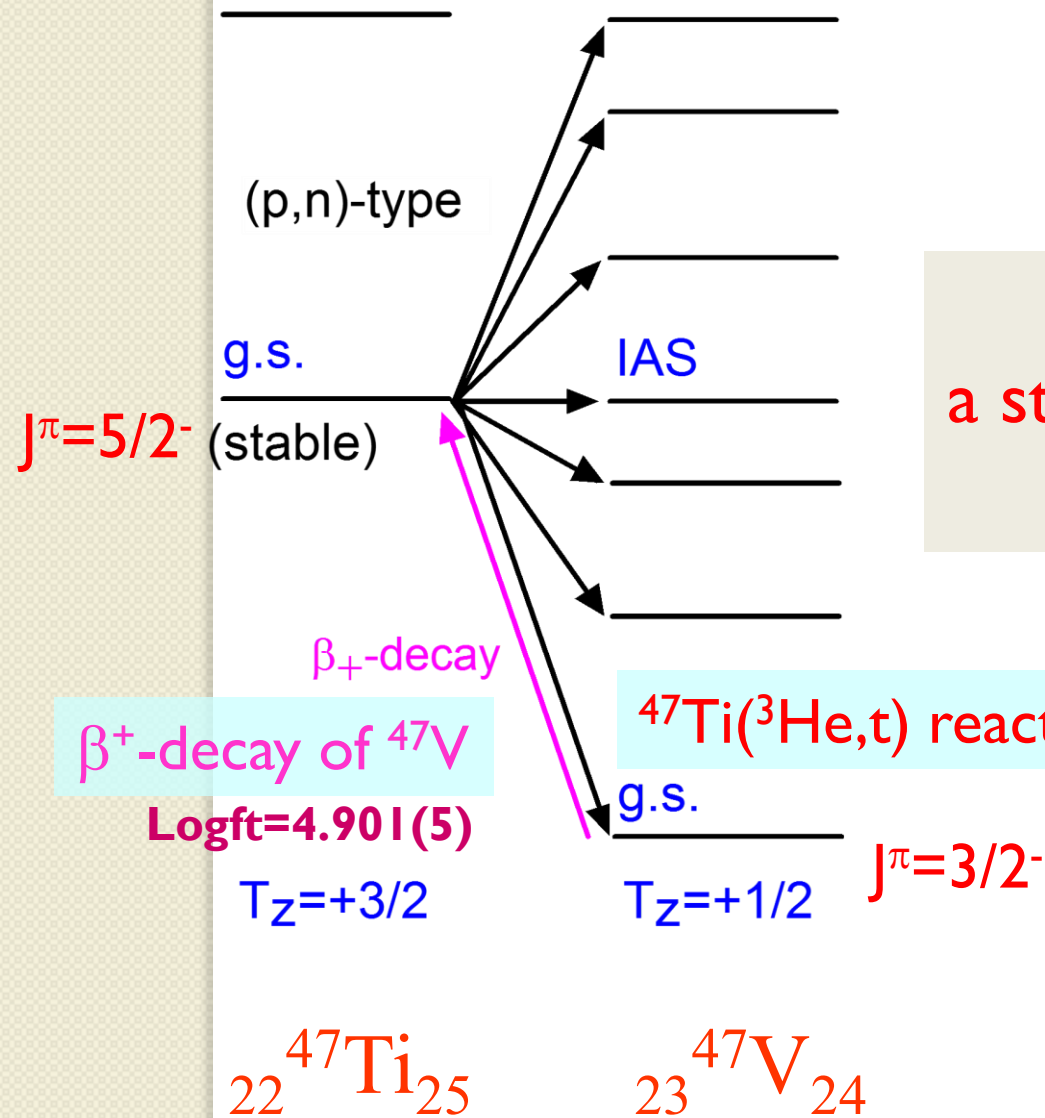
E. Ganioglu et al., Phy. Rev. C 87, 014321 (2013)

**Resolution
21 keV**



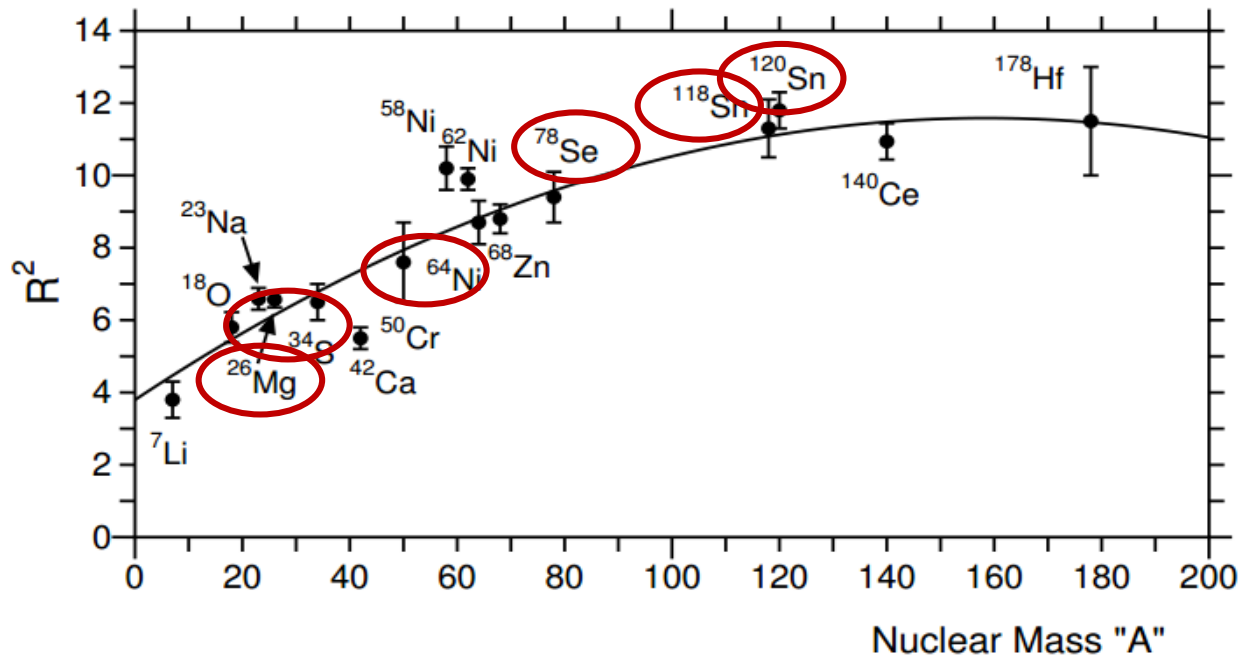
E. Ganioglu et al., in preparation

Deriving B(GT)s I:



In the $A=47$ system,
a standard B(GT) is obtained
from β -decay of ^{47}V

Deriving B(GT)s II: Nuclear Mass Dependence of R2



R^2 for $^{46}\text{V} =$

7.7 ± 0.9

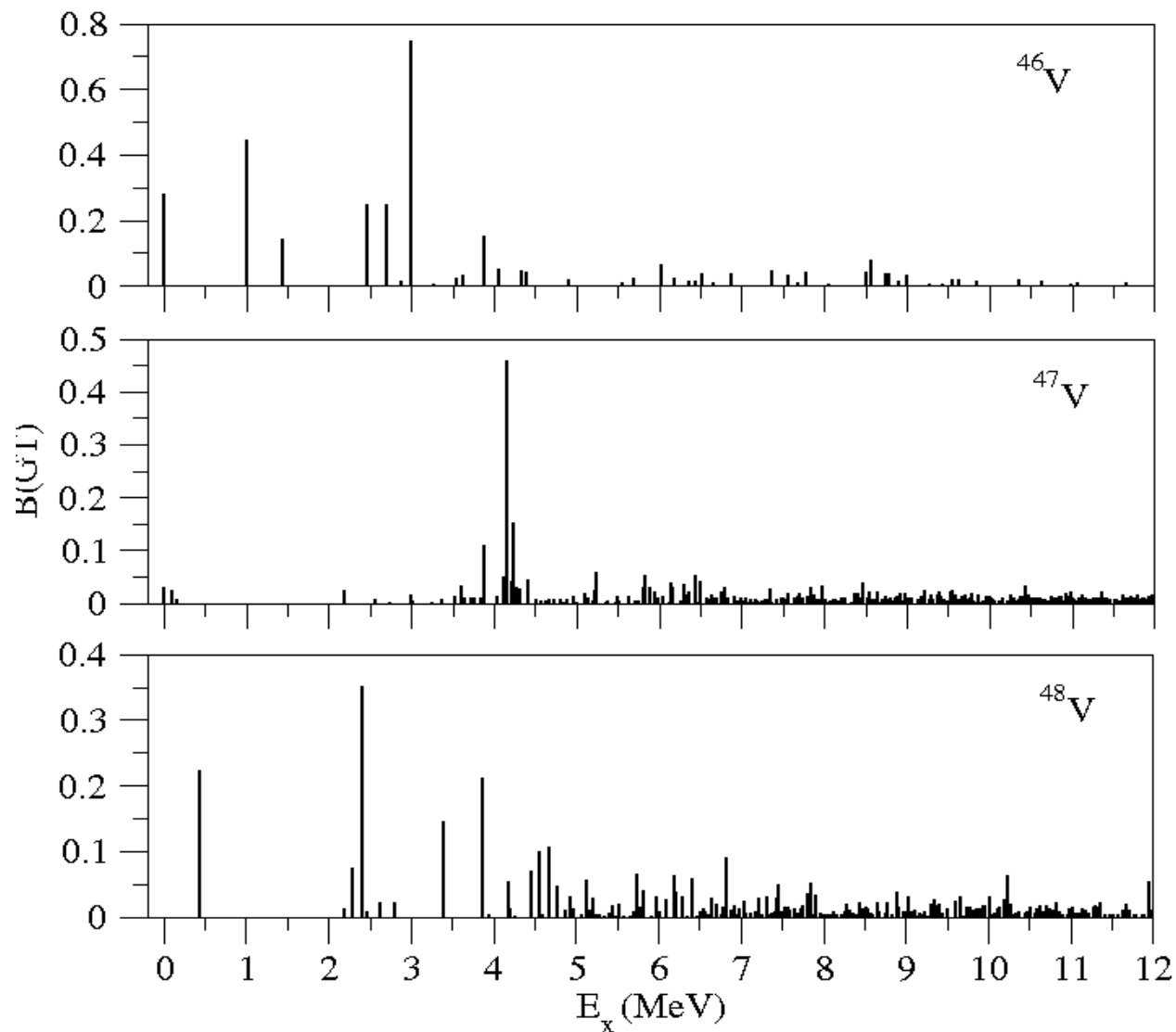
R^2 for $^{48}\text{V} =$

8.2 ± 0.4

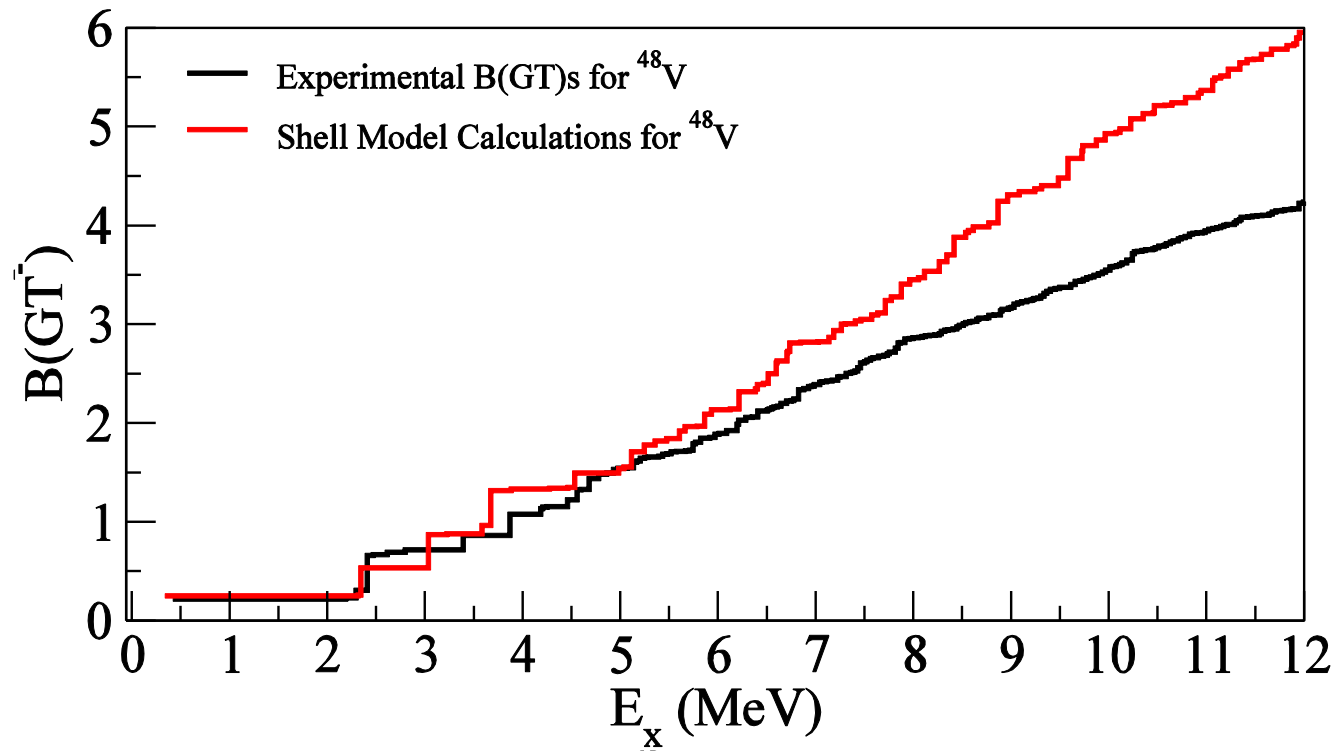
$$R^2 = \frac{\hat{\sigma}_{\text{GT}}(0^\circ)}{\hat{\sigma}_{\text{F}}(0^\circ)} = \frac{\sigma_{\text{GT}}(0^\circ)}{B(\text{GT})} / \frac{\sigma_{\text{F}}(0^\circ)}{B(\text{F})}$$

T. Adachi et al., Nucl. Phys. A 788 (2007) 70c,
and H. Fujita, Y. Fujita, private communication

B(GT) Distributions



Cumulative Sum of B(GT)



SM calculations by M. Honma,
Aizu Un, Japan

B(M1) [γ -transitions in ^{47}V] v.s. B(GT)

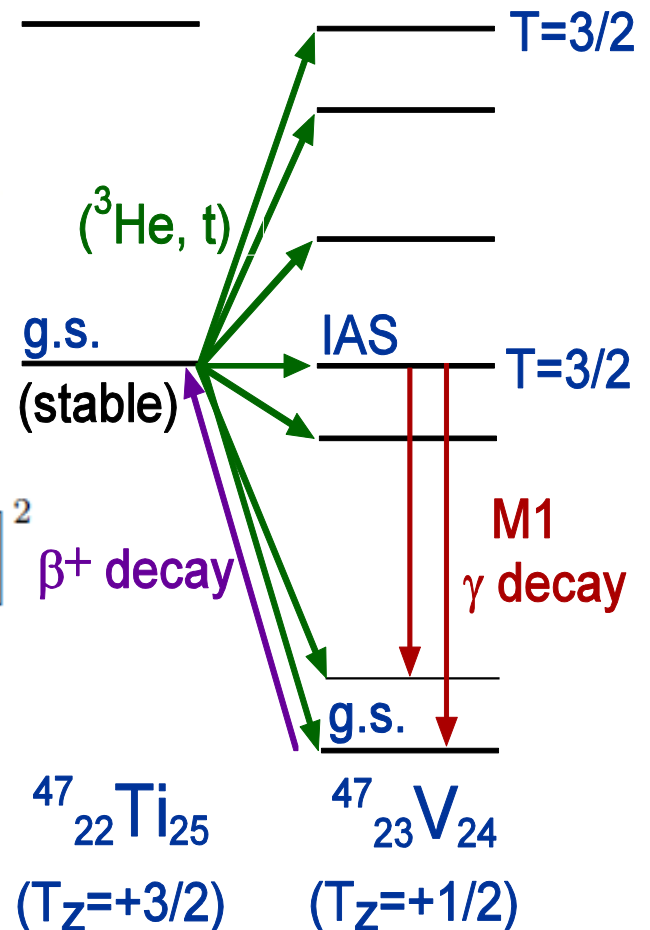
$$B(\text{GT}) = \frac{1}{(2J_i + 1)} \frac{1}{2} \frac{C_{\text{GT}}^2}{(2T_f + 1)} [M_{\text{GT}}(\sigma\tau)]^2$$

$$B(M1) = \frac{1}{(2J_i + 1)} \frac{3}{4\pi} \mu_N^2 \frac{C_{M1}^2}{(2T_f + 1)} \times \left[g_\ell^{\text{IV}} M_{M1}(\ell\tau) + g_s^{\text{IV}} \frac{1}{2} M_{M1}(\sigma\tau) \right]^2$$

β^+ decay

Under the assumption that the E2/M1 mixing ratios are small :

$$B(M1) \propto \frac{1}{E_\gamma^3} I_\gamma$$



Comparison of analogous B(M1) and B(GT)

States in ^{47}V		g transitions in ^{47}V		GT transitions to ^{47}V
Ex (MeV)	J^π	Eg (MeV)	B(M1) ratio	B(GT) ratio
0.0	$3/2^-$	4.150	1.00(2)	1.00(1)
0.0088	$5/2^-$	4.063	0.79(3)	0.81(13)
0.146	$7/2^-$	4.004	0.29(2)	0.22(6)

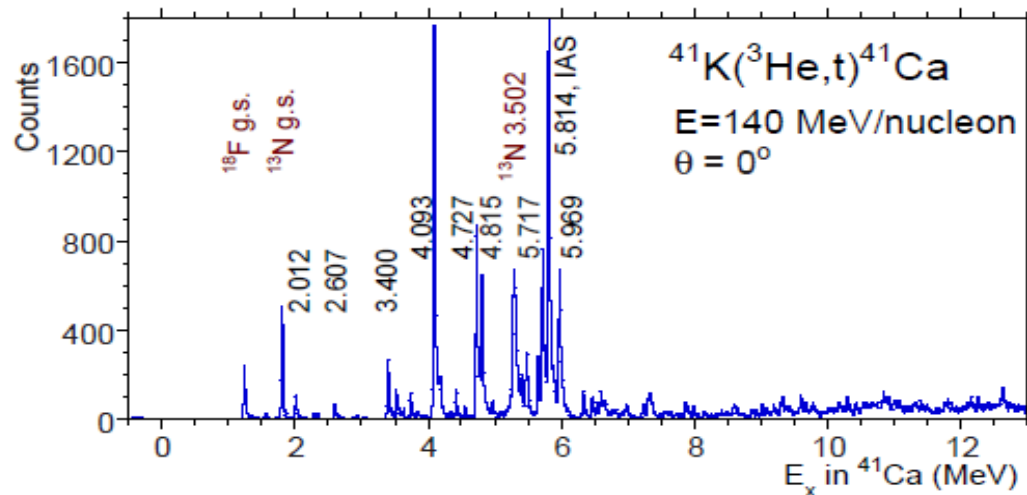
!Strongest M1 and GT strengths to the g.s of ^{47}V are normalized to unity!

*T.W. Burrows, Nuclear Data Sheets, **108, 923 (2007)**

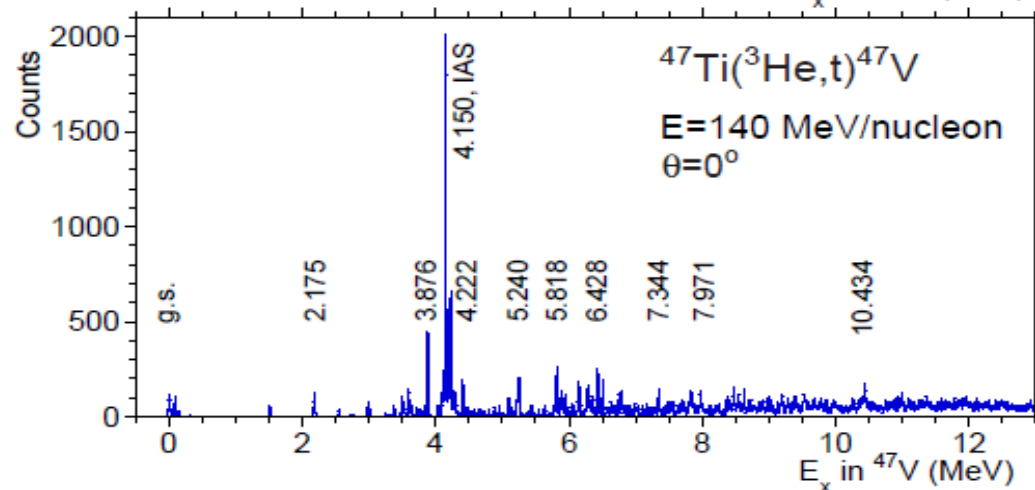
Tz=+3/2 to Tz=+1/2 GT transitions

$$\nu f_{7/2} \rightarrow \pi f_{7/2}$$

$$\nu f_{7/2} \rightarrow \pi f_{5/2}$$

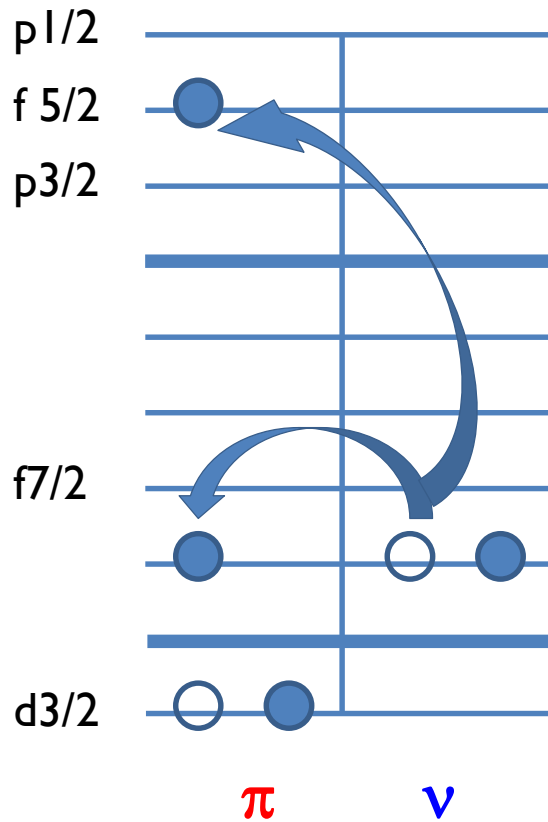


p-p character !
States lie at
relatively low
excitation energy.



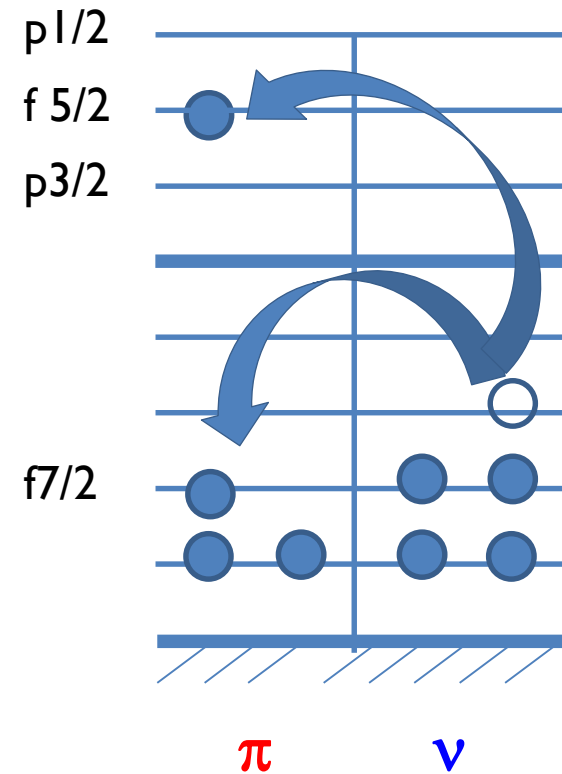
p-h character !
States are pushed up
in excitation energy.

$41\text{K} \rightarrow 41\text{Ca}$



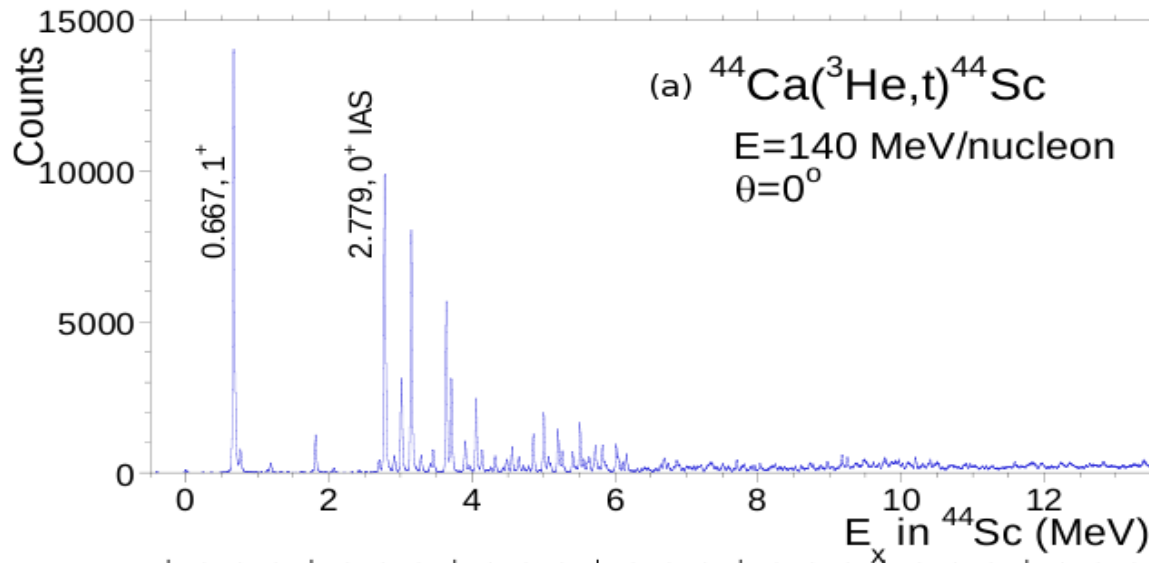
**p- p character
attractive**

$47\text{Ti} \rightarrow 47\text{V}$

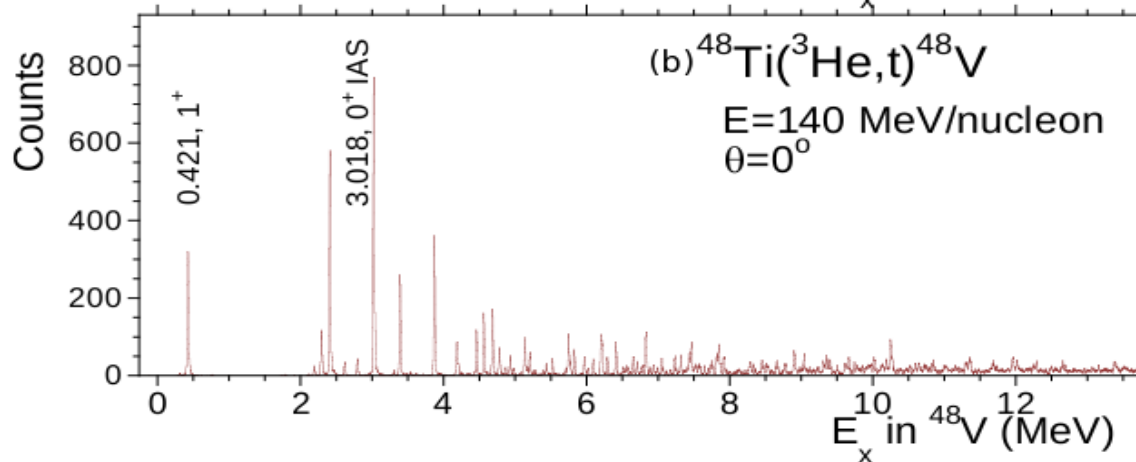


**p- h character
repulsive**

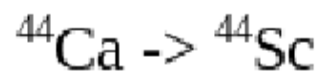
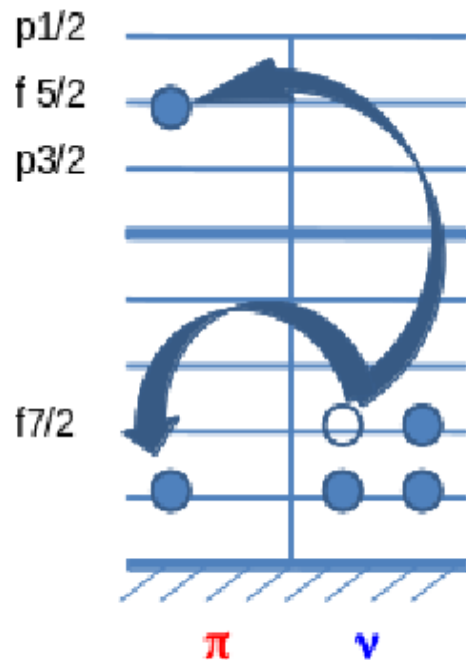
$T_z=+2$ to $T_z=+1$ GT transitions



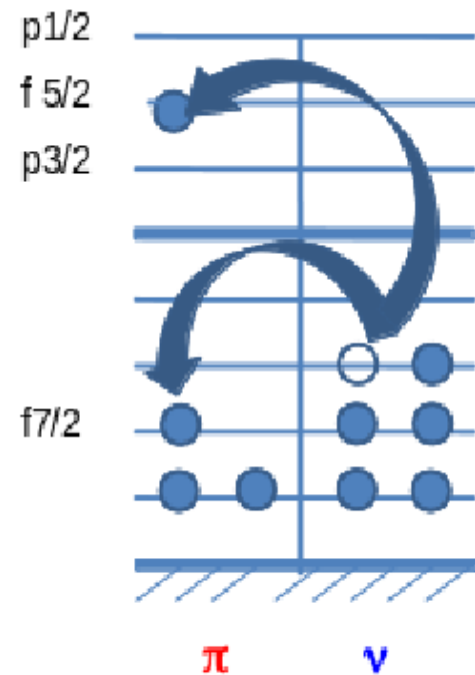
p-p character !
States lie at relatively low excitation energy.



p-h character !
States are pushed up in excitation energy.

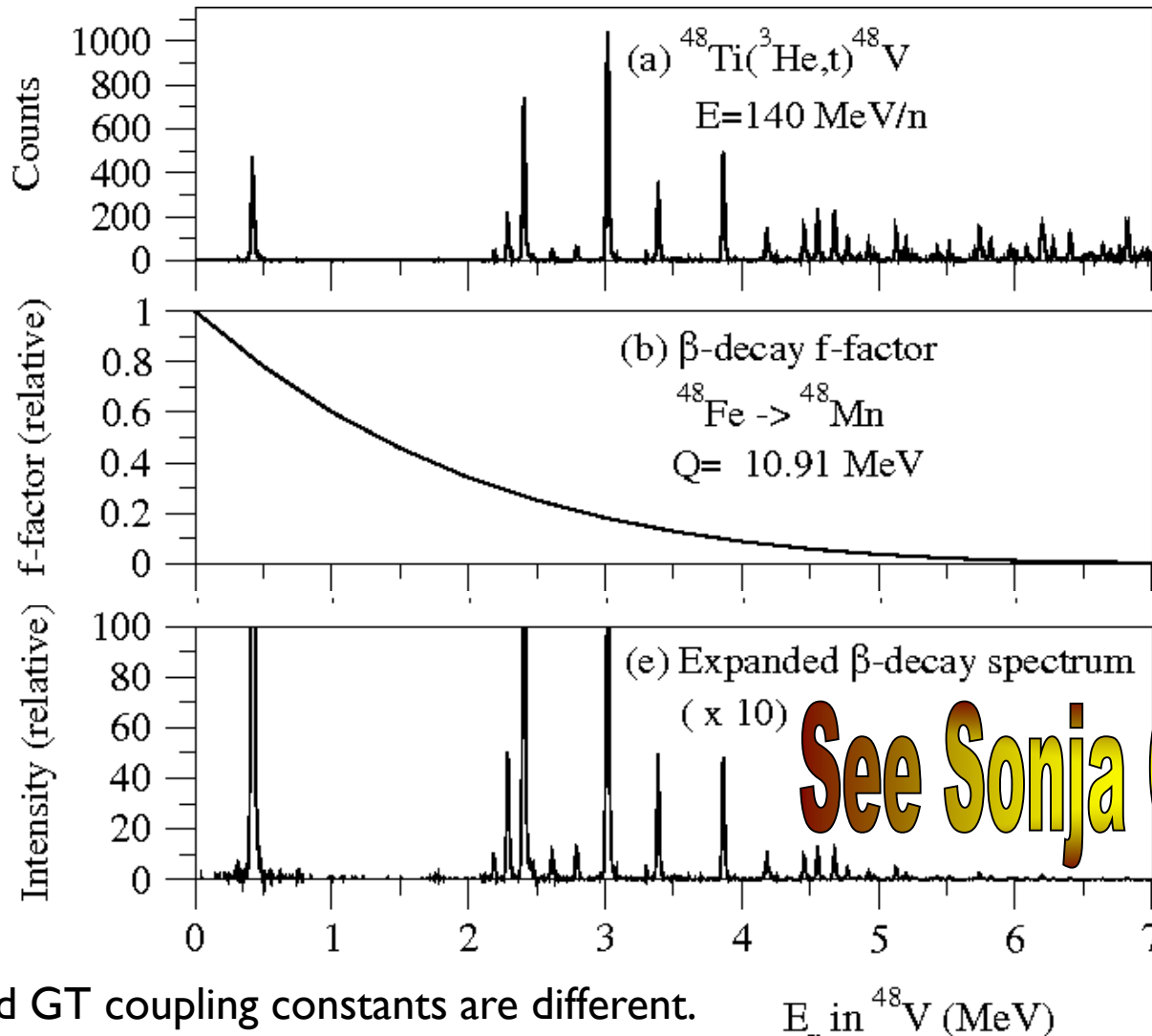


**p- p character
attractive**



**p- h character
repulsive**

Mirror Beta-decay



isospin symmetry
 assumption

$T_z = \pm 2 \rightarrow \pm 1$

See Sonja Orrigo's talk

! F and GT coupling constants are different.

$E_x \text{ in } {}^{48}\text{V} \text{ (MeV)}$

Conclusion

- In this work the studies of the ($^3\text{He}, t$) reaction on $T_z = 1/2$ and 1 , have been extended to the $T_z = +3/2$ and $T_z = +2$ nuclei and excitation energies of previously known states were reproduced to 5 keV up to 12 MeV.
- Relative intensities of the analogous M1 and GT transitions in the $A=47$ system are in good agreement.
- Shell model calculations were performed using the GXPF1 interaction. The experimental $B(\text{GT})$ distribution was well reproduced up to 5 MeV.

•A comparison was made of the $T_z = 3/2 \rightarrow 1/2$ GT transitions for ^{41}K and ^{47}Ti nuclei and $T_z = 2 \rightarrow 1$ GT transitions for ^{44}Ca and ^{48}Ti nuclei. In the ^{41}K , $^{44}\text{Ca} (^3\text{He}, t)^{41}\text{Ca}, ^{44}\text{Sc}$ spectrum, the GT strengths are concentrated in the region between 4-6 MeV, while in the $^{47}\text{Ti} (^3\text{He}, t)^{47}\text{V}$ spectrum, they are spread out in energy.

•A comparison was made of the $T_z = 2 \rightarrow 1$ GT transitions for ^{44}Ca and ^{48}Ti nuclei. In the $^{44}\text{Ca} (^3\text{He}, t)^{44}\text{Sc}$ spectrum, the GT strengths are concentrated in the region between 2-6 MeV, while in the $^{48}\text{Ti} (^3\text{He}, t)^{48}\text{V}$ spectrum, they are spread out in energy.

• $(^3\text{He}, t)$ type reactions with the other stable Ti targets ($^{49,50}\text{Ti}$) are being analysed.

$N=Z$

46Fe	47Fe	48Fe	49Fe	50Fe	51Fe	52Fe	53Fe	54Fe
45Mn	46Mn	47Mn	48Mn	49Mn	50Mn	51Mn	52Mn	53Mn
44Cr	45Cr	46Cr	47Cr	48Cr	49Cr	50Cr	51Cr	52Cr
43V	44V	45V	46V	47V	48V	49V	50V	51V
42Ti	43Ti	44Ti	45Ti	46Ti	47Ti	48Ti	49Ti	50Ti
41Sc	42Sc	43Sc	44Sc	45Sc	46Sc	47Sc	48Sc	49Sc
40Ca	41Ca	42Ca	43Ca	44Ca	45Ca	46Ca	47Ca	48Ca
39K	40K	41K	42K	43K	44K	45K	46K	47K

Collaborators

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