

# Fine Structure of Giant Resonances

## – What Can Be Learned



TECHNISCHE  
UNIVERSITÄT  
DARMSTADT



*Peter von Neumann-Cosel*  
*Institut für Kernphysik, Technische Universität Darmstadt*



iThemba  
LABS  
Laboratory for Accelerator  
Based Sciences



- Experimental evidence for fine structure
- Characteristic scales and decay modes of giant resonances
- K splitting of the ISGQR
- Level densities

# High-Resolution Measurements



TECHNISCHE  
UNIVERSITÄT  
DARMSTADT

QCLAM spectrometer  
S-DALINAC  
Darmstadt, Germany



vNC

K600 spectrometer  
iThemba LABS  
Cape Town, South Africa



Smit, Usman

Grand Raiden spectrometer  
RCNP  
Osaka, Japan



Frekers, H. Fujita, Y. Fujita,  
Matsubara, Tamii, ...

Techniques of high-resolution measurements → talk by **Georg Berg**



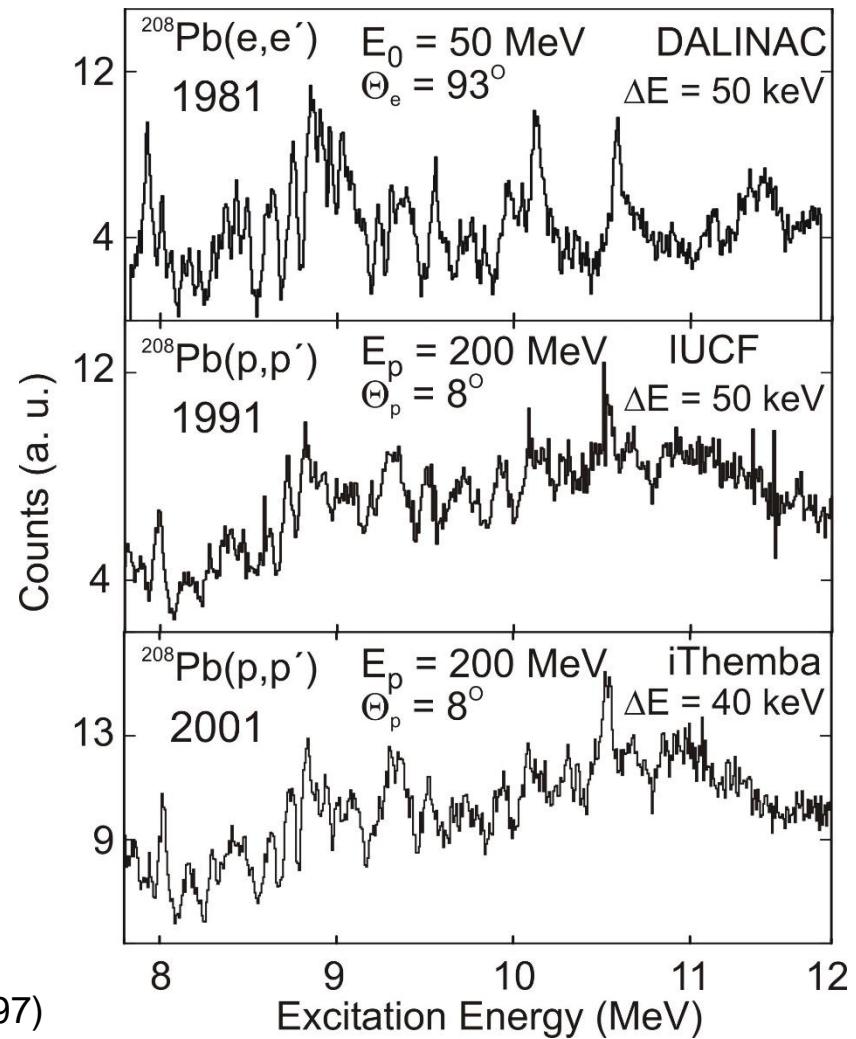
# Fine structure of giant resonances: Experimental evidence

# The Case of the ISGQR in $^{208}\text{Pb}$

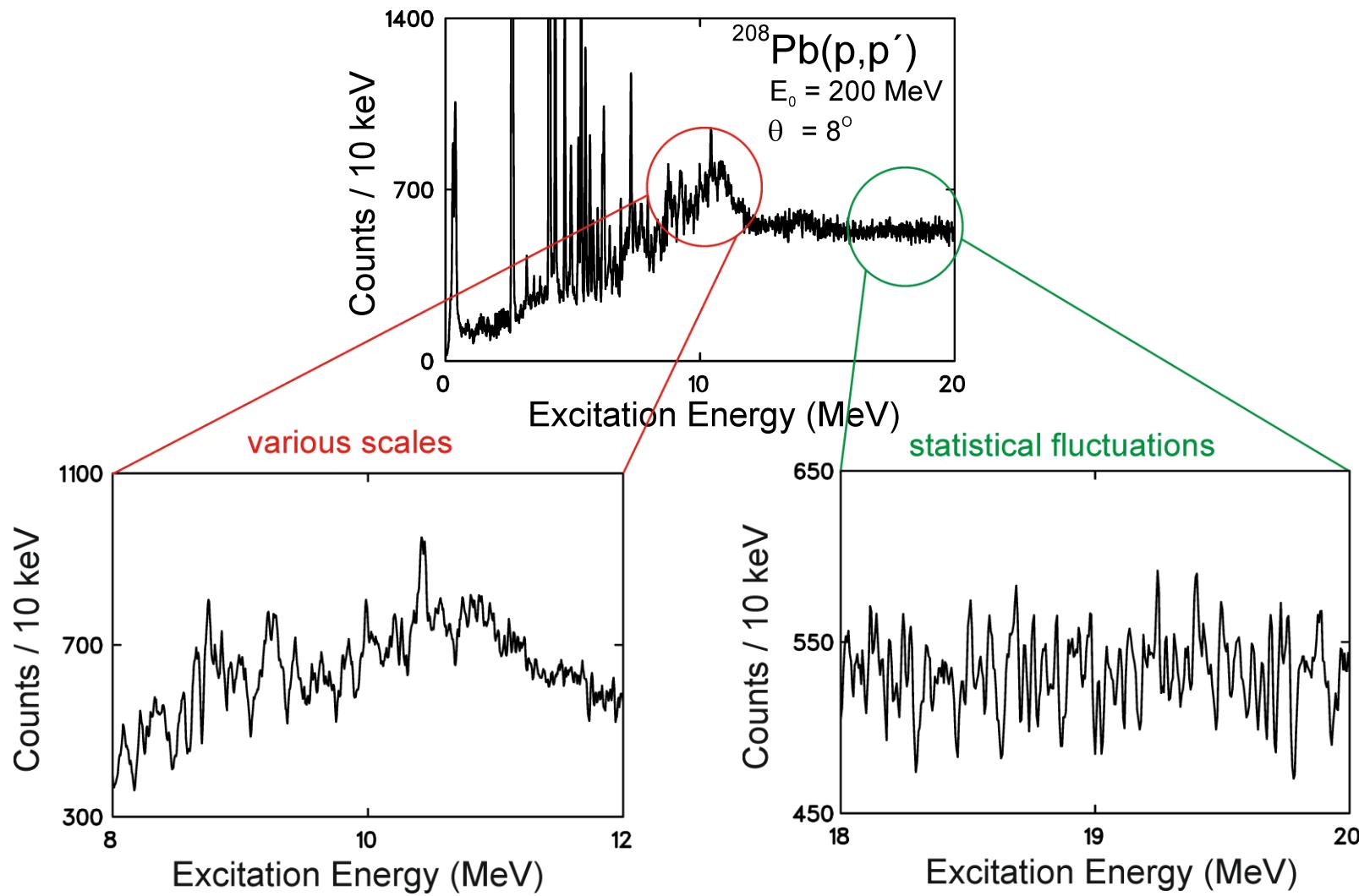


TECHNISCHE  
UNIVERSITÄT  
DARMSTADT

- Fine structure independent of exciting probe



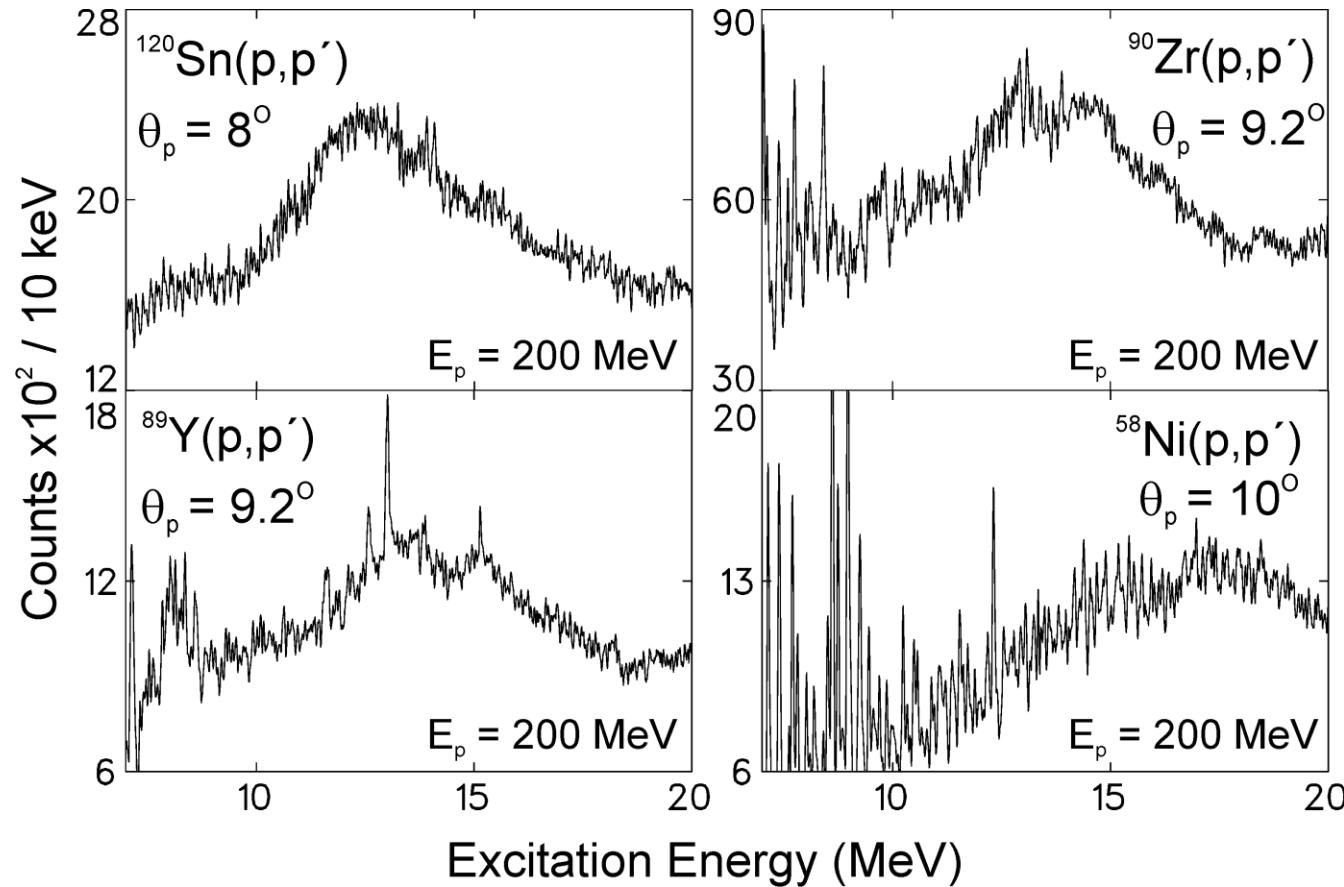
# Scales and Fluctuations



# Fine Structure of the ISGQR – a Systematic Phenomenon



TECHNISCHE  
UNIVERSITÄT  
DARMSTADT

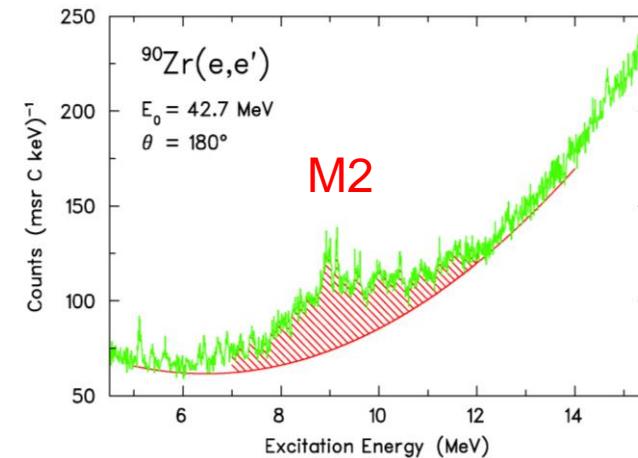
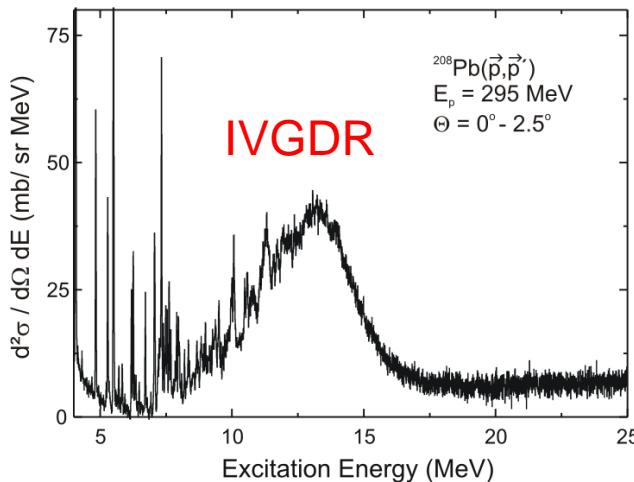


A. Shevchenko et al., Phys. Rev. C 79, 044305 (2009)

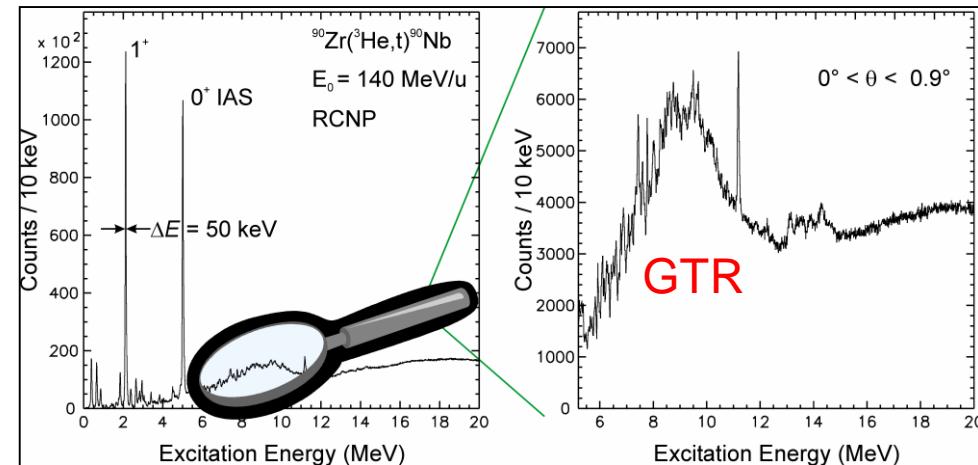
# Fine Structure of GRs – a Global Phenomenon



TECHNISCHE  
UNIVERSITÄT  
DARMSTADT



I. Poltoratska et al., Phys. Rev. C 89, 054322 (2014) PvNC et al., Phys. Rev. Lett. 82, 1105 (1999)



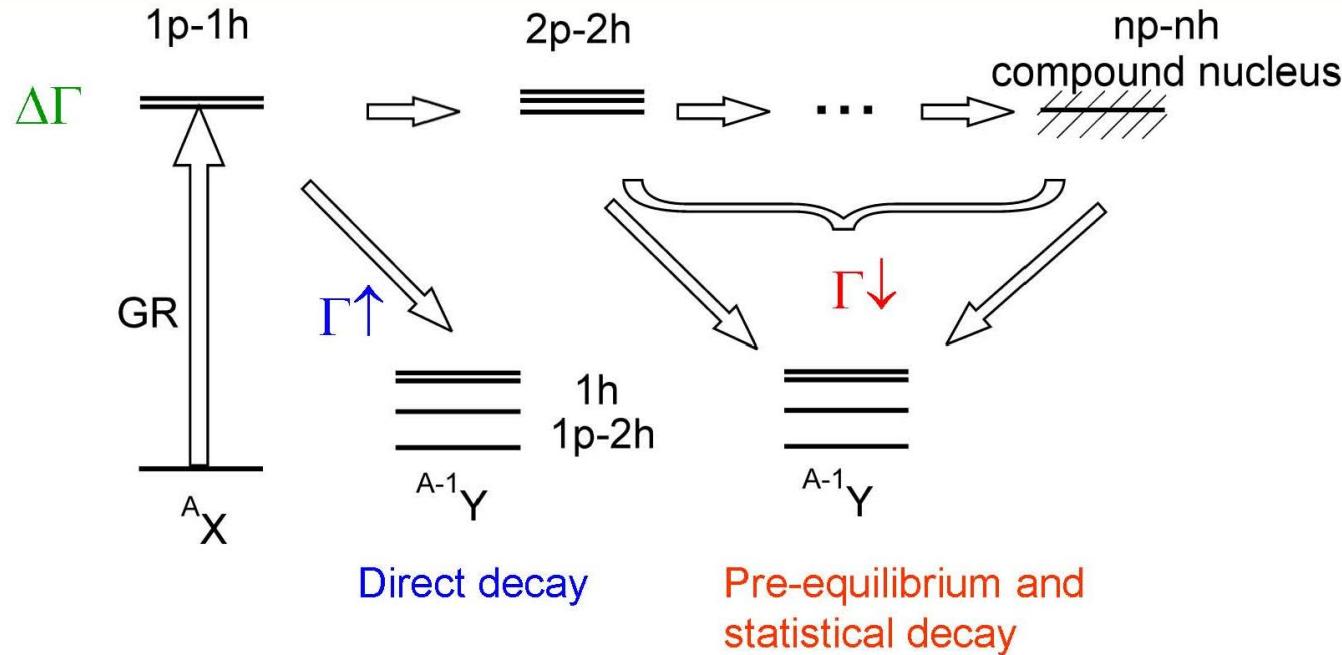
Y. Kalmykov et al.,  
Phys. Rev. Lett. 96, 012502 (2006)



## Characteristic scales:

A quantitative measure of fine structure

# Excitation and Decay of Giant Resonances



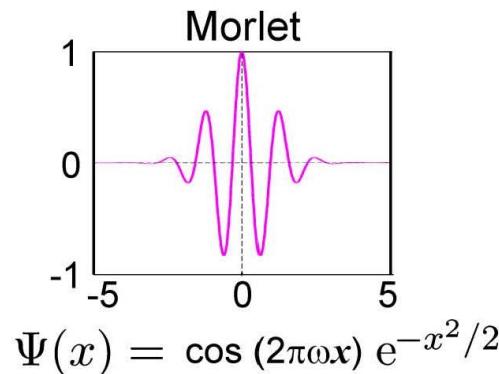
$$\Gamma = \Delta\Gamma + \Gamma \uparrow + \Gamma \downarrow$$

Resonance width      Landau damping      Escape width      Spreading width

# Wavelet Analysis



$$\int_{-\infty}^{\infty} \Psi^*(x) dx = 0 \quad \text{and} \quad \int_{-\infty}^{\infty} |\Psi^*(x)|^2 dx < \infty$$



Wavelet coefficients:

$$C(\delta E, E_x) = \frac{1}{\sqrt{\delta E}} \int \sigma(E) \Psi^*\left(\frac{E_x - E}{\delta E}\right) dE$$

↑      ↑      ↑      ↑  
scale    position    spectrum    wavelet

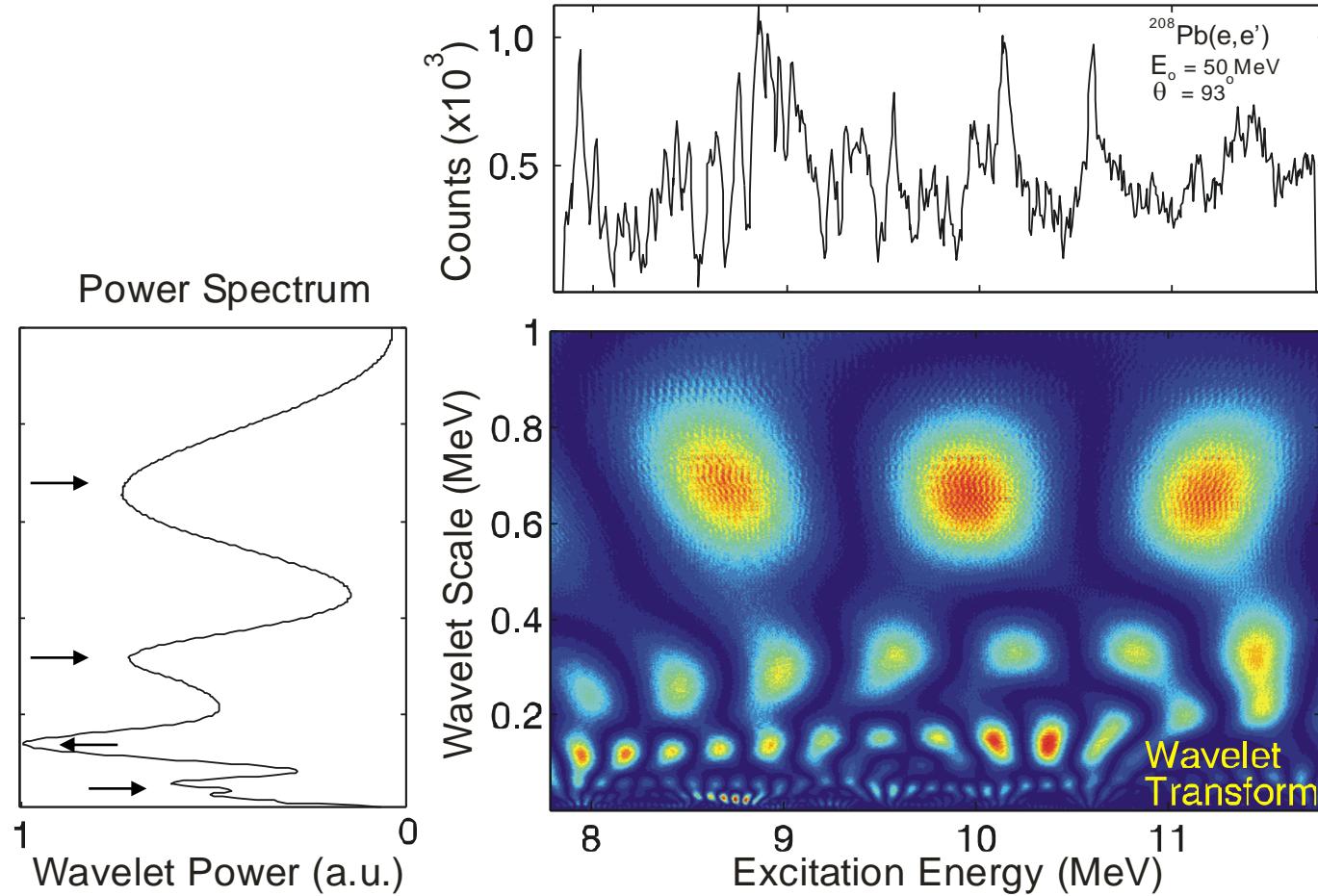
Continuous:  $\delta E, E_x$  are varied continuously

A. Shevchenko et al., Phys. Rev. C77, 024302 (2008)

# ISGQR in $^{208}\text{Pb}$ from $(e,e')$



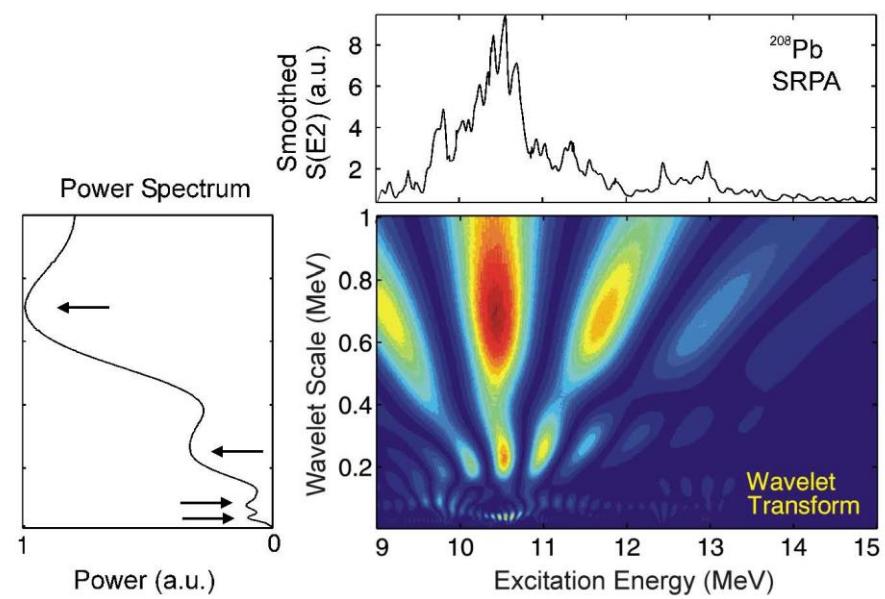
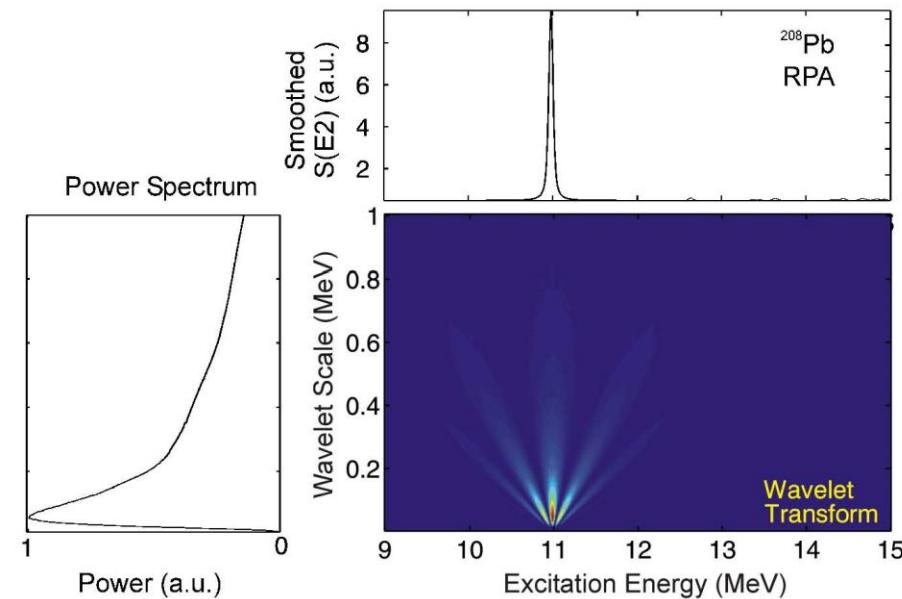
TECHNISCHE  
UNIVERSITÄT  
DARMSTADT



# (S)RPA Model Calculations



TECHNISCHE  
UNIVERSITÄT  
DARMSTADT



- No scales from 1p-1h states

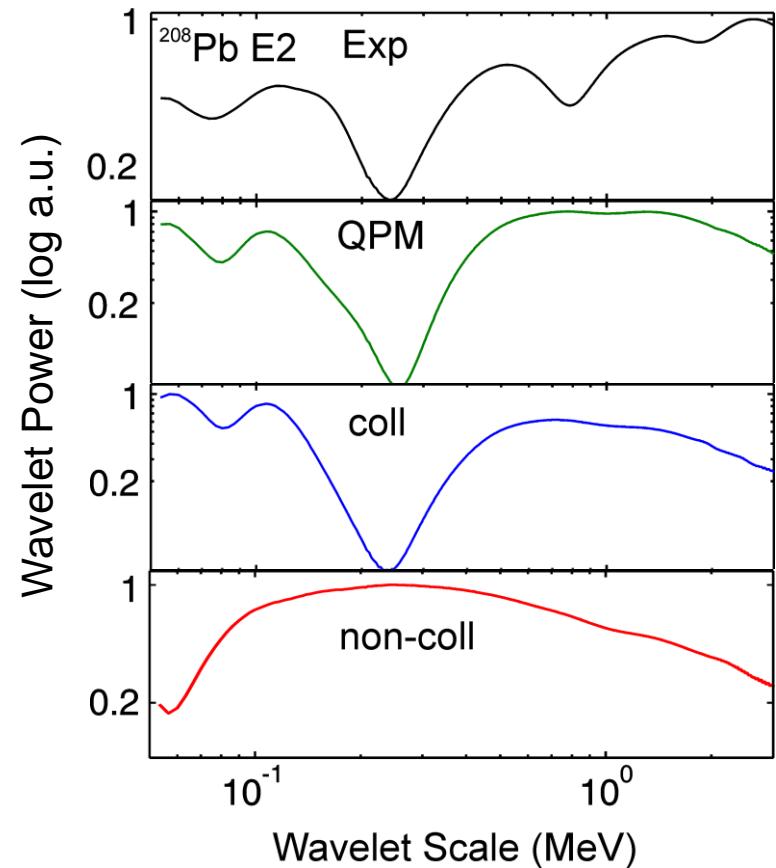
- Coupling to 2p-2h generates fine structure and scales

# Collective vs. Non-Collective Damping in $^{208}\text{Pb}$



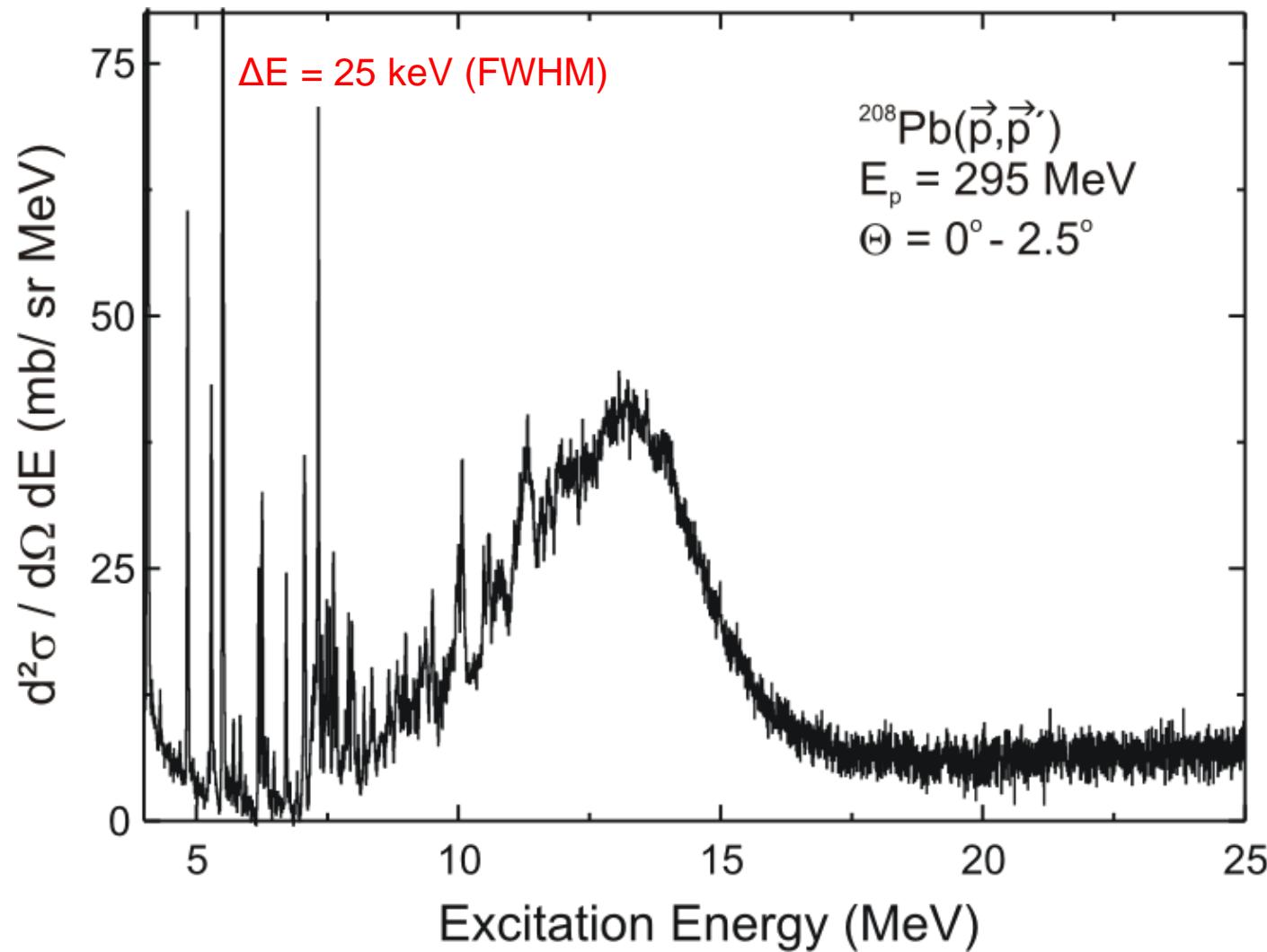
TECHNISCHE  
UNIVERSITÄT  
DARMSTADT

- Collective part: all scales
  - Non-collective part: no prominent scales
- ↗ Stochastic coupling



A. Shevchenko et al., Phys. Rev. Lett. 92, 122501 (2004)

# Scales of the IVGDR



# Scales of the IVGDR

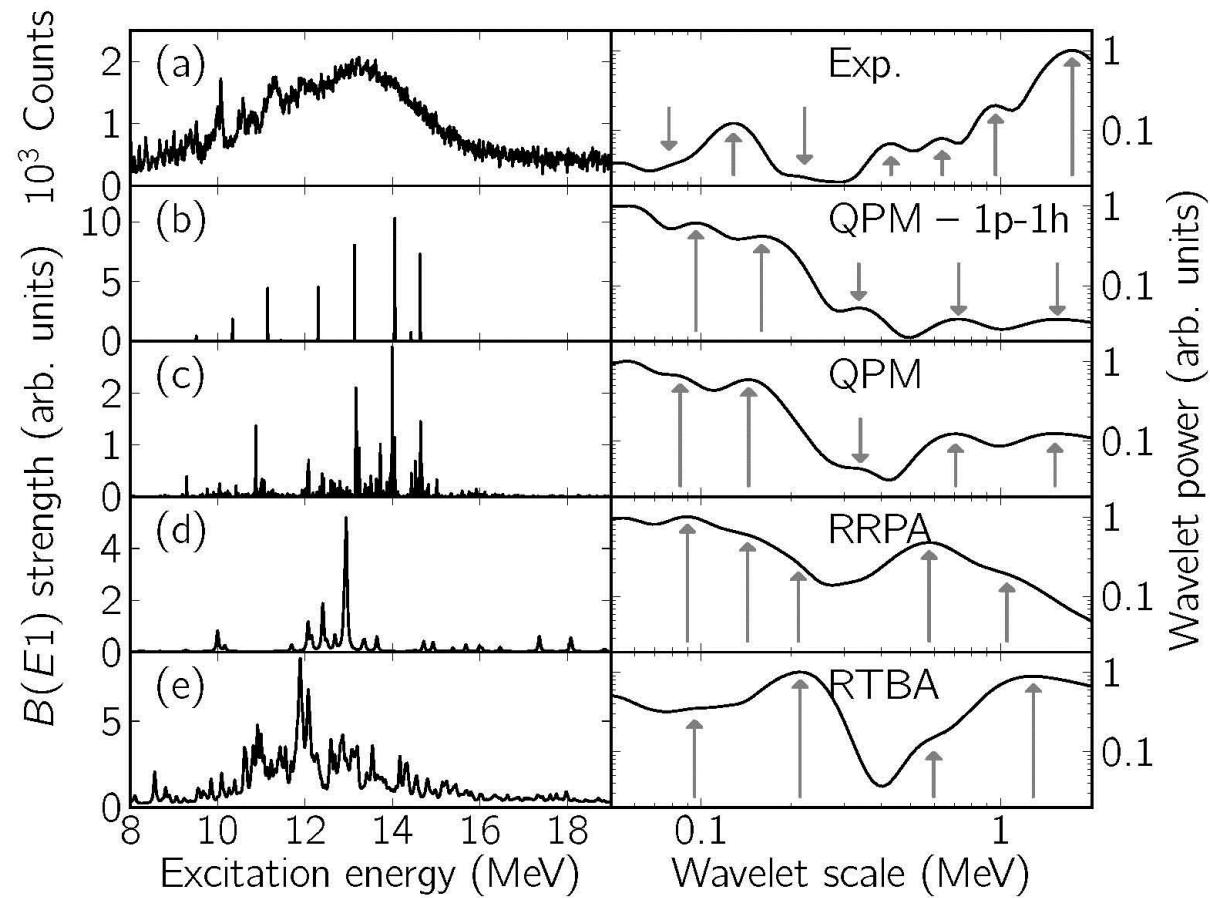


- Scales from 1p-1h states

- Scales from 1p-1h states



Landau damping



I. Poltoratska et al., Phys. Rev. C 89, 054322 (2014)

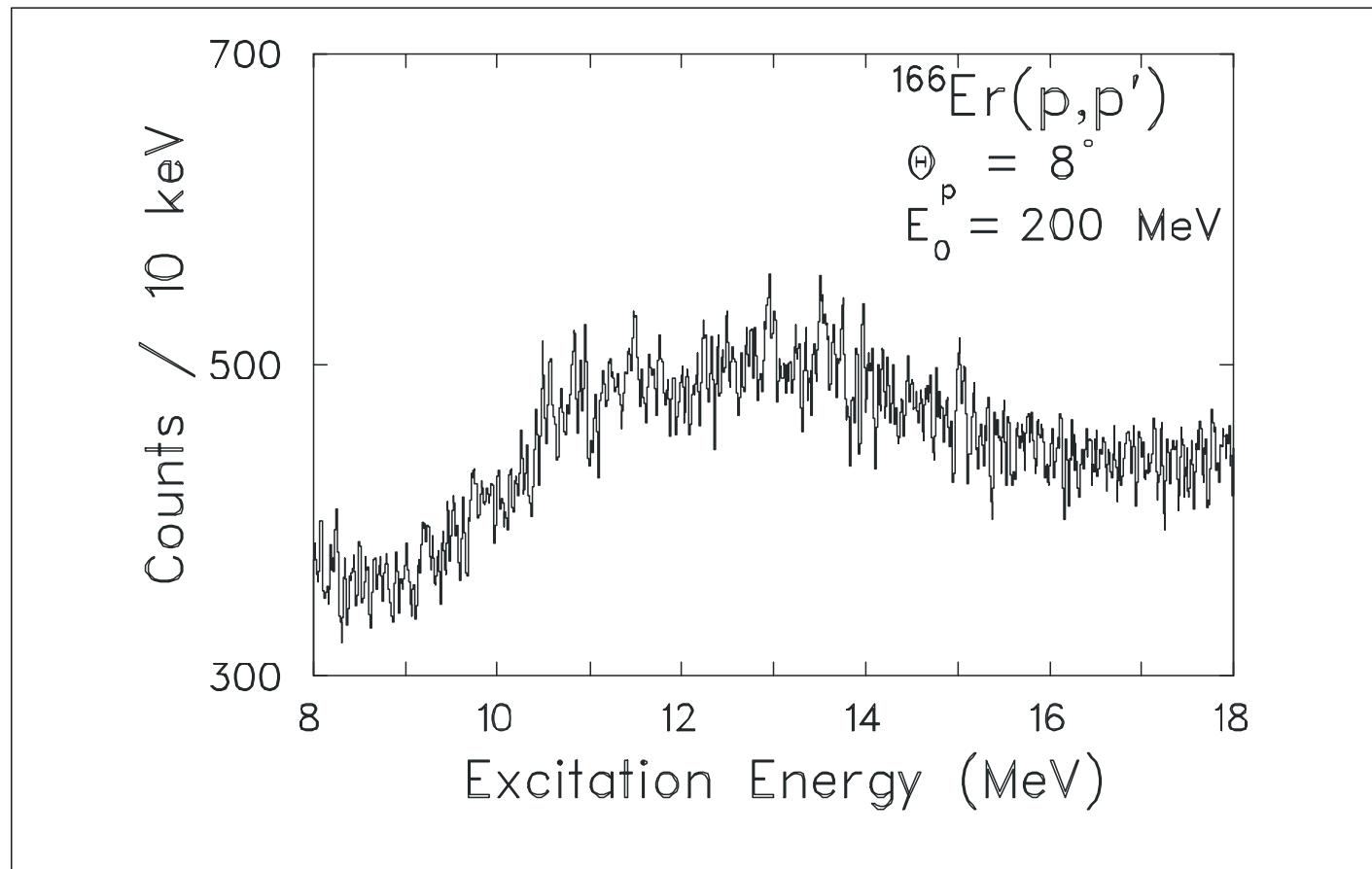


# Fine structure in heavy deformed nuclei: K splitting of the ISGQR

# Fine Structure in Heavy Deformed Nuclei?



TECHNISCHE  
UNIVERSITÄT  
DARMSTADT

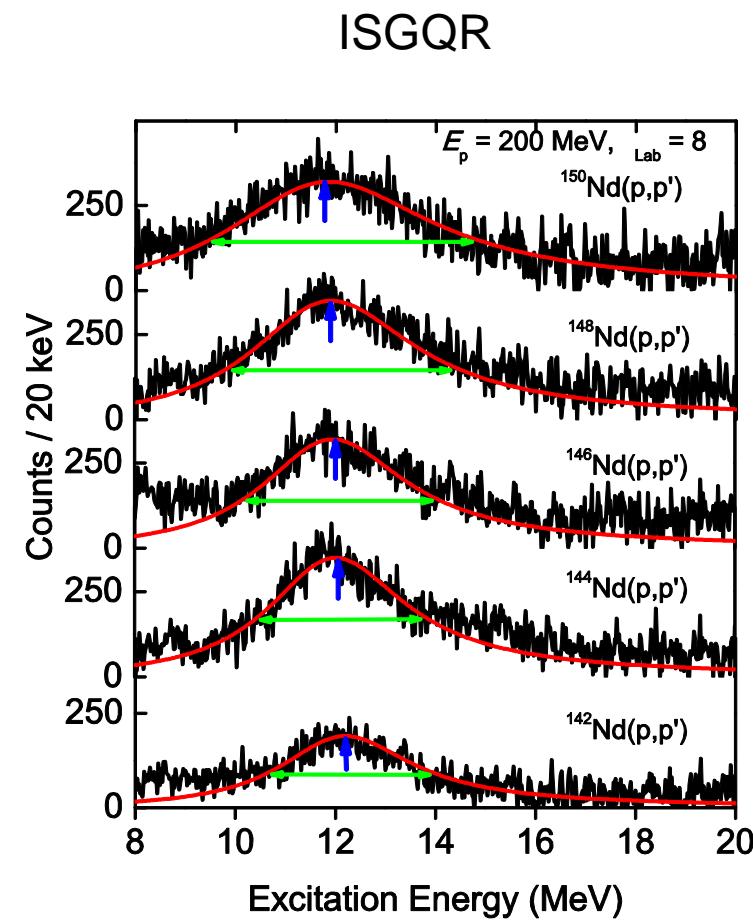
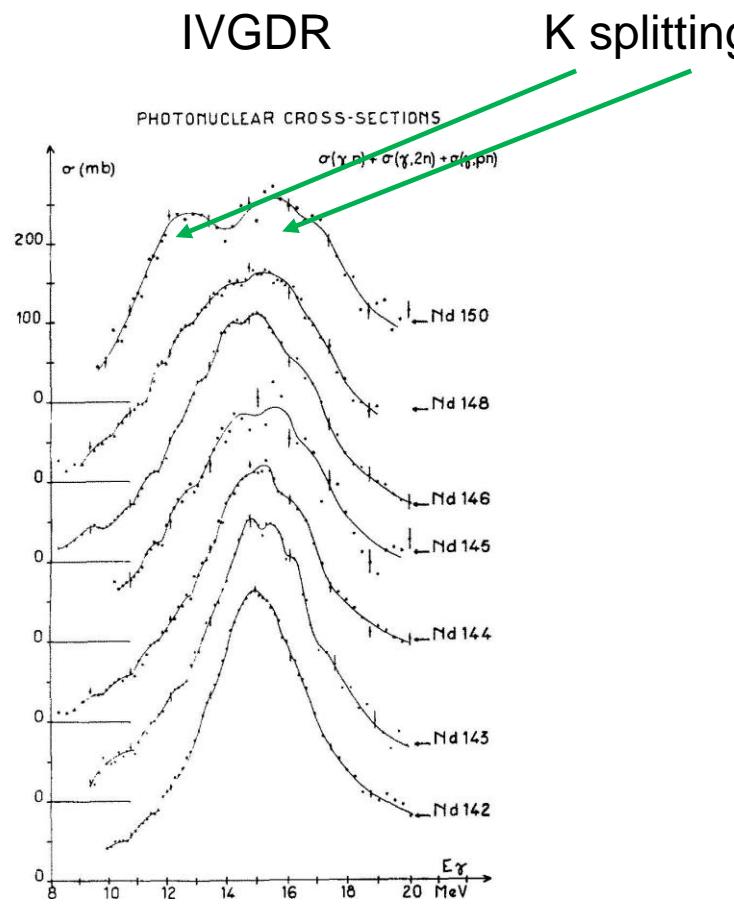


- Level density of  $2^+$  states in the ISGQR region  $10^6 - 10^7 / \text{MeV}$

# IVGDR and ISGQR Resonances in the Nd Chain



TECHNISCHE  
UNIVERSITÄT  
DARMSTADT



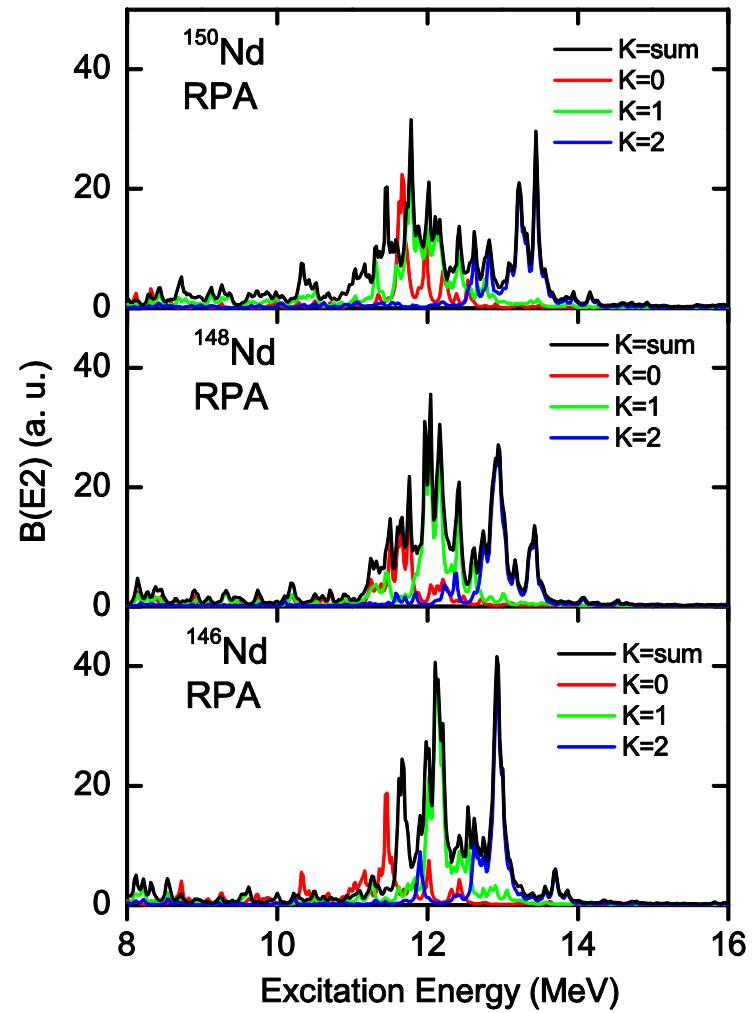
P. Carlos et al., Nucl. Phys. A 172, 437 (1971)

O. Kureba, PhD thesis, University of the Witwatersrand (2014); and to be published

# Predicted K splitting



TECHNISCHE  
UNIVERSITÄT  
DARMSTADT

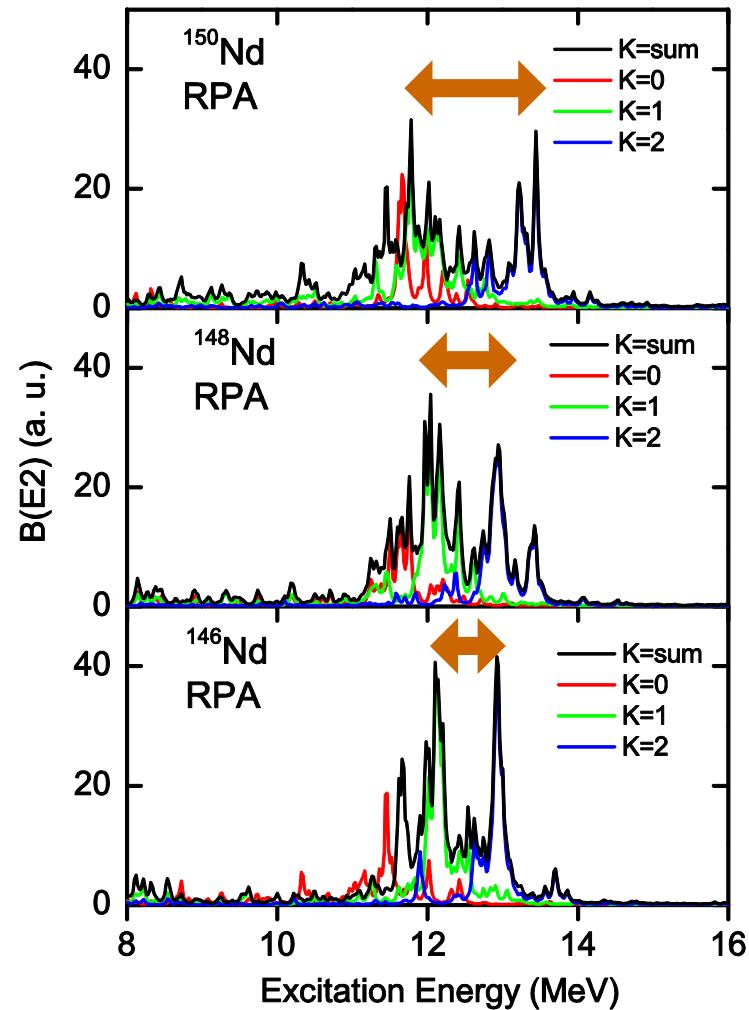


V.O. Nesterenko et al., Phys. Rev. C 74, 064306 (2006)

# Predicted K splitting



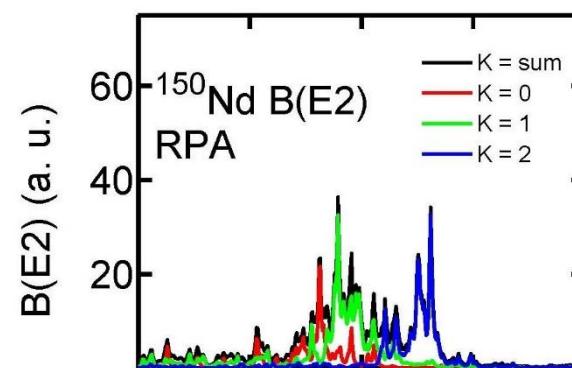
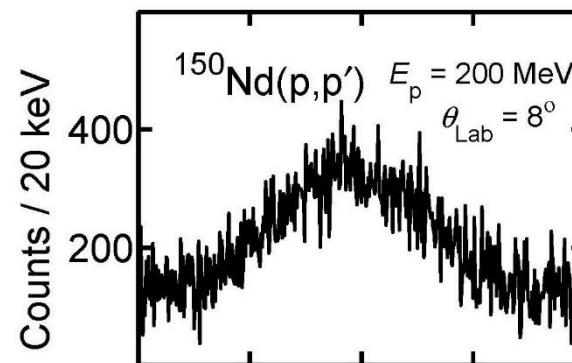
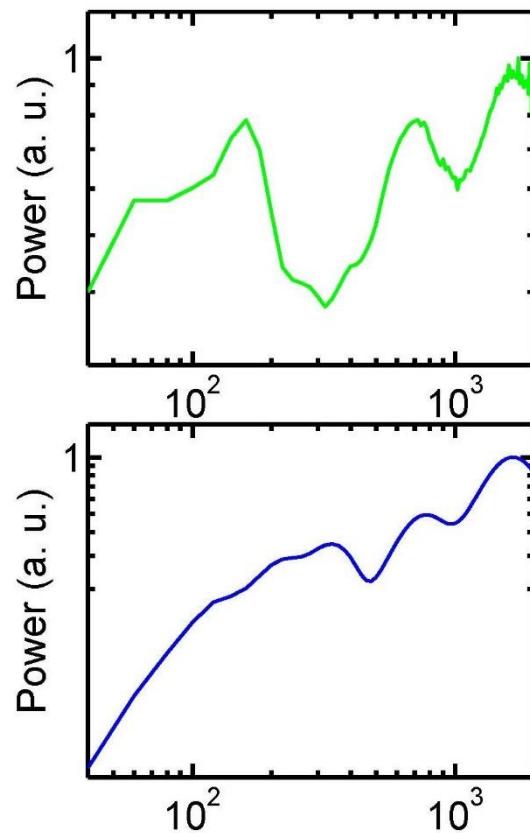
- Signature splitting of  $K = 1$  and  $K = 2$  components
- $K = 0$  component weak



# Fine Structure in the Deformed $^{150}\text{Nd}$



TECHNISCHE  
UNIVERSITÄT  
DARMSTADT



# Semblance Analysis

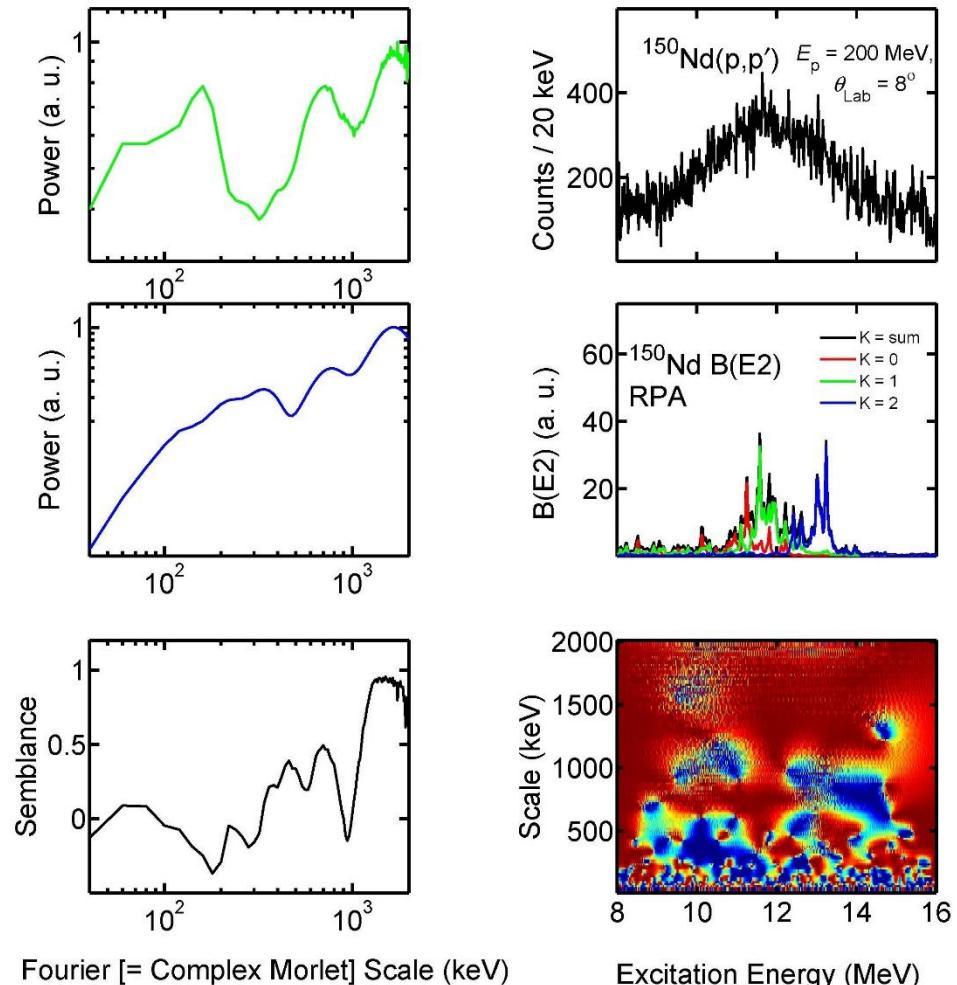


TECHNISCHE  
UNIVERSITÄT  
DARMSTADT

## Semblance

$$D = \cos^n(\theta) | C_1 C_2^* |$$

$$\theta = \tan^{-1}[Im(C_1 C_2^*) / Re(C_1 C_2^*)]$$



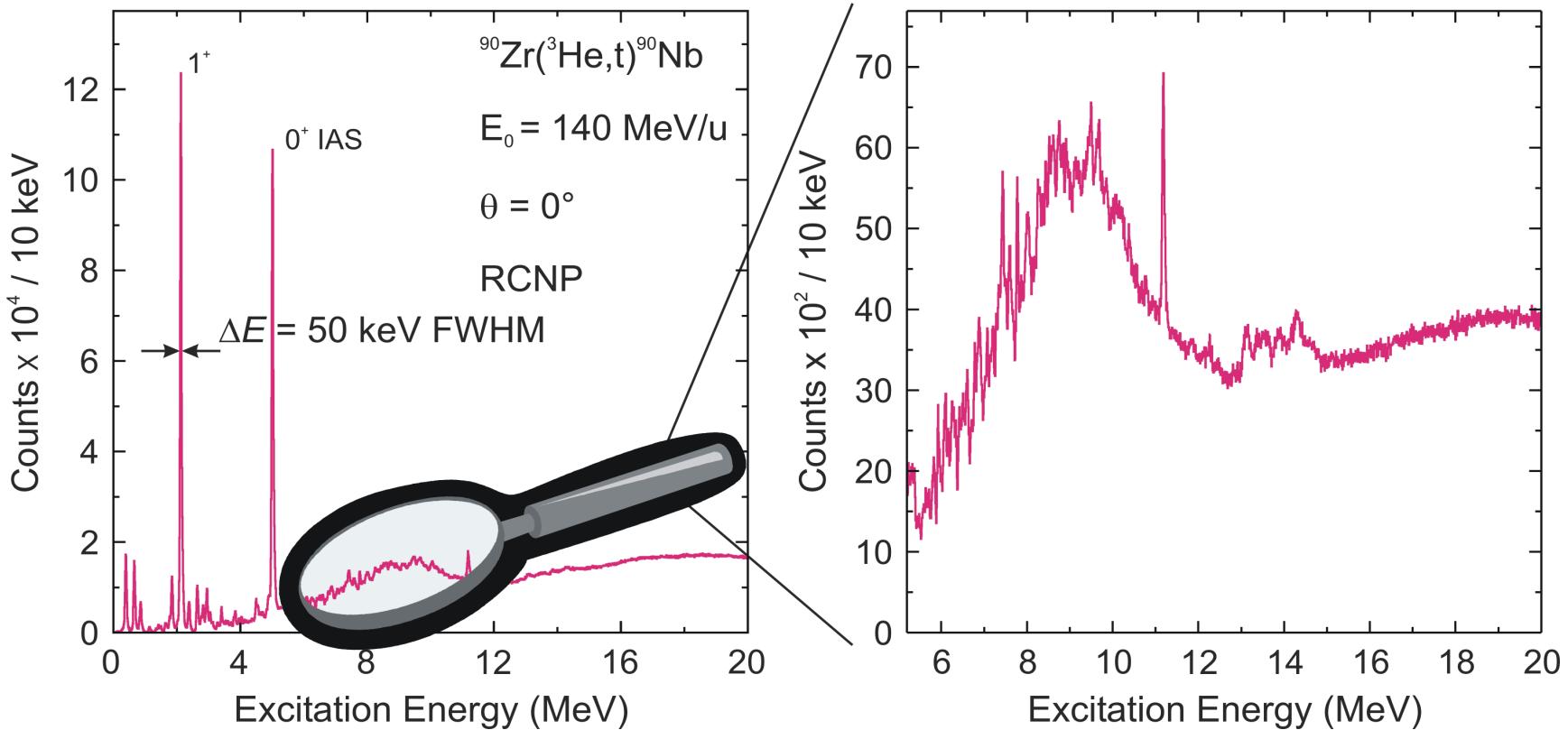


# Level densities

# Fine Structure of the spin-flip GTR: A = 90

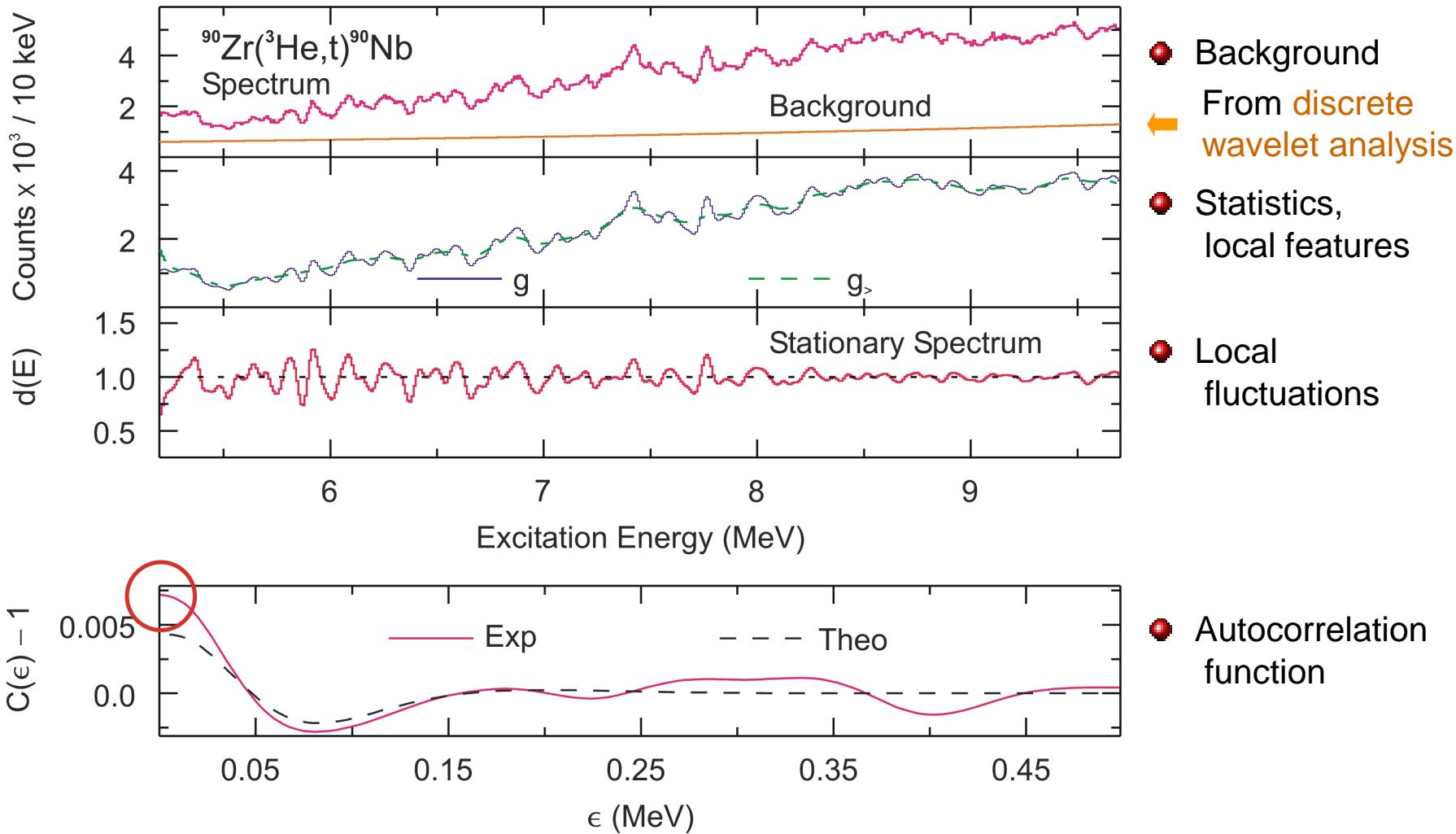


TECHNISCHE  
UNIVERSITÄT  
DARMSTADT



- Selective excitation of  $1^+$  states

# Fluctuation Analysis

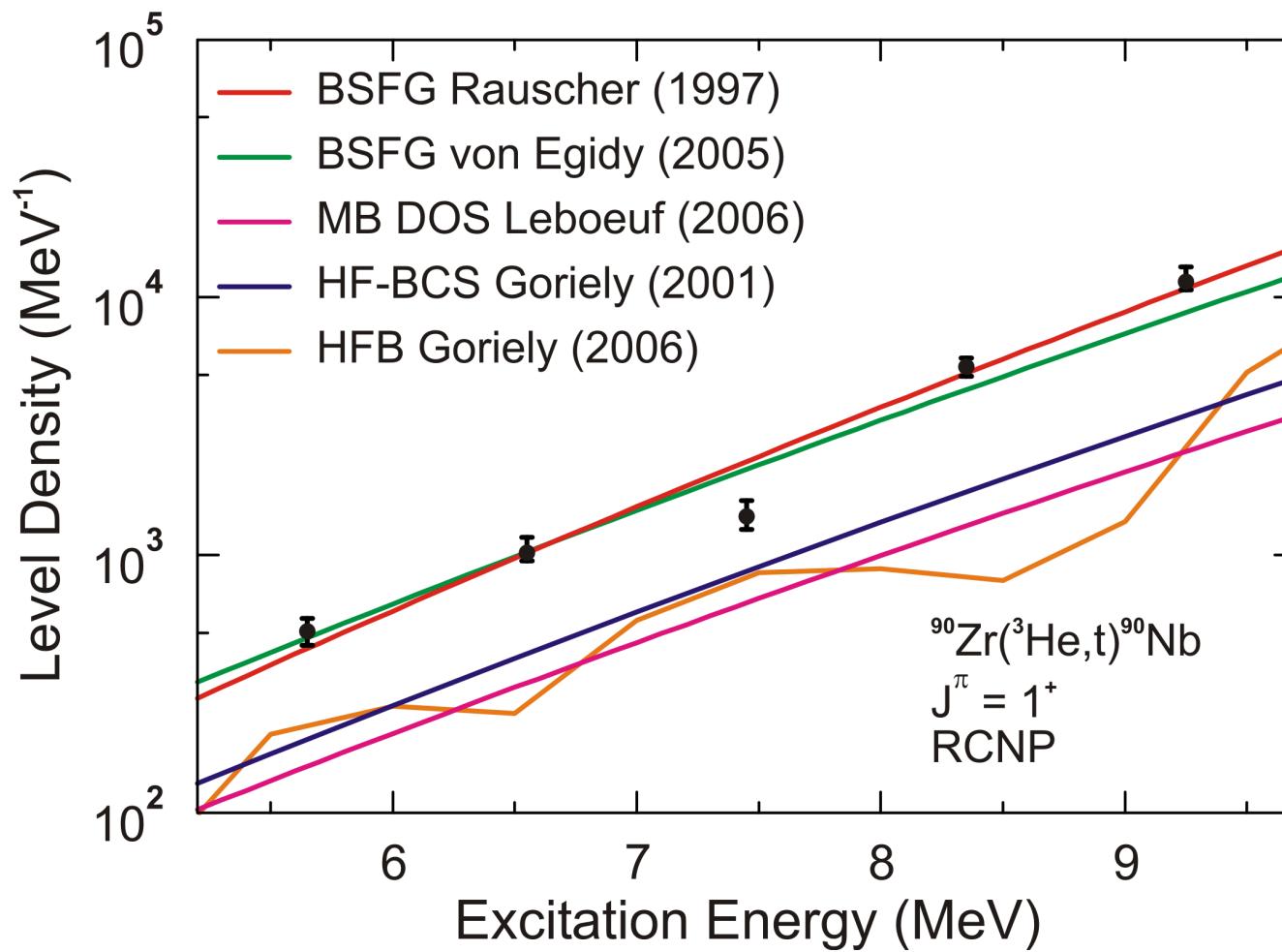


# Autocorrelation Function and Mean Level Spacing

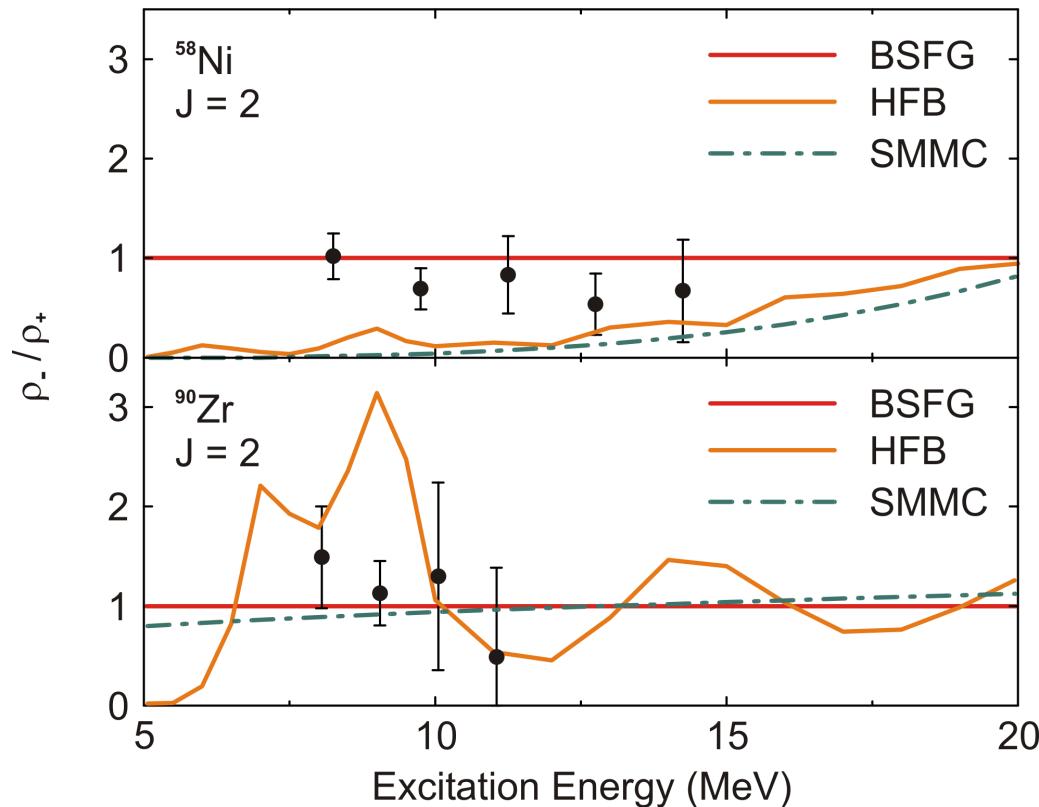


- $C(\varepsilon) = \frac{\langle d(E_x) \cdot d(E_x + \varepsilon) \rangle}{\langle d(E_x) \rangle \cdot \langle d(E_x + \varepsilon) \rangle}$  autocorrelation function
- $C(\varepsilon = 0) - 1 = \frac{\langle d^2(E_x) \rangle - \langle d(E_x) \rangle^2}{\langle d(E_x) \rangle^2}$  variance
- $C(\varepsilon = 0) - 1 = \frac{\alpha \langle D \rangle}{2\sigma\sqrt{\pi}}$  level spacing  $\langle D \rangle$
- $\alpha = \alpha_{PT} + \alpha_W$  statistical properties
- $\sigma$  resolution

# Results and Model Predictions



# Parity Dependence of Level Densities



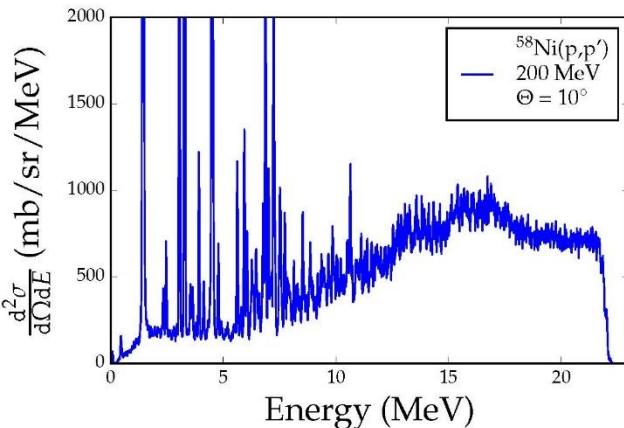
- Experiments: no parity dependence
- HFB and SMMC:  $^{58}\text{Ni}$  strong parity dependence:  $\rho_- \ll \rho_+$

# Spin Dependence of Level Densities

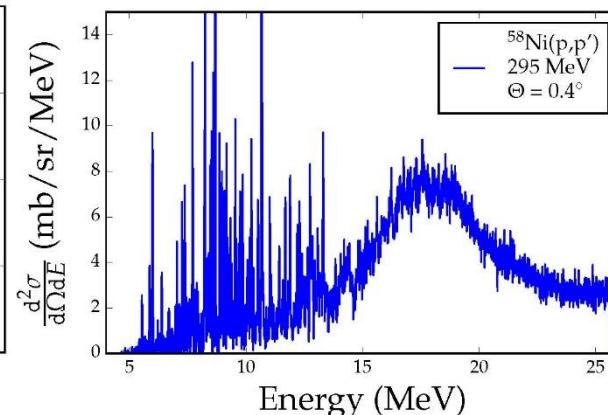


TECHNISCHE  
UNIVERSITÄT  
DARMSTADT

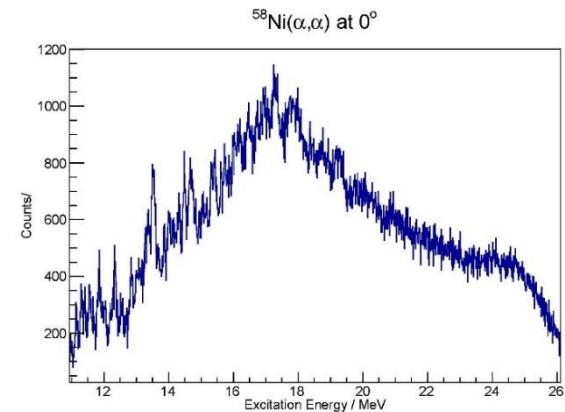
ISGQR  
@iThemba



IVGDR(+ M1)  
@RCNP



ISGMR  
@iThemba



$J = 0, 1, 2$  level densities in the same nucleus → test of spin dependence



## Fine structure:

A powerful tool for the study of  
nuclear structure in the continuum



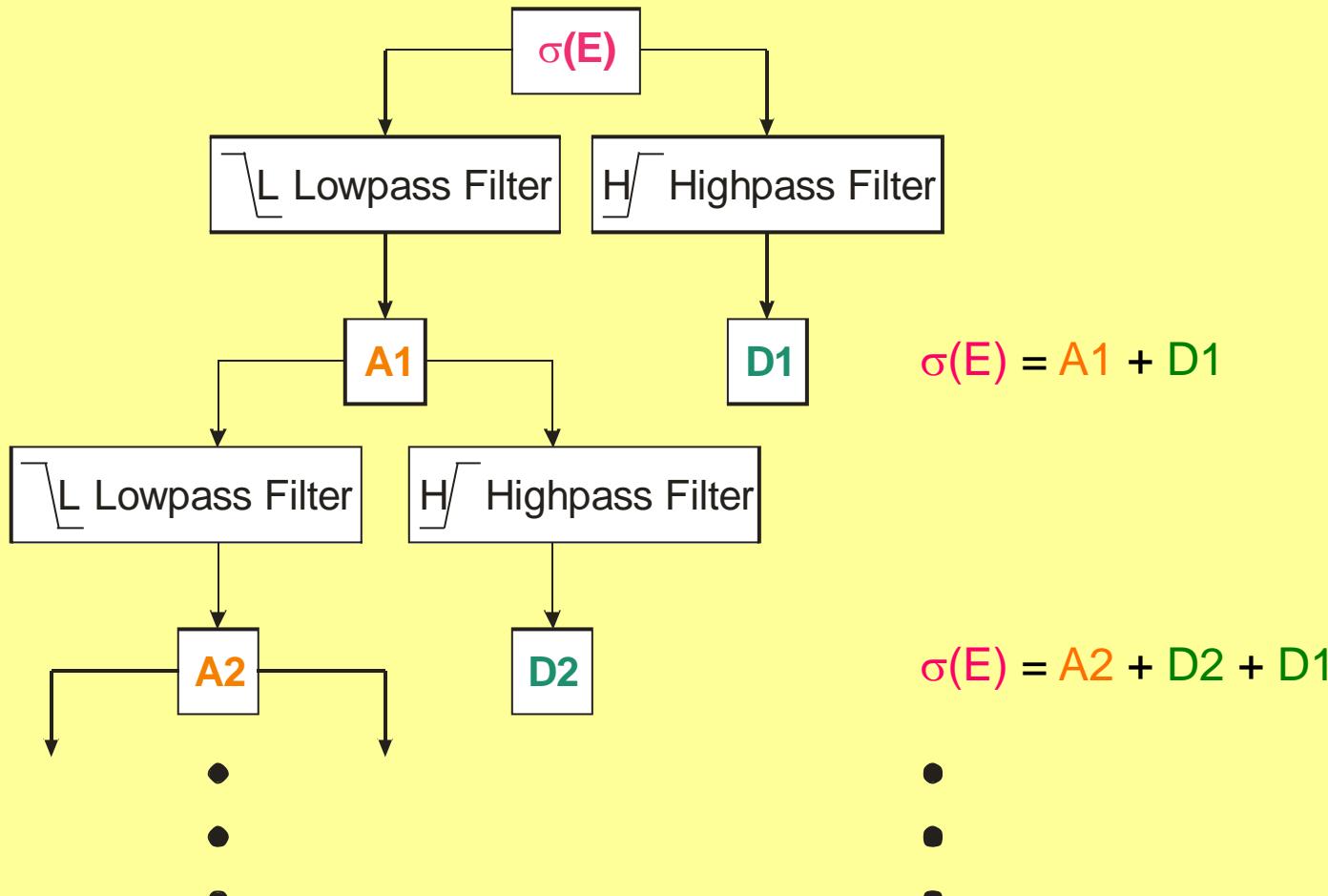
TECHNISCHE  
UNIVERSITÄT  
DARMSTADT

# Discrete wavelet transform

- $C(\delta E, E_x) = \frac{1}{\sqrt{\delta E}} \int_{-\infty}^{+\infty} \sigma(E) \Psi * \left( \frac{E_x - E}{\delta E} \right) dE$  wavelet coefficients
- Discrete wavelet transform \*
  - $\delta E = 2^j$  and  $E_x = k \cdot \delta E$  with  $j, k = 1, 2, 3, \dots$
  - exact reconstruction is possible
  - is fast
- $\int_{-\infty}^{+\infty} E^n \Psi * \left( \frac{E_x - E}{\delta E} \right) dE = 0, \quad n = 0, 1, \dots, m-1$  vanishing moments
  - this defines the shape and magnitude of the background

\* <http://www.mathworks.com/products/wavelet/>

# Decomposition of spectra



Background

# Decomposition of $^{90}\text{Zr}(^{3}\text{He},\text{t})^{90}\text{Nb}$ spectrum

