

# Nucleon swelling and Compton scattering

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Problem of  ${}^4\text{He}$  point nucleon density distribution  
Variable proton size in CMD calculation  
Quasifree Compton scattering

# Different effective masses for nucleon

non - relativistic     $[\frac{1}{2m} p^2 + U_s(r, \varepsilon)]\psi_s = \varepsilon\psi_s$

$$U_s = V_s + iW_s$$

- $\frac{m_s^*(\varepsilon)}{m} = 1 - \frac{d}{d\varepsilon} V_s(\varepsilon)$       (conventional effective mass)

- $\frac{\tilde{m}(\varepsilon)}{m} = [1 + \frac{m}{k} \frac{\partial}{\partial k} V_s]_{k=k(\varepsilon)}^{-1}$       (effective  $k$  - mass)

- $\frac{\bar{m}(\varepsilon)}{m} = [1 - \frac{\partial}{\partial \varepsilon} V_s]_{k=k(\varepsilon)}$       (effective  $E$  - mass)

relativistic     $[\vec{\alpha} \cdot \vec{p} + \gamma_0(m + U_\sigma + \gamma_0 U_0)]\phi = E\phi$

- $\frac{M^*}{m} = 1 + \frac{V_\sigma}{m}$       (Dirac mass)

- $\frac{m_e^*(\varepsilon)}{m} = 1 - \frac{d}{d\varepsilon} V_e(\varepsilon) = 1 - \frac{V_0}{m}$       (Lorentz mass)  
 (Schroedinger equivalent)

$$\frac{m_s^*(\varepsilon)}{m} = \frac{\tilde{m}(\varepsilon)}{m} \cdot \frac{\bar{m}(\varepsilon)}{m}$$

QCD base

- NJL

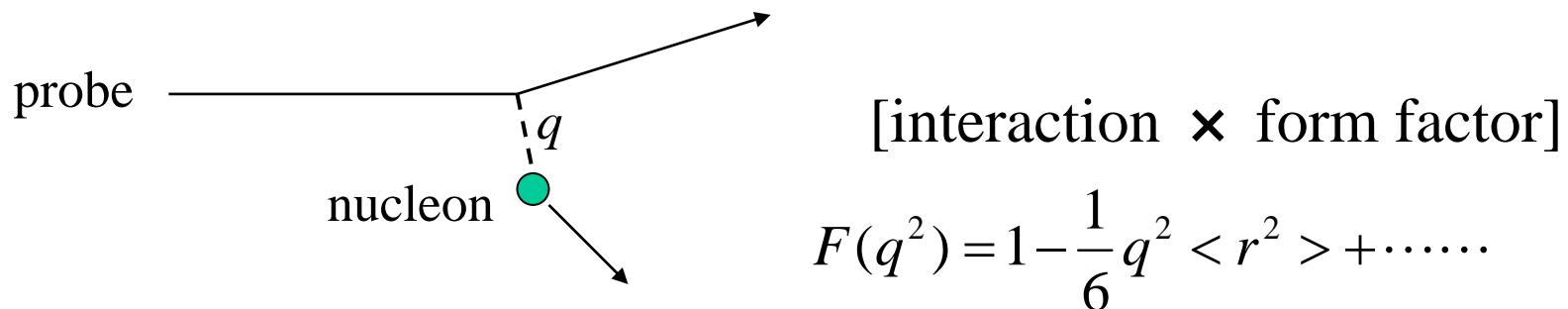
$$f_\pi^*/f_\pi \sim m_\sigma^*/m_\sigma \\ \sim m_V^*/m_V \sim m_N^*/m_N$$

- QCD sum rule

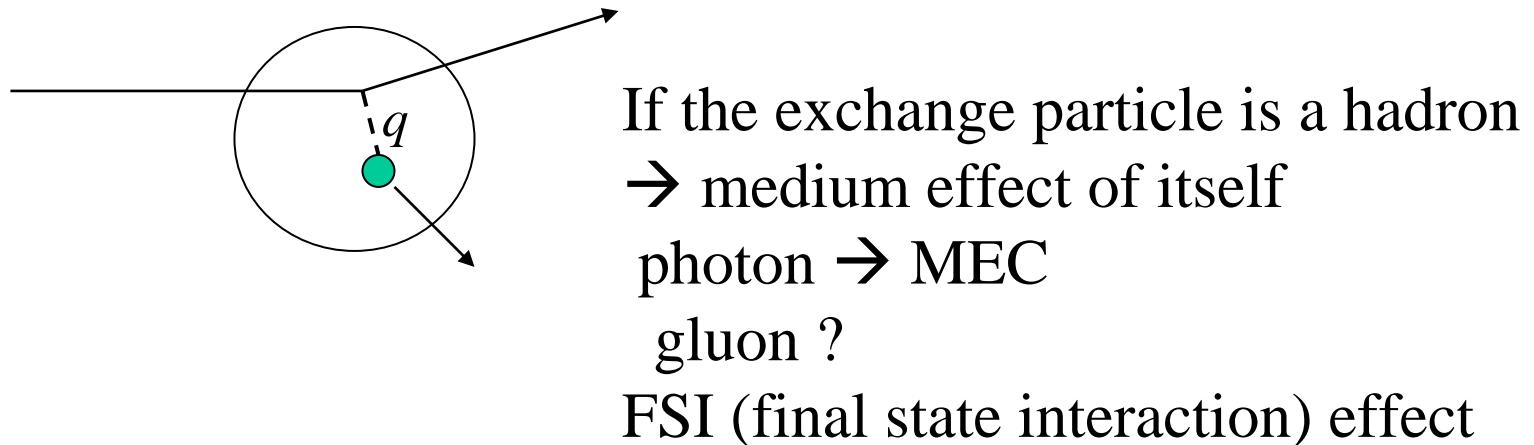
# Nucleon form factor (or size) in nuclear medium

## Is it changed from free nucleon? (medium effect other than mass shift)

- elastic



- quasi-elastic



# Quark substructure approach to ${}^4\text{He}$ charge distribution

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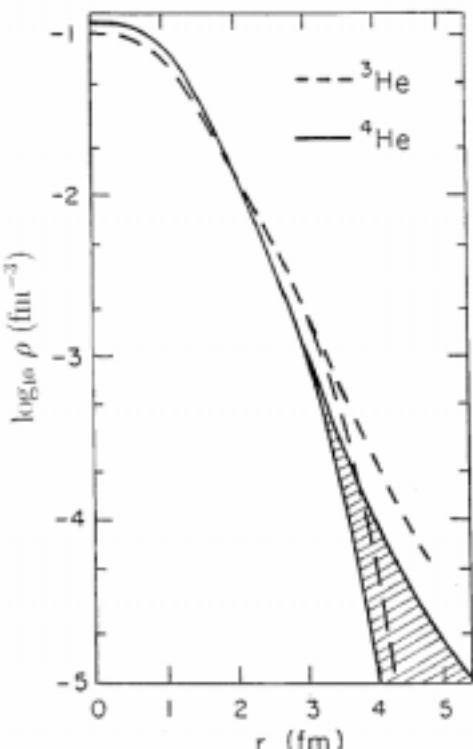


FIG. 1. Model-independent charge distributions for  ${}^3\text{He}$  and  ${}^4\text{He}$  extracted from experiment. Reproduced from McCarthy *et al.* [1], who state that "the extreme limits of  $\rho(r)$  cover the statistical, systematical as well as the completeness error of the data."

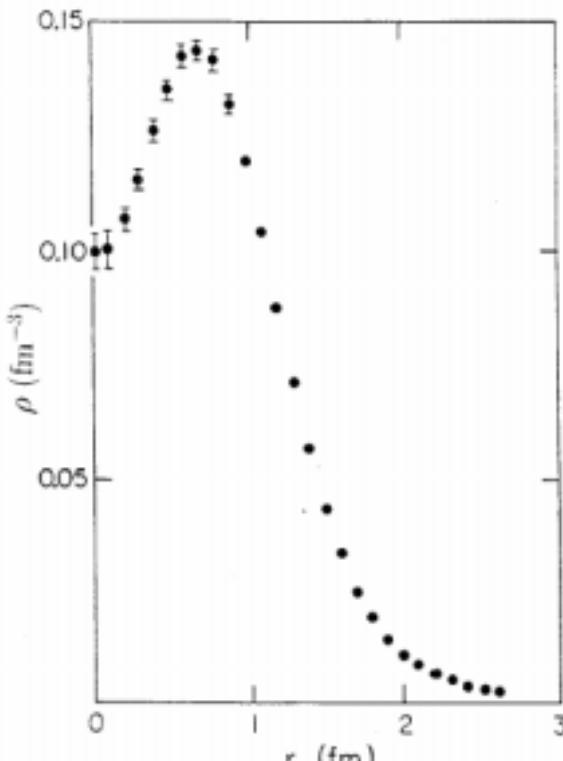


FIG. 2. Point-proton density distribution for  ${}^4\text{He}$  obtained by unfolding the free proton form factor, allowing for meson exchange corrections and relativistic effects. Reproduced from Sick [2].

# Nuclear density distribution

[Experiment]       $(e, e')$  or  $\mu$ -atom  
                        ← model-independent analysis  
                        charge density distribution  
fold  $\rho_p + \text{MEC}$       ← unfold proton charge distribution  $\rho_p$   
                        point proton density distribution

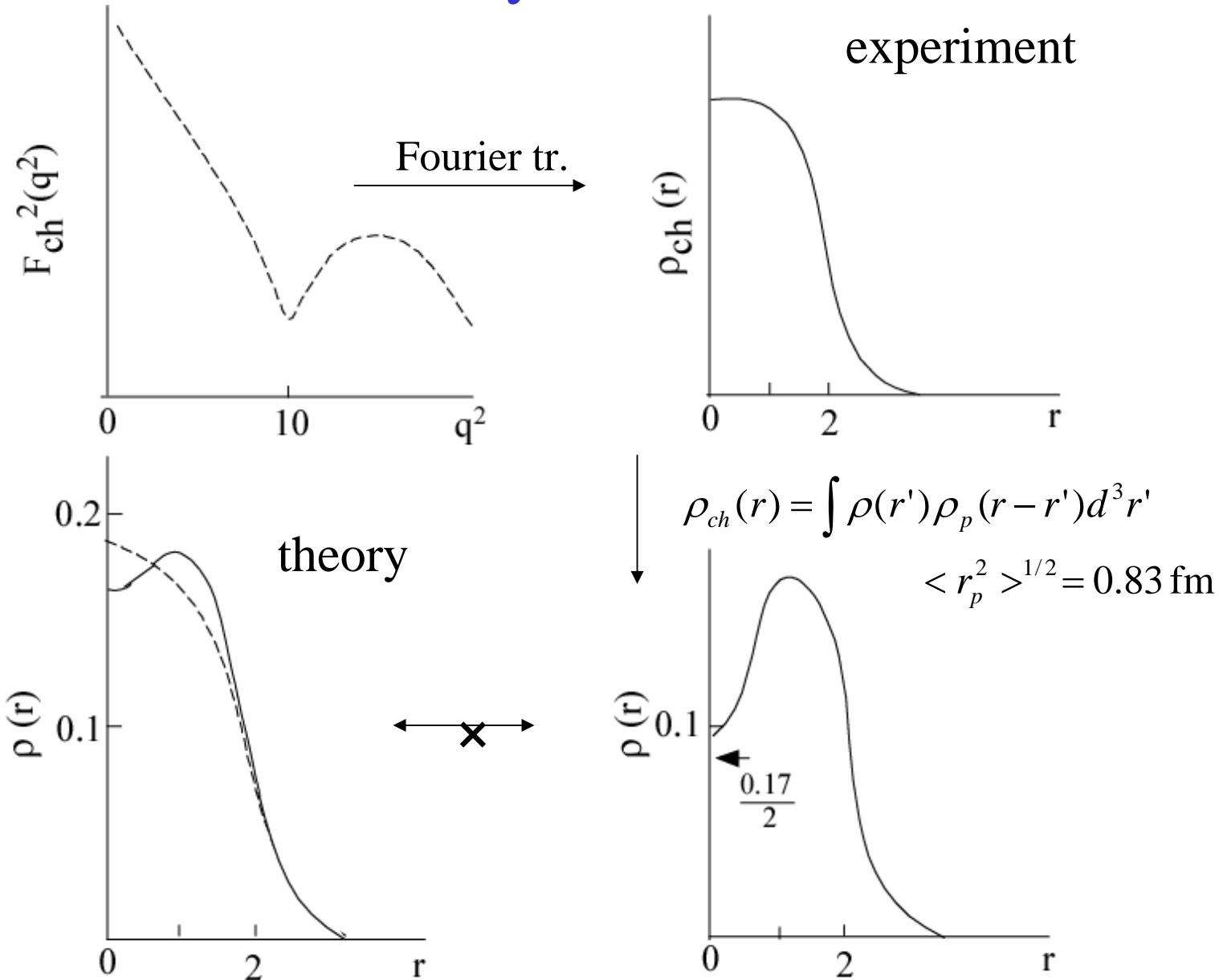
ground state wave function

← Green function MC, etc.  
(many body) Schroedinger eq. (Dirac eq.)

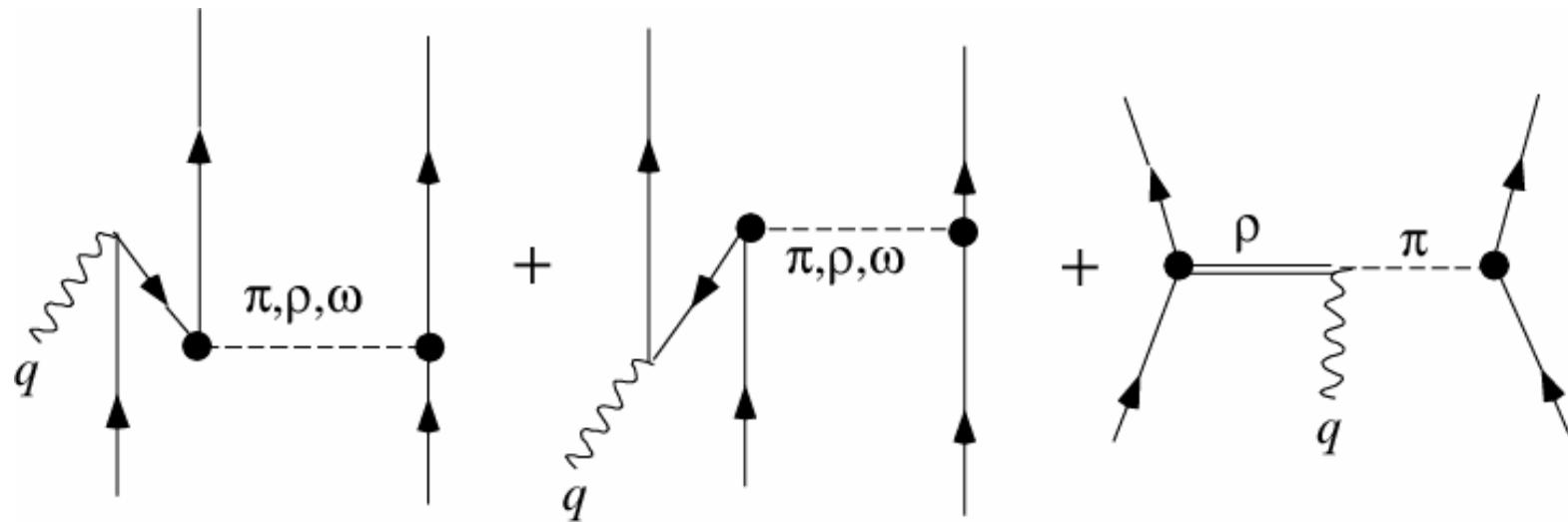
[Theory]      NN interaction (2-body, 3-body)

Usually unfold (fold) the charge distribution of free proton  
→ If proton is “swelling” in the nucleus, .....?

# Point nucleon density distribution in ${}^4\text{He}$



Usually it is due to MEC (meson exchange current)



# Chromodielectric Soliton Model

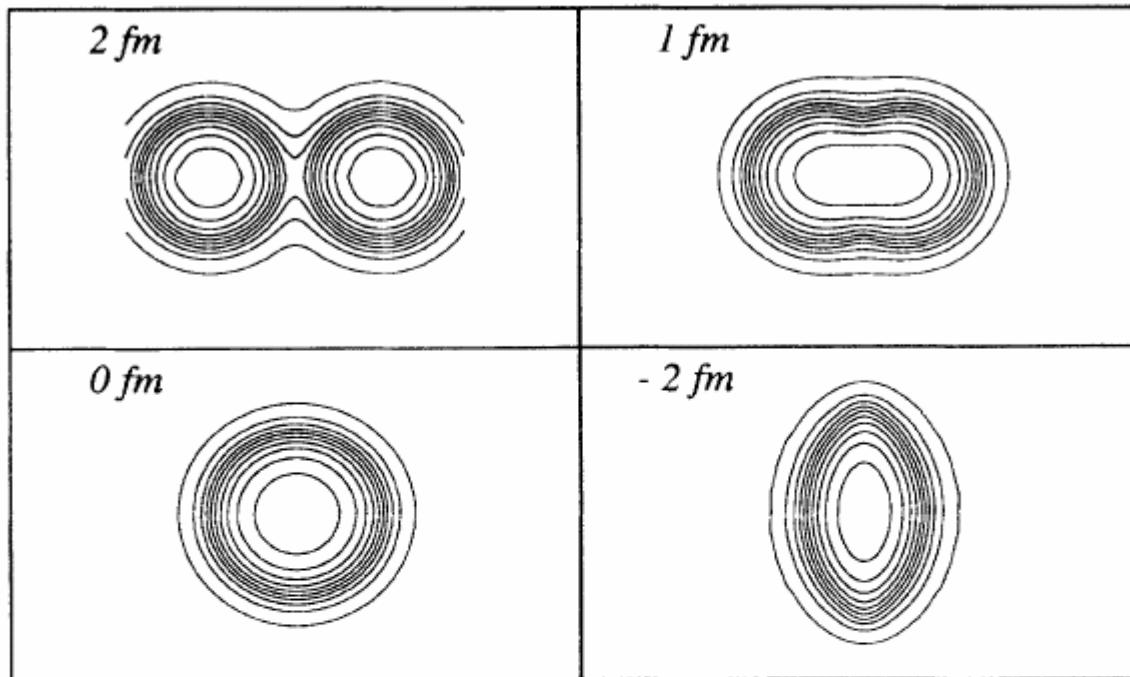


FIG. 1. The scalar field,  $\sigma_\alpha(\mathbf{r})$  of Eq. (16), from which the single-quark wave functions are generated, for four different values of the deformation parameter  $\alpha$  between 2 fm and  $-2$  fm. The fields correspond to the parameter set with  $f = 3$  and  $c = 10\,000$ , and are shown with equal increments between adjacent contours.

# Variable rms proton charge radius

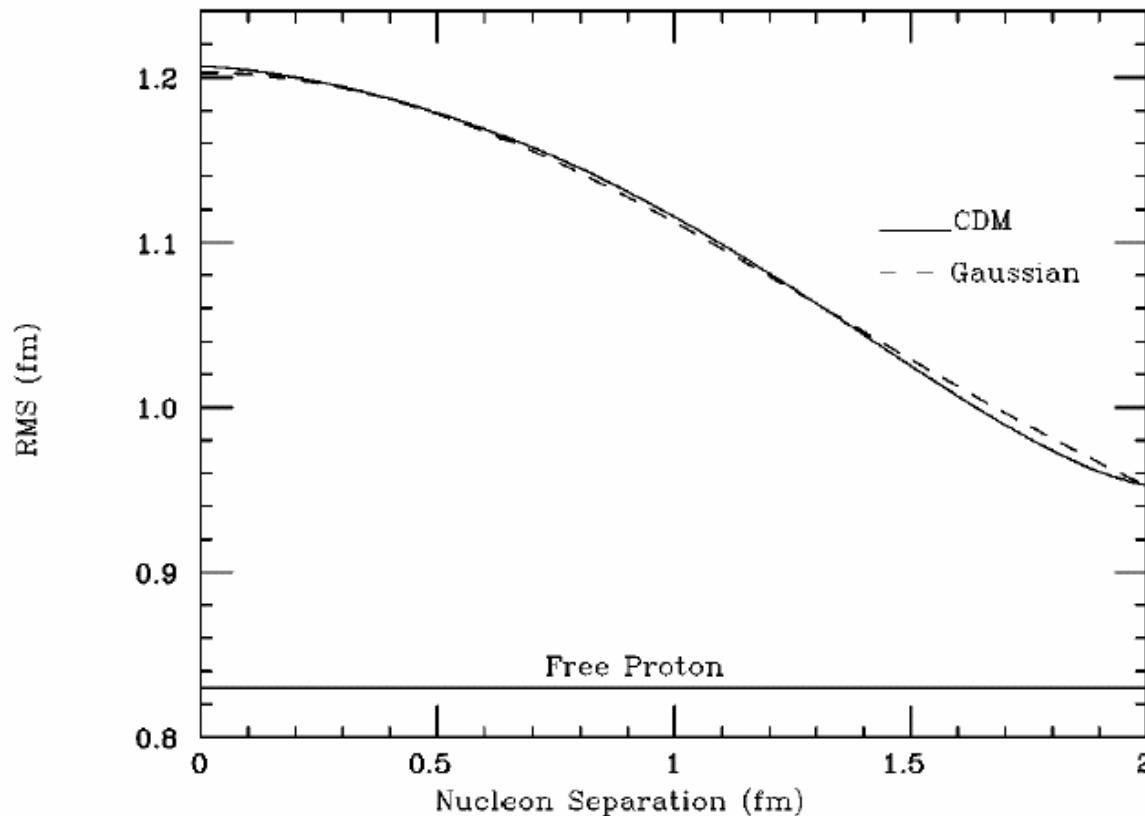


FIG. 3. Proton rms charge radius  $r_p$  of Eq. (1) as a function of internucleon separation. The line labeled CDM is the calculated chromodielectric model result. The dashed line is a Gaussian approximation, normalized to the free value, with a size parameter given by Eq. (3)

# Folding variable proton size to the point proton density distribution

- assume Gaussian distribution  $b(r') = \sqrt{2/3}r_p(r')$ .

- 2-nucleon pair charge density

$$\rho_{\text{pair}}(\mathbf{r}_i, \mathbf{r}_j; \mathbf{r}) = \{\delta_{ip} \exp[-|\mathbf{r} - \mathbf{r}_i|^2/b^2(r_{ij})] \\ + \delta_{jp} \exp[-|\mathbf{r} - \mathbf{r}_j|^2/b^2(r_{ij})]\}/\pi^{3/2}b^3(r_{ij}),$$

- independent pair approximation

$$\rho_{\text{ch}}(r) = \frac{1}{3} \sum_{i < j} \int d^3 r_i \int d^3 r_j f_2(\mathbf{r}_i, \mathbf{r}_j) \rho_{\text{pair}}(\mathbf{r}_i, \mathbf{r}_j; \mathbf{r}).$$

$$f_2(\mathbf{r}_1, \mathbf{r}_2) = \int |\psi(\mathbf{r}_1, \mathbf{r}_2, \mathbf{r}_3, \mathbf{r}_4)|^2 d^3 r_3 d^3 r_4,$$

# $^4\text{He}$ density distribution

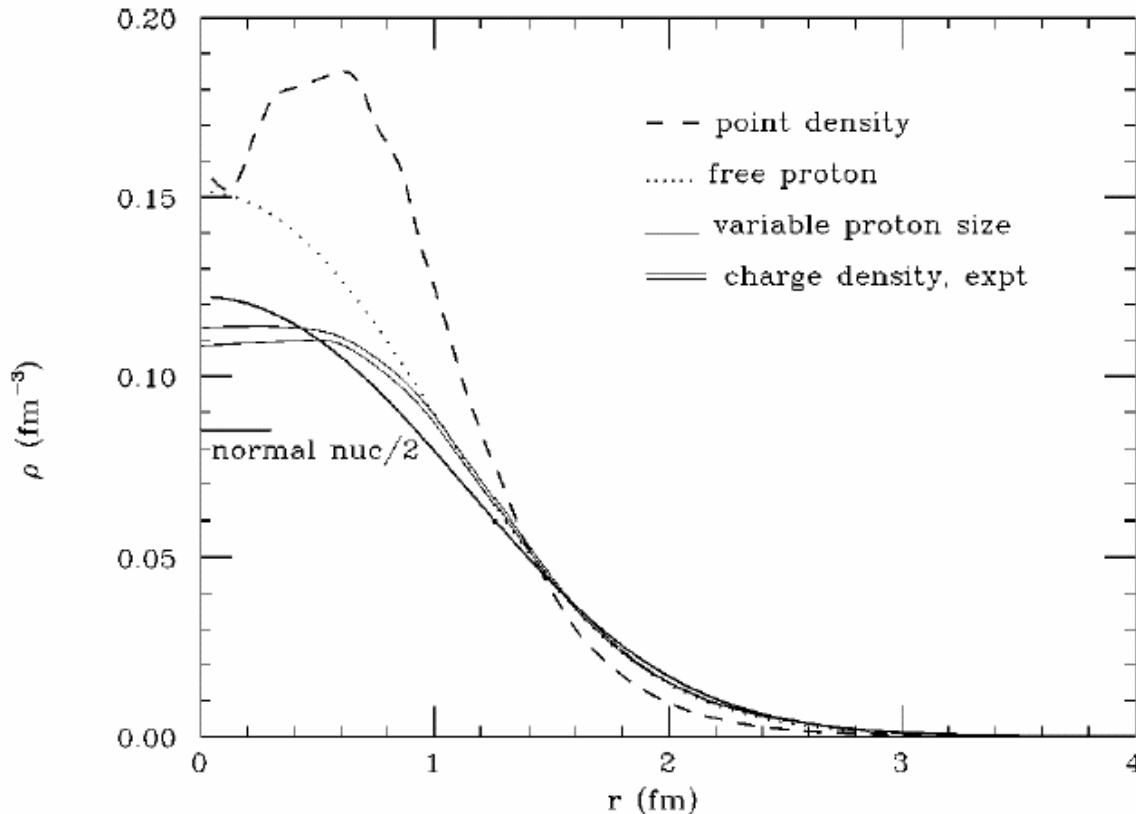
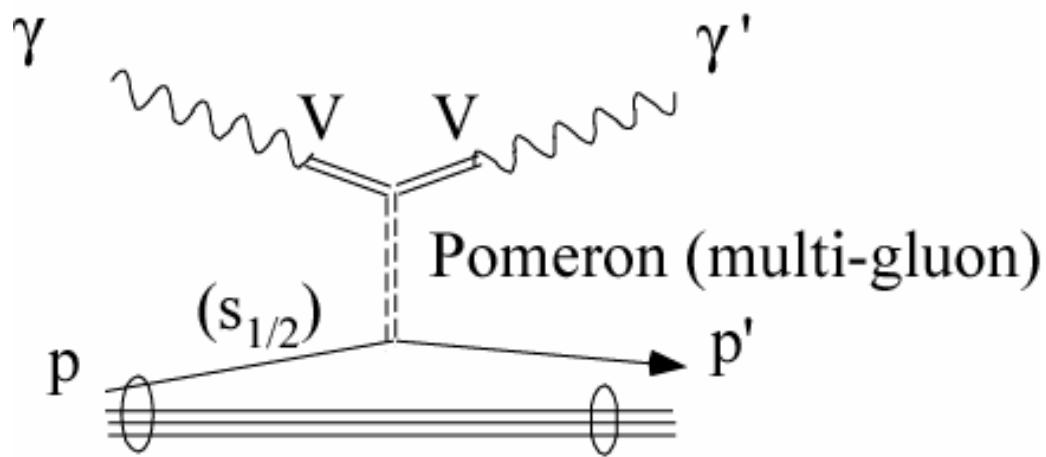
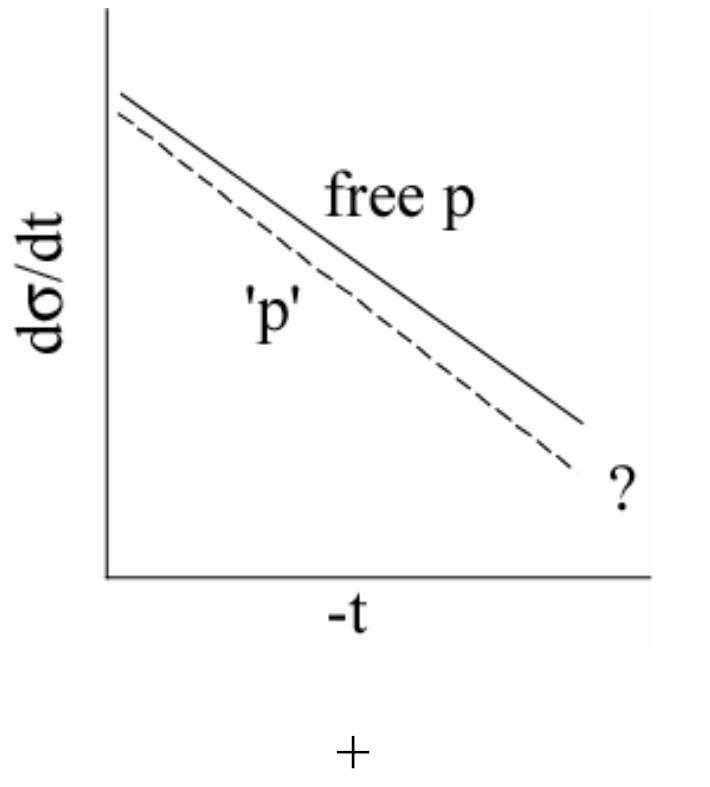


FIG. 4.  $^4\text{He}$  density distributions: The dashed line is the point density from a parametrized Green's function Monte Carlo calculation. The curve labeled “free proton” is the charge distribution obtained from a Gaussian proton charge distribution with a fixed size parameter (as is usually done). The curve labeled “variable proton size” uses the Gaussian fit of Fig. 3. We also indicate half the normal nuclear density  $0.17/2 \text{ fm}^{-3}$ .

# ${}^4\text{He}(\gamma, \gamma p) {}^3\text{H}$ in VD energy region

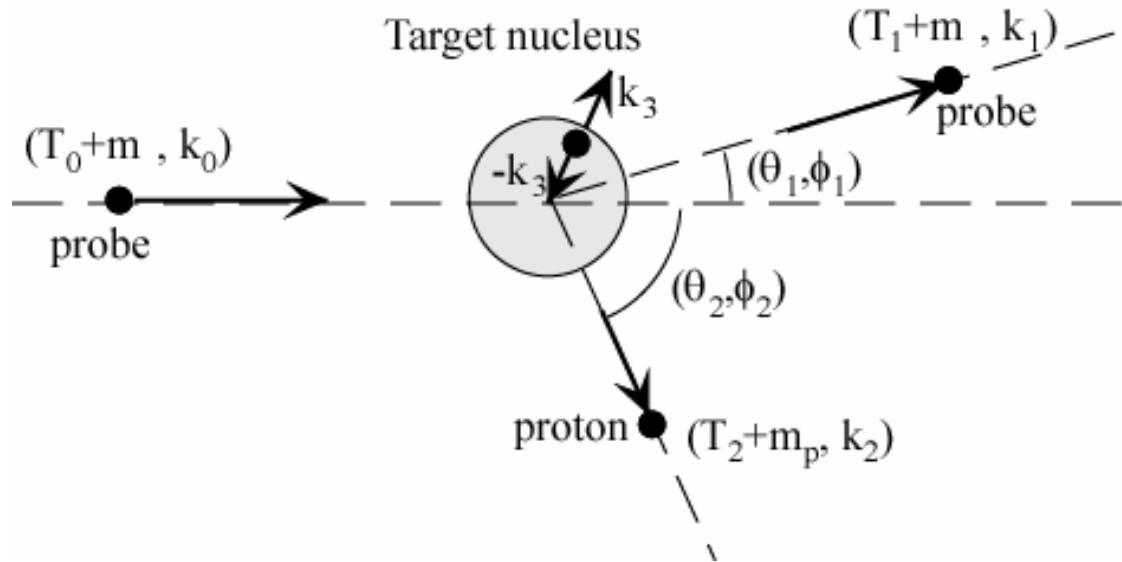


ISI, FSI: small  
no MEC ?  
 $E_\gamma \gg E_{\text{sep}}$



+  
Polarization observables

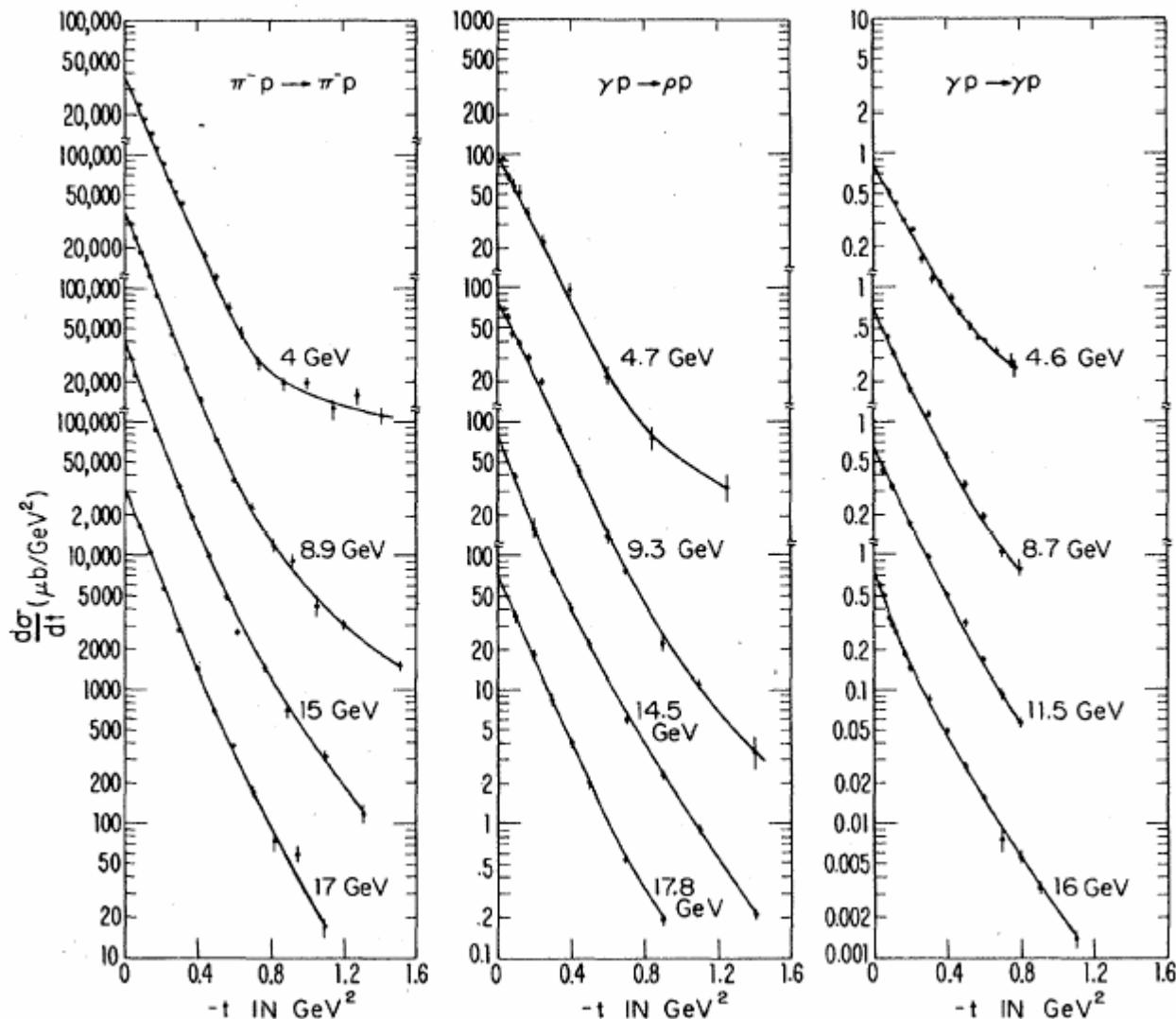
# Quasifree kinematics



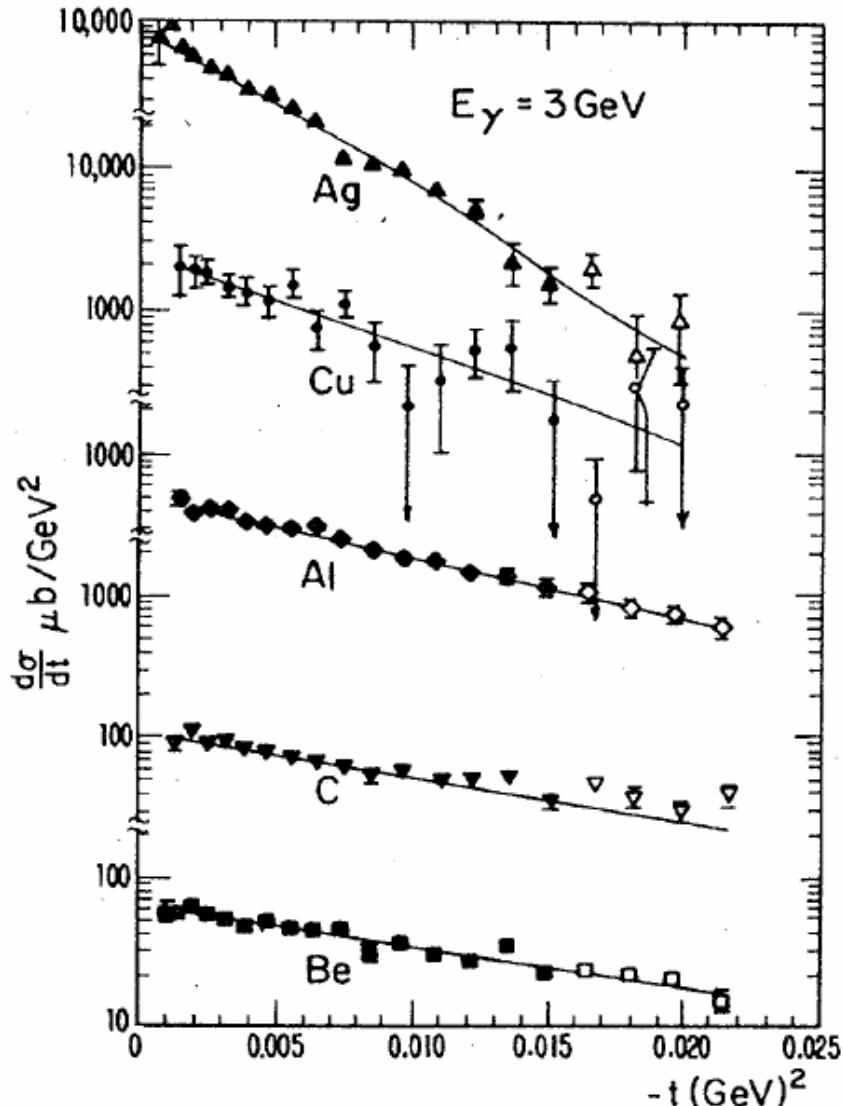
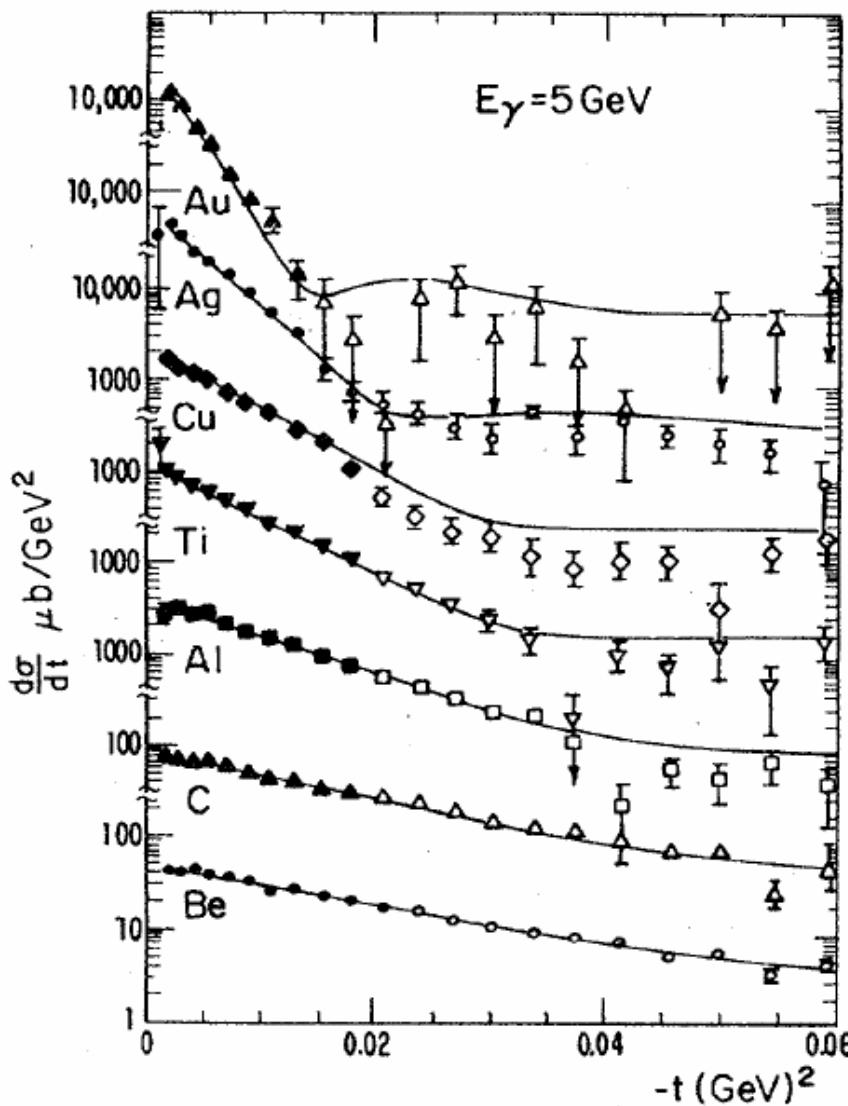
$$\vec{k}_3 = \vec{k}_0 - \vec{k}_1 - \vec{k}_2$$

$$E_{sep} = T_0 - (T_1 + T_2 + T_3)$$

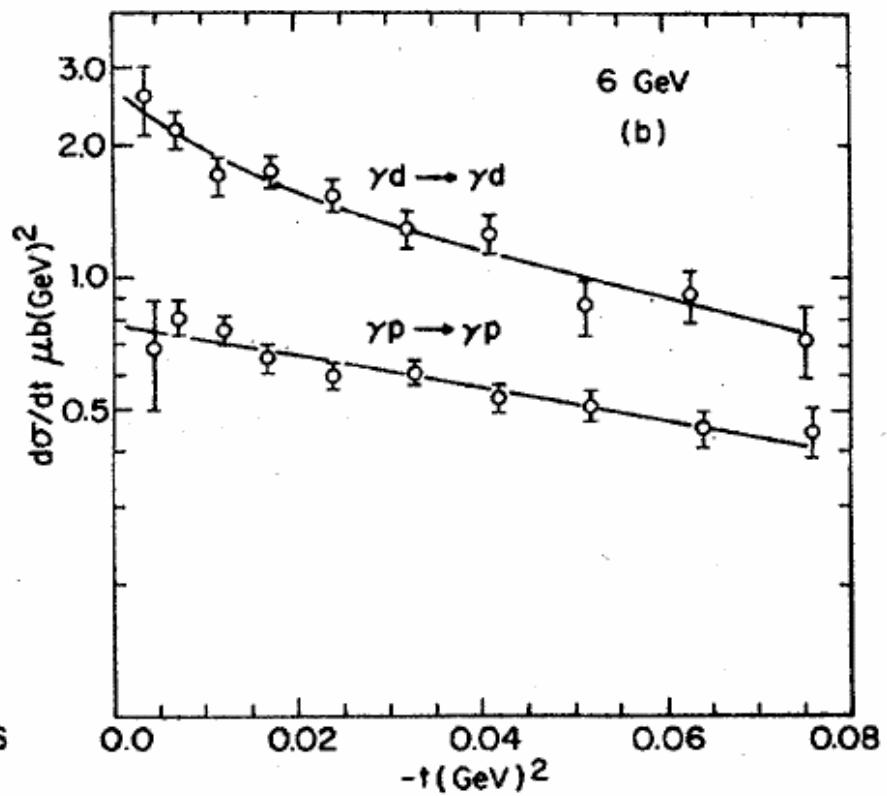
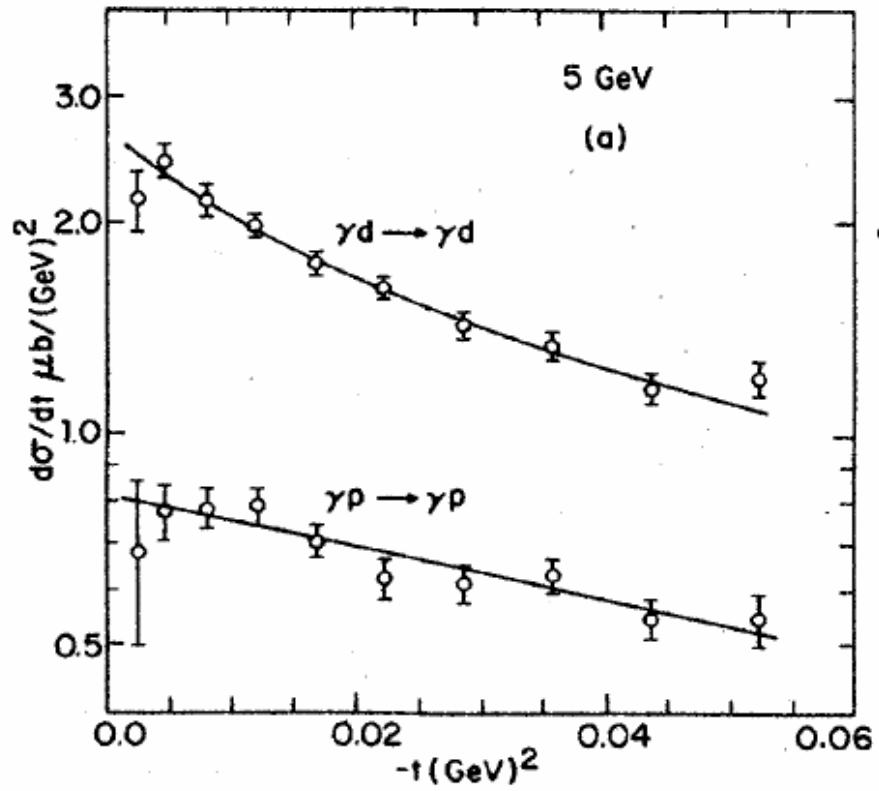
$\gamma p$      $\gamma p$  data above GeV energy (1960's-1970's)



# Compton scattering for nuclear target (coherent + incoherent)



$\gamma d$        $\gamma d$  data



after 1990, many precise  $\gamma p$        $\gamma p$  below 1 GeV  
→ Nucleon polarizability

# レーザー電子光によるクォーク核物理専用施設実行計画書 (平成8年)

## GeV領域偏極ガンマ線による陽子コンプトン散乱実験

### 1・実験提案者

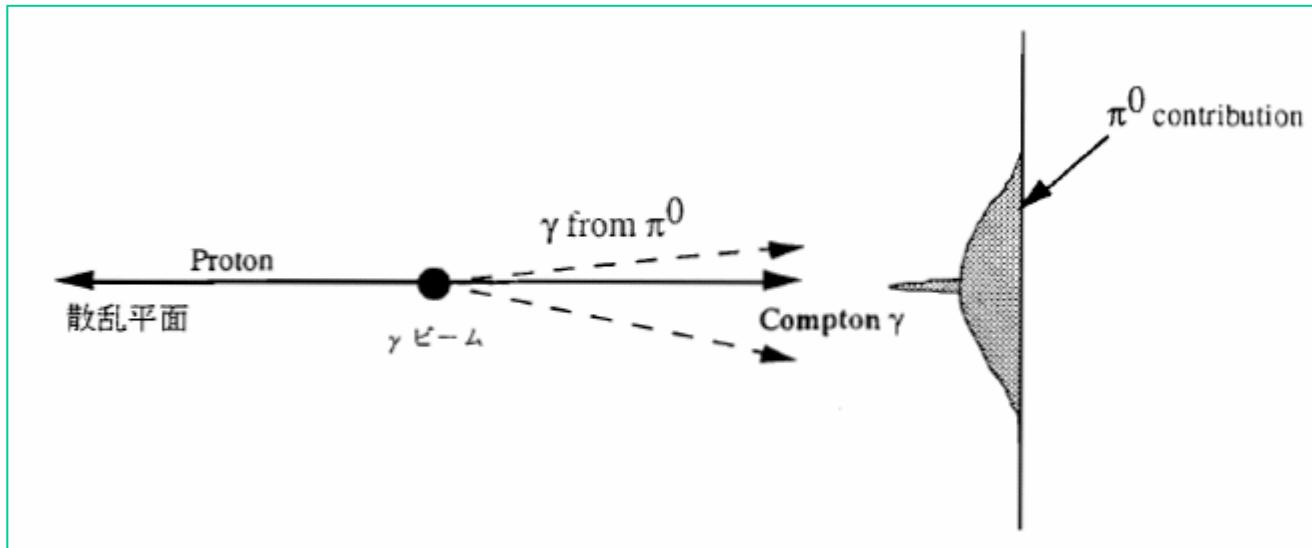
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### 2・目的：

GeV領域の偏極 $\gamma$ 線による陽子コンプトン散乱反応の断面積及び偏極分解能を測定し、核子構造を調べる。

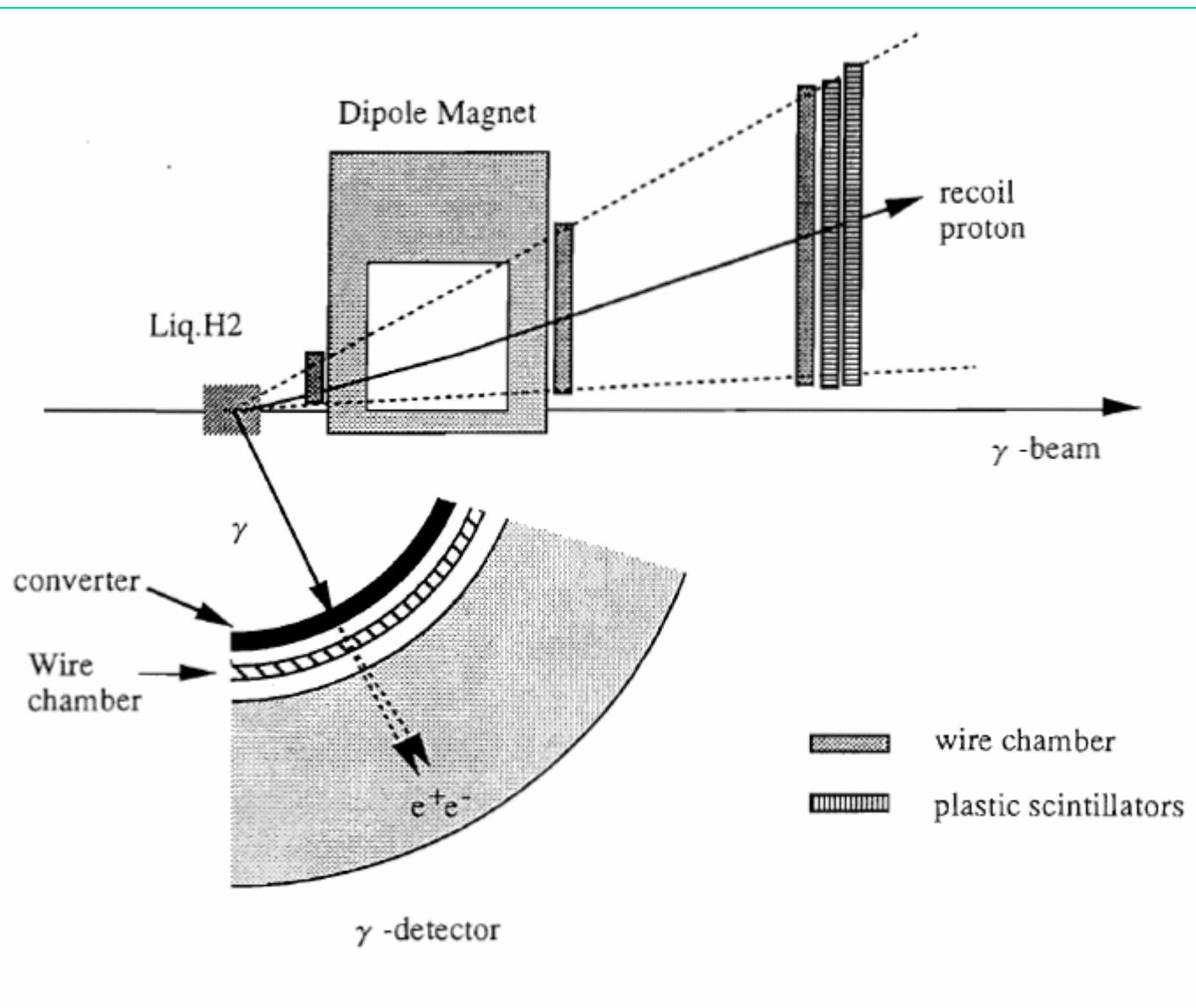
# Identification of Compton events

coincidence measurements of scattered- $\gamma$  and recoil-p



Co-planarity is important for Compton and  $\pi_0$  separation

# Detection system (by T.Suda)



## Yield estimation

- $d\sigma/d\Omega \sim 1 \text{ nb/sr}$
- $N_\gamma \sim 10^7 / \text{sec}$
- $N_t \sim 1 \text{ mol}$

$$\rightarrow Y = 0.006 \Delta\Omega \quad (\Delta\Omega \sim 1 \text{ sr})$$

need one order high intensity to divide  $E_\gamma$  into 10 energy bins