

# *Electric Dipole Response of Nuclei: Symmetry Energy and Neutron Skin*

*Neutrino*

Atsushi Tamii

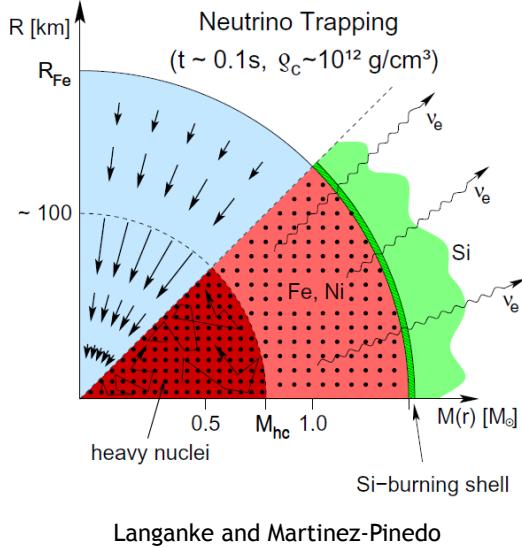
*Research Center for Nuclear Physics (RCNP)  
Osaka University, Japan*

On behalf of the RCNP Proton Inelastic Scattering Project Collaborators

Neutrinos, Electro-Weak interactions, and Symmetries  
(NEWS) Colloquium, June 20, 2019 at RCNP

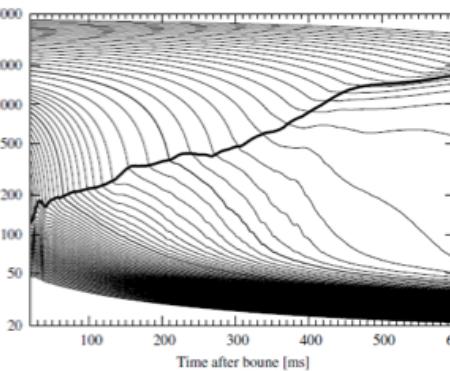
# Symmetry Energy of the Nuclear EOS is important for nuclear physics and nuclear-astrophysics

## Core-collapse supernova



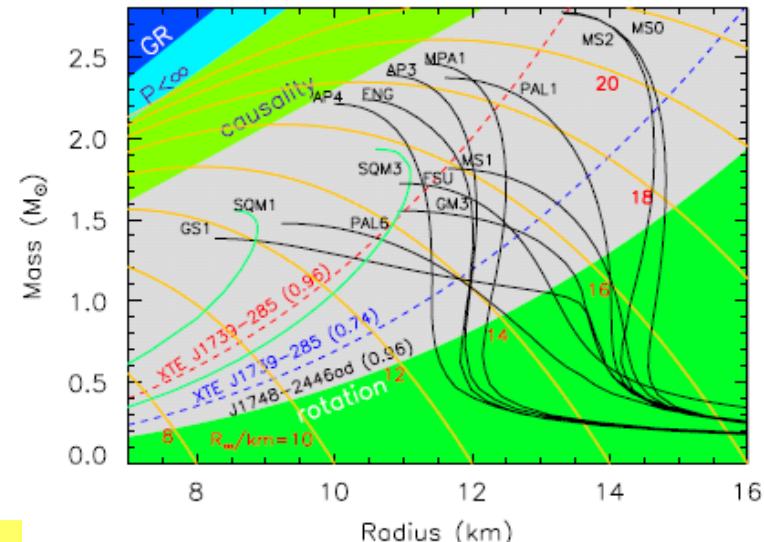
Langanke and Martinez-Pinedo

## Nucleosynthesis



Y. Suwa et al., ApJ764, 99 (2013).

## Neutron star mass vs radius

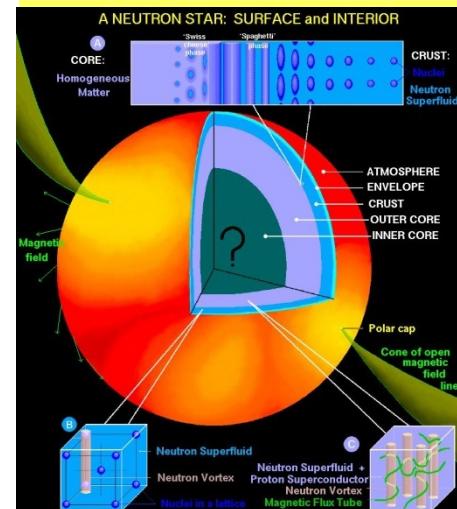


Lattimer et al., Phys. Rep. 442, 109(2007)

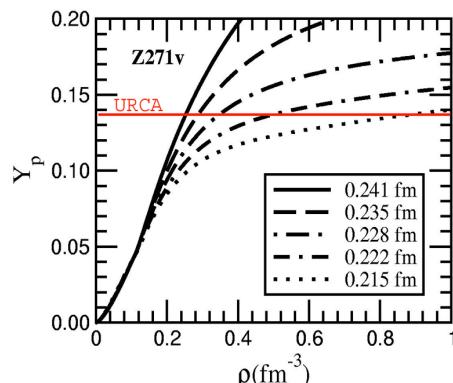
## Neutron Star Merger Gravitational Wave



## Neutron star structure



## Neutron star cooling



Lattimer and Prakash, Science 304, 536 (2004).

# Nuclear Equation of State (EOS) at zero temperature

## Nuclear EOS neglecting Coulomb

$$\frac{E}{A}(\rho, \delta) = \frac{E}{A}(\rho, 0) + S(\rho)\delta^2 + \dots$$

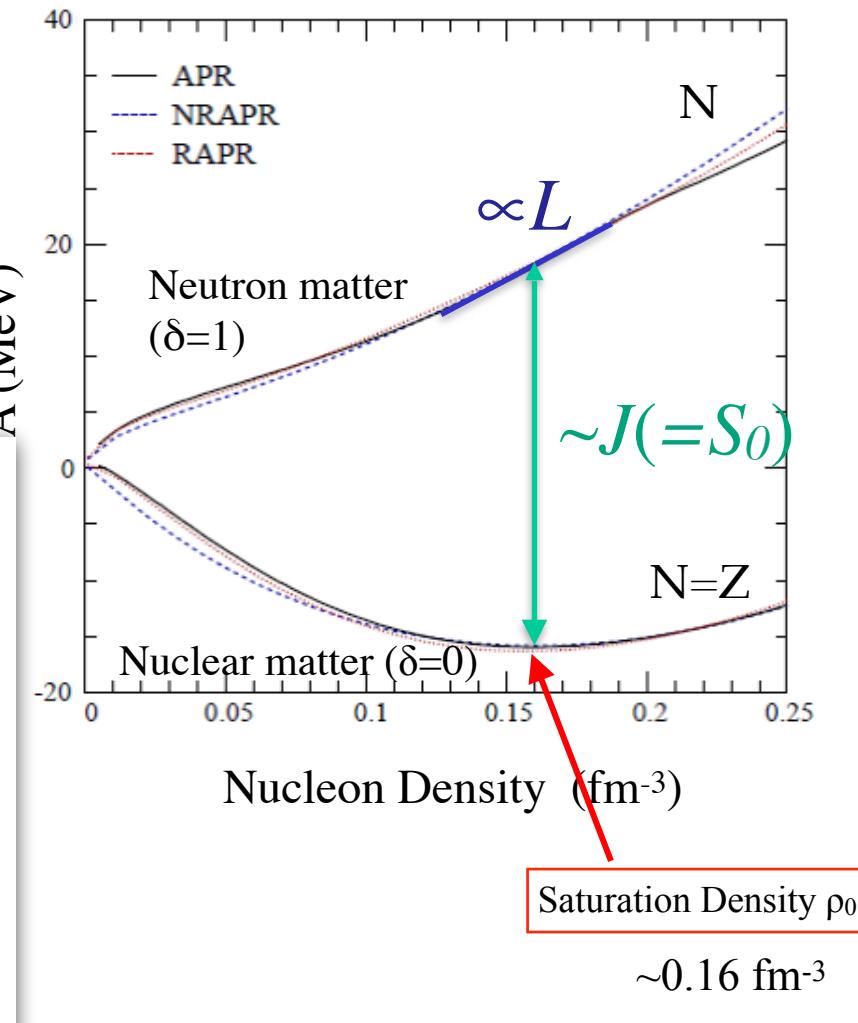
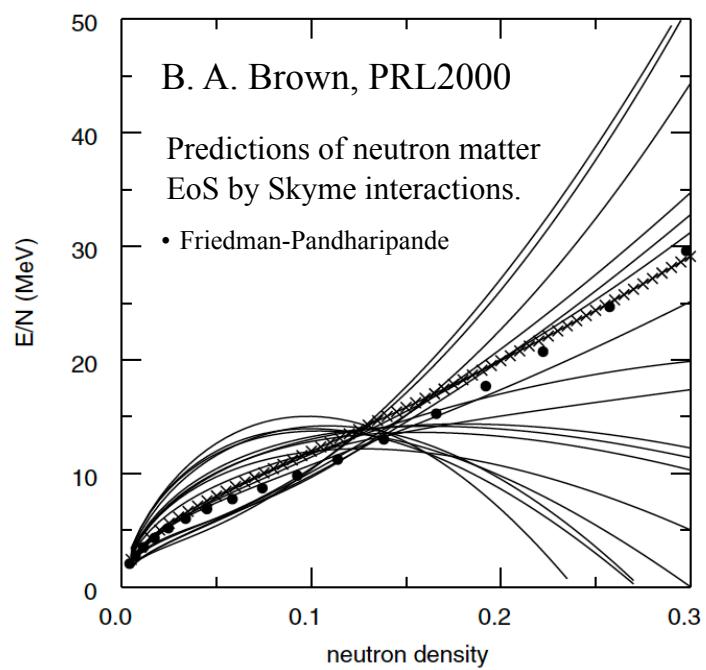
$$\delta \equiv \frac{\rho_n - \rho_p}{\rho_n + \rho_p} \quad \text{Asymmetry parameter}$$

# ~~Symmetry energy~~

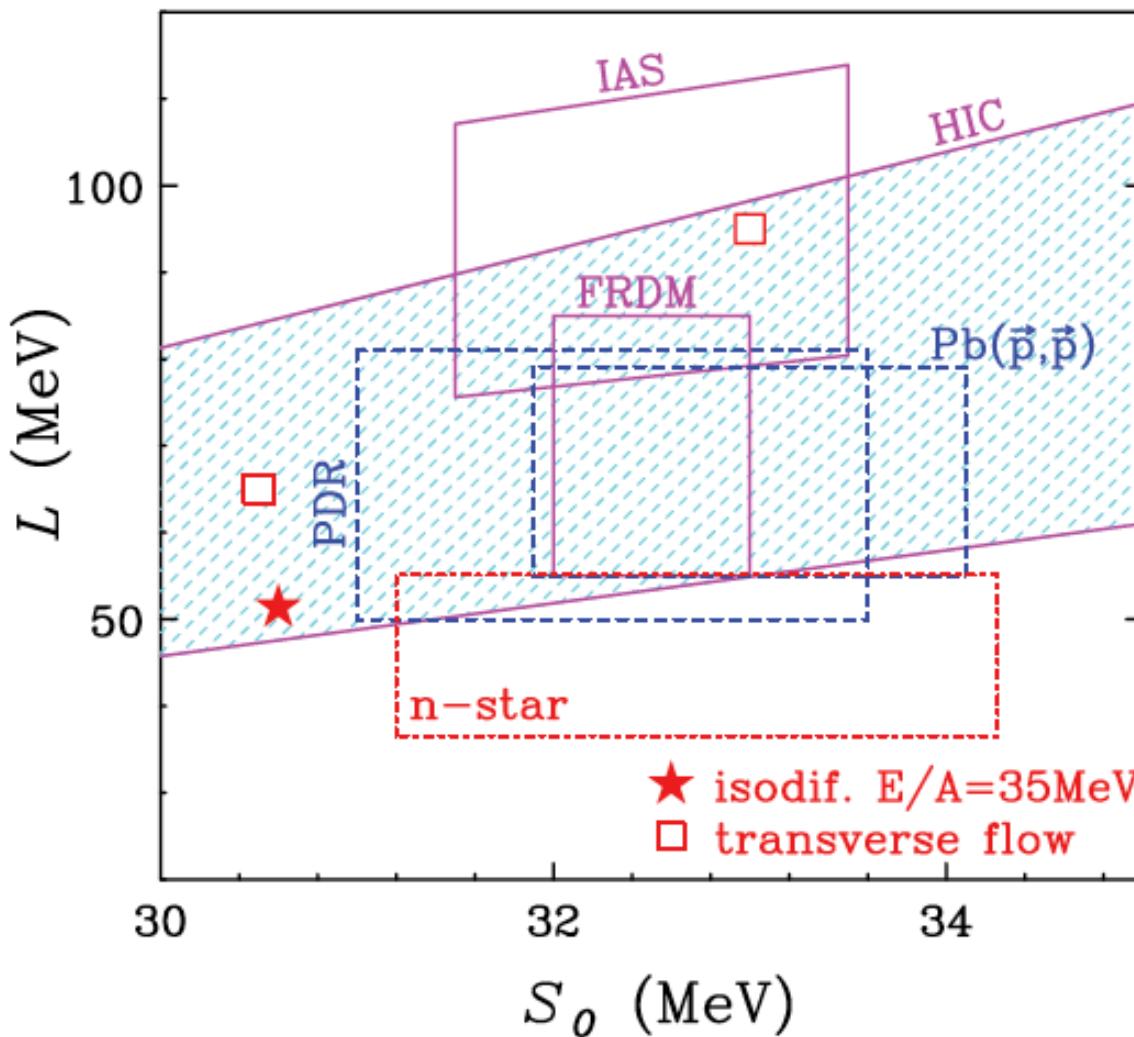
$$S(\rho)$$

$\Leftrightarrow$  difference  
how the sys  
are replaced

Nuclei



# Constraints on $J$ and $L$



M.B. Tsang et al., PRC2012

HIC: Heavy Ion Collision Analysis  
Tsang PRL2009

IAS: Isobaric Analog State Energy  
Danielewicz&Lee NPA2009

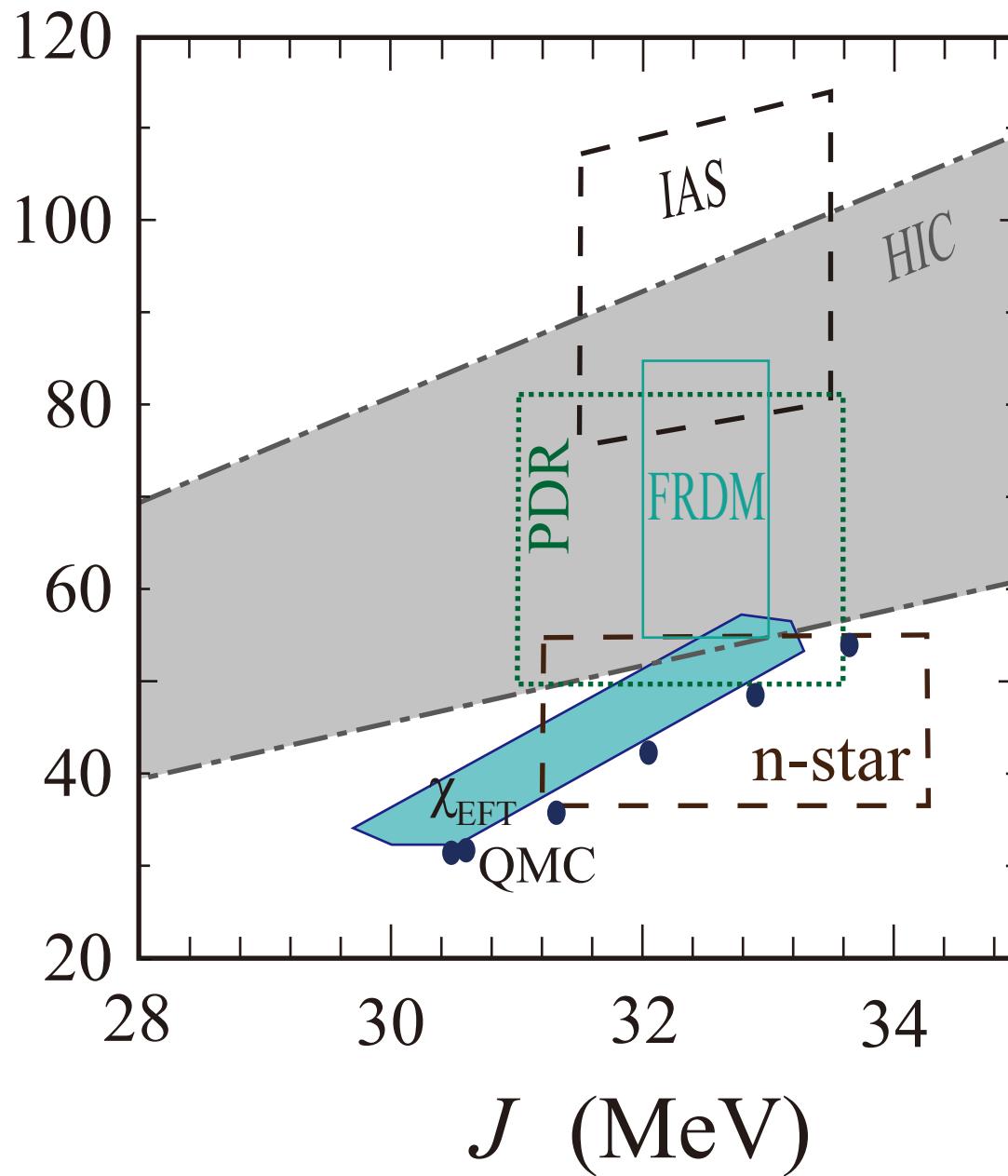
PDR: Pygmy Dipole Resonance in  
 $^{132}\text{Sn}$ ,  $^{68}\text{Ni}$ , Carbone PRC2010

FRDM: Finite Range Droplet Model  
Moeller PRL2012

n-star: Quiescent Low-Mass X-ray  
Binaries, Stainer PRL2012

Pb( $\vec{p},\vec{p}$ ): proton elastic scattering  
J. Zenihiro et al., PRC2010

# Constraints on $J$ and $L$



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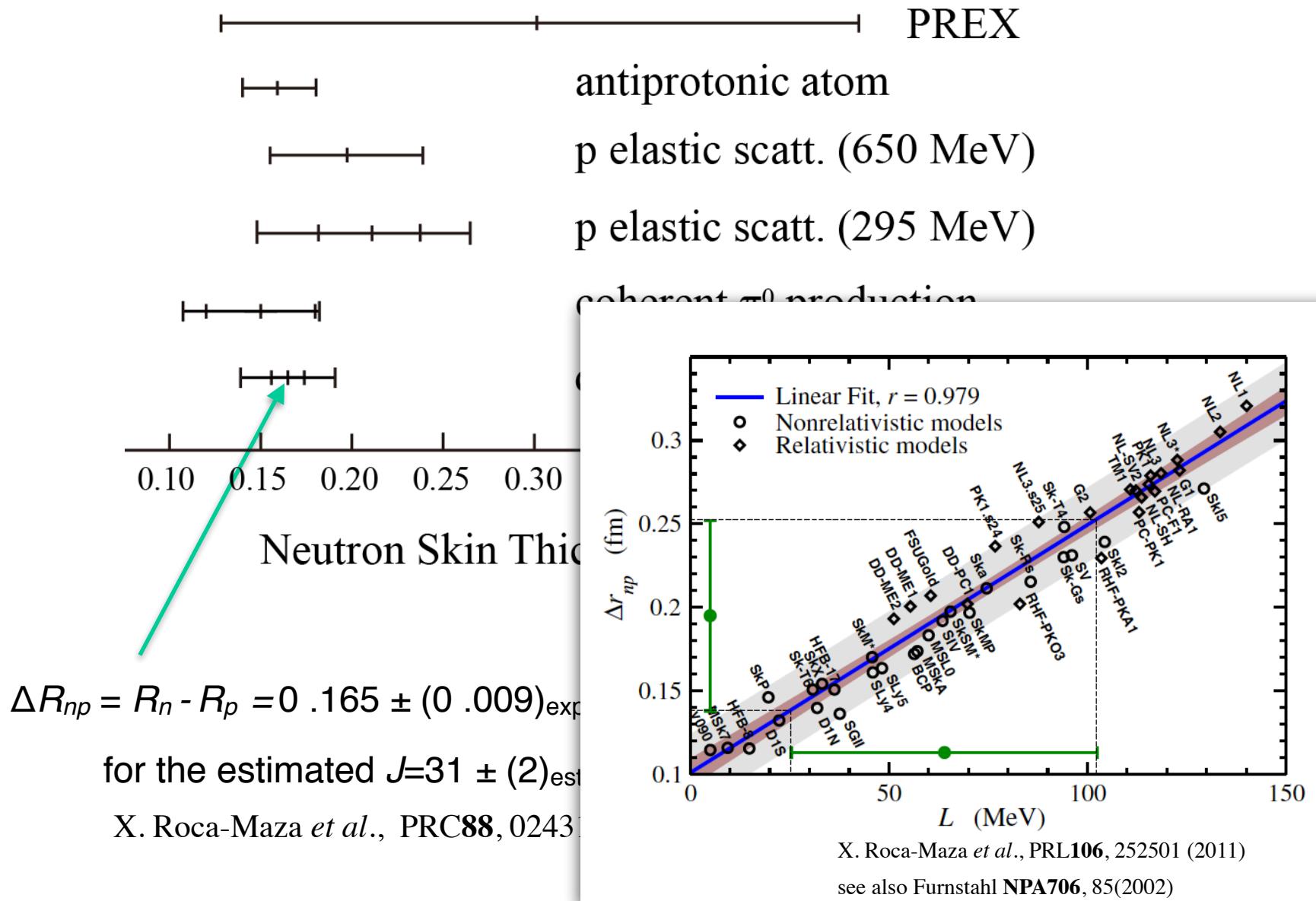
FRDM: Finite Range Droplet Model  
Moeller PRL2012

n-star: Quiescent Low-Mass X-ray  
Binaries, Stainer PRL2012

$\chi_{\text{EFT}}$ : Chiral Effective Field Theory,  
Tews PRL2013

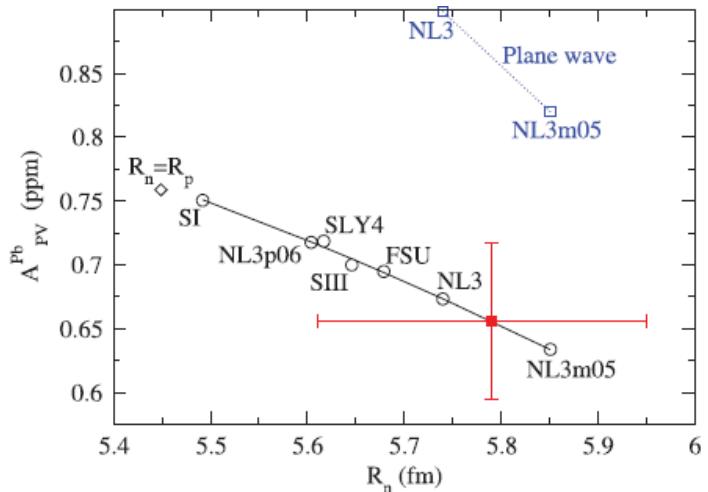
QMC: Quantum Monte-Carlo Calc.  
Gandolfi, EPJA50, 10(2014).

# Neutron Skin Thickness of $^{208}\text{Pb}$



# Parity Violating Electron Weak-Scattering from $^{208}\text{Pb}$ (PREX@J-Lab) for Neutron-Skin Thickness and $L$

S. Abrahamyan et al., PRL108, 112502 (2012)

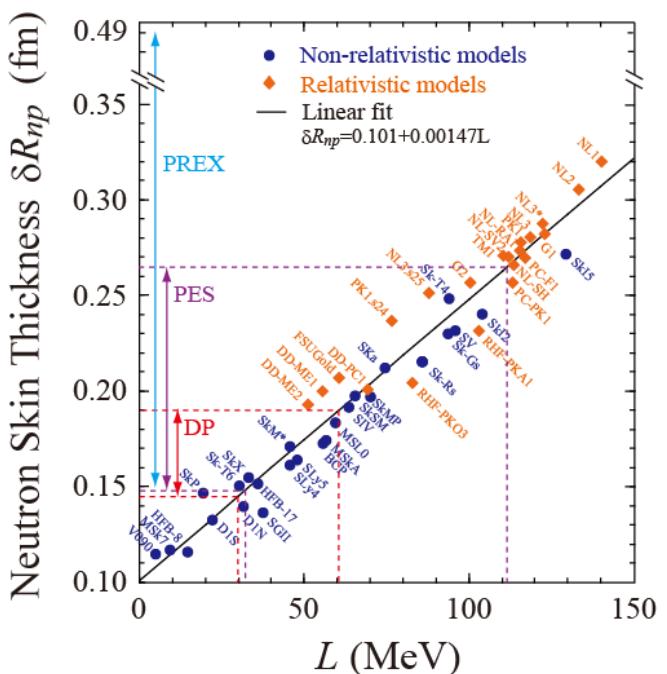


$$R_n = 5.78^{+0.16}_{-0.18} \text{ fm}$$

$$R_n - R_p = 0.33^{+0.16}_{-0.18} \text{ fm}$$

$$R_n - R_p = 0.302 \pm 0.175 \text{ (exp)} \pm 0.026 \text{ (mod)} \pm 0.005 \text{ (str)} \text{ fm.}$$

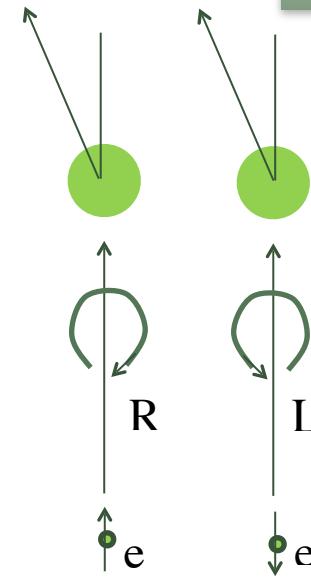
C.J. Horowitz et al., PRC85,032501(R)(2012)



Predictions from X. Roca-Maza *et al.*, PRL106, 252501 (2011)

PREX-II and C-REX in ~2019

Lead ( $^{208}\text{Pb}$ ) Radius  
Experiment: PREX



“Model independent” determination of the neutron radius of  $^{208}\text{Pb}$ .



Jefferson Laboratory Hall-A

by Adrian Cho on 2 March 2012

## Science Now

...

Nailing down such parameters would have equally big implications for the theory of neutron stars, says James Lattimer, a theoretical astrophysicist at Stony Brook University in New York state. "That directly tells you the radius of a neutron star [of a given mass] and a lot of other things like the thickness of its crust, the response of its surface to explosions, et cetera," Lattimer says.

Alas, the uncertainty on the PREX measurement is still too large to pin down the parameters, Lattimer says. "It's a very important experiment and has the potential to constrain theory very nicely, but it's not there yet," he says. JLab's Michaels says the PREX team will run the experiment next year and aims to reduce the uncertainty to one-third its current value. "Then it becomes a very interesting result," he says.

Something else physicists will be watching for: The PREX measurement suggests that the neutron skin of lead-208 is twice as thick as more-precise but model-dependent methods indicate. Right now, the PREX result has too much uncertainty to pose a direct challenge to earlier estimates. But if the new value holds up as the uncertainty shrinks, things could get really interesting, Nazarewicz says: "Then, there is something wrong with all theoretical models." There's a possibility to set your skin a-tingling.

# Outline of Our Work

## Purpose

Symmetry energy of nuclear EOS at  $\leq \rho_0$



## Method

An observable that is sensitive to the density difference between  $p$  and  $n$  in heavy nuclei



## Experiment

Measured electric dipole response of Nuclei



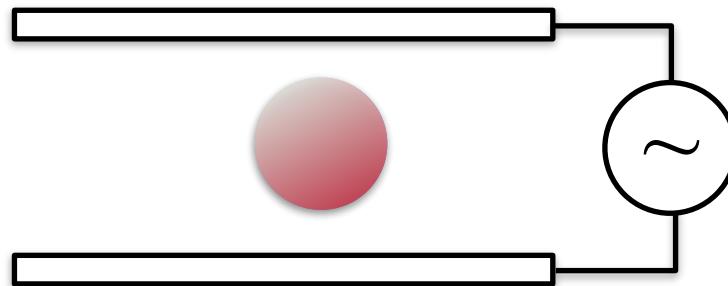
## Results

Constraints on symmetry energy

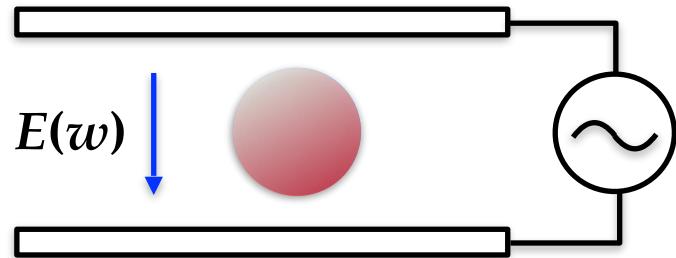
$N \gtrsim Z$   
 $\rho \lesssim \rho_0$   
 $T=0$   
 $p$  and  $n$

Ordinary nuclear matter  
Starting point to further exotic conditions

# Electric Dipole Response of Nuclei and the Nuclear Symmetry Energy

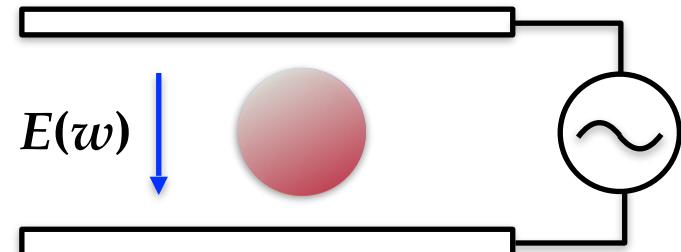
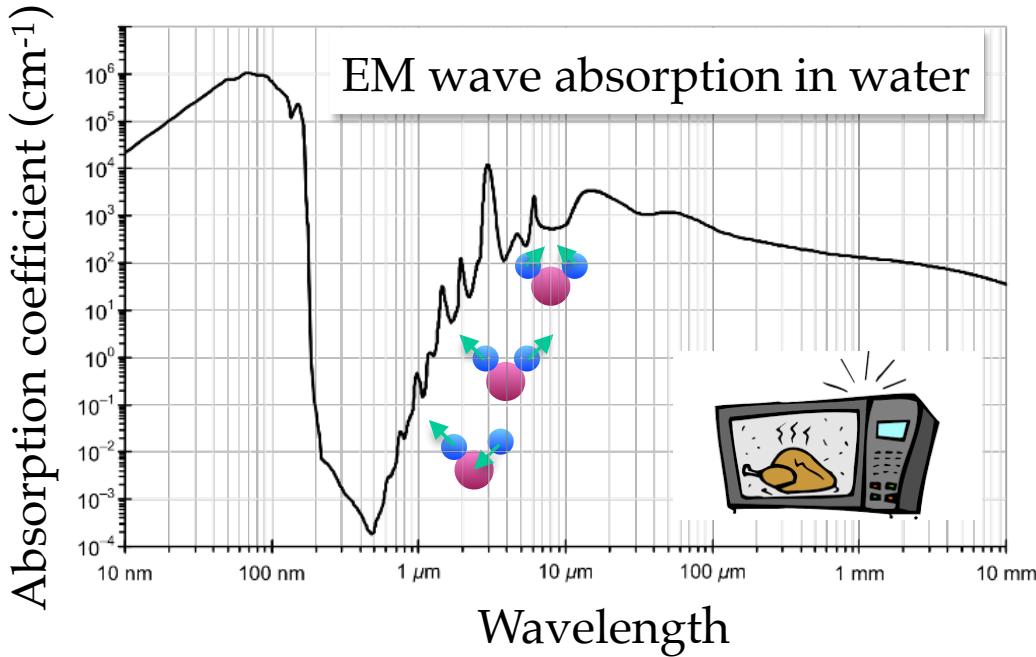


# Electric Dipole Response of Nuclei



dielectric material  
in an oscillating electric field

# Electric Dipole Response of Nuclei



dielectric material  
in an oscillating electric field

# Electric Dipole Response of Nuclei

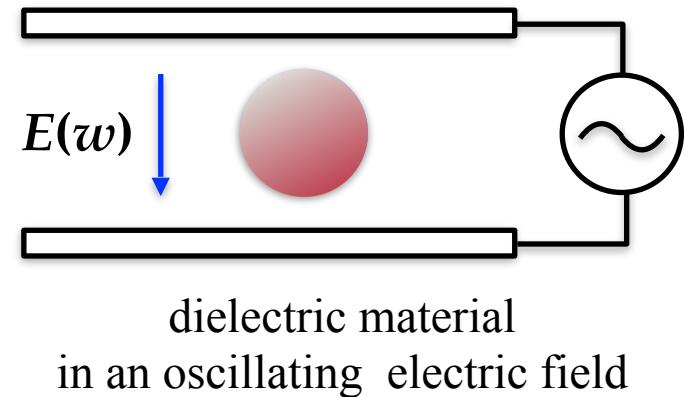
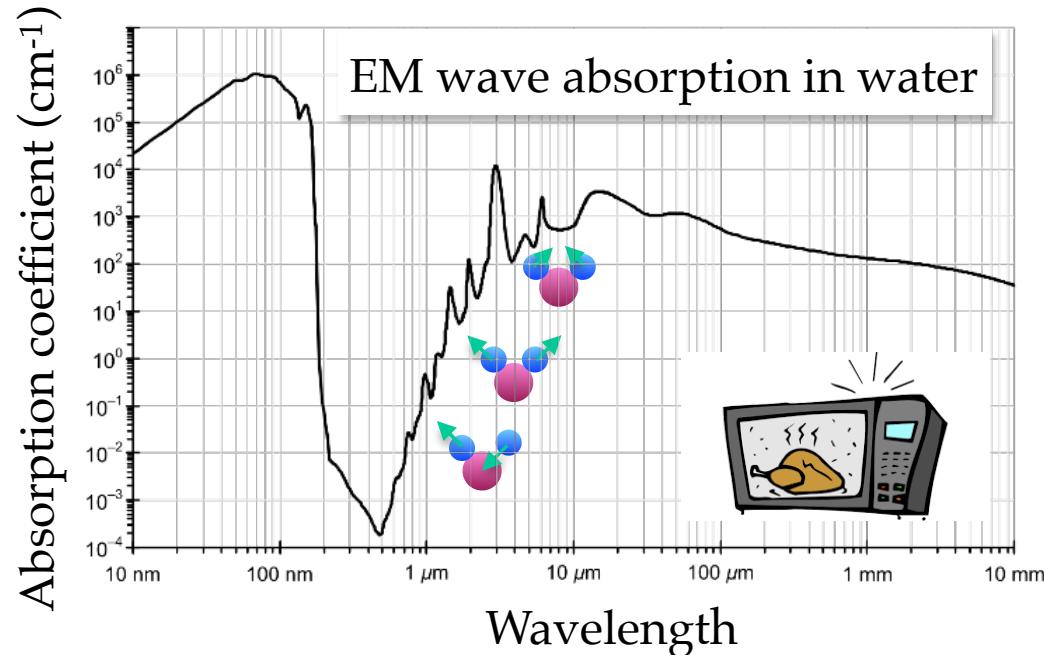
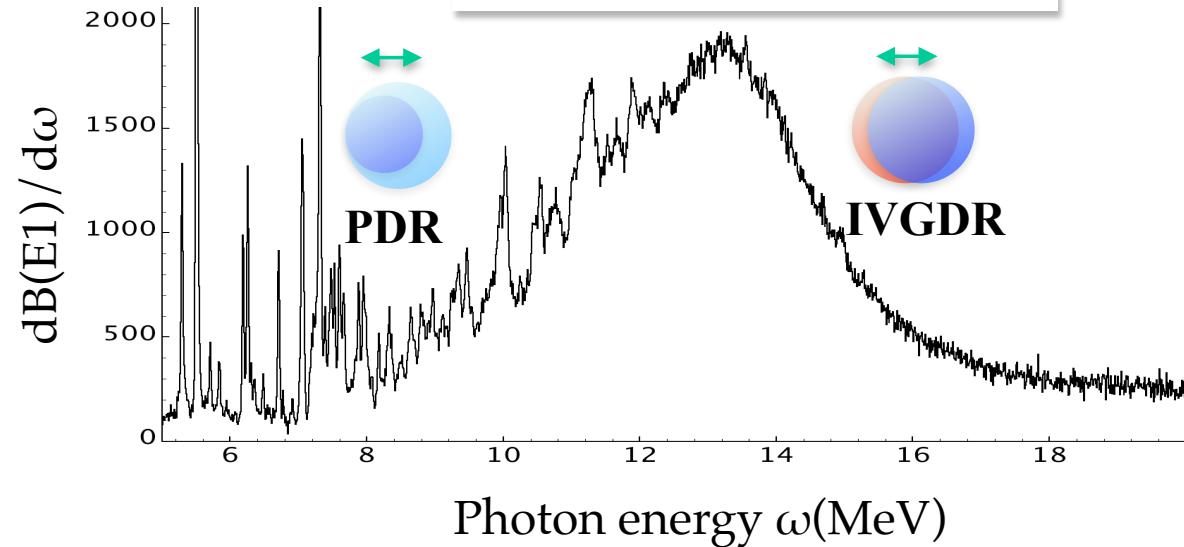


Photo-absorption by  $^{208}\text{Pb}$

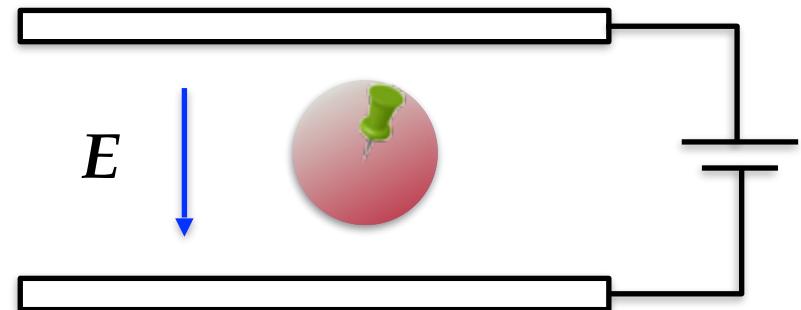


# Static Electric Dipole Polarizability ( $\alpha_D$ )

Electric dipole moment

$$p = \alpha_D \times E$$

$\alpha_D$ : electric dipole polarizability



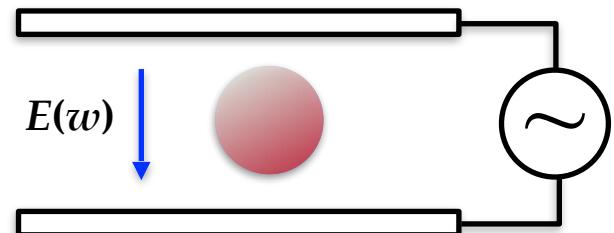
nucleus

in a static electric field  
with fixing the c.m. position

Inversely energy-weighted sum-rule of  $B(E1)$

$$\alpha_D = \frac{8\pi e^2}{9} \int \frac{dB(E1)}{E_x}$$

first order perturbation calc. A.B. Migdal: 1944



# Static Electric Dipole Polarizability ( $\alpha_D$ )

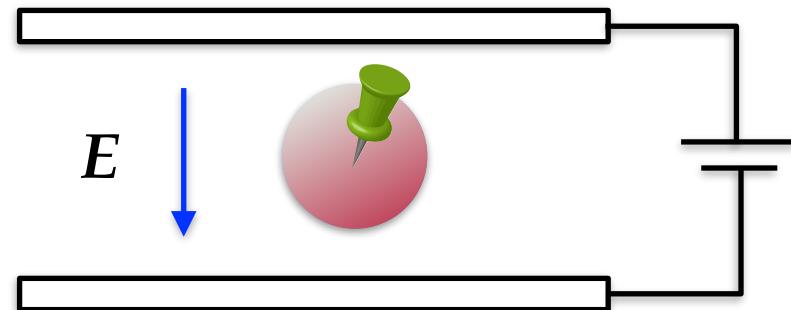
Electric dipole moment

$$p = \alpha_D \times E$$

$\alpha_D$ : electric dipole polarizability



The **restoring force** originates from the **symmetry energy**.



nucleus

in a static electric field  
with fixing the c.m. position

Electric dipole polarizability (EDP) is sensitive to the symmetry energy below the nuclear saturation density and to the neutron skin thickness.

# Nuclear Equation of State (EOS) at zero temperature

Nuclear EOS neglecting Coulomb

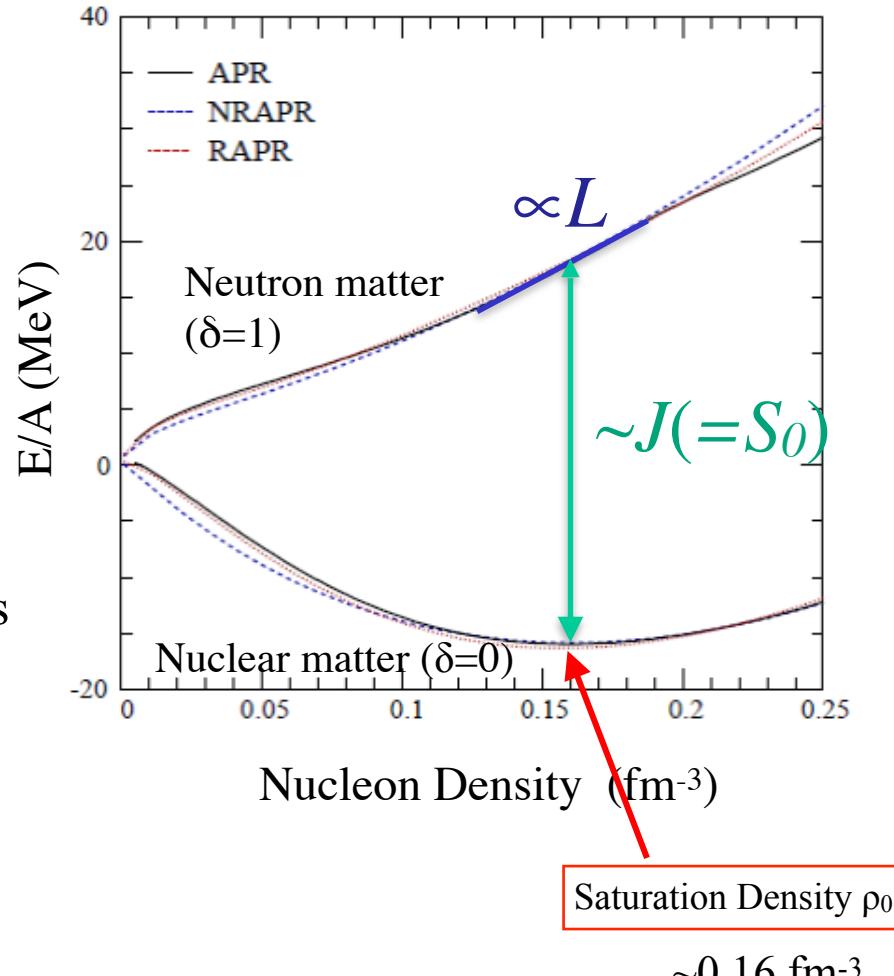
$$\frac{E}{A}(\rho, \delta) = \frac{E}{A}(\rho, 0) + S(\rho)\delta^2 + \dots$$

$$\delta \equiv \frac{\rho_n - \rho_p}{\rho_n + \rho_p} \quad \text{Asymmetry parameter}$$

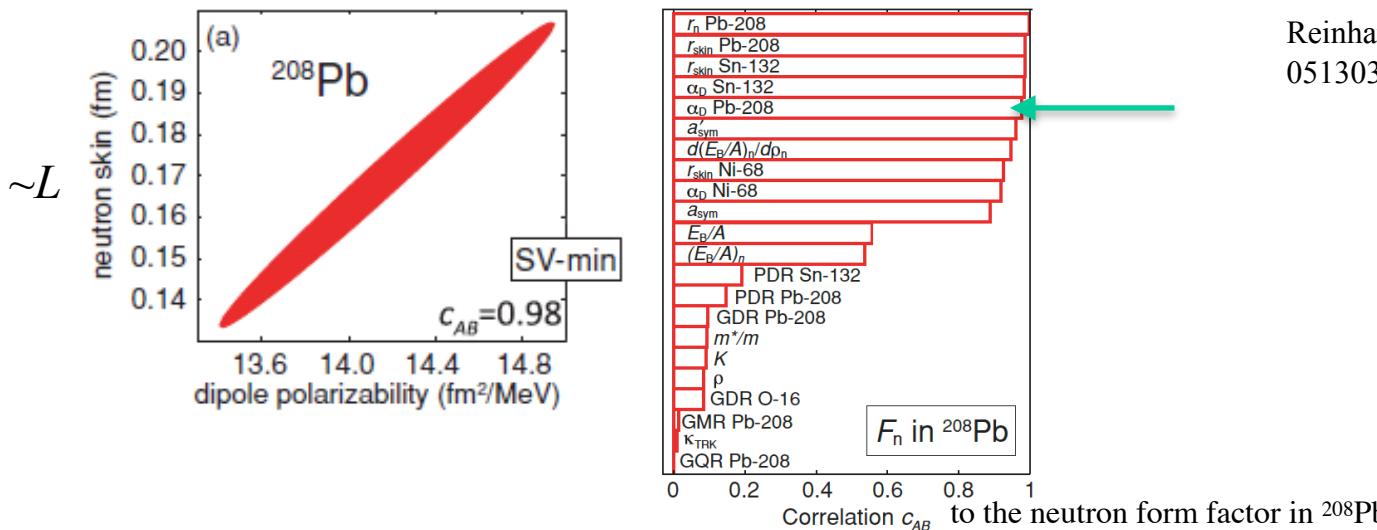
Symmetry energy

$$S(\rho) = J - \frac{L}{3\rho_0}(\rho - \rho_0) + \dots$$

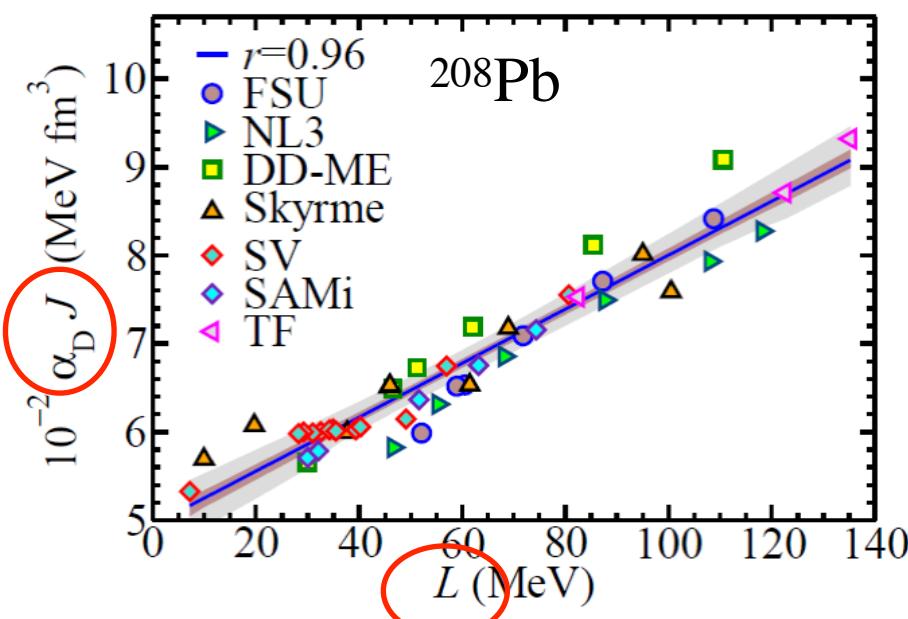
Density difference between  $n$  and  $p$  increases the system energy by the symmetry energy.



# Electric Dipole Polarizability ( $\alpha_D$ ) in the correlation of $J$ and $L$



Reinhard and Nazarewicz, PRC81,  
051303(R) (2010)



X. Roca-Maza *et al.*, PRC88, 024316(2013)

Correlations observed in various interaction sets in the framework of EDF.

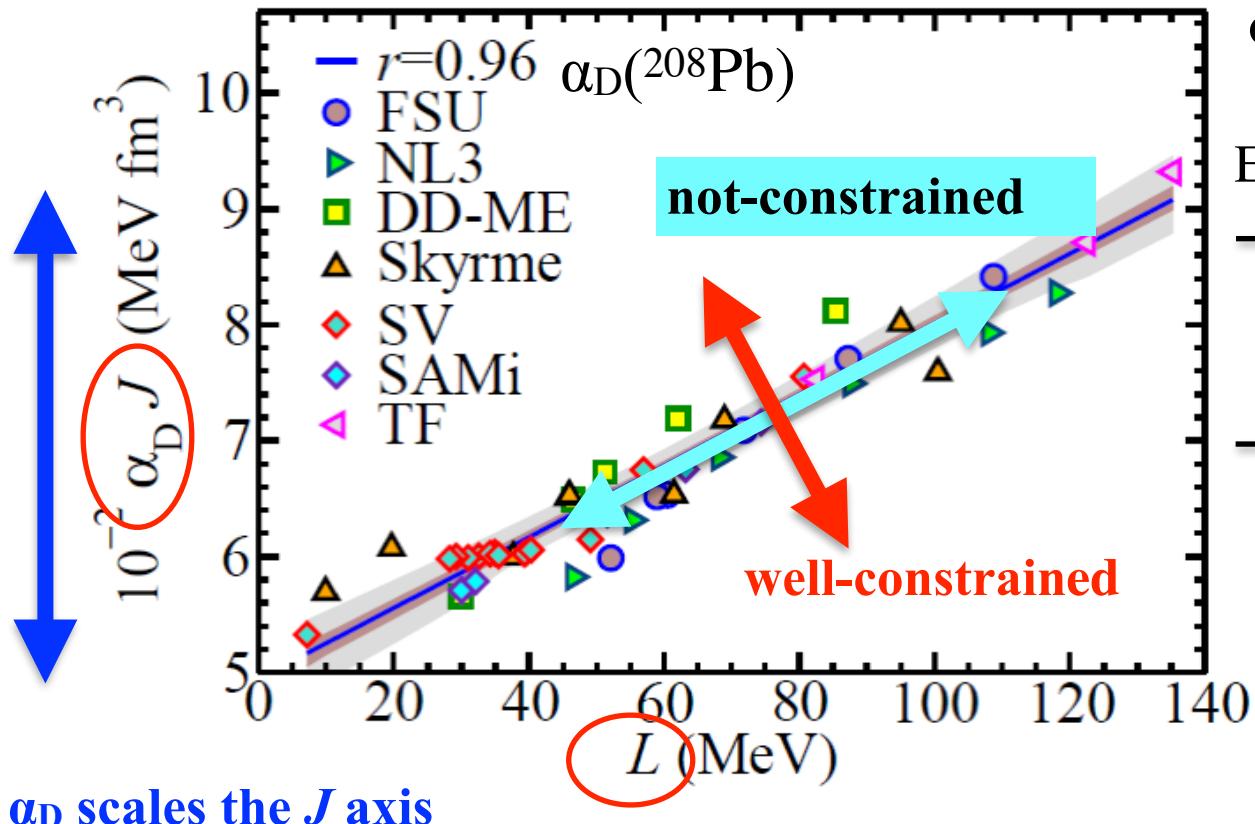
$$\alpha_D^{\text{DM}} \approx \frac{\pi e^2}{54} \frac{A \langle r^2 \rangle}{J} \left[ 1 + \frac{5}{3} \frac{L}{J} \epsilon_A \right]$$

insights from the droplet model

Precise determination of  $\alpha_D$  of  $^{208}\text{Pb}$  gives a constraint band in the  $J$ - $L$  plane.

# Electric Dipole Polarizability ( $\alpha_D$ ) in the correlation of $J$ and $L$

X. Roca-Maza *et al.*, PRC88, 024316(2013)



$\alpha_D$  scales the  $J$  axis.

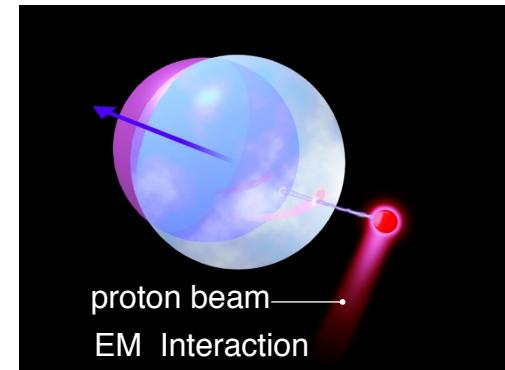
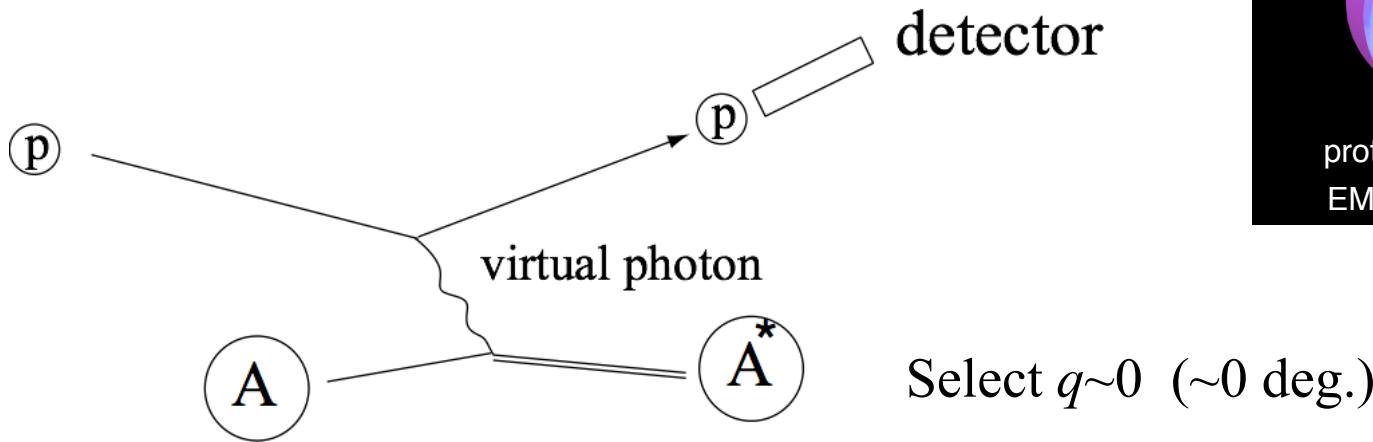
Effective Interactions

- reproduce e.g. nuclear masses and charge radii of representative nuclei
- constrained in one direction but not in the other

One of the unknowns,  $\alpha_D$ , has been determined experimentally to extract the constraint band in the  $J-L$  plane.

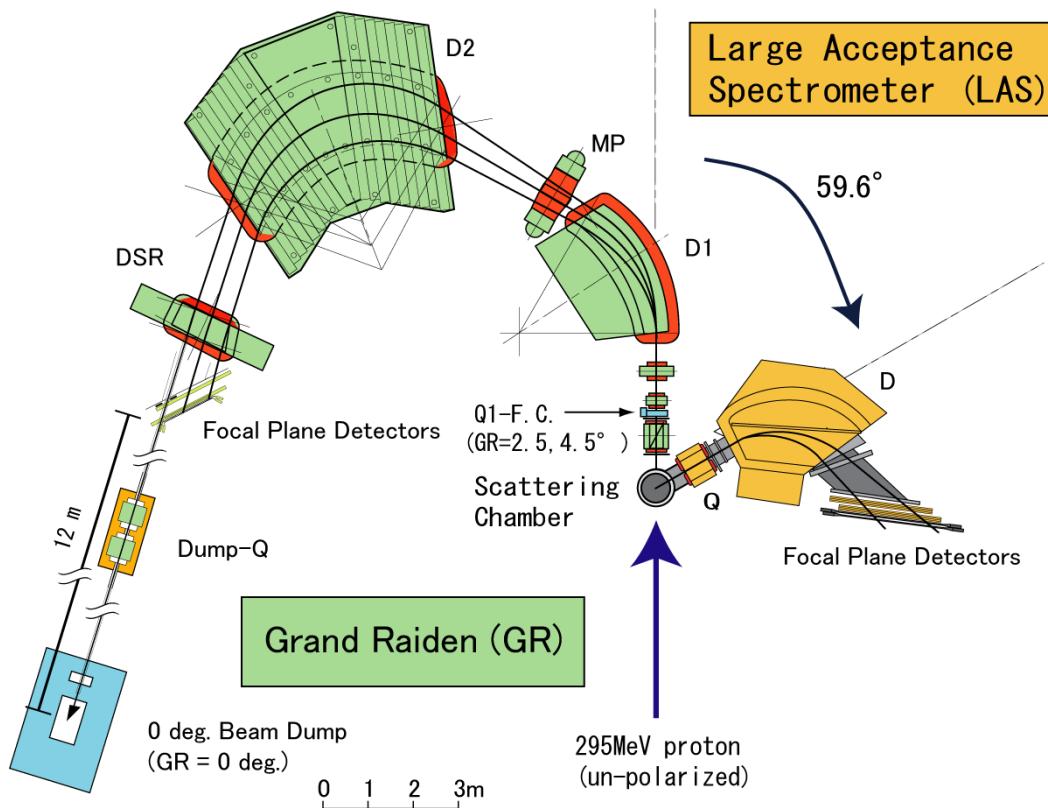
# Probing the E1 Response by Proton Scattering

## Missing Mass Spectroscopy by Virtual Photon Excitation



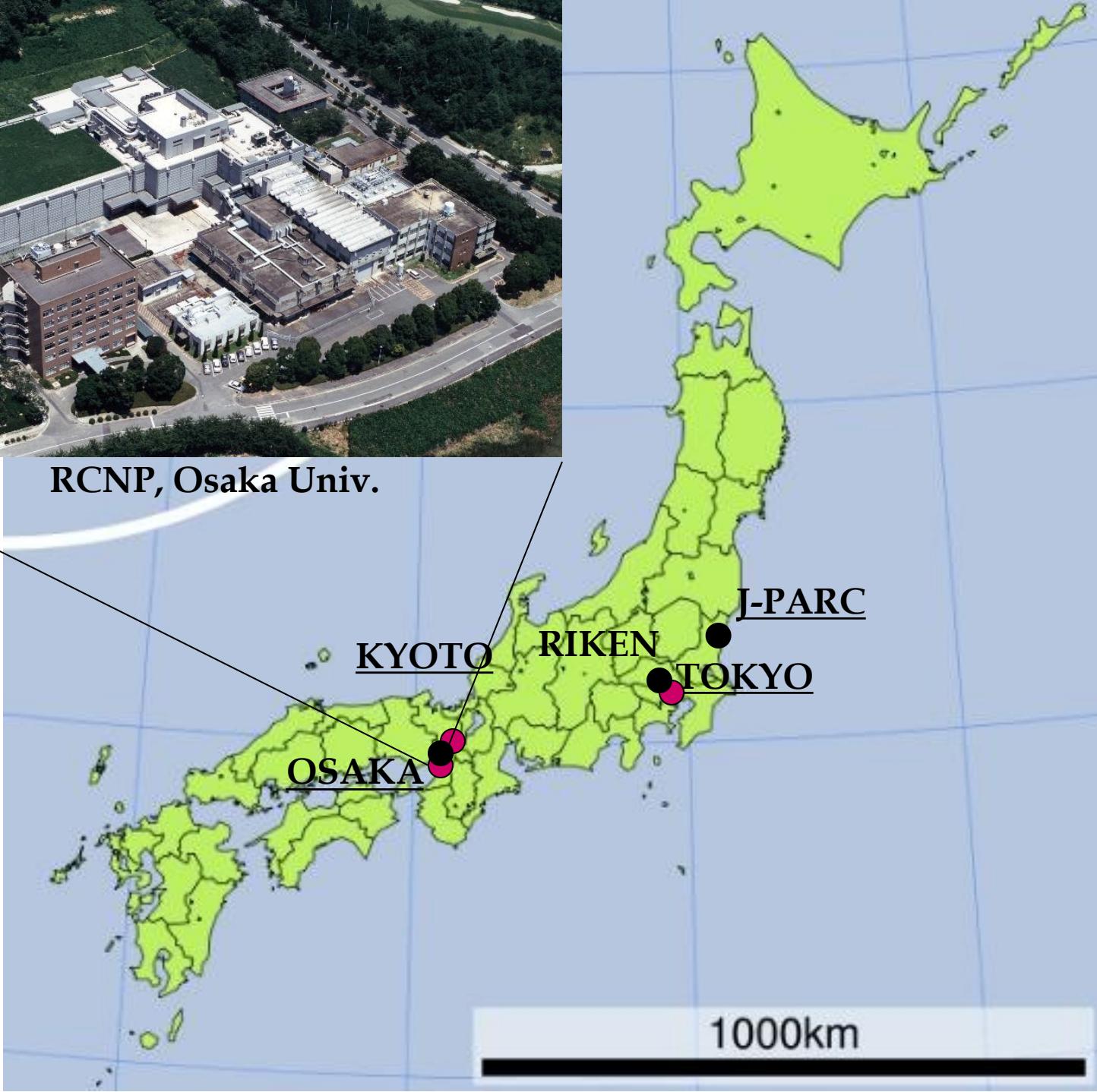
- **Missing mass spectroscopy:**  
Total strength is measured independently from the decaying channels.
- **Multipole decomposition** of the strength in the continuum:  
Includes the contribution of unresolved small states
- **Coulomb excitation:** EM Interaction  
Absolute determination of the transition strength.

# Experimental Methods



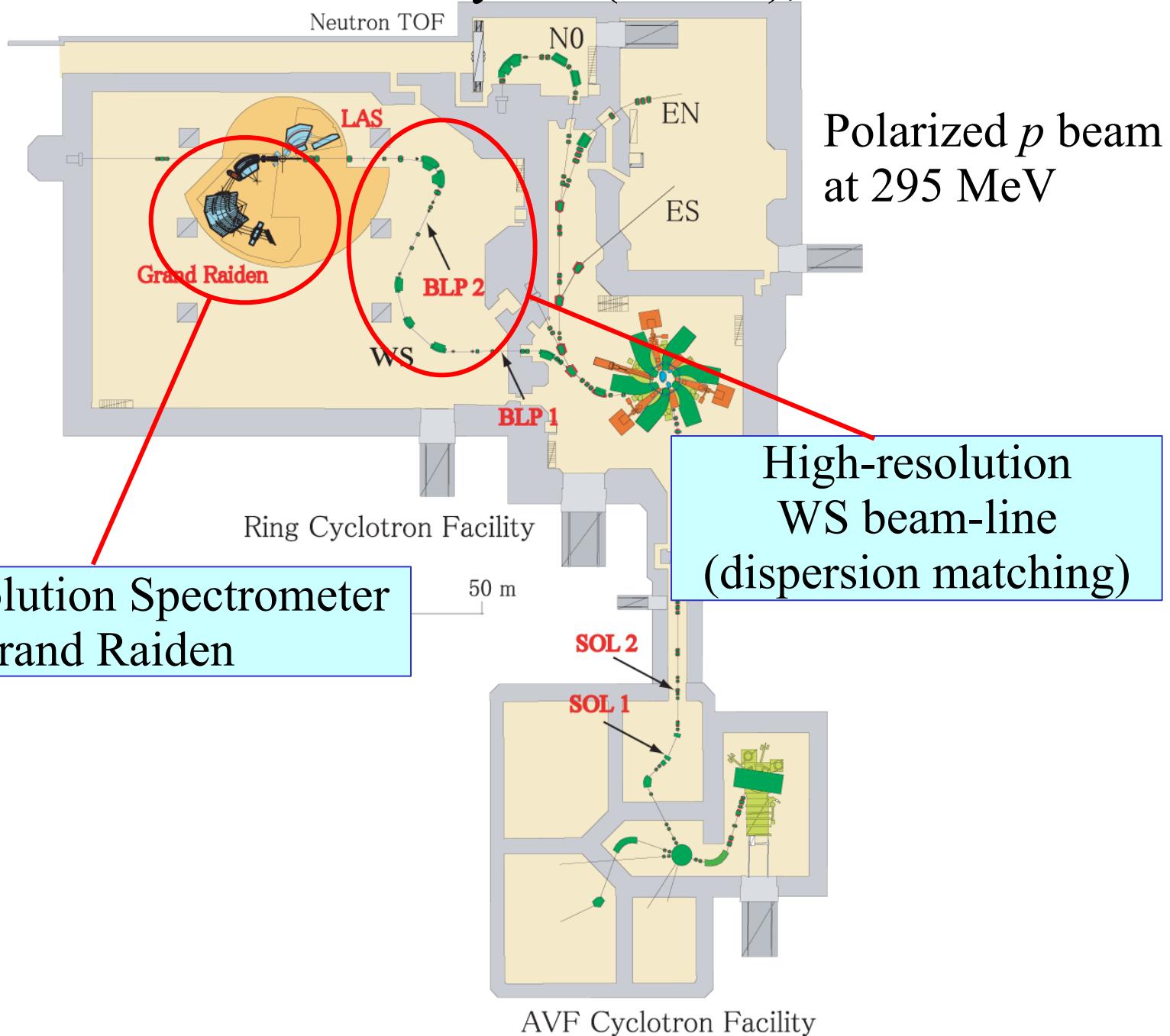


RCNP, Osaka Univ.



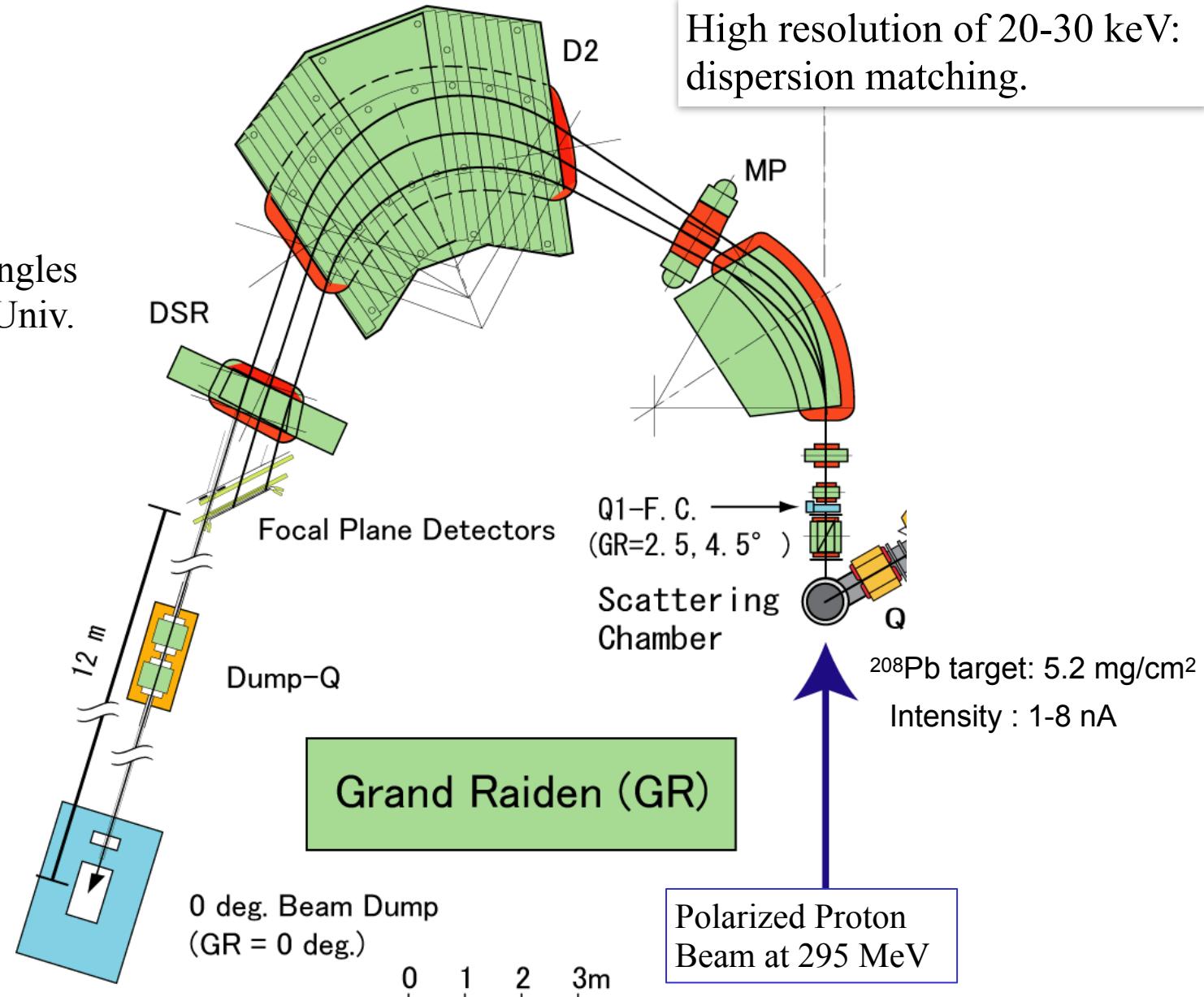
1000km

# Research Center for Nuclear Physics (RCNP), Osaka University



# High-Resolution Spectrometer “Grand Raiden”

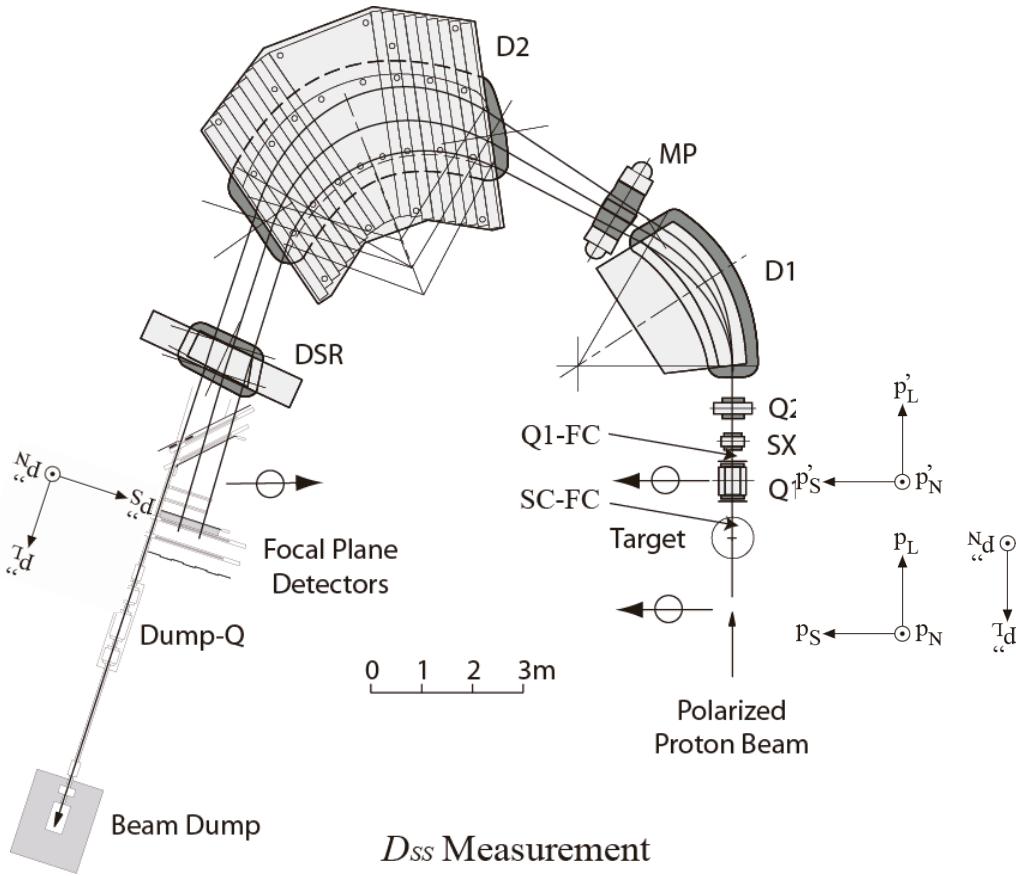
Proton scattering  
at very forward angles  
at RCNP, Osaka Univ.



# Spin Precession in the Spectrometer

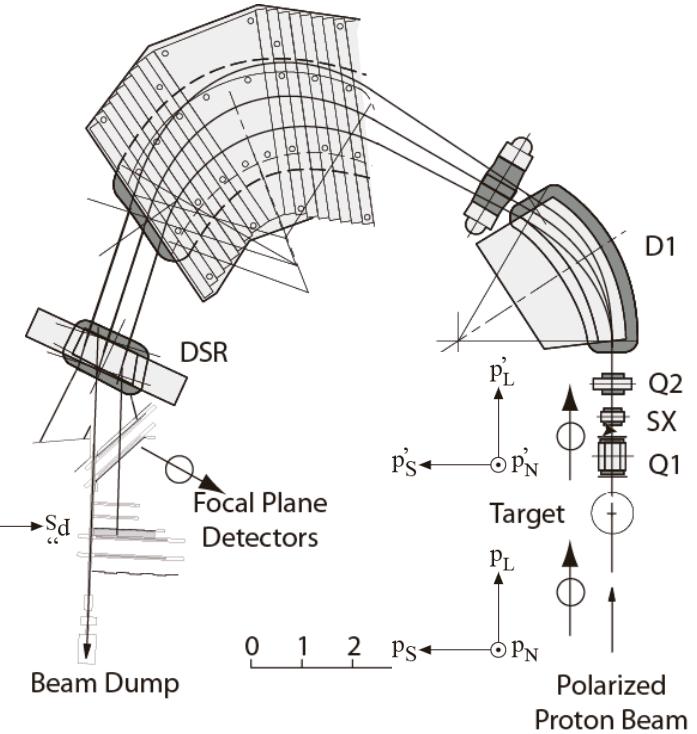
$$\theta_p = \gamma \left( \frac{g}{2} - 1 \right) \theta_b$$

$\theta_p$ : precession angle with respect to the beam direction  
 $\theta_b$ : bending angle of the beam  
 $g$ : Lande's g-factor  
 $\gamma$ : gamma in special relativity



$$\theta_b \approx 162^\circ$$

$D_{ss}$  Measurement



$$\theta_b \approx 180^\circ$$

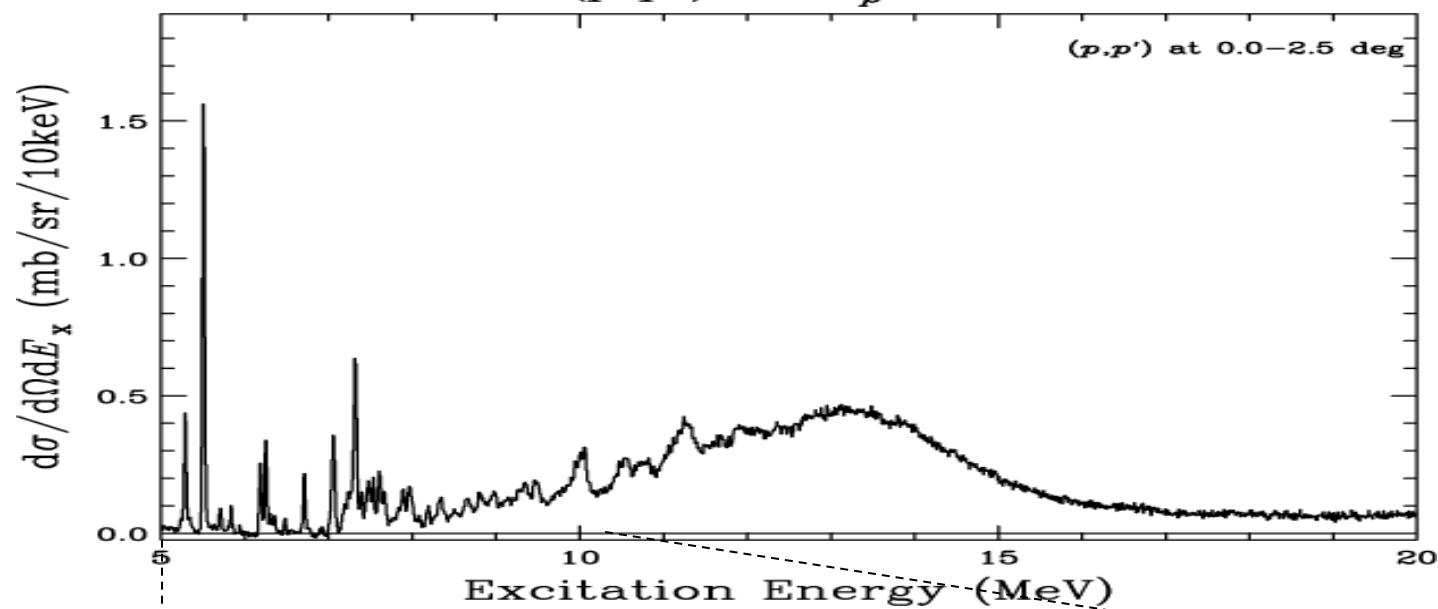
$D_{ll}$  Measurement

# Setup for E282&E316



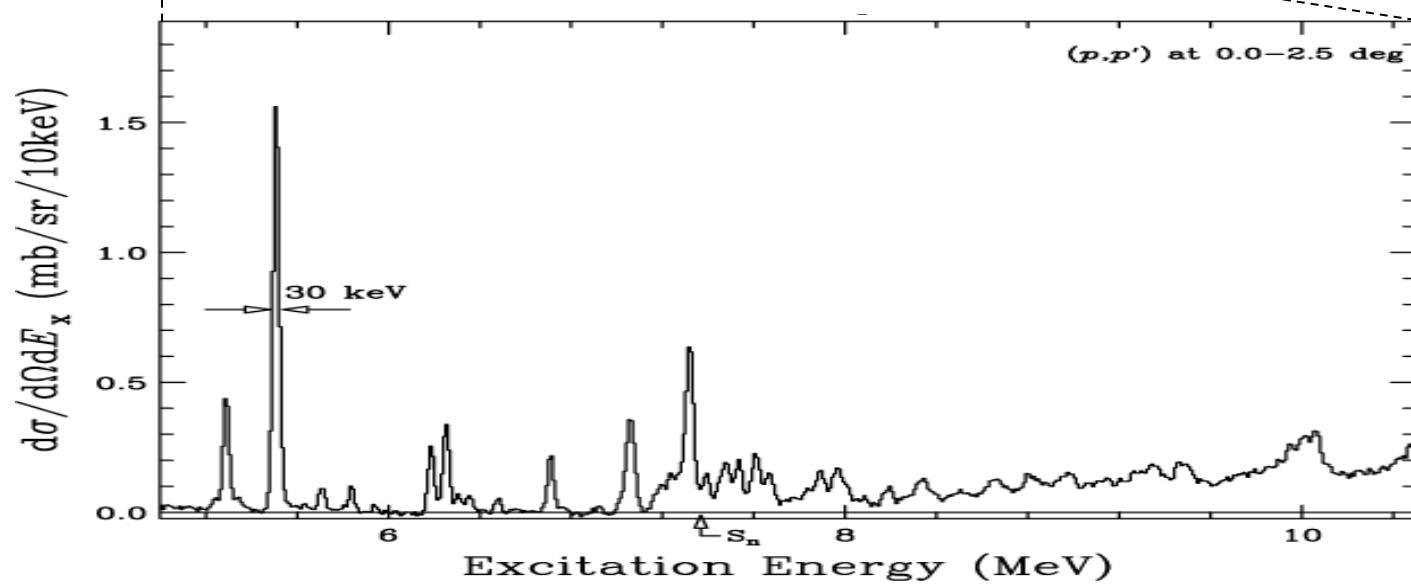
$^{208}\text{Pb}(p,p')$  at  $E_p = 295$  MeV

( $p,p'$ ) at 0.0–2.5 deg



Excitation Energy (MeV)

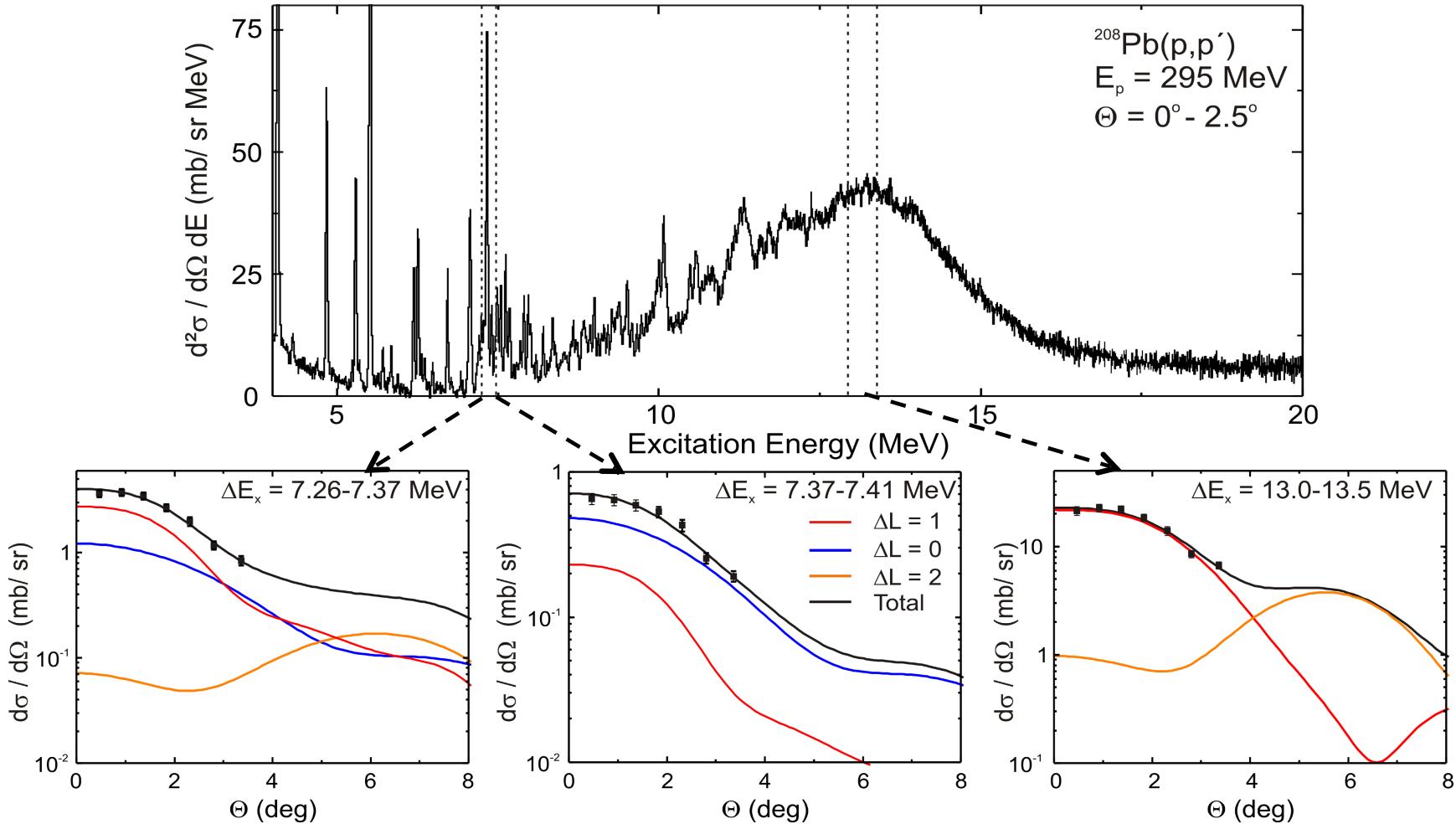
( $p,p'$ ) at 0.0–2.5 deg



Excitation Energy (MeV)

# B(E1): continuum and GDR region

## Method 1: Multipole Decomposition



- Neglect of data for  $\Theta > 4$ :  $(p,p')$  response too complex
- Included E1/M1/E2 or E1/M1/E3 (little difference)

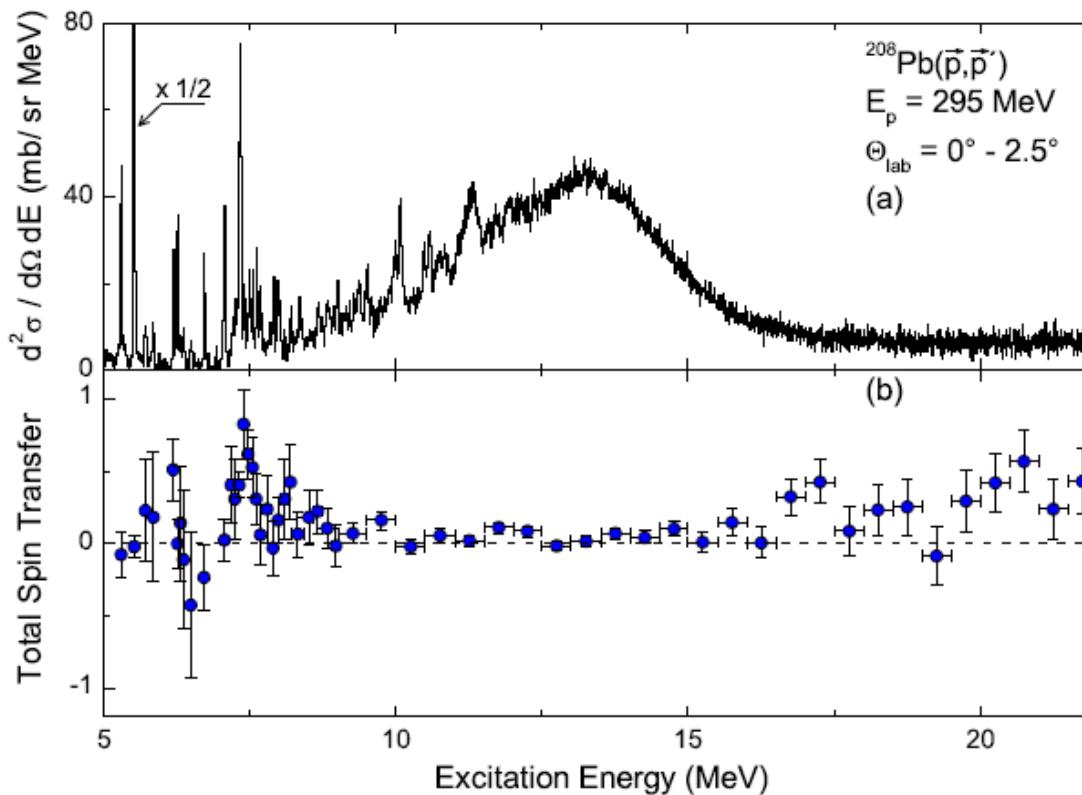
Grazing Angle = 3.0 deg

# B(E1): continuum and GDR region

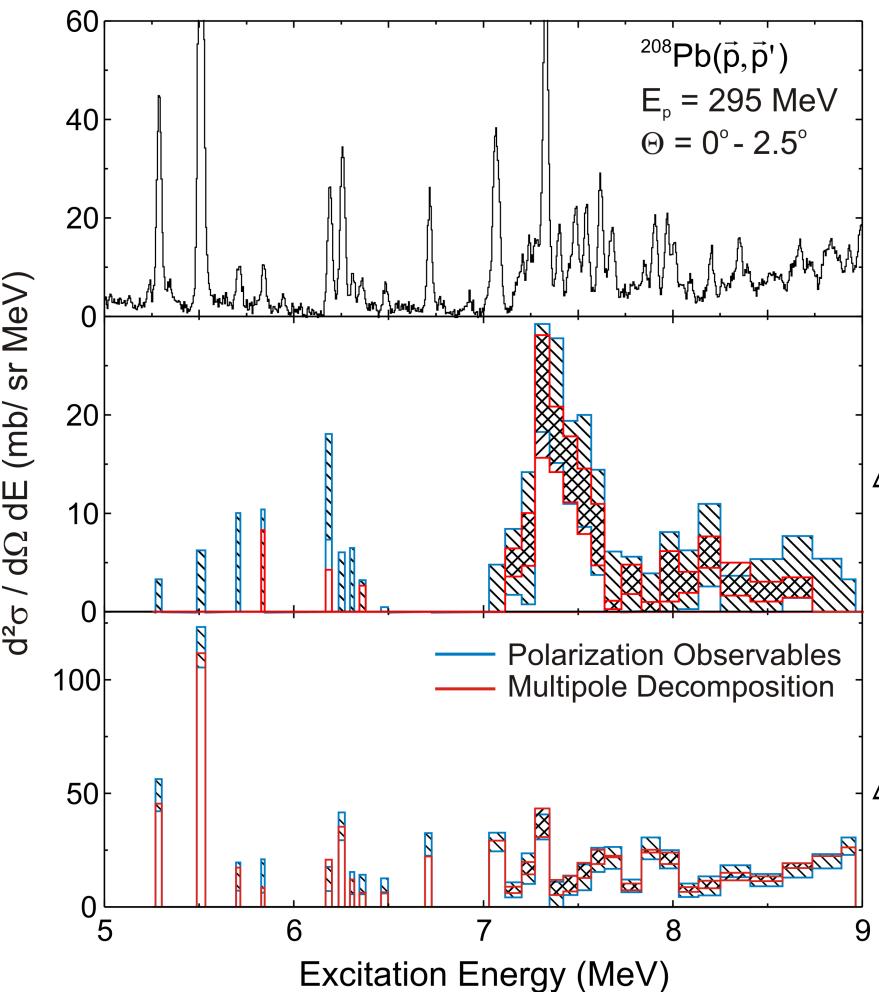
## Method 2: Decomposition by Spin Observables

Polarization observables at  $0^\circ$   spinflip / non-spinflip separation  
model-independent  
E1 / spin-M1 decomposition  
T. Suzuki, PTP 103 (2000) 859

$$\text{Total Spin Transfer } \Sigma \equiv \frac{3 - (2D_{ss} + D_{ll})}{4} = \begin{cases} 1 & \text{for } \Delta S = 1 \quad \text{spin-M1} \\ 0 & \text{for } \Delta S = 0 \quad \text{E1} \end{cases}$$



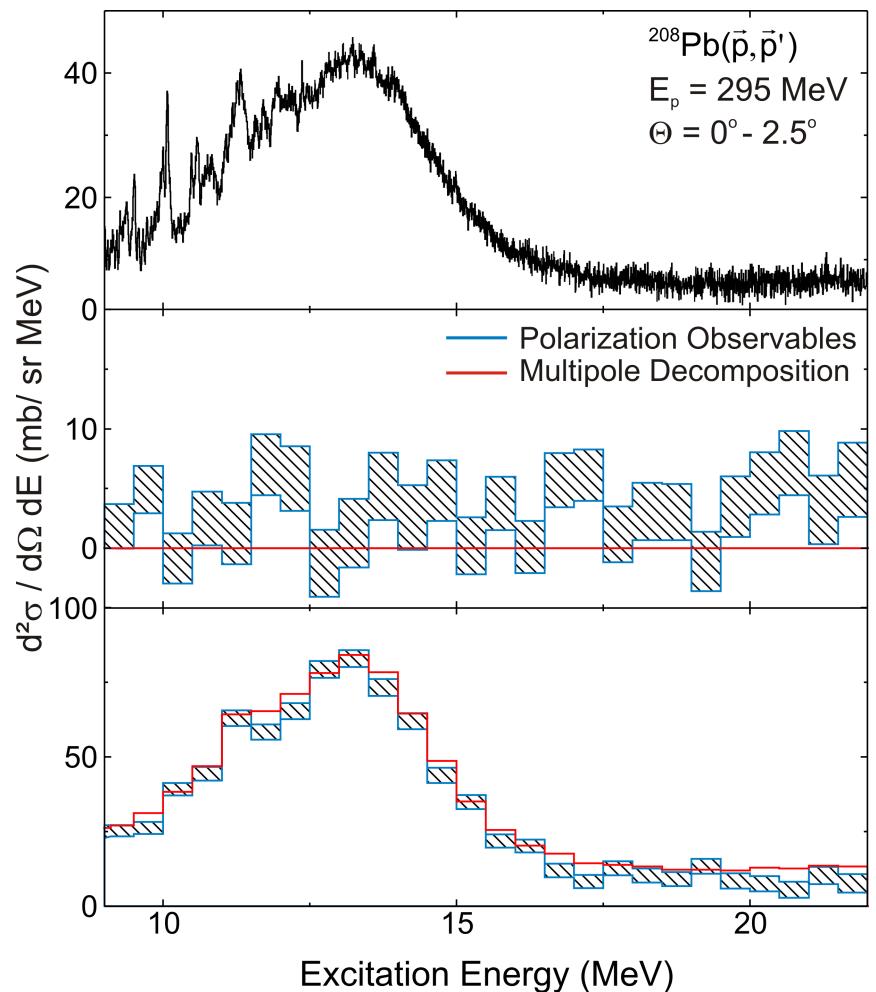
# Comparison between the two methods



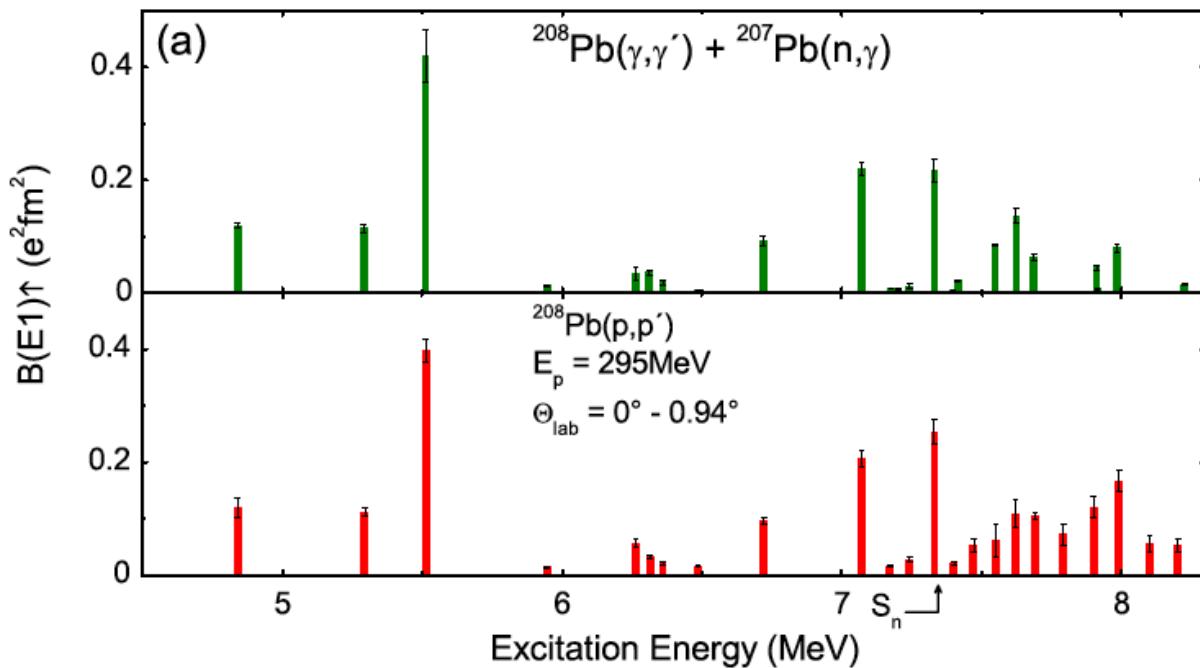
Total

$\Delta S = 1$

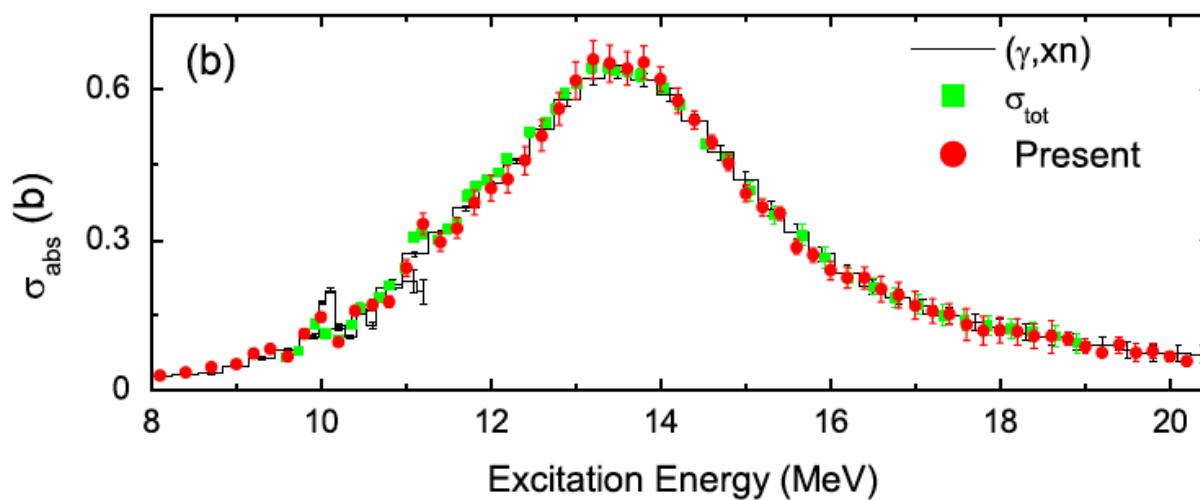
$\Delta S = 0$



# Comparison with $(\gamma, \gamma')$ and $(\gamma, xn)$



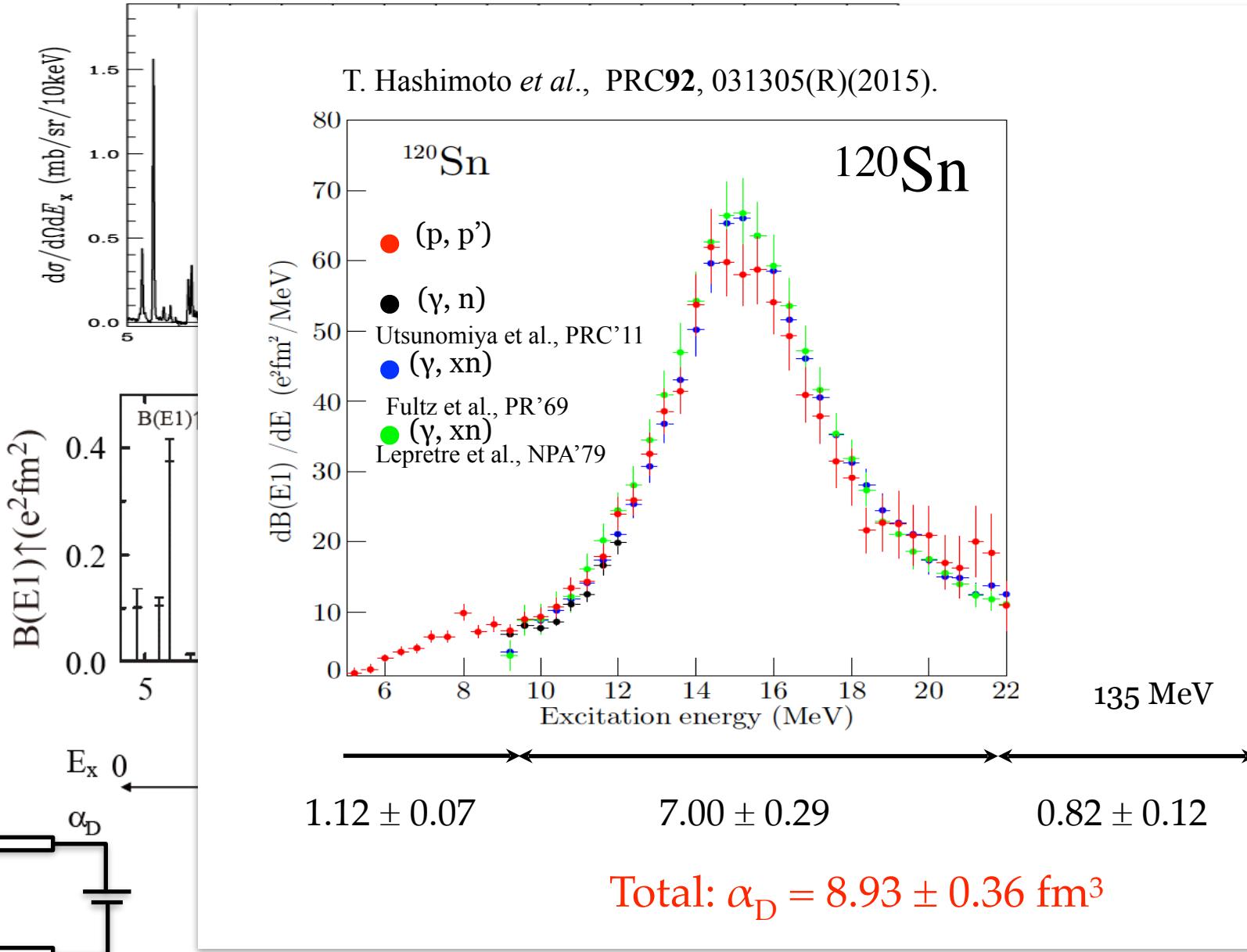
low-lying  
discrete states



GDR region

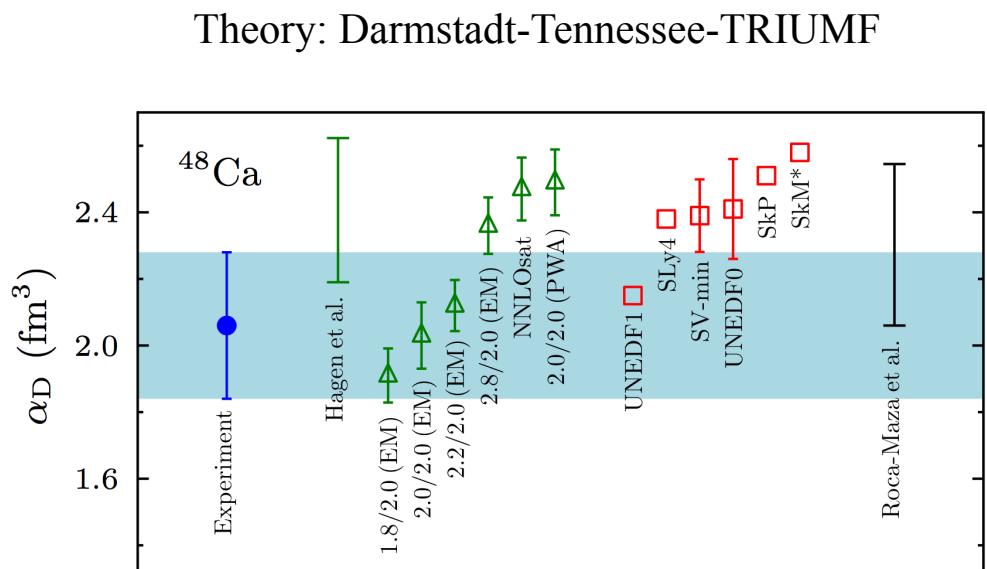
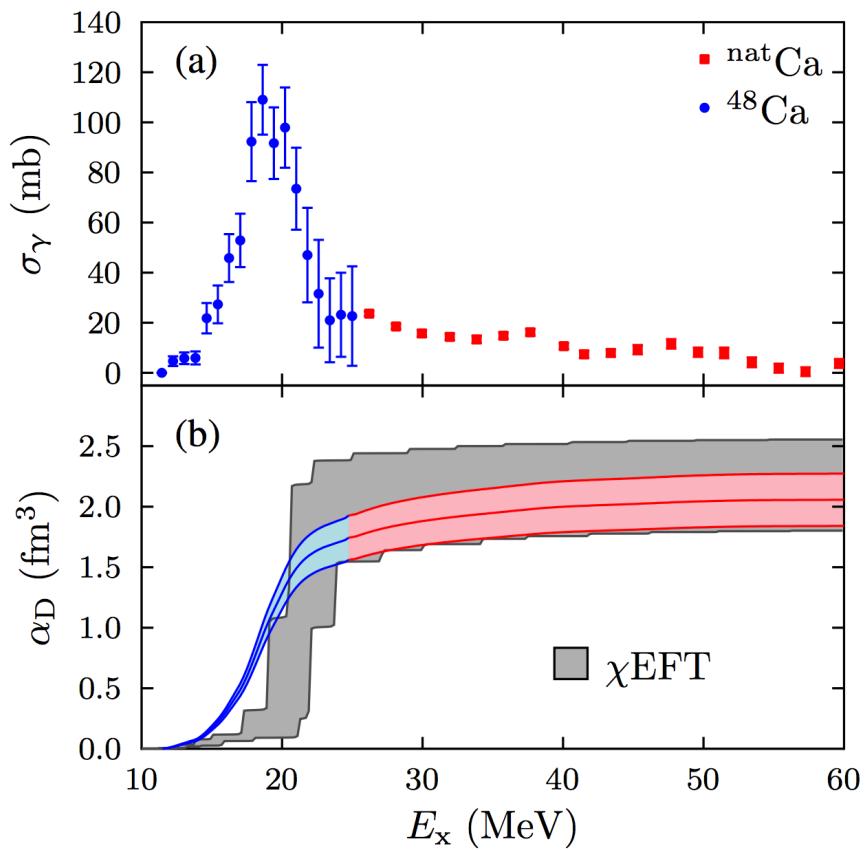
# Electric Dipole Polarizability: $^{208}\text{Pb}$ , $^{120}\text{Sn}$

$^{208}\text{Pb}(p, p')$  at  $E_p = 295$  MeV



# Electric Dipole Polarizability of $^{48}\text{Ca}$

where the EDF and ab-initio calculations meet each other



# Electric Dipole Polarizability

Clear definition

Unambiguous in the integration range

↔ Pygmy Dipole Strength

Inversely energy weighted sum-rule

More sensitive to the low-energy strength

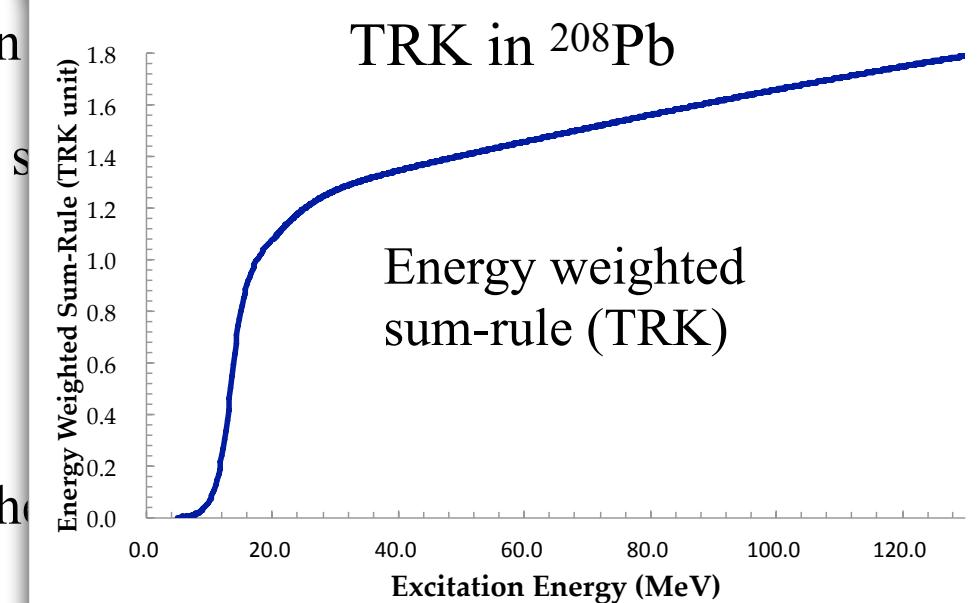
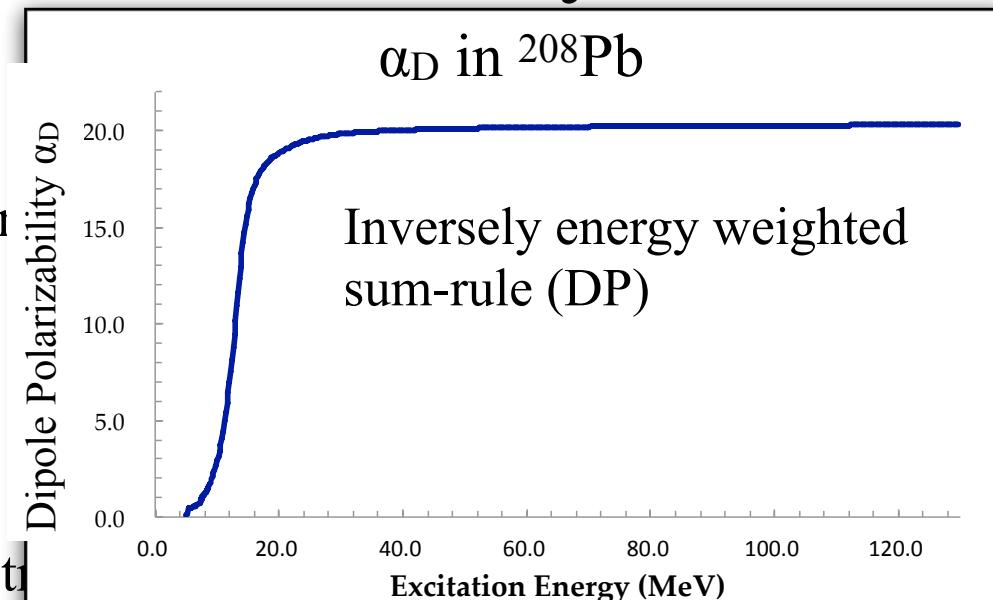
Good convergence in the excitation range

↔ energy-weighted (TRK) sum rule

Sum-rule for all the transitions

= Ground state property

↔ easier comparison with theory

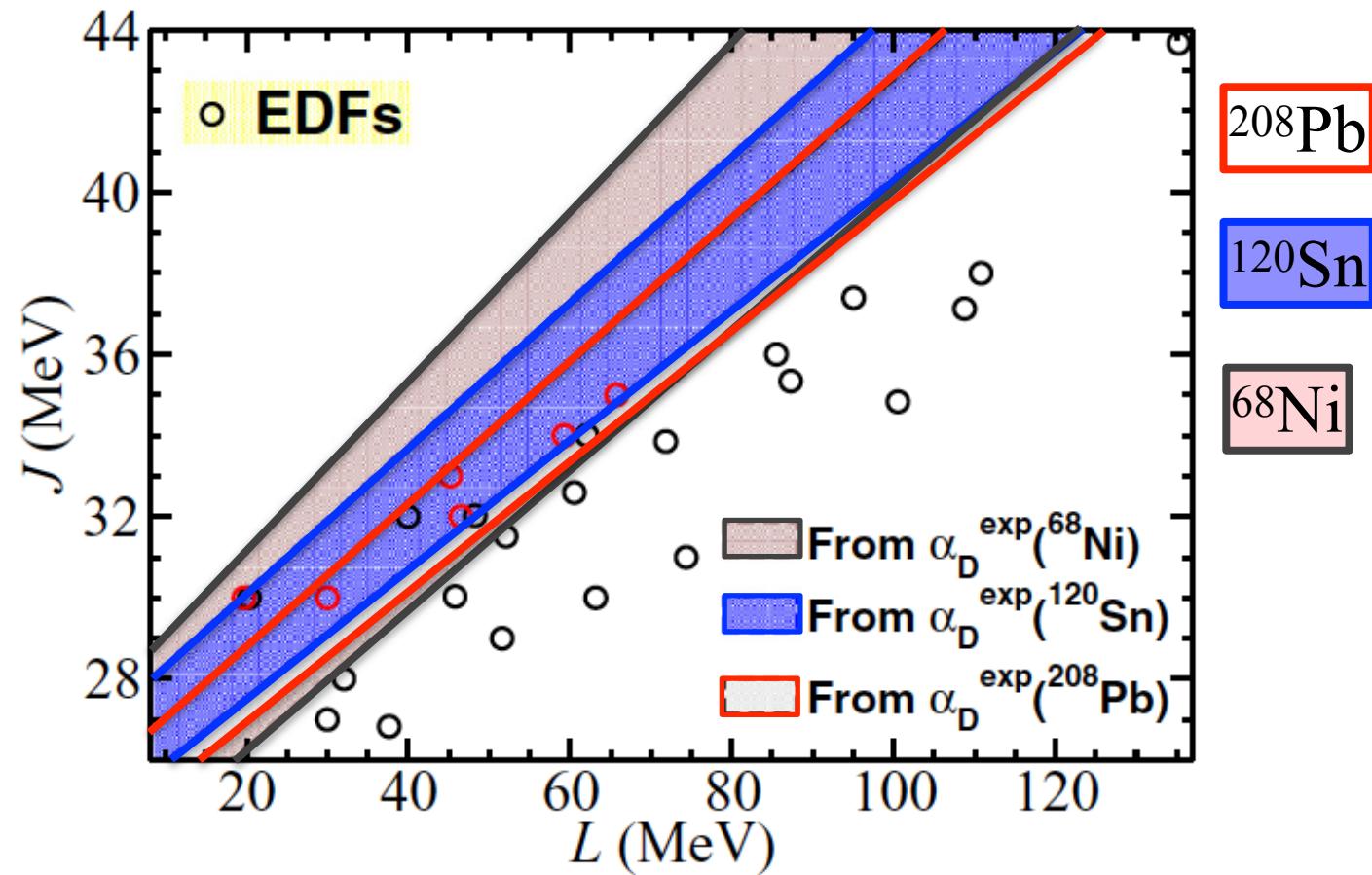


# Constraints on the Symmetry Energy



# Constraints on $J$ - $L$ from the EDP data

X. Roca-Maza et al., PRC92, 064304(2015)



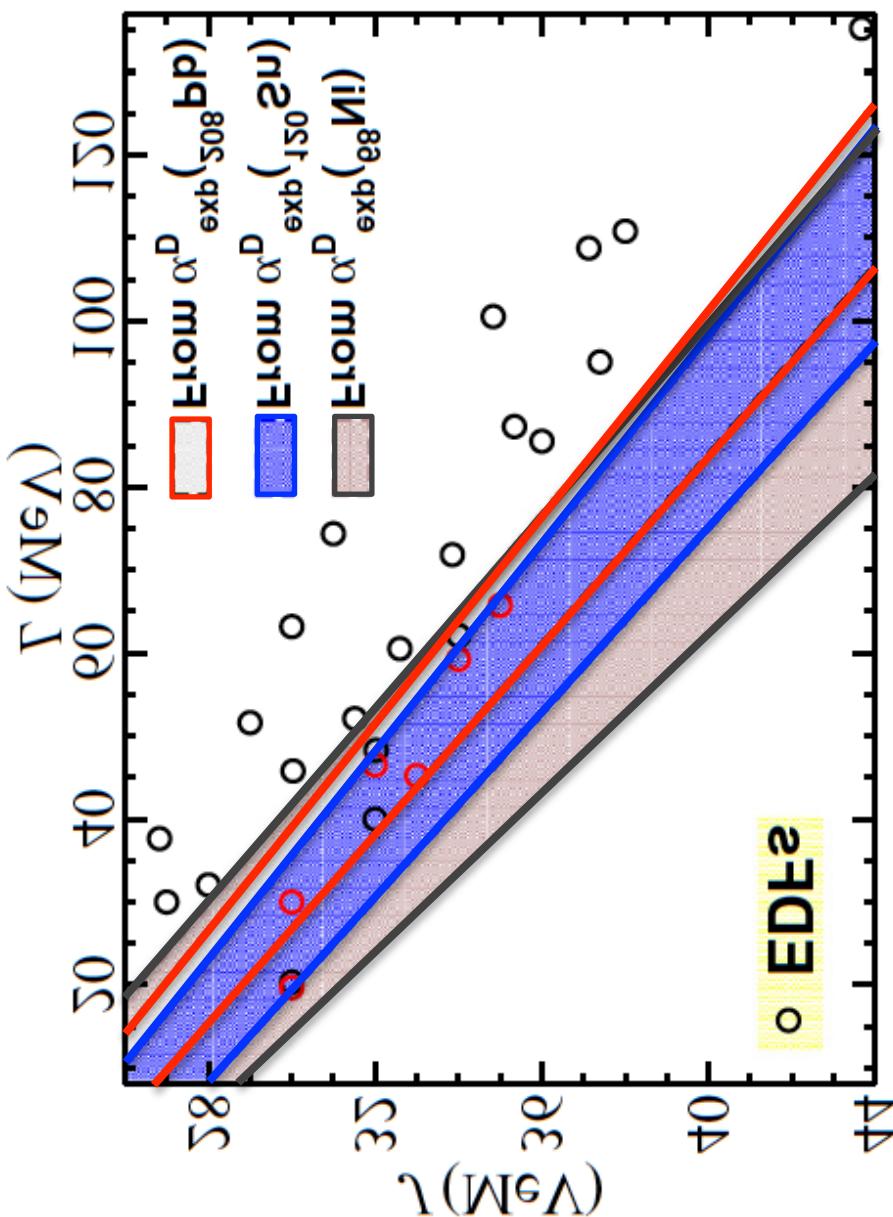
**RCNP**  $^{208}\text{Pb}$ : AT *et al.*, PRL107, 062502 (2011).

**RCNP**  $^{120}\text{Sn}$ : T. Hashimoto *et al.*, PRC92, 031305(R)(2015).

**GSI**  $^{68}\text{Ni}$ : D.M. Rossi *et al.*, PRL111, 242503 (2013).

# Constraints on $J$ - $L$ from the EDP data

X. Roca-Maza et al., PRC92, 064304(2015)



$^{208}\text{Pb}$

$^{120}\text{Sn}$

$^{68}\text{Ni}$

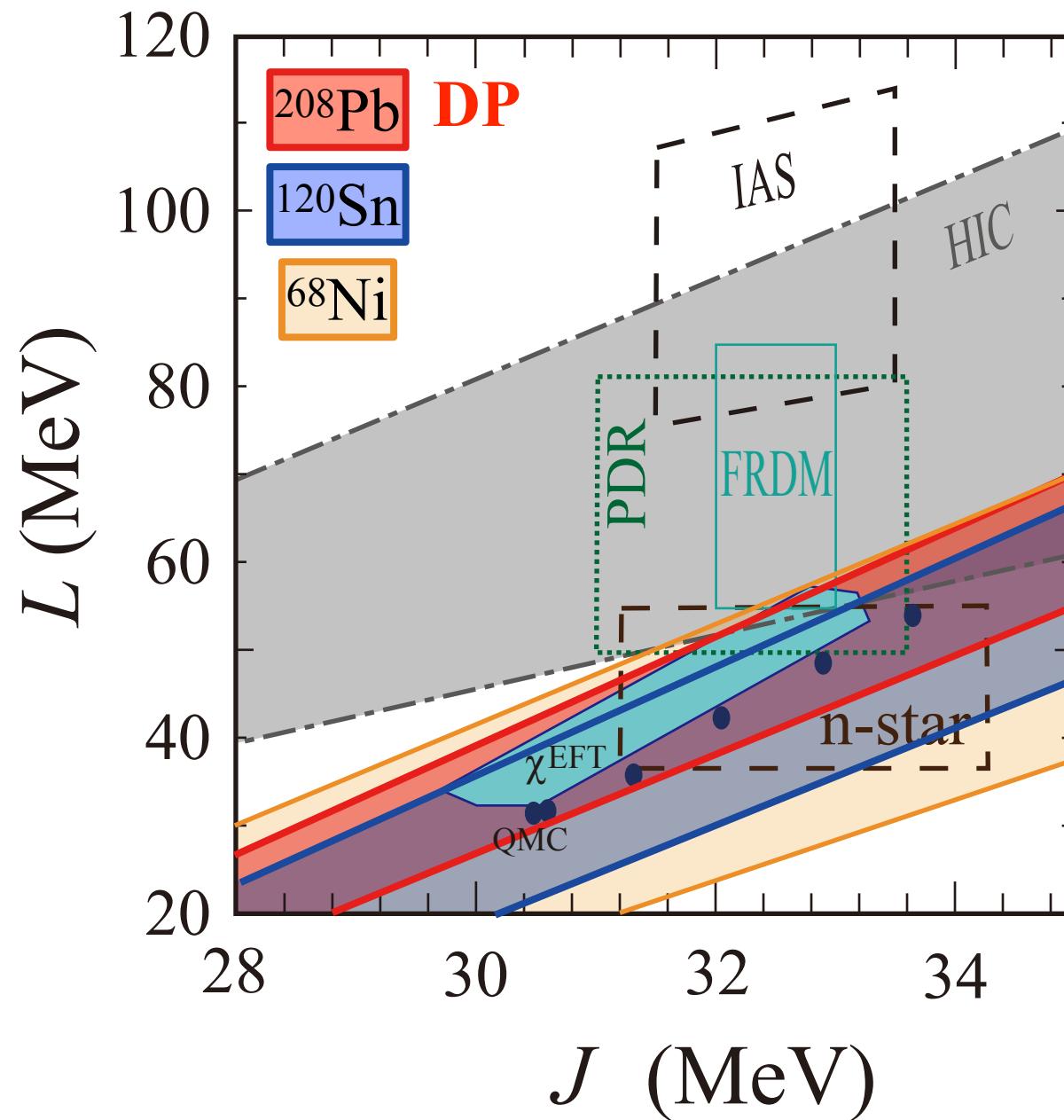
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**GSI**  $^{68}\text{Ni}$ : D.M. Rossi *et al.*, PRL111, 242503 (2013).

These  $\alpha_D$  data give essentially one constraint on the symmetry energy in the  $J$ - $L$  plane.

# Constraints on $J$ and $L$



Tsang PRC2012

HIC: Heavy Ion Collision Analysis  
Tsang PRL2009

IAS: Isobaric Analog State Energy  
Danielewicz&Lee NPA2009

PDR: Pygmy Dipole Resonance in  
 $^{132}\text{Sn}$ ,  $^{68}\text{Ni}$ , Carbone PRC2010

FRDM: Finite Range Droplet Model  
Moller PRL2012

n-star: Quiescent Low-Mass X-ray  
Binaries, Stainer PRL2012

$\chi_{\text{EFT}}$ : Chiral Effective Field Theory,  
Tews PRL2013

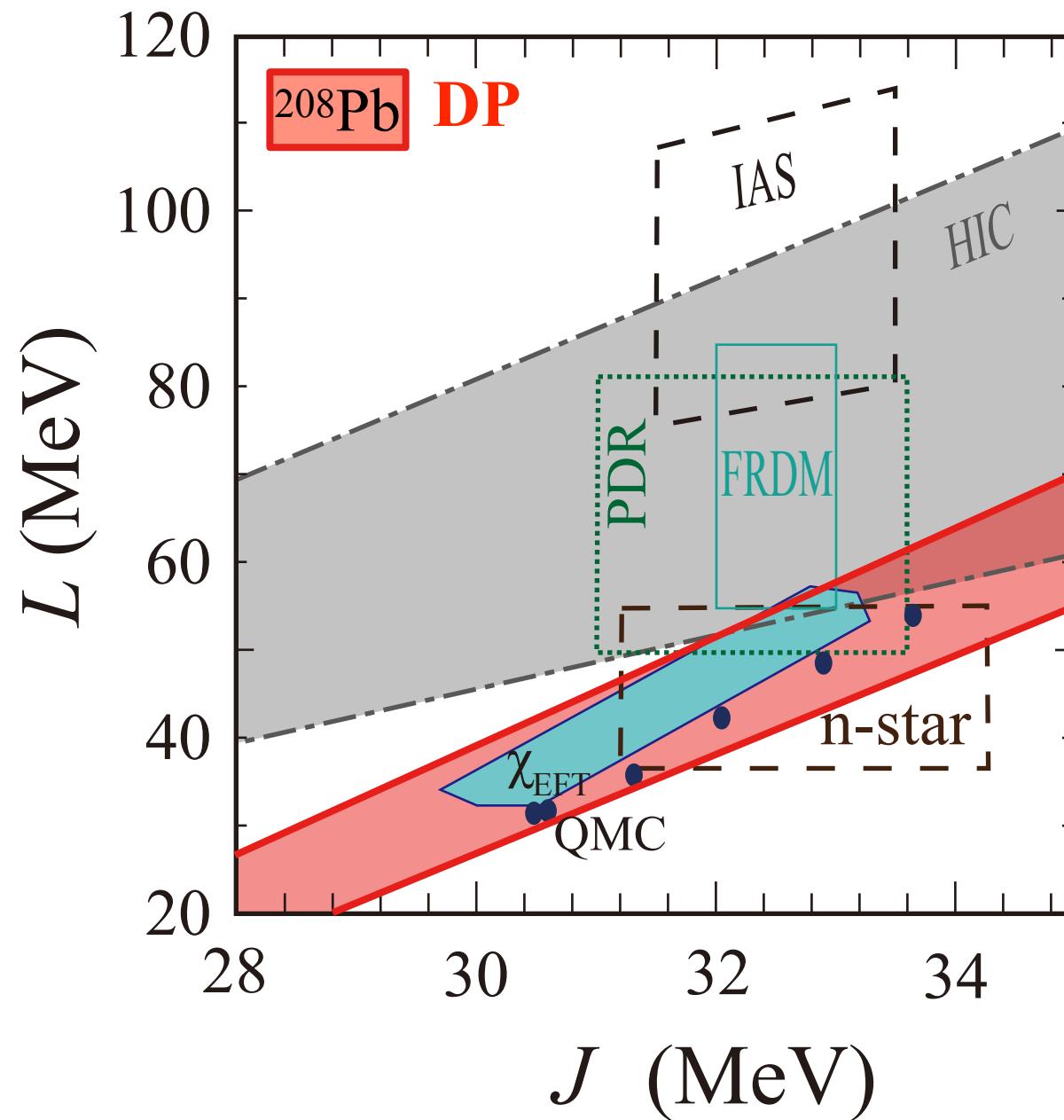
QMC: Quantum Monte-Carlo Calc.  
Gandolfi, EPJA50, 10(2014).

DP: Dipole Polarizability  
 $^{208}\text{Pb}$  AT PRL2011

$^{120}\text{Sn}$  Hashimoto PRC2015

$^{68}\text{Ni}$  Rossi PRL2013

# Constraints on $J$ and $L$



Tsang PRC2012

HIC: Heavy Ion Collision Analysis  
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IAS: Isobaric Analog State Energy  
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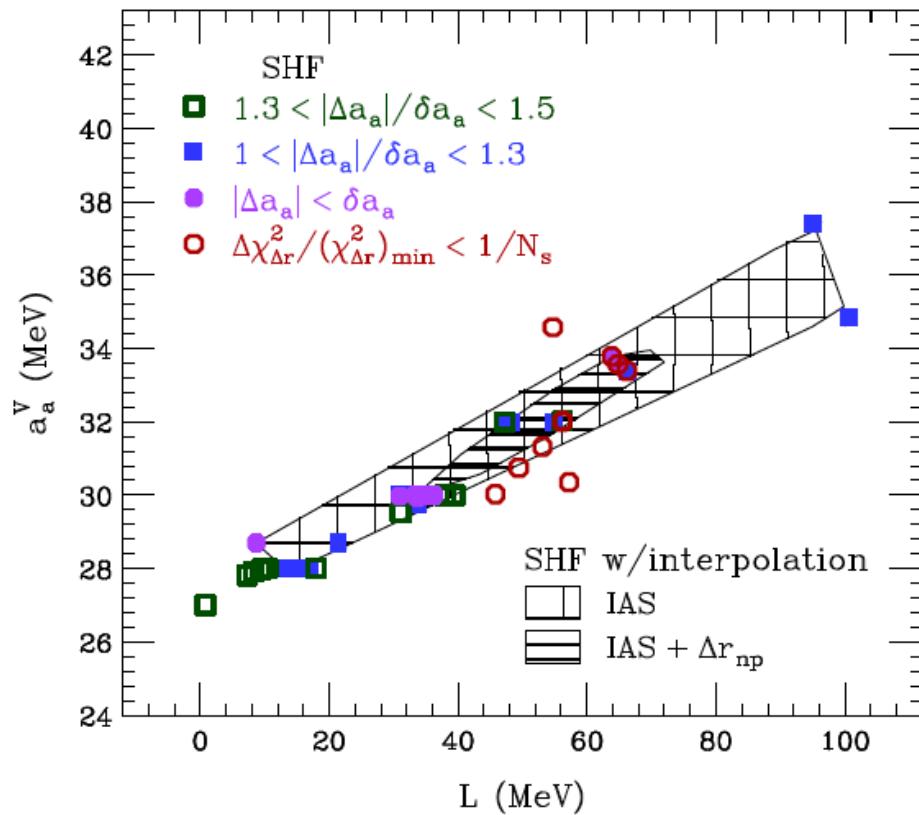
$\chi_{\text{EFT}}$ : Chiral Effective Field Theory,  
Tews PRL2013

QMC: Quantum Monte-Carlo Calc.  
Gandolfi, EPJA50, 10(2014).

DP: Dipole Polarizability  
 $^{208}\text{Pb}$  AT PRL2011

# IAS: Isobaric Analog State Energy

## Danielewicz&Lee NPA2014

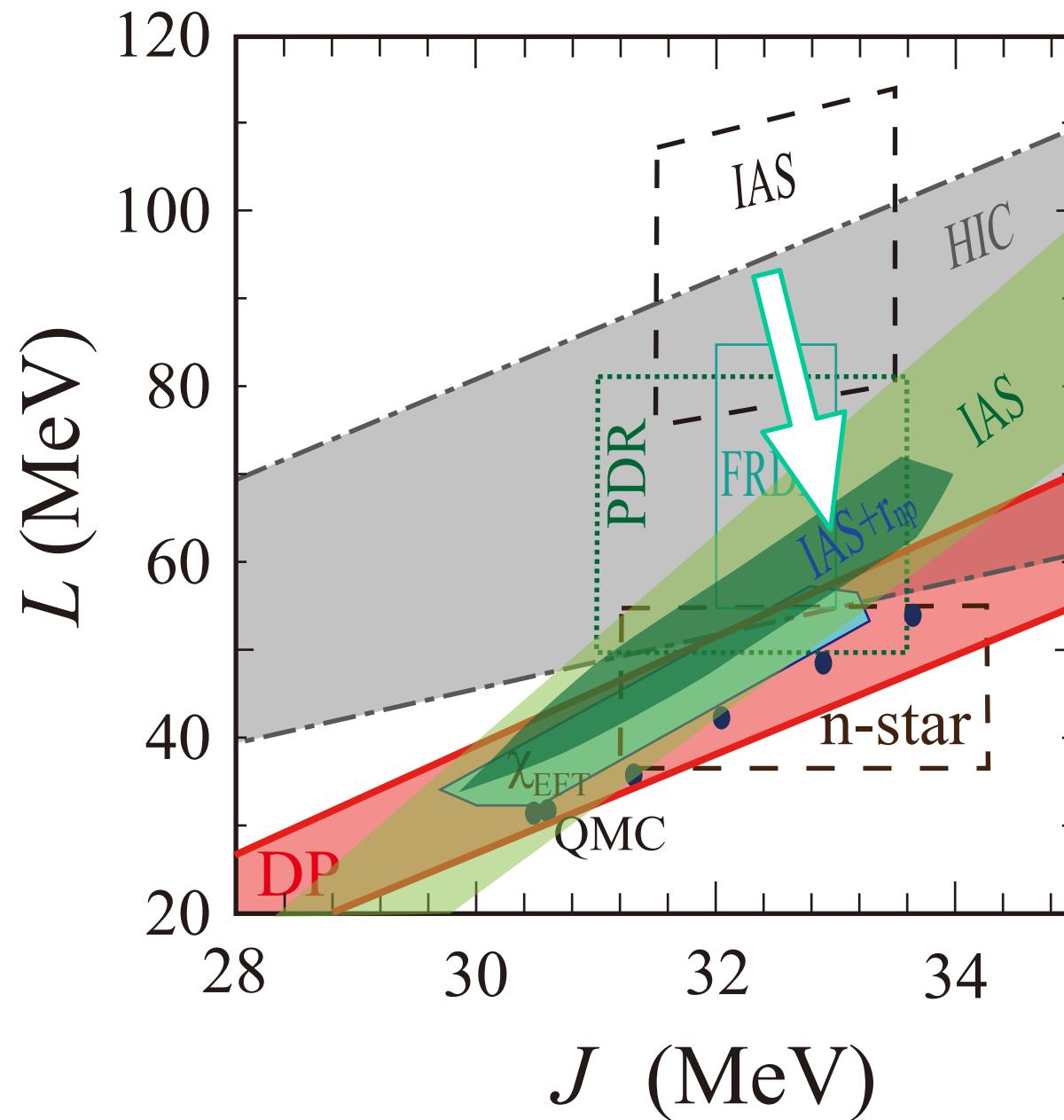


quoted neutron-skin studies

Nucleus	Reference	Data source	$\Delta r_{np}$ [fm]	$\Delta r_{np}^{GF}$ [fm]
<sup>48</sup> Ca	Friedman [93]	pionic atoms	0.13 ± 0.06	
	Gils et al. [94]	elastic $\alpha$ scattering	0.175 ± 0.050	
	Ray [95]	elastic $\bar{p}$ scattering	0.229 ± 0.050	
	Clark et al. [96]	elastic $p$ scattering	0.103 ± 0.040	
	Shlomo et al. [97]	elastic $p$ scattering	0.10 ± 0.03	
	Gibbs et al. [98]	elastic $\pi$ scattering	0.11 ± 0.04	
<sup>50</sup> Ti	combined results			
	Gils et al. [94]	elastic $\alpha$ scattering	0.129 ± 0.053*	0.218 ± 0.015
<sup>64</sup> Ni	Ray [95]	elastic $\bar{p}$ scattering	0.031 ± 0.040	0.133 ± 0.011
<sup>116</sup> Sn	Ray [95]	elastic $\bar{p}$ scattering	0.167 ± 0.050	0.102 ± 0.015
<sup>124</sup> Sn	Ray [95]	elastic $\bar{p}$ scattering	0.146 ± 0.050	0.103 ± 0.015
<sup>204</sup> Pb	Zenihiro et al. [99]	elastic $p$ scattering	0.252 ± 0.050	0.184 ± 0.021
<sup>206</sup> Pb	Zenihiro et al. [99]	elastic $p$ scattering	0.178 ± 0.059	0.161 ± 0.024
<sup>207</sup> Pb	Starodubsky et al. [100]	elastic $p$ scattering	0.180 ± 0.064	
	Starodubsky et al. [100]	elastic $p$ scattering	0.181 ± 0.045	
<sup>208</sup> Pb	combined results			
	Starodubsky et al. [100]	elastic $p$ scattering	0.181 ± 0.037	0.172 ± 0.024
	Starodubsky et al. [100]	elastic $p$ scattering	0.186 ± 0.041	0.178 ± 0.024
	Ray [95]	elastic $p$ scattering	0.197 ± 0.042	
	Clark et al. [96]	elastic $\bar{p}$ scattering	0.16 ± 0.05	
	Zenihiro et al. [99]	elastic $p$ scattering	0.119 ± 0.045	
	Friedman [93]	elastic $p$ scattering	0.211 ± 0.063	
	Friedman [93]	pionic atoms	0.11 ± 0.06	
		combined results	0.15 ± 0.08	
			0.159 ± 0.041*	0.179 ± 0.023

any average effects of asymmetry on the reactions competing with a variety of physical effects subject to modeling uncertainties. In this paper we attempt to learn about the average effects of neutron–proton asymmetry on nuclear energies, exploiting excitation energies to isobaric analog states and to reach the conclusions in as model-independent manner as possible. Our early efforts in this direction have been reported in [1–3]. As we progress, we find that we need to reassess our strategy.

# Constraints on $J$ and $L$



Tsang PRC2012

HIC: Heavy Ion Collision Analysis  
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IAS: Isobaric Analog State Energy  
Danielewicz&Lee **NPA2009→2014**

PDR: Pygmy Dipole Resonance in  
 $^{132}\text{Sn}$ ,  $^{68}\text{Ni}$ , Carbone PRC2010

FRDM: Finite Range Droplet Model  
Moller PRL2012

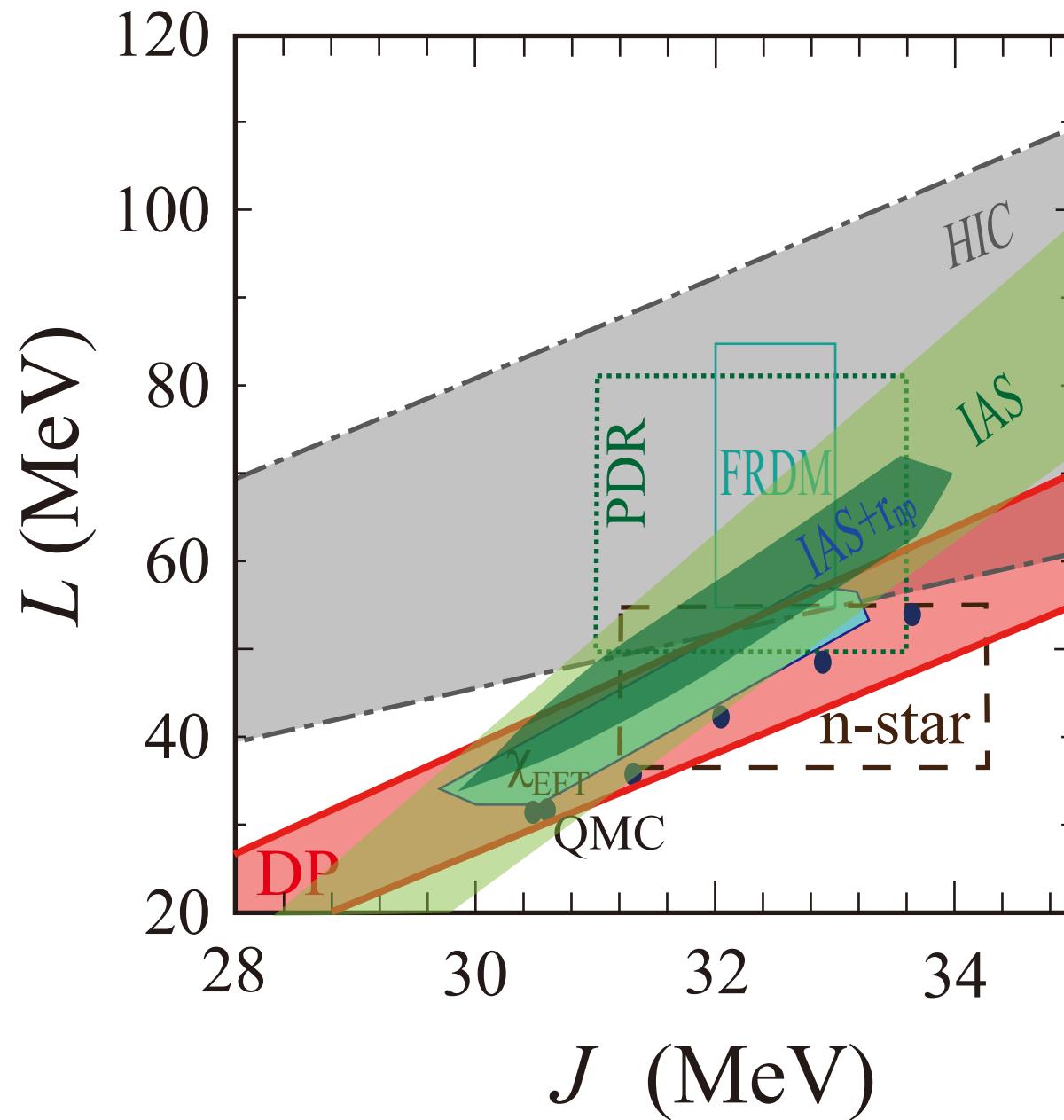
n-star: Quiescent Low-Mass X-ray  
Binaries, Stainer PRL2012

$\chi_{\text{EFT}}$ : Chiral Effective Field Theory,  
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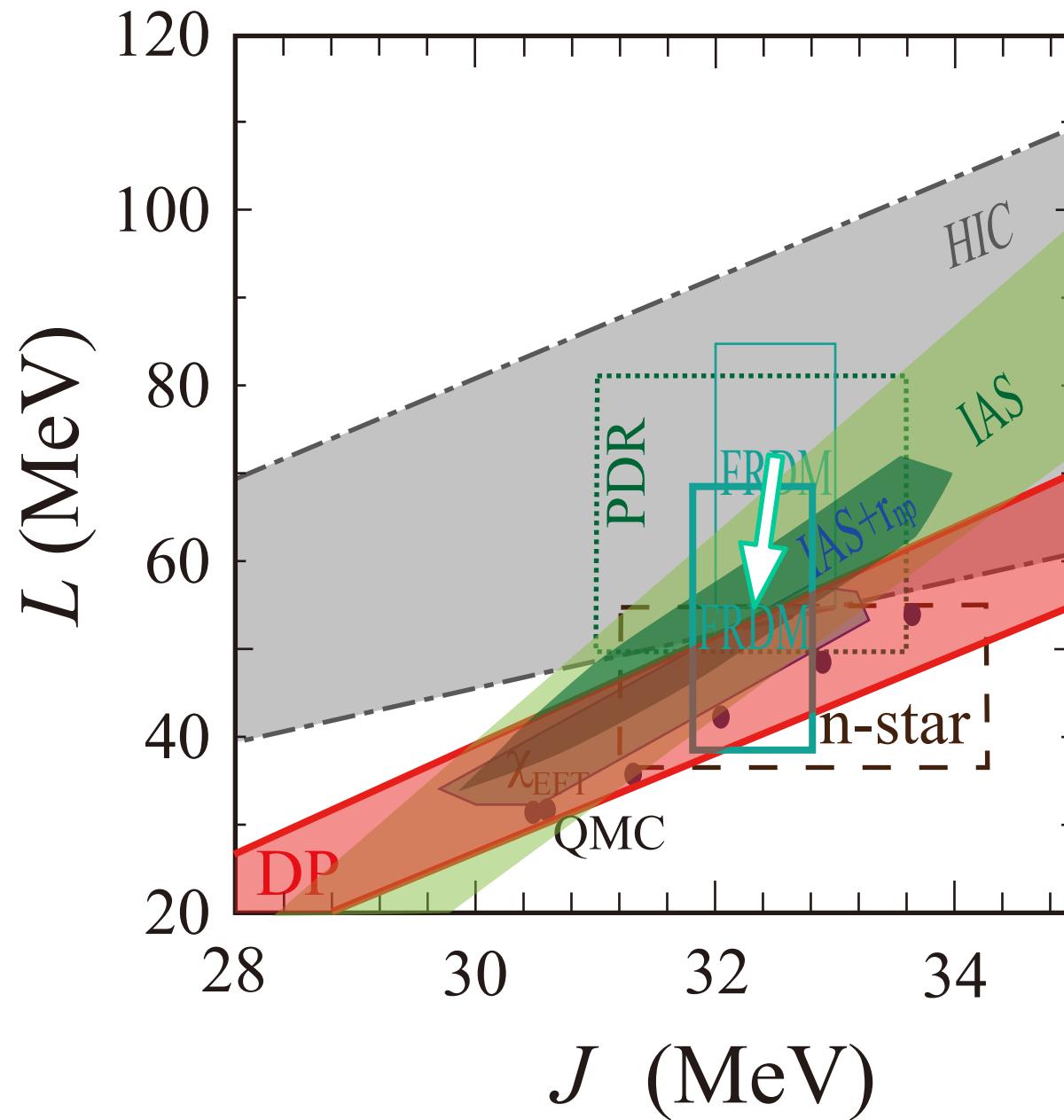
The optimal values of the asymmetry variables  $J$  and  $L$  that we obtained from the mass model FRDM (2012) study are

$$J = 32.3 \pm 0.5 \text{ MeV}$$

$$L = 53.5 \pm 15 \text{ MeV}$$

with the minimum rms deviation of  $\sigma < 560$  keV as shown in Fig. 2. The above optimal  $L$  value is somewhat smaller than the value in Ref. [3], because we have implemented a more accurate calculation of the zero-point fluctuation effect see [2] for more details.

# Constraints on $J$ and $L$



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FRDM: Finite Range Droplet Model  
Moller **PRL2012→ADNTD2016**

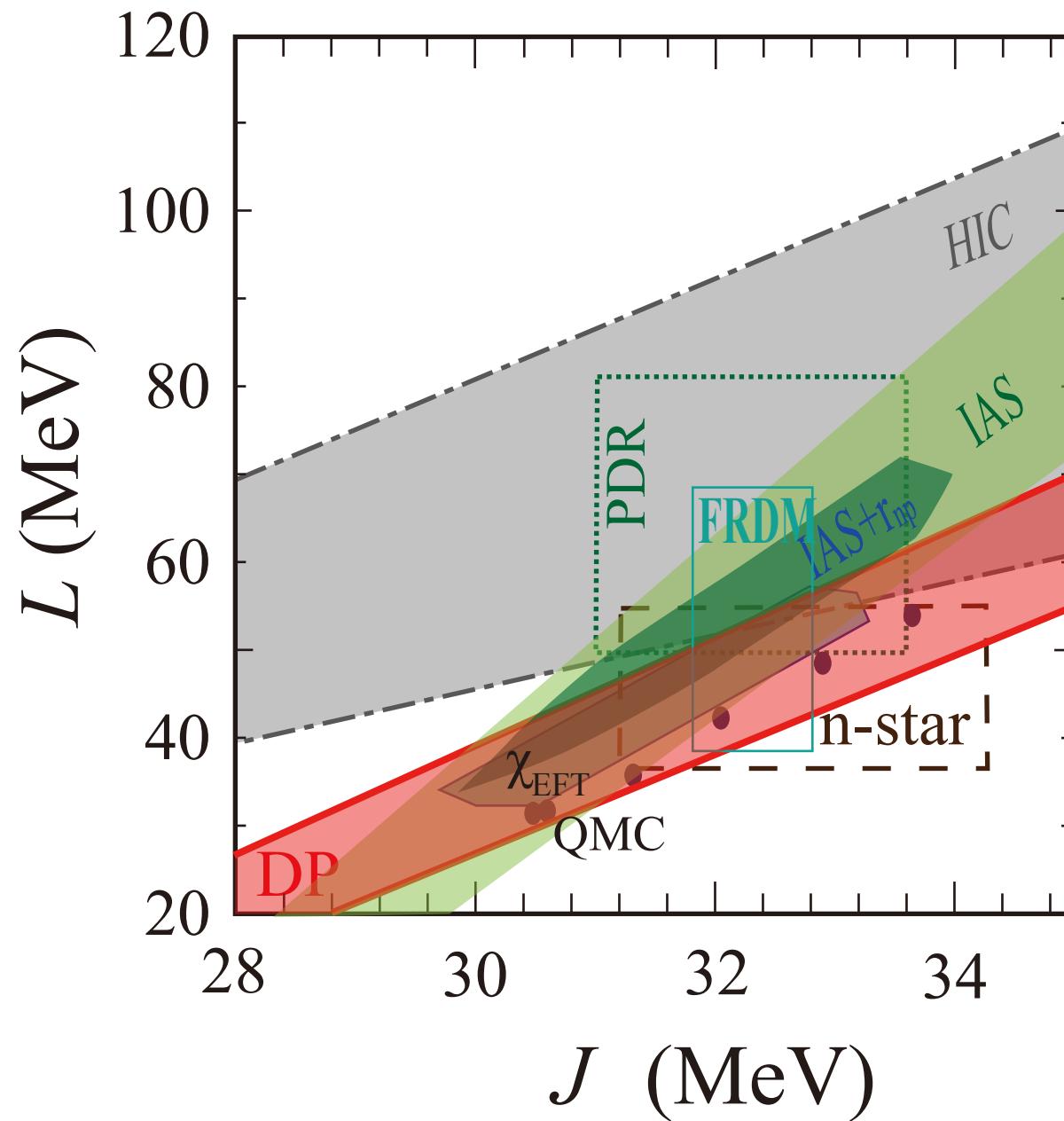
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Tews PRL2013

QMC: Quantum Monte-Carlo Calc.  
Gandolfi, EPJA50, 10(2014).

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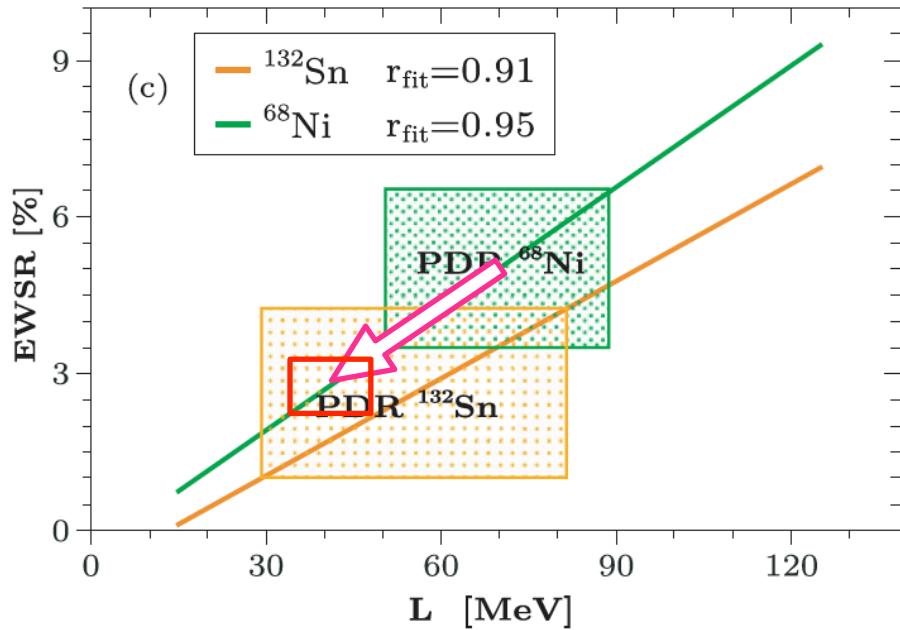
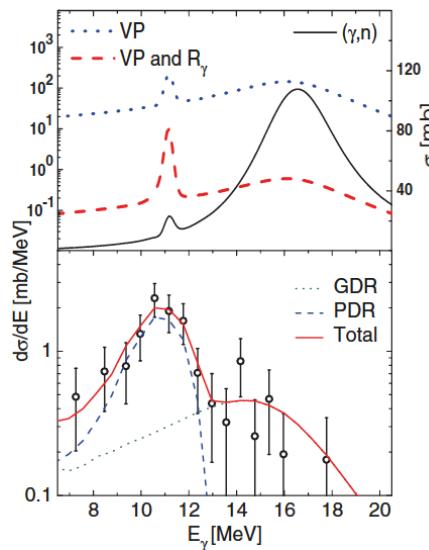
QMC: Quantum Monte-Carlo Calc.  
Gandolfi, EPJA50, 10(2014).

DP: Dipole Polarizability  
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# PDR: Pygmy Dipole Resonance in $^{132}\text{Sn}$ , $^{68}\text{Ni}$ , Carbone PRC2010

## Wieland: PRL2009

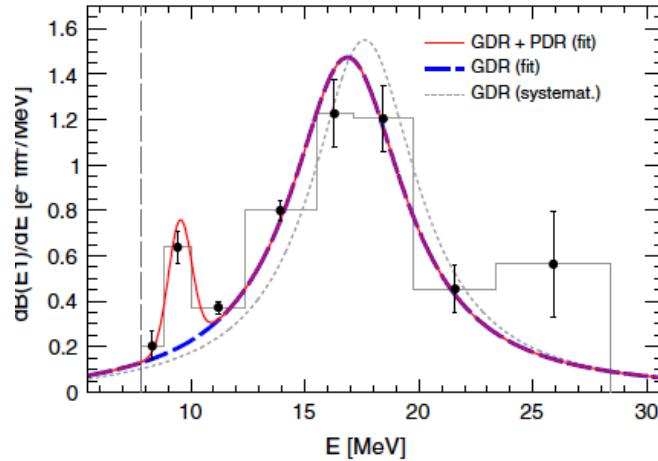
In summary, we have here presented the first experimental search of a pygmy resonance in the neutron-rich  $^{68}\text{Ni}$  nucleus using the virtual photon scattering technique. Evidence is found for the presence of sizeable strength energetically located below the GDR and centered at  $\approx 11$  MeV with approximately 5% of the EWSR strength.



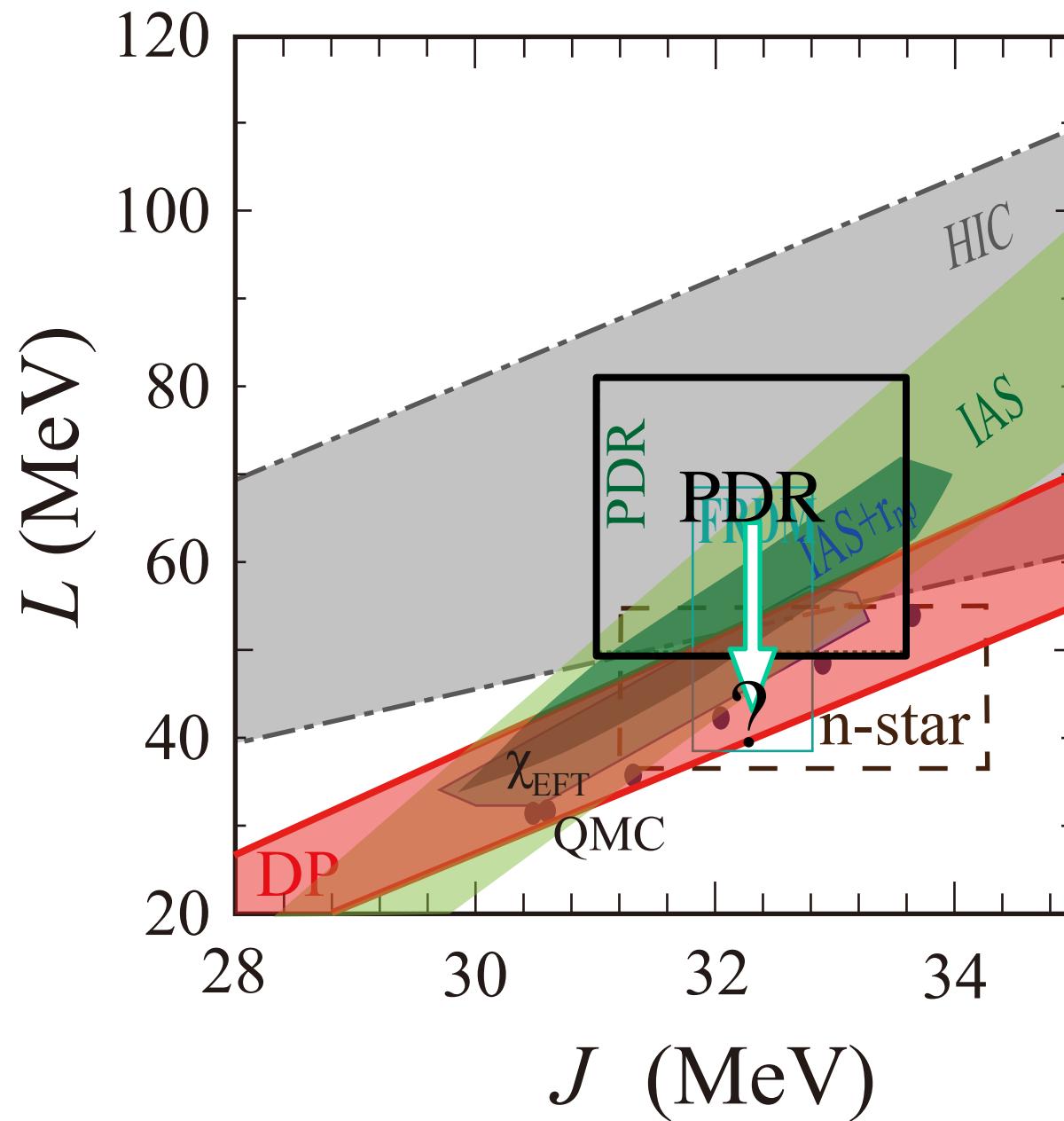
## Rossi: PRL2013

TABLE I. GDR and PDR parameters for  $^{68}\text{Ni}$  from fit to  $E1$  strength, as shown in Fig. 3. Included as well are the GDR and PDR parameters from the literature.

	This work		Literature	Reference
GDR	$E_m$ [MeV]	17.1(2)	17.84	[30]
	$\Gamma$ [MeV]	6.1(5)	5.69	[30]
	$S_{\text{EWSR}}$ [%]	98(7)	100	
PDR	$E_m$ [MeV]	9.55(17)	11.0(5)	[25,31]
	$\sigma$ [MeV]	0.51(13)	<1	[25]
	$S_{\text{EWSR}}$ [%]	2.8(5)	5.0(1.5)	[13,25]



# Constraints on $J$ and $L$



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 $^{132}\text{Sn}$ ,  $^{68}\text{Ni}$ , Carbone **PRC2010→?**

FRDM: Finite Range Droplet Model  
Moller ADNDT2016

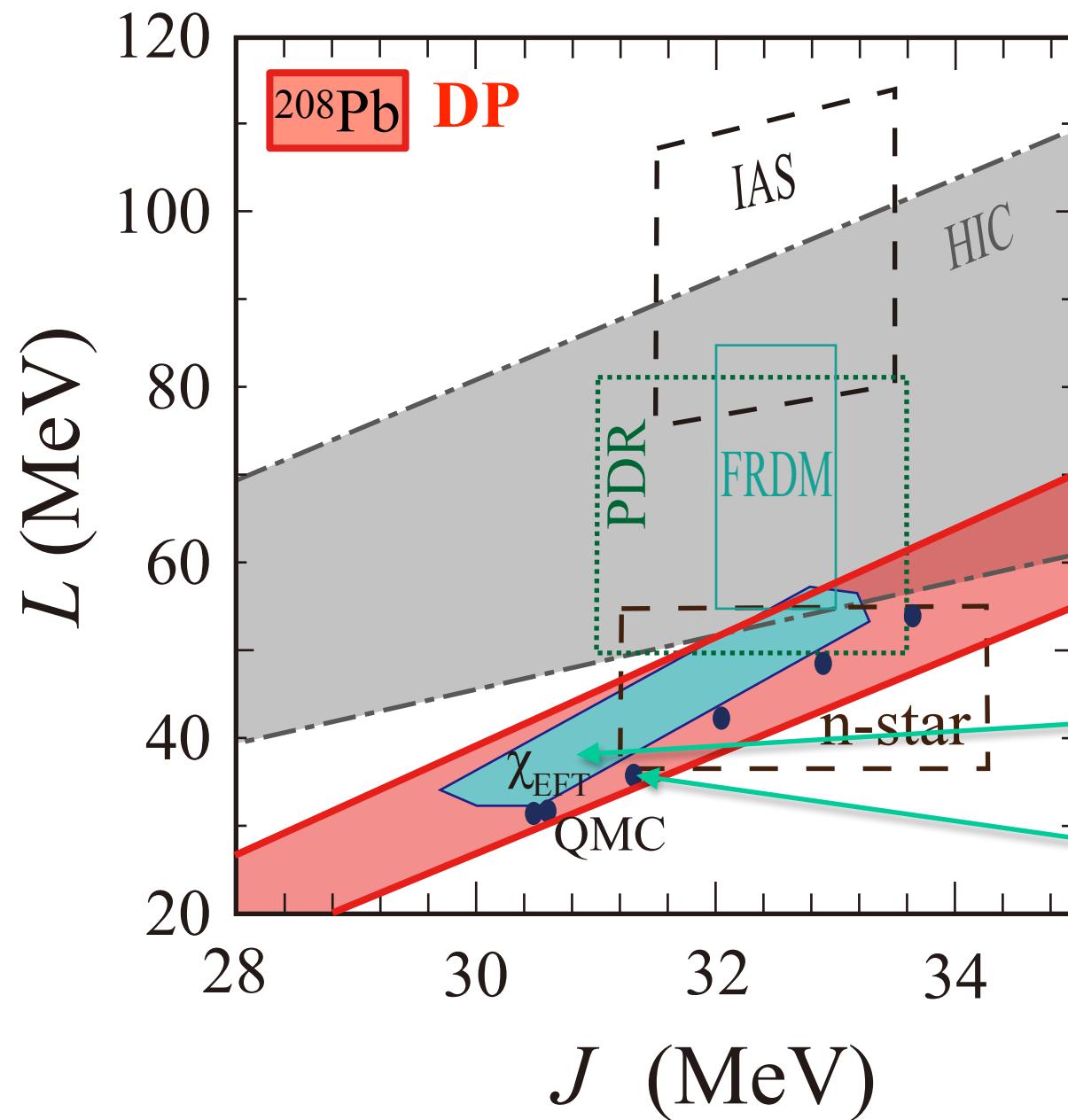
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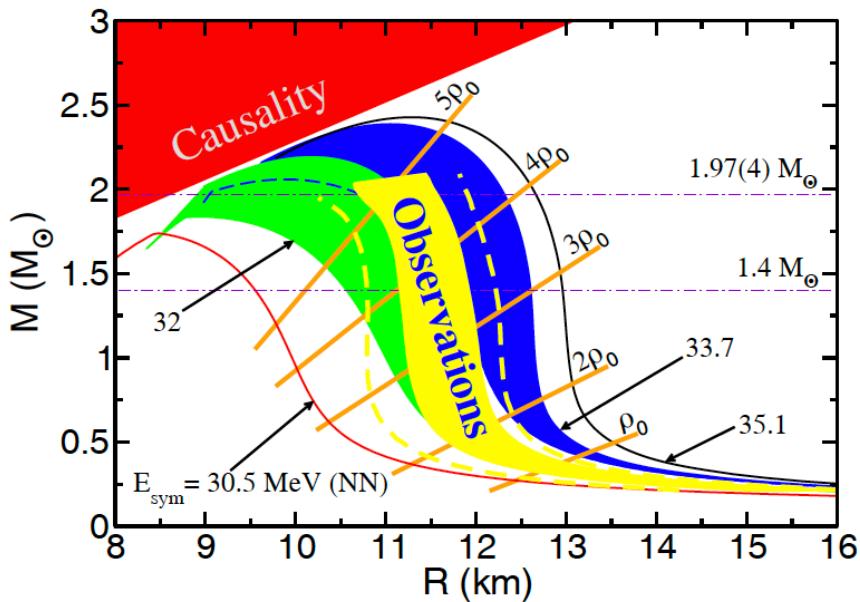
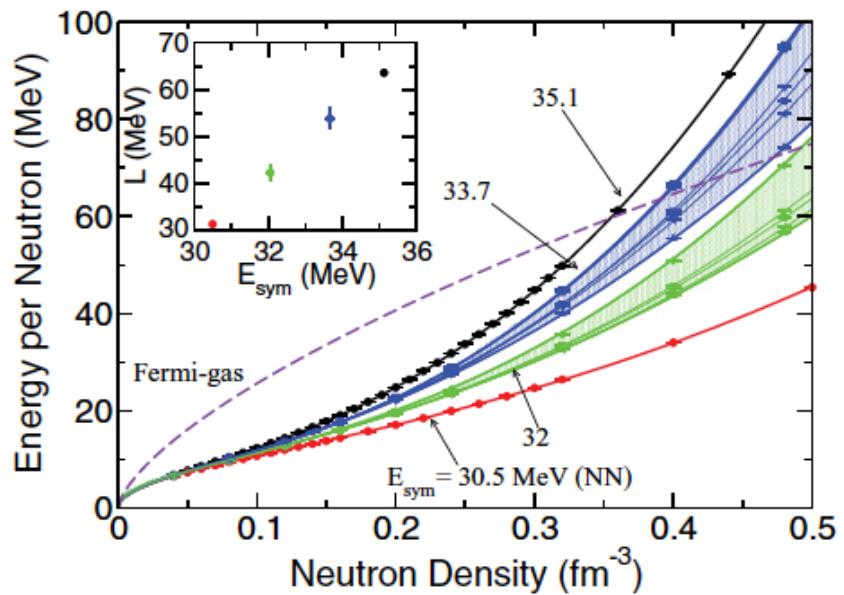
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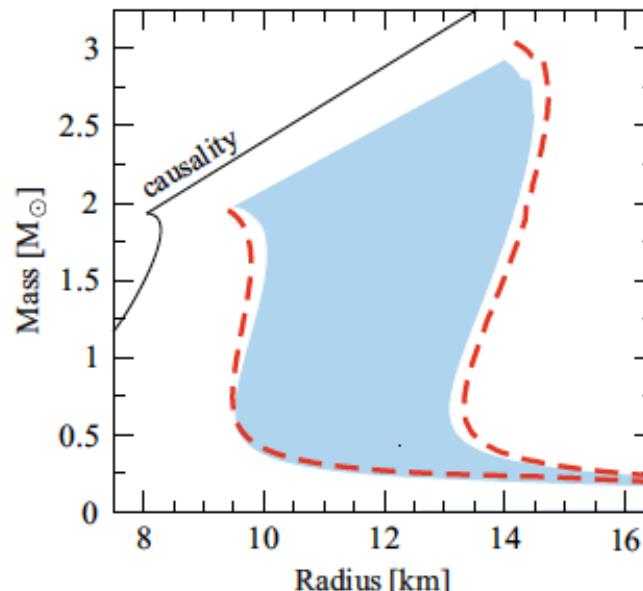
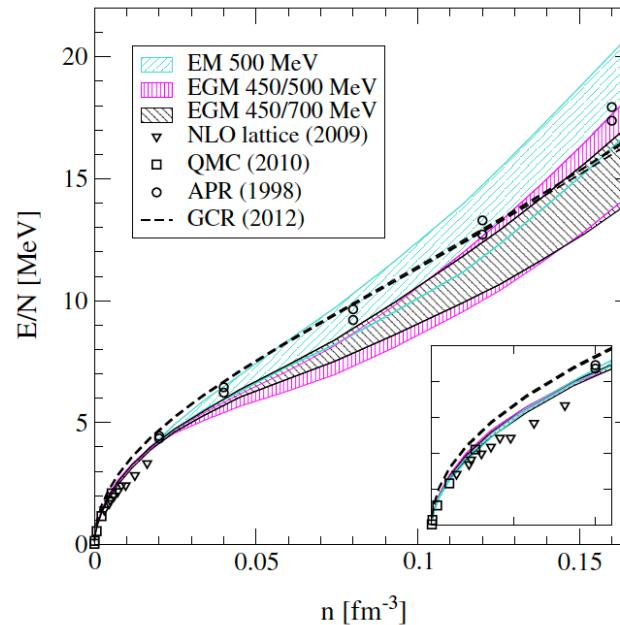
# QMC

S. Gandolfi, J. Carlson et al., EPJA50, 10 (2014)

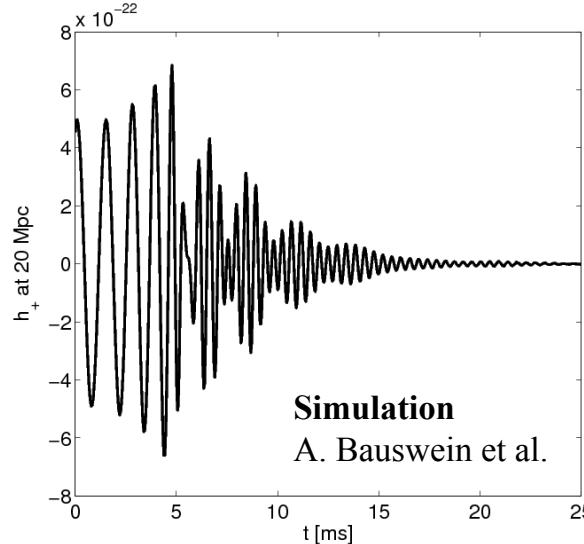
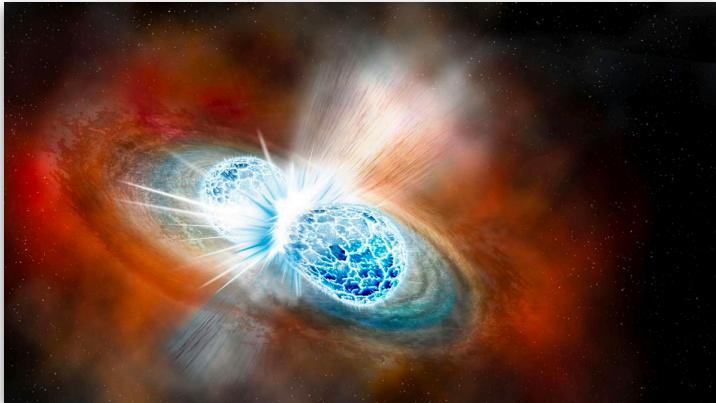


# $\chi$ EFT

I. Tews, K. Hebeler et al., PRL110, 032504(2013)  
K. Hebeler et al., et al., EPJA50, 11 (2014)



# Neutron Star Merger GW170817

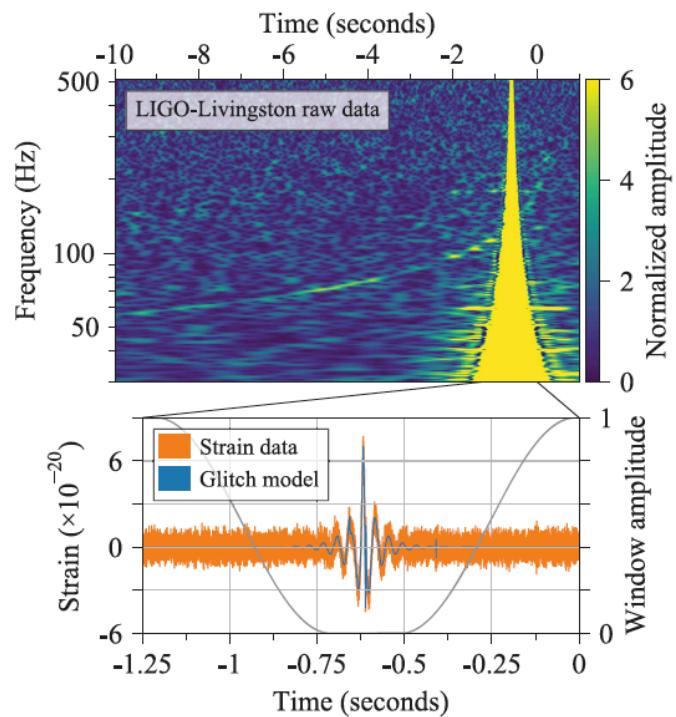


Simulation  
A. Bauswein et al.

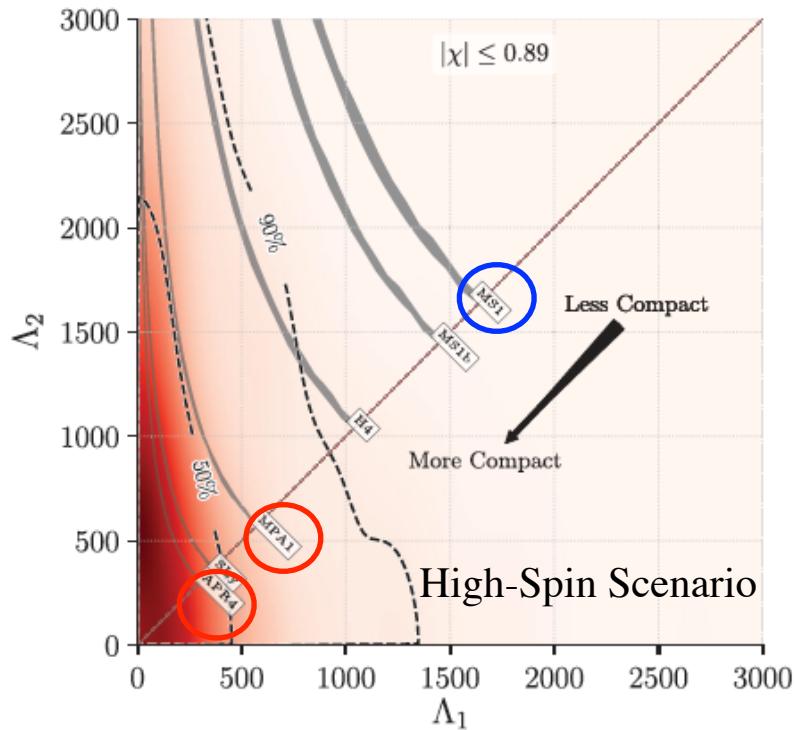


GW170817  
PRL119, 161101(2017)

LIGO



# Constraints from the N-Star Merger GW



Tidal Deformation Parameters

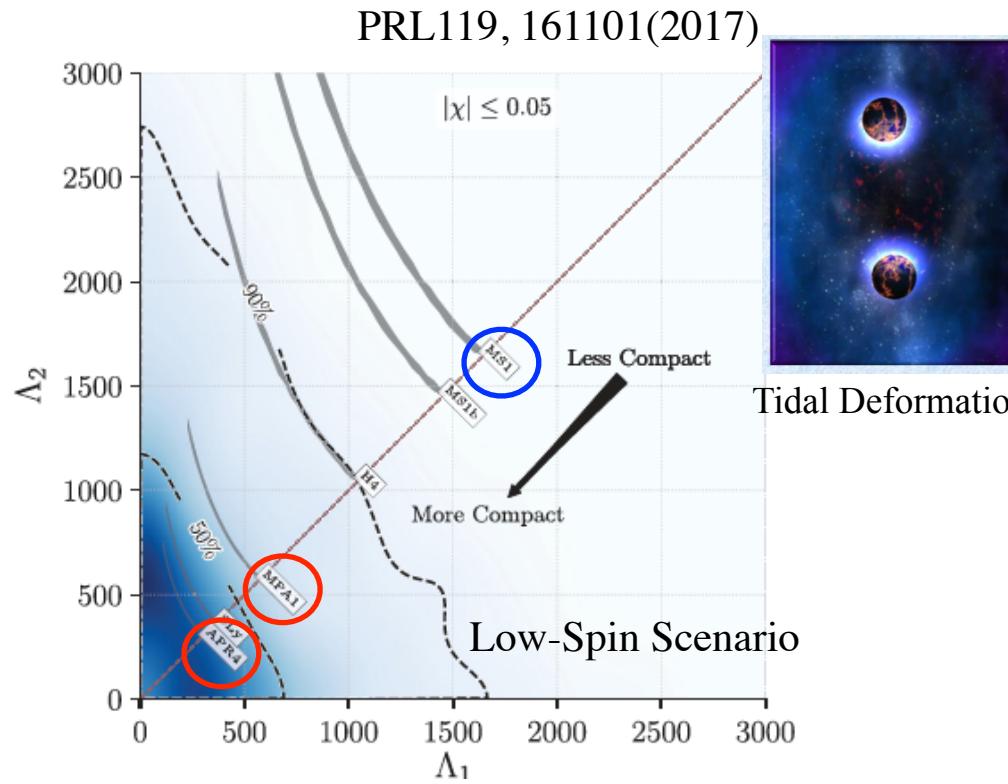
N-Star Radius ( $1.4M_{\odot}$ )

**$R^{1.4} < 13.76 \text{ km}$**  F.J. Fattoyev et al., PRL120, 172702(2018)

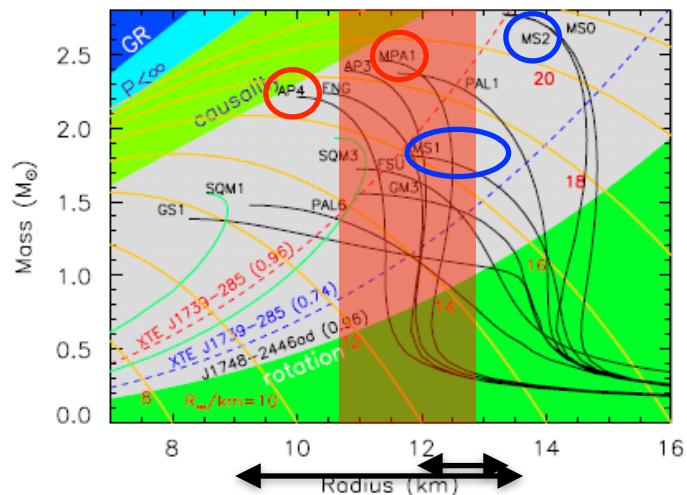
**$12.00 < R^{1.4} < 13.45 \text{ km}$**  E.R. Most et al., PRL120, 261103(2018)

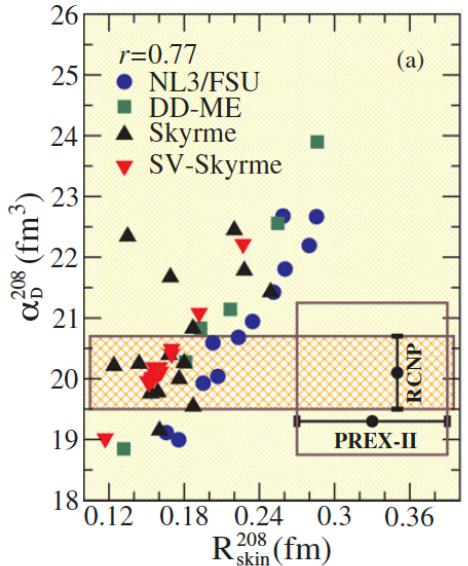
**$9.0 < R^{1.4} < 13.6 \text{ km}$**  I. Tews et al., talk in the next session

N-star merger GW analysis is giving constraints on the nuclear EOS that are consistent with the study of atomic nuclei.

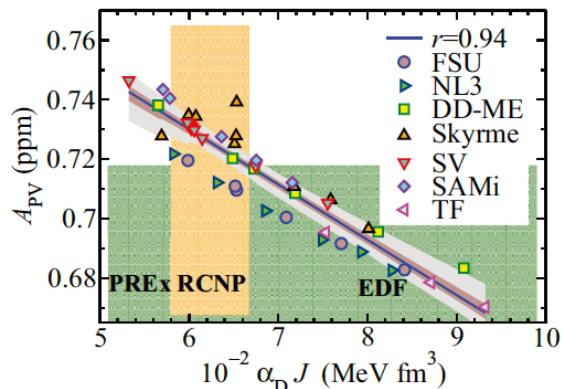


Tidal Deformation



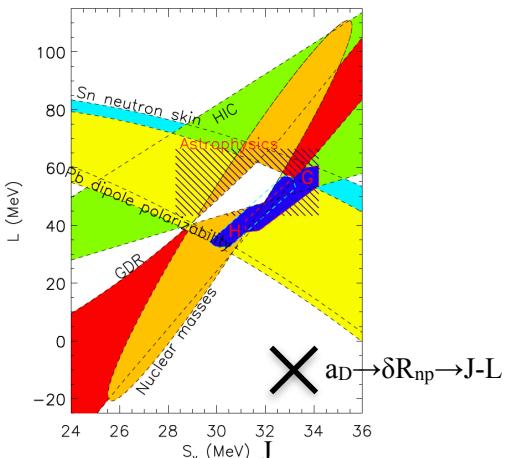


C.J. Horowitz et al., JPG41, 093001(2014)



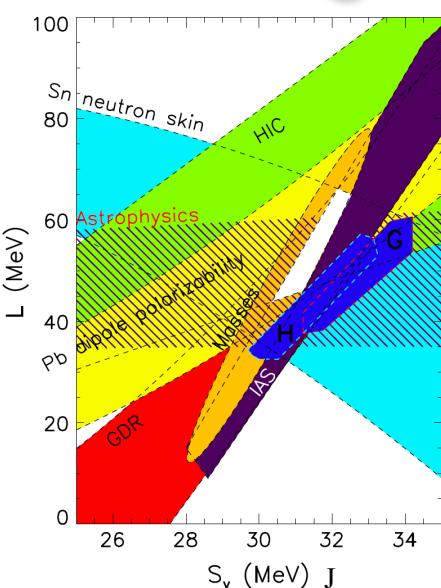
Roca-Maza et al, PRC88, 024316(2013)

PREX:  $A_{\text{PV}} = 0.656 \pm 0.060_{\text{stat}} \pm 0.014_{\text{syst}}$  ppm.



Lattimer and Lim, AJ771, 51(2013)

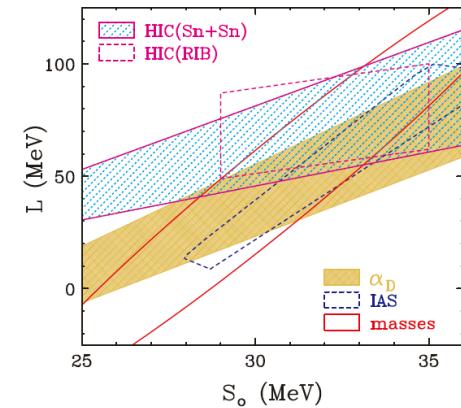
\*PREX-II  
in preparation for exp.



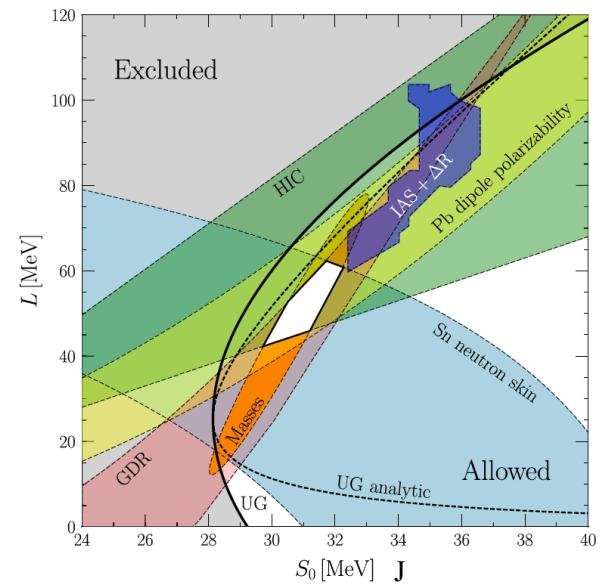
Lattimer and Steiner, EPJA50, 40(2014)

Lattimer, GenRelativGravit 46, 1713(2014)

Roca-Maza and Paar, PPNP101, 96(2018)



C.J. Horowitz et al., JPG41, 093001(2014)



Tew, Lattimer, Ohnishi, Kolomeitsev, ApJ848, 105(2017)

# Publications from Proton Inelastic Scattering Project

- **Electric Dipole Polarizability and the Symmetry Energy**

- J. Birkhan et al., Physical Review Letters **118**, 252501 (2017).  
T. Hashimoto et al., Physical Review C **92**, 031305 (2015).  
A. Tamii et al., Butsuri **69**, 6 (2014).  
A. Tamii et al., European Physical Journal A **50**, 28 (2014).  
A. Tamii et al., Physical Review Letters **107**, 062502 (2011).

- Pygmy Dipole Resonance

- A. M. Krumbholz et al., Physics Letters B **744**, 7 (2015).  
C. Iwamoto et al., Physical Review Letters **108**, 262501 (2012).  
I. Poltoratska et al., Physical Review C **85**, 041304 (2012).

- Spin-M1 Strengths

- M. Mathy et al., Physical Review C **95**, 044616 (2017)  
J. Birkhan et al., Physical Review C **93**, 041302 (2016).  
H. Matsubara et al., Physical Review Letters **115**, 102501 (2015).

- Gamma Strength Function and Nuclear Level Densities

- D. Martin et al., Physical Review Letters **119**, 182503 (2017).  
R. W. Fearick et al., Physical Review C **97**, 044325 (2018).  
S. Bassauer et al., Physical Review C **94**, 054313 (2016).  
I. Poltoratska et al., Physical Review C **89**, 054322 (2014).

- Technical Development

- H. Matsubara et al., Nucl. Inst. Meth. A **678**, 122 (2012).  
H. Matsubara et al., Nucl. Inst. Meth. B **267**, 3682 (2009).  
A. Tamii et al., Nucl. Inst. Meth. A **605**, 326 (2009).

- Gamma Decay Coincidence

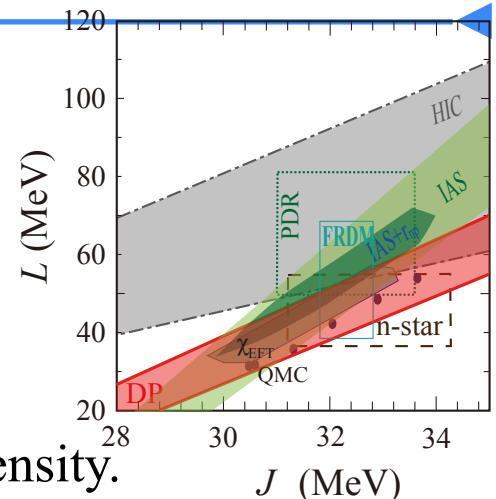
- M.S. Reen et al., submitted to PRC  
N. Kobayashi et al. submitted to EPJA  
C. Sullivan et al, Physical Review C **98**, 015804 (2018)

- Review Papers

- A. Bracco, E. G. Lanza and A. Tamii,  
Prog. in Part. Nucl. Phys., **106**, 360 (2019).  
(E1 response of nuclei)
- P. von Neumann-Cosel and A. Tamii,  
to be published in EJPA (2019);  
[arXiv:1903.11159 \[nucl-ex\]](https://arxiv.org/abs/1903.11159)  
(proton inelastic scattering)

# Summary

- The **electric dipole polarizability** (EDP) of  $^{208}\text{Pb}$ ,  $^{120}\text{Sn}$ , and  $^{48}\text{Ca}$  were measured precisely with Coulomb excitation by proton scattering.
- Constraint bands in the  $J$ - $L$  plane has been determined that describes the **symmetry energy** at and below the saturation density.
- The result from the laboratory nuclear experiments is consistent with the information from GW170817. Further observation of N-Star merger GW's are anticipated.



## Works in near future

- More experimental data are still in the analysis:  
Sn isotopes, Zn isotopes,  $^{154}\text{Sm}$
- Gamma-decay of Giant Resonances: damping mechanism and fine structure
- Systematic measurement on E1 with  $\gamma$ , p,  $\alpha$ -decays for nuclei  $A \leq \sim 60$ .

*RCNP, Osaka University*

A. Tamii, H. Matsubara, H. Fujita, K. Hatanaka,  
H. Sakaguchi Y. Tameshige, M. Yosoi and J. Zenihiro

*IKP, TU-Darmstadt*

P. von Neumann-Cosel, A-M. Heilmann,  
Y. Kalmykov, I. Poltoratska, V.Yu. Ponomarev,  
A. Richter and J. Wambach

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T. Adachi and L.A. Popescu

*IFIC-CSIC, Univ. of Valencia*

B. Rubio and A.B. Perez-Cerdan

*Sch. of Science Univ. of Witwatersrand*

J. Carter and H. Fujita

*iThemba LABS*

F.D. Smit

*Texas A&M Commerce*

C.A. Bertulani

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K. Nakanishi,  
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*Dep. of Phys., Kyushu University*

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Y. Shimbara

<sup>120</sup>Sn

# RCNP-316 Collaboration

T. Hashimoto<sup>†</sup>, A. M. Krumbholz<sup>1</sup>, A. Tamii<sup>2</sup>, P. von Neumann-Cosel<sup>1</sup>, N. Aoi<sup>2</sup>,  
O. Burda<sup>2</sup>, J. Carter<sup>3</sup>, M. Chernykh<sup>2</sup>, M. Dozono<sup>4</sup>, H. Fujita<sup>2</sup>, Y. Fujita<sup>2</sup>,  
K. Hatanaka<sup>2</sup>, E. Ideguchi<sup>2</sup>, N. T. Khai<sup>5</sup>, C. Iwamoto<sup>2</sup>, T. Kawabata<sup>6</sup>,  
D. Martin<sup>1</sup>, K. Miki<sup>1</sup>, R. Neveling<sup>7</sup>, H. J. Ong<sup>2</sup>, I. Poltoratska<sup>1</sup>, P.-G. Reinhard<sup>8</sup>,  
A. Richter<sup>1</sup>, F.D. Smit<sup>6</sup>, H. Sakaguchi<sup>2,4</sup>, Y. Shimbara<sup>9</sup>, Y. Shimizu<sup>4</sup>, T. Suzuki<sup>2</sup>,  
M. Yosoi<sup>1</sup>, J. Zenihiro<sup>4</sup>, K. Zimmer<sup>1</sup>

<sup>†</sup>Institute for Basic Science, Korea

<sup>1</sup>IKP, Technische Universität Darmstadt, Germany

<sup>2</sup>RCNP, Osaka University, Japan

<sup>3</sup>Wits University, South Africa

<sup>4</sup>RIKEN, Japan

<sup>5</sup>Institute for Nuclear Science and Technology (INST), Vietnam

<sup>6</sup>Kyoto University, Japan

<sup>7</sup>iThemba LABs, South Africa

<sup>8</sup>Institut Theoretical Physik II, Universität Erlangen-Nürnberg, Germany

<sup>9</sup>CYRIC, Tohoku University, Japan

# Collaboration $^{48}\text{Ca}$

---



TECHNISCHE  
UNIVERSITÄT  
DARMSTADT

Experiment: Darmstadt-Osaka

Theory: Darmstadt-Tennessee-TRIUMF

S. Bacca (TRIUMF)

S. Bassauer (TUD)

J. Birkhan (Darmstadt)

G. Hagen (ORNL)

H. Matsubara (RCNP)

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P. von Neumann-Cosel (TUD)

T. Papenbrock (U Tennessee)

N. Pietralla (TUD)

A. Richter (TUD)

A. Schwenk (TUD)

A. Tamii (RCNP)

Thank you

for your attention