

NEWS colloquium
2024. 11. 29

Alpha clusters in nuclear surface

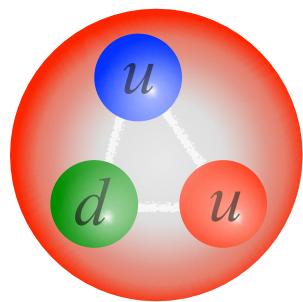
Junki Tanaka
RCNP, Osaka University
RCNP $\text{Sn}(p,p\alpha)$ collaboration
ONOKORO collaboration

Correlation and Clustering

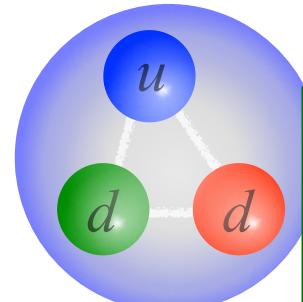


Credits: NASA, ESA, CSA, I. Labbe (Swinburne University of Technology) and R. Bezanson (University of Pittsburgh). Image processing: Alyssa Pagan (STScI)

Quarks

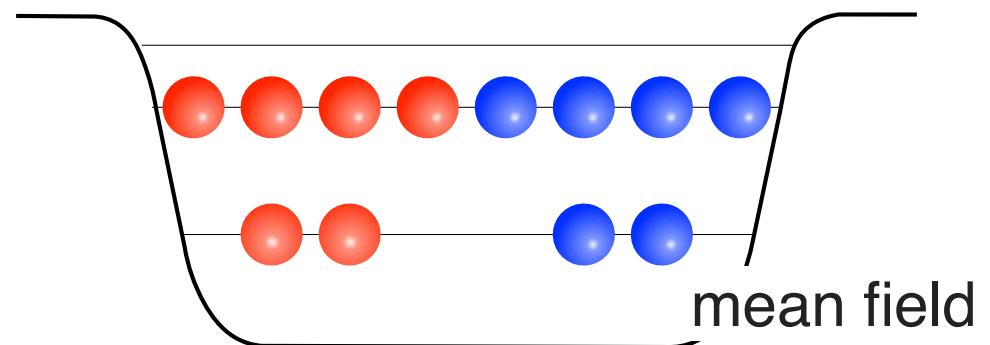


proton



neutron

Atomic Nuclei



The properties of the nucleus can be roughly explained by a model using a mean-field composed of all nucleons.

Clustering

Correlation and clustering are universal phenomenon that appears in all hierarchies of nature, from the universe to the quarks.

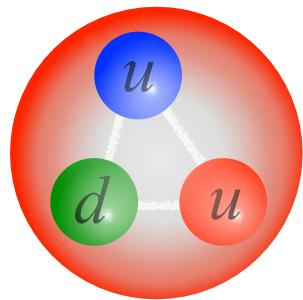
Clustering



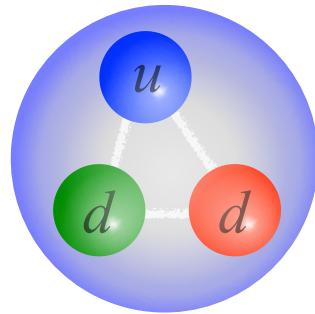
Universe

Credits: NASA, ESA, CSA, I. Labbe (Swinburne University of Technology) and R. Bezanson (University of Pittsburgh). Image processing: Alyssa Pagan (STScI)

Quarks

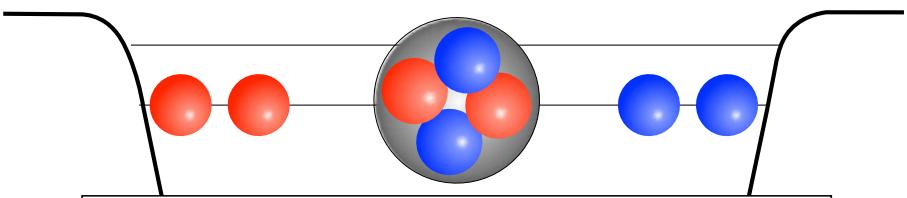


proton

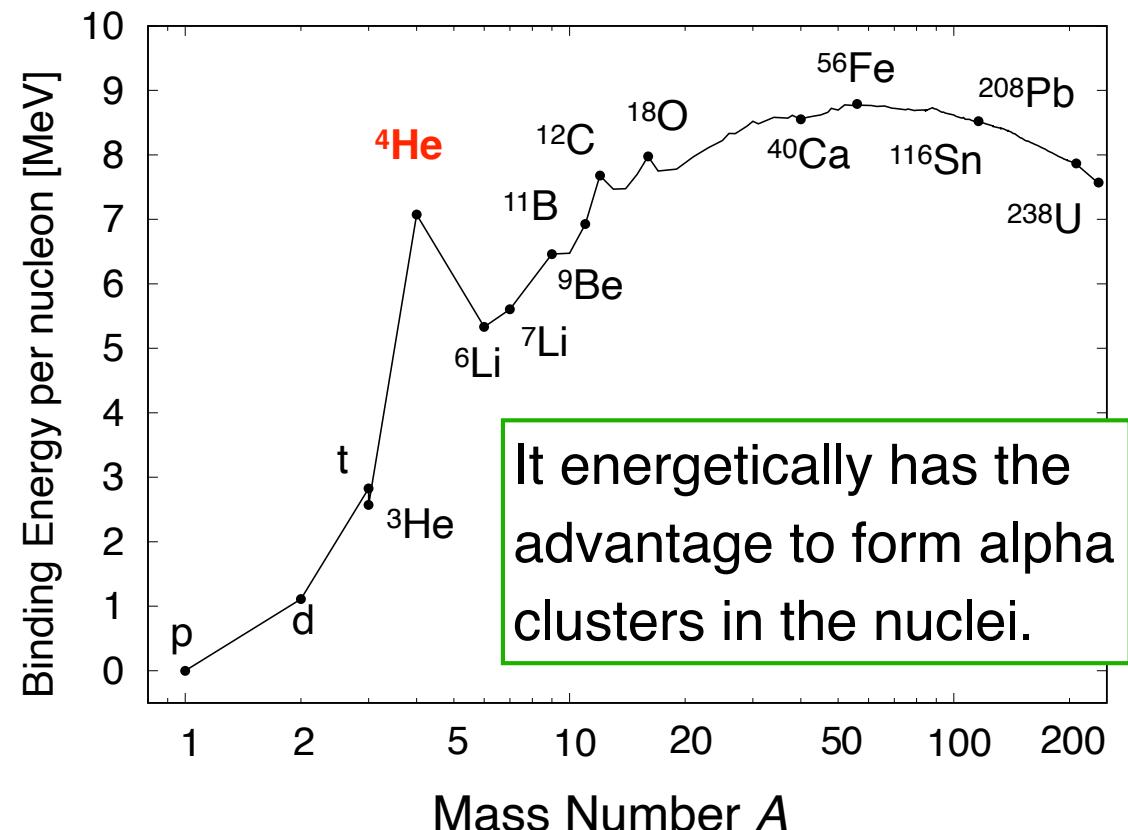


neutron

Atomic Nuclei

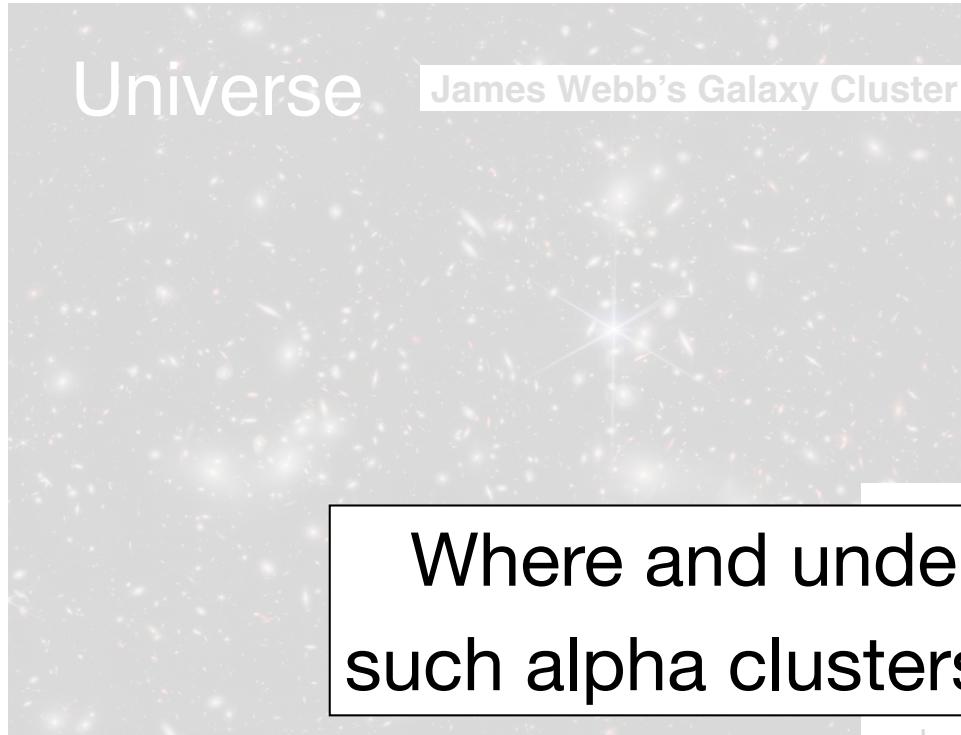


Multi-nucleons behave as if they are single particles!!



It energetically has the advantage to form alpha clusters in the nuclei.

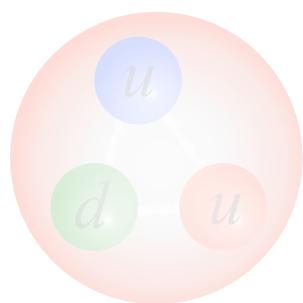
Clustering



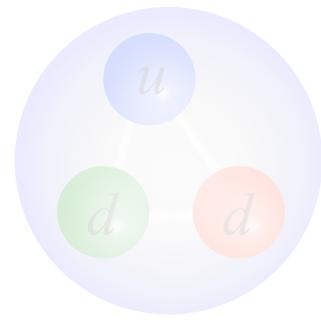
Where and under what conditions do such alpha clusters appear in the nuclei?

Credits: NASA, ESA, CSA, I. Labbe (Swinburne University of Technology) and R. Bezanson (University of Pittsburgh). Image processing: Alyssa Pagan (STScI)

Quarks

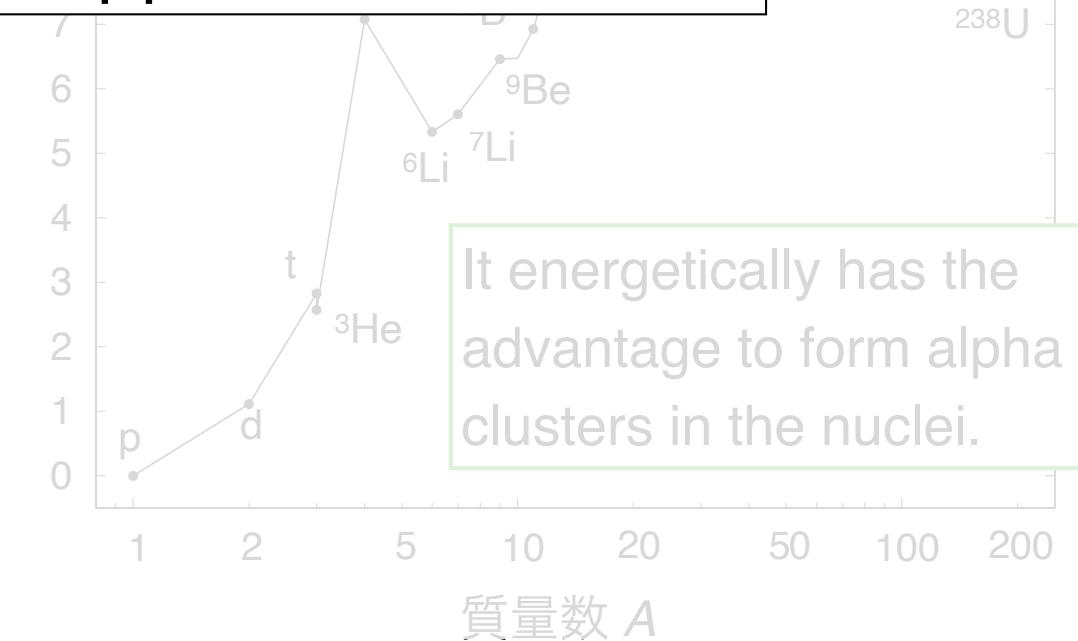


proton



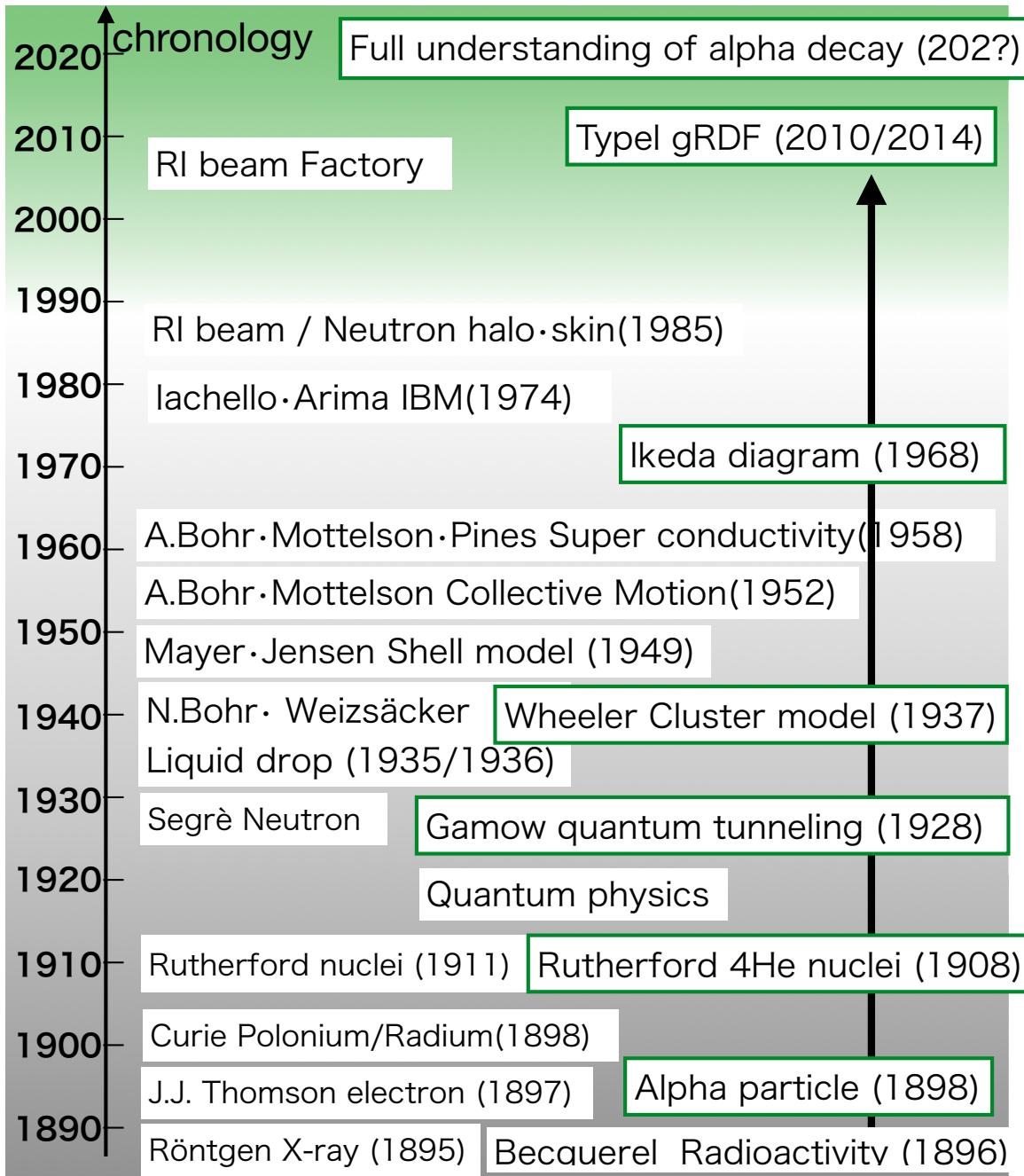
neutron

核子あたり結合エネルギー



It energetically has the advantage to form alpha clusters in the nuclei.

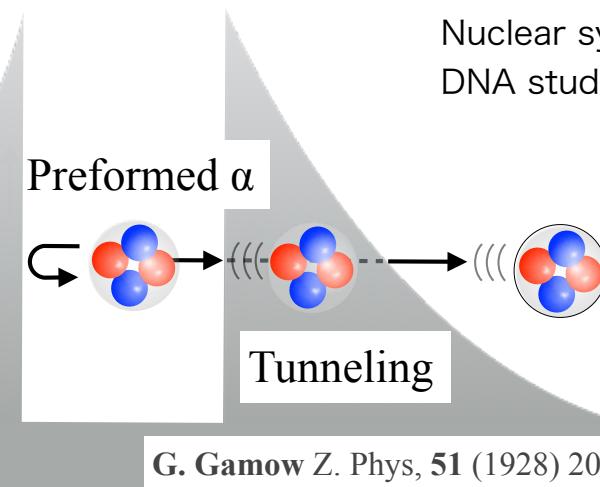
Alpha clusters in the ground state of heavy nuclei



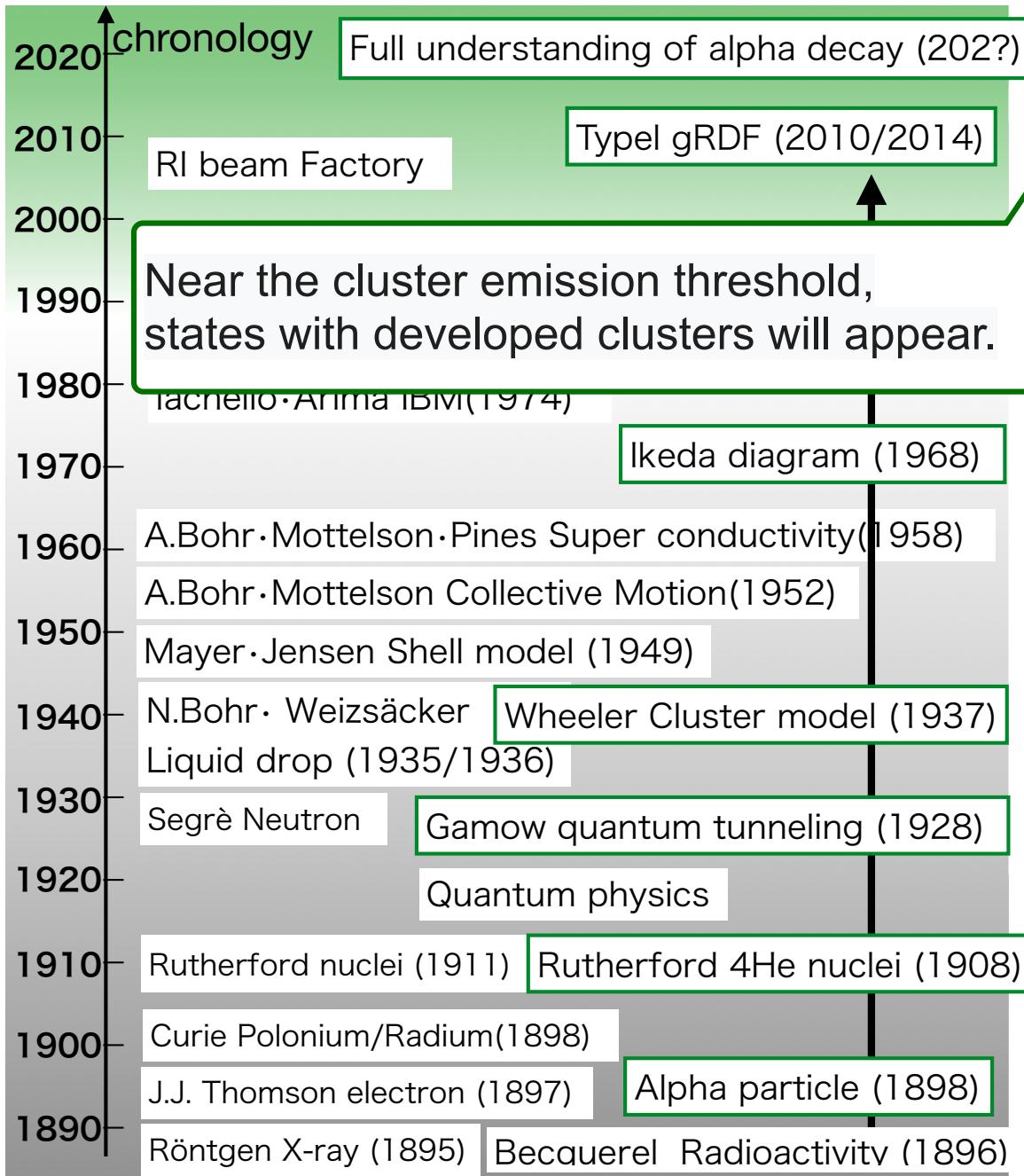
Alpha decay theory



George Gamow
Alpha decay theory
Big Bang theory
Cosmic MW BG
Nuclear synthesis
DNA studies

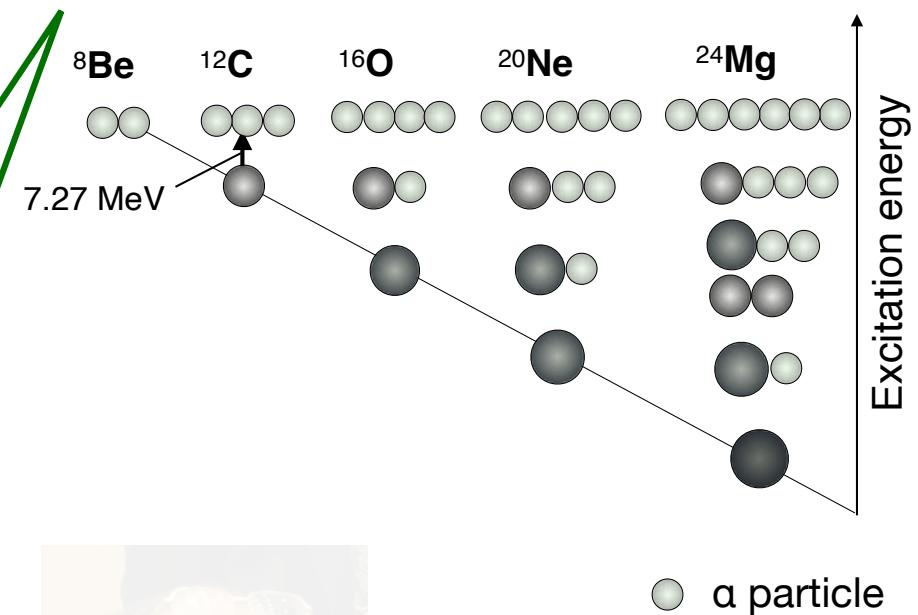


Alpha clusters in the ground state of heavy nuclei



Ikeda Diagram

K. Ikeda Prog. Theo. Phys.
Suppl. E68 (1968) 464

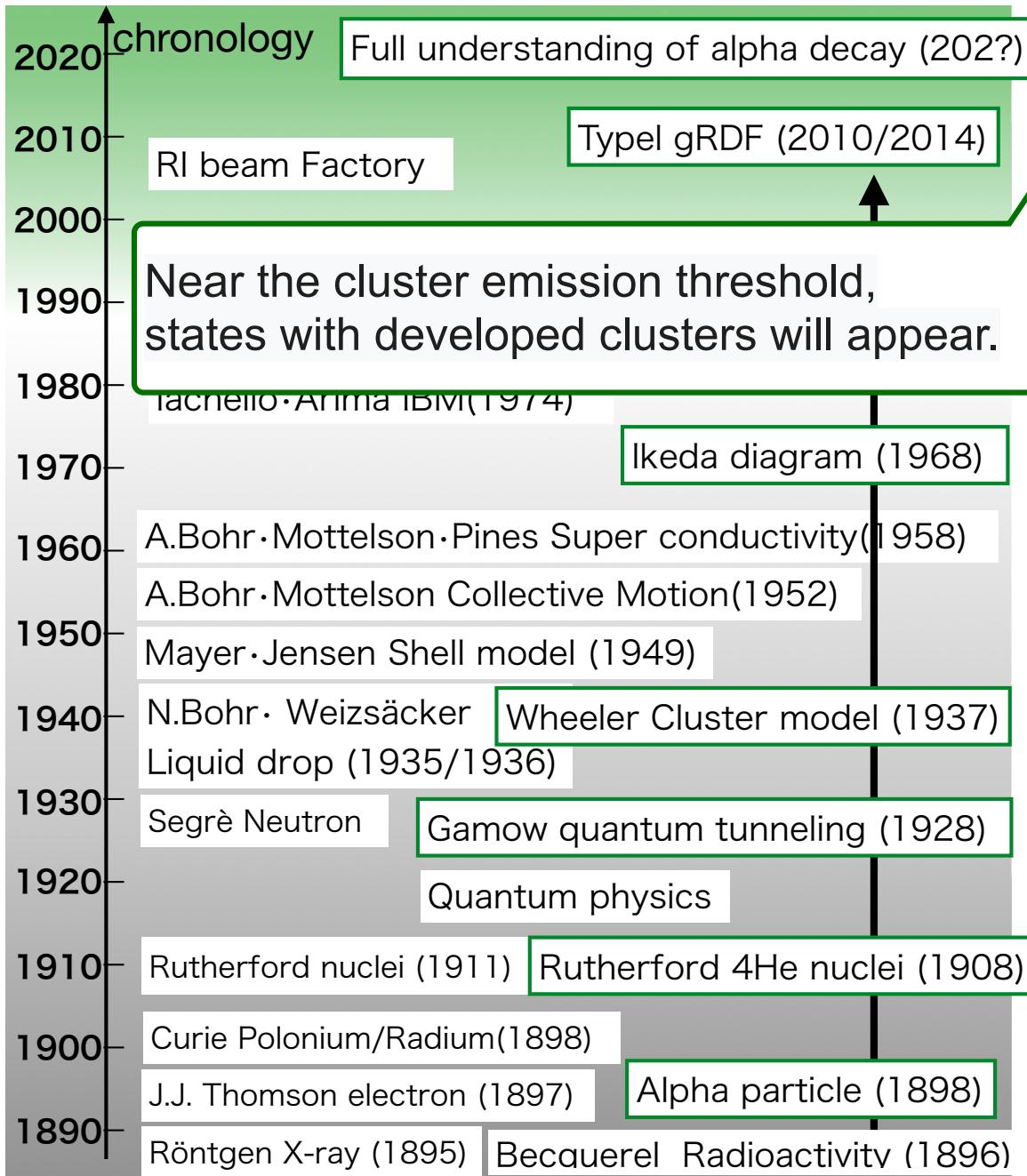


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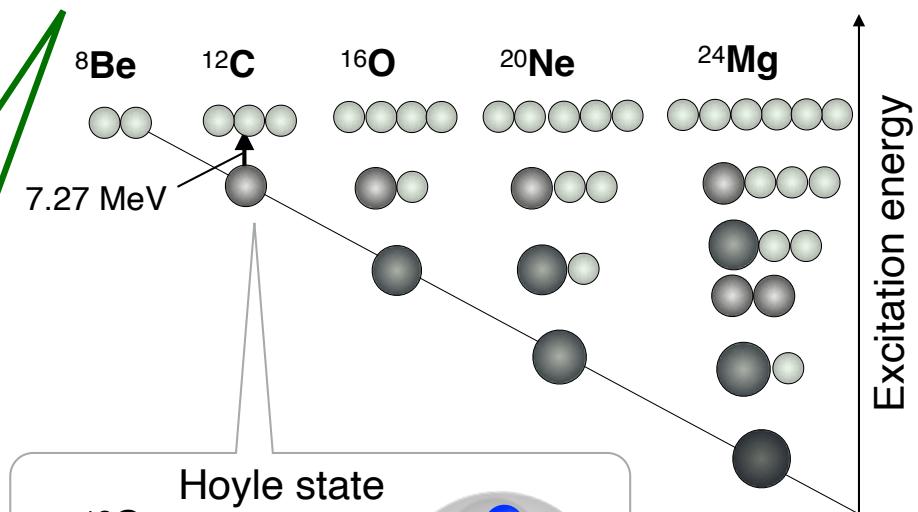
Kiyomi Ikeda

Ikeda diagram
soft dipole resonance
Ikeda sum rule

Alpha clusters in the ground state of heavy nuclei



Ikeda Diagram



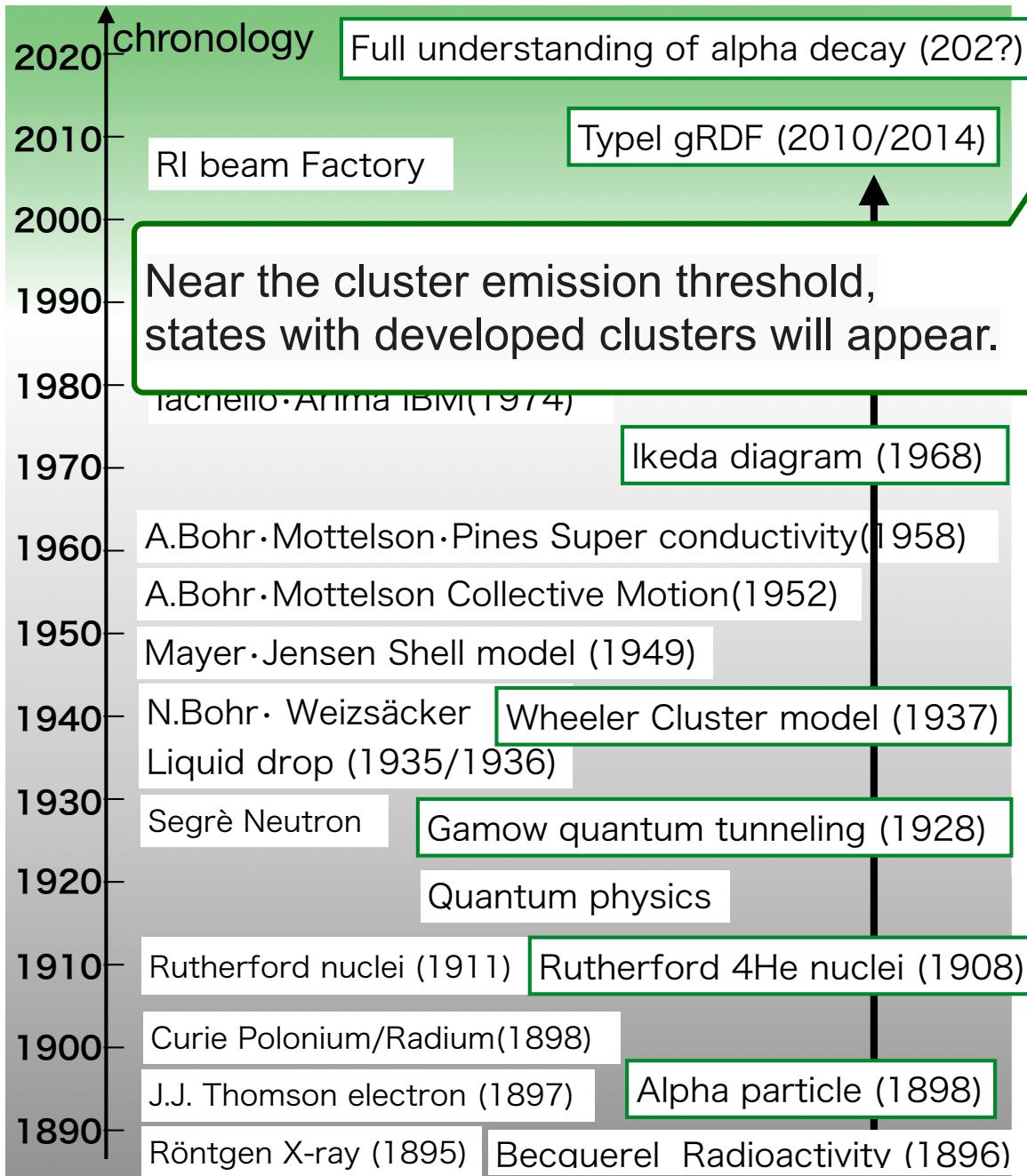
K. Ikeda Prog. Theo. Phys.
Suppl. E68 (1968) 464

^{12}C 7.65 MeV
Hoyle state

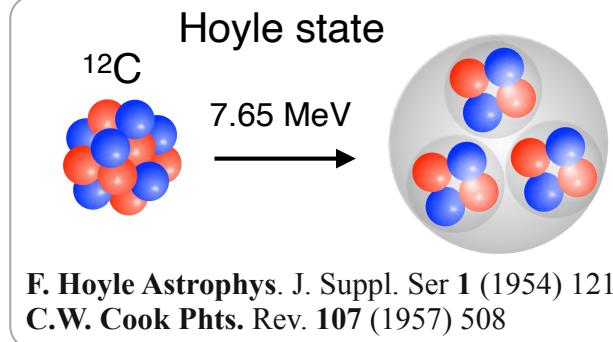
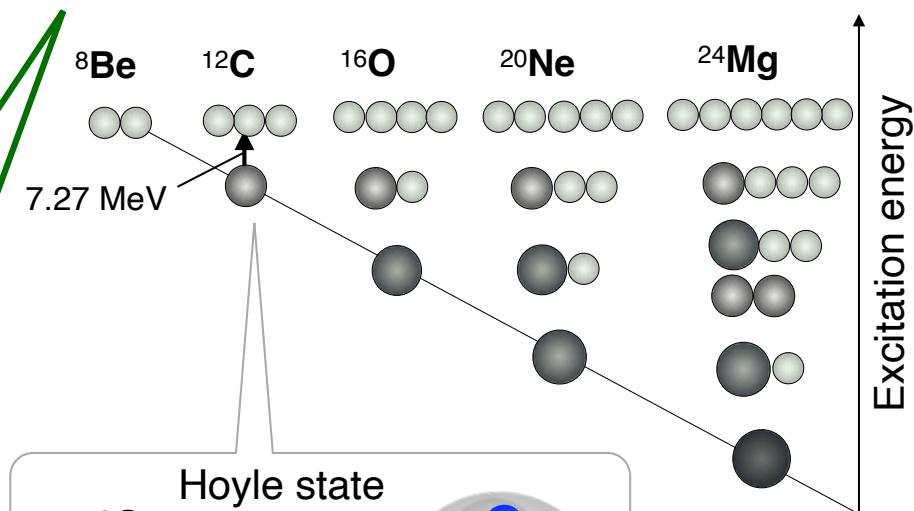
F. Hoyle Astrophys. J. Suppl. Ser 1 (1954) 121
C.W. Cook Ph.D. Rev. 107 (1957) 508

The Hoyle state plays an important role in nature, such as in the synthesis of ^{12}C in stars through the triple-alpha reaction.

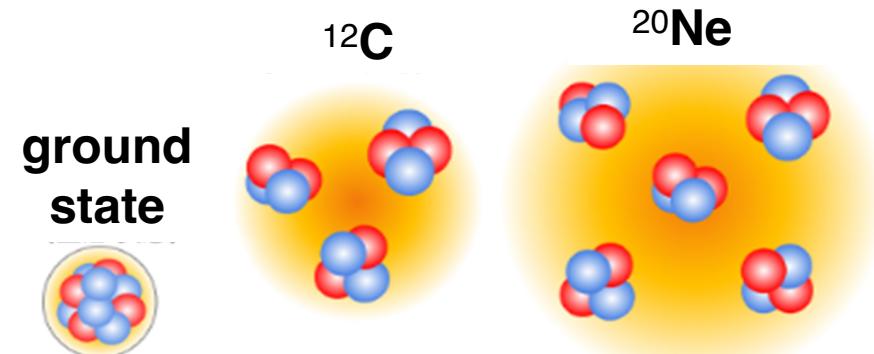
Alpha clusters in the ground state of heavy nuclei



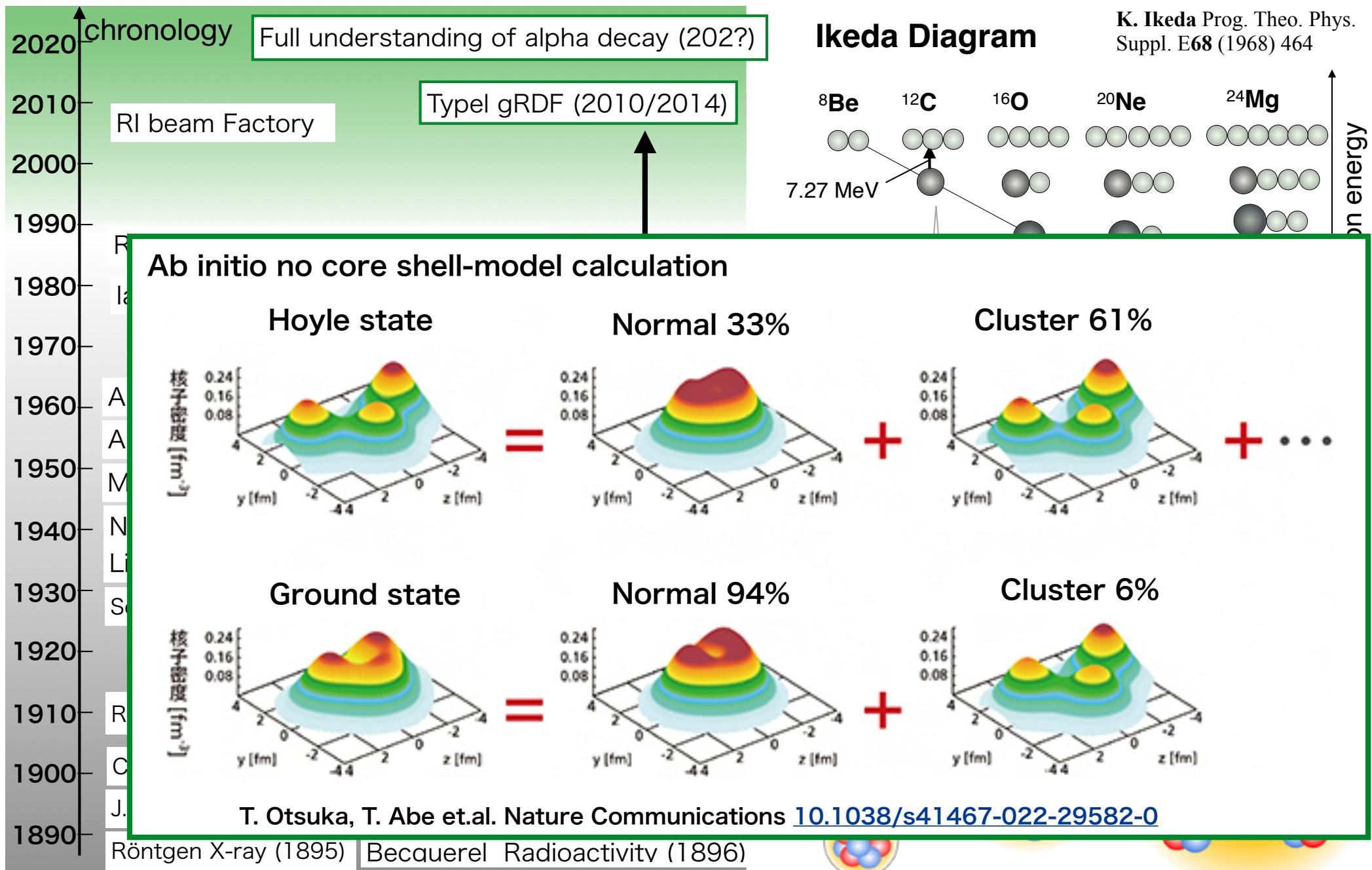
Ikeda Diagram



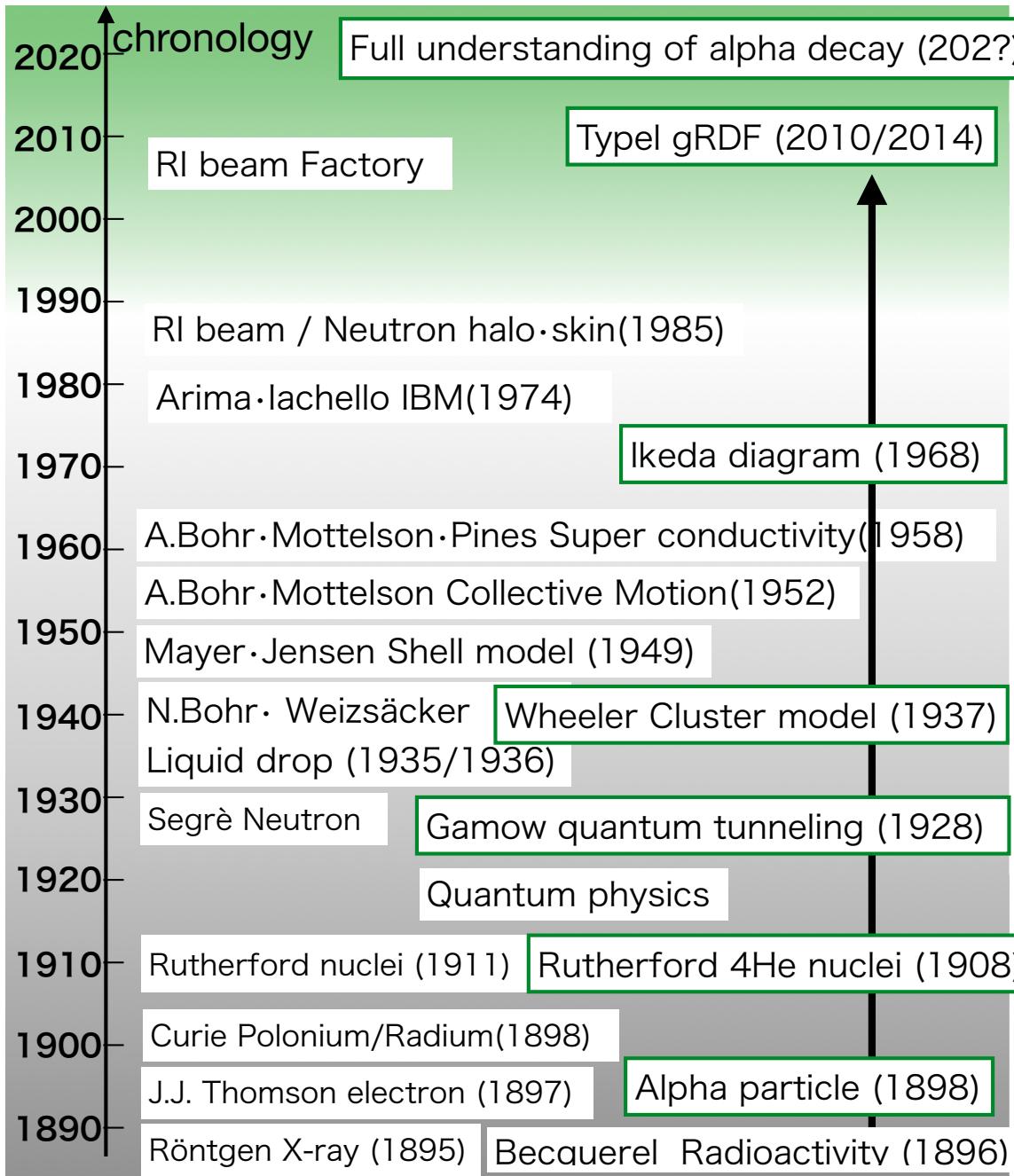
Alpha condensate states studies



Alpha clusters in the ground state of heavy nuclei



Alpha clusters in the ground state of heavy nuclei



Success of theories to explain the bulk part of atomic nuclei

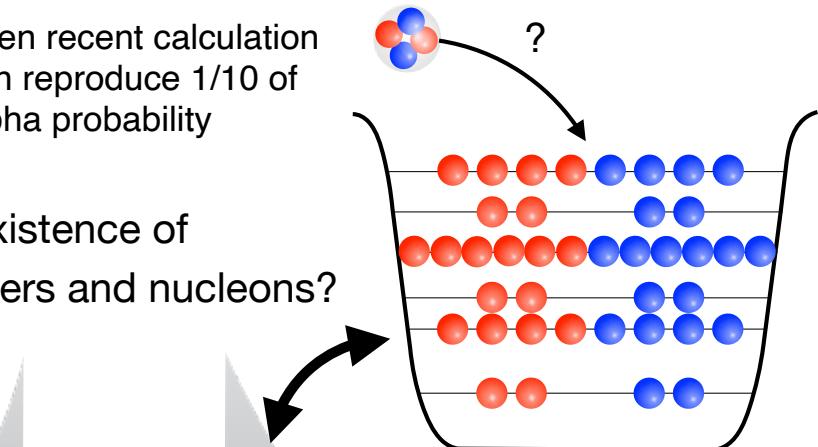
- Liquid drop model
 - Shell model
 - Collective model
- ↔
- Cluster model
 - limited in light nuclei ?

✓ Tonozuka, Arima- shell model calculation → 1/14

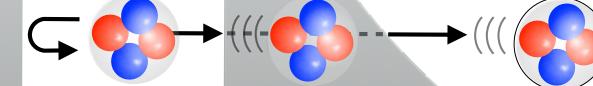
I. Tonozuka and A. Arima, Nucl. Phys. A 323, 45 (1979)

✓ Even recent calculation can reproduce 1/10 of alpha probability

Coexistence of clusters and nucleons?



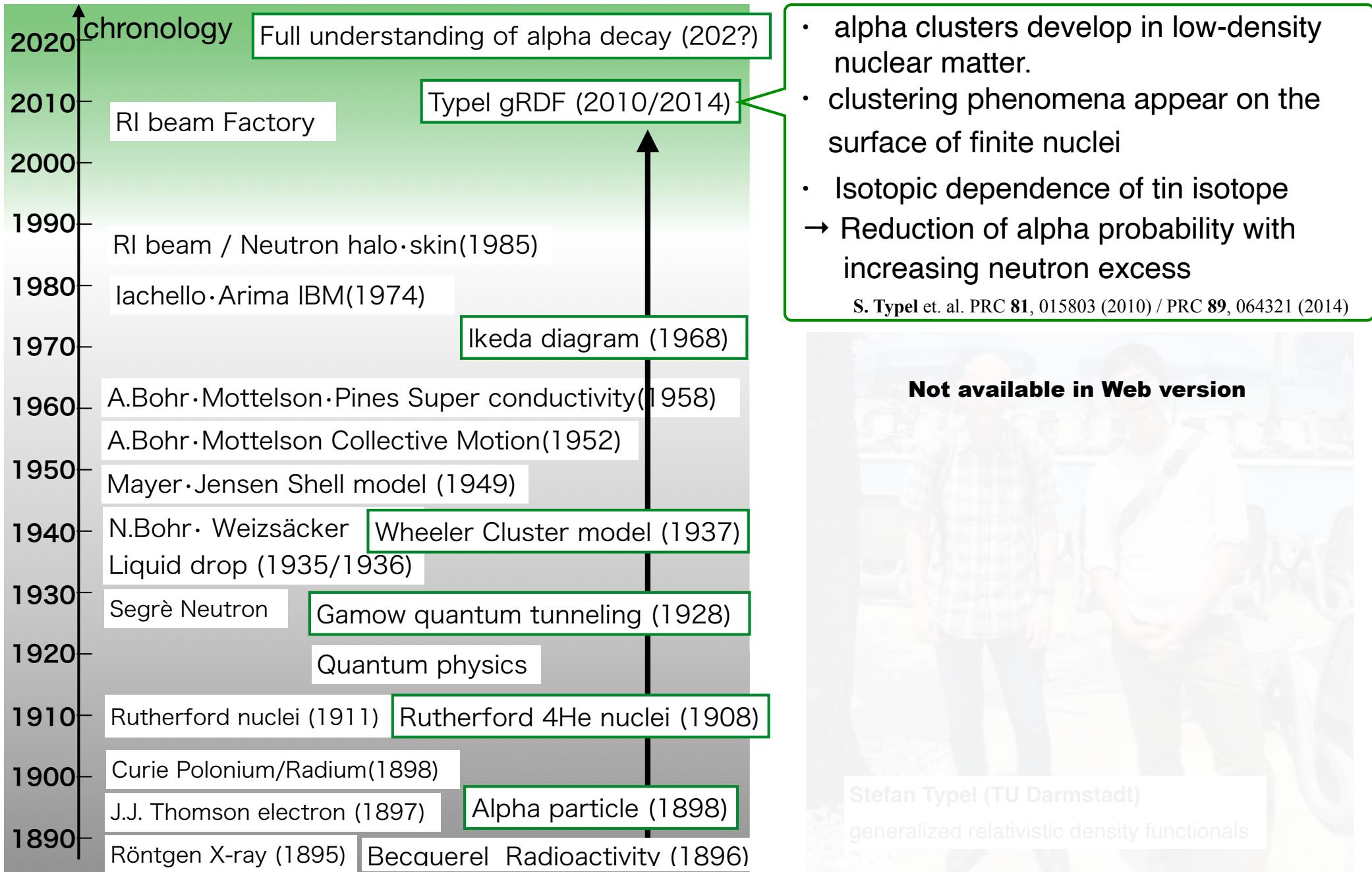
Preformed α



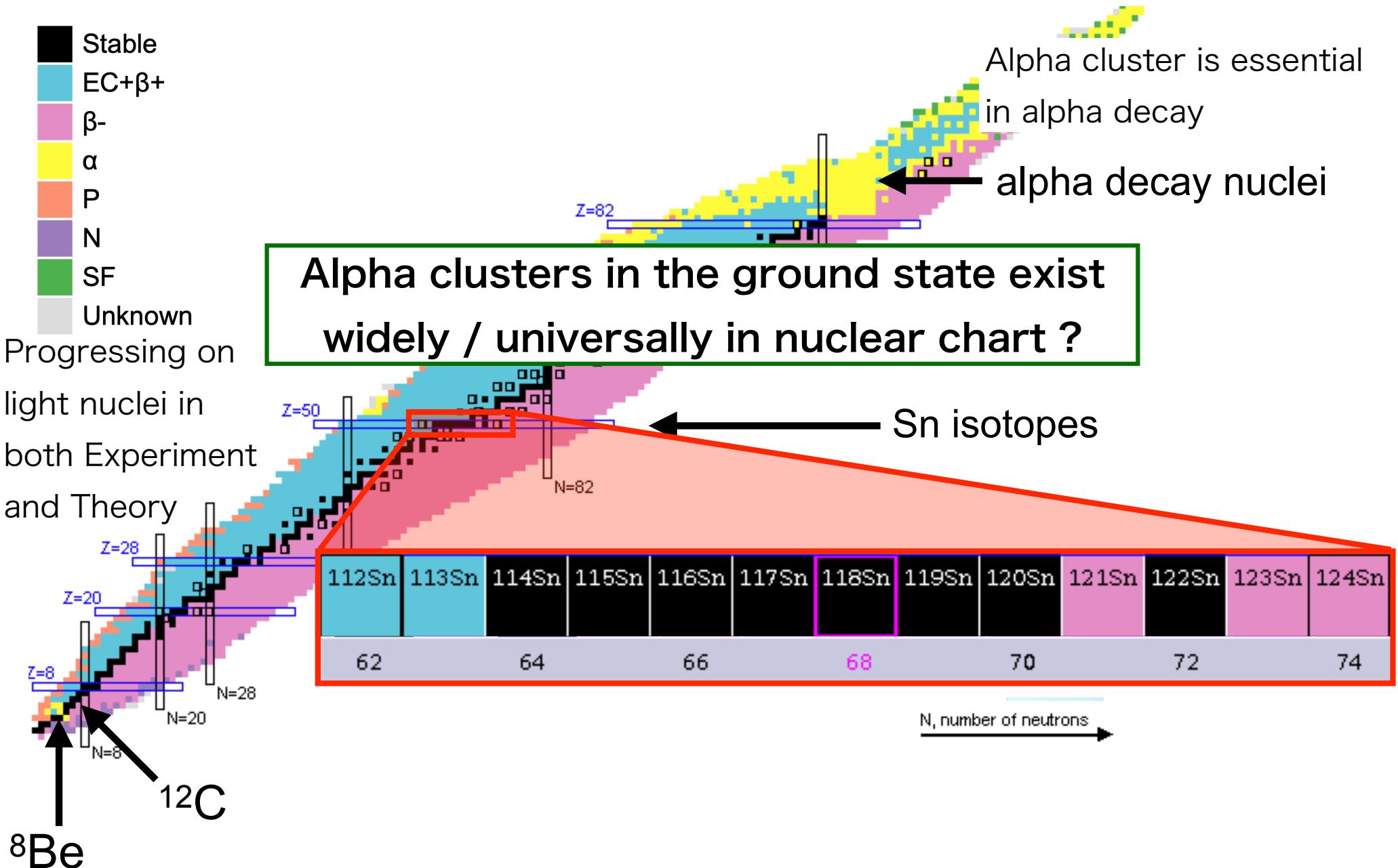
Tunneling

G. Gamow Z. Phys, 51 (1928) 204

Alpha clusters in the ground state of heavy nuclei



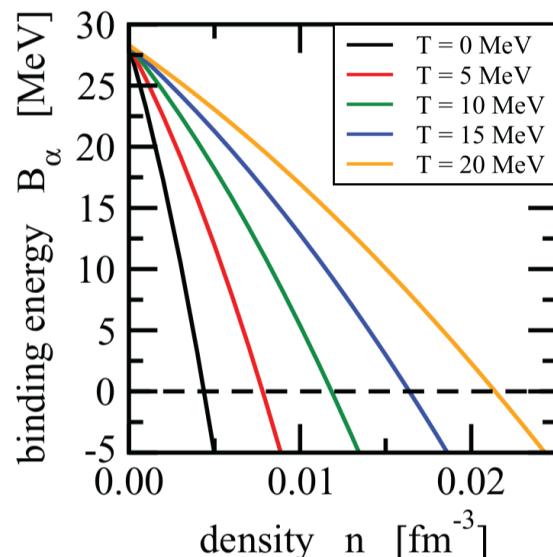
Alpha clusters in the ground state of heavy nuclei



Alpha cluster formation predicted in gRDF

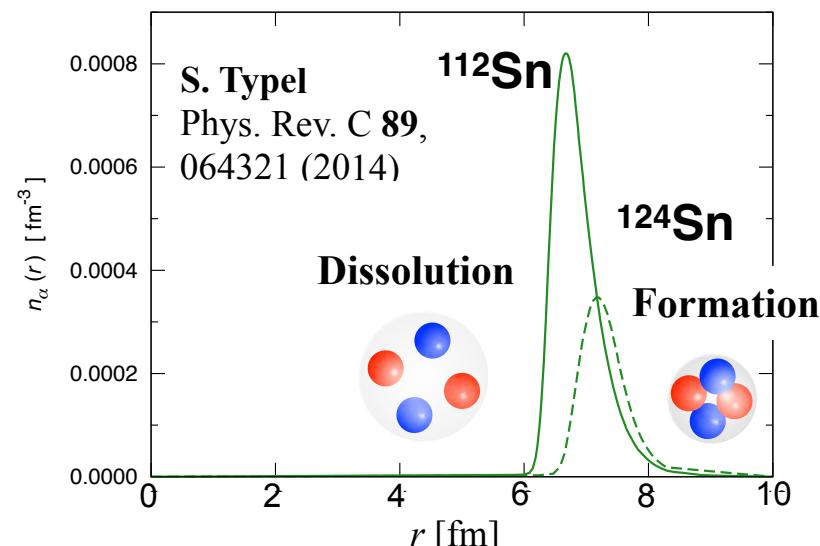
- ✓ Binding energy of alpha particles varies according to the nucleon density.
- ✓ Density is zero, it corresponds to the binding energy of a naked alpha particle
- ✓ When density is increased, the binding energy decreases, and the clusters dissolve.
- ✓ Properties of the infinite system of nuclear matter are applied to the finite nuclei.
- ✓ These degrees of freedom of alpha particles are explicitly taken into account, it determines the most energetically stable distribution of alpha particles.

Binding energy of alpha cluster changes in the nuclear matter



S. Typel et. al.
Phys. Rev. C **81**,
015803 (2010)

Alpha cluster formation and dissolution based on density functionals



Alpha cluster formation predicted in gRDF

trial density function

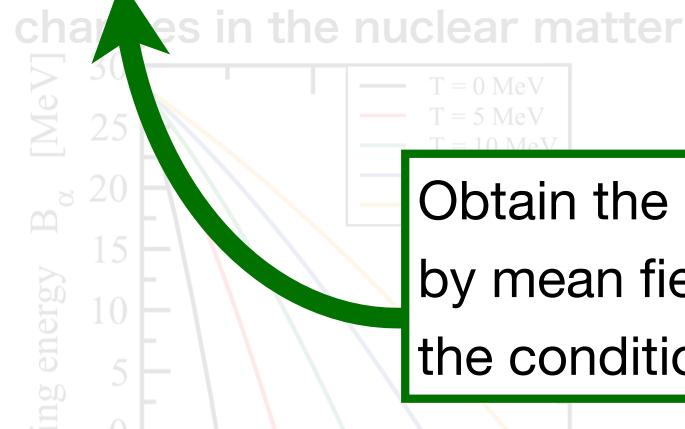
$$\rho_\alpha / \rho_p / \rho_n$$

Nucleons on the surface are used to form alpha clusters and are reduced

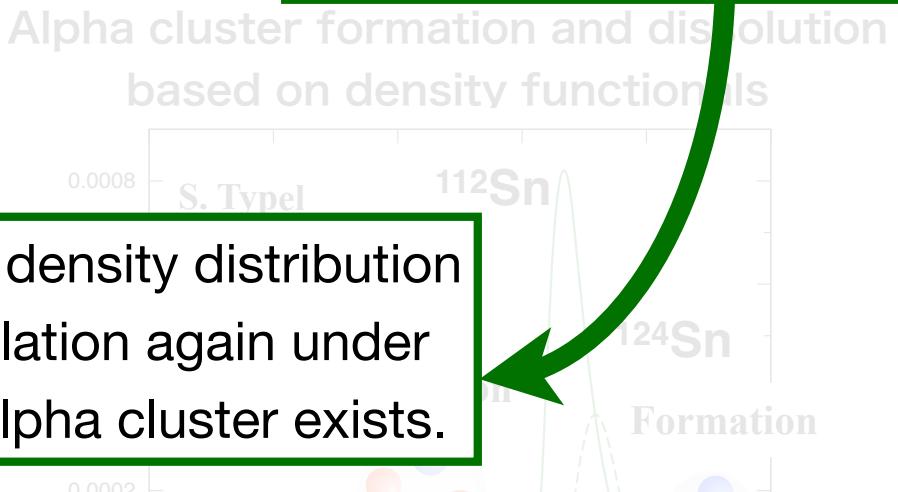
- ✓ Density is zero, it corresponds to the binding energy of a naked alpha particle
- ✓ When density is increased, the binding energy decreases, and the clusters dissolve.
- ✓ Properties of the infinite system of nuclear matter are applied to the finite nuclei.

Again applying the results to the formation and dissolution of alpha clusters

The bulk part of the nucleus is no longer the lowest in energy.



Obtain the nucleon density distribution by mean field calculation again under the condition that alpha cluster exists.

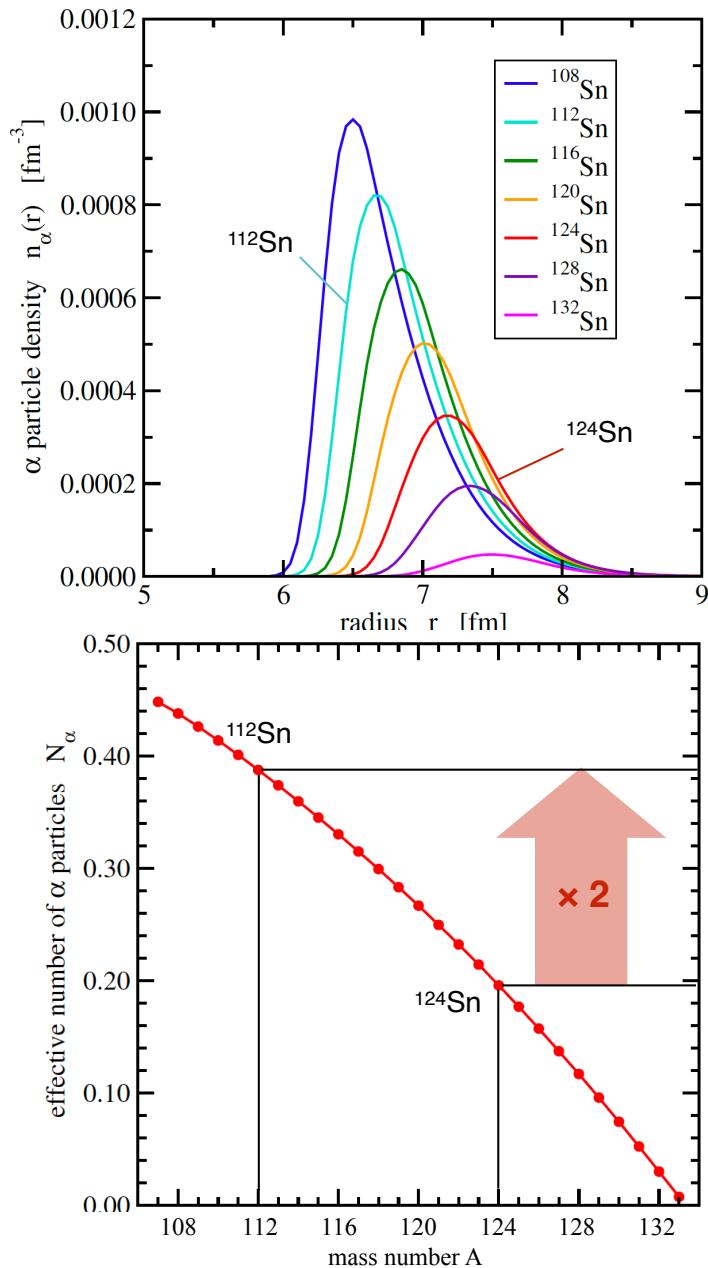


Determine the distribution of alpha clusters self-consistently with the bulk part.

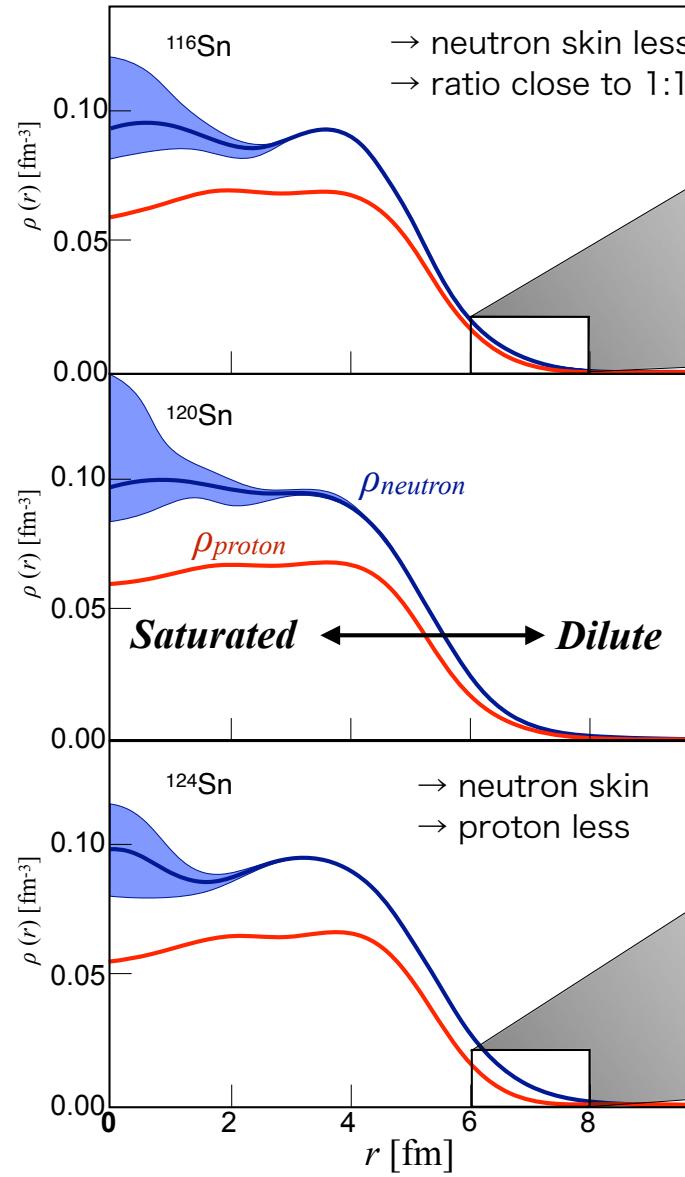
→ Determine the distribution of alpha particles that will be most energetically stable for the entire atomic nuclei.

Formation and dissolution of alpha clusters

S. Typel Phys. Rev. C 89, 064321 (2014)

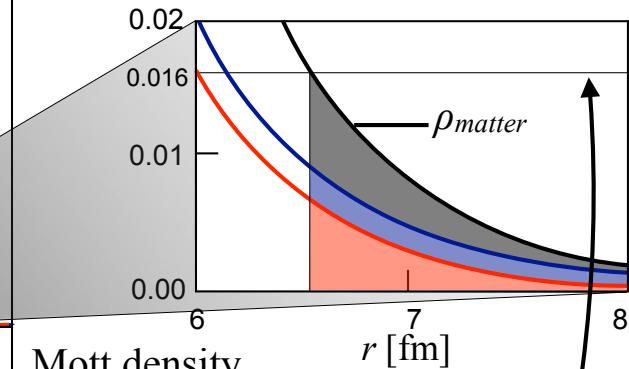


Proton/Neutron-density distributions



S. Terashima et.al.

Phys. Rev. C 77 (2008) 02317

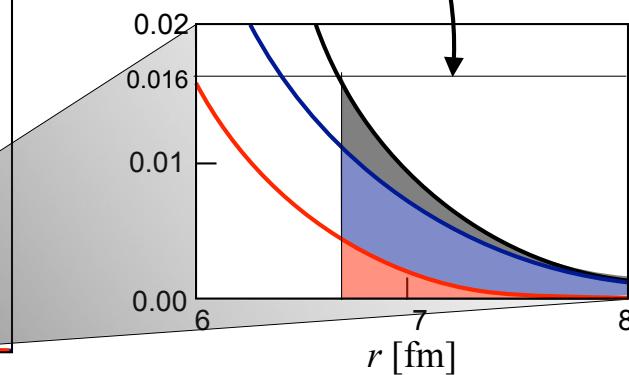


Mott density

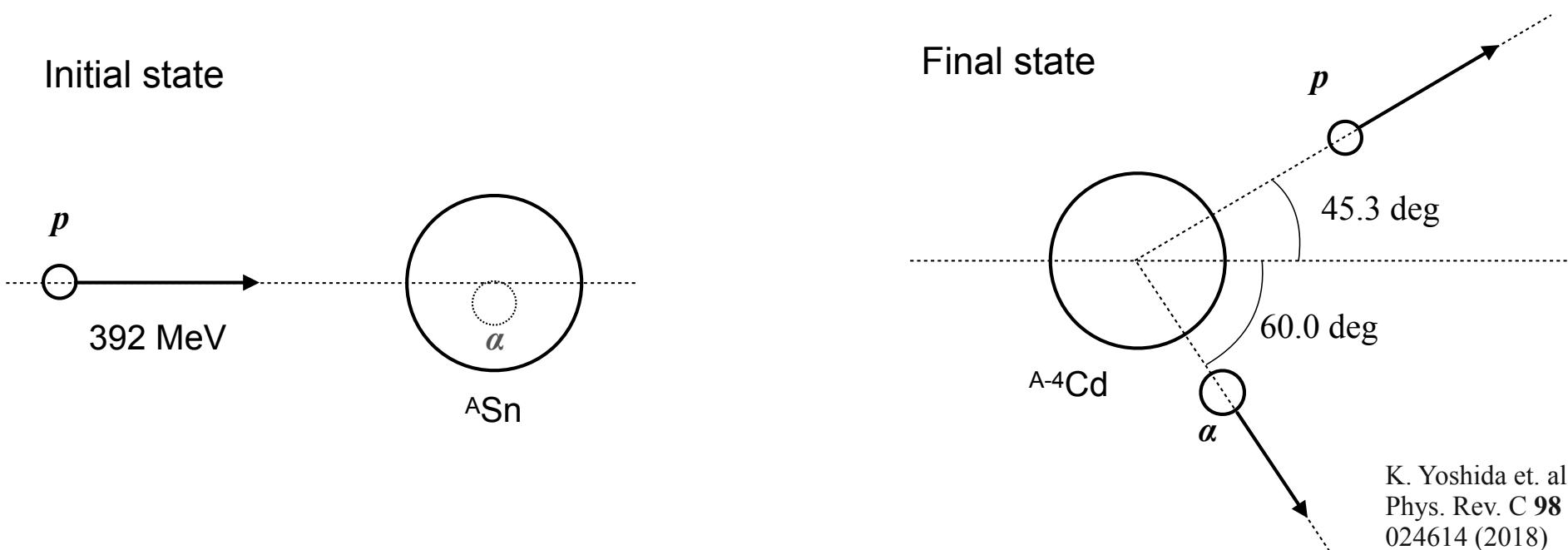
Below 1/10 of saturation
density 0.16 [fm $^{-3}$]

S. Typel et. al. Phys. Rev. C 81, 015803 (2010)
K. Hagel et. al. PRL. 108, 062702 (2012)

$\rho < 0.016$ [fm $^{-3}$]



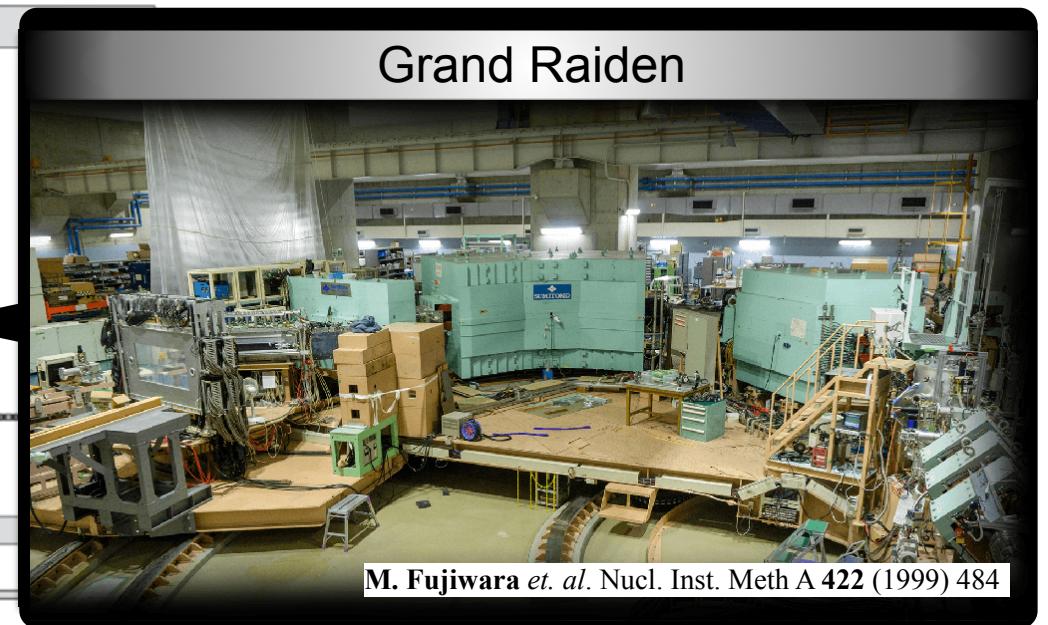
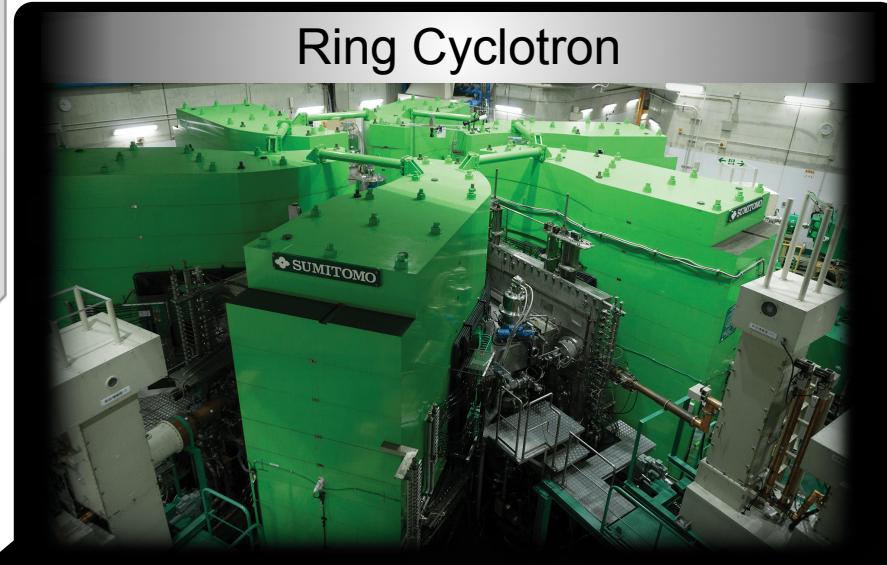
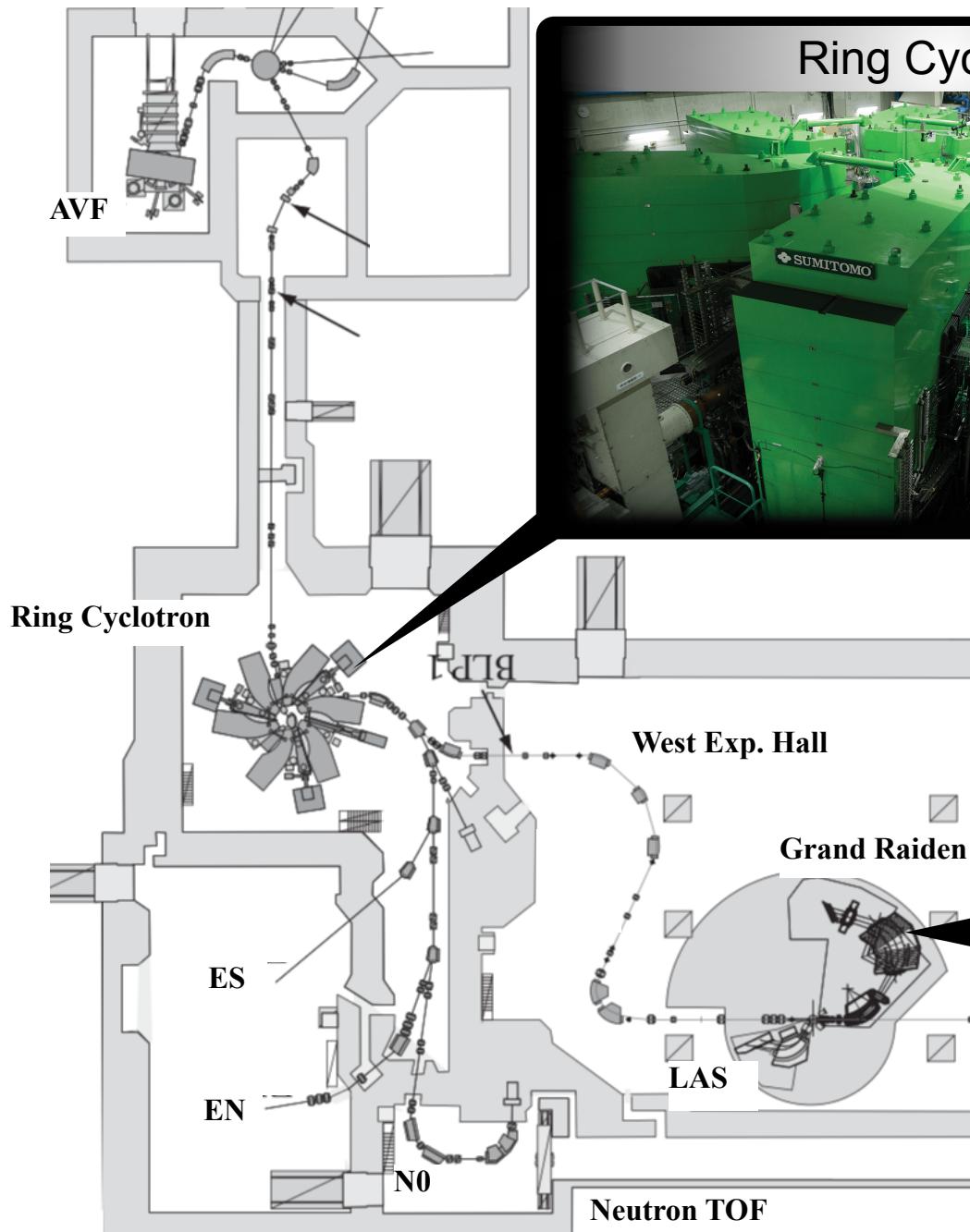
Quasi-Free Alpha knockout reaction



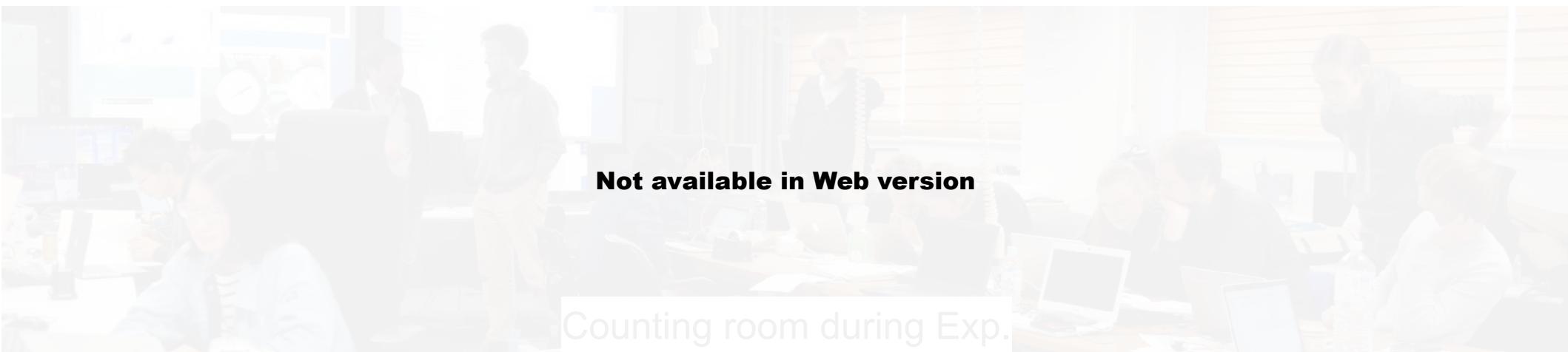
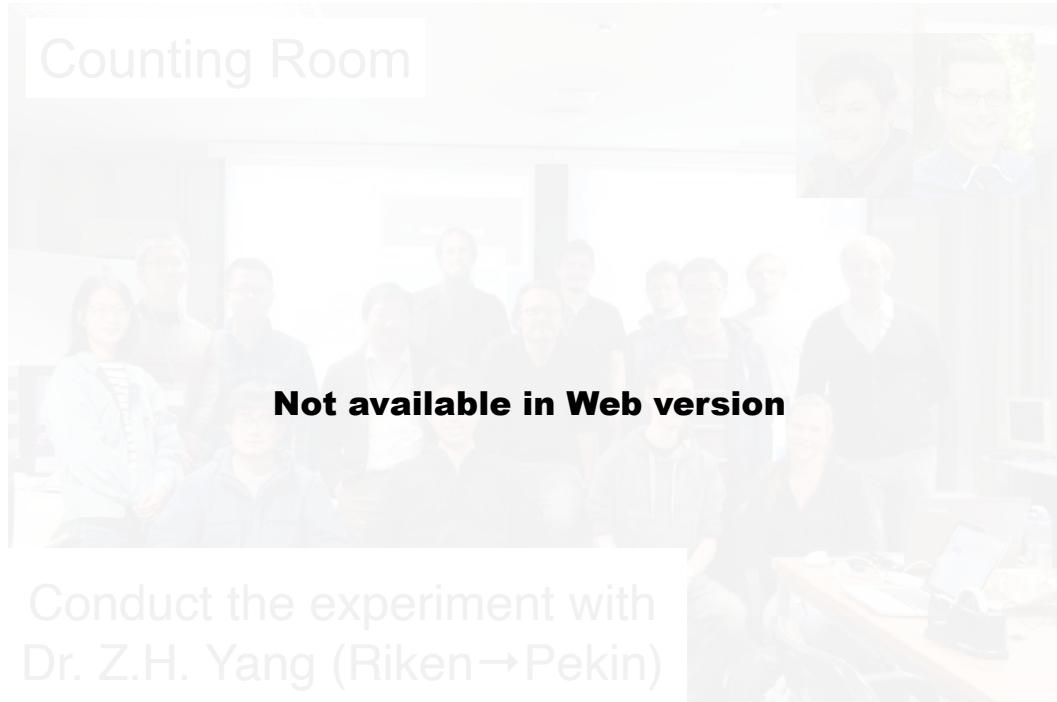
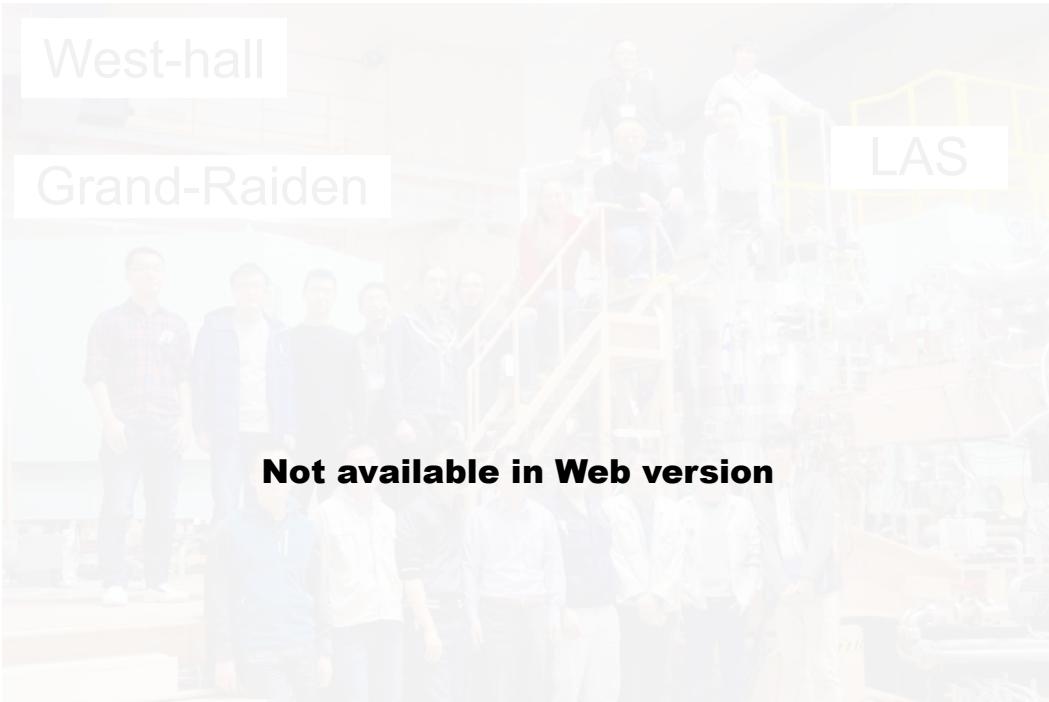
K. Yoshida et. al.
Phys. Rev. C **98**
024614 (2018)

- High-energy proton beam collides with the target nucleus.
 - At the moment of the reaction, momentum is transferred.
 - Alpha particles received momentum are ejected from the target.
 - If the momentum transfer is large,
 - the $(p, p\alpha)$ reaction is regarded to be $p\alpha$ elastic.
 - The residual nuclei are not disturbed by the reaction.
- If this condition holds, the reaction is called "quasi-free"
- The reaction cross-section is a good measure of the probability of alphas.

Experiment at RCNP Osaka University

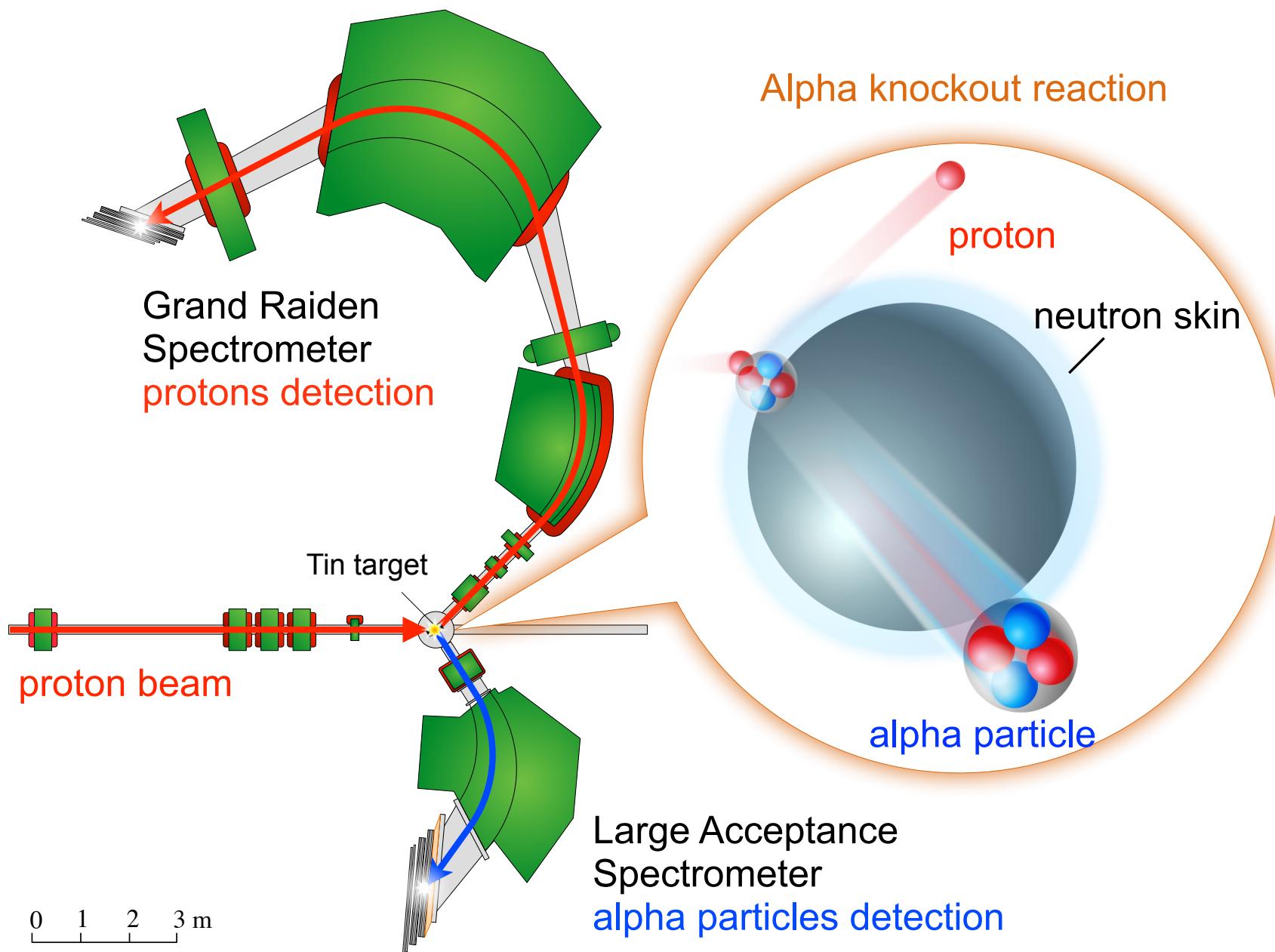


Experiment at RCNP Osaka University



(Feb. 2018)

Alpha knockout reaction using double-arm spectrometer



M. Fujiwara *et. al.* Nucl. Inst. Meth A 422 (1999) 484

Alpha separation energy spectrum

Energy Conservation

$$E_{p_{in}} + E_{Sn} = E_{p_{out}} + E_{\alpha} + E_{Cd}$$

$$\cancel{m_p} + T_{p_{in}} + m_{Sn} = \cancel{m_p} + T_{p_{out}} + m_{\alpha} + T_{\alpha} + m_{Cd} + T_{Cd}$$

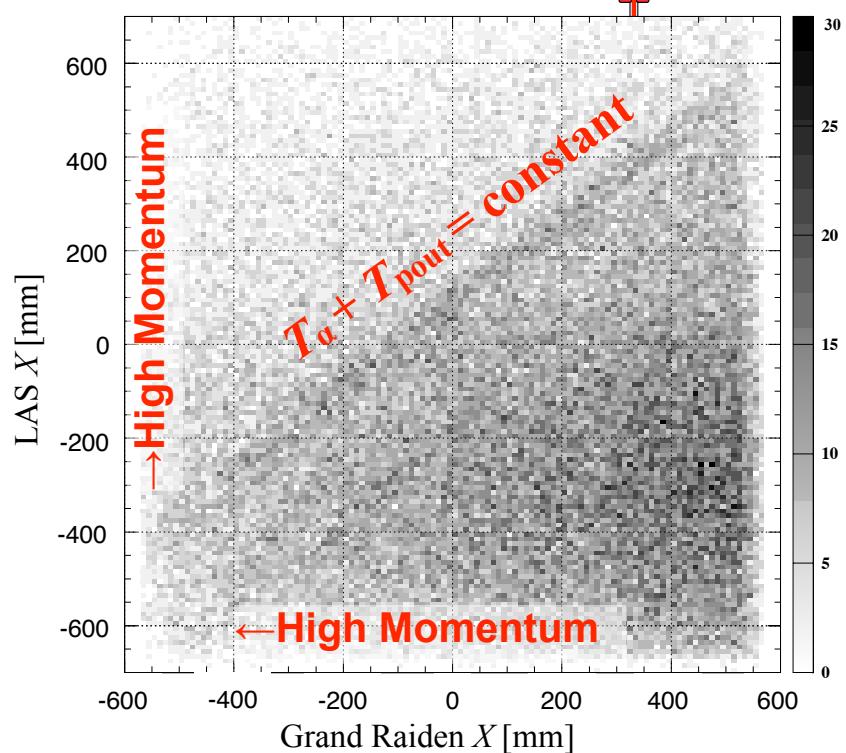
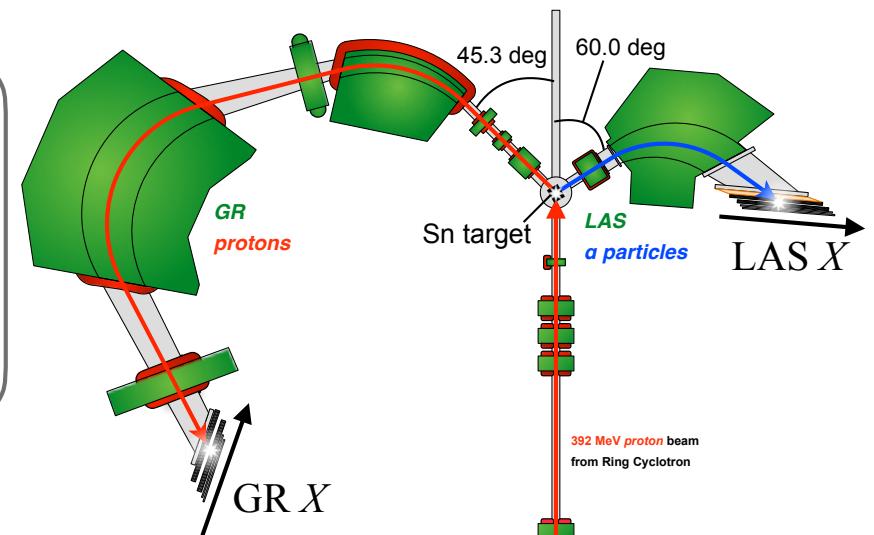
Alpha separation energy

$$S_{\alpha} \equiv m_{\alpha} + m_{Cd} - m_{Sn}$$

$$= T_{p_{in}} - (T_{p_{out}} + T_{\alpha} + \cancel{T_{Cd}})$$

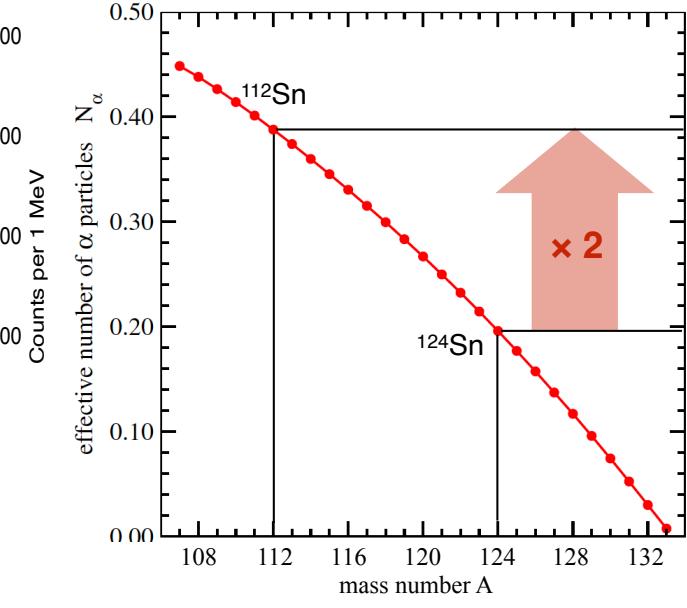
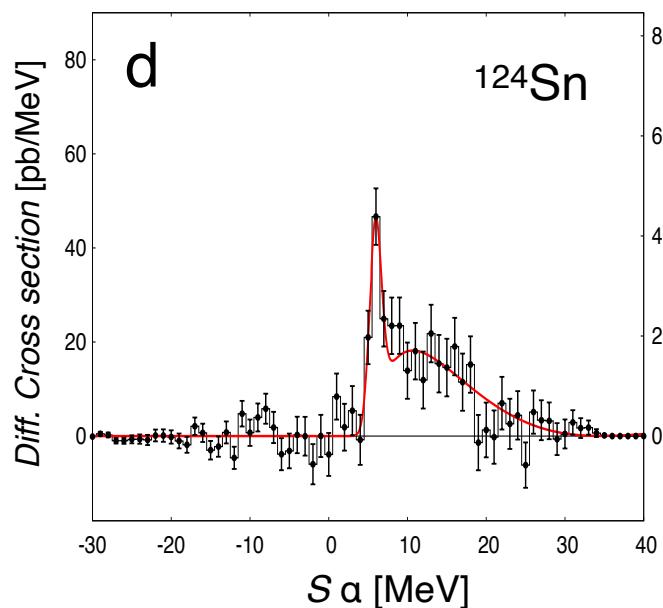
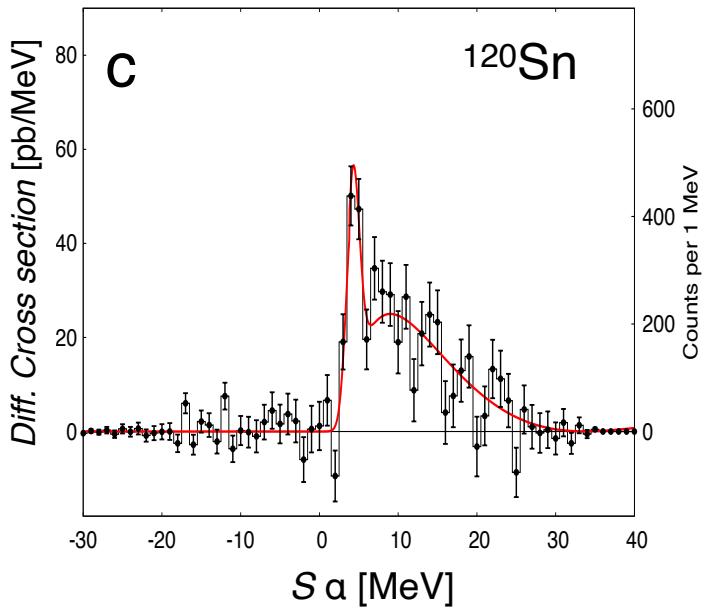
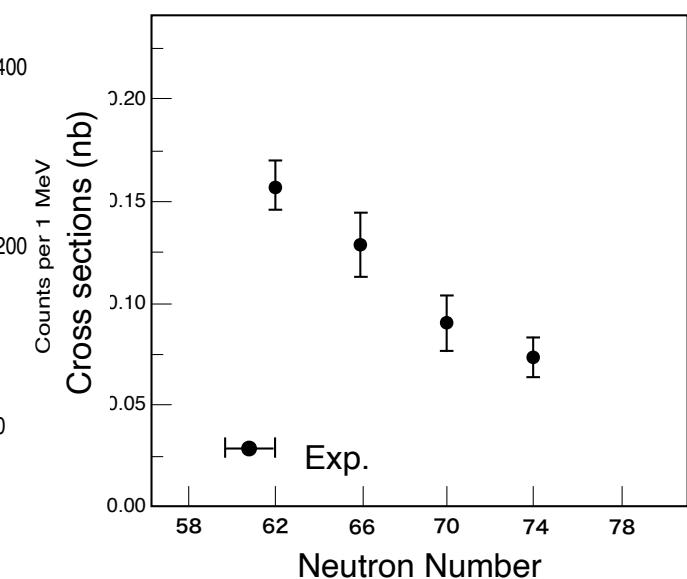
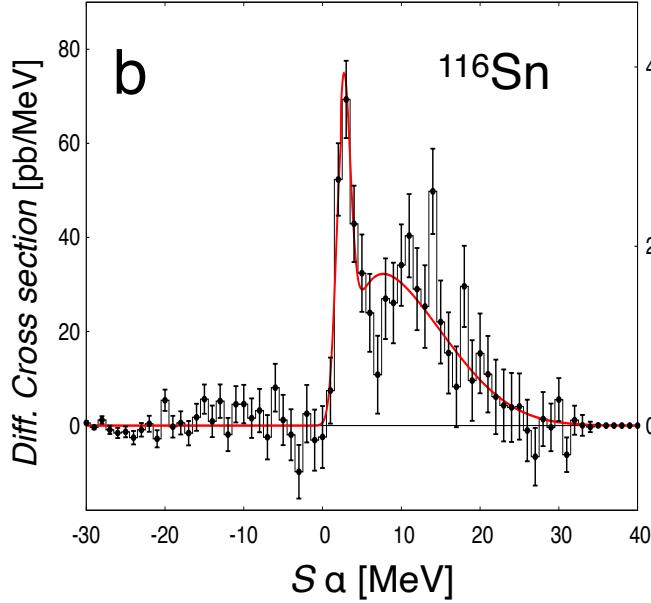
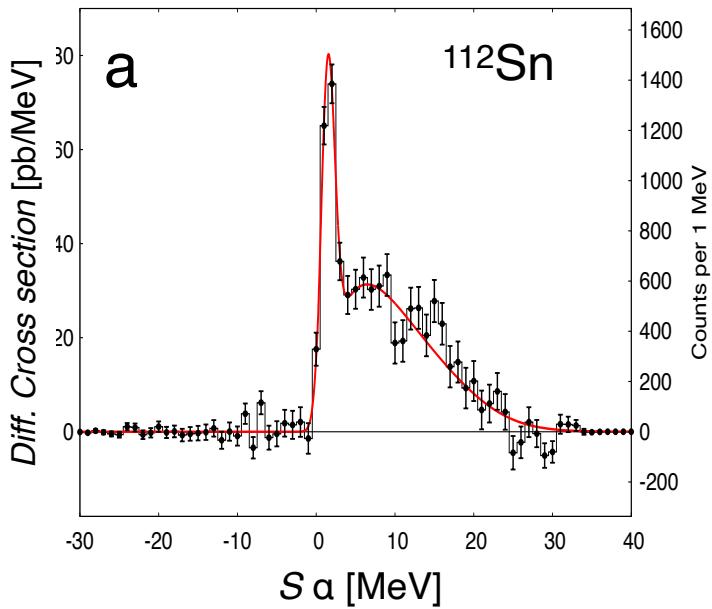
$$S_{\alpha} = T_{p_{in}} - (T_{p_{out}} + T_{\alpha})$$

$$T_{Cd} \sim \frac{|\vec{q}|^2}{2m_{Cd}} \sim \frac{|50|^2}{2 \cdot 931 \cdot 108} \sim 0.01 [MeV]$$



Alpha separation energy spectrum and its isotopic dependence

J. Tanaka, Z.H. Yang, S.Typel et al., Science 371, 260–264 (2021)



Reaction Analysis to convert predicted N_α into σ_α

Distorted wave impulse approximation

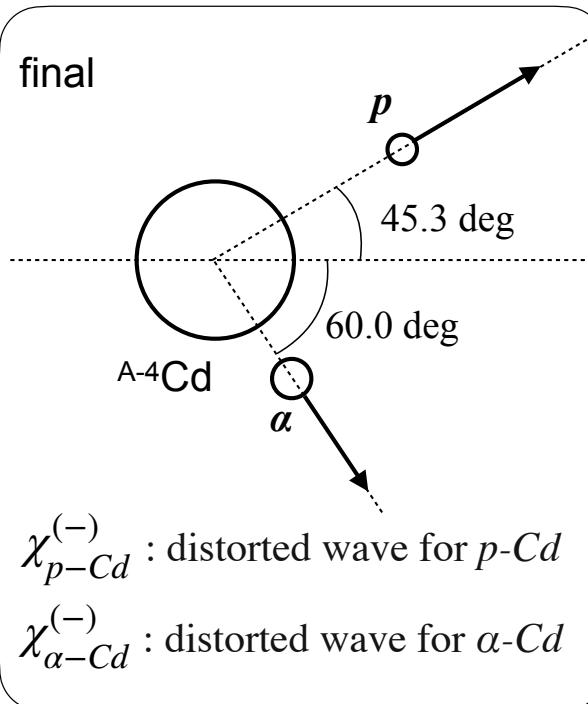
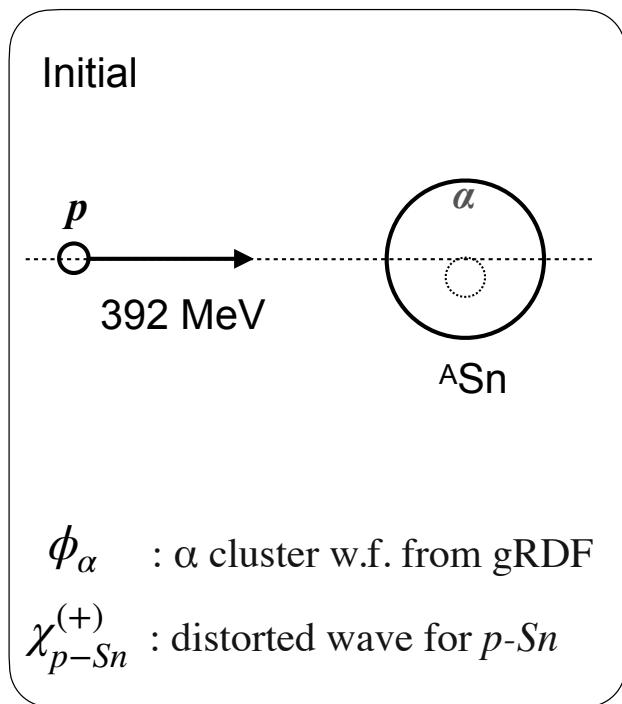
Triple
Differential
Cross section

$$\frac{d^3\sigma}{dE_1 d\Omega_1 d\Omega_2} = \frac{(2\pi)^4}{\hbar v} F_{kin} |T|^2$$

$$T = \left\langle \chi_{\alpha-Cd}^{(-)} \chi_{p-Cd}^{(-)} \left| t_{p-\alpha} \right| \phi_\alpha \chi_{p-Sn}^{(+)} \right\rangle$$

$t_{p-\alpha}$: free $p-\alpha$ scattering matrix

χ : distorted waves



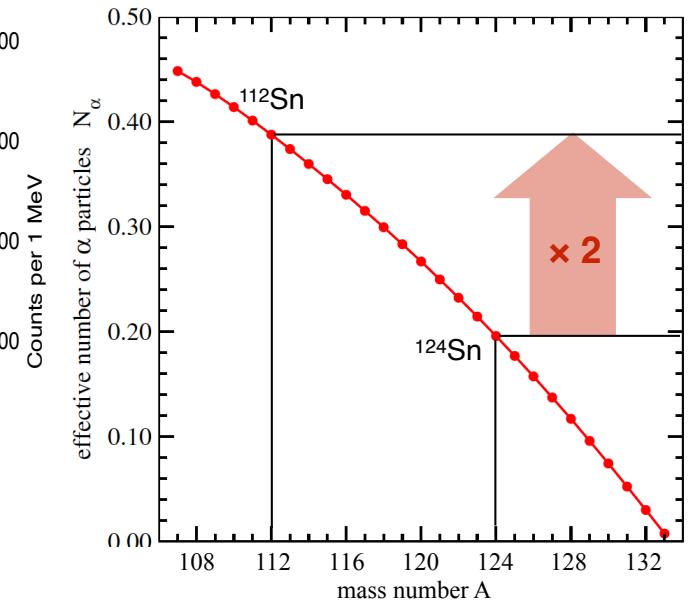
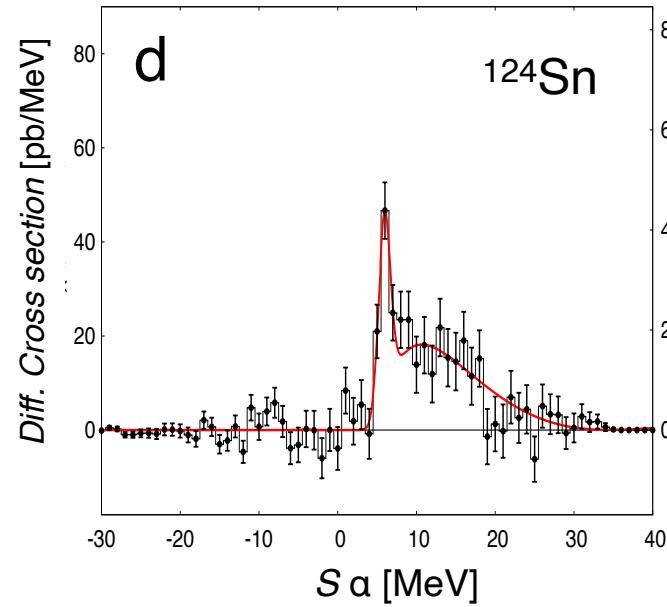
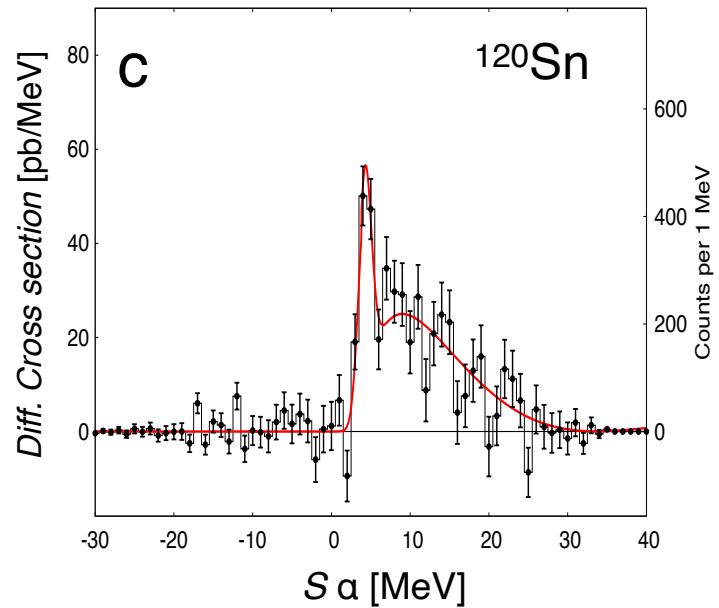
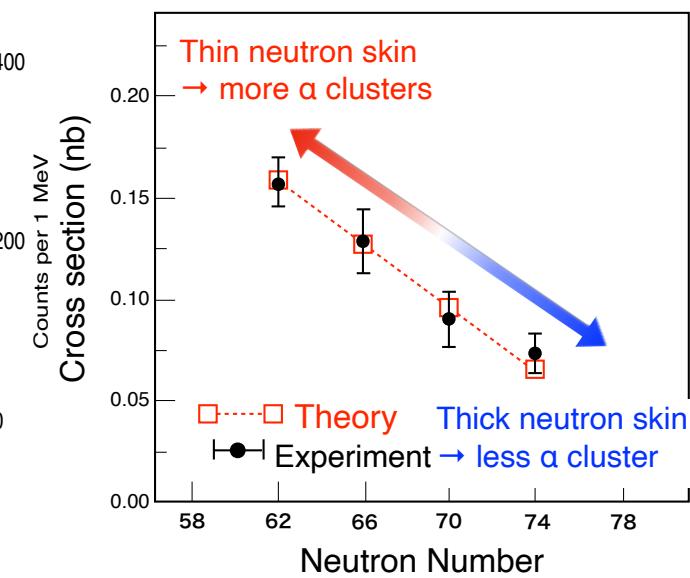
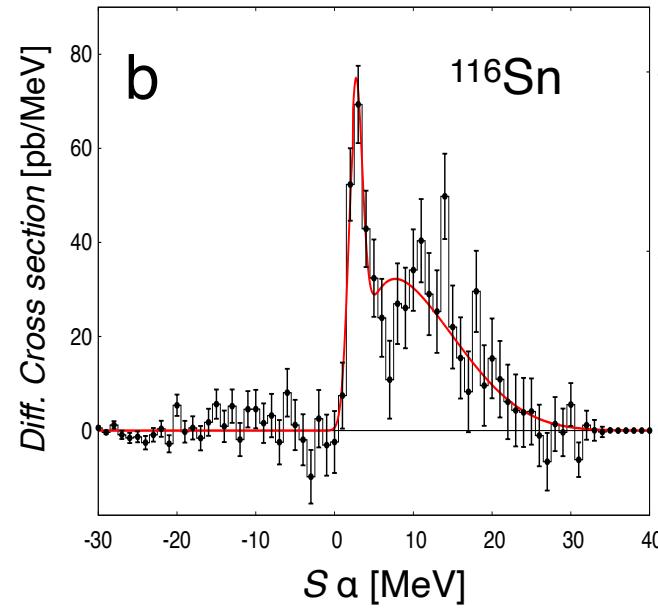
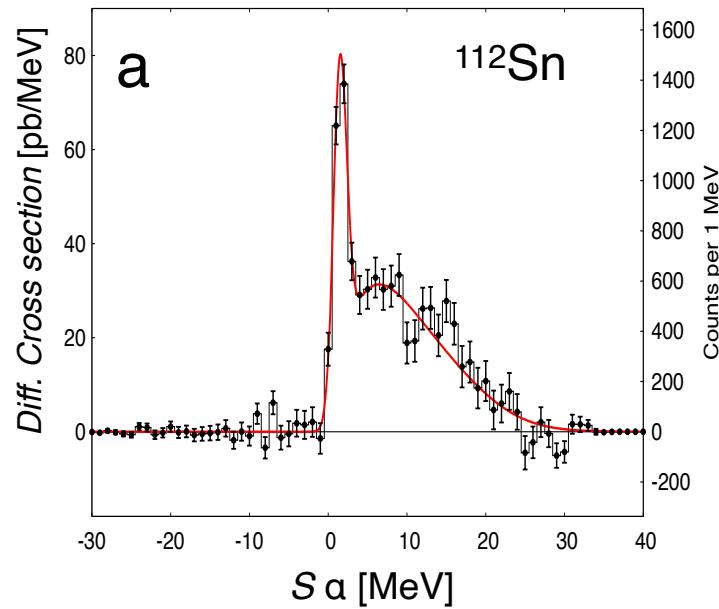
1. Kinematics factor
 2. $p-\alpha$ scattering matrix
K. Yoshida et. al.
Phys. Rev. C **98** 024614 (2018)
 3. momentum of α in nuclei
gRDF theory by S. Typel
Phys. Rev. C **89**, 064321 (2014)
 4. absorption of protons
Optical potential from S. Hama et. al. Phys. Rev. C **41** 2327 (1990)
 5. absorption of alpha
Optical potential from M. Nolte et. al.
Phys. Rev. C **36** 1312 (1987)
- The depth of the imaginary part was tuned to the experimental data. Use the same reduction factor for all isotopes.

Theoretical support by S. Typel

Advice from K. Yoshida and K. Ogata

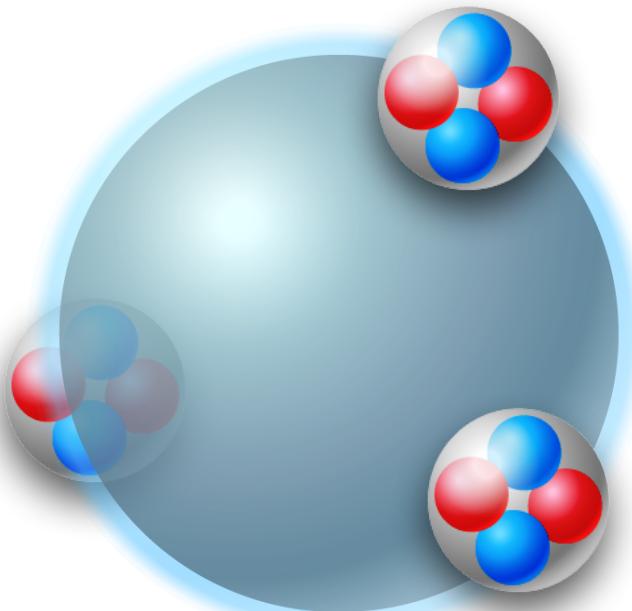
Experimental result and comparison with theory

J. Tanaka, Z.H. Yang, S.Typel et al., Science 371, 260–264 (2021)



Summary of Sn(p,pa) experiment

1. The existence of alpha clusters in the ground state of heavy nuclei (Sn) was clarified by measuring the cross-section of the alpha knockout reaction.
2. The isotope dependence of the reaction cross section is consistent with the theoretical prediction, and what we observed is likely to be alpha clusters localized on the nuclear surface.



J. Tanaka, Z.H. Yang, S.Typel et al.,
Science 371, 260–264 (2021)

The ground state of the tin nucleus is not always such one body which written in the conventional droplet model or single particle model picture, the experimental result indicated that the configurations with the alpha clusters are mixed and co-exist in certain probability by a quantum mechanical superposition. The alpha-knockout reaction selectively extracts and probes such a component.

Collaborators of Sn(p,pa) experiment



TECHNISCHE
UNIVERSITÄT
DARMSTADT



S. Typel

T. Aumann

P.v.Beek

S. Heil

M. Knoesel

H. Scheit

F. Schindler

D. Symochko

V. Wagner

A. Tamii

N. Kobayashi

S. Adachi

A. Inoue

S. Nakamura

K. Ogata

Y. Maeda



Z.H. Yang

J. Zenihiro

T. Uesaka

V. Panin

Y. Kubota

S. Bai

J. Han

S. Huang

Y. Jiang

W. Liu

J. Lou

D. Beaumel

Y. Matsuda



所属は研究当時

K. Miki

P. Schrock

Y. Fujikawa

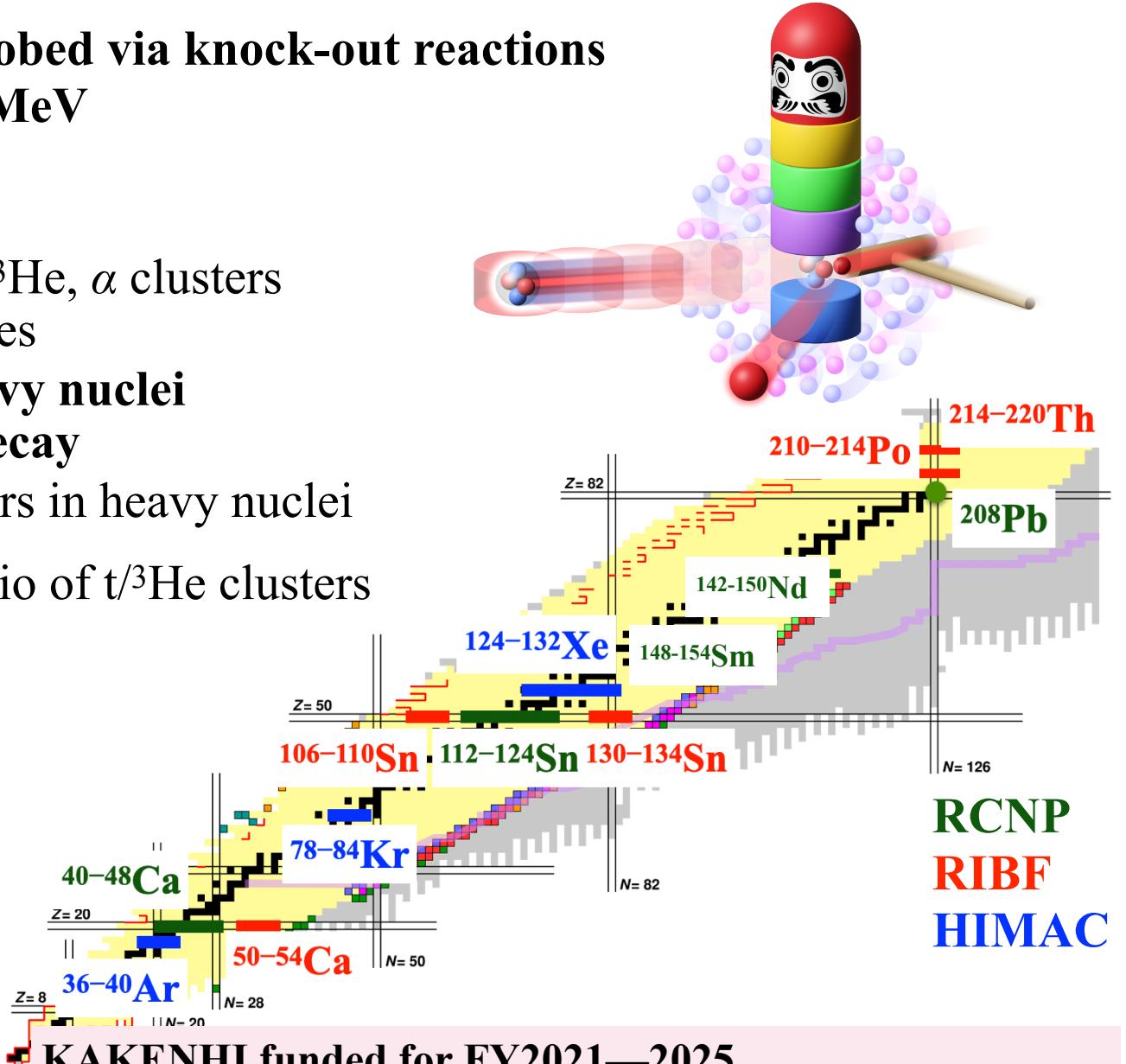
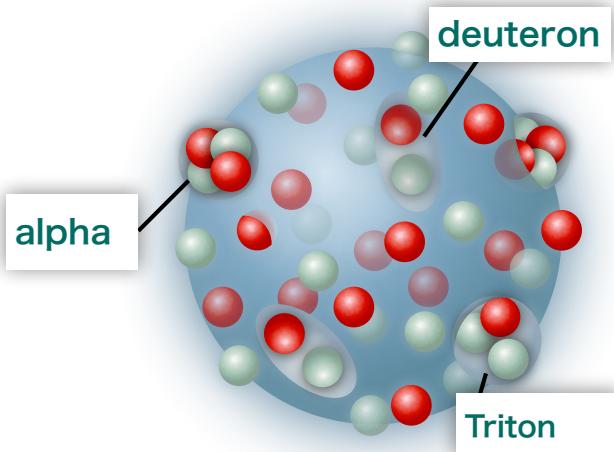
K. Yoshida

ONOKORO project overview

Clustering in heavy nuclei probed via knock-out reactions

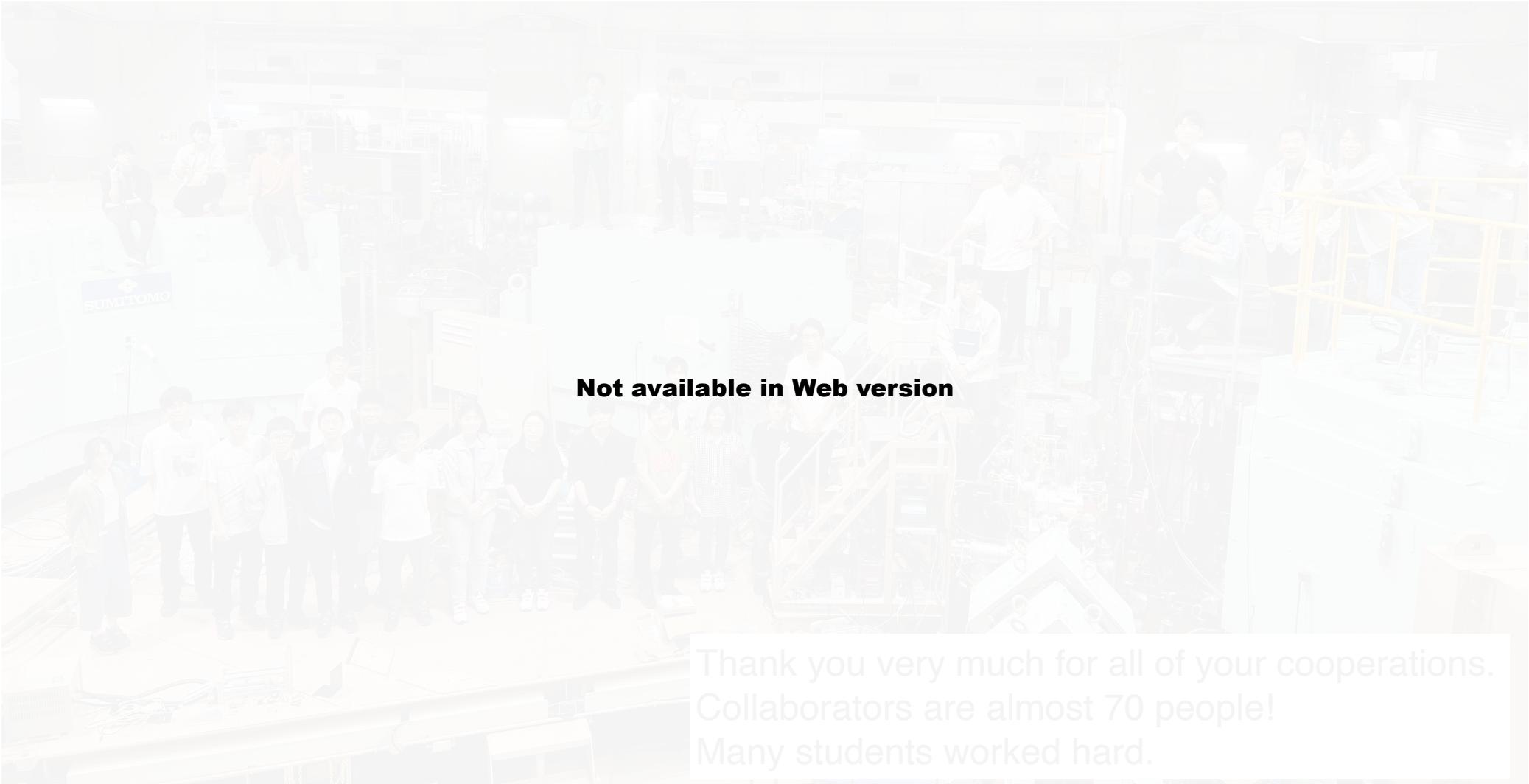
(p, pX) @ E/A = 200—300 MeV
 $X: d, t, {}^3\text{He}, \alpha$

- Relative abundances of $d, t, {}^3\text{He}, \alpha$ clusters and their isotope dependences
- Surface α formation in heavy nuclei → understanding of α -decay
- Discovery of deuteron clusters in heavy nuclei
- First determination of the ratio of $t/{}^3\text{He}$ clusters



Universality of alpha clustering in atomic nuclei

40/42/44/48^{Ca}(p,pX)experiment@RCNP in March-May 2024



Not available in Web version

Thank you very much for all of your cooperations.
Collaborators are almost 70 people!
Many students worked hard.

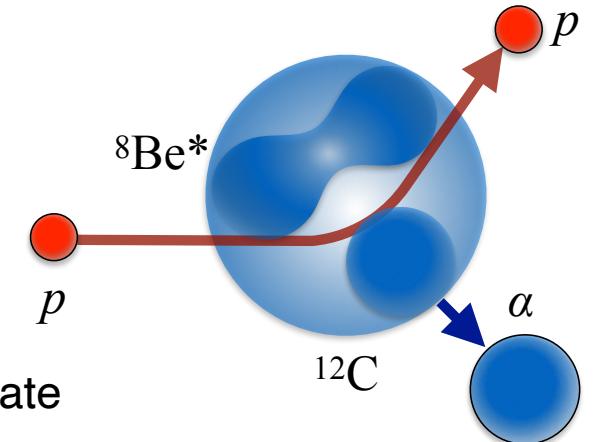
Collaboration : Kyoto Univ, RIKEN, RCNP, Kyushu Univ, Osaka Univ, Konan Univ, Miyazaki Univ, Pekin Univ, CENS IBS, IJCLab Orsay, TU Darmstadt, TU Munich, York Univ, Saitama Univ, iThemba

Today I will focus mainly on alpha knockout reactions

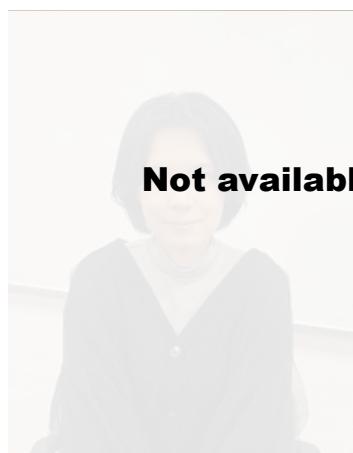
Probing alpha clusters in the ground state of ^{12}C via alpha-knockout reactions

Motivation

- Astrophysical interest in terms of nucleosynthesis
- Hoyle state component in ^{12}C ground state
- *Ab-initio* calculations already exist.
- Residues are $^8\text{Be}(0+)$ unbound ground state and $^8\text{Be}(2+)$ excited state
- Momentum analysis may reveal spacial information of Hoyle state



Analysis is ongoing by



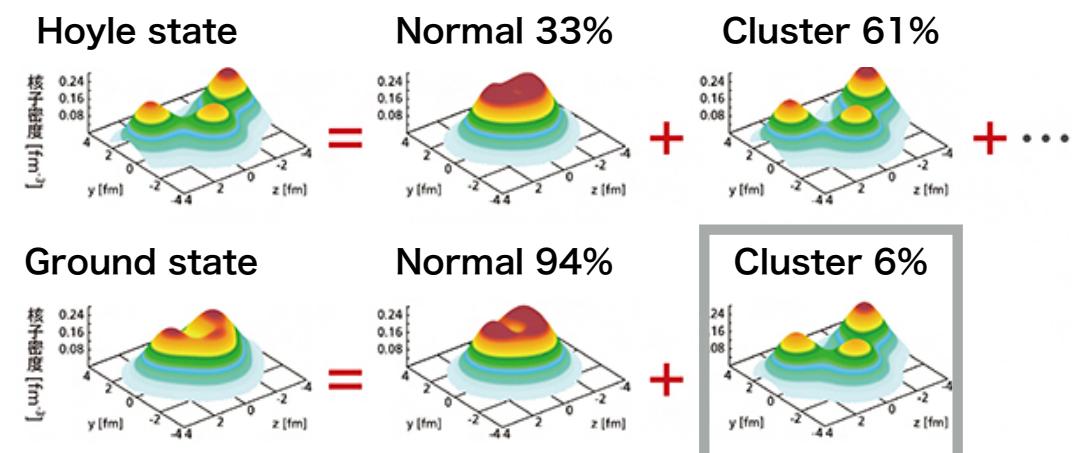
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Fengyi Chen (B4 Osaka Univ.)

Jiawei Bian (D Pekin Univ.)

Ab initio calculation

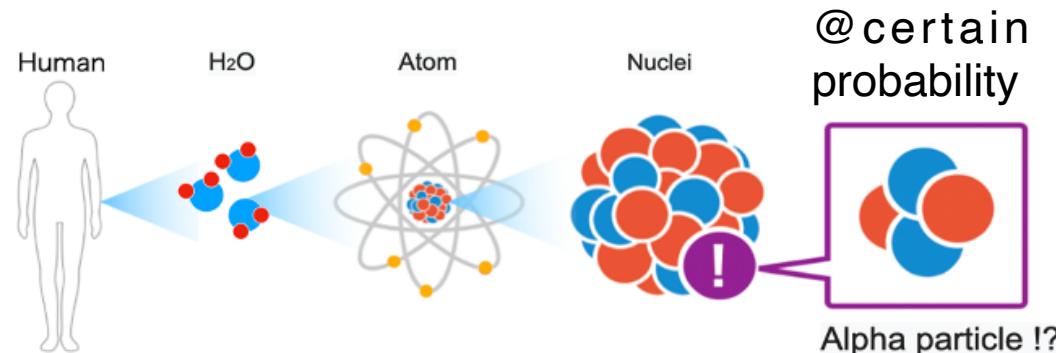


T. Otsuka, T. Abe et.al. Nature Communications [10.1038/s41467-022-29582](https://doi.org/10.1038/s41467-022-29582)

Alpha particles as building block of ^{16}O ground state probed by alpha knockout reaction

Motivation

- " Can alpha particles be the basic building blocks of atomic nuclei? "
- Conventional mean-field picture v.s. alpha cluster formation in double magic nucleus ^{16}O .
- ^{16}O is the most abundant nucleus in the human body.
" How much alpha clusters we have in our body ? "
- Residues are $^{12}\text{C}(0^+)$ g.s., $^{12}\text{C}(2^+)$ ex.s., and $^{12}\text{C}(0^+)$ Hoyle state.
- Momentum analysis may clarify their motion.
- Evolution of stars



Conceptual figure of alpha particles existing as building block.

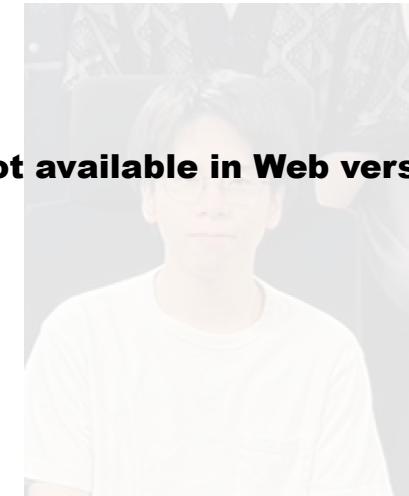


Taichi Miyagawa (M1 RCNP)

Emergence of α -cluster correlations proved by α -knockout reactions in Ca isotopes

Motivation

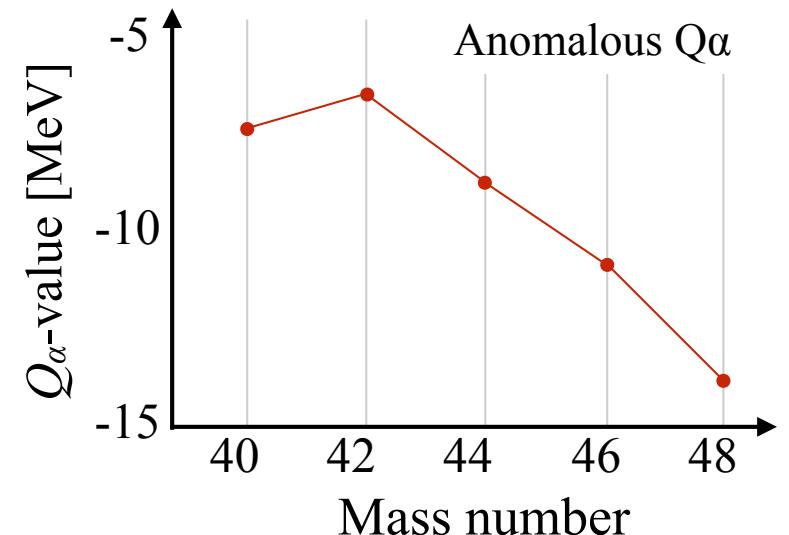
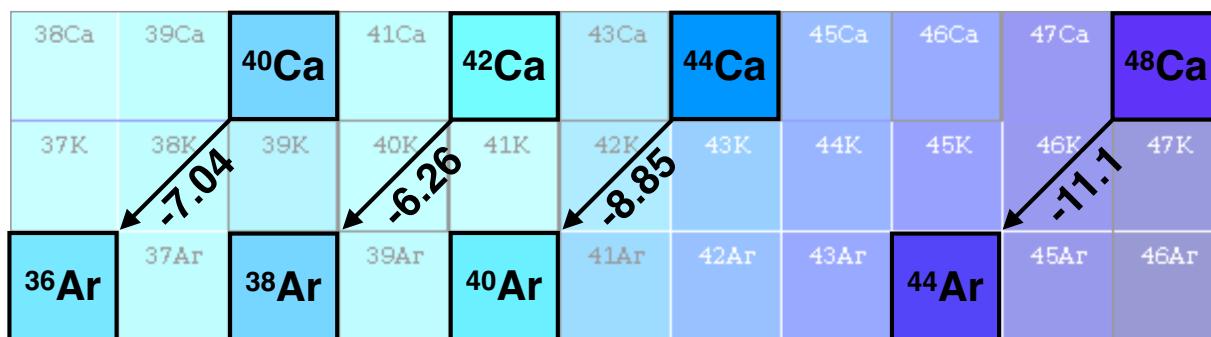
- Emergence of cluster correlations in finite many-body system
- Correlation between the α -formation probability and the Q_α value
- Anomalous isotope dependence of Q_α values in Ca isotopes
- Ca isotopic dependence of (p,pa) reaction cross-sections
- $^{40,42,44,48}\text{Ca}$ targets available
- Importance of double magic nuclei $^{40,48}\text{Ca}$ in nuclear matter study



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Riku Matsumura (D3 Saitama Univ.)

Experimental Q_α -values [MeV]



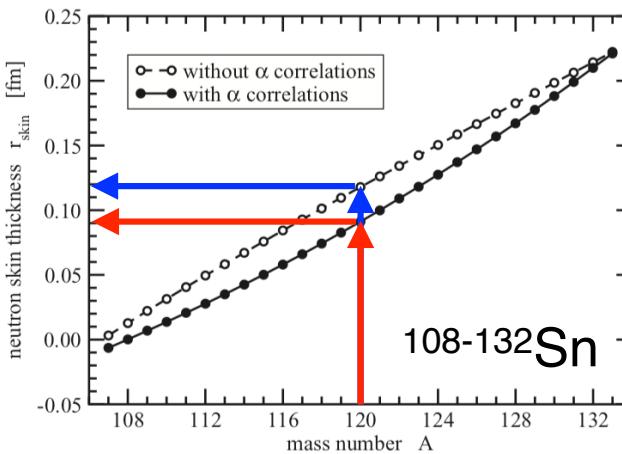
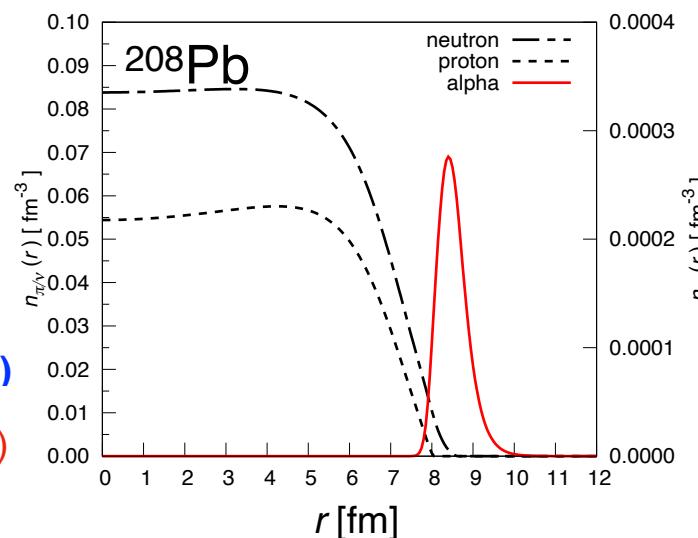
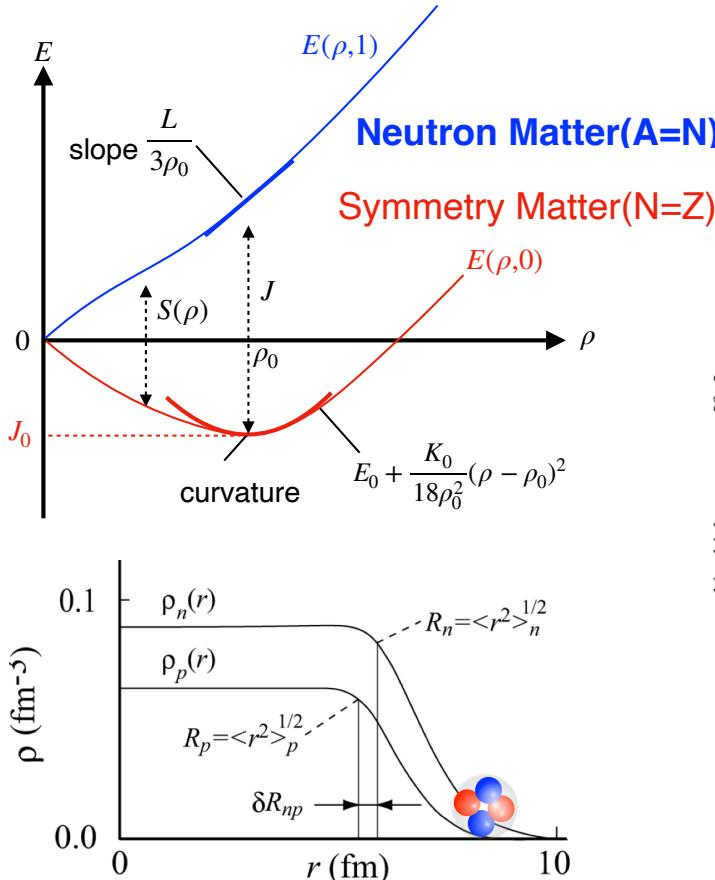
future

“Alpha clustering in Pb isotopes !?”

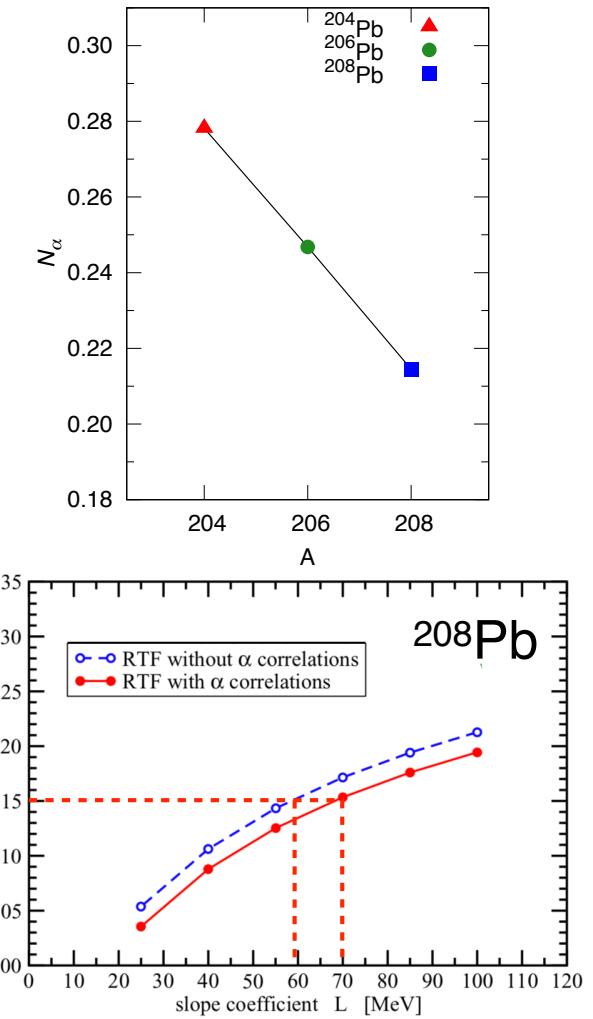
~ Approaching the relation between neutron-skin thickness and neutron-star radius/mass ~

Motivation

- Nuclear EOS
- Alpha cluster in ^{208}Pb
- Relation bw Δr_{np} and L



Sn isotope mass number dependence of Δr_{np}



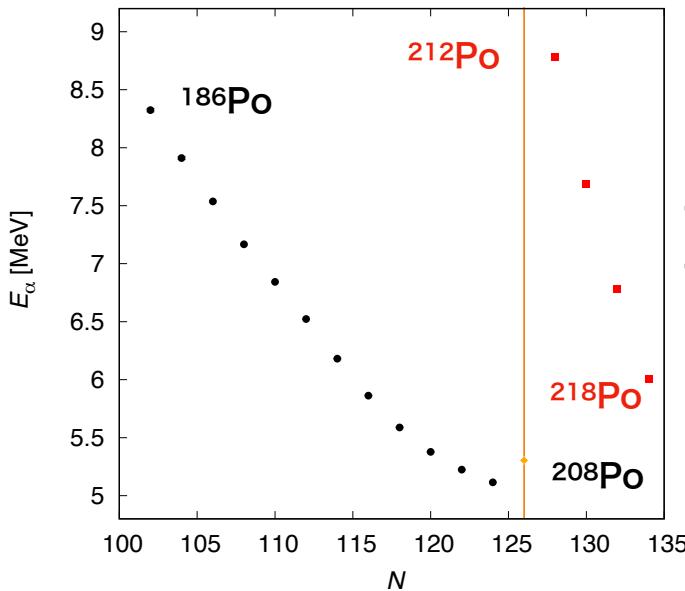
Effect of α cluster correlation on Δr_{np} and L

α -knockout reactions from α -decay nuclei

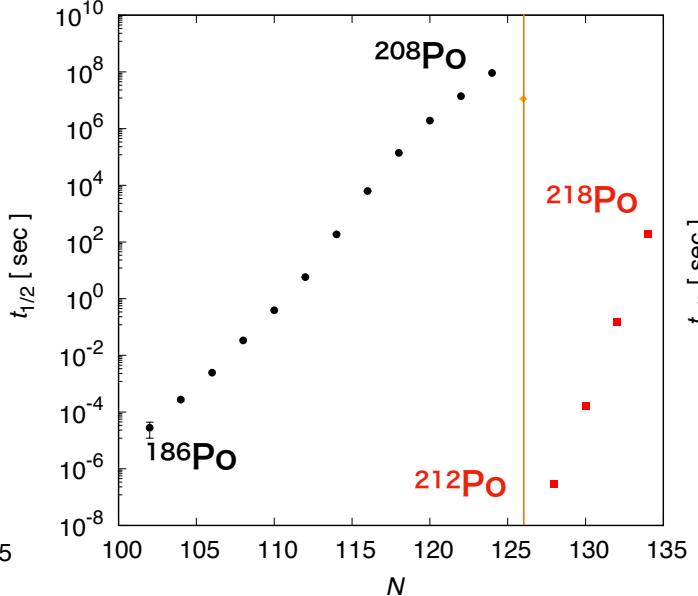
Motivation

- Clarify the relation of preformed α -particle in α -decay and surface α -cluster observed α -knockout
- Full-understanding of α -decay

Decay energy : E_α

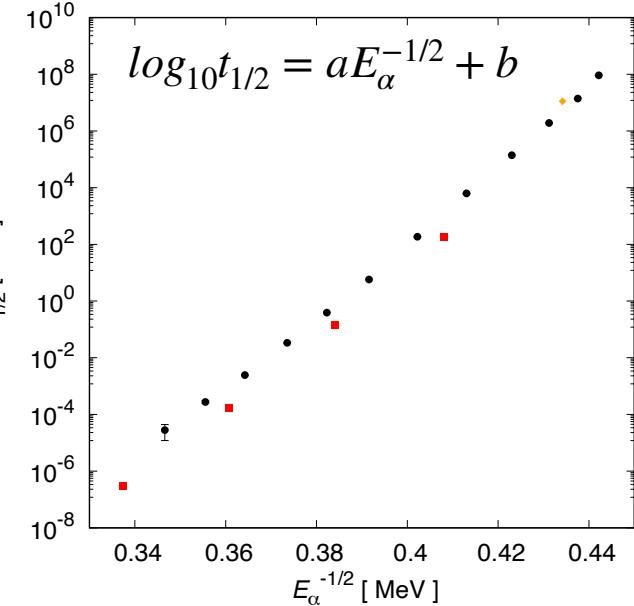


$$\text{Decay width} : \Gamma_\alpha = \hbar\lambda = \frac{\hbar}{\tau} = \frac{\hbar \ln 2}{t_{1/2}}$$



Geiger-Nuttall law :

Relation between E_α v.s. $t_{1/2}$



Characteristic change in neutron magic number 126 with a difference in lifetime of 10^{15} between ^{212}Po with an alpha decay energy of 8.8 MeV and ^{208}Po with 5.0 MeV, influenced by the double magic number of ^{208}Pb .

Quantum tunneling

$P \sim e^{-2\sqrt{\frac{2m}{\hbar^2}} \int_R^b \sqrt{V(r) - E_\alpha} dr}$ account for the 10^{15} difference in life.

Tunneling probability P from decay energy E. $\Gamma_\alpha \sim f_\alpha \nu P$

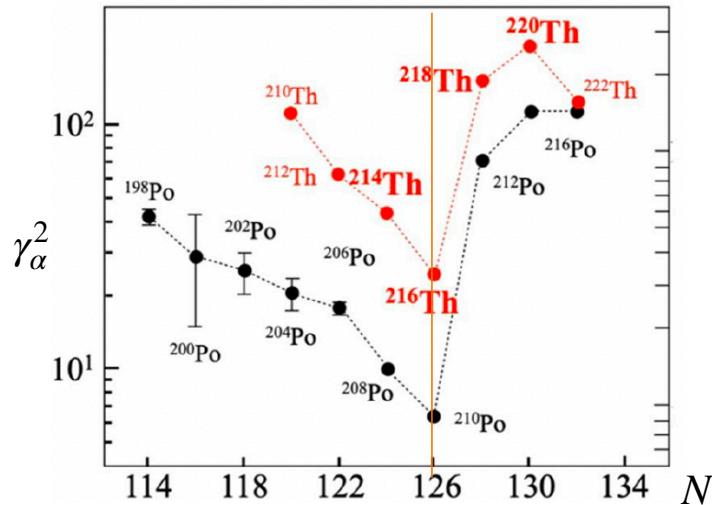
Reduced decay width

$$\gamma_\alpha^2 \equiv \frac{\Gamma_\alpha}{2P} \sim \frac{1}{2} f_\alpha \nu \quad \begin{aligned} f_\alpha &: \alpha\text{-preformation factor} \\ \nu &: \text{frequency} \end{aligned}$$

Reduced decay width

$$\gamma_\alpha^2 \equiv \frac{\Gamma_\alpha}{2P} \sim \frac{1}{2} f_\alpha \nu \quad f_\alpha : \text{α-preformation factor}$$

$\nu : \text{frequency}$

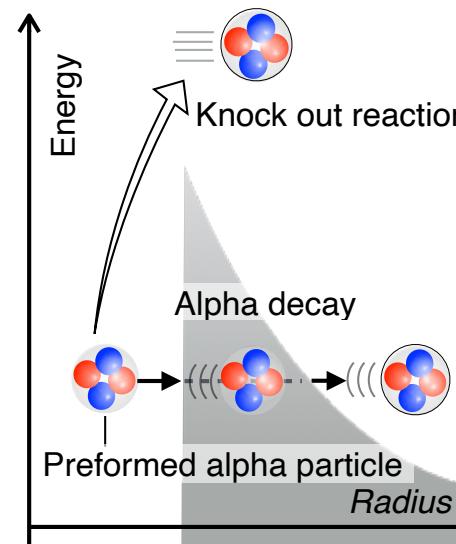


- 10^{15} difference in decay width.
- 10^{14} reduced by P.
- **10 times difference in γ_α^2 remains.**
- Is it preformation factor $f_\alpha \nu$?
- P accurate? **Shape of Coulomb barrier.**

Shell model Calculation

- Absolute value comparison of γ_α^2 (^{212}Po)
- Tonozuka and A. Arima, Nucl. Phys. A 323, 45 (1979) → **1/14** of the experimental value.
- The importance of configurations involving higher orbitals.
- Still not fully reproduced, with discrepancies remaining within **an order of magnitude**. → 90% not known!

Proving preformed α particle before decay



Contrast of knockout reaction and alpha decay

- α-knockout reaction
- Higher energy than barrier
- **Independent of penetrability**
- good measure of α-formation
- $\sigma(^{212}\text{Po}(p,p\alpha))/\sigma(^{210}\text{Po}(p,p\alpha))$

Effect of reaction mechanism

K. Yoshida, J. Tanaka
PRC 106 (1), 014621

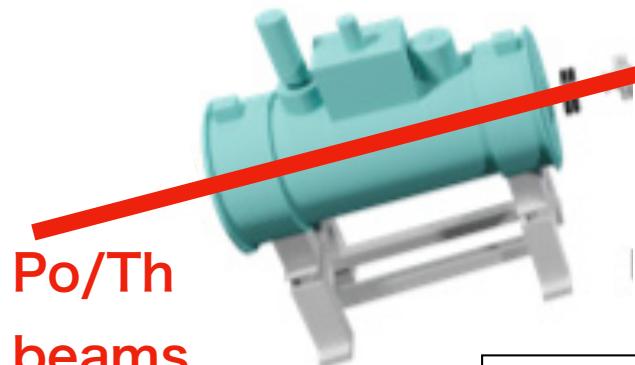
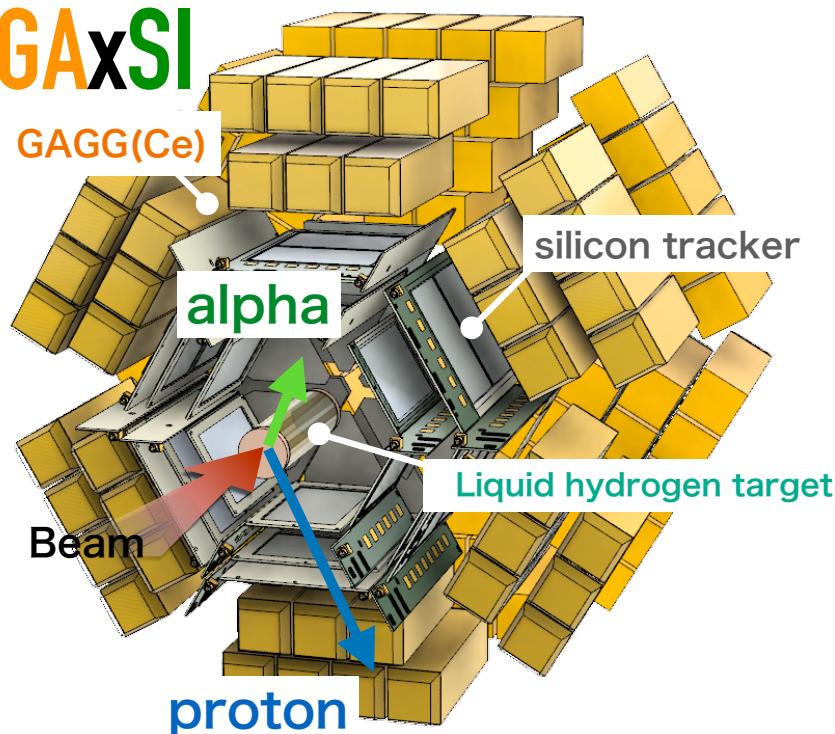
Preparing wave functions reproduce γ_2 values for ^{212}Po and ^{210}Po
Calculate α-knockout reaction cross sections

$$\frac{\sigma_{(p,p\alpha)}^2(^{212}\text{Po})}{\sigma_{(p,p\alpha)}^2(^{210}\text{Po})} \sim \frac{|RF(R)|^2(^{212}\text{Po})}{|RF(R)|^2(^{210}\text{Po})} \sim \frac{\gamma_\alpha^2(^{212}\text{Po})}{\gamma_\alpha^2(^{210}\text{Po})} \sim 10$$

Reaction is peripheral

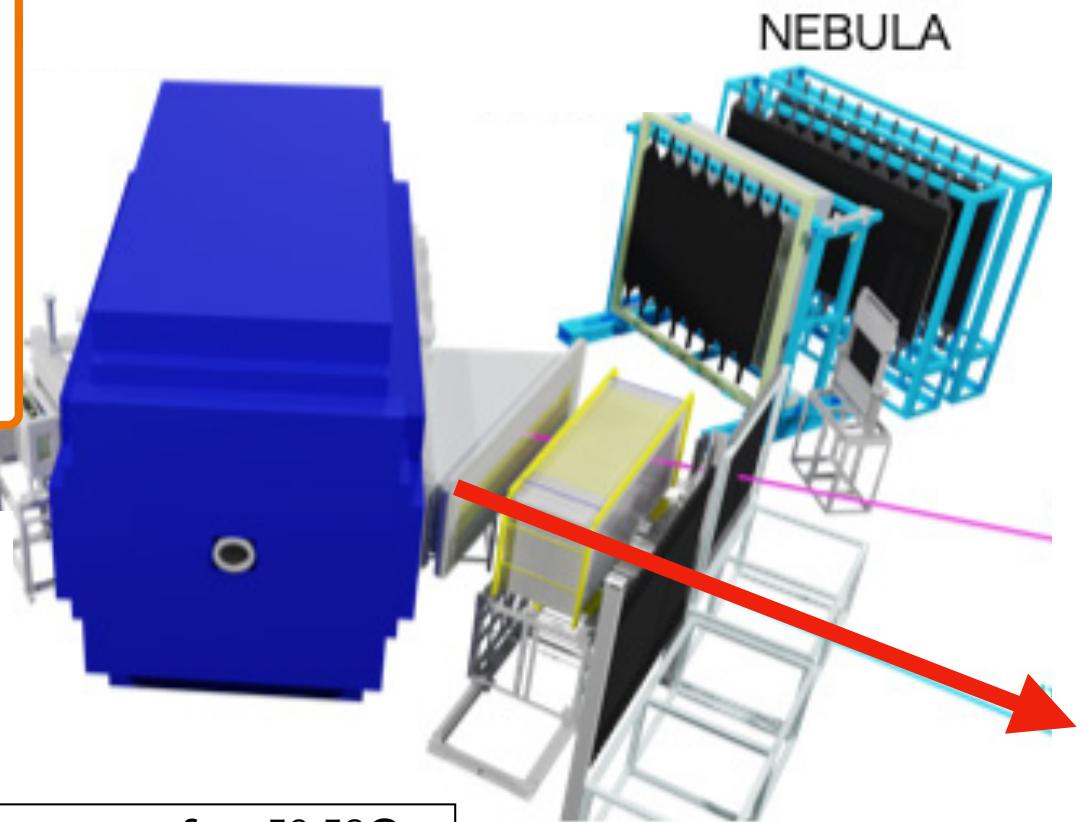
→ σ is almost proportional to γ_2 ($|RF|^2$ in R-matrix theory).

TOGAXSI



J. Tanaka et. al, "Designing TOGAXSI"
NIMB 542, 4-6 (2023)

K. Higuchi and J. Tanaka et. al, "Silicon tracker for cluster-knockout reactions at intermediate energies"
NIMB 542, 84-86 (2023)

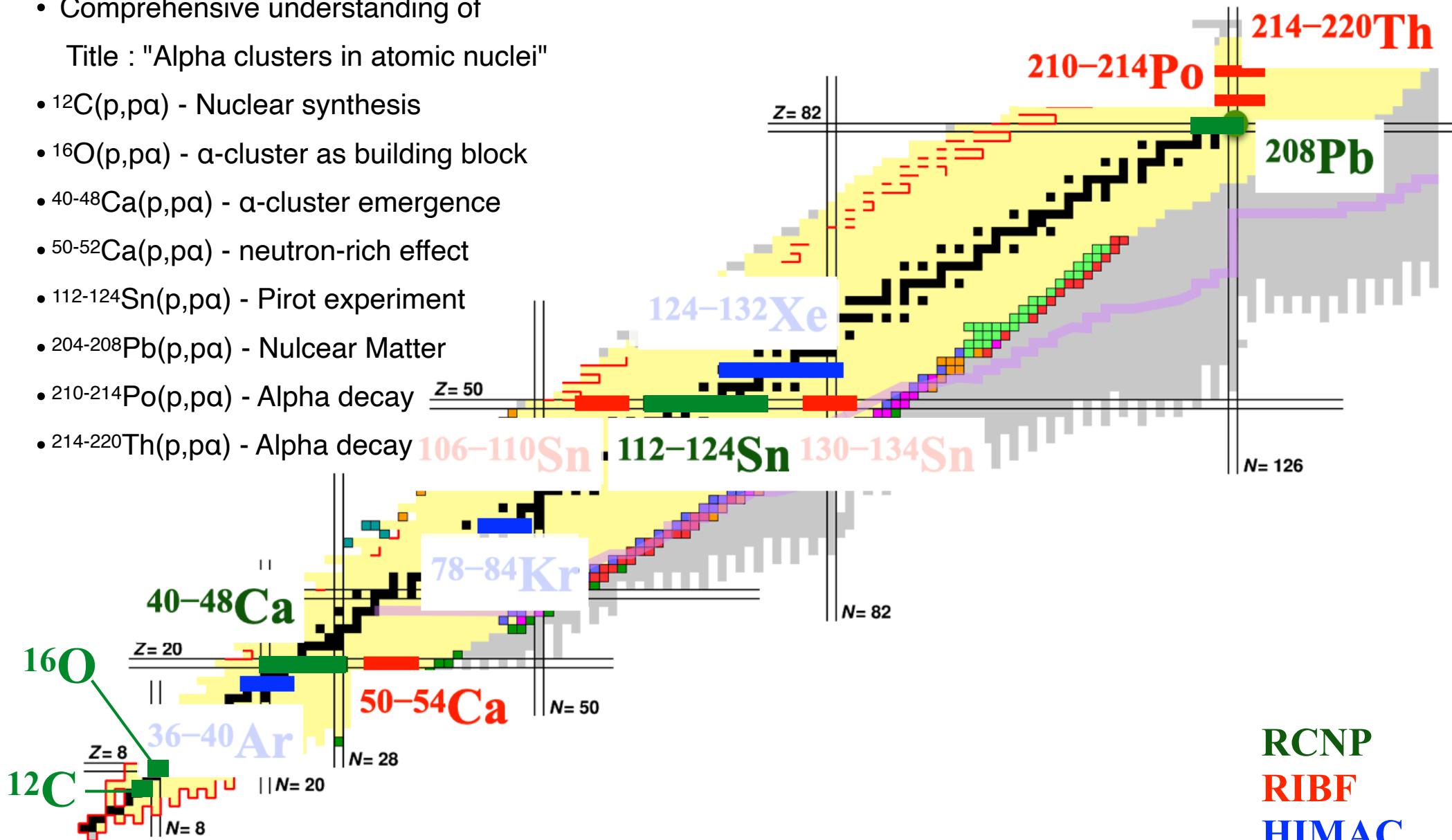


First campaign in next year for $^{50-52}\text{Ca}$

Pb/Ra residues

Summary until near future

- Comprehensive understanding of
Title : "Alpha clusters in atomic nuclei"
- $^{12}\text{C}(\text{p},\text{pa})$ - Nuclear synthesis
- $^{16}\text{O}(\text{p},\text{pa})$ - α -cluster as building block
- $^{40-48}\text{Ca}(\text{p},\text{pa})$ - α -cluster emergence
- $^{50-52}\text{Ca}(\text{p},\text{pa})$ - neutron-rich effect
- $^{112-124}\text{Sn}(\text{p},\text{pa})$ - Pirot experiment
- $^{204-208}\text{Pb}(\text{p},\text{pa})$ - Nuclear Matter
- $^{210-214}\text{Po}(\text{p},\text{pa})$ - Alpha decay
- $^{214-220}\text{Th}(\text{p},\text{pa})$ - Alpha decay

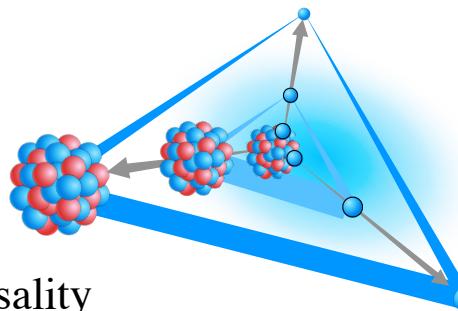


More future
Of course, I continue alpha knock out reactions, but here I introduce others

Nuclear Giants

Motivation

- Explore the largest nuclear system (exclude gravity-bound neutron stars)
- Scale-conversion symmetry and its universality
- Unified understanding of neutron halo and Efimov states
- Large scattering length and large neutron-capture cross sections

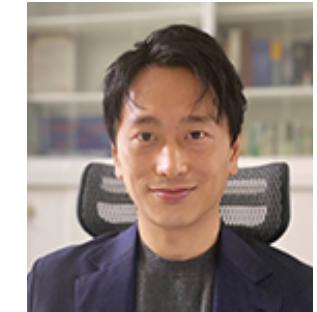


RCNP Core-Net

Exploring Nuclear Giants: Structure and Reactions of Extremely Large Nuclei



S. Endo (UEC)

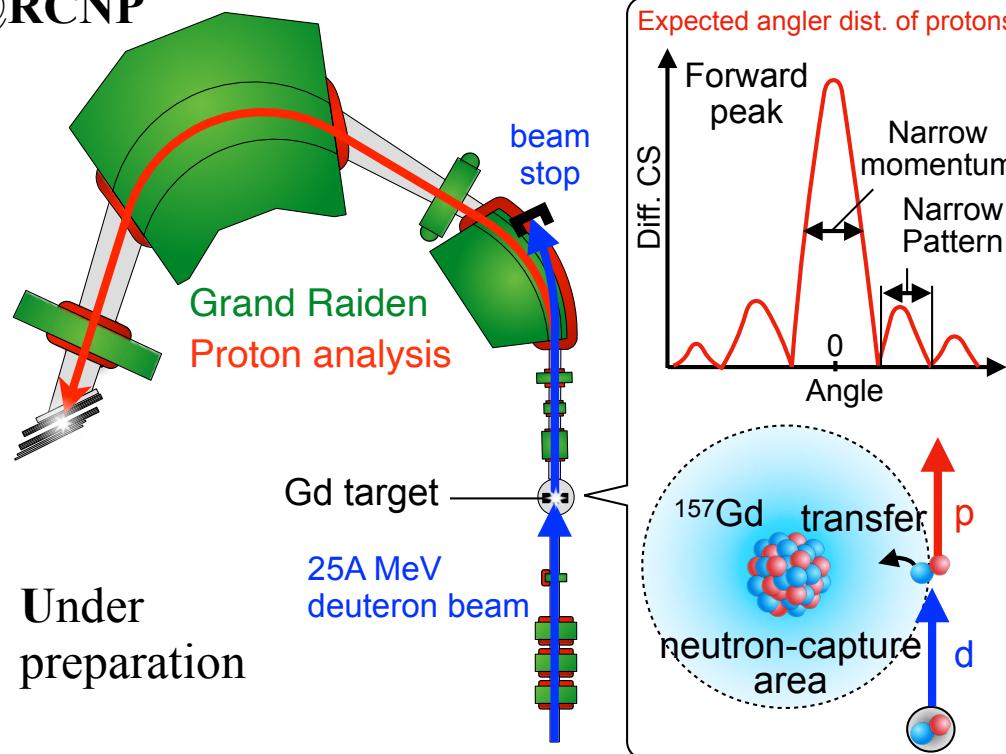


T. Fukui (Kyushu)

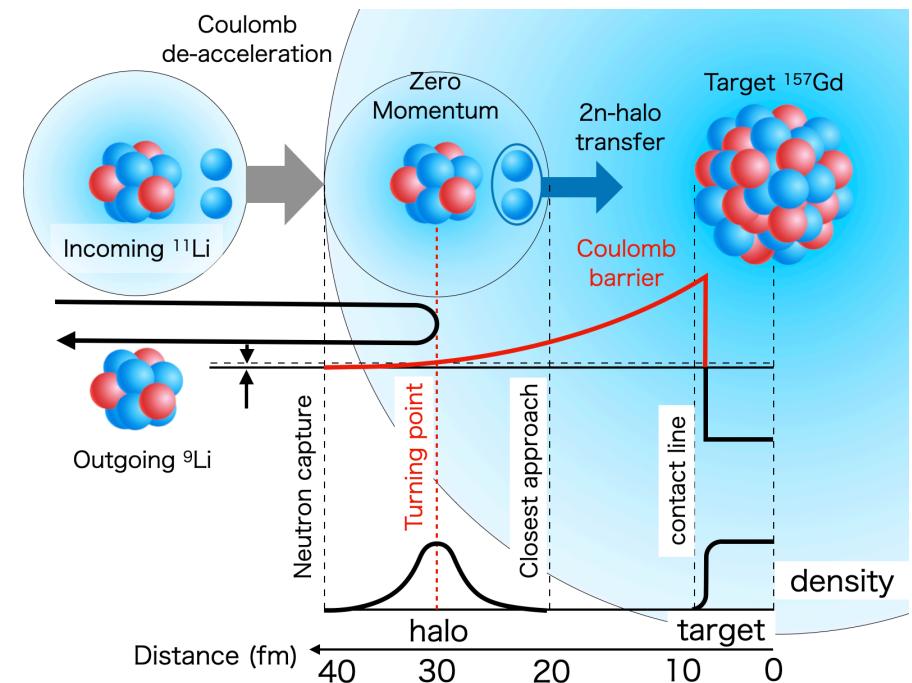
S. Endo, J. Tanaka, Efimov state in excited nuclear halos
arXiv preprint arXiv:2309.04131

Tamii-lab honer seminar for undergraduate students

@RCNP



@ISOL facility



Dreaming more future

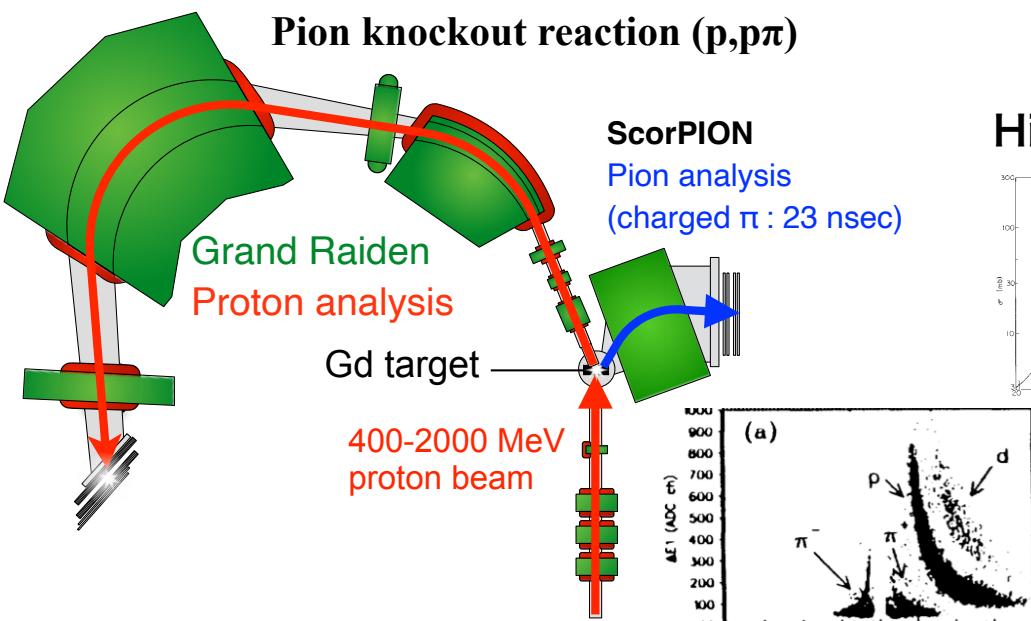
As a RCNP staff, I should, or I am happy to think of RCNP-experiment future!

PIONeer KEIKAKU ~ Dream ~

Motivation

- Importance of Pions in atomic nuclei
"Why nuclear matter saturate?" - tensor force (Bethe)
- "Why atomic nucleus no-collapse?" - repulsive core
- "Why stable? / unstable?" - binding energy
- "What is three nucleon forces" - $\Delta(n-\pi)$ resonance
- "Why alpha cluster formed?" - binding energy of alpha
- Last few decades, understanding of tensor force progress
- Still there are challenges in theory
- Delving into **essence of atomic nuclei** at RCNP.
- Generate many groundbreaking studies.

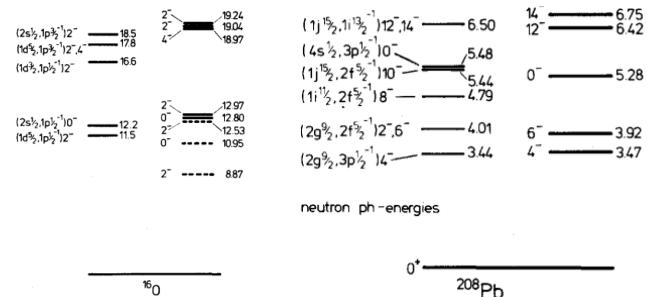
All the complexity = The nature of the nucleus comes from pions!



From the bottom of my heart, I hope many of you could provide the suggestion for the future !

1st-stage proton-400MeV

- Pion production threshold 280 MeV
- unnatural parity, pionic mode spectroscopy
- isotope dependence
- High resolution** missing mass spectroscopy

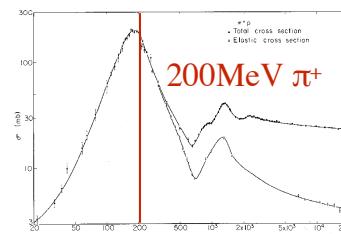


Pion cloud knockout from proton

- p-wave scattering

(Discussion@iThemS : T. Hatsuta, A. Hosaka, K. Yoshida, and J.T.)

Higher energy proton-2 GeV



- $p-\pi^+$ scattering
- 2 GeV proton
- high momentum

Discussing with



H. Toki (RCNP)
Thank you so much!

Let's knockout π !

- Grow-up project
- Yield estimation
- Write white paper

Thank you !!

I can't wait for the future !

