

Delta–isobar (Δ) resonances and isospin-spin ($\tau\sigma$) couplings for weak ($\nu, \beta, \beta\beta$), electromagnetic (γ) and nuclear interactions.

Hiro Ejiri, RCNP, Osaka Univ.

- Nuclear matrix elements (NMEs) for neutrinoless $\beta\beta$ decays (DBD) and inverse β decays are crucial for studying ν properties beyond the standard model and astro- ν nuclear interactions. The NMEs consist mainly of the isospin spin ($\tau\sigma$) component. The $\tau\sigma$ strength (square of the $\tau\sigma$ NME) for DBD nuclei is studied experimentally by charge exchange reactions (CERs). The summed Gamow-Teller (GT $\tau\sigma$) and spin-dipole (SD $\tau\sigma Y_1$) strengths measured by CERs are shown to be reduced by half with respect to the nucleon-based sum rule limits. The $\tau\sigma$ NMEs are shown to be quenched due to the non-nucleonic Δ -isobar giant resonance effect on the basis of the measured summed strength and the QRPA analysis with the NN and $N\Delta$ $\tau\sigma$ interactions. The quenching effect is incorporated by using an effective $\tau\sigma$ coupling of $g_{\tau\sigma}^{\Delta}/g_{\tau\sigma} \sim 0.7$ with $g_{\tau\sigma}$ being the $\tau\sigma$ coupling for a free nucleon. The quenching coefficient is applied for the $\tau\sigma$ components of weak, electromagnetic and nuclear interaction NMEs. Impact of the Δ giant resonance effect on ν studies in nuclei is discussed.

Refs. H. Ejiri, Phys. Rev. C 112 045505 2025.

- H. Ejiri, T. Fukuyama and T. Sato Phys. Rev. C 111 065501 2025

A brief note on Prof. Hiro Ejiri since 1936-2-21.

1. Born in the same 1930's as the nucleus with n & p by Heisenberg et al.
2. Start nuclear exp. of β rays in 1958 at Univ. Tokyo being inspired by the coherent nuclear excitations by Bohr Mottelson in 1953-54, the Delta resonance, the discovery of neutrinos by Reines and Cowan in 1956, and
 - the P-violation of the weak force in 1956 by Lee Yang Wu
3. The first paper in 1960 on nuclear resonances.
4. PhD in 1963 at Univ. Tokyo by nuclear coherent excitations of sd-nuclei.
5. Works: Univ. Tokyo INS, Univ. Washington NPL, Univ. Copenhagen NBI, Univ. California LBL, Osaka-Univ. Phys. & RCNP (Director), Spring -8, Univ. Washington CENPA, ICU Tokyo, IIAS Kyoto, CTU Prague, others.
6. Subjects: Nuclear and hyper nuclear structures and reactions, weak(ν), EM and nuclear interactions and β - γ spectroscopy for NEWS, and others.
7. DBD with ELEGANT since 1982 and CERs for ν response since 1993.
8. Supervisor for ~40 PhD's in 4 countries.
9. Today's talk in NEWS is mainly on the recent works of Δ giant resonances and $\tau\sigma$ couplings for Neutrinos, Weak and Electromagnetic interactions and Symmetries..

**Delta–isobar (Δ) resonance and isospin-spin ($\tau\sigma$)
coupling for weak ($\nu, \beta, \beta\beta$),
electromagnetic (γ) and nuclear interactions.**



Hiro Ejiri RCNP Osaka-U 2026-2-26

Thanks Prof. T. Shima and Prof. A. Tamii

The present subject is concerns with **Nuclear Interaction** involved in ν and Weak NMEs

In case of $0\nu\beta\beta$ $A = B + \beta + \beta$

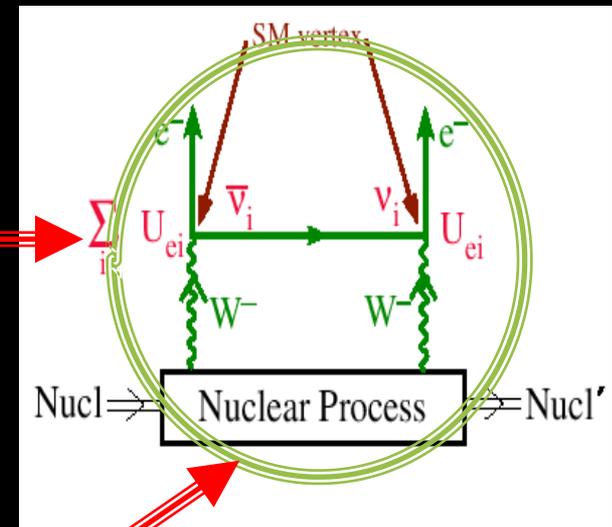
Lepton number $\Delta L=2$ beyond SM.

Particle astro physics
Majorana ν , m_ν CP, RHC

$$T^{0\nu} = G^{0\nu} [M^{0\nu} m_\nu]^2$$

EXP

NME : Nucl. phys.
 g_Δ Delta (Δ) GR,
 $\tau \sigma$ correlation



$\beta\beta$ Review Doi Kotani Takasugi PTP 1985,
ROPP 2012 J. Vergados, H. Ejiri, F. Simkovic, .

Subjects to be discussed

- 1. Spin isospin NMEs and NN and $N\Delta$ GRs (Giant Resonances.)
- 2. GT and SD summed strengths and $g_{\tau\sigma}^{\text{eff}}(\Delta)$
- 3. **NEWS** (Neutrino, Electromagnetic, Weak and Symmetries) with **$N\Delta$ GR**
- 4. Concluding remarks

• For question, indicate the page number

Δ -isobar resonance effects studied by $\tau\sigma$ summed strengths and nuclear matrix elements for β and $\beta\beta$ decays

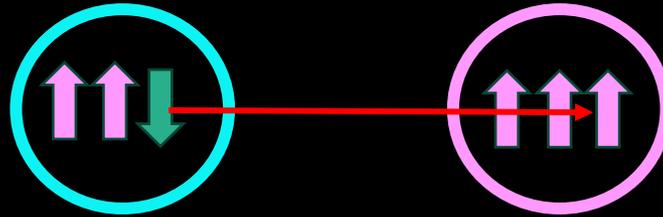
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Nuclear matrix elements (NMEs) for neutrinoless $\beta\beta$ decays and inverse- β decays are crucial for studying ν properties beyond the standard model and astro- ν nuclear interactions. The NMEs consist mainly of the isospin (τ) spin (σ) component, and the $\tau\sigma$ strength (square of the $\tau\sigma$ NME) is studied experimentally by charge exchange reactions (CERs). The summed Gamow-Teller ($\tau\sigma$) and spin dipole ($\tau\sigma Y_1$) strengths measured by CERs are shown to be reduced half with respect to the nucleon-based sum-rule limits. The $\tau\sigma$ NMEs are shown to be quenched due to the non-nucleonic Δ -isobar resonance effect on the basis of the measured strengths and the quasiparticle random-phase approximation analysis with effective nucleon-nucleon and $N\Delta$ $\tau\sigma$ interactions. The quenching effect is incorporated by using an effective $\tau\sigma$ coupling of $g_{\tau\sigma}^\Delta/g_{\tau\sigma} \approx 0.7$ with $g_{\tau\sigma}$ being the coupling for a free nucleon. The quenching effect is applied to the $\tau\sigma$ components of the weak, electromagnetic and nuclear interaction NMEs. Impact of the Δ -resonance effect on ν studies in nuclei is discussed.

1. Nuclear Physics with nucleons /baryons/ Δ



Nucleon $\tau \sigma$ flip Δ

Quark uud udd $\tau=\sigma=1/2$ uuu, uud, udd, ddd $\tau=\sigma=3/2$

1. Nucleus = A baryon interacting system : $A=10-200$ (baryon number A) and Z (charge Z) and $S=0$ strangeness.
with strong τ σ r dependent nuclear (meson) field $V_N \sim 30 \text{ MeV}$

Photo-disintegration of a nucleus yields A baryons and many mesons and photons, but not Z protons , N neutrons.

A-interacting nucleon system is Ok in some cases, but **not in many others like weak, EM and nuclear transitions.**

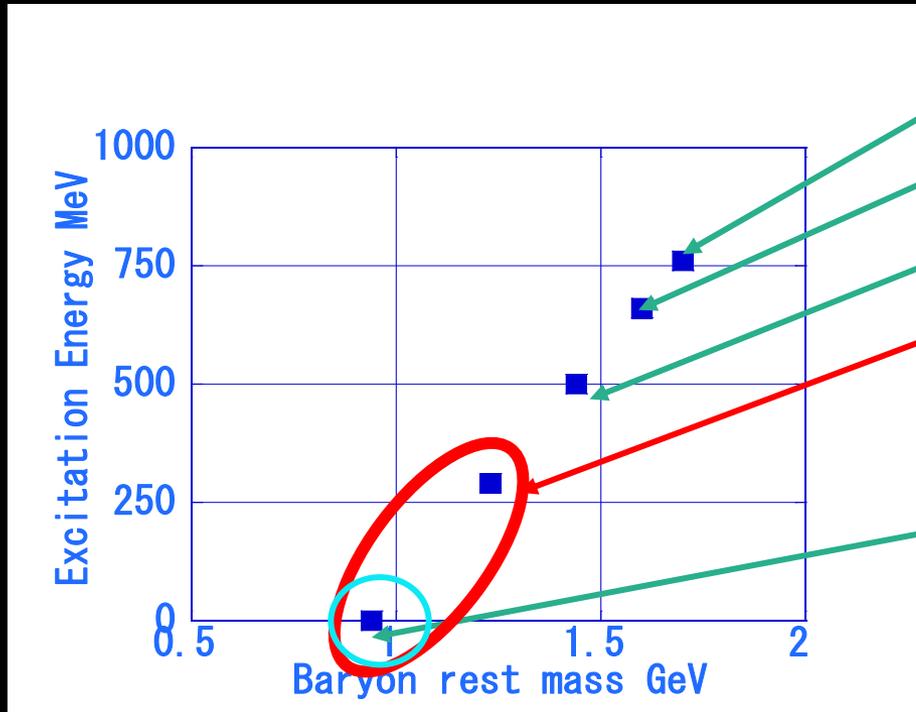
2. The present talk is on nuclear matrix element NMEs for **low-E = a few MeV** : $\beta-\gamma$, DBD- ν , SN- ν , nuclear reaction \ll non-nucleon baryon mass excess $E \sim 0.3-0.5 \text{ GeV}$.

Nucleon model with nucleons and nucleon interactions ????? **No**
Non-nucleonic baryon effects $V/E_\Delta \sim 0.01$ negligible ??? **No**

Baryons in low-energy (1-01 MeV) Nuclear Physics

Nucleons n, p (constituent udd, uud) with $\sigma=1/2$ $\tau=1/2$ 0.94 GeV

Delta Δ^{++} Δ^+ , Δ^0 , Δ^- , with uuu,udu,udd,ddd $\sigma=3/2$, $\tau=3/2$



ΣK (uds s-bar u) Hyperon K
 Λk (uds s-bar u) Hyperon λ
 N^*1440 ud, one radial excited d
 Δ^{++} Δ^+ , Δ^0 , Δ^- $\tau\sigma$ quark
 excitation $N\pi$ **Present**

N (n,p) ud quark ground state
 & low-E nuclear physics with
 n/p in a 30 MeV well.

Low-E state (single QP (quasi-particle state) with mixings of

nuclear state b and Δ state as $|i\rangle = |a\rangle + k|b\rangle + k'|\Delta\rangle$

$k=v/E$ (a few MeV), $k'=MeV/0.3$ GeV : Not neg.

Giant resonances in nuclei and core polarization

Ground state $|0\rangle$ in the shell model potential (frozen nucleus $T \sim 0$)

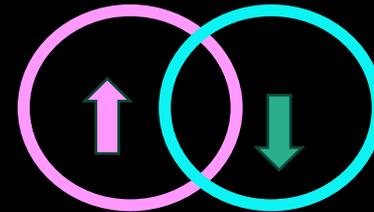
QP excitation to higher (MeV) shell. $|i\rangle = \alpha^+ |0\rangle$ single QP state.

Giant resonance (vibration/photon)

$T|0\rangle$ T-phonon:GR

$V = \chi T \cdot T$ Interaction

$[H, T] \sim ET$ commutator relation



$T = \tau$ Isospin GR IAS = $\sum \tau$ N-Z $n \leftrightarrow p$ vibration

$T = \tau\sigma$ Isospin spin GT-GR

$T = \tau\sigma Y_1$ Isospin spin dipole SD -GR

$T = \tau_3 r Y_1$ EI -GR

$T = \tau\sigma Y_n$ Iso-vector spin multipole GR

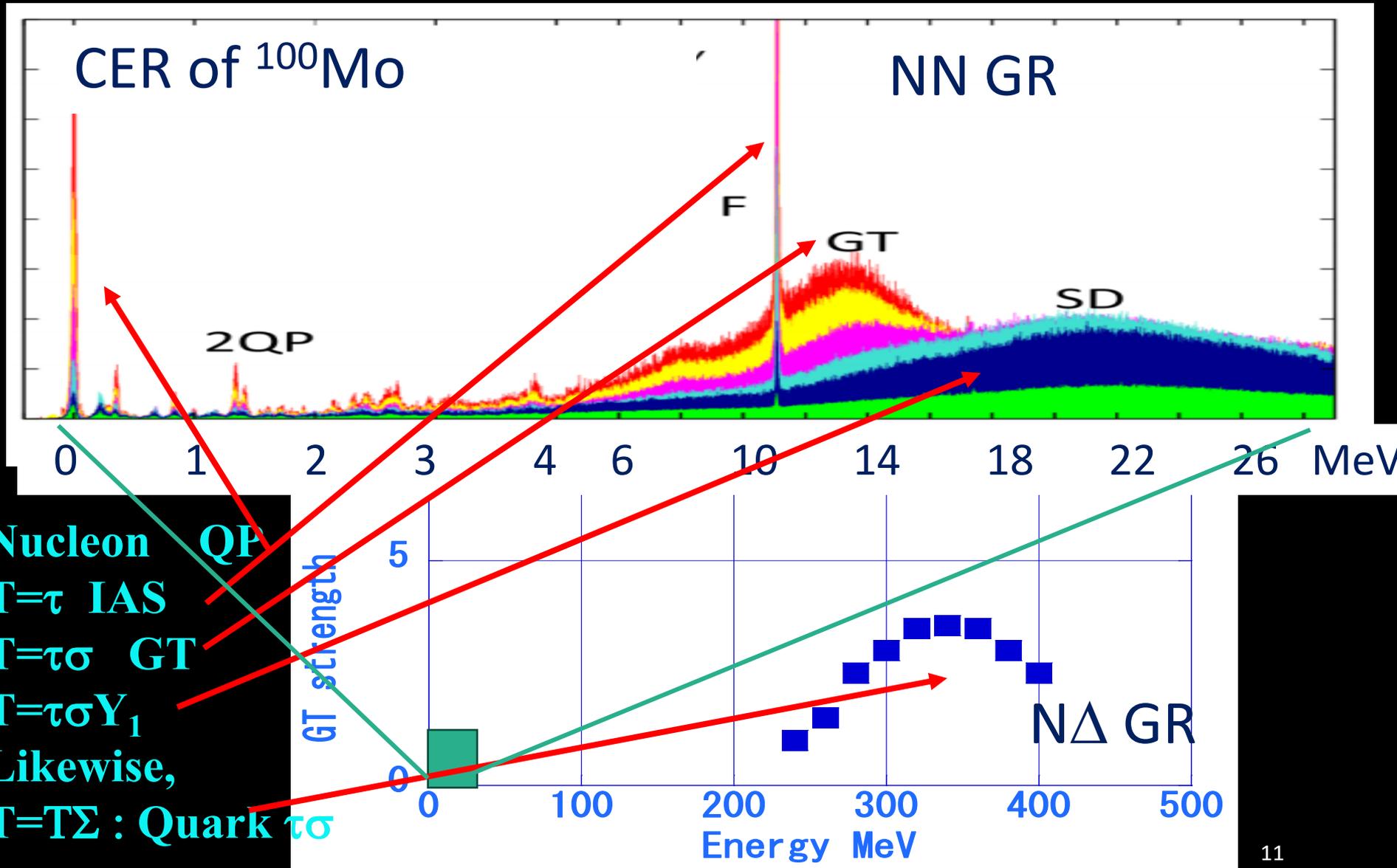
$T = r^2 Y_2$ E2 phonon

Spin Isospin repulsive interactions give rise to GRs at higher E.

EL attractive interaction pushes down the EL phonon states

This talk: extends to the **quark $\tau\sigma \Delta$ GR.**

3. RCNP $\tau\sigma$ CER. GT and SD summed $\sigma\tau$ strengths shift to NN GR and $N\Delta$ GR, leaving only \sim a few % in QP. Region.



GR -NME absorbs most T-mode strength (NME=M)

$$|\text{GR}\rangle = \sum c_k |f_k\rangle$$

Coherent sum of QP states with $k \sim 20 \gg 1$ $c_k \sim 1/k^{1/2}$

$$\text{GR NME } M(\text{GR}) = \sum c_k M_k \sim k^{1/2} M(\text{QP})$$

$$S(\text{GR}) = |M(\text{GR})|^2 \sim k |M(\text{QP})|^2 \sim \text{Total sum}$$

IAS (Fermi GR) : $k=2T_z=N-Z$ sum of n-p QP-F states and absorbs full N-Z Fermi strengths ($M(F)=1$).

GT GR : N-Z GT QP states, and absorbs most GT strengths , N-Z of [$M(\text{GT})=3$]. IFF rule

Non-GR QP NME is reduced much because the strength is taken away by the GR, i.e. destructive interference with GR.

$$|f\rangle \sim |f\rangle - \varepsilon |\text{GR}\rangle \quad M \sim M(\text{QP}) - \varepsilon M(\text{GR}) \quad \text{i.e.}$$

$M \sim M(\text{QP}) / (1 + \chi)$ with $\chi \sim \varepsilon M(\text{GR}) / M(\text{QP})$ susceptibility

$\sim (g^{\text{eff}}/g) M(\text{QP})$ with g^{eff} : effective (renormalized) coupling.

g being g_A in case of the axial-weak NME

$g^{\text{eff}}/g \ll 1$ in case of repulsive V , while $\gg 1$ like e^{eff} if attractive.

Effective couplings g^{eff} for β - γ transitions and NN-giant resonances

1978 PR38 H.Ejiri, J.I. Fujita

H. Ejiri and J.I. Fujita, *Effective coupling constants for beta and gamma transitions in medium and heavy nuclei*

91

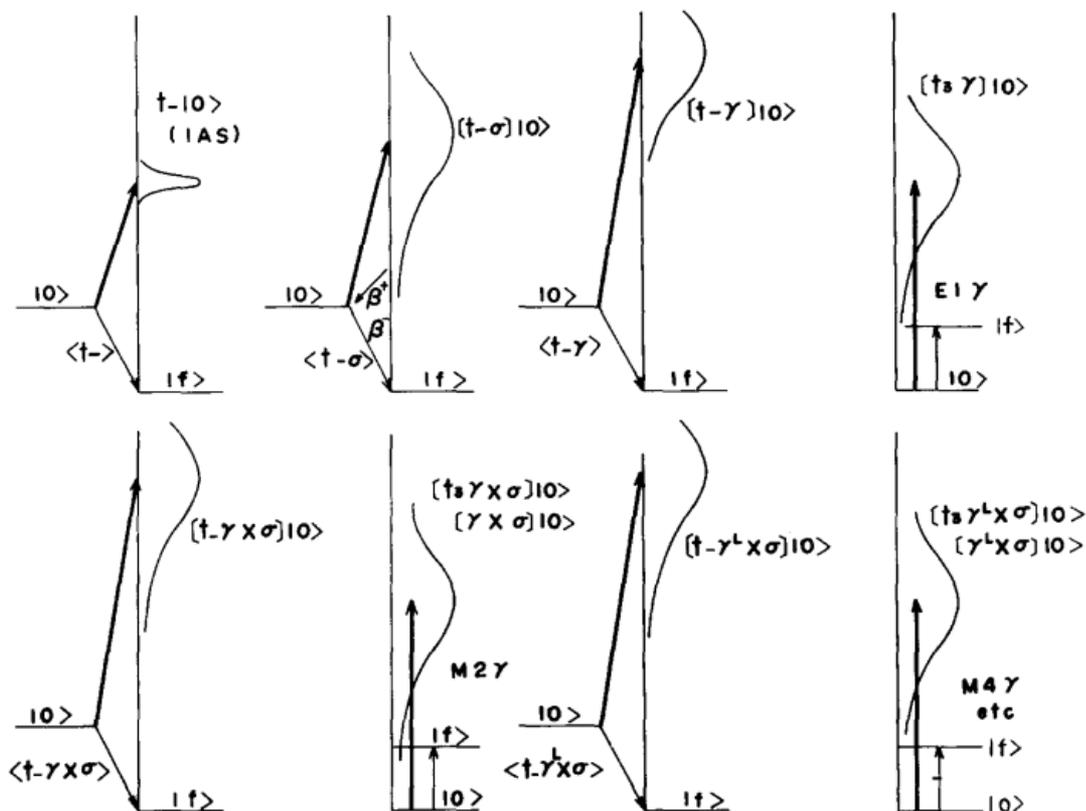


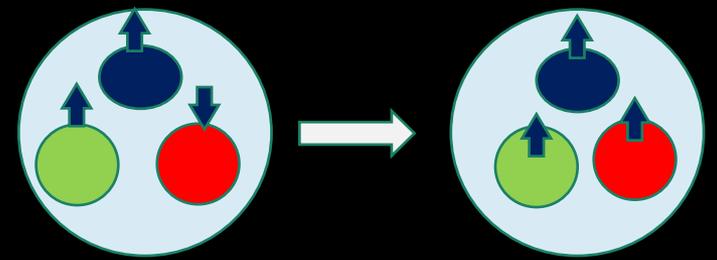
Fig. 2. Transition and level schemes showing schematically the (possible) giant resonance absorbing a large fraction of the transition strength, and the reduced single particle transition.

$g^{\text{eff}} = g/(1+\gamma)$ has been used to incorporate NN $\tau\sigma$ GR (GT, SD)
 Present : extend to the Δ GR in DBD nuclei

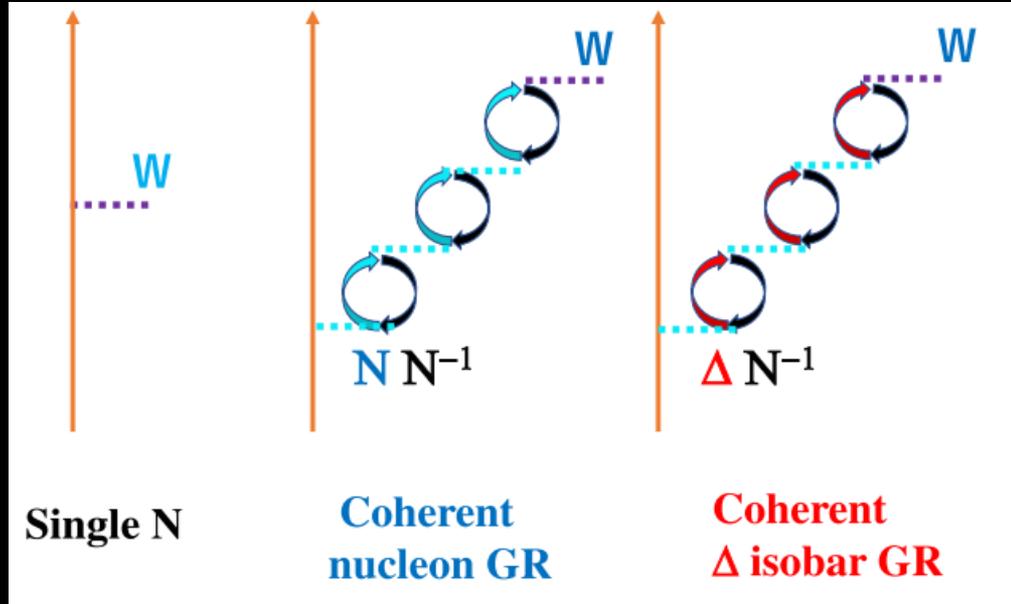
Nuclear physics with Δ

$A = \text{No of Baryons, } p, n, \Delta \text{ etc.}$

with interaction fields of $\pi, \rho, \tau, \sigma, \gamma$



Nucleon quark σ τ flip to Δ

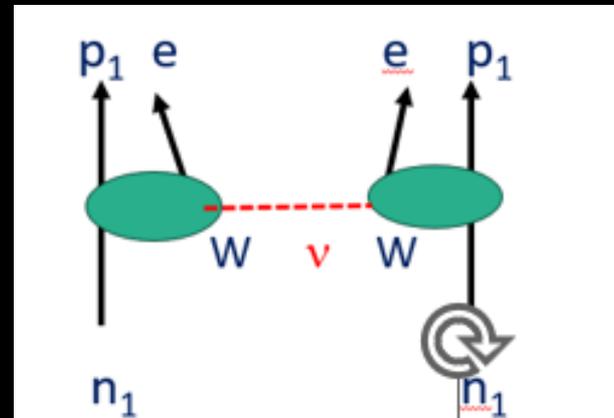
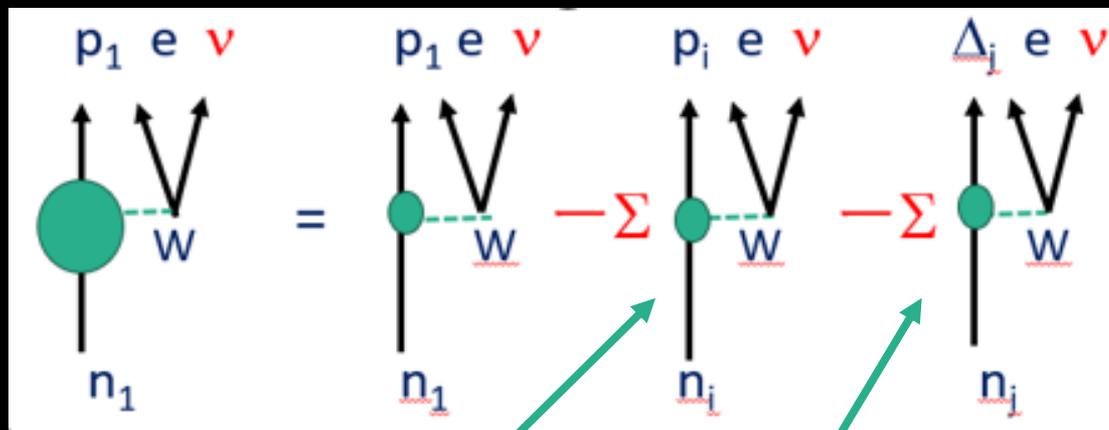


Baryons like $\Delta(1232)$ etc are effective in case of **resonances**, i.e

1. Amplitude : $a_i = (V / (300 \text{ MeV})) = \mathbf{0.001}$,
2. No $N \sim 100$ in case of $A=100$ DBD nuclei.
2. Probability $\sim N (a_i)^2 = \mathbf{0.0001}$ per nucleus.
3. $\mathbf{NME = \sum a_i \times M_i (\tau\sigma) = 100 \text{ of } 0.001 M \sim 0.1 \text{ effect}}$

Weak $n^{-1}p$ with $n^{-1}p$ GR and $N^{-1}\Delta$ GR

$$|i\rangle \Rightarrow |f\rangle = |f_1\rangle - \varepsilon |GR-N\rangle - \delta |GR-\Delta\rangle$$



$$M = M_0 - \varepsilon M(\text{GR-N}) - \delta M(\text{GR-D}) \quad \text{Tamm Dancoff}$$

NN: $(V=0.3 \text{ MeV})/10 \text{ MeV} = \text{mixing amplitude} \sim 3 \cdot 10^{-2}$
 $(3 \cdot 10^{-2}) \times (N-Z=20 \text{ coherent}) = 0.6 \text{ quench } 0.4 .$

N Δ : $(V=0.3 \text{ MeV}/300 \text{ MeV mass difference})$
 $= \text{mixing amplitude for } A=100 \text{ is } \sim 10^{-3} .$

A-nucleons produce A Δ of $\Delta^0 \Delta^- \Delta^+ \Delta^{++}$ coherent ~ 100
 $10^{-3} \times A \times 2 \text{ for f and b} = 0.2, \text{ reduce } K_{\Delta} = 0.8 \text{ reduction}$
 $\Delta \text{ probability in A nucleus} = (10^{-3})^2 \times 2A = 2 \cdot 10^{-4}$

DBD with ν exchange in 2 quarks I

n N or Δ in 2 + DBD

Enhanced by $1/r_{ij}$

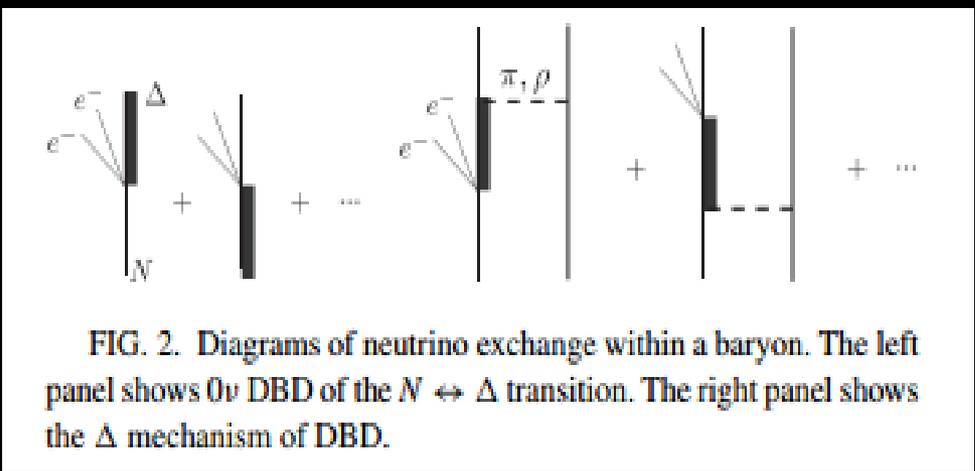
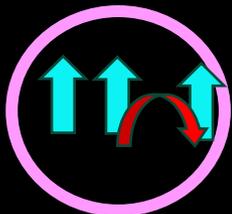
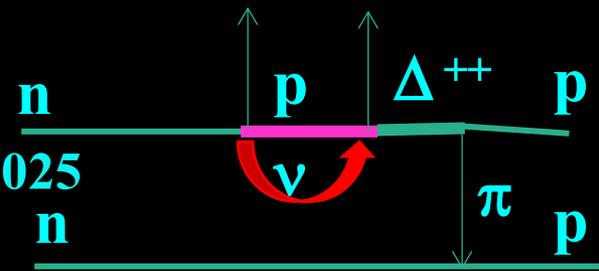
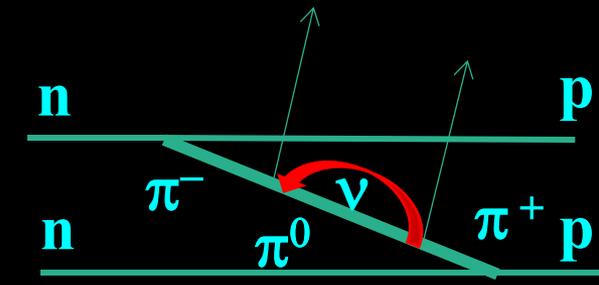
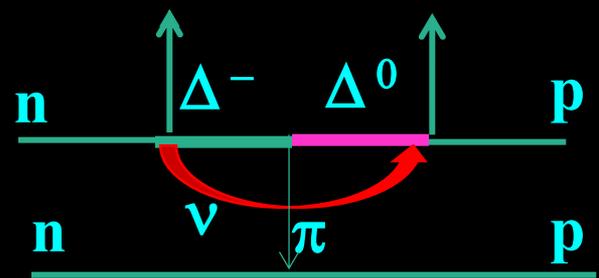
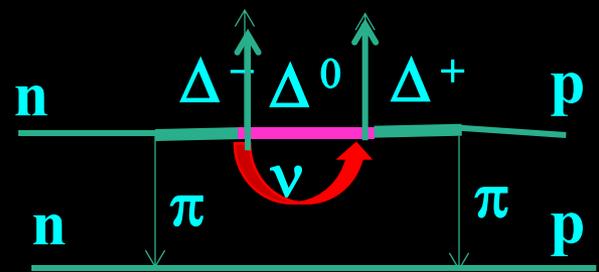


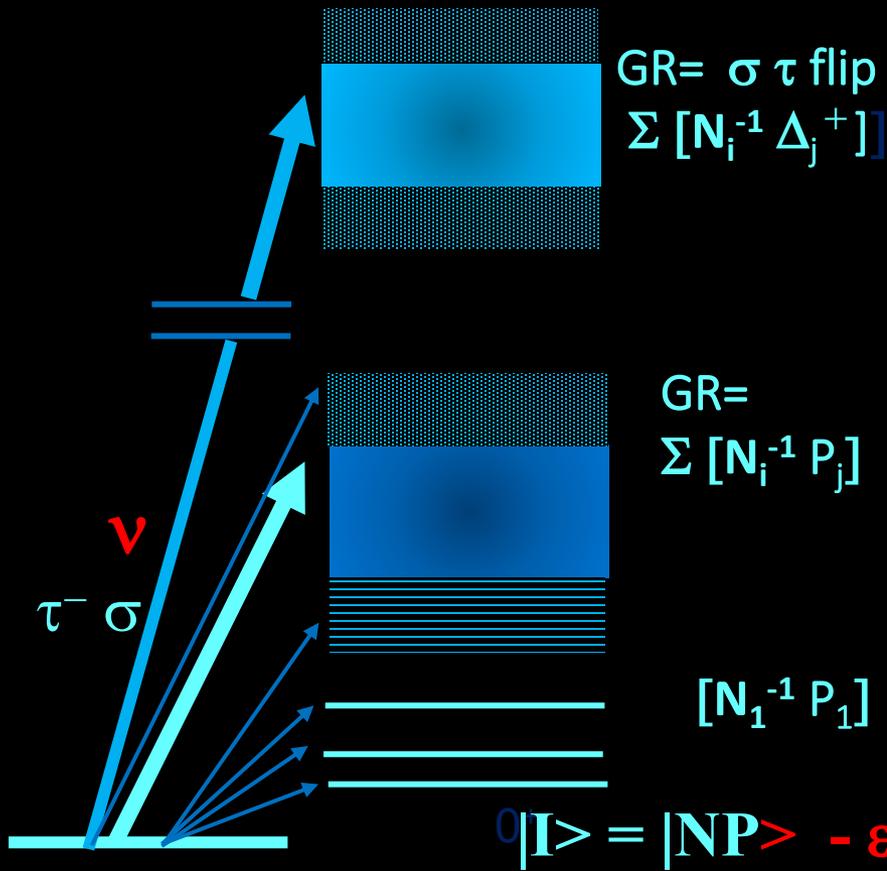
FIG. 2. Diagrams of neutrino exchange within a baryon. The left panel shows 0ν DBD of the $N \leftrightarrow \Delta$ transition. The right panel shows the Δ mechanism of DBD.



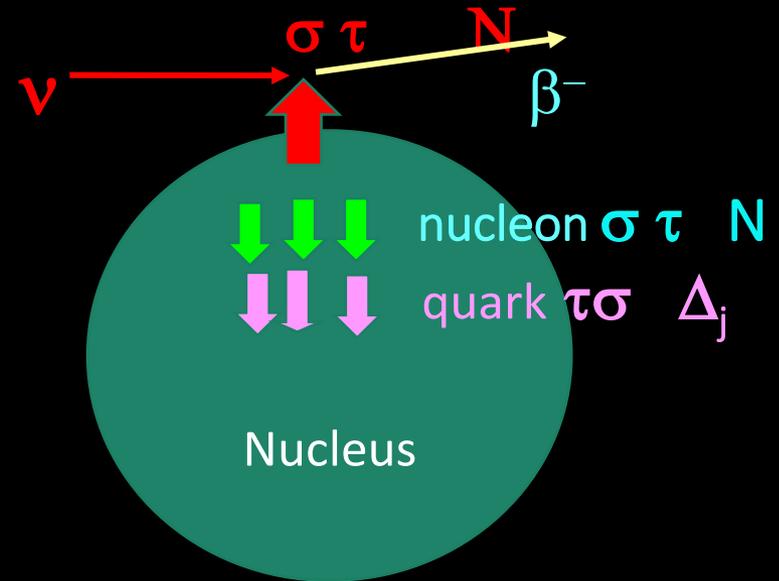
H.Ejiri, T. Fukuyama, T. Sato PR C 111 065501 2025
 E. Hiyama, H. Suganuma for hadron physics.

N-GR and Δ -GR and $\tau\sigma$ core polarization

Repulsive NN and N Δ correlations make negative $\tau\sigma$ polarizations like an effective charge = true e_0 - pol charge e



Nuclear medium $\sigma\tau$ polarization



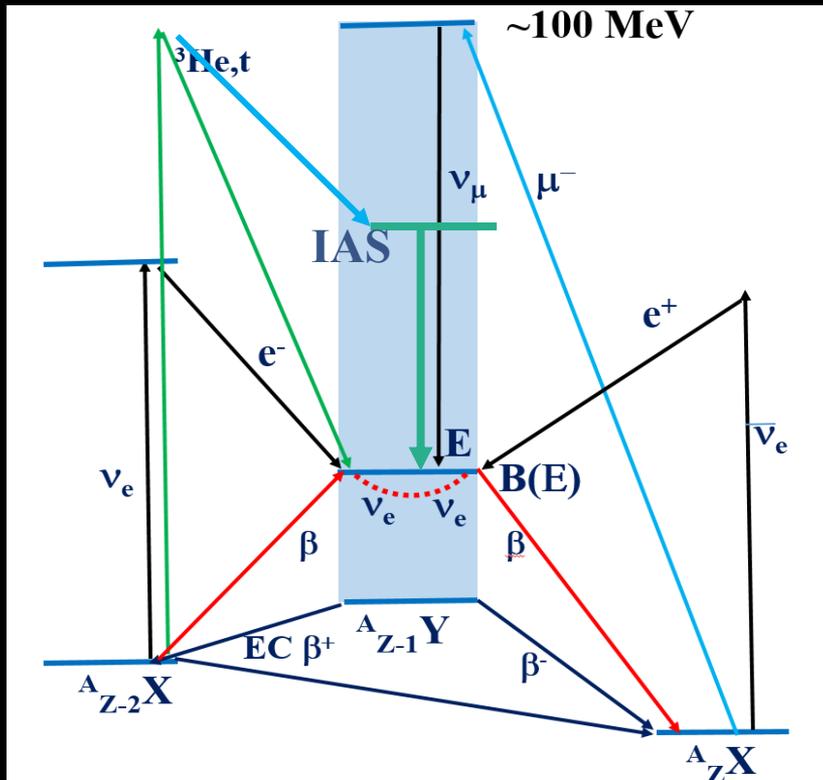
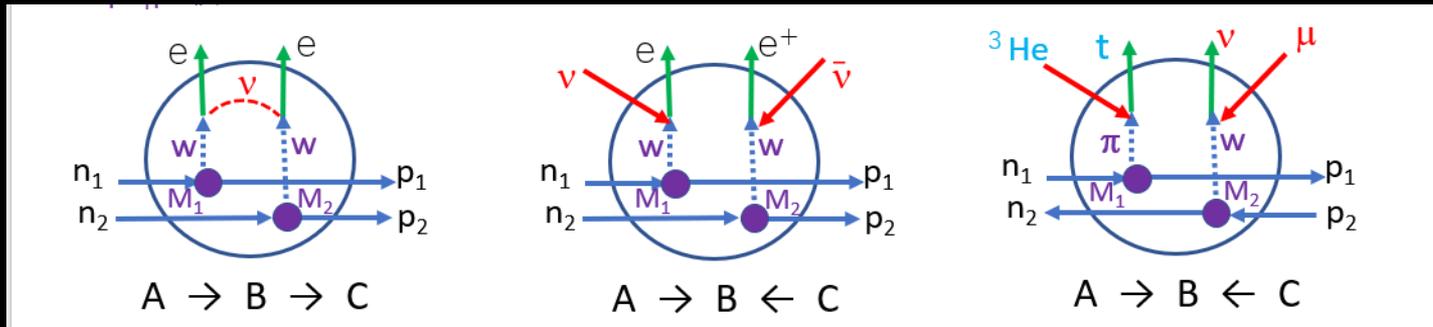
Δ - $\tau\sigma$ polarization effects

- A. Bohr and B. Mottelson PL B 100 10 1981 GT
- H. Ejiri Nucl. Phys. A 396 181 1983 SD
- F. Oesterfeld RMP 64 49 1992 , E
- D. Kirchuk et al., Phys. Scr. 59, 416 1999,
- G. Cattapan, Review PR 362, 303, 2002 , and in others.

Exchange current $=\pi+N\sim(\Delta)=2B$ current effects

- I.S. Towner PR 155 263 1987 Review
- J. Menendez et al, for DBD PRL 107, 062501 2011,
- P. Gysbergs et al, for β -decay Nat. Phys. 14, 428, 2019,
- L. Corragio et al, Review PR C 109, 014301 2024

Weak (β , $\beta\beta$, astro- ν) NMEs and CERs at RCNP



Weak ν cross sections: 10^{-43}

Studied by
Nuclear reaction
with strong interaction
CER (${}^3\text{He}, t$) RCNP
(present talk)

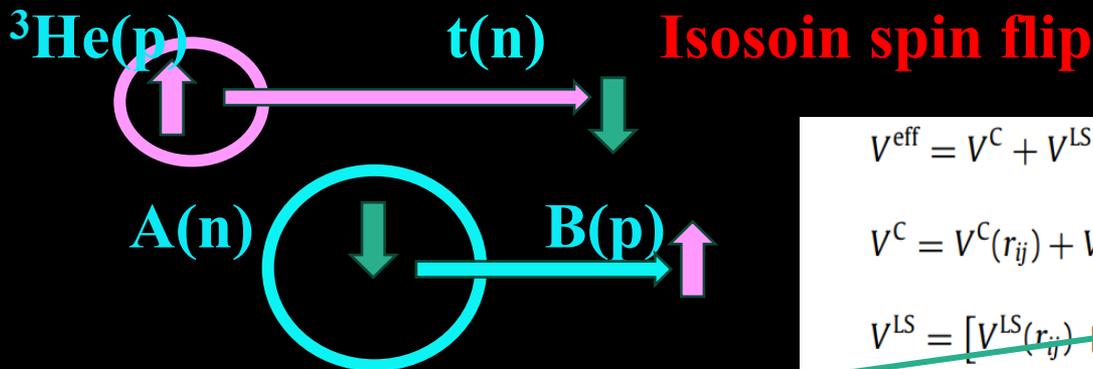
EM photon via IAS Ejiri
& μ, ν_μ capture
(Hashim Ejiri, Shima et al)

2 GT and SD summed strengths by CERs .

Summed GT –SD $\tau\sigma$ strengths in nucleon region of $E=0-30$ MeV
are reduced half, resulting in $\tau\sigma$ coupling $g^{\text{eff}}(\Delta)\sim 0.7$



Charge exchange reactions (CER) at RCNP are powerful for nuclear τ σ response studies



$$V^{\text{eff}} = V^{\text{C}} + V^{\text{LS}} + V^{\text{T}},$$

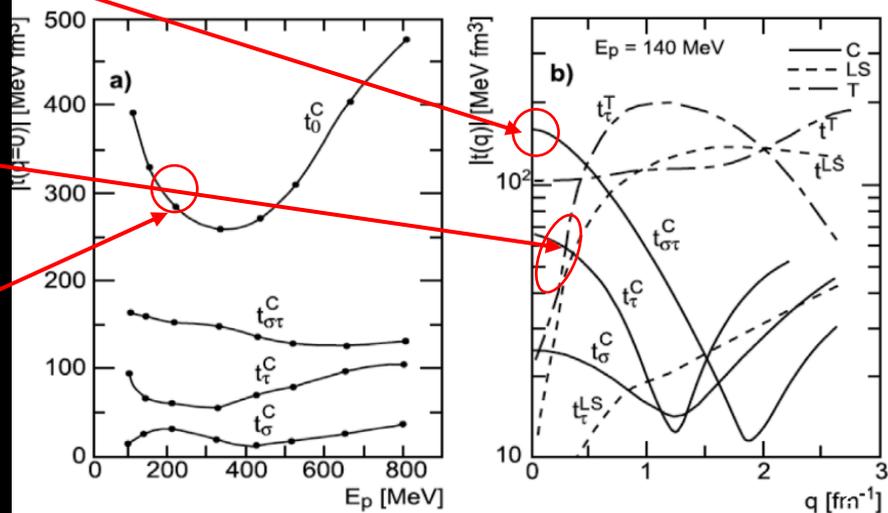
$$V^{\text{C}} = V^{\text{C}}(r_{ij}) + V_{\sigma}^{\text{C}}(r_{ij})\sigma_i \cdot \sigma_j + V_{\tau}^{\text{C}}(r_{ij})\tau_i\tau_j + V_{\sigma\tau}^{\text{C}}(r_{ij})\sigma_i \cdot \sigma_j\tau_i\tau_j,$$

$$V^{\text{LS}} = [V^{\text{LS}}(r_{ij}) + V_{\tau}^{\text{LS}}(r_{ij})\tau_i\tau_j]\mathbf{L} \cdot \mathbf{S},$$

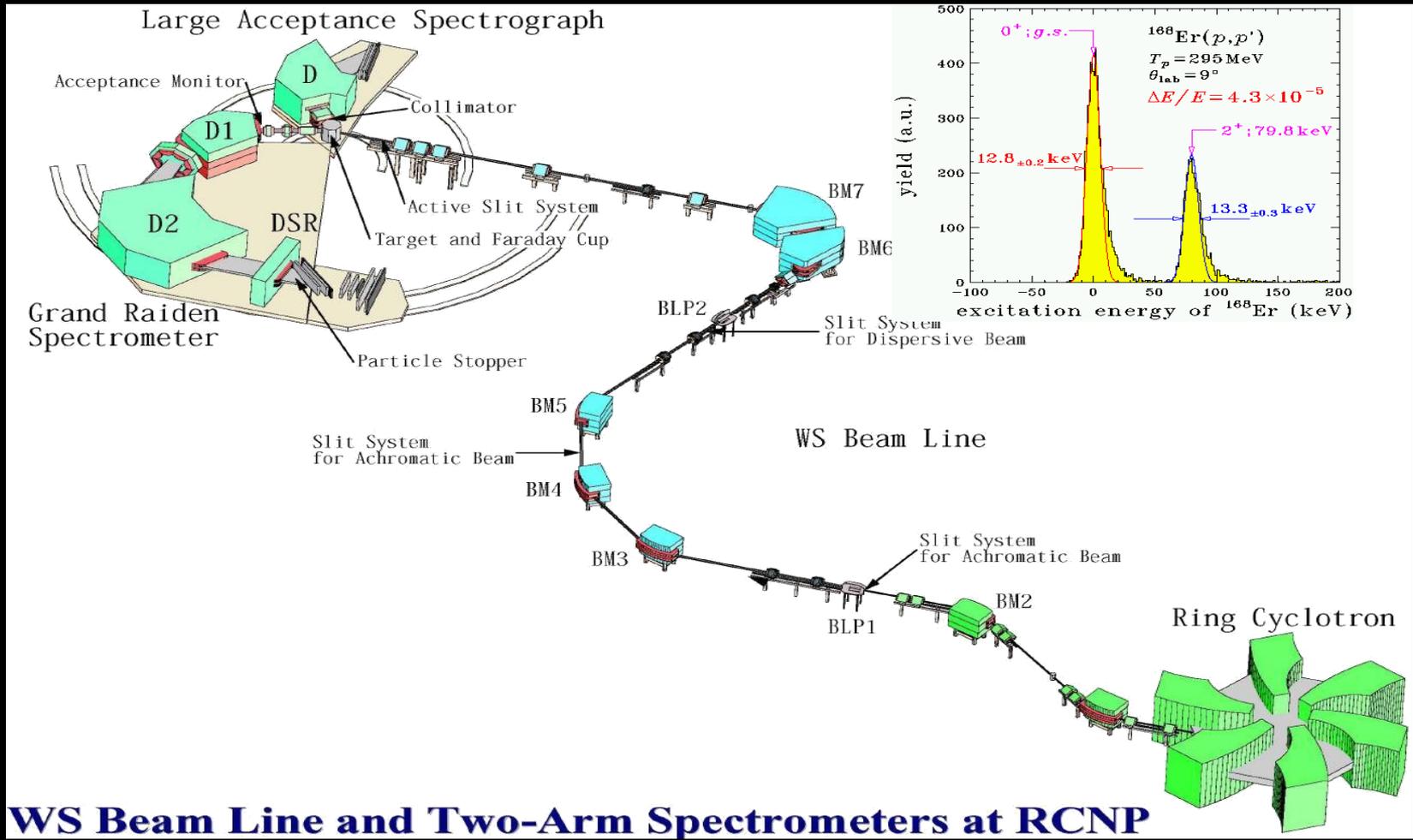
$$V^{\text{T}} = [V^{\text{LS}}(r_{ij}) + V_{\tau}^{\text{LS}}(r_{ij})\tau_i\tau_j]S_{ij}^{\text{T}}.$$

- $V_{\sigma\tau}$ interaction for GT,SD $\tau\sigma$ response is dominant at RCNP $E/A \sim 0.15$ GeV.
- Tensor /LS interactions are small at $q=0 - 0.5$ /fm
Tensor effect Y. Iwata,
H. Ejiri, Sakar 2026
- Distortion and multi-step process get minimum at $E/A=0.2 - 0.4$ GeV.

H. Ejiri, J. Suhonen and K. Zuber / Physics Reports 797 (2019) 1-102



RCNP cyclotron $E/A=0.15$ GeV warrants one step CER. Spectrometer with energy resolution 30 keV is used to select individual F, GT, SD states up to 30 MeV of current interest.



H. Akimune, M. Fujiwara, D. Frekers, A. Tamii and others for CERs

CER nuclear interaction excites isospin (τ), spin (σ), l (angle), n (radial)

Select GT ($\tau\sigma$ $\Delta l=0, \Delta n=0$) (^{128}Te)

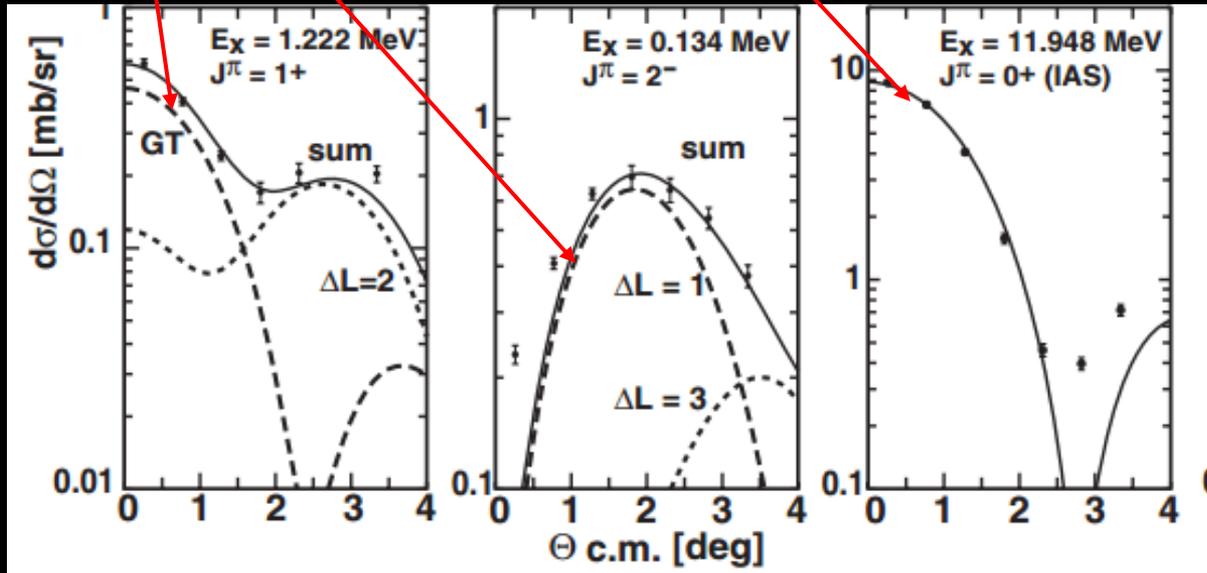
τ : CRE $n \Rightarrow p$ reaction IAS

σ 1^+ s-wave $|j_0(qr)|^2$ 0^+ neg. except IAS

$\Delta n=0$ radial node change = 0 low-excitation < 20 MeV

$\Delta n=2,4,6$ at higher 2-6 $\hbar\omega$ are at high excitations = 20-60 MeV

σ r 2^- p-wave $|j_1(qr)|^2$



RCNP CERs with ($^3\text{He}, t$) reactions to select GT

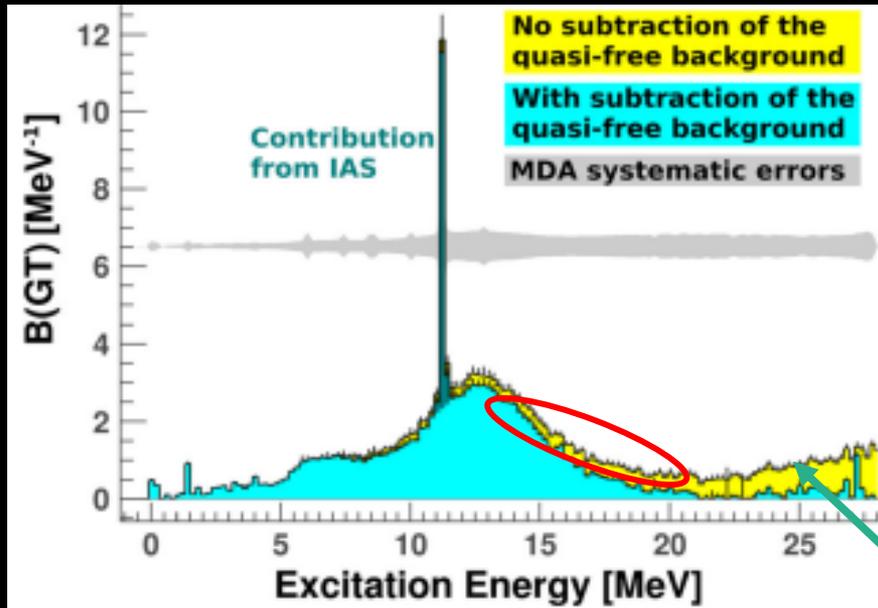


Fig. 14 Same as Fig. 13, but now for the $^{122}\text{Sn}(^3\text{He}, t)^{122}\text{Sb}$ reaction

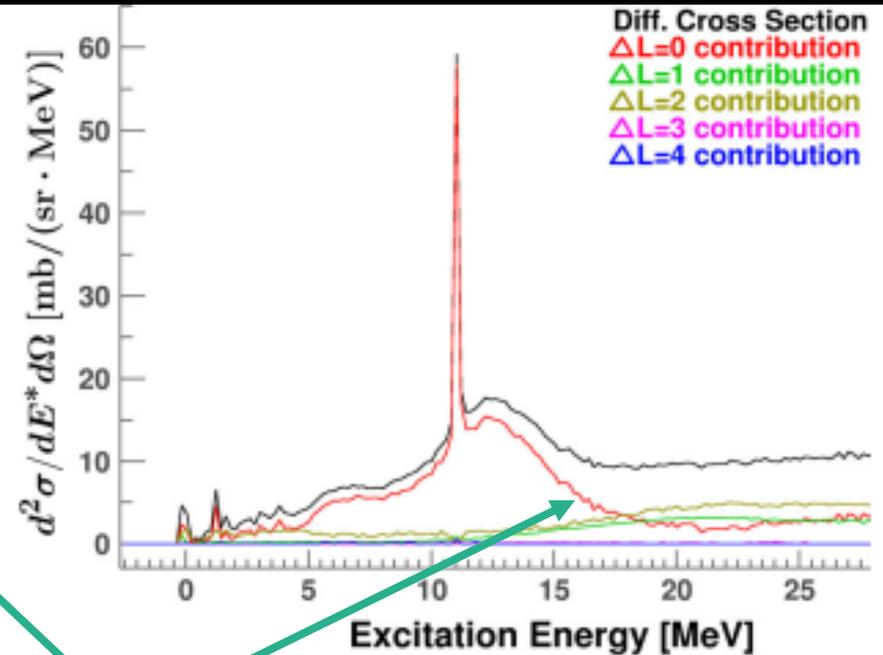


Fig. 16 Same as Fig. 15, but now for the $^{122}\text{Sn}(^3\text{He}, t)^{122}\text{Sb}$ reaction at 140 MeV/u

GT = $\tau\sigma$ $\Delta L=0$ (angular node = 0), $\Delta n=0$ (radial node = 0)
 QF Quasi-free scattering (spreading to 2p-2h) with $\Delta n=0$ (GT)
 and $\Delta n=2, 4, 6$ = Non GT, to be corrected for
 from the observed and calculated ratio of the $n=0$ and $n=2$ GRs.

DBD nuclei at RCNP

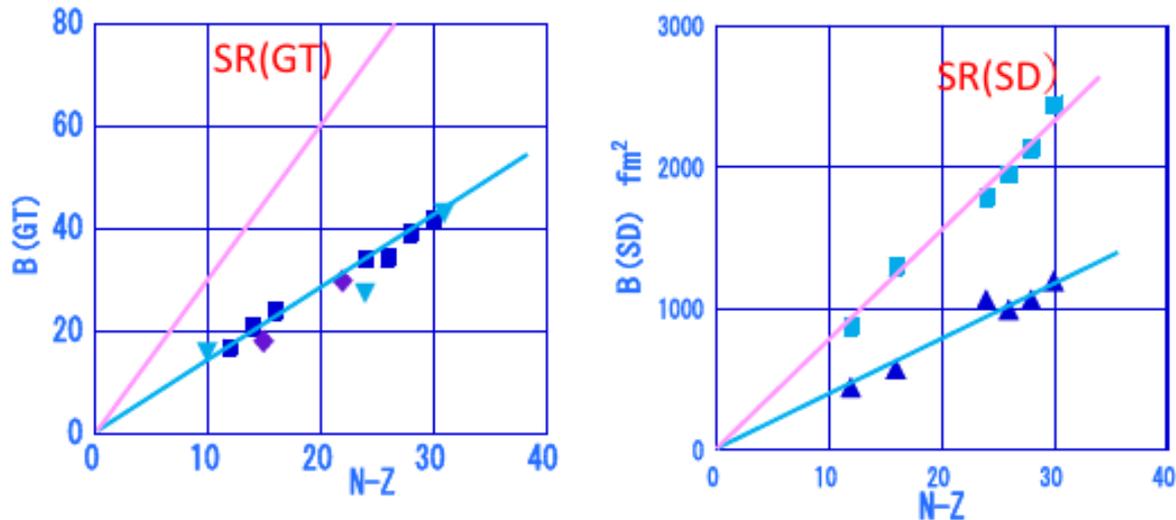


FIG. 3. Left panel: Summed GT strength of S^- (GT). Blue squares: $(^3\text{He}, t)$ on DBD nuclei. Blue diamonds: $(^3\text{He}, t)$ on Sn isotopes. Light blue squares: (p,n). Solid thin line: $S_N(\text{GT})$. Thick line: $0.47 S_N(\text{GT})$. Right panel: Summed SD strength of S^- (SD). Blue triangle: $(^3\text{He}, t)$ on DBD nuclei. Light blue square: sum rule limit of $S_N(\text{SD})$. Thick line: $0.50 S_N(\text{SD})$.

$$\text{IFF } S(\text{GT})=3(N-Z) \quad S^-(\text{SD})=\sum(2l+1)(N^{\text{eff}}/2\pi) \langle r^2 \rangle$$

$$r^2=0.6 R^2 \quad \text{with } R \sim 1.35 A^{1/3} \text{ for n to p effective radius}$$

Experimental summed GT and SD strengths are a half of the nucleon-based IFF sum rule limits. First results on DBDs.

Comments on Summed GT strengths ~ 0.5 of IFF sum rule $\Sigma=3(N-Z)$ is

based on the $t_z = \pm 1/2$ n,p model with no non-nucleons like Δ .

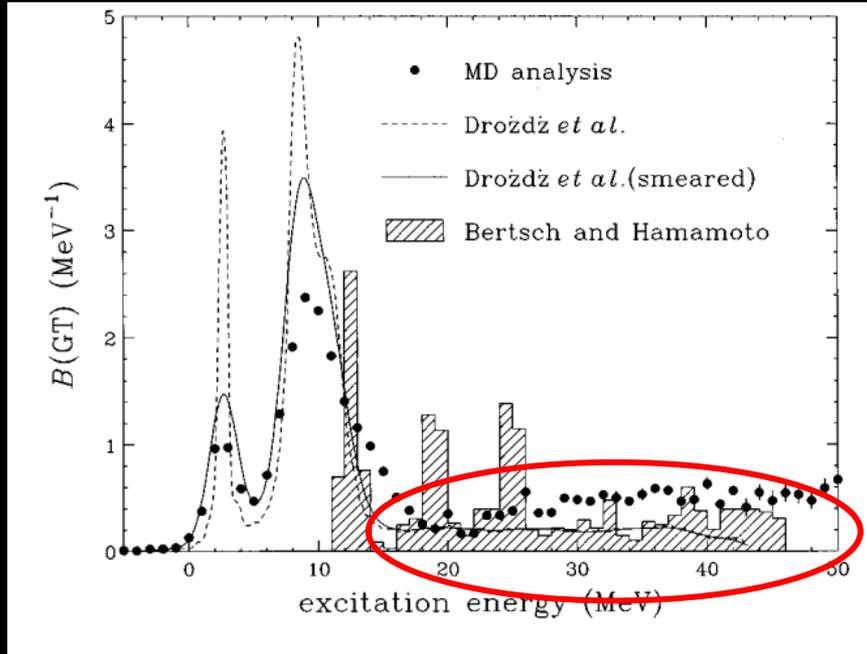
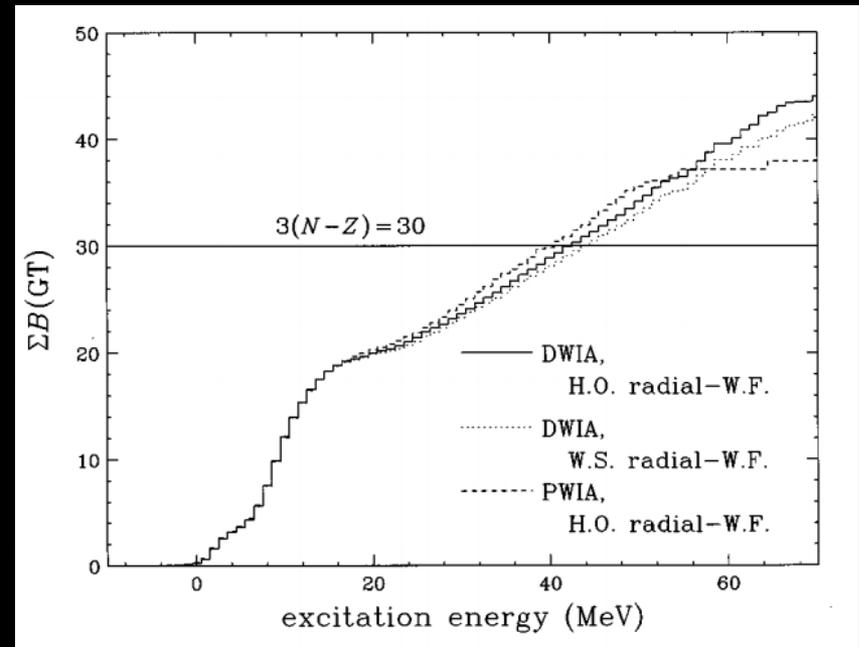


FIG. 13. Gamow-Teller strength distribution (filled circles) obtained from the 0° $L=0$ cross section which is deduced from the MD analysis. The dashed curves and hatched histogram represent the SRPA calculation by Drożdż *et al.* [22] and the perturbative calculation by Bertsch and Hamamoto [15], respectively. The



Gaarde and others $\ll 3(N-Z)$
Wakasa et al PR C 55 2909 1997
Full $3(N-Z)$, mainly in $n=2,4,6$ $\hbar\omega$

Berch Hamamoto PR C 26 1323 1082
 $B(GT) > 50\%$ of $3(N-Z)$ beyond GT-GR
No Δ coupling, No $n=2,4$ $\hbar\omega$

4. NEWS (Neutrino, Electromagnetic, Weak and Symmetries) with $N\Delta$ GR

- Nuclear states $f \supseteq |n\rangle - \delta|\Delta$ GR \rangle with $\delta \sim V/\Delta$ -mass ~ 0.001 .
Weak, EM and nuclear $\tau\sigma$ -NMEs much quenched .



QRPA with NN and N Δ separable interactions

Quenching of $\tau\sigma$ NMEs by Δ effects and exchange (2B) currents since 1980

A. Bohr and B. Mottelson

F. Osset Gaarde

Present QRPA for NN and N Δ separable interactions

$$V = g'_{NN} C V_{12} \sigma_1 \sigma_2 \tau_1 \tau_2 + g'_{N\Delta} C' V_{12} S_1 \sigma_2 T_1 \tau_2, \quad (1)$$

where $V_{12} = \delta^3(r_1, r_2)$, $C = 392 \text{ MeV fm}^3$ and $C' = (f_{\pi N\Delta}/f_{\pi NN})C = 2C$ [22, 23, 48], and S and T are

$g'_{NN'} C V_{12} = \chi_N/A$ and $g'_{N\Delta} C' V_{12} = \chi_\Delta/A$. They are written as $\chi_N = 48 g'_{NN'}$ MeV and $\chi_\Delta = 96 g'_{N\Delta}$ MeV.

Interactions $g'_{NN} = 0.5$, $g'_{N\Delta} \sim 0.6$ Julich Tokyo Potential
The same NN and N Δ $\tau\sigma$ interactions for
GT weak, EM and strong $\tau\sigma$ NMEs.

Dispersion equation with NN and NΔ interactions

$$\frac{\chi_N}{A} \sum_i \frac{|\langle \phi_i^- || \sigma \tau^- || 0 \rangle|^2}{\epsilon_i - \epsilon} + \frac{\chi_\Delta}{A} \sum_j \frac{|\langle \psi_j^- || ST^- || 0 \rangle|^2}{\epsilon_{\Delta j} - \epsilon} + \frac{\chi_\Delta}{A} \sum_k \frac{|\langle \psi_k^+ || ST^+ || 0 \rangle|^2}{\epsilon_{\Delta k} + \epsilon} = -1 \quad (3)$$

where ϕ_i^- stands for the $n_i^{-1}p_i$ state, ψ_j^- for the $n_j^{-1}\Delta_j^+$ and $p_j^{-1}\Delta_j^{++}$ states and ψ^+ for the $n_k^{-1}\Delta_k^-$ and $p_k^{-1}\Delta_k^0$

$V=\tau\sigma$, $M=\tau\sigma$, thus the product is $|\langle \sigma \tau \rangle|^2$, all with the same phase, NN for forward correlation because of blocking of backward $p \Rightarrow n$ in case of DBD nuclei with $N \gg Z$ $N_0 = N - Z \sim 15$

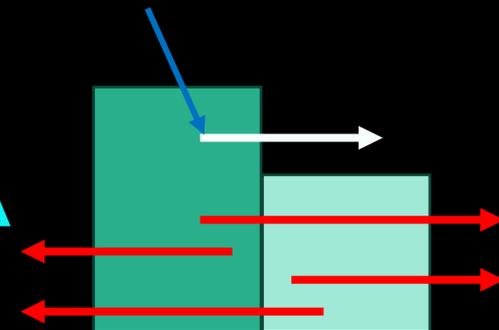
The NΔ terms of the dispersion equation.

NΔ for both forward and backward $p, n \Rightarrow \Delta$

Number of GT $N \Rightarrow \Delta \sim 2(N+Z) = 2A \sim 200$

since all n and $p \Rightarrow \Delta^+, \Delta^{++}, \Delta^-$ and Δ^0

Then the Δ effects get significant



$N\Delta$ contribution amounts to 30 %, very important effect on NME
 $\Delta \tau\sigma$ susceptibility = $V \times \text{Sum of NME}^2/\text{Energy gap}$

$$\kappa_{\Delta} \approx \frac{\chi_{\Delta}}{A} \left[\frac{2(A + 0.33A)}{300} \right] / \text{MeV} = 0.009\chi_{\Delta} / \text{MeV}.$$

Using $g'_{N\Delta} \sim 0.5$ and $\chi_{\Delta} = 48 \text{ MeV}$ Julich Tokyo Potential,
Susceptibility for $\Delta \tau\sigma$ GR/correlations $\kappa_{\Delta} = 0.43$,

Nuclear part of the dispersion equation is expressed as

$$\frac{\chi_N}{A(1 + \kappa_{\Delta})} \left[\sum_i \frac{\langle n_i^{-1} p_i | | \sigma \tau^- | | 0 \rangle|^2}{\epsilon_i - \epsilon} \right] = -1,$$

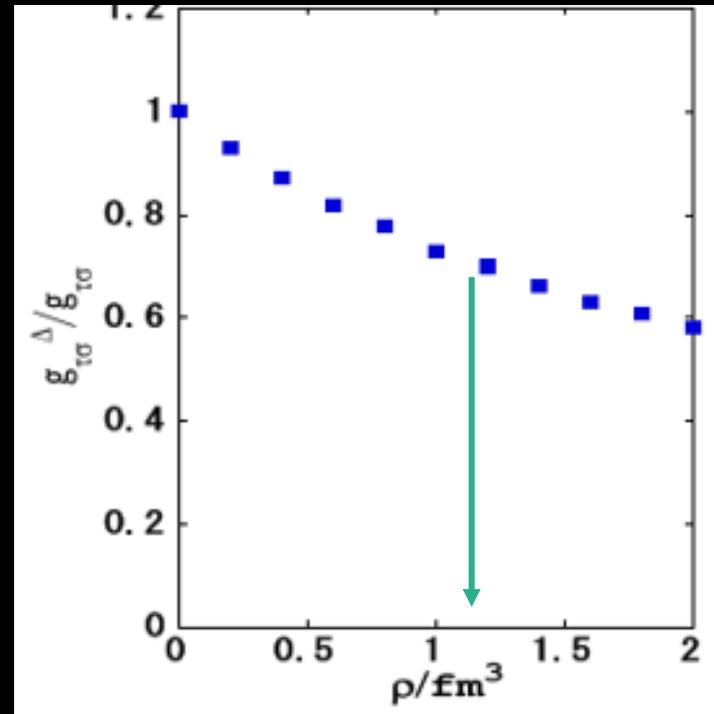
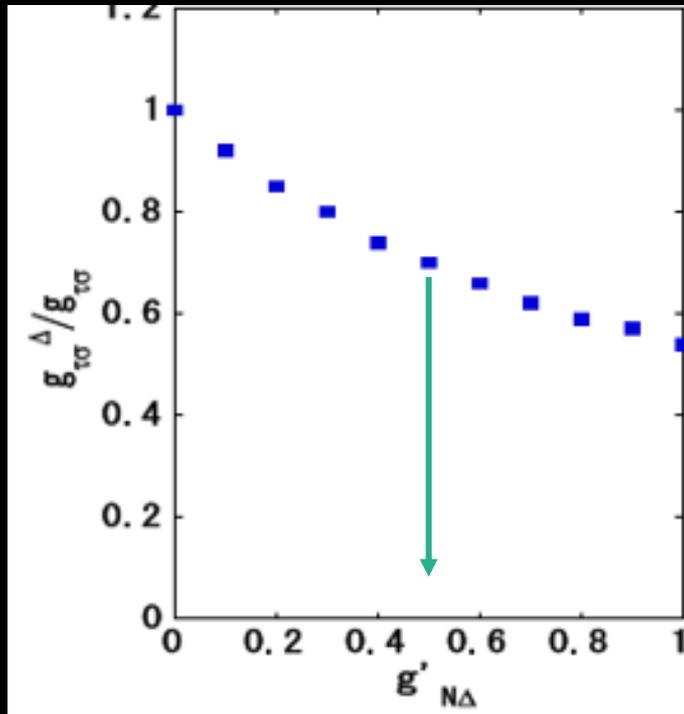
Renormalized NN coupling by the coefficient
 $1/(1 + \kappa_{\Delta}) = 0.7$

Renormalization (effective coupling) due to Δ

$$\mathbf{K}_{\Delta} = \mathbf{g}_{\tau\sigma}^{\Delta} / \mathbf{g}_{\tau\sigma} = 1/(1 + \kappa_{\Delta}) = 0.7$$

in agreement with exp. summed strength.

Effective $\tau\sigma$ coupling $g_{\tau\sigma}^{\Delta}$ depends on the $N\Delta$ interaction and density.



It is around 0.7

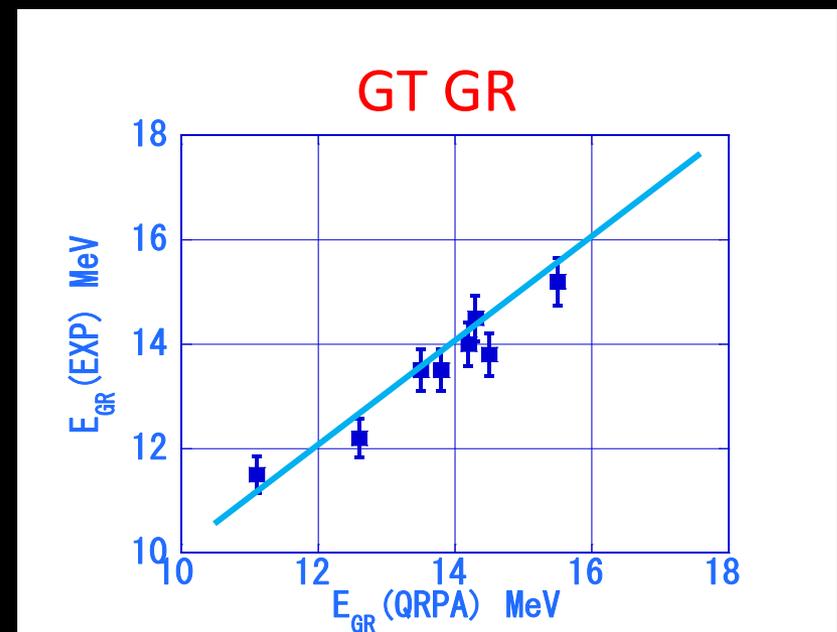
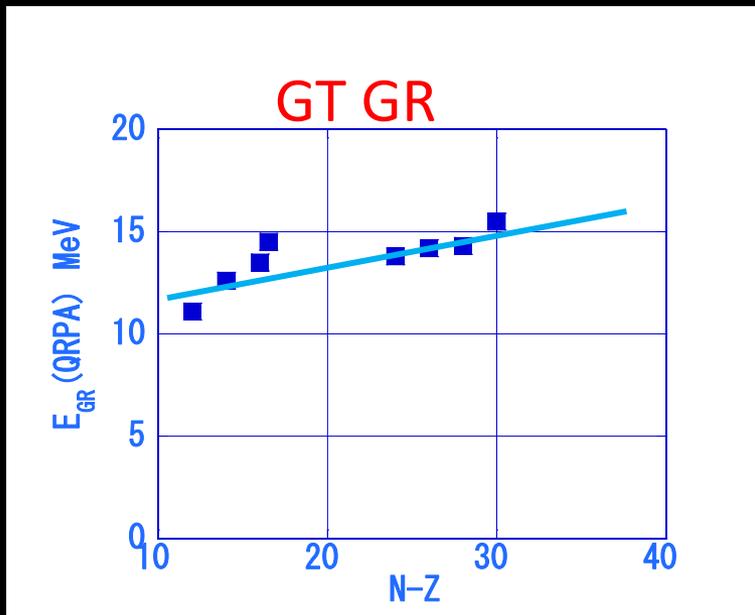
at the realistic interaction 0.5 and the density 1.2
Similar r dependence in 2B (Menendez PRL 107)

NN GR GT Energy and NN interaction

N- Δ interaction pushes down the NN GR(GT)

NN interaction pushes up the NN GR(GT).

Using N Δ $g'_{N\Delta}=0.5$ ($\chi_{\Delta}=48\text{MeV}$) from the summed strength,
and the experimental N-GR GT energies,
one gets $g'_{NN}=0.62$ ($\chi_N=30\text{ MeV}$), as Julich Tokyo potential



Δ GR energy and cross section

GR cross sections are proportional to A as observed in (γ, A)

Thus $\sigma/A \sim$ constant for all A

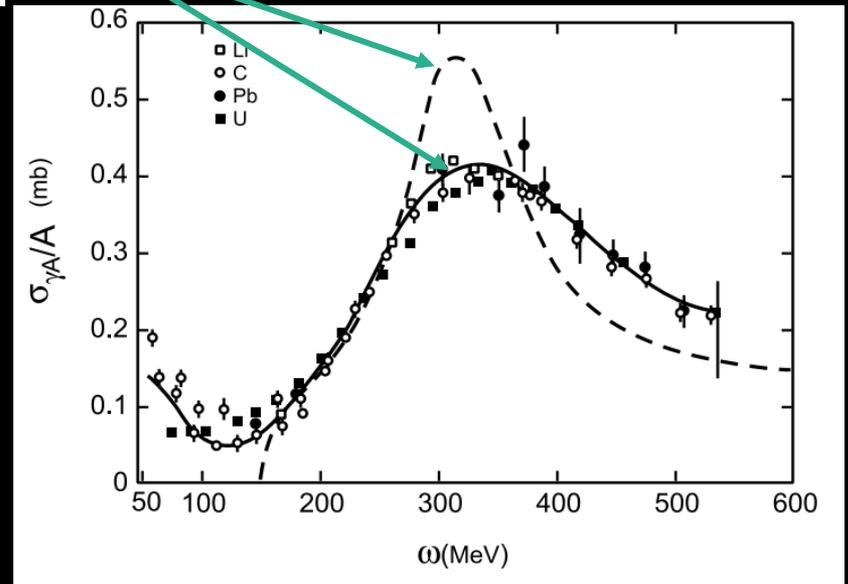
Recoil energy ~ 50 MeV for p and 0.5 MeV for $A=100$.

$$E(\text{GR}_\Delta) = E_\Delta(0) + \frac{\chi_\Delta}{A} \frac{6Z + N}{3}$$

284 MeV Δ in
a nucleus $\sim 294-10$

48 MeV/A

335 MeV



Giorgio Cattapan^{b,c}, LÍdia S. Ferreira^{a,*}

PR 362 303 2002

J. Ahrens, L.S. Ferreira, W. Weise, Nucl. Phys. A 485 (1988) 621.

Low lying QP $\tau\sigma$ (axial-vector) NME

M(QP)=UV M(SP) Vacancy-occupation corrected SP NME

Reduced(quenched) due to NN GR and N Δ $\tau\sigma$ GR correlations

$$M = K_{N\Delta} M_{QP}, \quad K_{N\Delta} = \frac{1}{1 + \kappa_N + \kappa_\Delta},$$

$K_{N\Delta}$ =NN and N Δ $\tau\sigma$ GR correlations /susceptibilities.

χ_Δ =48 MeV and the summed strength =0,7, one gets κ_Δ =0.43

$$\kappa_N = \frac{\chi_N N_f G^2}{A \bar{\epsilon} - \epsilon_1},$$

**κ_N =2.1 from NN $\tau\sigma$ correlations χ_N =30 MeV
derived from experimental GR GT energy.**

Then one gets $K_{\Delta N}$ =1/(1+2.1 + 0,43)=0.28,

The same quenching coefficient is derived as

$$K_{N\Delta} = K'_N \times K_\Delta,$$

$$K'_N = 1/(1 + \kappa'_N) \text{ and } \kappa'_N = \kappa_N K_\Delta \approx 0.7\kappa_N.$$

NME($\tau\sigma$) for low-states in DBD nuclei $A=76-136$

Spin isospin (axial-vector) NMEs are reduced by N-GR and Δ -GR

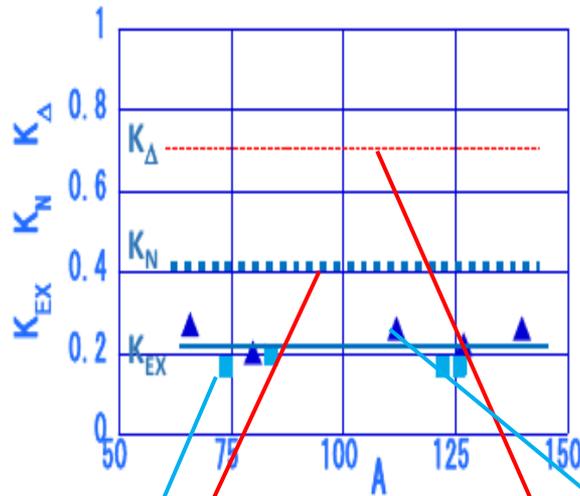
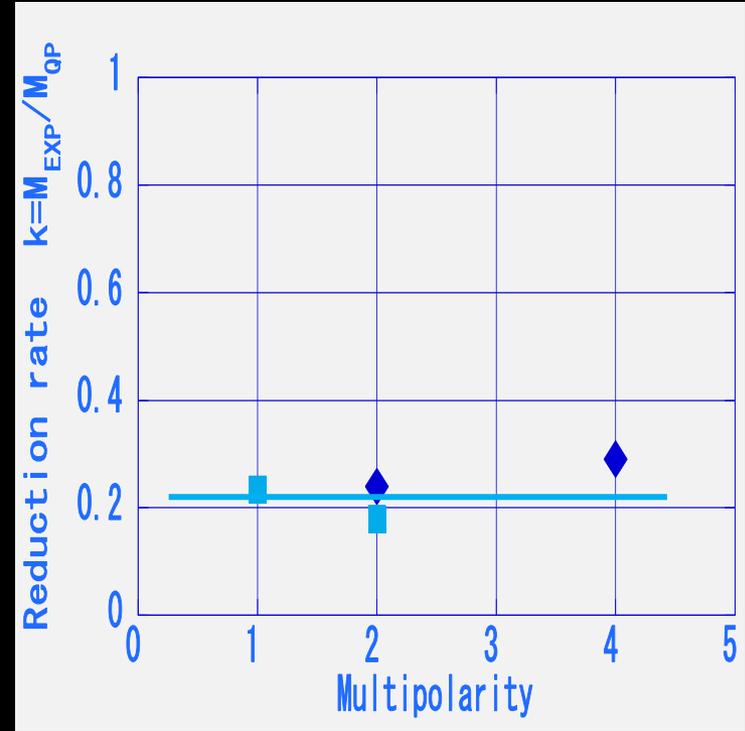


FIG. 4. Quenching coefficients. Blue triangles: $K_{EX}(GT)$ and Blue squares: $K_{EX}(SD)$. Thick blue line: $K_{EX}=0.21$. Thick dotted blue line: K_N . Thin dotted red line: $K_{\Delta}=0.7$.



$$M(EXP) = K_{EX} M(QP) \quad K_{EX} \sim 0.21 : \text{Ejiri Suhonen G. Phys. 42 2015}$$

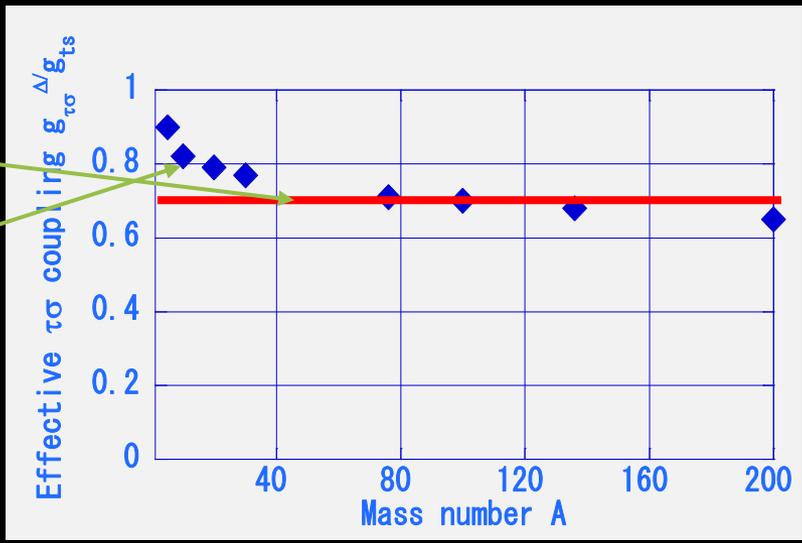
$$K_{EX} = K_{QR} K_m K_{\Delta} \quad K_{GR} = 0.4 \quad (0.28/0.7) \text{ for NN } \tau\sigma \text{ (NN GR)}$$

$$K_{\Delta} = 0.7 \text{ N}\Delta \text{ } \tau\sigma \text{ correlations (N}\Delta \text{ GR)}$$

Then $K_m = 0.8$ 2p-2h and others, not in QRPA.

1. A dependence

$g_{\tau\sigma}^{\Delta} / g_{\tau\sigma} = 0.7$ with constant V .
 $A^{0.3}$ depend. (Honma PRC 54 2972)



2. Comments on g_A^{eff} DBD

* $g_A^{\text{eff}} / g_A = (M^{2\nu}(\text{exp}) / M(\text{model}))^{1/2}$,
 reflect NN-GR, higher-shells,
 2p-2h, $N\Delta$ - exchange-(2B), others,
 if not included in models.

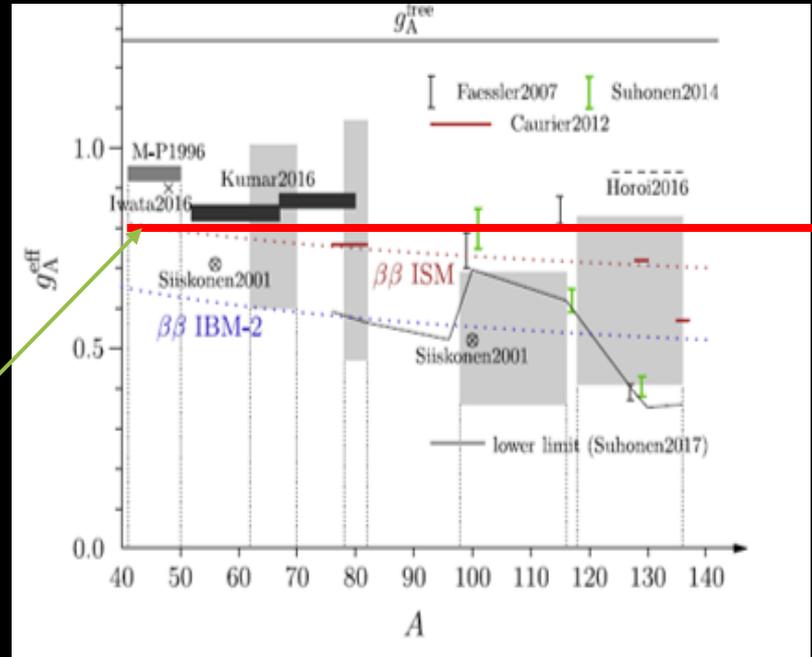
Thus they scatter much.

* If the M(model) includes all
 except the Δ GR,

$$g_A^{\text{eff}} / g_A = g_{\tau\sigma}^{\Delta} / g_{\tau\sigma} = 0.7$$

* In QRPA with N-GR,

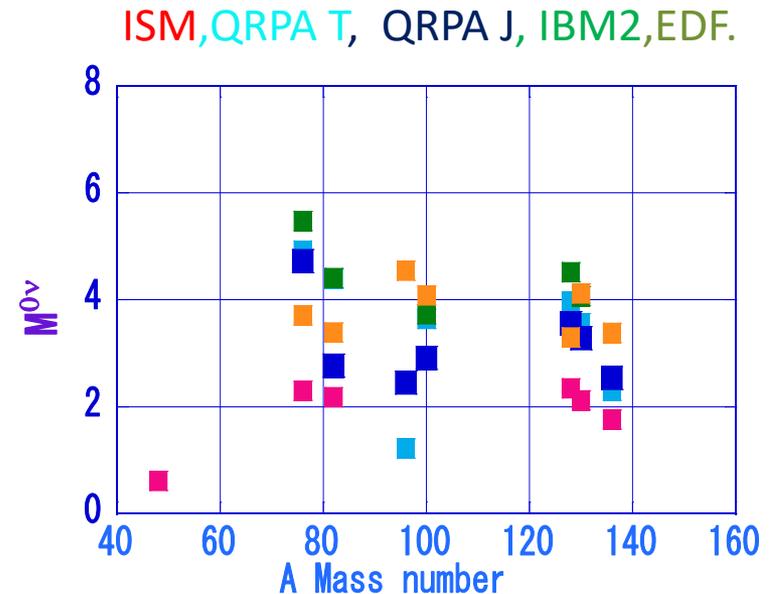
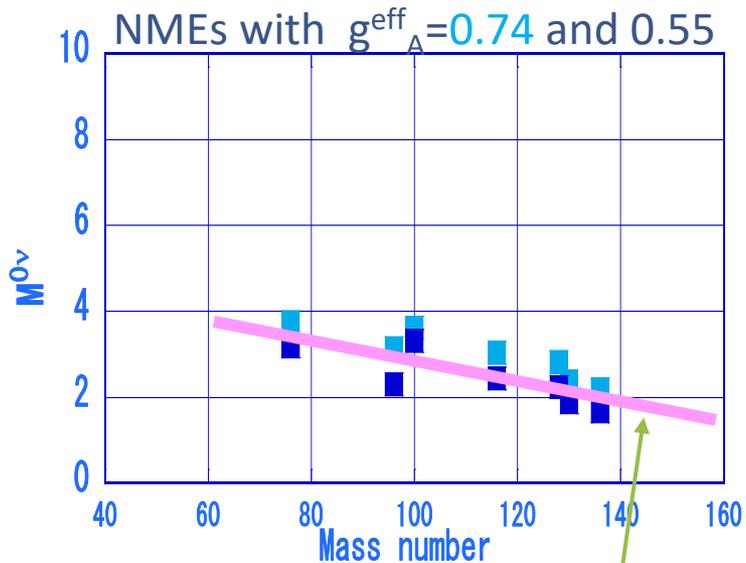
$$g_A^{\text{eff}} = \Delta\text{-GR and } K_m = 0.7 \times 0.8 \times 1.27$$



1. Exp. approaches to DBD and astro ν NMEs

Double ν & astro- ν $P \sim 100$ MeV $\tau \sigma$ $l=0-6$

NMES are sensitive to models and $\tau \sigma$ correlations,



pnQRPA with experimental inputs

Ejiri Jokiniemi Suhonen PRC L 104 2022

Recommended NMEs with $g_A = 0.7 \times 0.8 = 0.56$

$$M^{0\nu} \sim 5.2 - 0.023 A$$

$M^{0\nu} \sim$ depends on models

ROPP 2014 Vergados Ejiri Simkovic

5. Concluding Remarks

The spin isospin strength gets away by half from the nucleon world to the Delta world .



1. The summed GT and SD (spin dipole) strengths measured by $(^3\text{He},t)$ on DBD nuclei are quenched by $(g_{\Delta}^{\Delta}/g_{\Delta})^2 \sim (0.7 \pm 0.07)^2$ with respect to $3(N-Z)$ IFF limit based on a simple N model. This indicates **non-nucleonic $\tau\sigma$ Δ GR** correlation.
2. The experimental quenching coefficients are well reproduced by the **QRPA with such NN and $N\Delta$ interactions of $g'_{\text{NN}} \sim 0.62$ and $g'_{\text{N}\Delta} = 0.5$** , that reproduce the experimental NN and $N\Delta$ GR (giant resonance) energies and the summed strengths.
3. Axial vector β QP NMEs for $\beta\beta$ nuclei are reduced by **$K_{\text{EX}} \sim 0.21$** , due to the NN GR correlations of **$K_{\text{N}} \sim 0.4$** and the nuclear medium effect of **$K_{\text{M}} \sim 0.8$** and the Δ GR effect of **$K_{\Delta} = 0.7$** .
4. The Δ GR effect, being due to the Δ mixture by the **$N\Delta - \tau\sigma$ nucl. interaction, quenches all weak, electro-magnetic and strong $\tau\sigma$ NMEs** involved in Neutrino, EM, Weak, Strong interactions in nuclei. Thus the impact on particle-nuclear physics is great.

**Thank you for your attention, and
all collaborators for the supports for the 0.9 century, including**



**U Tokyo, INS, UW, NBI, LBL, Osaka-U, RCNP, CTU, Jyvaskyla, TUD, UOI,
ELEGANTs, Majorana-Dem., UTM, and all other collaborations.**

TABLE II: Calculated Landau parameters g'_0 and $g'_{N\Delta}$. The value of g'_0 is measured in units of $C_0 = 392 \text{ MeV fm}^3$, while $g'_{N\Delta}$ is measured in units of $2 \times C_0 = 784 \text{ MeV fm}^3$. Listed are results of G -matrix calculations performed by the Jülich group (Nakayama *et al.*, 1984) and by the Tokyo group (Cheon *et al.*, 1983). The various calculations were performed with different input and different approximations. Set I: Bare nonrelativistic G matrix based on the Bonn potential (Holinde *et al.*, 1972). Set II: Bare G matrix plus induced interaction. Set III: Bare G matrix plus induced interaction plus relativistic corrections. From Towner, 1987.

		g'_0	$g'_{N\Delta}$
Jülich	I	0.49	0.35
	II	0.58	0.56
	III	0.56	0.68
Tokyo	I	0.52	0.35
	II	0.61	0.45

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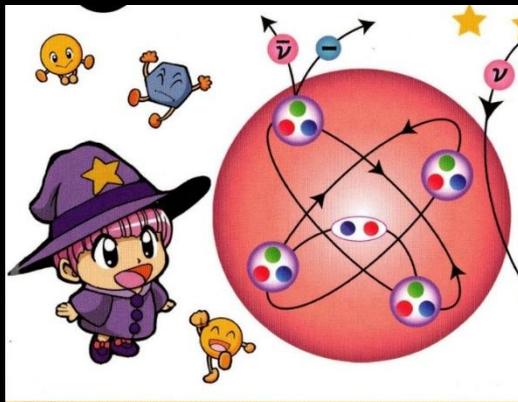
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Science Gallery

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Welcome to Hiro Ejiri's Galleries



Hiro Ejiri

PhD and Prof. EM &SP

RCNP, Osaka Univ.

ejiri@rcnp.osaka-u.ac.jp

<https://hiro-ejiri-mark.com>





Hiroyasu Ejiri, PhD

Physicist, Researcher

📍 Osaka, Japan

Profile

Professor Hiroyasu Ejiri graduated from University of Tokyo (Physics course), earning his B.S. in 1958 and Ph.D. in 1963.

*He has held extensive academic appointments at research institutes and/or physics departments of leading universities, including **University of Tokyo, University of Washington, University of California, University of Copenhagen, Osaka University, International Christian University, and Czech Technical University.***

*He has played leading roles in nuclear physics research, serving as the professor and/or the supervisor at these universities, the chairperson of the Nuclear Physics Committee in Japan, **the director of Research Center for Nuclear Physics Osaka Univ., and the director General of Yamada Science Foundation.***

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Cyclotron accelerator



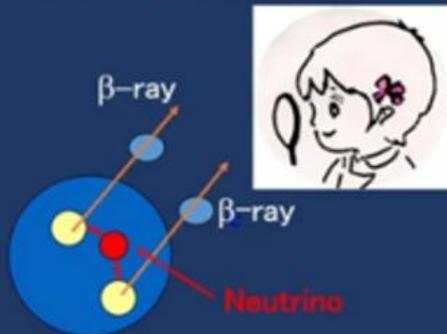
Research Center for Nuclear Physics (RCNP)
Osaka University



Research Center for Nuclear Physics.
Prof. Ejiri, Director 1993-1999



Electron Gamma-ray Neutrino Telescope ELEGANT



Ohto Underground Lab.

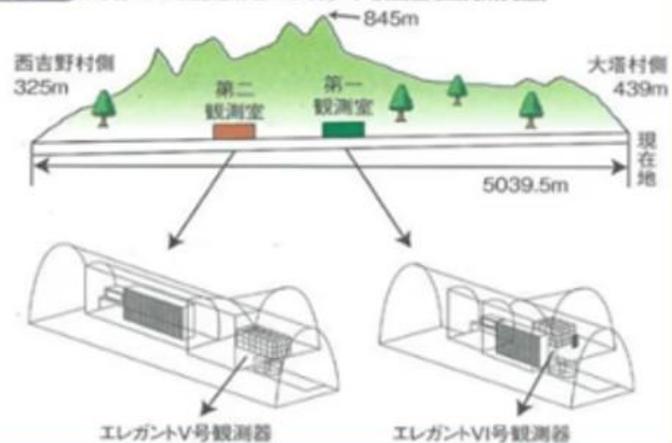


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Nuclear Structures – Nuclear vibrations and rotations.

Nuclear Reactions – Pre-equilibrium processes and charge-exchange reactions.

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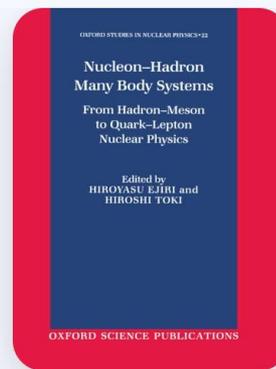
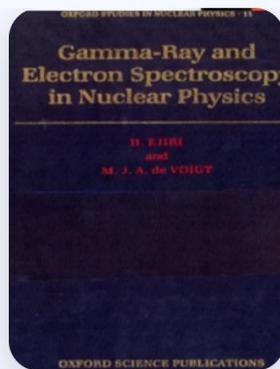
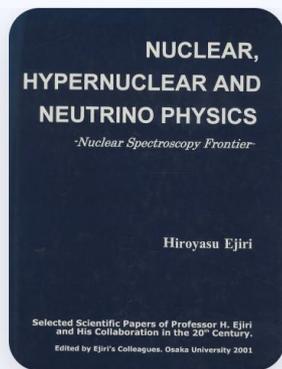
Neutrino Nuclear Physics – Neutrino interactions and double beta decays.

Symmetry and Dark Matter – Fundamental symmetries and their implications for cosmology.

Experimental and theoretical research works were carried out at INSICU Univ. Tokyo, NPL Univ. Washington, NBI Univ. Copenhagen, IBL Univ. California, RCNP Osaka Univ., KEK, Kamioka, JASRI Spring8, IAS Kyoto, ICU and others.

Through these studies, Professor Ejiri has developed **advanced experimental frameworks** and **theoretical frameworks** in nuclear particle spectroscopy, making significant contributions to **nuclear, hypernuclear, and neutrino nuclear physics**.

Books:



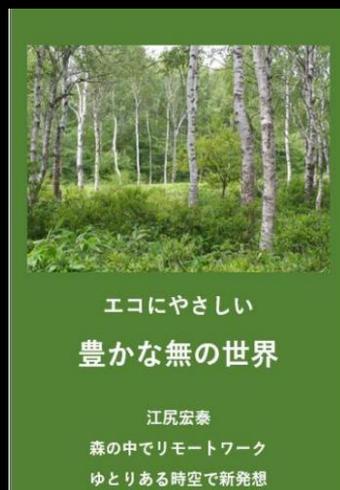
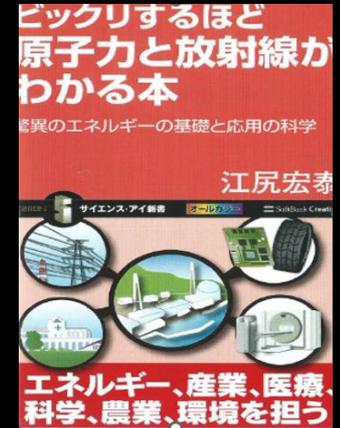
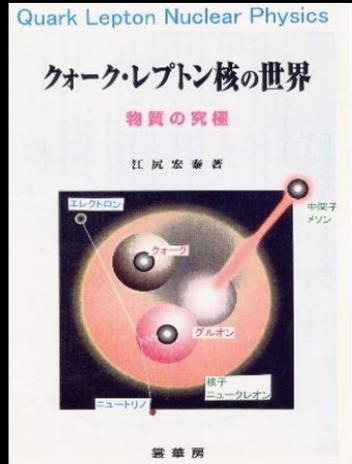
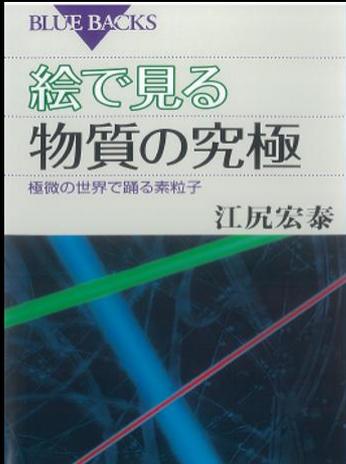
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豊かな無の世界

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ゆとりある時空で新発想

色即是空 空即是色

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Poety of the Sea



海の詩

江尻宏泰

Ocean Light Serenade



潮光
セレナーデ

- 1.潮光
- 2.潮様
- 3.照洋

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Blue Light Sonata



水彩

水映
水彩
湖照
水相
水精

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Flower Fragrance Melody

花香のメロディ



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Rhythmic Light Sonata



彩律

翠の旋律
黄の旋律
緋の旋律
能の雅楽

江尻宏泰

Woods Light Sonata



樹想

梢影
樹様
樹精

江尻宏泰

Flower Light Serenade



花想

セレナーデ

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Emerald Light Sonata



葉彩

葉光
翠風
葉映
照葉

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Solemn Stone Sonata



肅石

肅然
想徳侘

江尻宏泰

Flower Color Cadenza



花彩
カデンツア

江尻宏泰

Thanks for collaborations,

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T. Tsujita, Y. Adachi, N. Kamikubota, M. Fukuda, T. Watanabe,
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A. Higashi, G. Choi, K. Fushimi, T. Ohshima, F. Nakamura, .
K. Nagata, N. Kudomi, K. Kume, N. Shinkai, H. Tazaki, R. Hazama,
R. Hayashi, S. Yoshida, S. Umehara, I. Hashim, and all others**

All the best wishes for your productive own way.

3歩下がらず、向きを変えて 我が道拓く

An aerial photograph of a ship's wake in the ocean. The water is a deep blue, with white foam and churning water forming a large, irregular shape that extends from the top left towards the center. The rest of the water is dark blue with small, rhythmic waves.

**Thank all for joining NEWS/party /contributions.
Thanks in advance for your continued encouragement
Family MEETS Dir. M. Ejiri, Prof. A. Ejiri, and Prof. K. Ejiri**

An aerial photograph of a ship's wake in the ocean. The water is a deep, vibrant blue, and the wake is a complex, white, frothy pattern of foam and bubbles that spreads out from the center. The texture of the water is highly detailed, showing the intricate patterns of the wake. The overall scene is dynamic and energetic.

意次に 素核を究む 日々愉しく