

# Isvector and Isoscalar Spin Isospin Responses

Atsushi Tamii

*Research Center for Nuclear Physics (RCNP)*

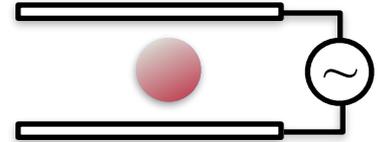
*Osaka University, Japan*

Neutrino Nuclear Responses for Double Beta Decays  
and Astro-Neutrino Interactions (NNR16)

September 29-30, 2016, Osaka

# Outline

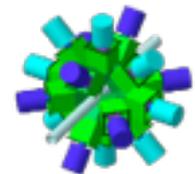
## I. Electric Dipole Response of Nuclei and the Symmetry Energy of the Nuclear EOS



## II. Spin-Magnetic Response of Nuclei

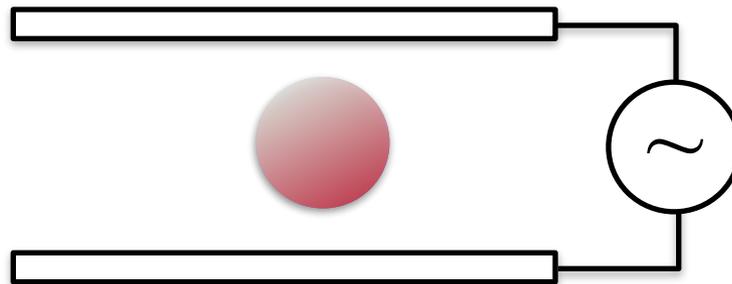


## III. Summary



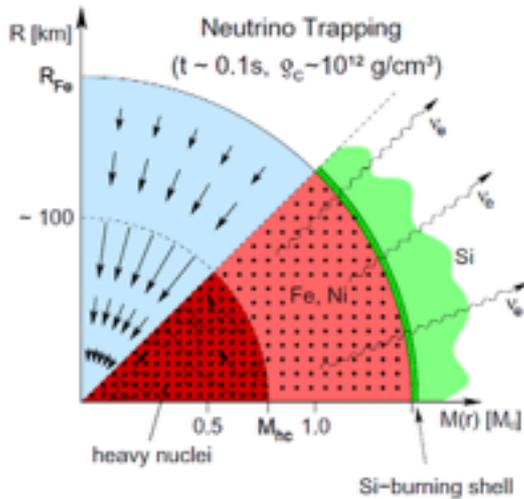
I.

# Electric Dipole Response of Nuclei and the Symmetry Energy of the Nuclear EOS

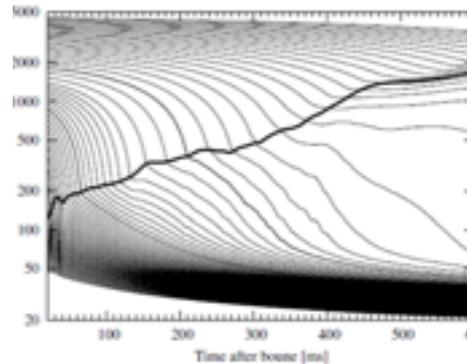


# Symmetry Energy of the Nuclear Equation of State is important for nuclear physics and nuclear-astrophysics

## Core-collapse supernova



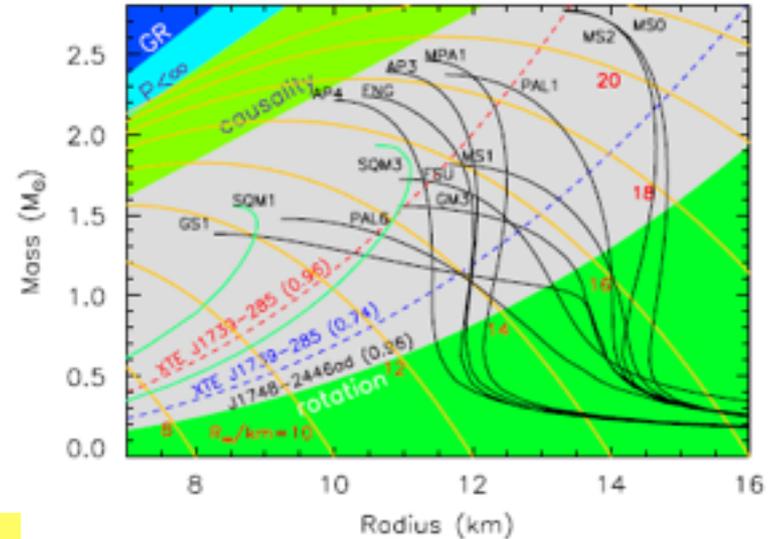
Langanke and Martinez-Pinedo



Y. Suwa et al., ApJ764, 99 (2013).

## Nucleosynthesis

## Neutron star mass vs radius



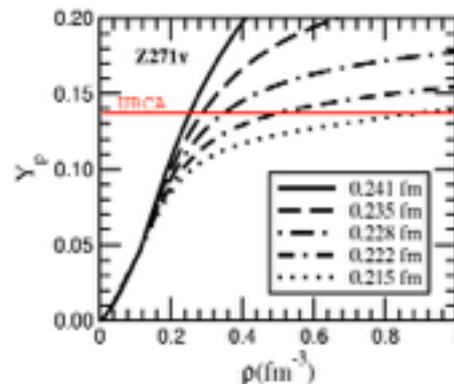
Lattimer et al., Phys. Rep. 442, 109(2007)

## Neutron Star Merger Gravitational Wave



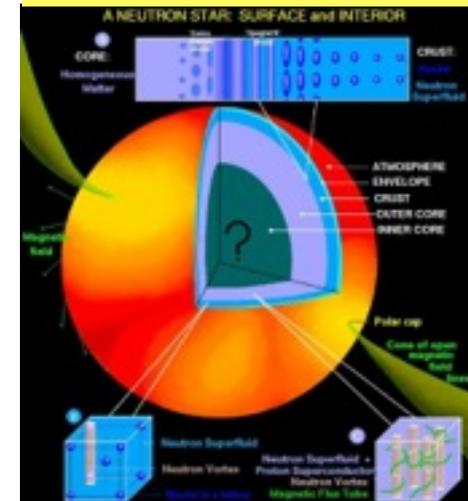
[https://www.youtube.com/watch?v=IZhNWh\\_lFuI](https://www.youtube.com/watch?v=IZhNWh_lFuI)

## Neutron star cooling



Lattimer and Prakash, Science 304, 536 (2004).

## Neutron star structure



<http://www.astro.umd.edu/~miller/nstar.html>

# Nuclear Equation of State

How to study the EOS?

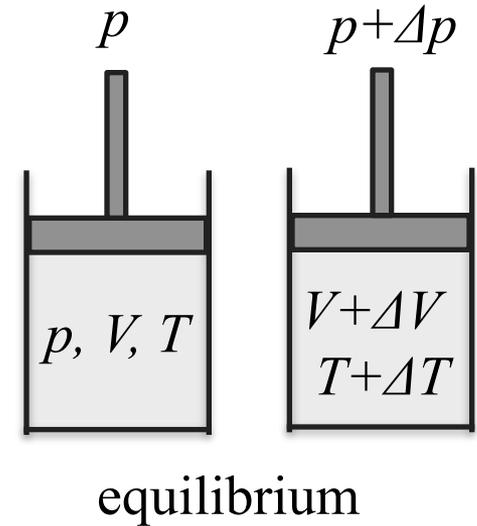
## Thermodynamics

Give a “small perturbation” to the system

then observe how the system changes

→ response

$$\kappa = -\frac{1}{V} \left( \frac{dV}{dp} \right)_S \quad \text{adiabatic compressibility}$$

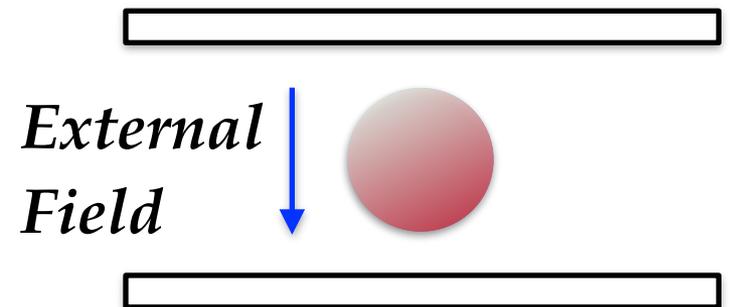


## Nuclear EOS

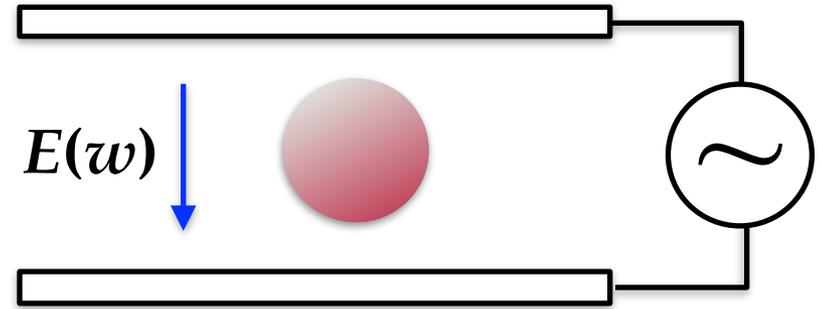
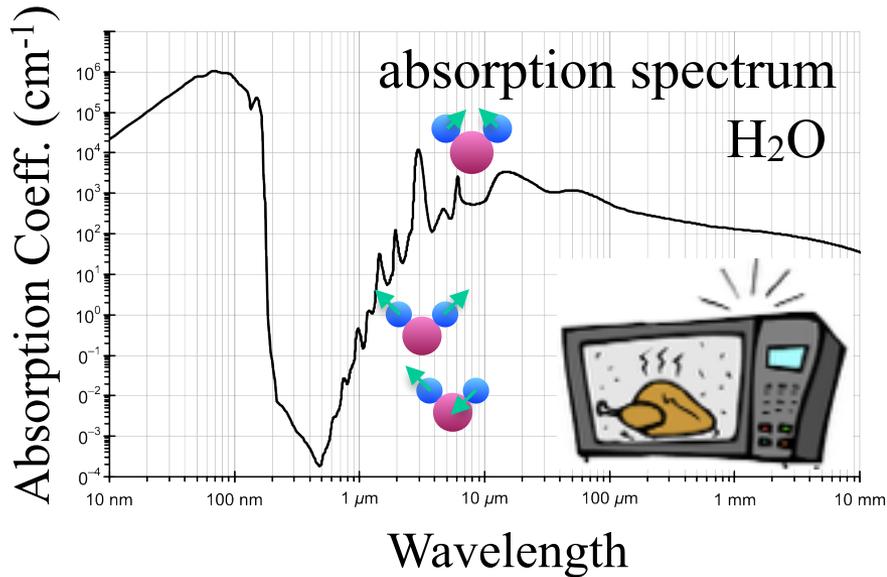
Small perturbation by an external field

Observe how the system change

→ nuclear response



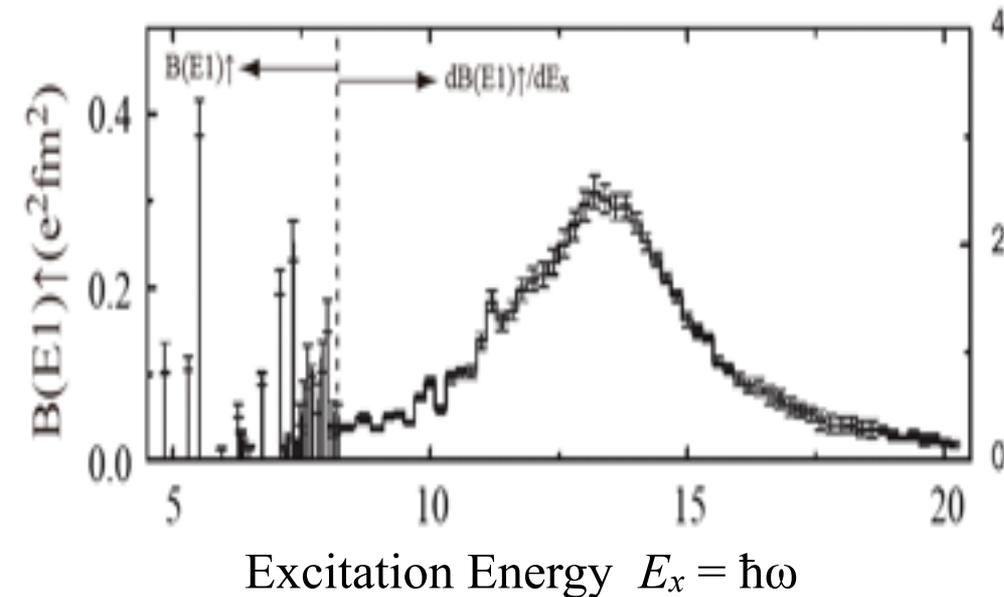
# Electric Dipole Response



dielectric material  
in an oscillating electric field

Electric Dipole (E1)  
Reduced Transition Probability

$$\frac{dB(E1)}{dE_x} = \frac{9\hbar c}{16\pi^3 e^2} \frac{\sigma_{\text{abs}}^{E1}}{E_x}$$

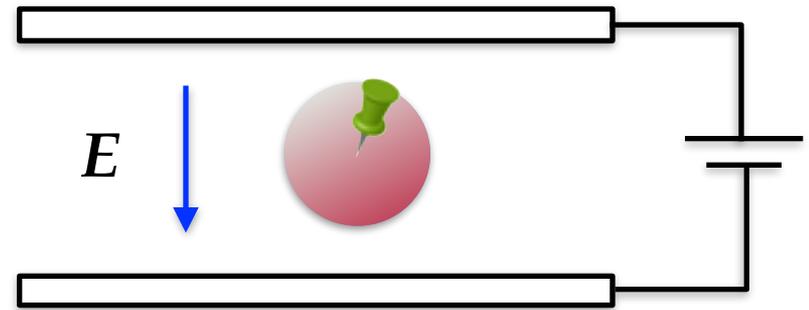


# Electric Dipole Polarizability ( $\alpha_D$ )

Electric dipole moment

$$p = \alpha_D \times E$$

$\alpha_D$ : electric dipole polarizability

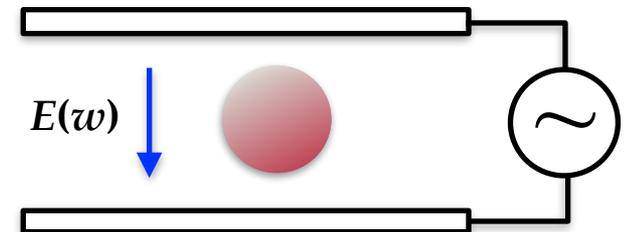


nucleus

in a static electric field  
with fixing the c.m. position

Inversely energy-weighted sum-rule of B(E1)

$$\alpha_D = \frac{8\pi e^2}{9} \int \frac{1}{E_x} \frac{dB(E1)}{E_x}$$



first order perturbation calc. A.B. Migdal: 1944

# Electric Dipole Polarizability ( $\alpha_D$ )

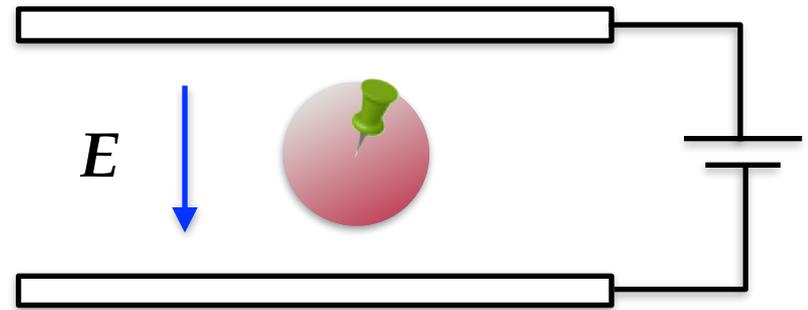
Electric dipole moment

$$p = \alpha_D \times E$$

$\alpha_D$ : electric dipole polarizability



The **restoring force** originates from the **symmetry energy**.

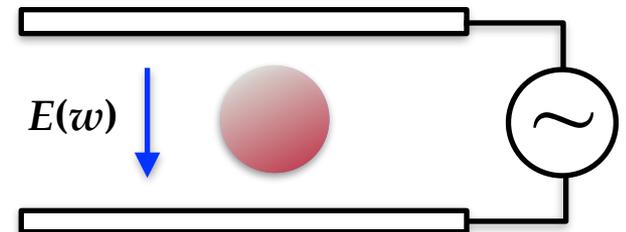


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Inversely energy-weighted sum-rule of B(E1)

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first order perturbation calc. A.B. Migdal: 1944

# Nuclear Equation of State (EOS) at zero temperature

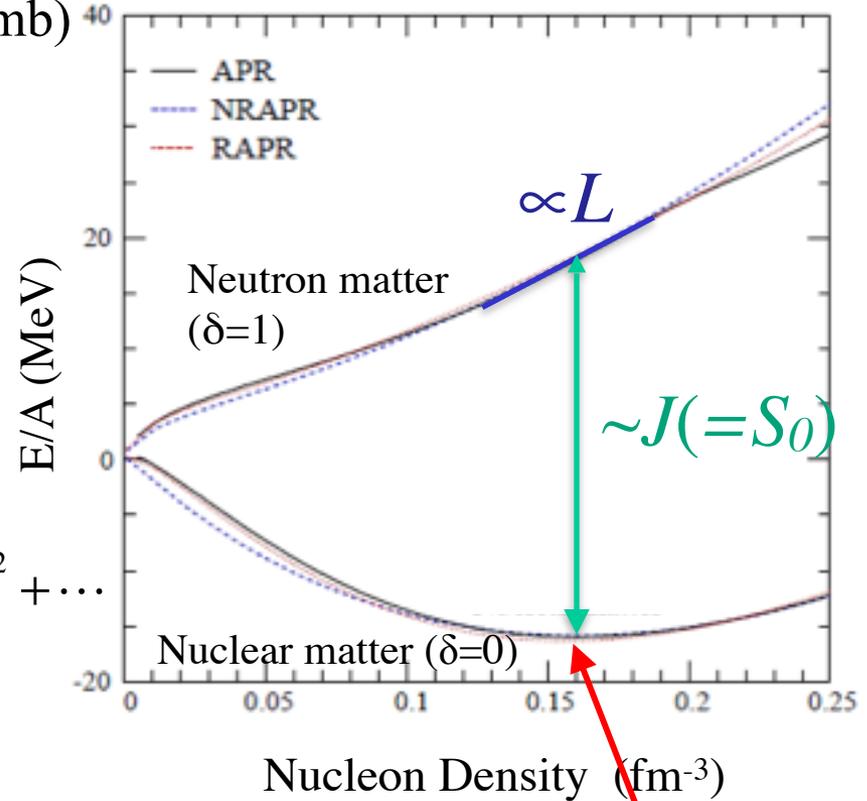
Nuclear equation of state (neglecting Coulomb)

$$\frac{E}{A}(\rho, \delta) = \frac{E}{A}(\rho, 0) + S(\rho)\delta^2 + \dots$$

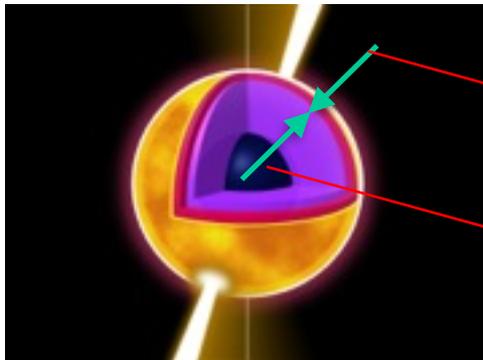
$$\delta(r) \equiv \frac{\rho_n(r) - \rho_p(r)}{\rho_n(r) + \rho_p(r)}$$

Symmetry energy

$$S(\rho) = J + \frac{L}{3\rho_0}(\rho - \rho_0) + \frac{K_{sym}}{18\rho_0^2}(\rho - \rho_0)^2 + \dots$$



Neutron Star



gravitational pressure

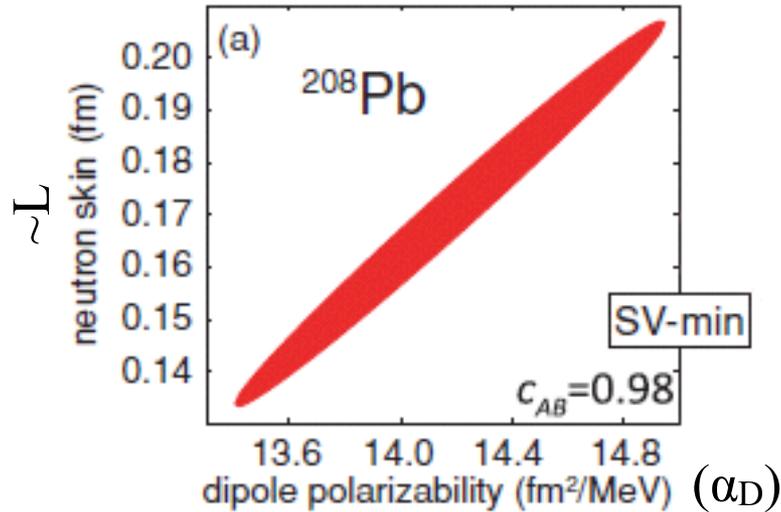
baryonic pressure  $\propto L$

$\propto R_{nstar}^4$  Lattimer&Prakash, PRep442, 109(2007)

Saturation Density  $\rho_0$

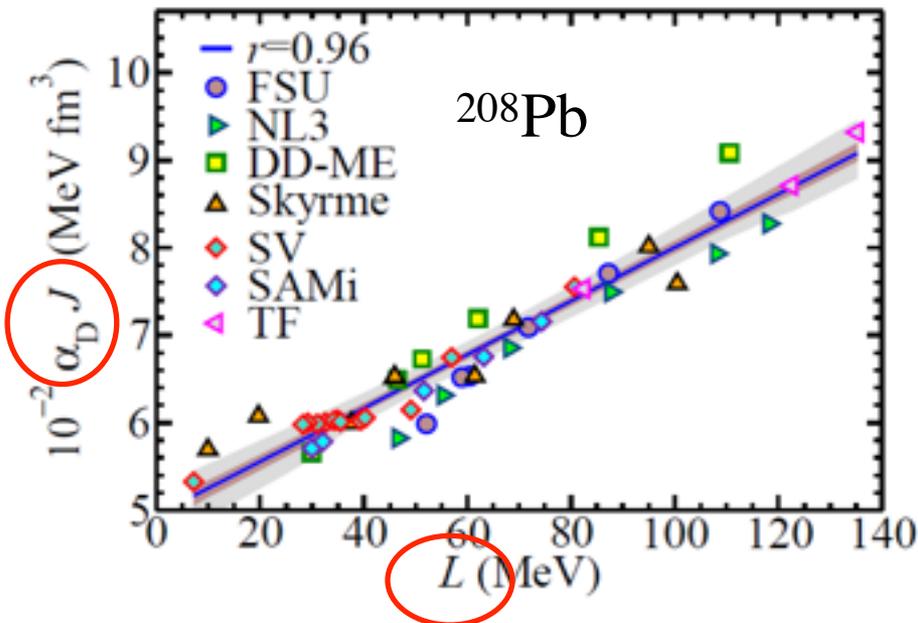
$\rho_0 \sim 0.16 \text{ fm}^{-3}$

# Theoretical Models to Connect $\alpha_D$ to the Symmetry Energy



P.-G. Reinhard and W. Nazarewicz,  
PRC 81, 051303(R) (2010).

Energy Density Functional (EDF) approach  
using the  $SV_{\text{min}}$  effective interaction.

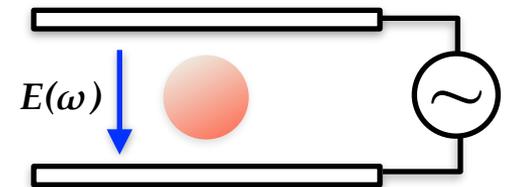
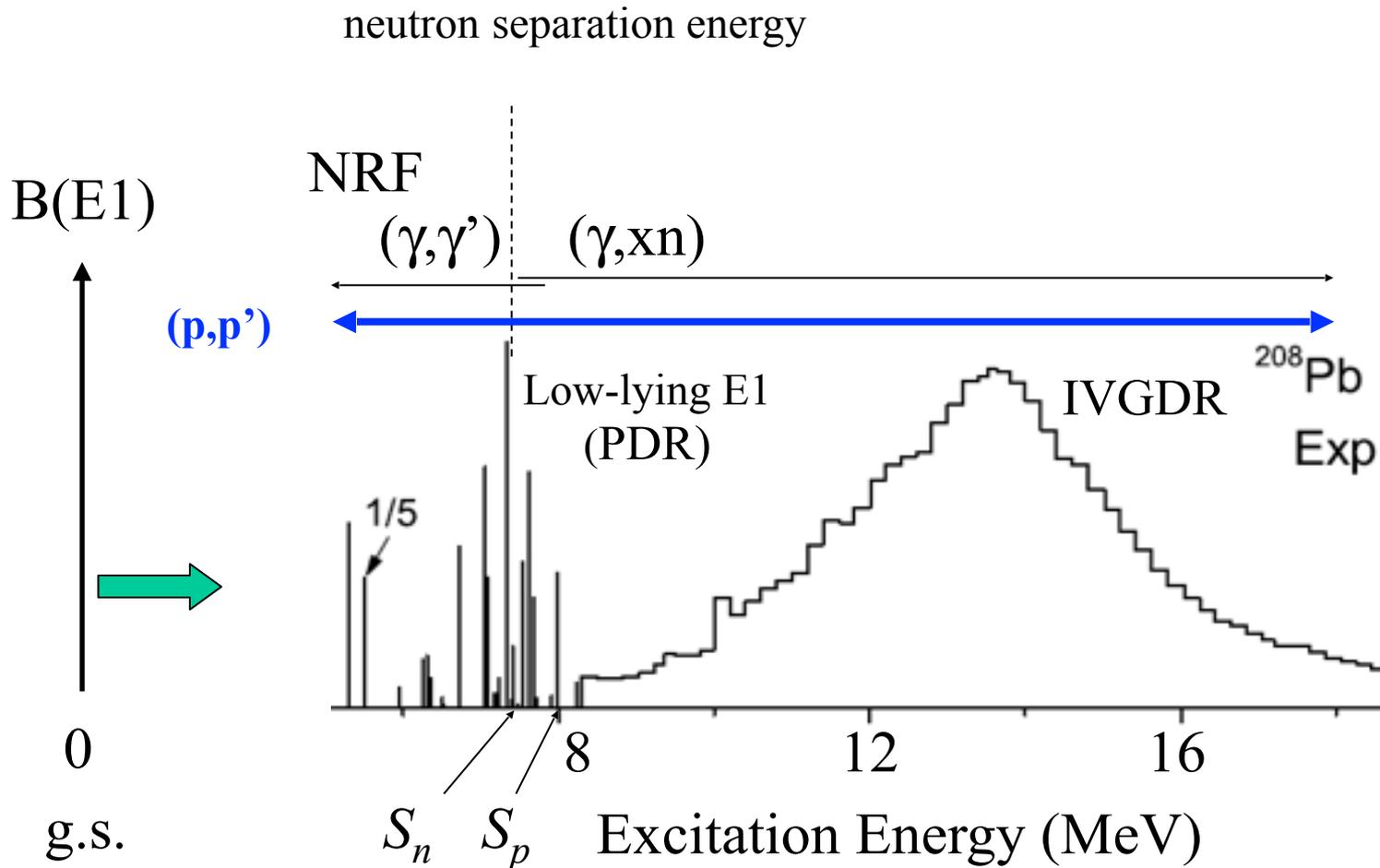


X. Roca-Maza *et al.*, PRC88, 024316(2013)

$$S(\rho) = J + \frac{L}{3\rho_0}(\rho - \rho_0) + \dots$$

Precise determination of  $\alpha_D$  of  $^{208}\text{Pb}$  gives a  
constraint band in the J-L plane.

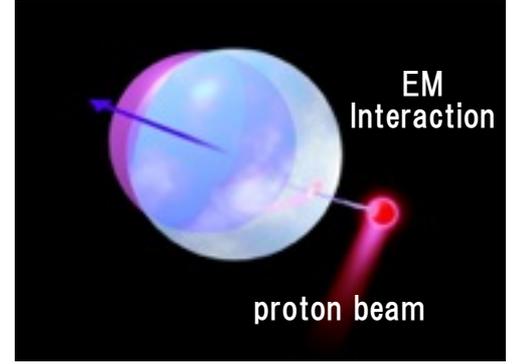
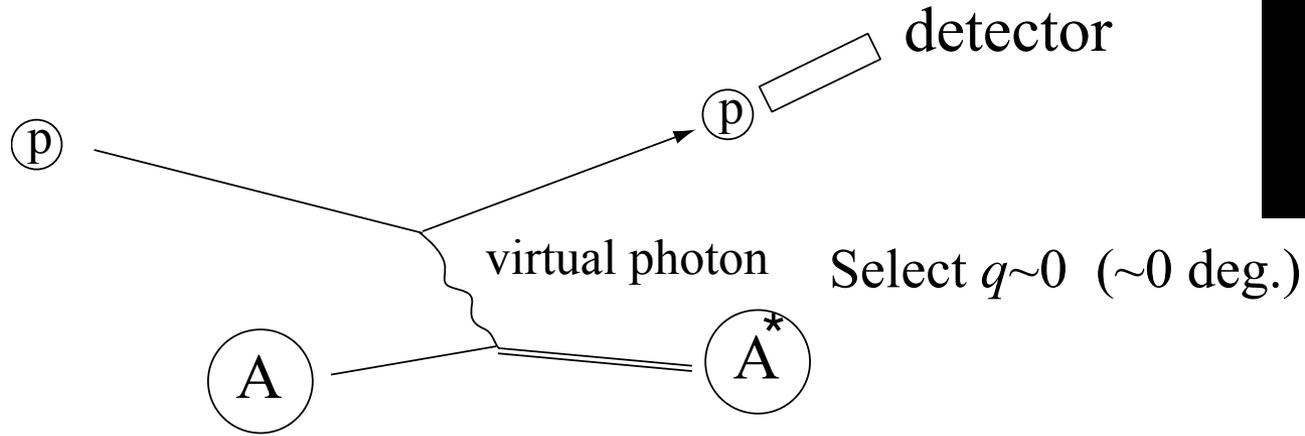
# Electric Dipole ( $E1$ ) Response of Nuclei



# Coulomb Excitation by Proton Scattering

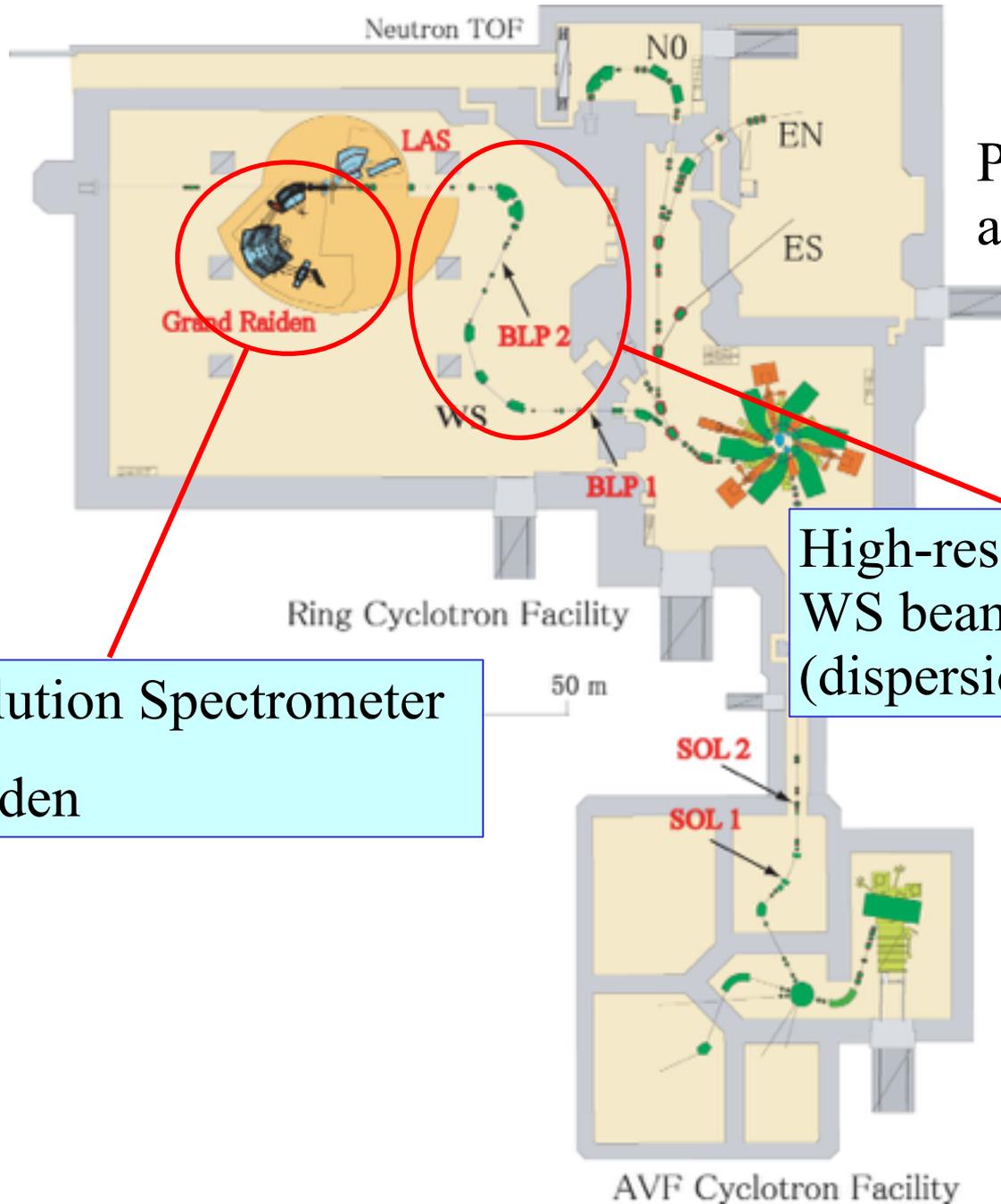


## Missing Mass Spectroscopy by Virtual Photon Excitation



- **Missing mass spectroscopy:**  
Total strength is measured independently of the decay channels.
- **Electromagnetic Probe:** the interaction is well known
- **Single shot measurement** across  $S_n$  in  $E_x = 5-22$  MeV.
- **High energy resolution** (20-30 keV)
- **Spin observable & angular distribution** → extraction of E1

# Research Center for Nuclear Physics (RCNP), Osaka University



Polarized  $p$  beam  
at 295 MeV

High-resolution Spectrometer  
Grand Raiden

High-resolution  
WS beam-line  
(dispersion matching)

AVF Cyclotron Facility

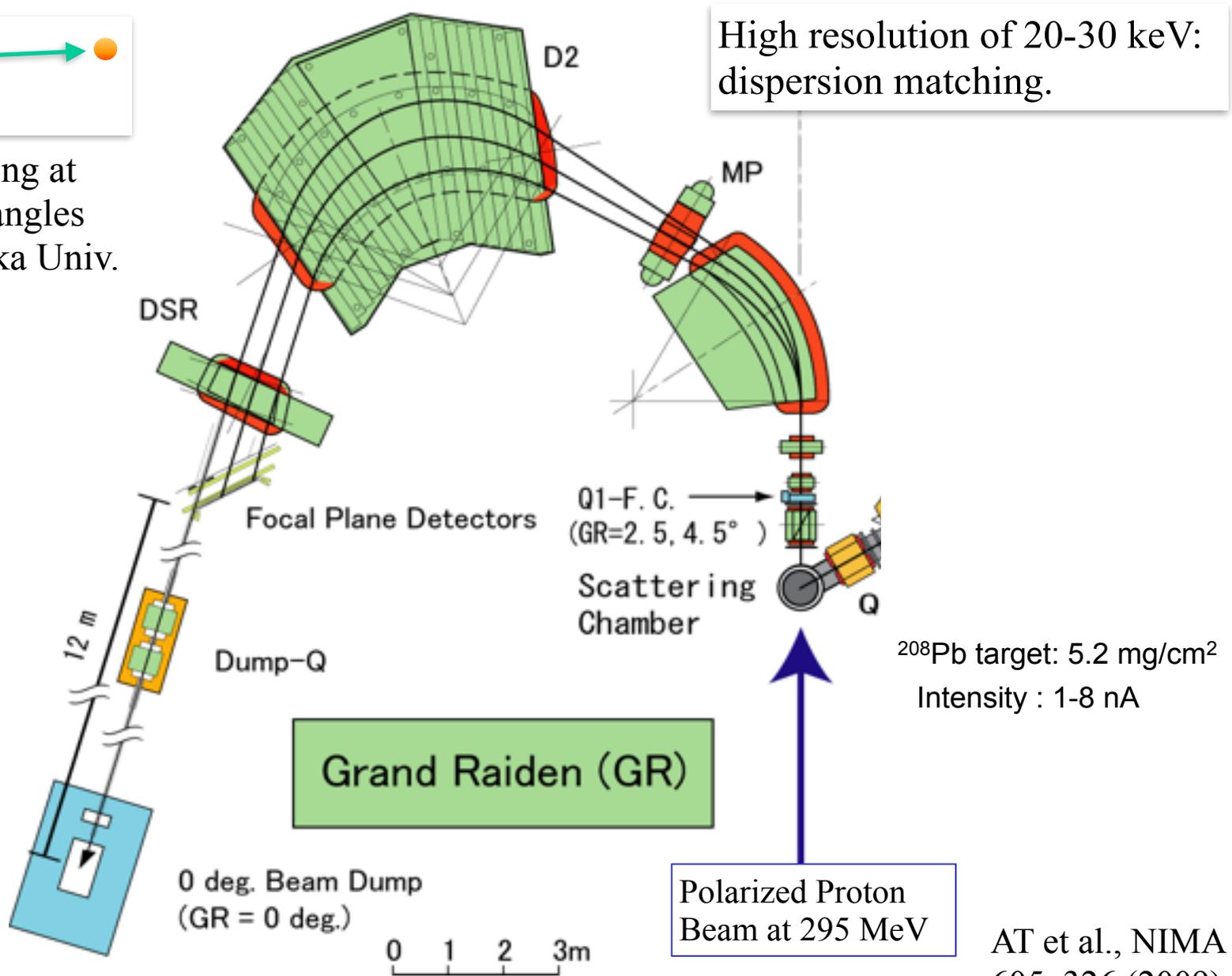


RCNP

# Missing mass spectroscopy by Coulomb Excitation



Proton scattering at very forward angles at RCNP, Osaka Univ.



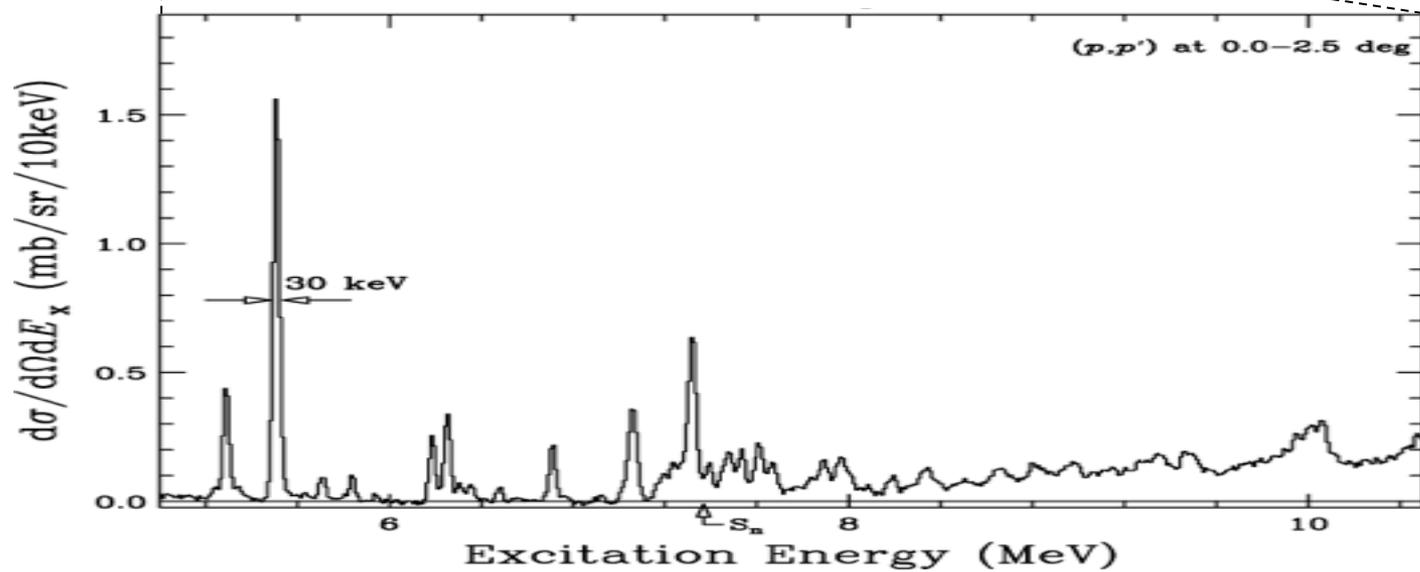
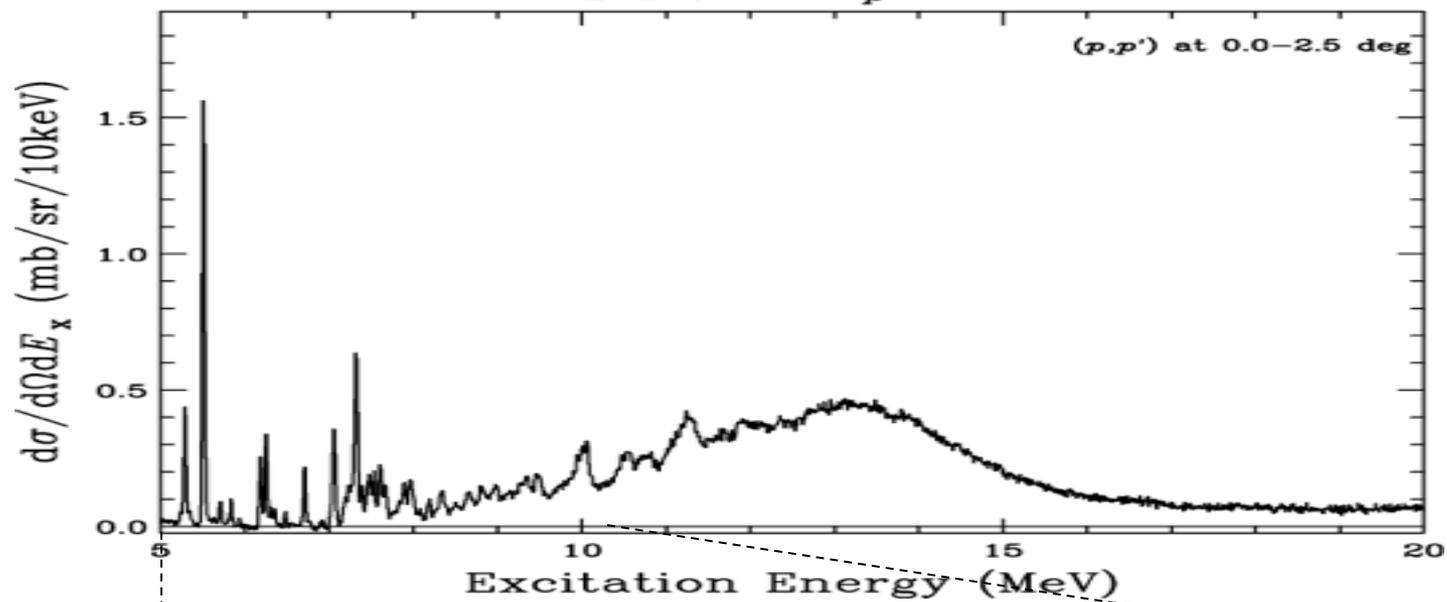
High resolution of 20-30 keV: dispersion matching.

$^{208}\text{Pb}$  target: 5.2 mg/cm<sup>2</sup>  
Intensity : 1-8 nA

Polarized Proton Beam at 295 MeV

AT et al., NIMA 605, 326 (2009)

$^{208}\text{Pb}(p,p')$  at  $E_p=295$  MeV



# B(E1): continuum and GDR region

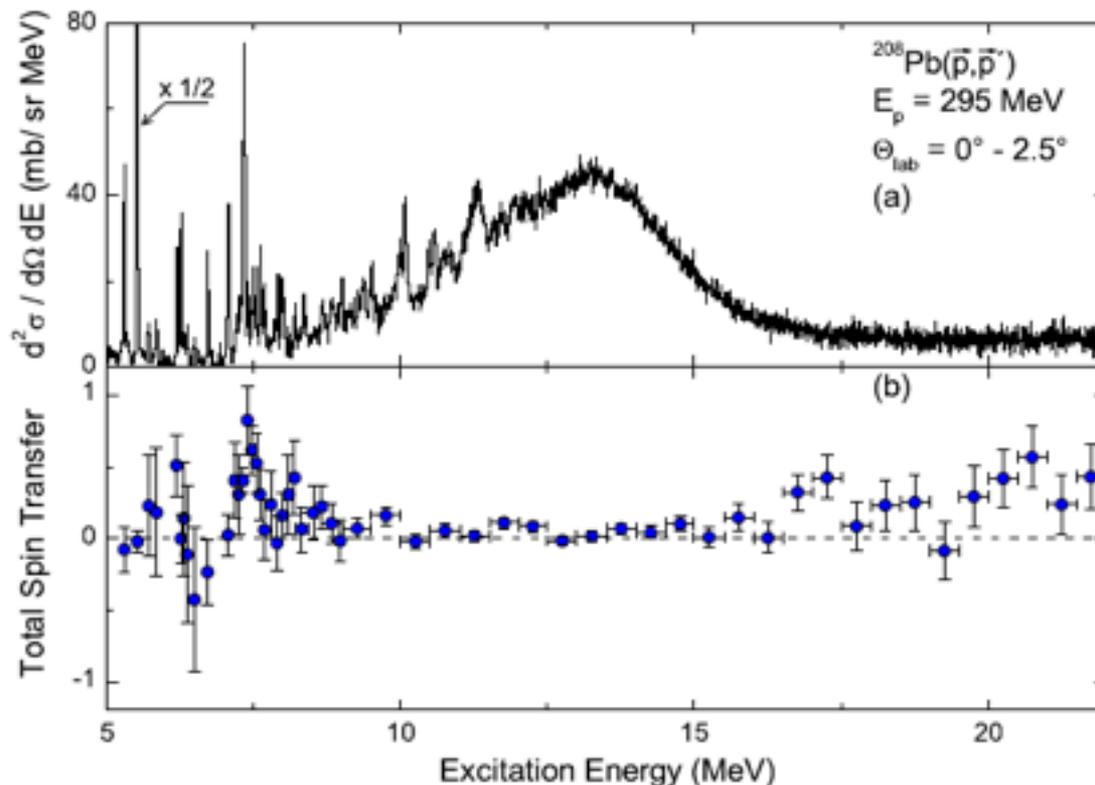
## Method 2: Decomposition by Spin Observables

● Polarization observables at  $0^\circ$   $\rightarrow$  **spinflip / non-spinflip separation**  
model-independent

E1 / spin-M1 decomposition

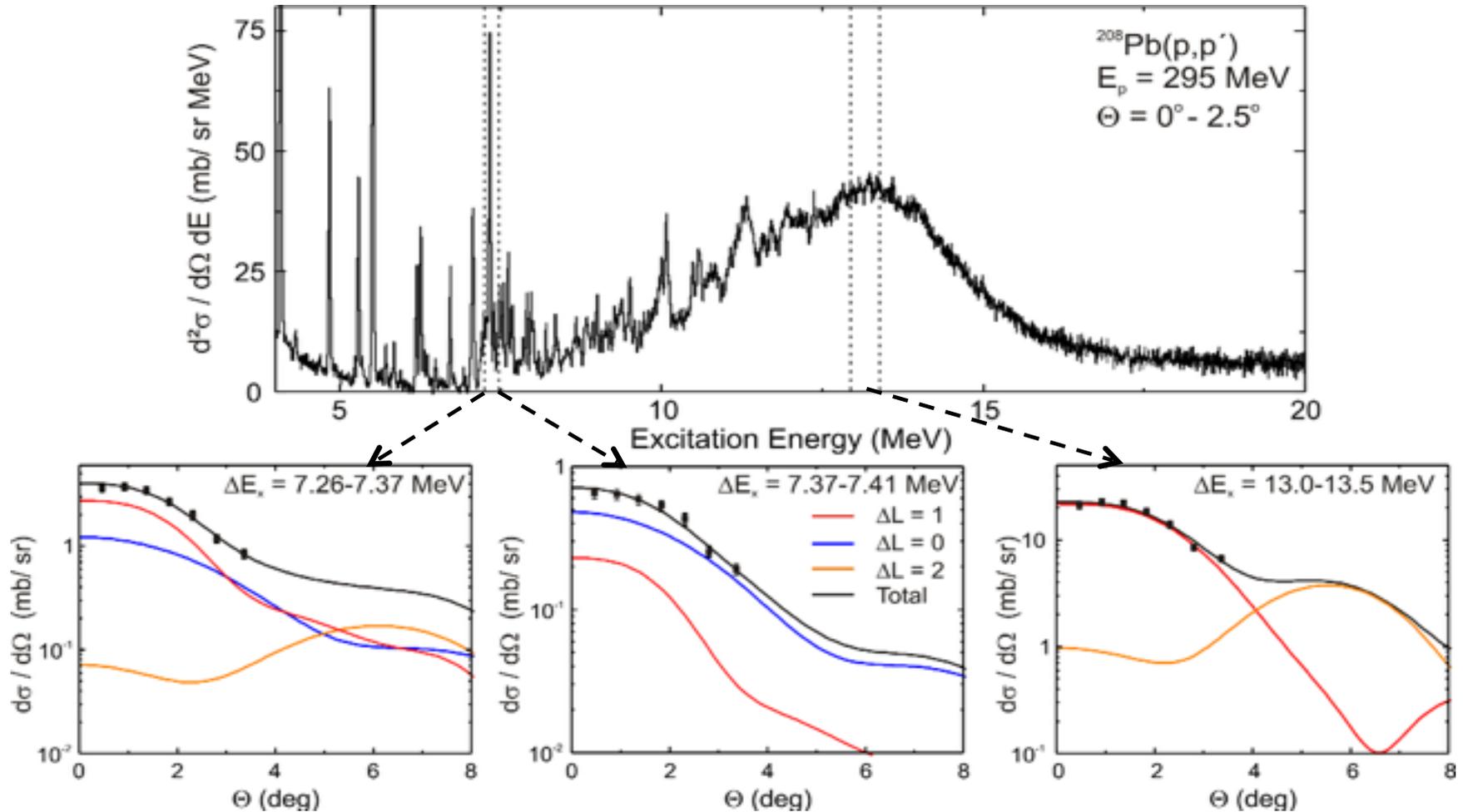
T. Suzuki, PTP 103 (2000) 859

$$\text{Total Spin Transfer } \Sigma \equiv \frac{3 - (2D_{SS} + D_{LL})}{4} = \begin{cases} 1 & \text{for } \Delta S = 1 \quad \text{spin-M1} \\ 0 & \text{for } \Delta S = 0 \quad \text{E1} \end{cases}$$



# B(E1): continuum and GDR region

## Method 1: Multipole Decomposition

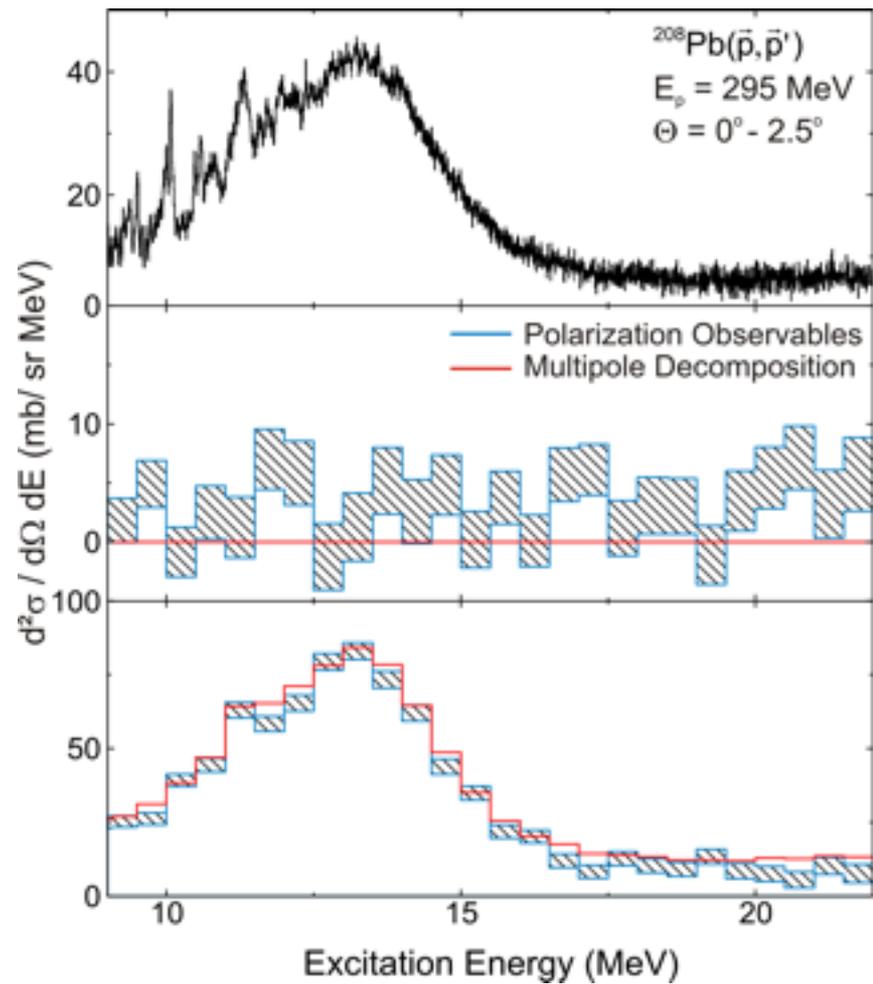
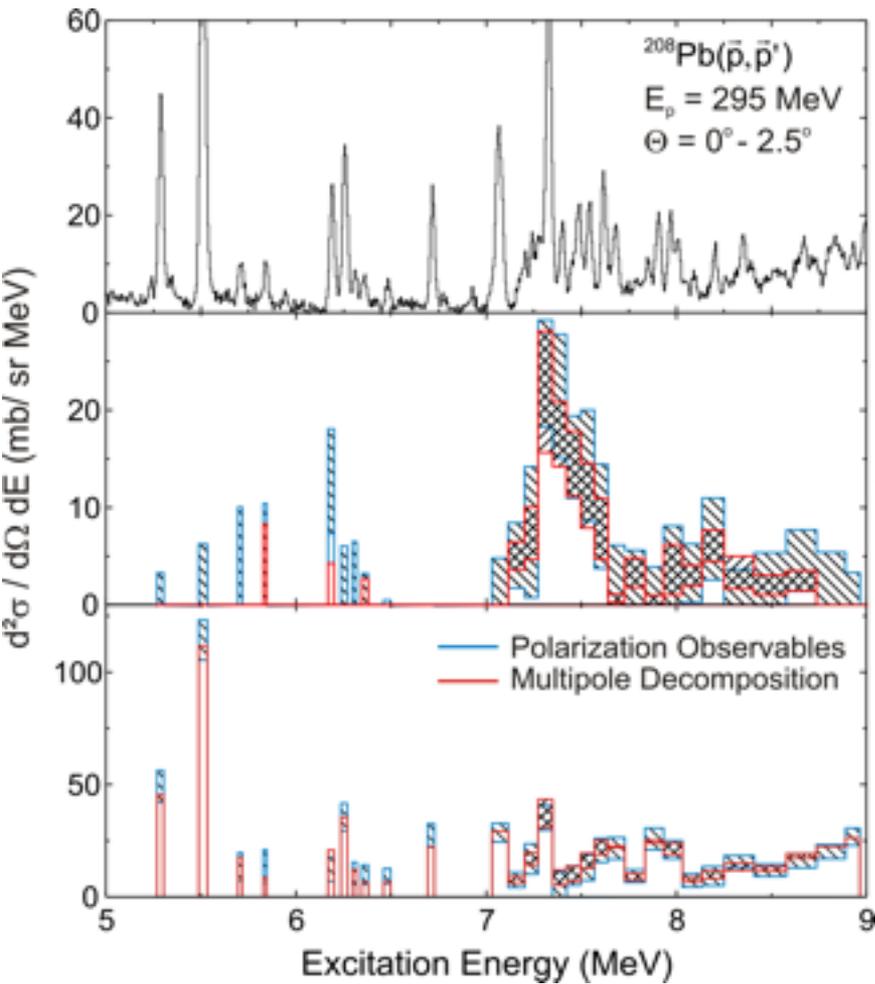


● Neglect of data for  $\Theta > 4$ : (p,p') response too complex

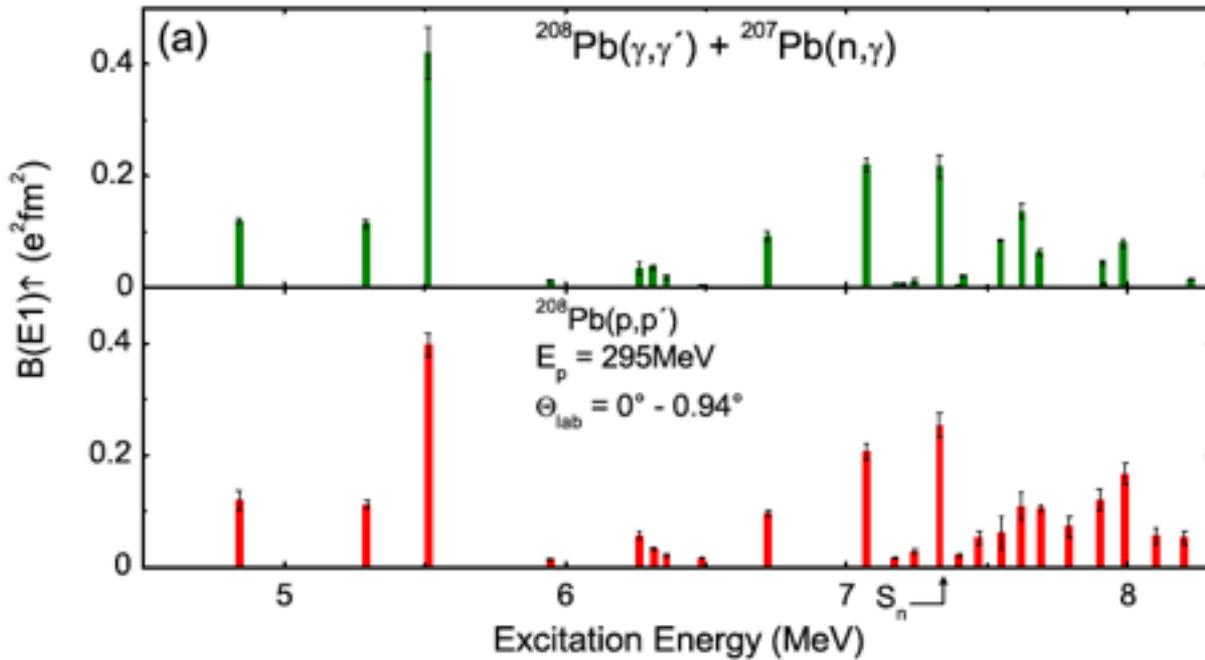
● Included E1/M1/E2 or E1/M1/E3 (little difference)

Grazing Angle = 3.0 deg

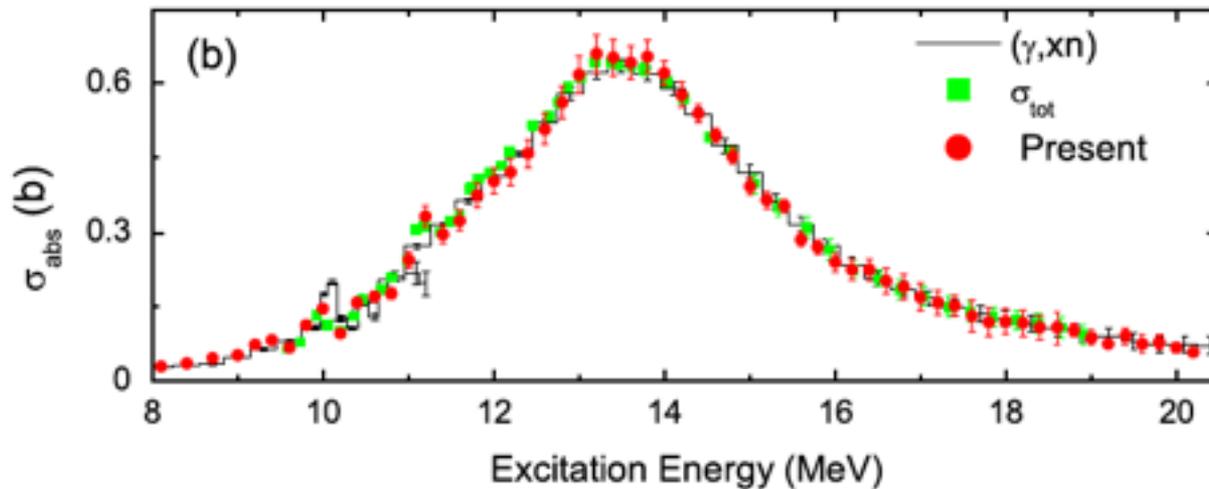
# Comparison between the two methods for the decomposition of E1 and spin-M1



# Comparison with $(\gamma,\gamma')$ and $(\gamma,xn)$

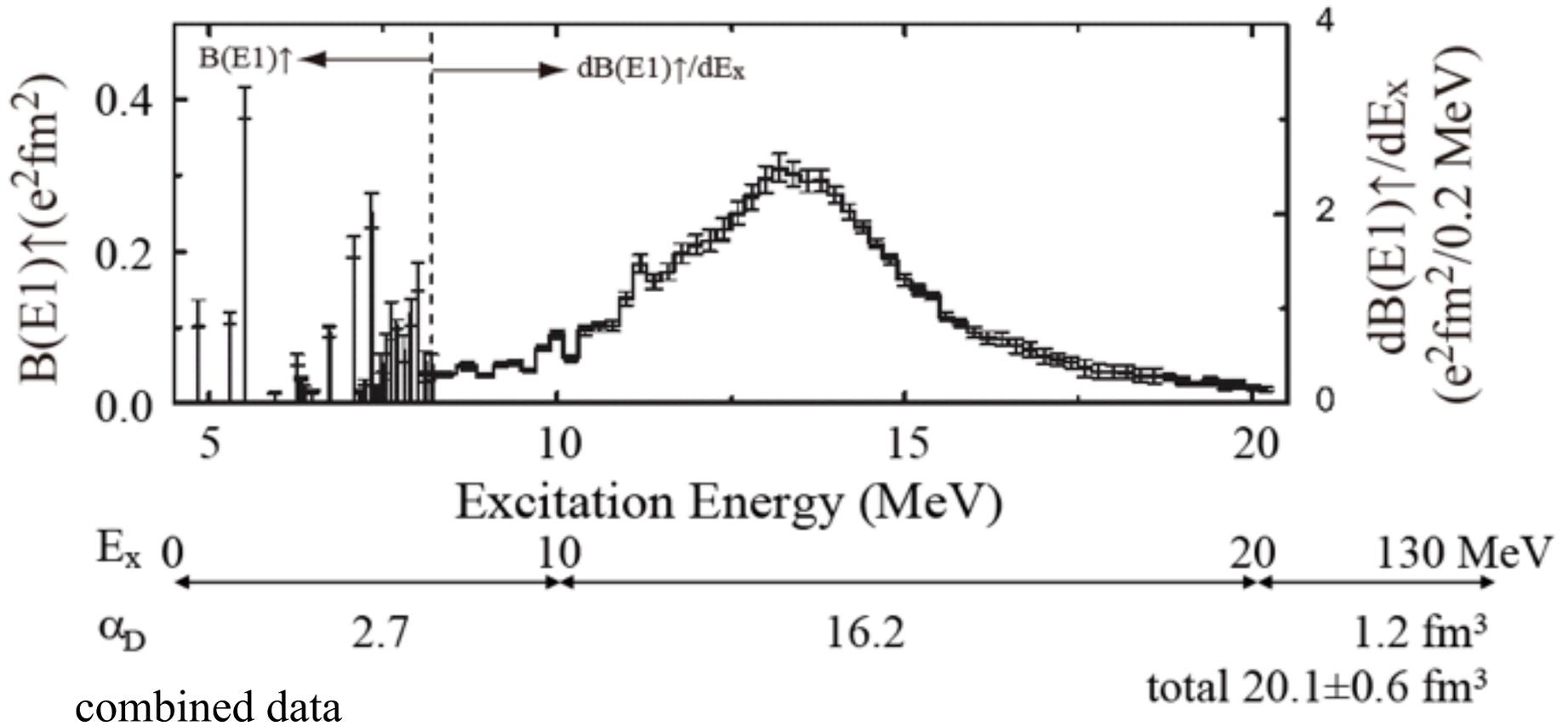


low-lying  
discrete states

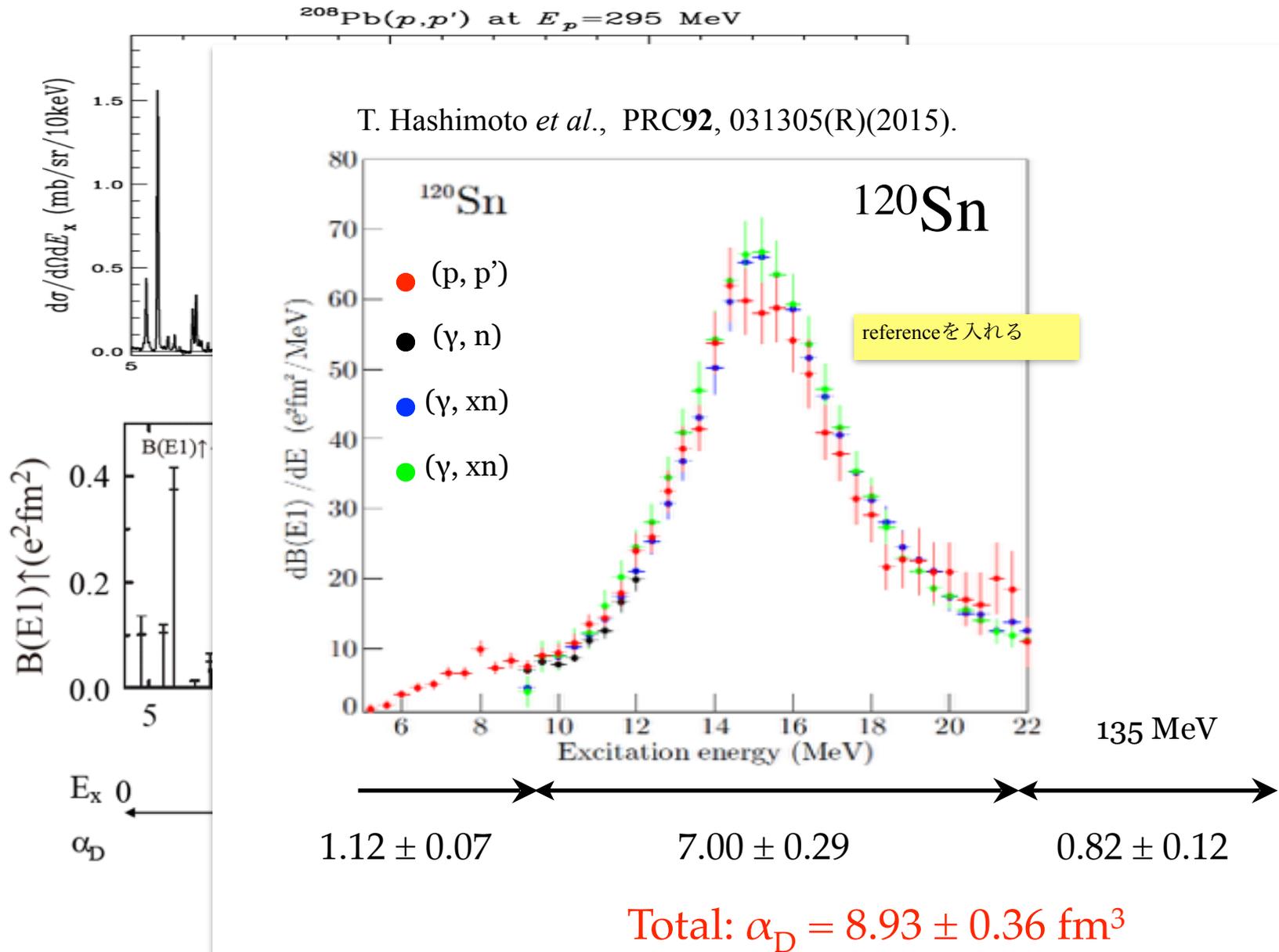


GDR region

# E1 Response of $^{208}\text{Pb}$ and $\alpha_D$

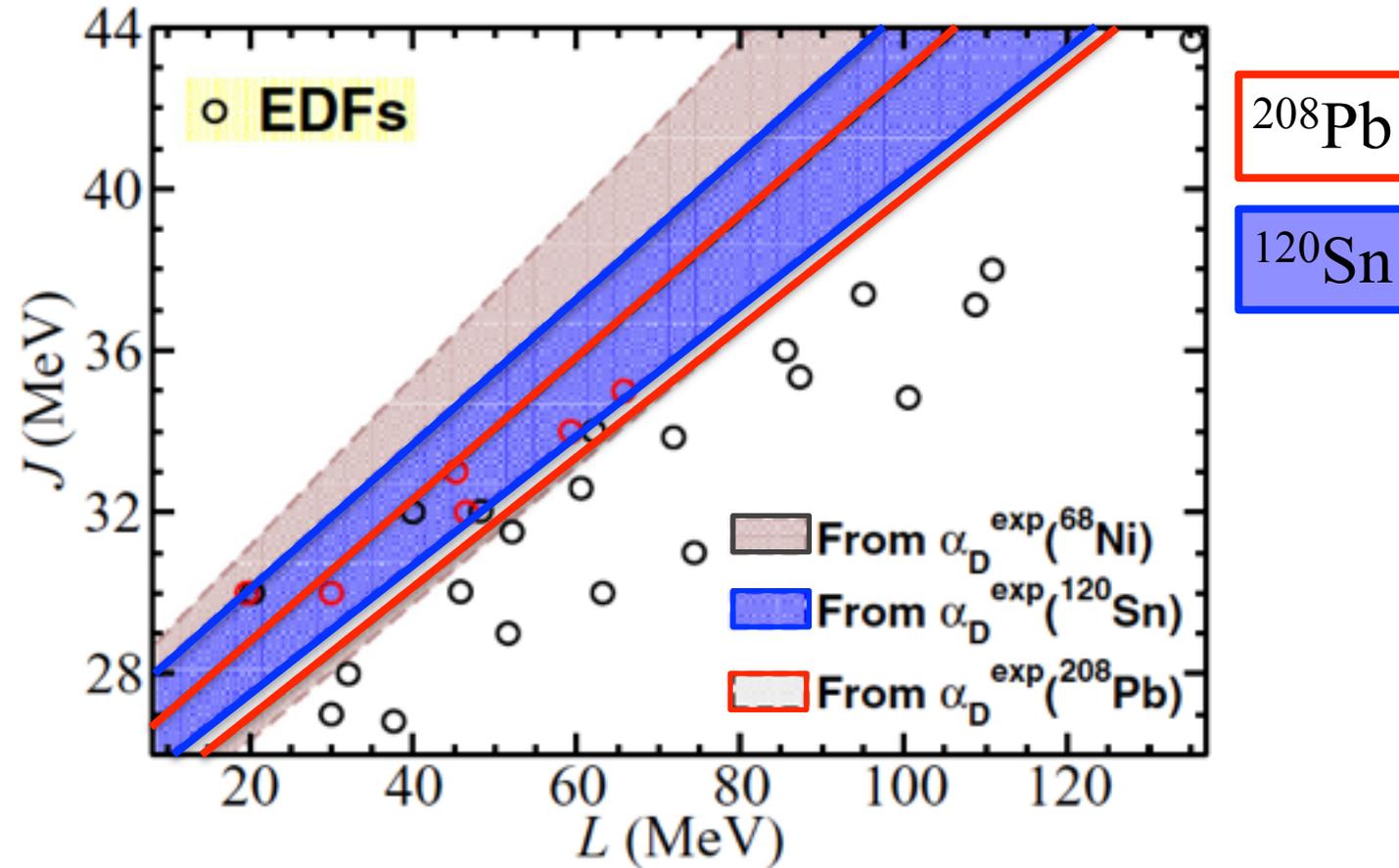


The full dipole response of  $^{208}\text{Pb}$  has been determined.



# Constraints on J-L and the n-skin thickness

X. Roca-Maza et al., PRC92, 064304(2015)

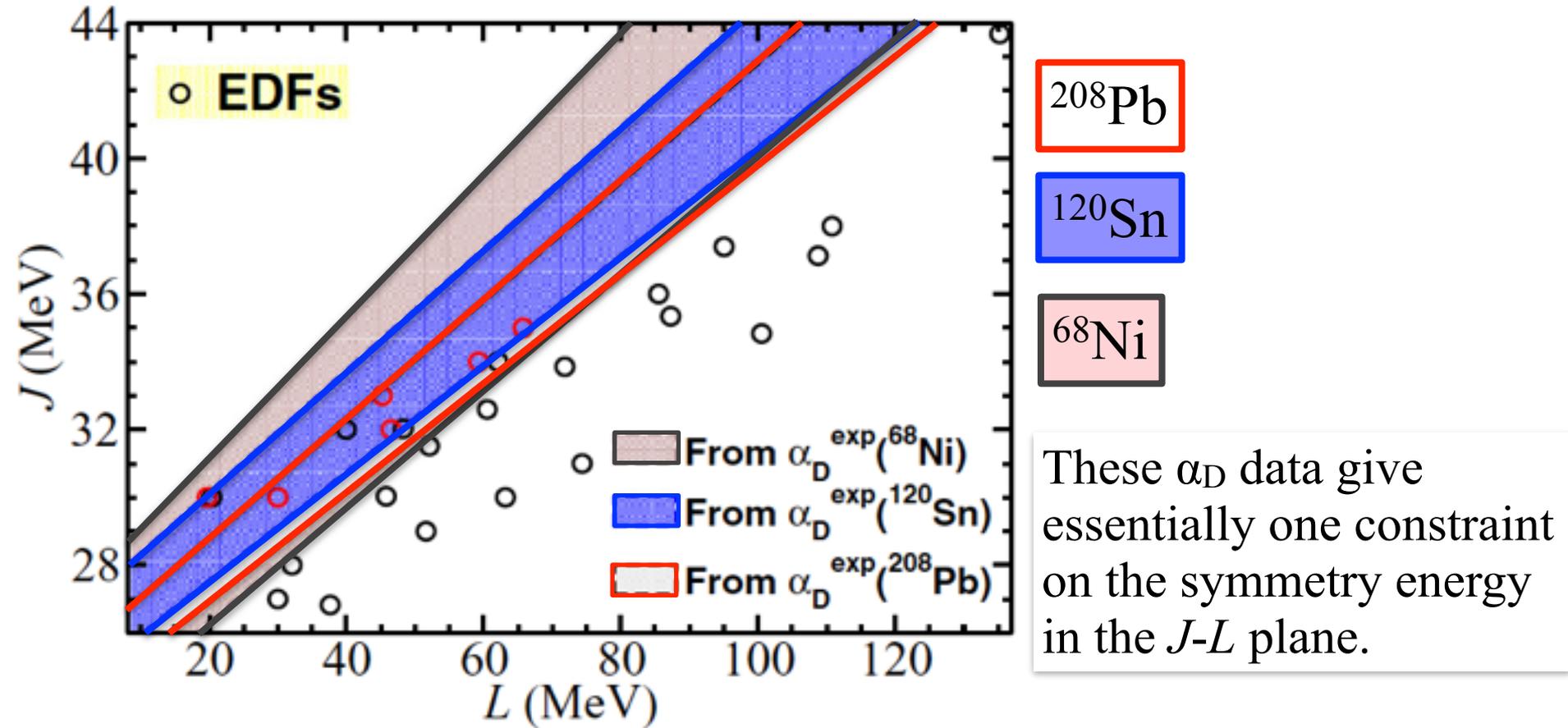


**RCNP**  $^{208}\text{Pb}$ : AT *et al.*, PRL107, 062502 (2011).

**RCNP**  $^{120}\text{Sn}$ : T. Hashimoto *et al.*, PRC92, 031305(R)(2015).

# Constraints on $J$ - $L$ and the $n$ -skin thickness

X. Roca-Maza et al., PRC92, 064304(2015)

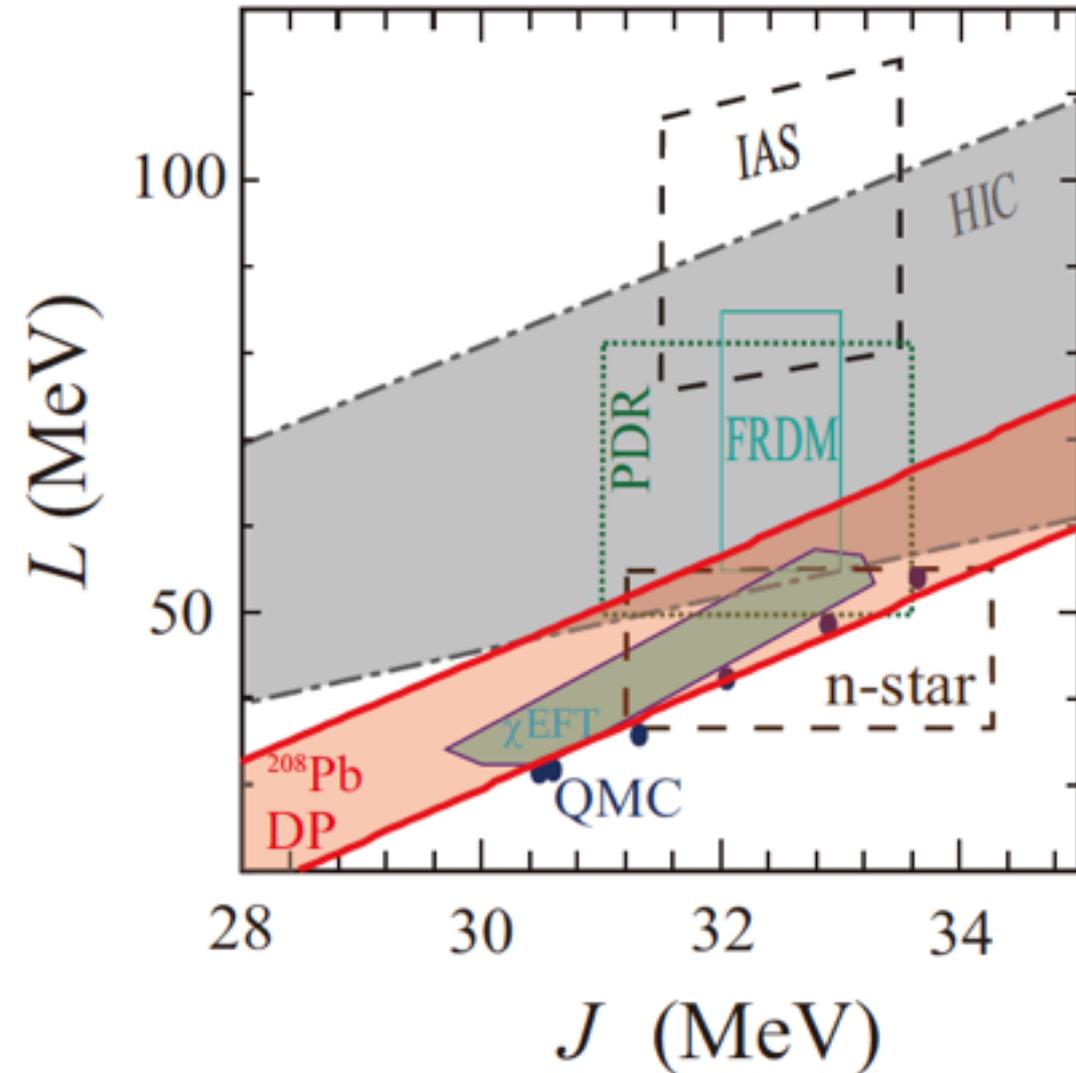


**RCNP**  $^{208}\text{Pb}$ : AT *et al.*, PRL107, 062502 (2011).

**RCNP**  $^{120}\text{Sn}$ : T. Hashimoto *et al.*, PRC92, 031305(R)(2015).

**GSI**  $^{68}\text{Ni}$ : D.M. Rossi *et al.*, PRL111, 242503 (2013).

# Constraints on $J$ and $L$



AT et al., EPJA**50**, 28 (2014).

M.B. Tsang *et al.*, PRC**86**, 015803 (2012)

C.J. Horowitz et al., JPG**41**, 093001 (2014)

DP: Dipole Polarizability

HIC: Heavy Ion Collision

PDR: Pygmy Dipole Resonance

IAS: Isobaric Analogue State

FRDM: Finite Range Droplet

Model (nuclear mass analysis)

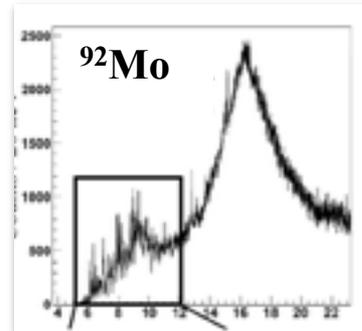
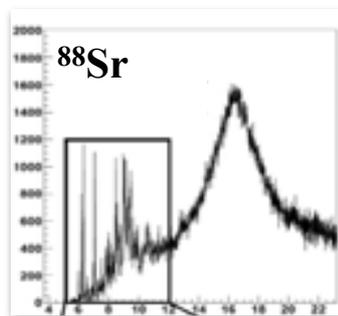
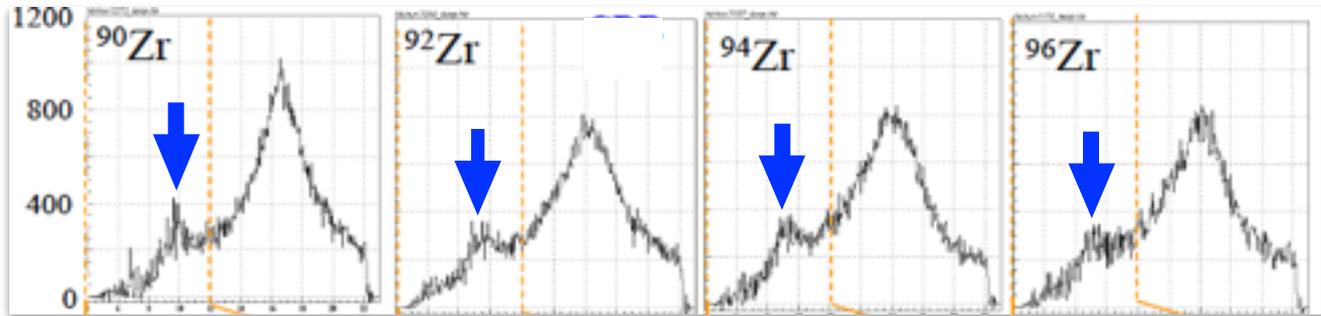
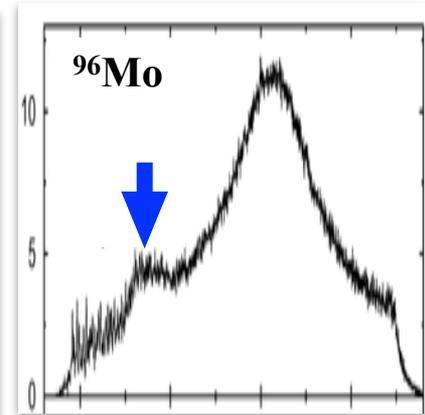
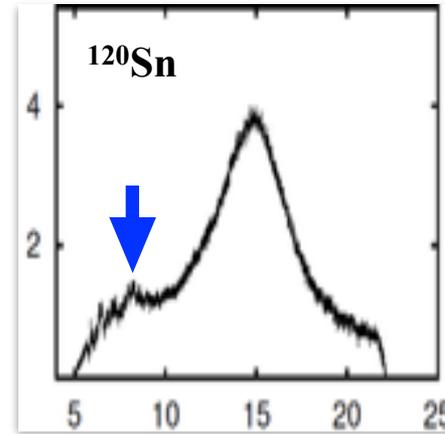
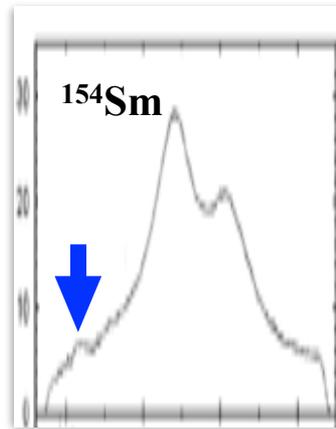
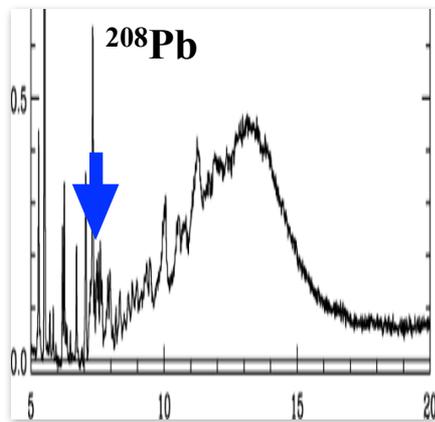
n-star: Neutron Star Observation

$\chi$ EFT: Chiral Effective Field Theory

QMC: S. Gandolfi, EPJA**50**, 10(2014).

I. Tews et al., PRL**110**, 032504 (2013)

# Universal Existence of PDR in Nuclei with $A > \sim 90$ ?

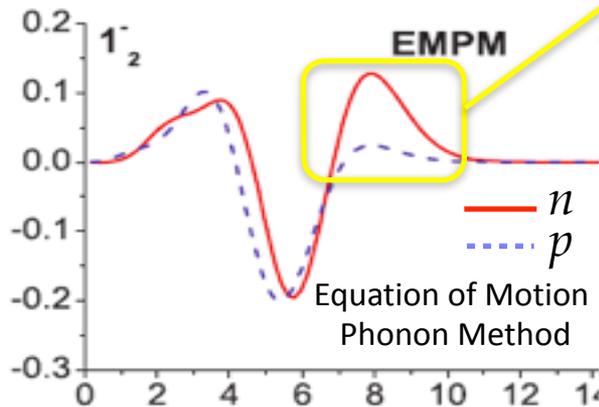


There must be a common reason of the existence.

# Excess Neutron Oscillation of the PDR

Theoretical predictions of the transition densities.

$^{208}\text{Pb}$   
**PDR**  
**region**



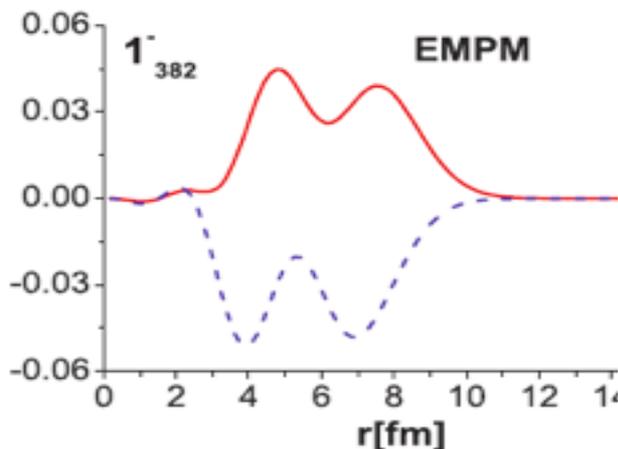
Dipole oscillation of the excess neutron on surface against the isospin saturated core?

In both the IS and IV response

Signature of the neutron excess oscillation

- surface sensitivity
- IS excitation
- characteristic  $q$ -dependence

**GDR**  
**region**



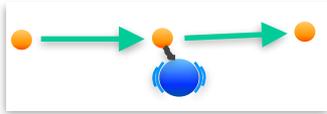
Out of phase  $n$ - $p$  oscillation

Only in the IS response

# Experimental hints on the structure of the PDR

- Universal existence for nuclei with  $A \sim 90$ ?
  - Splitting of the PDR strengths  $(\alpha, \alpha') \Leftrightarrow (\gamma, \gamma')$
  - Large cross section for surface sensitive probes
  - Different angular distribution in  $(p, p')$  at forward angle?
  - Splitting of PDR in deformed nuclei?
  - Larger strength (in TRK) in neutron rich nuclei
-

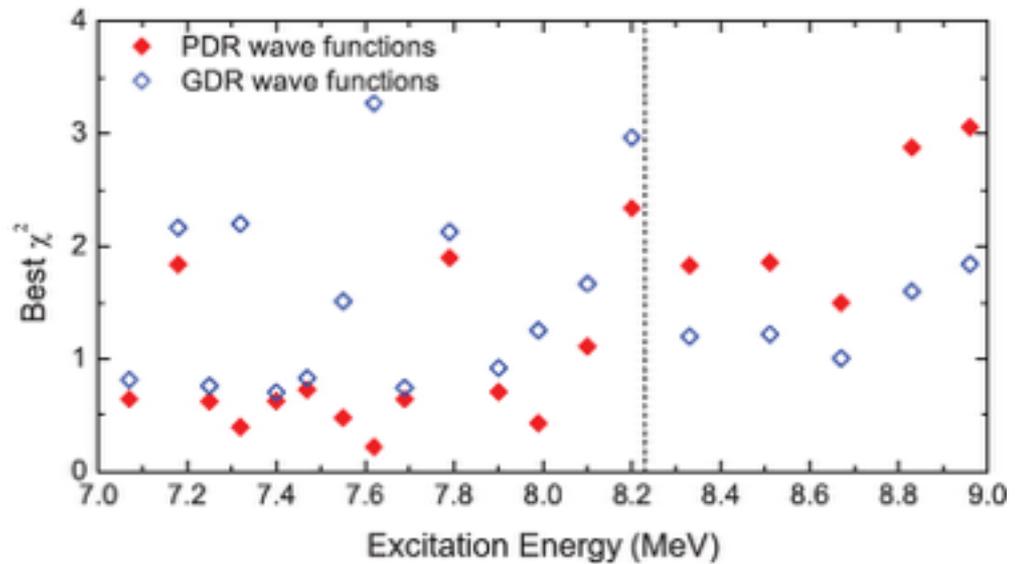
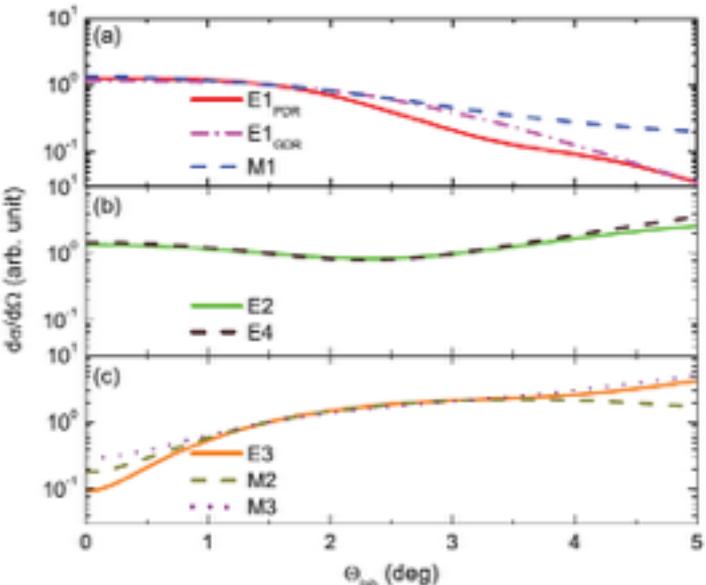
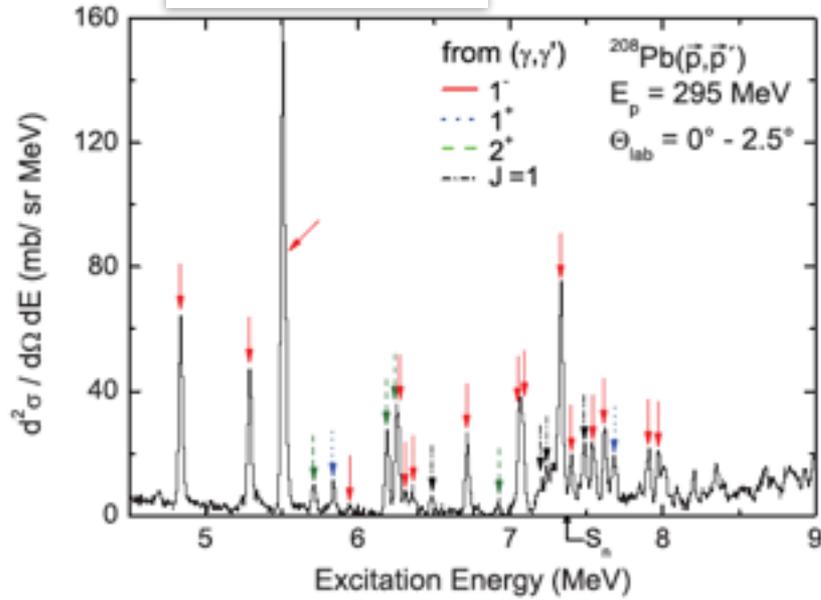
# MDA of the E1 excitations



Proton scattering

$^{208}\text{Pb}$

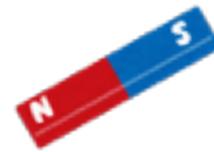
I. Poltoratska et al., PRC85, 041304 (2012)



## II. Spin Magnetic Response of Nuclei



# Spin Susceptibility

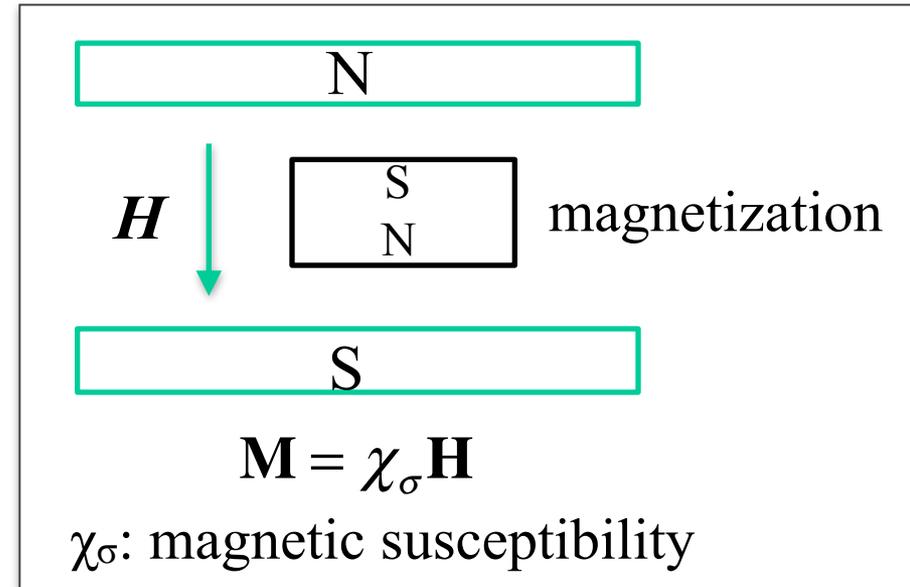


Magnetic dipole ( $M1$ ) operator

$$O(M1) = g_\ell^{\text{IS}} \ell + \underline{g_s^{\text{IS}} \sigma} + g_\ell^{\text{IV}} \ell \cdot \tau + \underline{g_s^{\text{IV}} \sigma \cdot \tau}$$

IS(1) and IV( $\tau$ ) terms

→ **Magnetic Susceptibility**



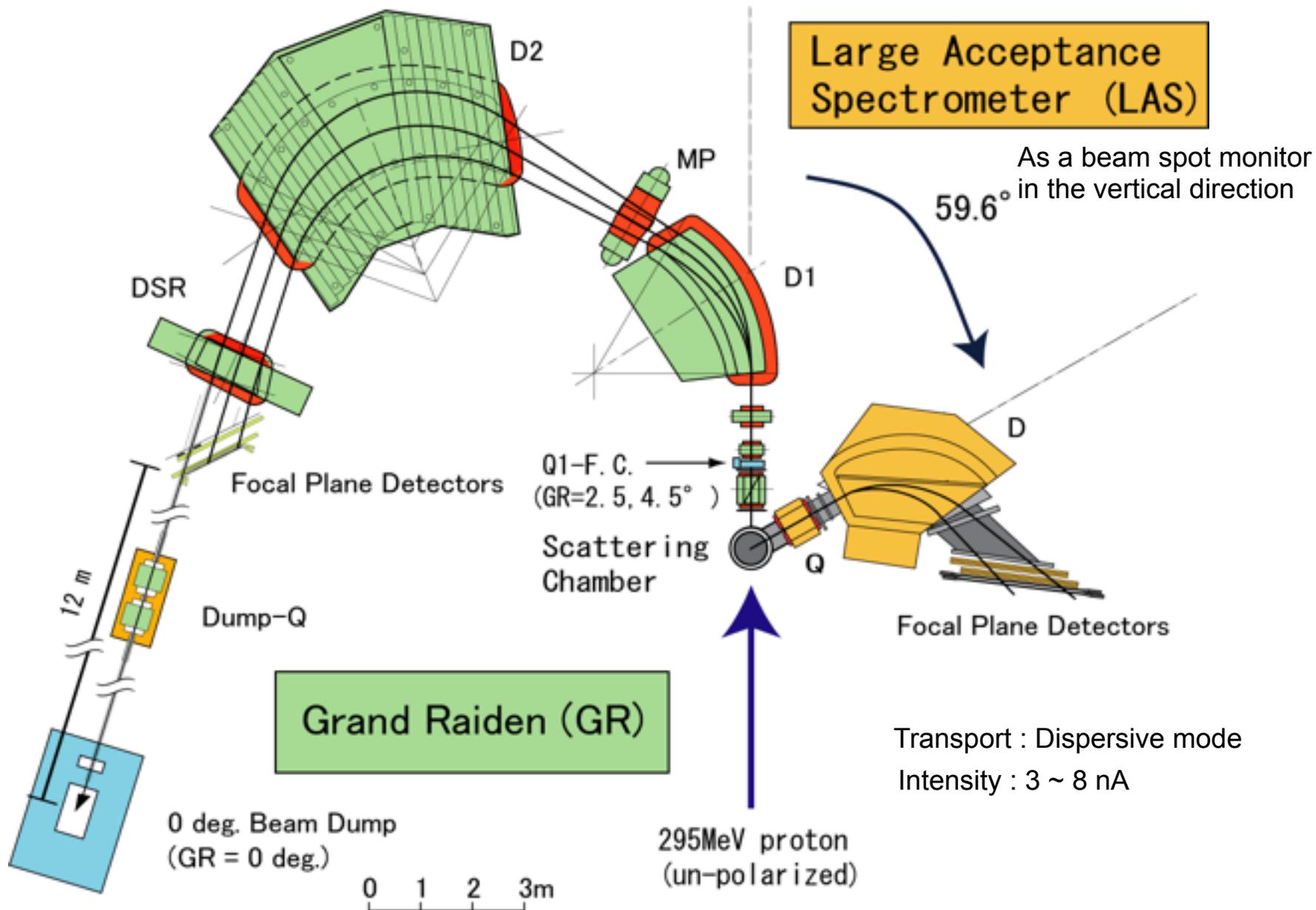
Inversely energy-weighted sum rule of the spin-M1 strengths

→ **Spin Susceptibility**

$$\chi_\sigma^{\text{spin}} = \frac{8}{3N} \sum_f \frac{1}{\omega} \left| \langle f | \sum_i \sigma_i | 0 \rangle \right|^2$$

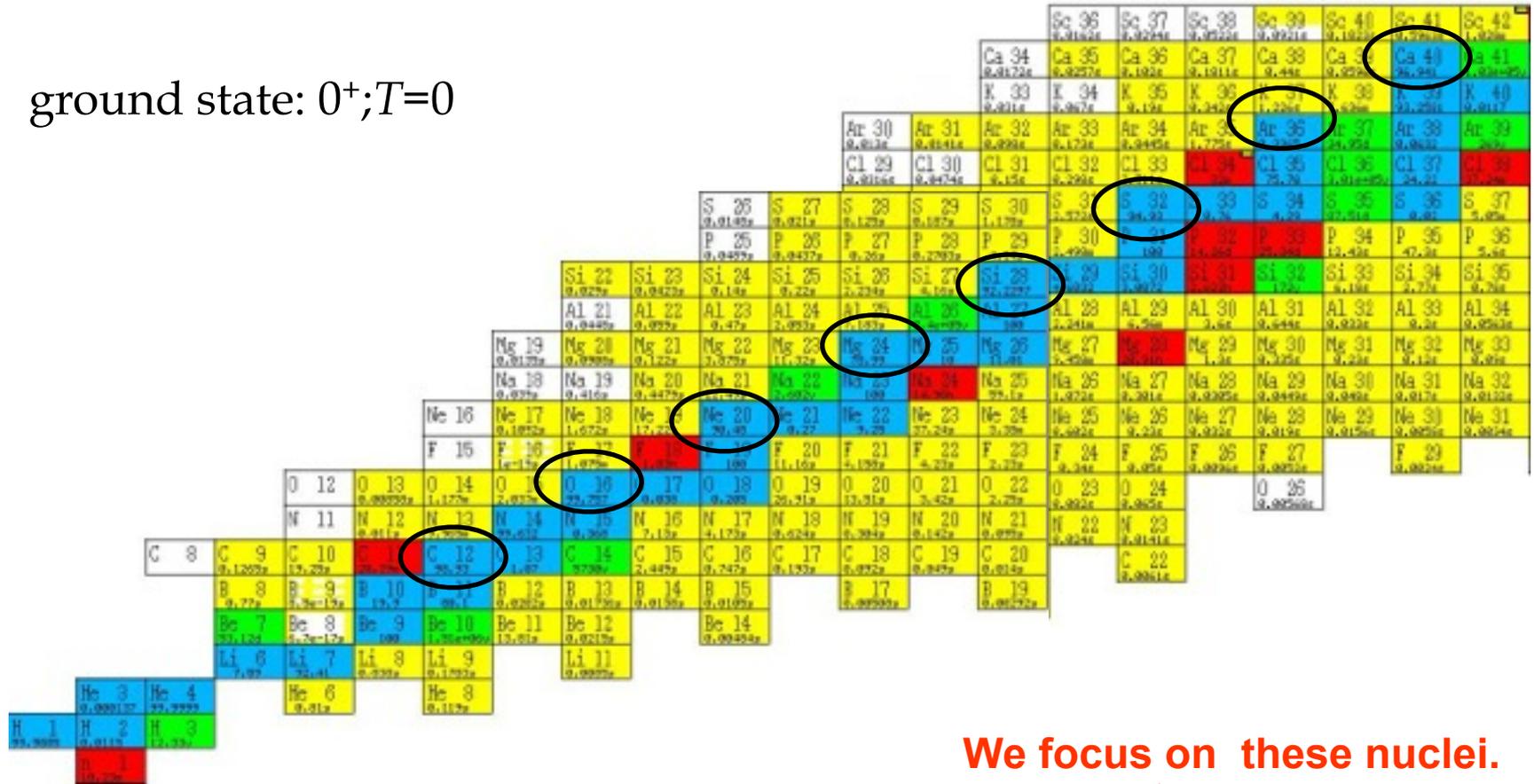
- magnetic response of nuclear matter (e.g. in a magnetar)
- $\nu$ -emissivity
- $\nu$ -transportation

# Spectrometer Setup for 0-deg (p,p') at RCNP



# Self-Conjugate ( $N=Z$ ) even-even Nuclei

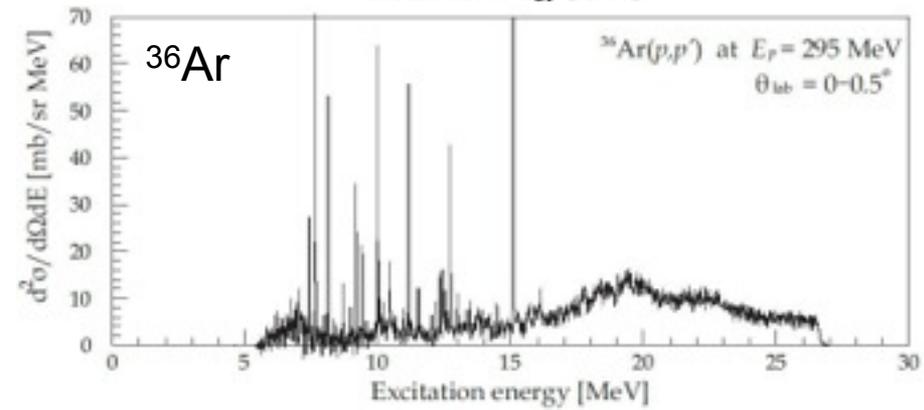
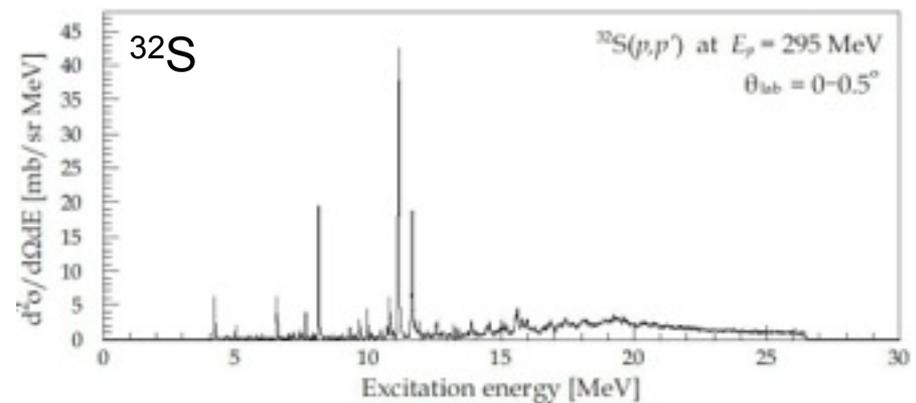
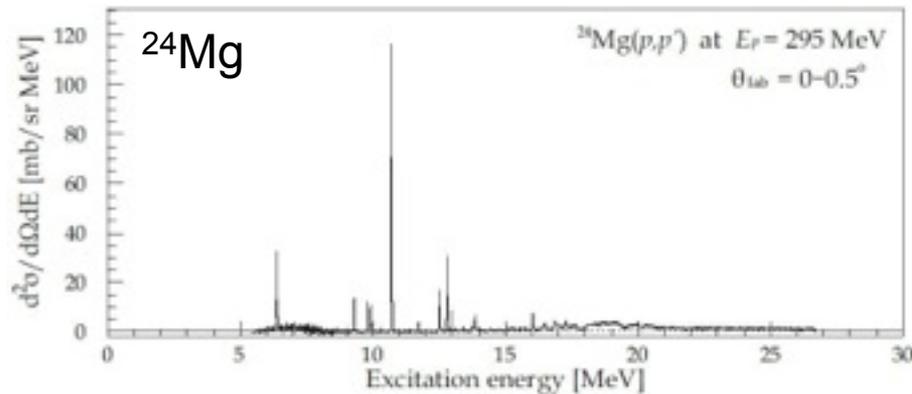
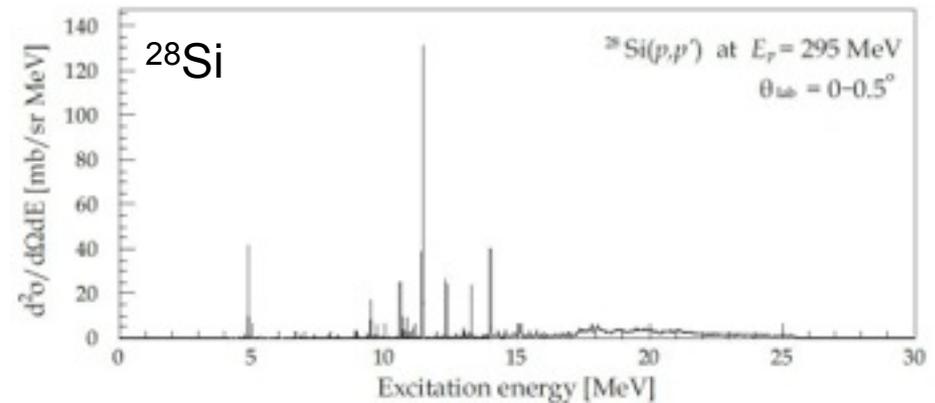
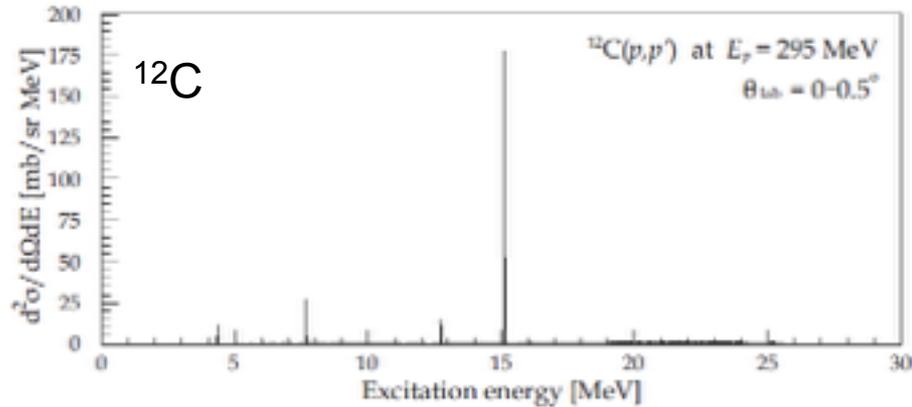
ground state:  $0^+; T=0$



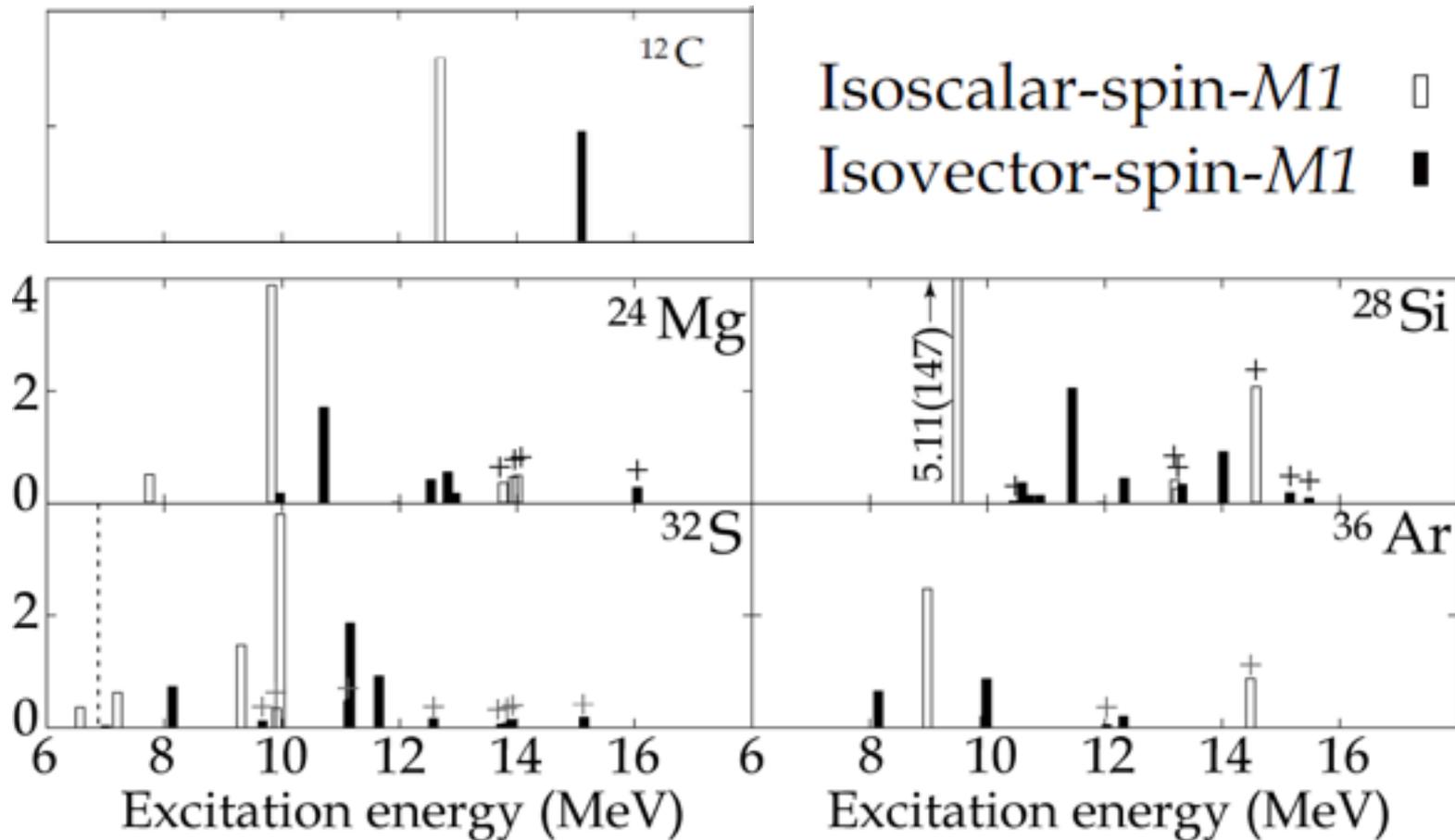
Stable self-conjugate even-even nuclei:

$({}^4\text{He})$ ,  ${}^{12}\text{C}$ ,  ${}^{16}\text{O}$ ,  ${}^{20}\text{Ne}$ ,  ${}^{24}\text{Mg}$ ,  ${}^{28}\text{Si}$ ,  ${}^{32}\text{S}$ ,  ${}^{36}\text{Ar}$ ,  ${}^{40}\text{Ca}$

# Energy spectra at 0-degrees



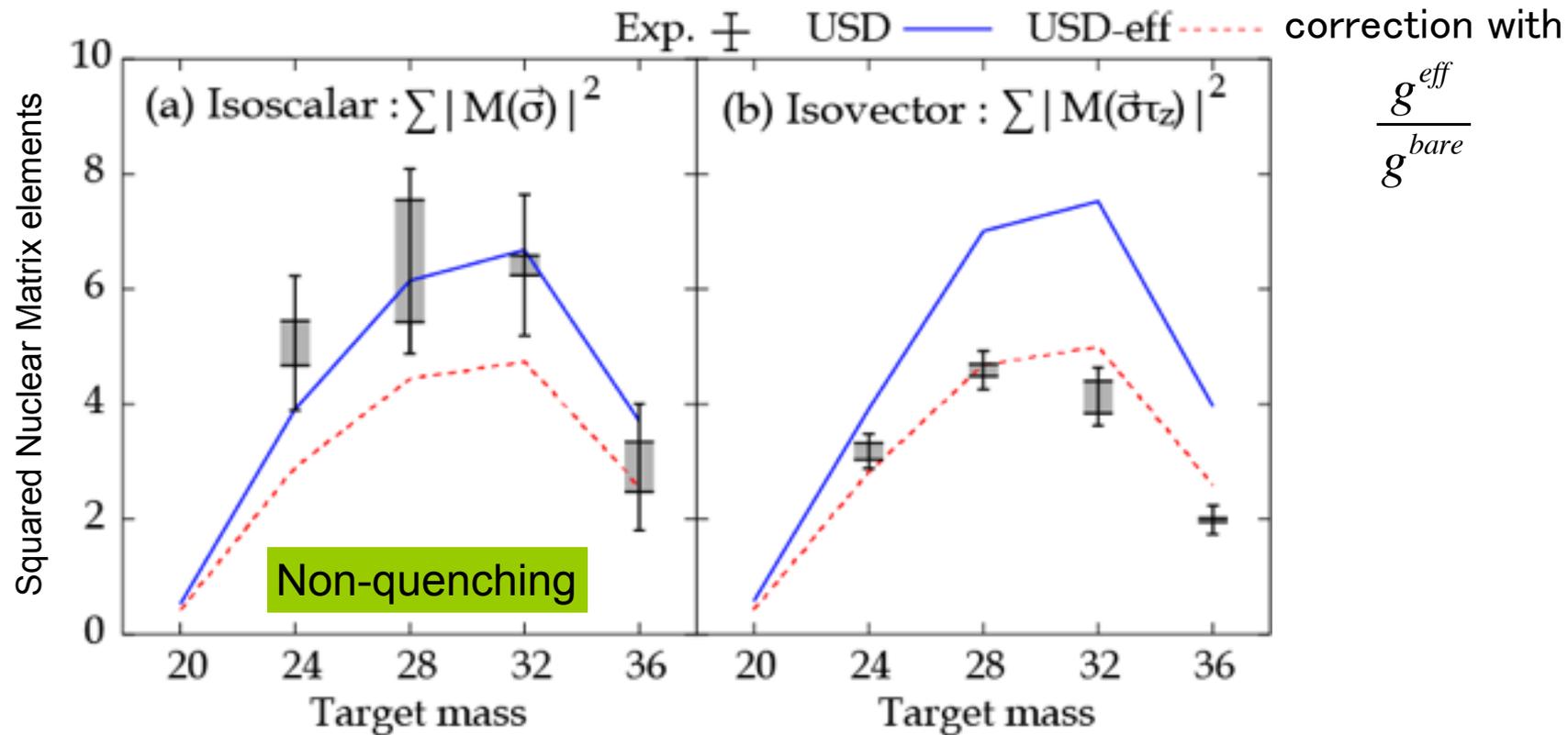
# IS / IV-spin-M1 distribution



# Spin-M1 SNME

H. Matsubara et al., PRL115, 102501 (2015)

- Summed up to 16 MeV.
- Compared with shell-model predictions using the USD interaction

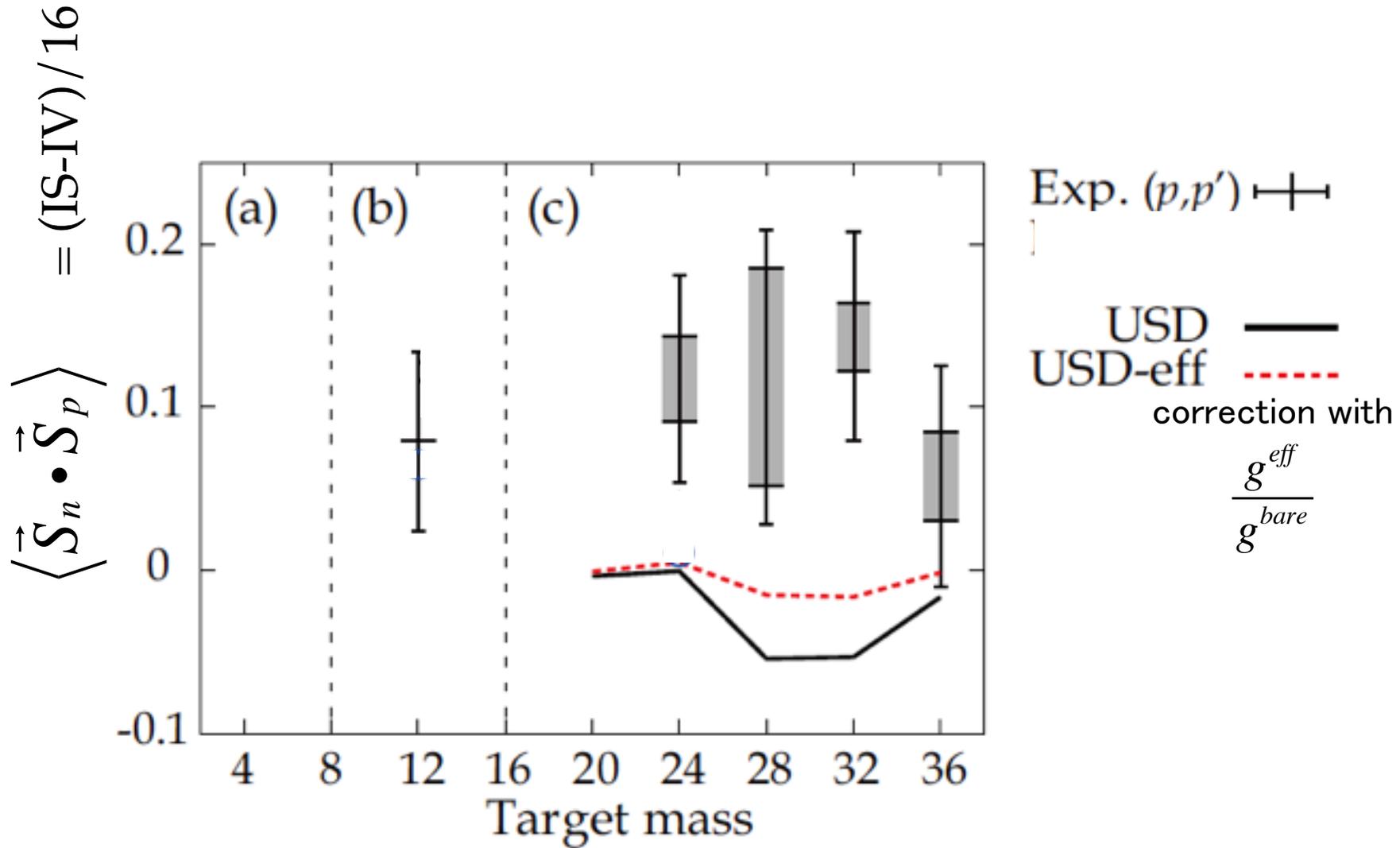


Isoscalar spin-M1 SNME is NOT quenching.

# $np$ Spin Correlation Function

H. Matsubara et al., PRL115, 102501 (2015)

Shell-Model: USD interaction



# $np$ Spin Correlation Function

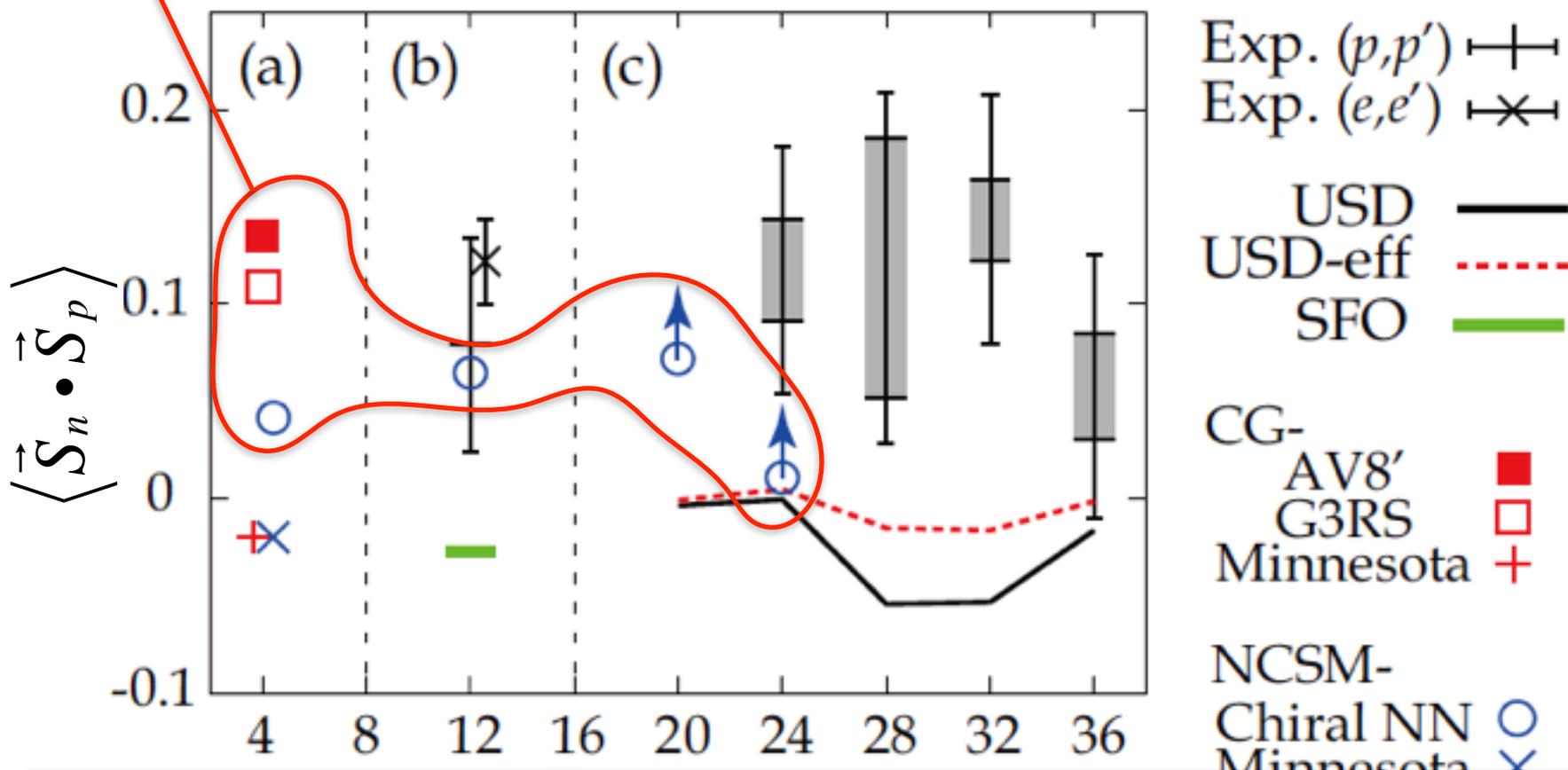
H. Matsubara et al., PRL115, 102501 (2015)

Shell-Model: USD interaction

Correlated Gaussian Method: W. Horiuchi

Non-Core Shell Model: P. Navratil

ab-initio type calc.  
with realistic NN int.



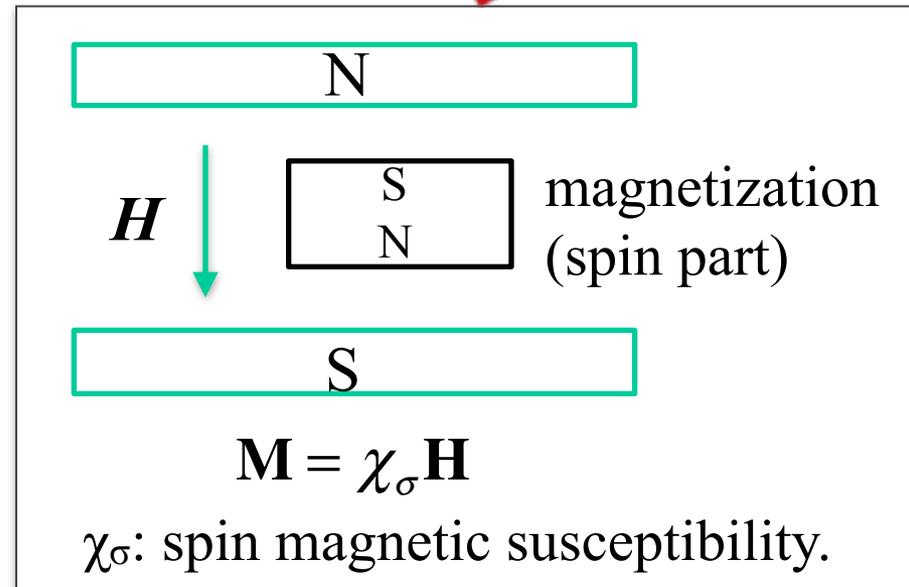
Relevance to tensor correlation and  $np$ -pairing in nuclear ground states

# Spin Susceptibility

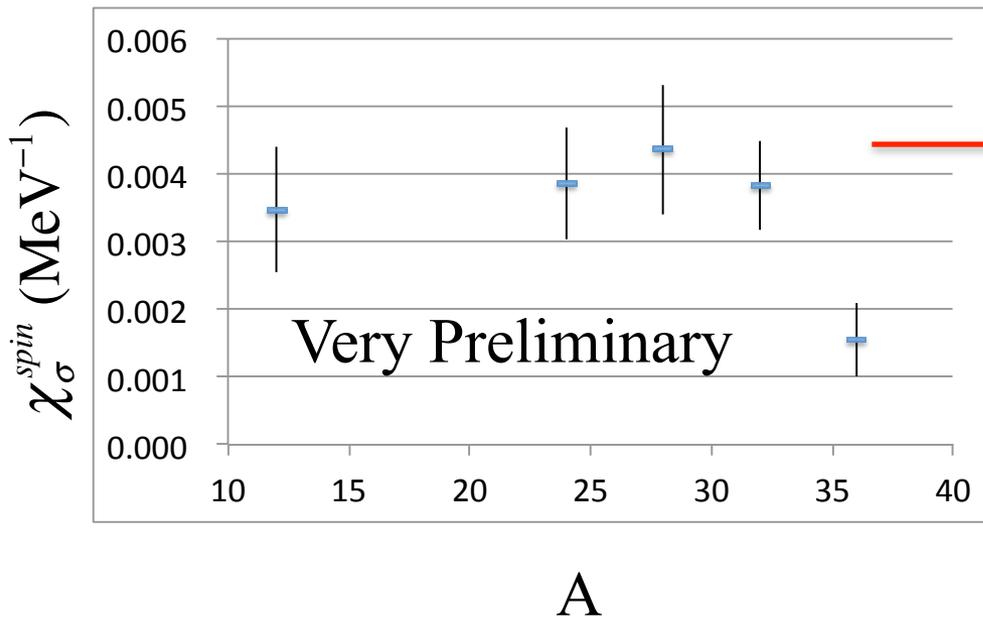


Inversely energy-weighted sum rule of the spin-M1 strengths

$$\chi_{\sigma}^{spin} = \frac{8}{3N} \sum_f \frac{1}{\omega} \left| \langle f | \sum_i \sigma_i | 0 \rangle \right|^2$$



## Spin Susceptibility of $N=Z$ Nuclei



0.0044(7) MeV<sup>-1</sup> at  $\rho=0.16$  fm<sup>-3</sup>

Neutron matter calc.  
by AFDMC model

G. Shen et al., PRC**87**, 025802 (2013)

Further theoretical analysis  
is required.

# CAGRA+GR Campaign Exp. From Oct. 2016

1. Structure of the PDR \*1 ( $\alpha, \alpha' \gamma$ ) and ( $p, p' \gamma$ ) on  $^{58}\text{Ni}$ ,  $^{90,94}\text{Zr}$ ,  $^{120,124}\text{Sn}$ ,  $^{206, 208}\text{Pb}$
2. Inelastic  $\nu$ -nucleus response, S. Noji et al.,
3. Super-deformed states, high-spin states, D. Jenkins et al.,

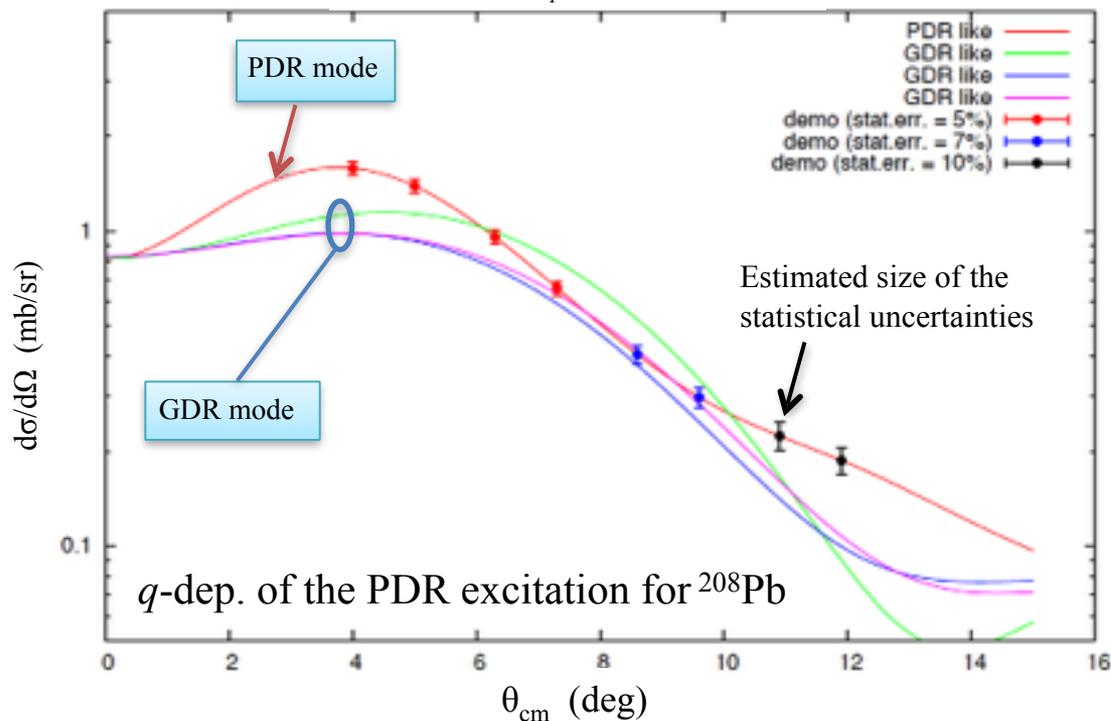
\*1 A. Bracco, F. Crespi, V. Derya, M.N. Harakeh, T. Hashimoto, C. Iwamoto, P. von Neumann-Cosel, N. Pietralla, D. Savran, A. Tamii, V. Werner, and A. Zilges *et al.*



beam to beam dump

GRAF

$^{208}\text{Pb}(p, p')$  at  $E_p = 80$  MeV

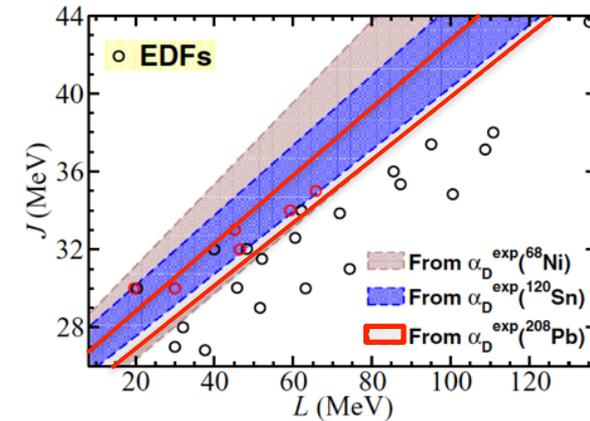


Talk by M. Carpenter tomorrow

# Summary

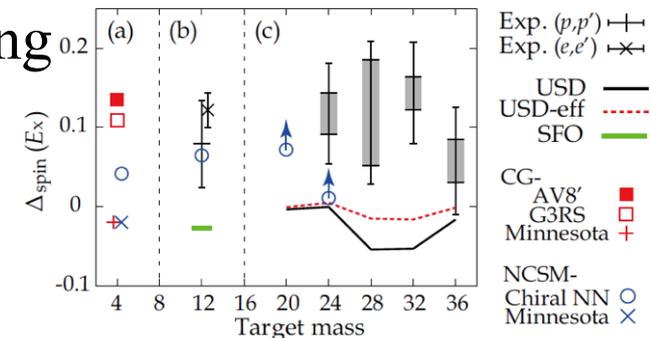
- The electric dipole response of nuclei is one of the fundamental properties nuclei.

A constraint band has been obtained for the symmetry energy parameters from the measured electric dipole polarizability.



- Spin magnetic response of nuclei has been measured for N=Z even even nuclei in the sd-shell.

The IS spin excitation strength is not quenching while the IV spin excitation strength is quenching as the Gamow-Teller strength.



*Thank you  
for your attention*