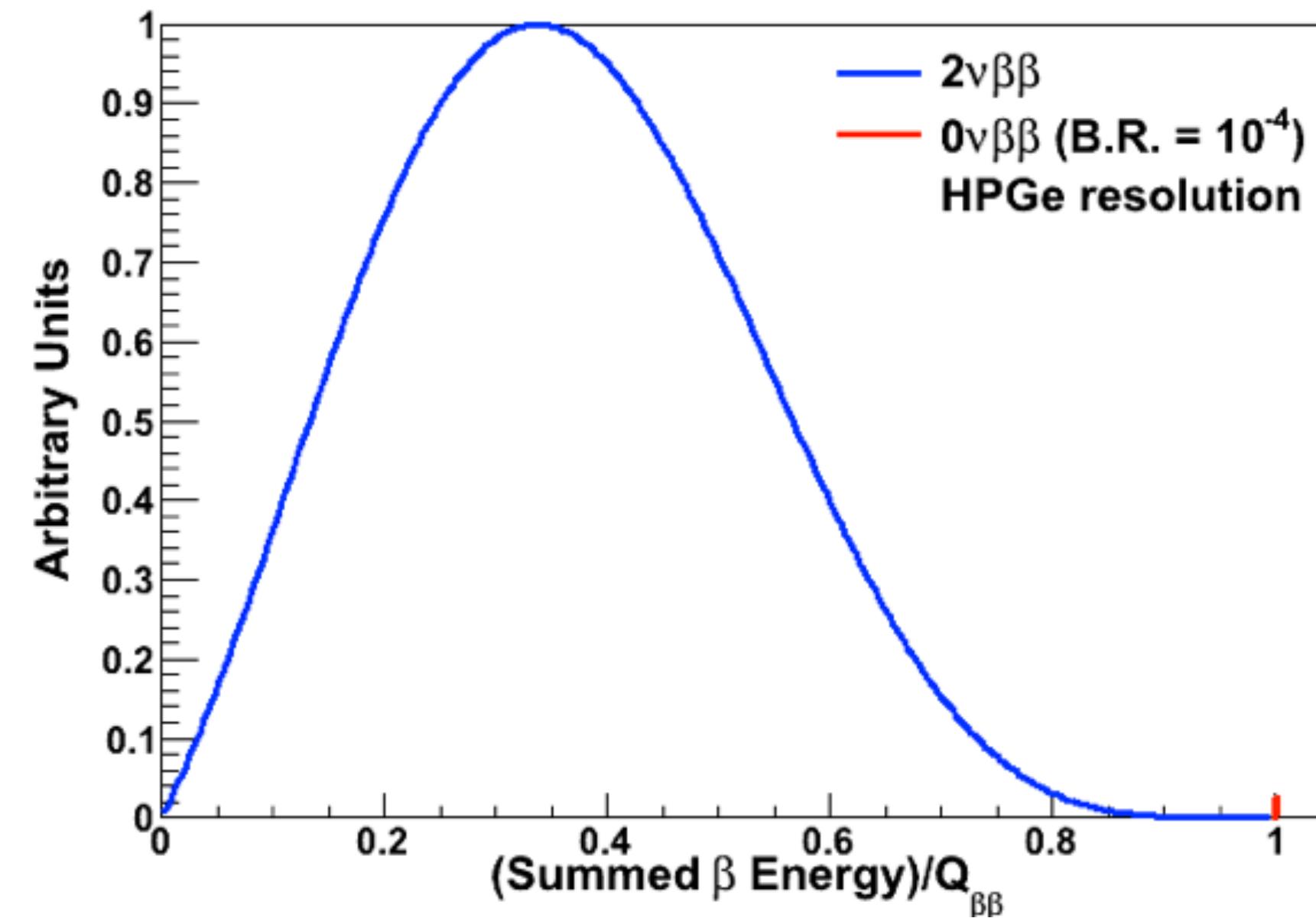
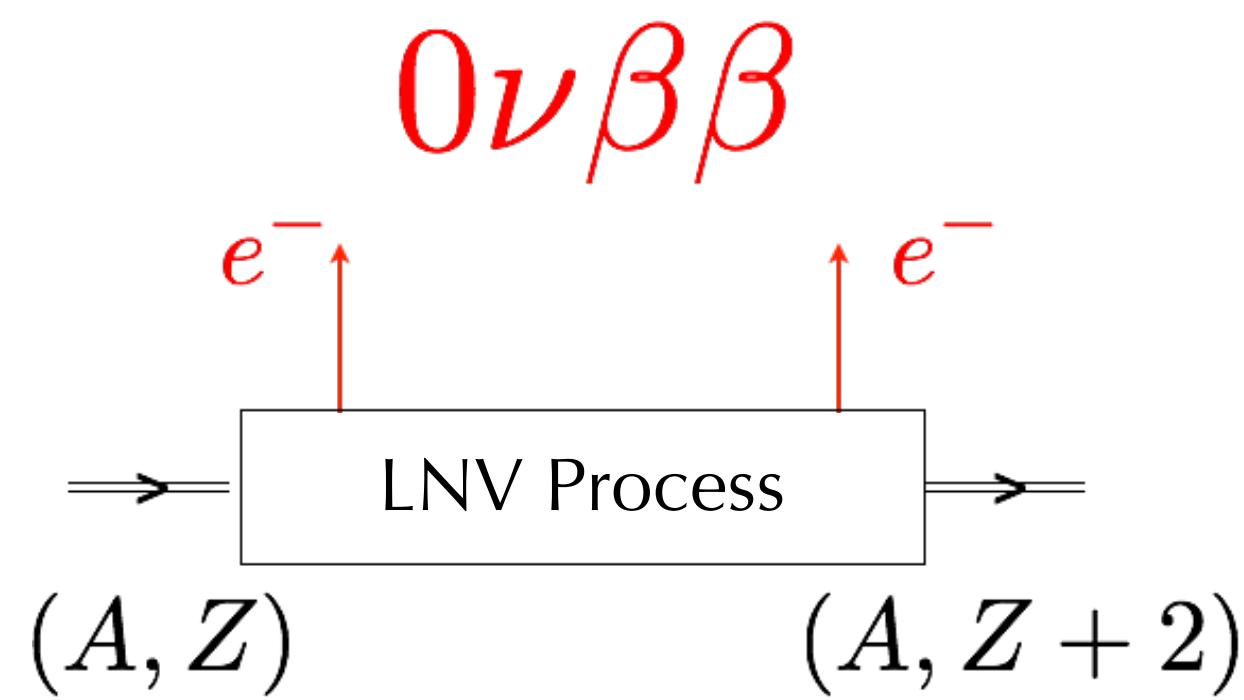


# Discovery Potential of Future Neutrinoless Double-Beta Decay Experiments

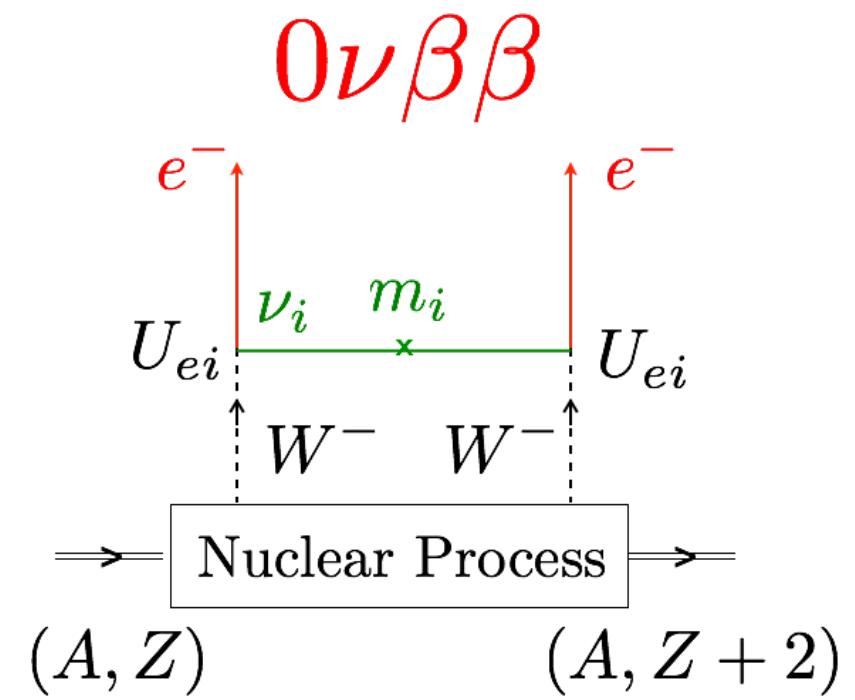
Jason Detwiler, University of Washington  
DBD18, Waikoloa, Hawaii  
October 21, 2018

# Neutrinoless Double-Beta Decay



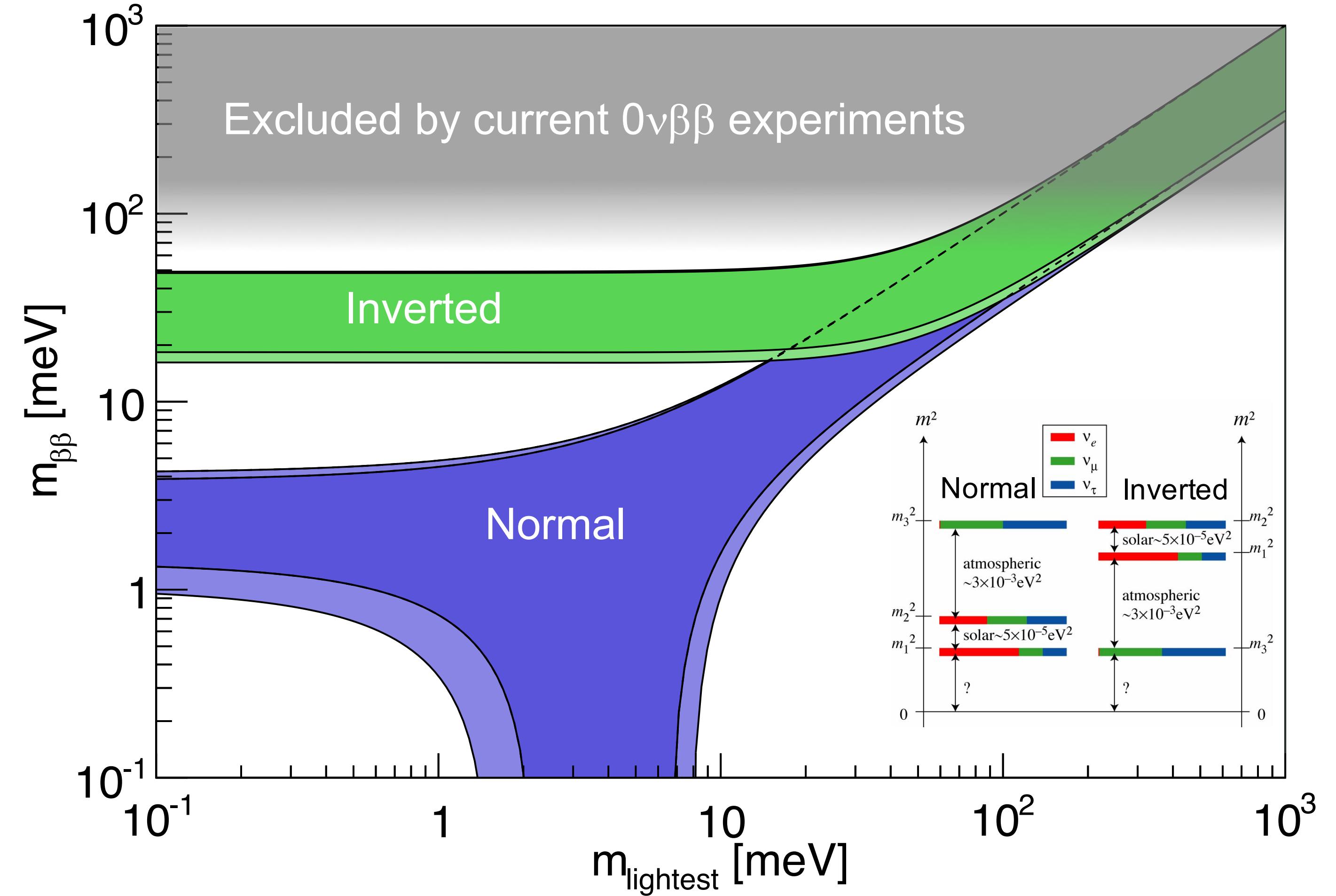
- Matter creation process
- The peak in the plot exceeds current limits
- Must measure summed electron kinetic energy to distinguish from Standard-Model  $2\nu$  process: scintillation, ionization, and/or heat
- Some experiments can also measure electron momenta (tracking), provides a handle on the LNV process

# Pure-Majorana SM Neutrino Exchange

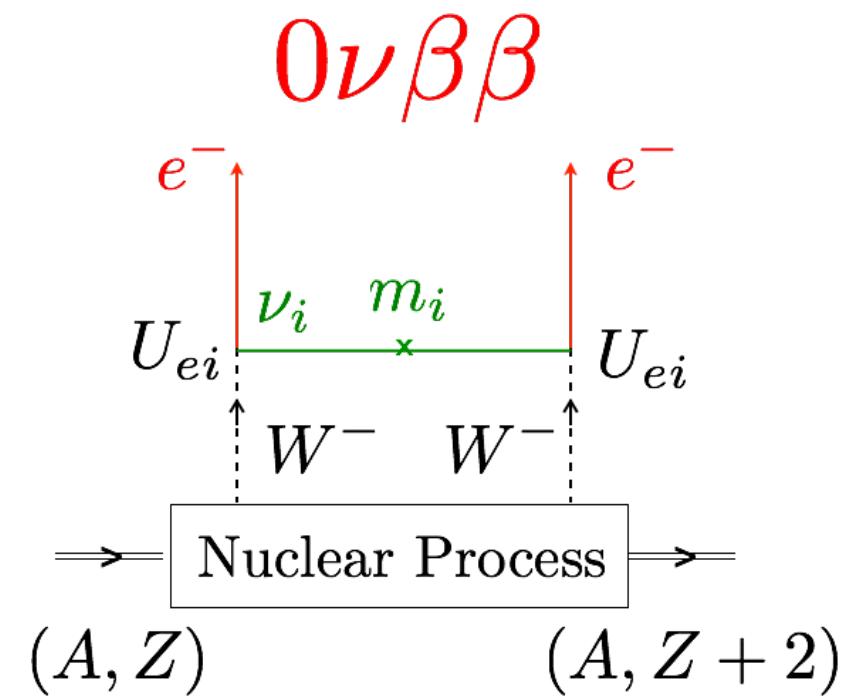


$$\Gamma_{1/2}^{0\nu} = G^{0\nu} |M^{0\nu}|^2 \left| \sum_{i=1}^3 U_{ei}^2 m_i \right|^2$$

- “Minimal” model: add just one parameter to the SM Lagrangian
- Simple goal post for future experiments

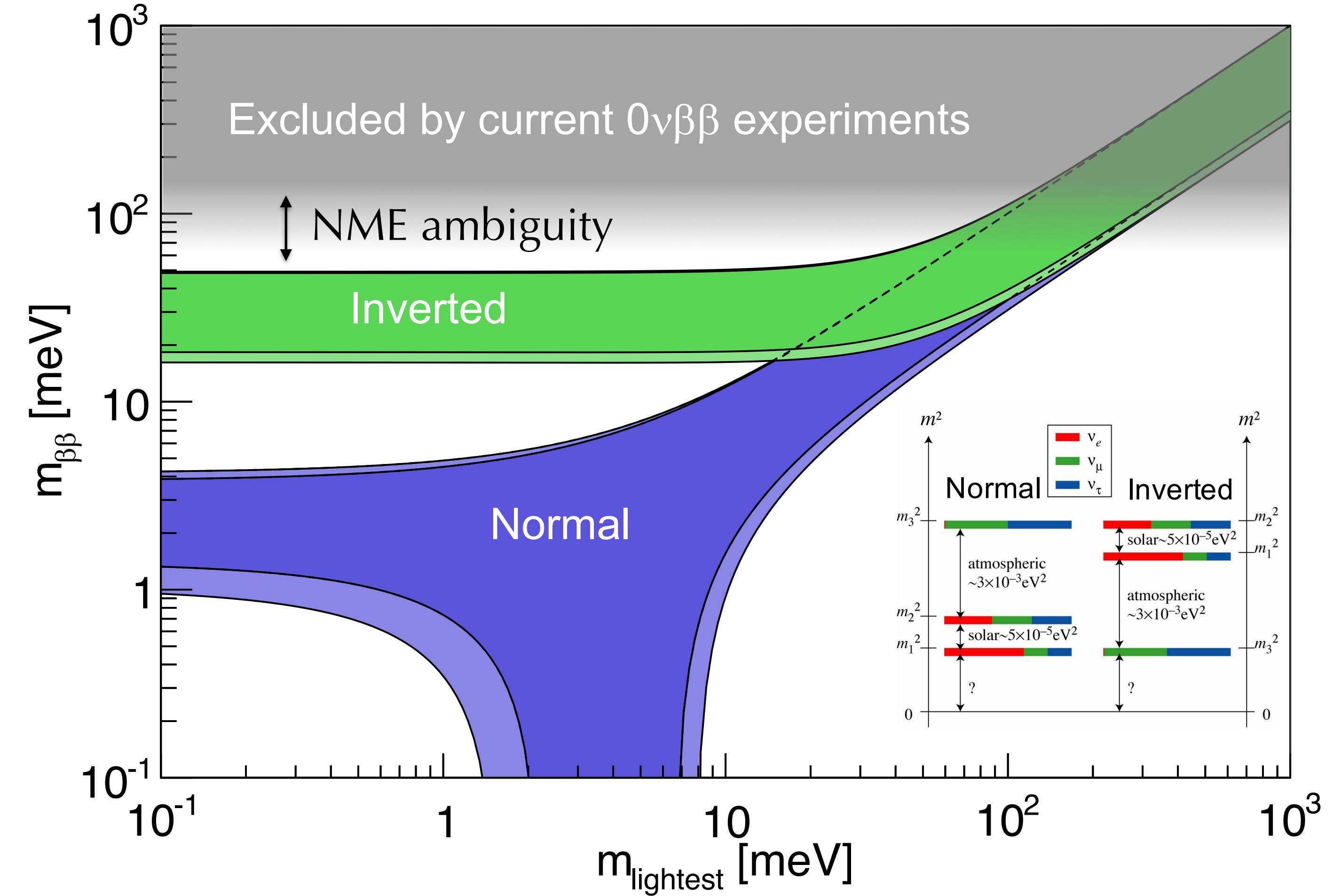


# Pure-Majorana SM Neutrino Exchange

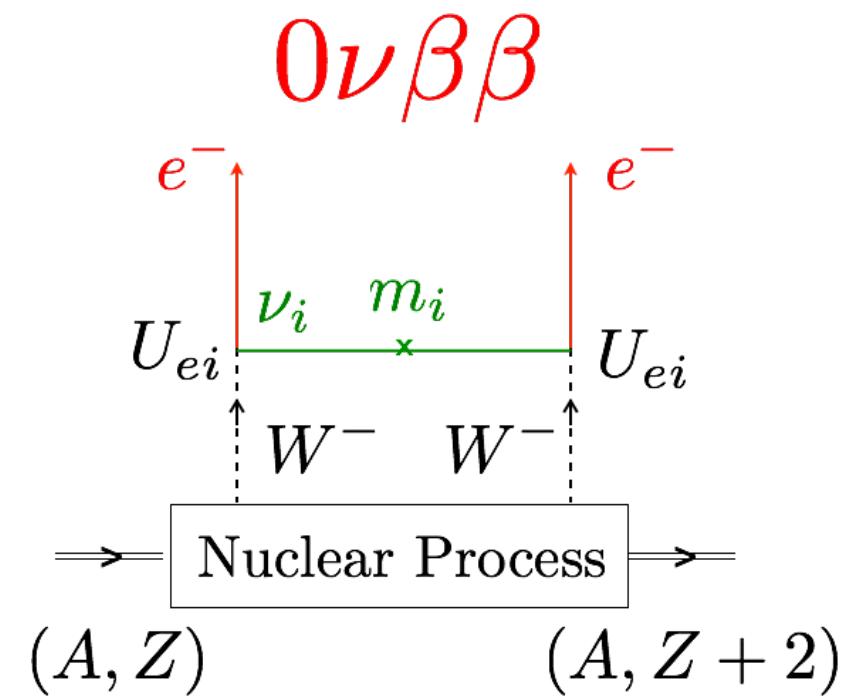


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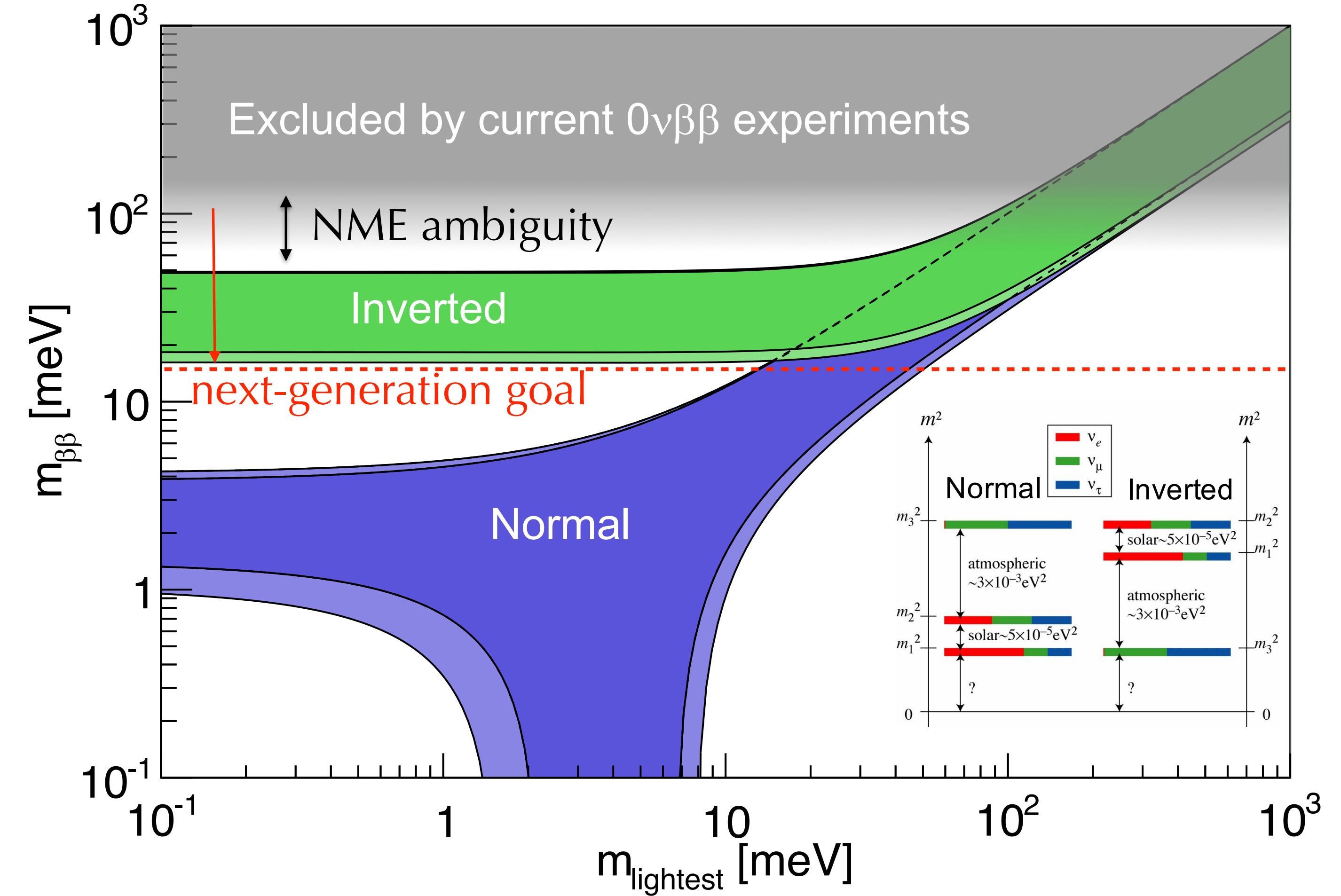


# Pure-Majorana SM Neutrino Exchange



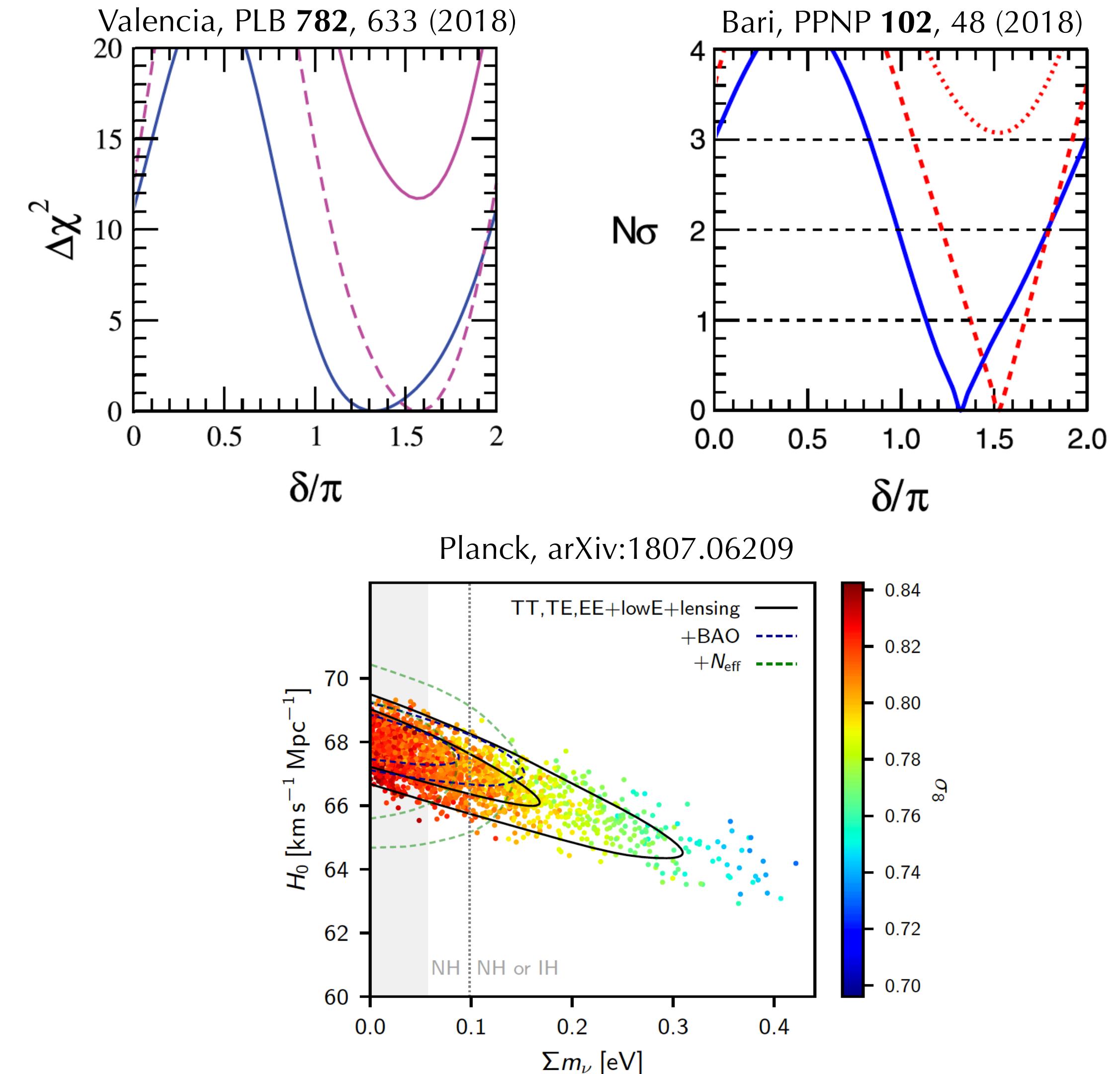
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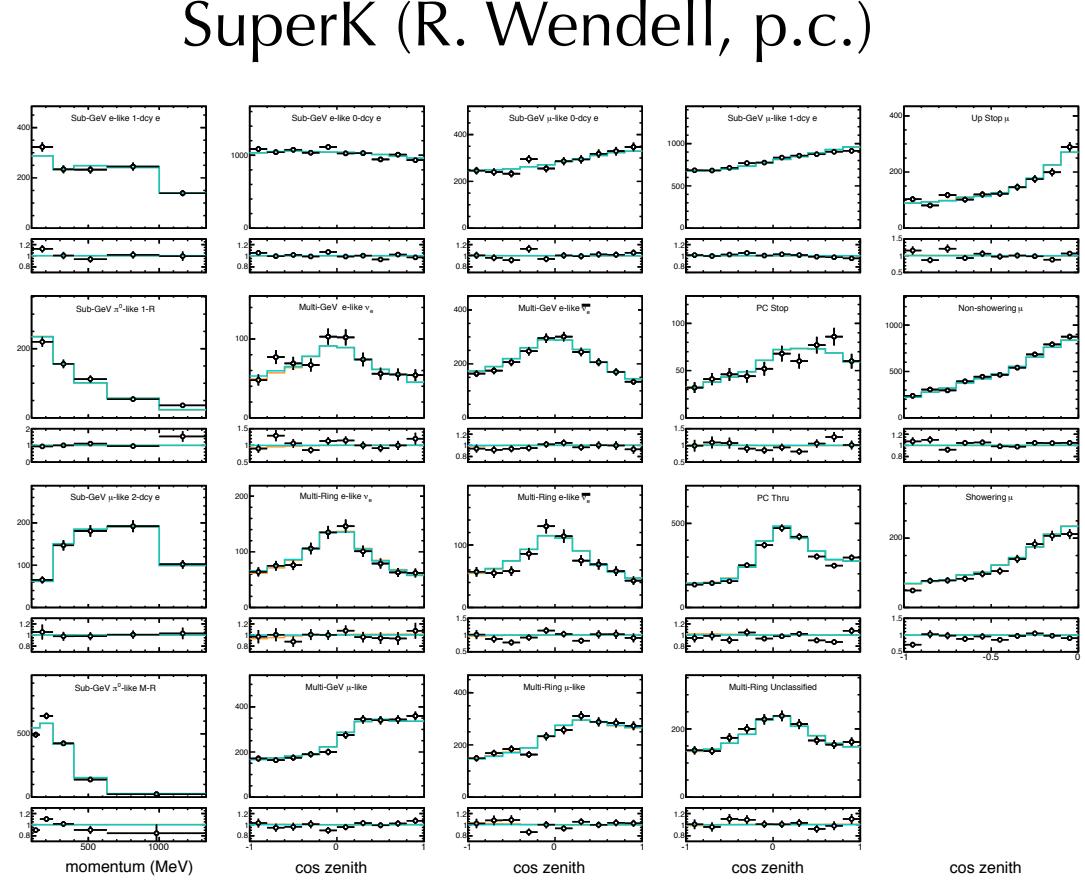
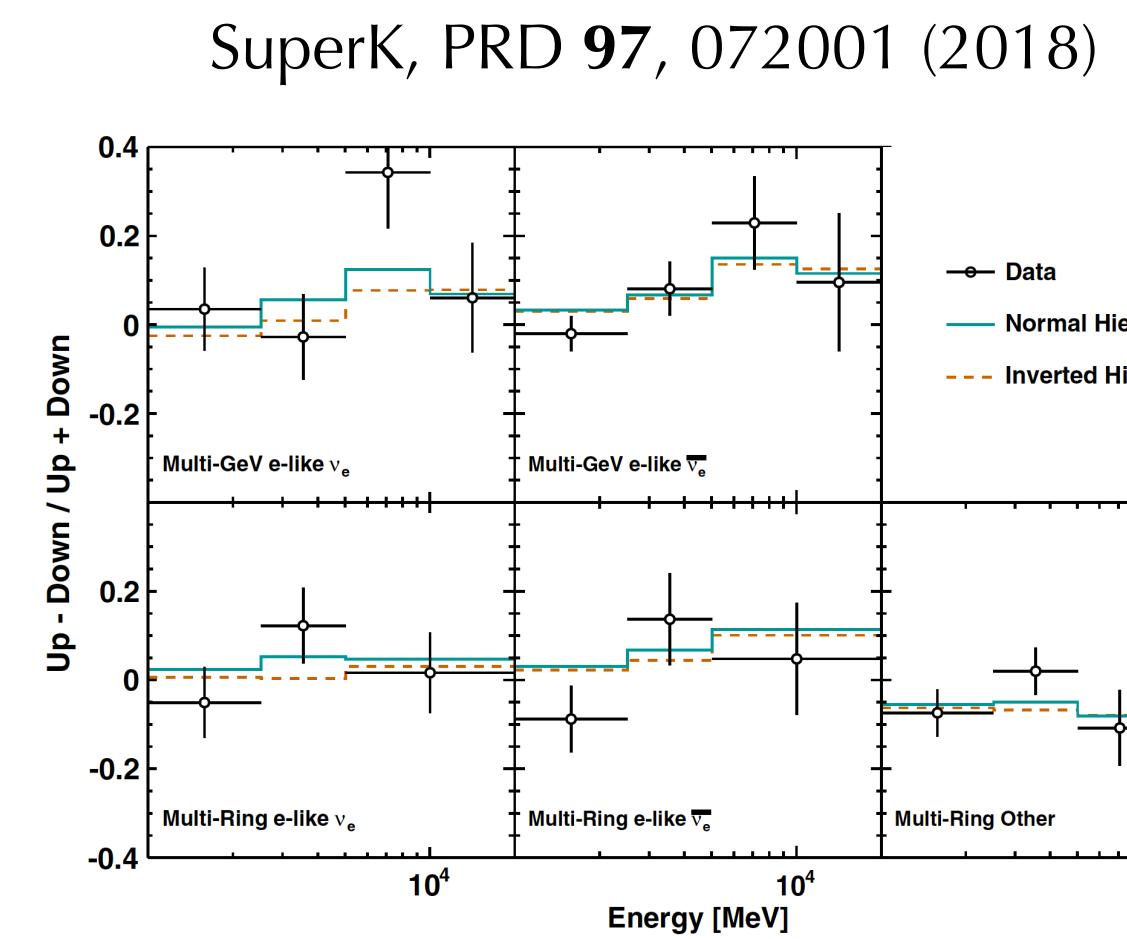
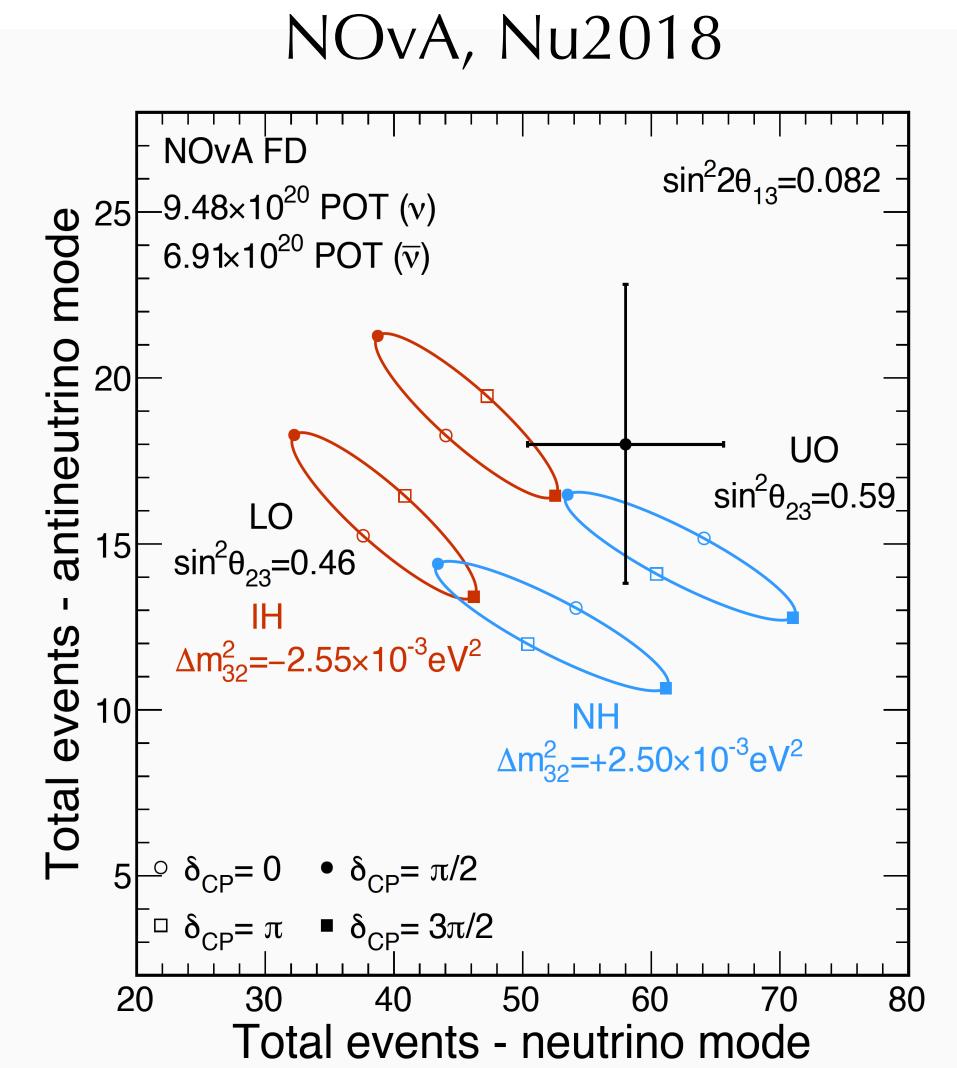
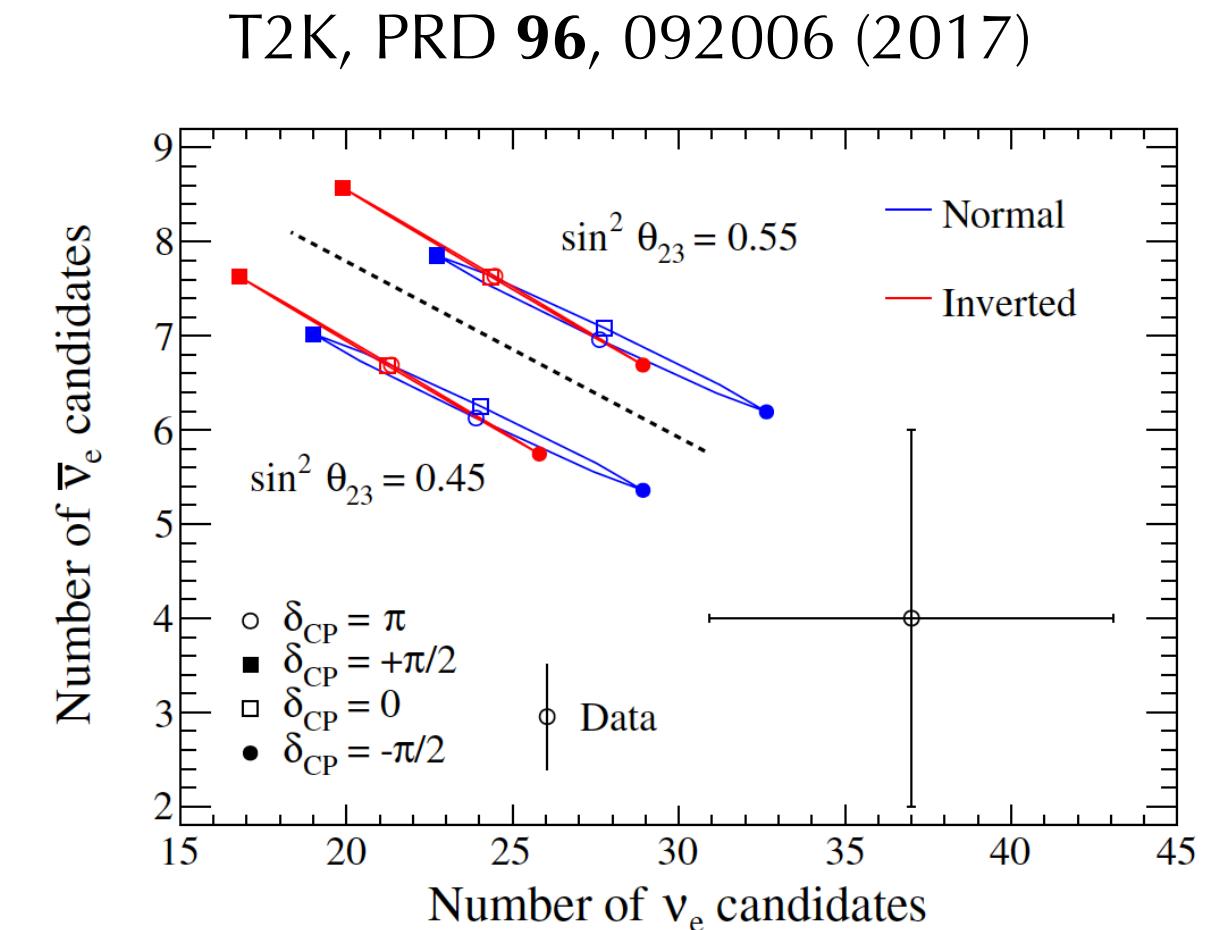
# $\text{IO}_{\min}$ is still a reasonable goal

- NO preferred at  $\sim 3\sigma$  in global oscillation analyses. Also preferred by cosmology. However:
  - Visibility of such preference in the data is still poor: large  $\Delta\chi^2$  but small ΔG.O.F
  - Phenomenologists cannot reproduce the strong contribution from SK ( $>3\sigma$  global analyses just use the SK  $\chi^2$  map)
  - Cosmological limits are systematic-dominated, still favor  $\Sigma \rightarrow 0$
- Also:  $\text{IO}_{\min}$  still represents  $\sim 2$  orders-of-magnitude improvement in  $T_{1/2}$  sensitivity
  - Significant potential for discovery even in the case of NO (this talk)
  - Non-minimal models open up the entire parameter space for discovery anywhere below current limits!

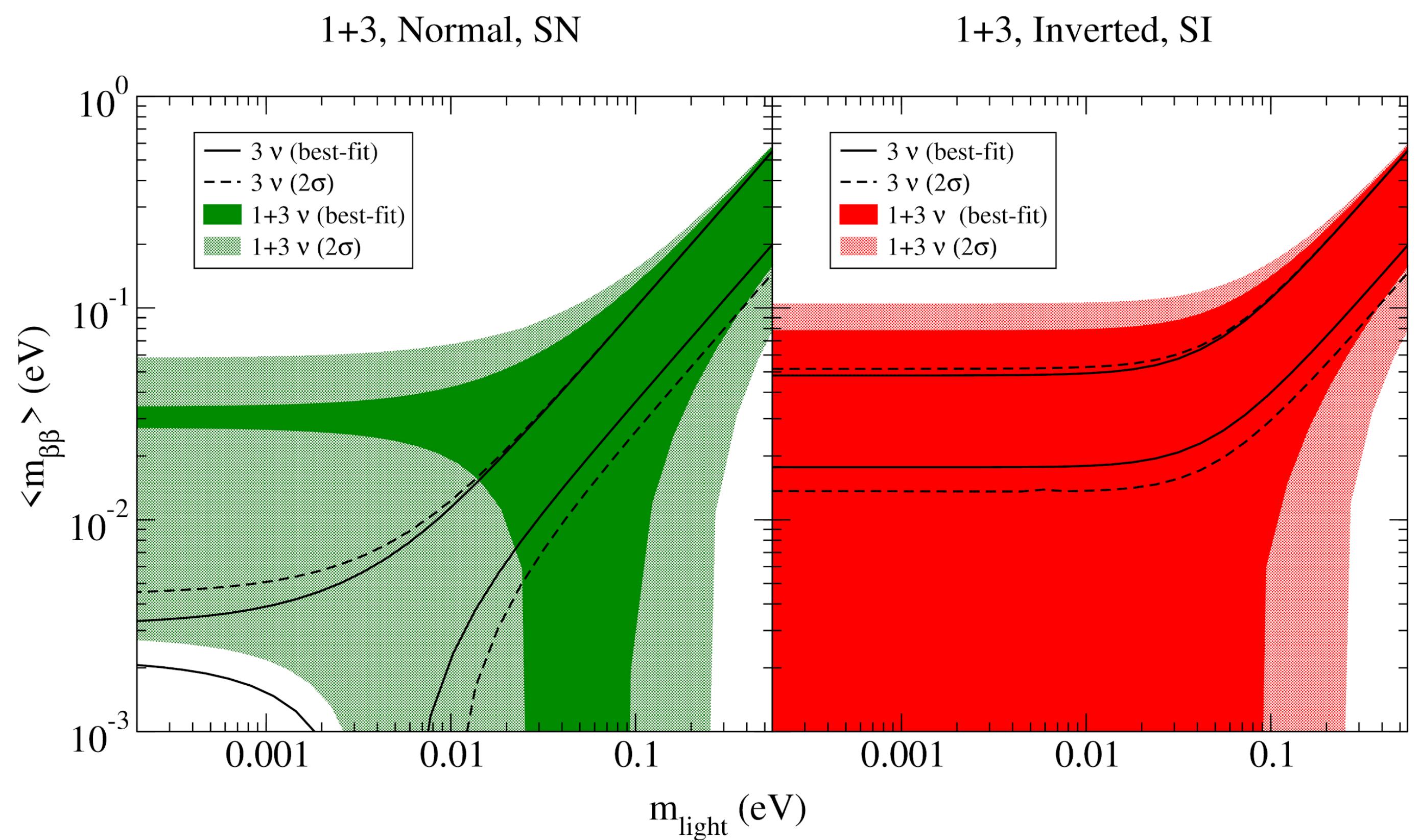
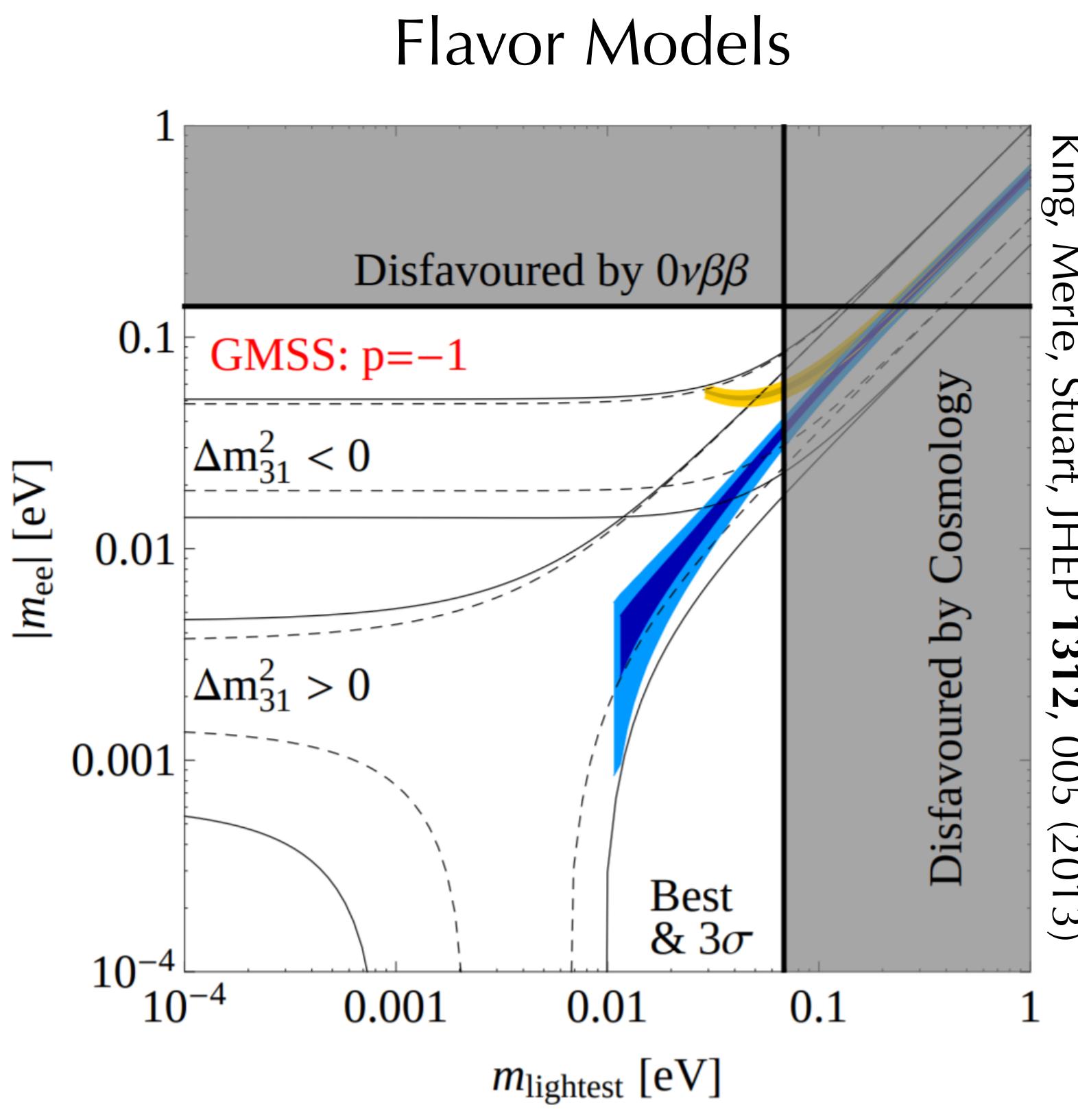


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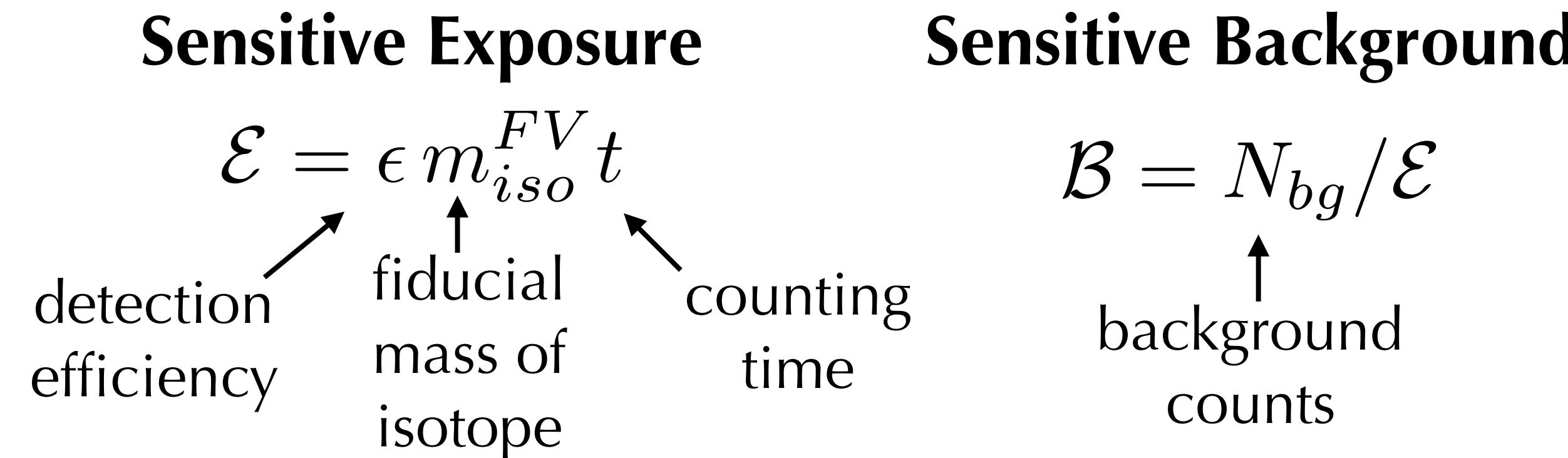
# Alternative Mechanisms



# $0\nu\beta\beta$ : Qualitative Experimental Description

- Energy is the only observable quantity that is both a necessary and sufficient condition for discovery of  $0\nu\beta\beta$  decay
- Sensitivity is dominated by Poisson counting in the region-of interest (ROI): observing some number of counts during an exposure in the presence of background.
- Relevant parameters:

Sensitive Exposure	Sensitive Background
$\mathcal{E} = \epsilon m_{iso}^{FV} t$	$\mathcal{B} = N_{bg}/\mathcal{E}$
detection efficiency	background counts
fiducial mass of isotope	
counting time	



The diagram illustrates the components of the Sensitive Exposure equation. It shows three terms: detection efficiency ( $\epsilon$ ), fiducial mass of isotope ( $m_{iso}^{FV}$ ), and counting time ( $t$ ). Arrows point from each term to its corresponding label below the equation.

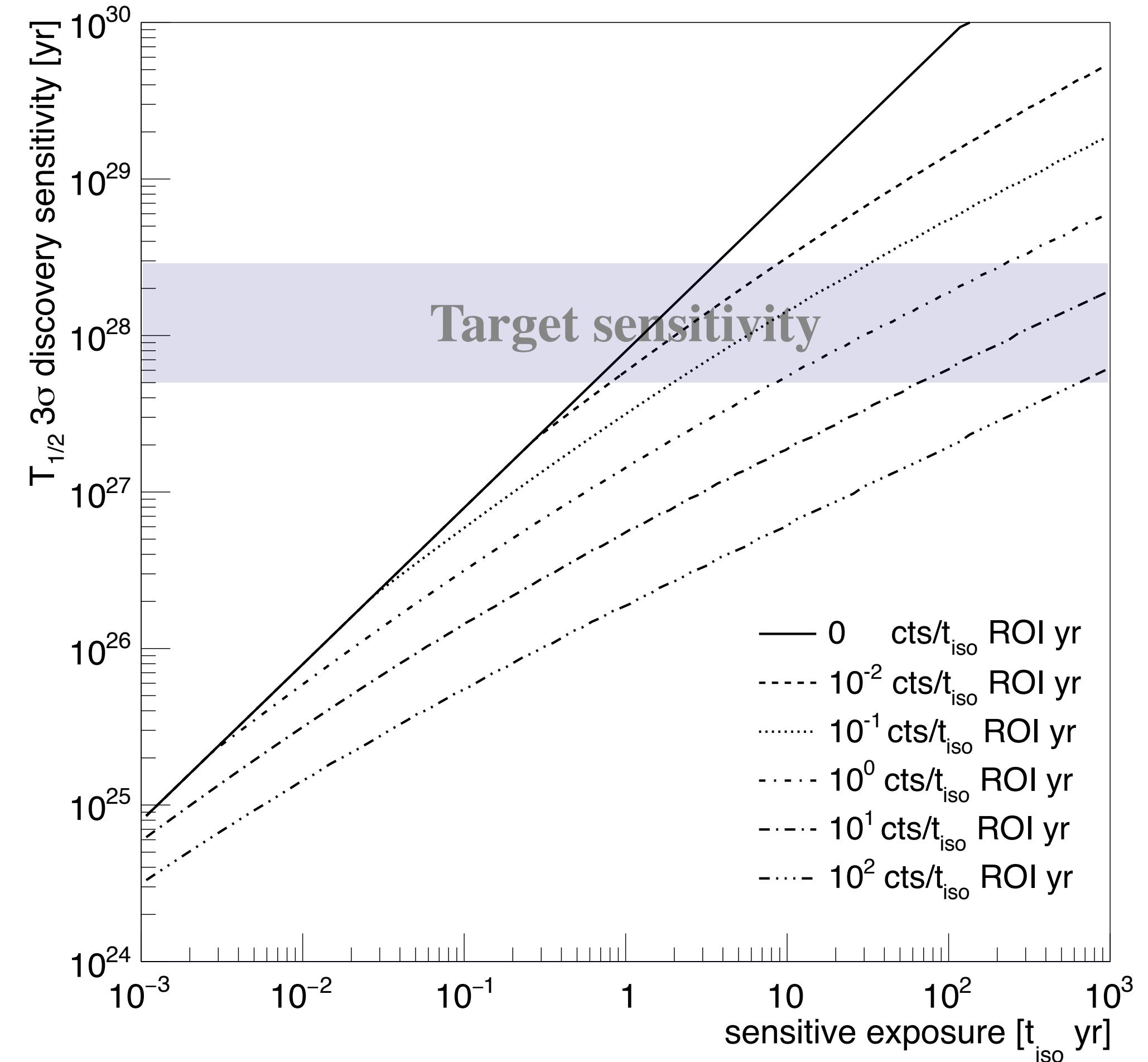
- In most (all) experiments, background is well-constrained, either from energy or volumetric side-bands

# Experimental Focus: Discovery

- Discovery sensitivity: the value of  $T_{1/2}$  for which an experiment has a 50% chance to observe a signal above background with  $3\sigma$  significance:

$$T_{1/2}^{3\sigma} = \ln 2 \frac{N_A \mathcal{E}}{m_a S_{3\sigma}(\mathcal{B}\mathcal{E})}$$

- $S_{3\sigma}(B) =$  Poisson signal expectation at which 50% of experiments report  $3\sigma$  fluctuation above  $B = \mathcal{B}\mathcal{E}$

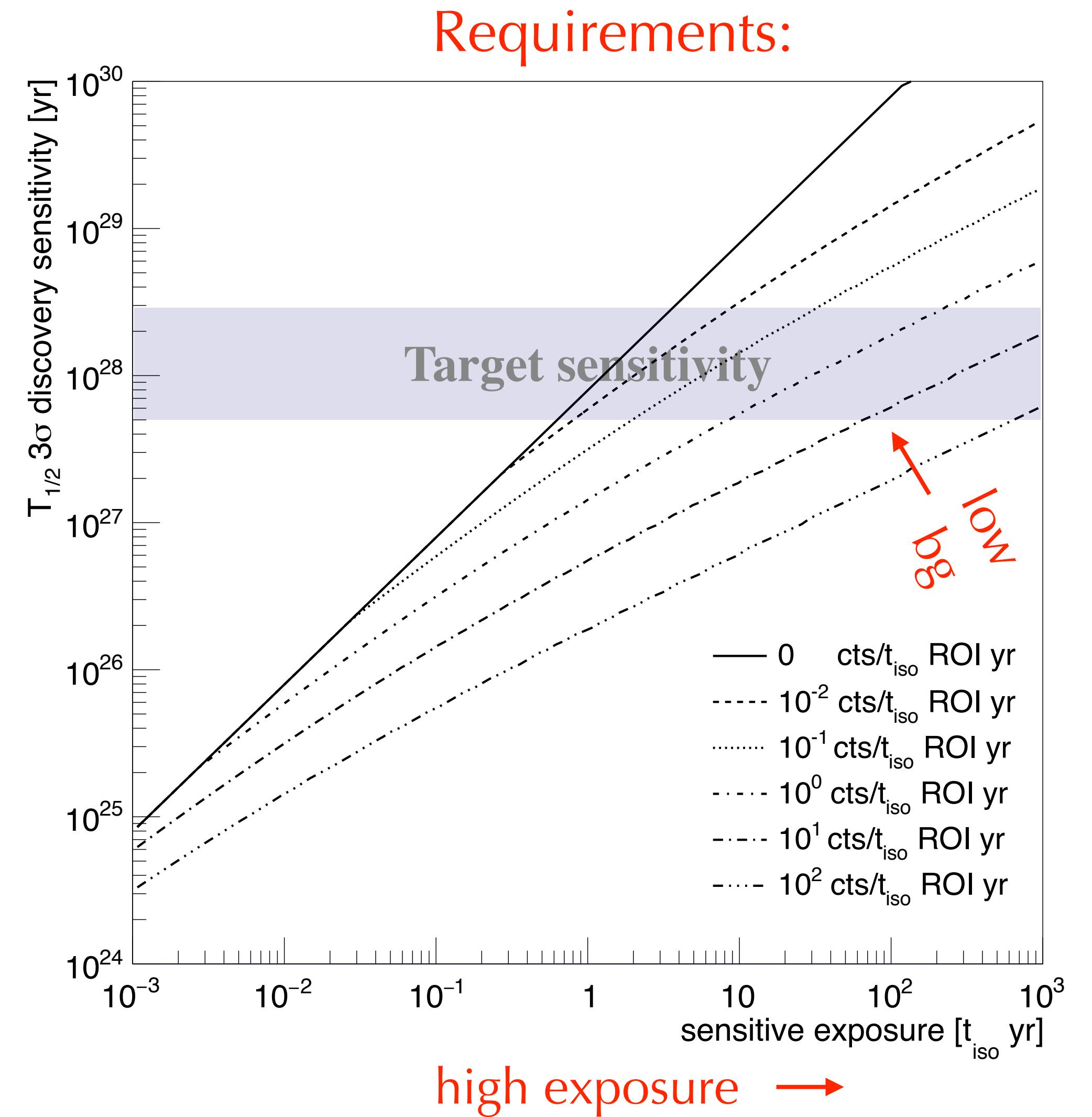


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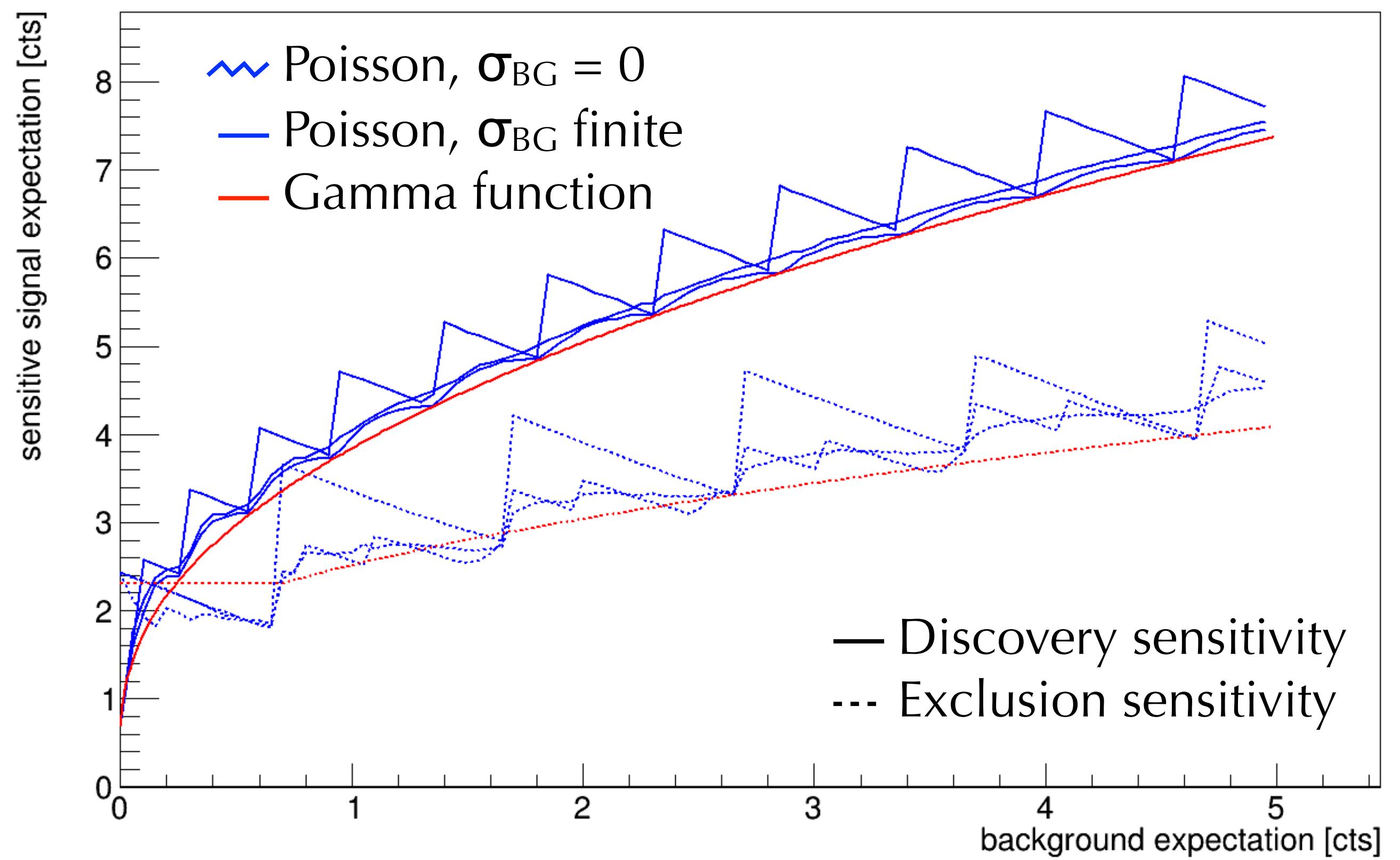


# Poisson + BG Uncertainty

- Shortcut: approximate the Poisson CDF using the  $\Gamma$  function

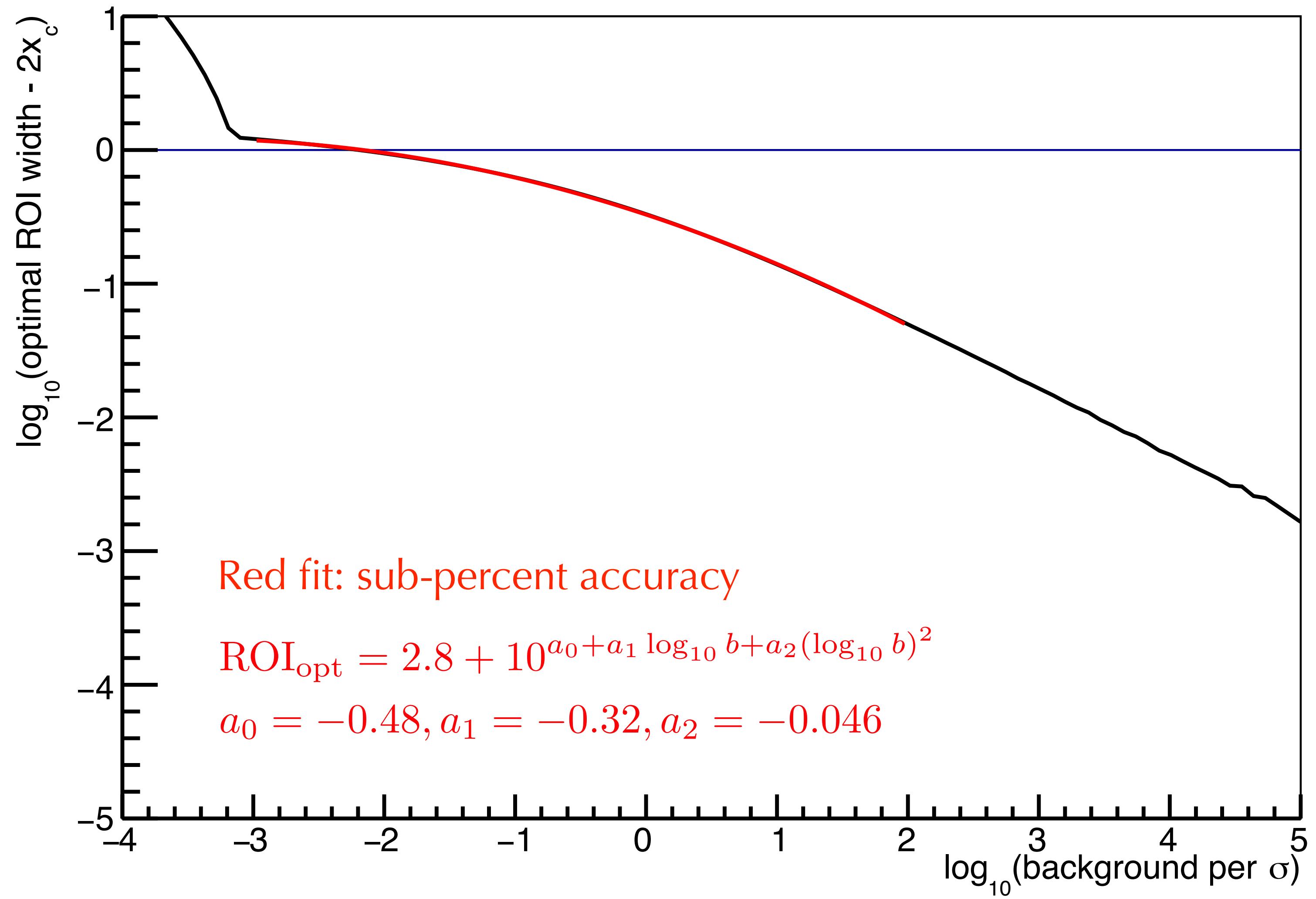
$$CDF(C|\mu) \approx \frac{\Gamma(C+1|\mu)}{\Gamma(C+1)}$$

- Extremely fast calculation (avoid lengthy MC)
- Better approximation when BG uncertainty is considered



# ROI Optimization

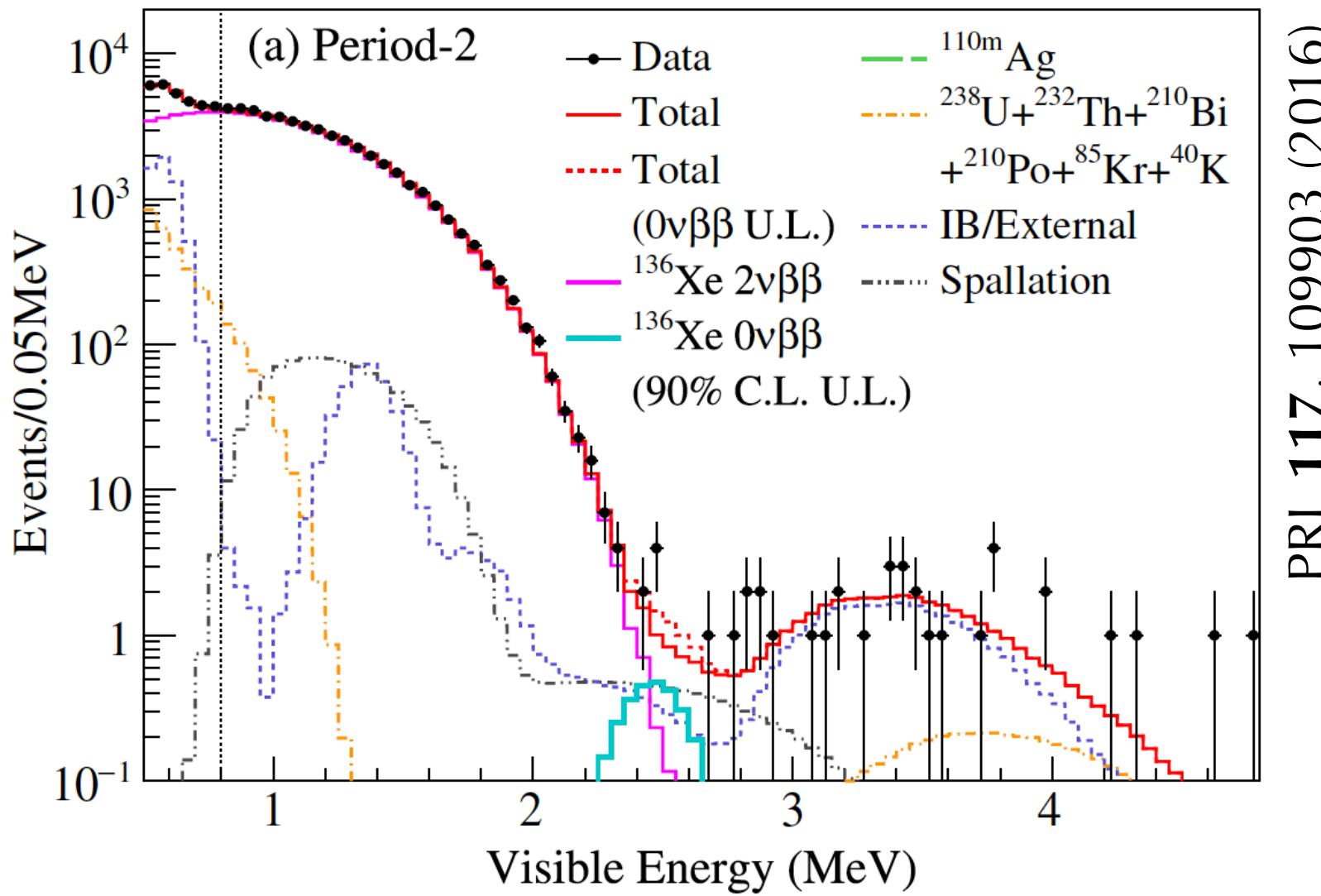
- Optimize ROI to maximize discovery sensitivity
- $x_c \approx 1.4$  solves
$$x_c e^{-\frac{x_c^2}{2}} = \frac{\sqrt{2\pi}}{4} \operatorname{erf}\left(\frac{x_c}{\sqrt{2}}\right)$$
- Kink: “Truly” BG-free at  
 $-\ln[\operatorname{erf}(3/\sqrt{2})] = 0.0027$  cts / ROI
- Typical approximations
  - “Nearly” BG-free:  $Q_{\beta\beta} \pm 2\sigma$
  - Large, flat BG:  $Q_{\beta\beta} \pm 1.4\sigma$
  - Poor resolution:  $[Q_{\beta\beta}, Q_{\beta\beta} + 1.4\sigma]$



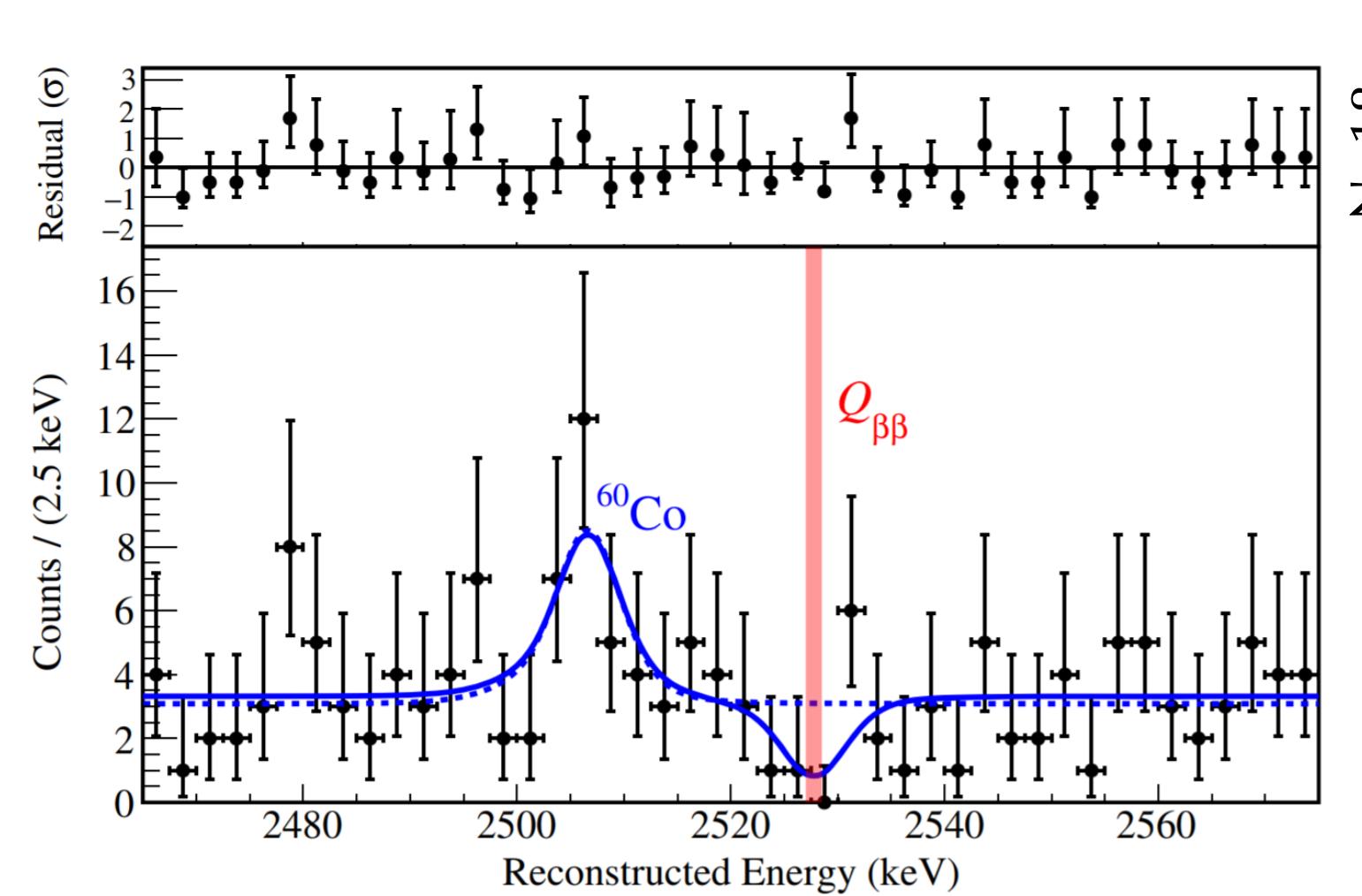
# Signal Extraction and Shape Uncertainties

- Sensitivity doesn't capture well systematic background shape uncertainties
- Several illustrative examples:

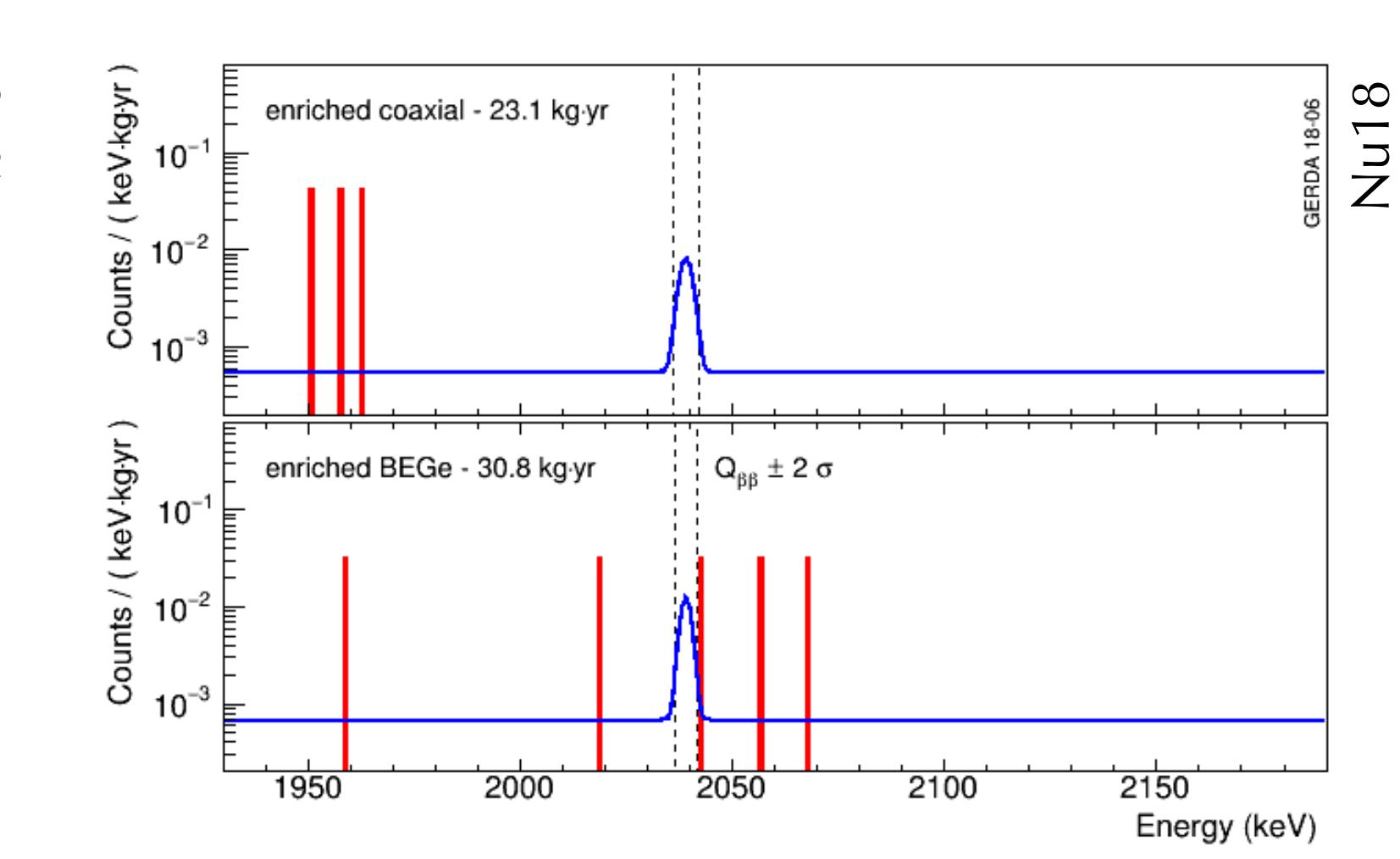
KamLAND-Zen: O(10) c/ROI, complex shape



CUORE: O(10) c/ROI, simple shape



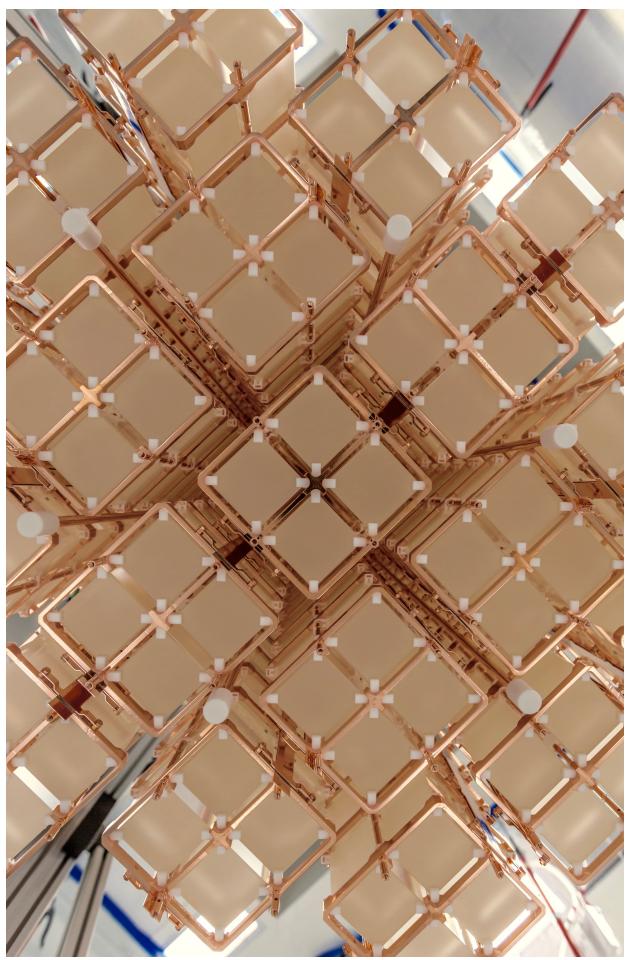
GERDA: O(0.1) c/ROI, simple shape



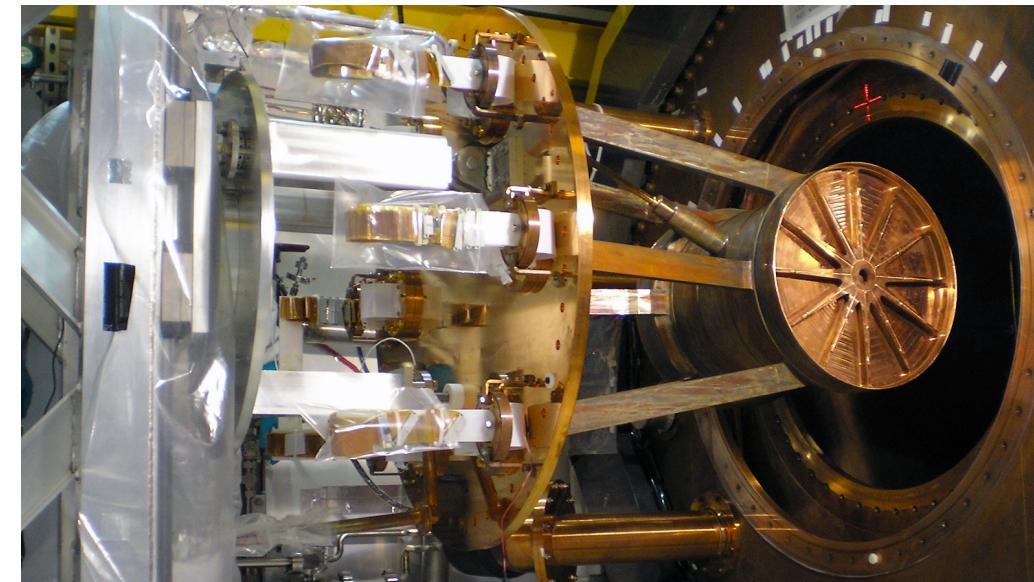
# Experimental Techniques

- Scintillators (KamLAND-Zen, SNO+, CANDLES)
  - Measure energy ( $\sigma \sim 3\text{-}10\%$ ) + position from scintillation light; some PID
- TPCs (EXO, NEXT, PandaX)
  - Collect scintillation + ionization: measure energy ( $\sigma \sim 1\text{-}3\%$ ) + tracks / position + PID
- Bolometers (CUORE, CUPID, AMORE)
  - Measure energy ( $\sigma \sim 0.2\%$ ) from phonons; some PID
  - R&D underway for instrumenting with photon detectors for background rejection
- Semiconductors (GERDA, Majorana, COBRA, SELENA)
  - Measure energy ( $\sim 0.1\text{-}0.3\%$ ) from ionization; some PID and tracking / position sensitivity
- External detectors (NEMO, SuperNEMO, DCBA)
  - Trackers + calorimeters, measure energy ( $\sigma \sim 3\text{-}10\%$ ) + tracks / positions + PID

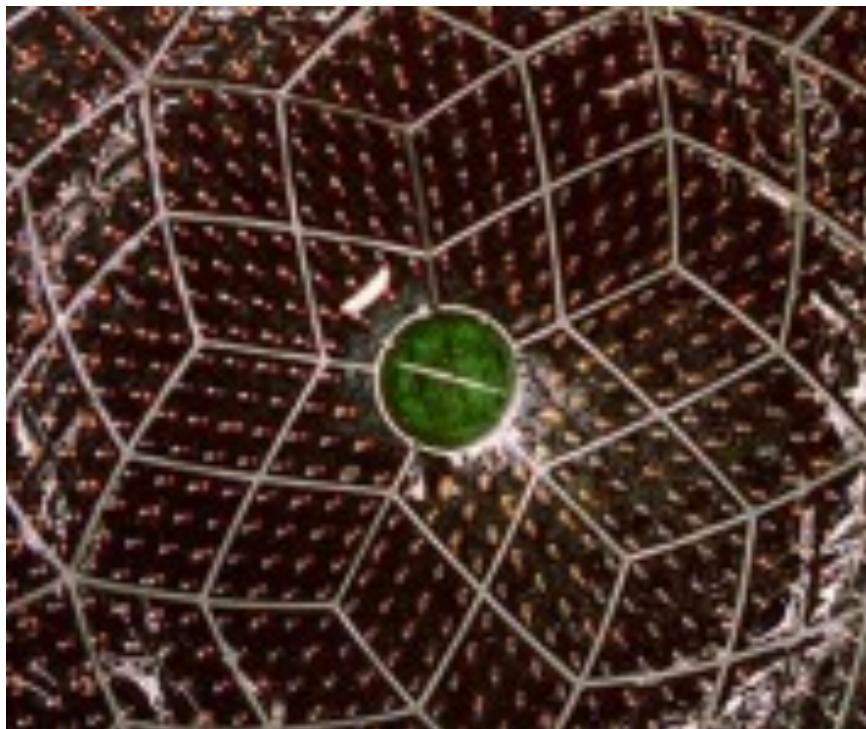
CUORE



EXO-200



KamLAND-Zen



# Experiments

Collaboration	Isotope	Technique	mass ( $0\nu\beta\beta$ isotope)	Status
AMoRE	Mo-100	CaMoO <sub>4</sub> bolometers (+ scint.)	5 kg	Construction
CANDLES	Ca-48	305 kg CaF <sub>2</sub> crystals - liq. scint	0.3 kg	Operating
CARVEL	Ca-48	<sup>48</sup> CaWO <sub>4</sub> crystal scint.	16 kg	R&D
GERDA I	Ge-76	Ge diodes in LAr	15 kg	Complete
GERDA II	Ge-76	Point contact Ge in active LAr	20 kg	Operating
MAJORANA DEMONSTRATOR	Ge-76	Point contact Ge in Lead	30 kg	Operating
LEGEND 200	Ge-76	Best of GERDA + MJD	200 kg	Construction
LEGEND 1000	Ge-76	Best of GERDA + MJD	1 tonne	R&D
NEMO3	Mo-100 Se-82	Foil with tracking	6.9 kg 0.9 kg	Complete
SuperNEMO Demonstrator	Se-82	Foil with tracking	7 kg	Construction
SuperNEMO	Se-82	Foil with tracking	100 kg	R&D
COBRA	Cd-116, Te-130	CdZnTe detectors	10 kg	Operating / Construction
CUORICINO	Te-130	TeO <sub>2</sub> Bolometer	11 kg	Complete
CUORE-0	Te-130	TeO <sub>2</sub> Bolometer	11 kg	Complete
CUORE	Te-130	TeO <sub>2</sub> Bolometer	206 kg	Operating
CUPID	Several	Scintillating Bolometers	~tonne	R&D
SNO+	Te-130	0.3% <sup>nat</sup> Te in liquid scint.	800 kg	Construction
KamLAND-Zen	Xe-136	2.7% in liquid scint.	370 kg	Complete
KamLAND-Zen 800	Xe-136	2.7% in liquid scint.	750 kg	Construction
KamLAND2-ZEN	Xe-136	2.7% in liquid scint.	~tonne	R&D
NEXT-100	Xe-136	High pressure Xe TPC	10 kg	Construction
PandaX	Xe-136	2 phase Xe liquid TPC	~tonne	R&D
EXO-200	Xe-136	Xe liquid TPC	160 kg	Operating
nEXO	Xe-136	Xe liquid TPC	5 tonnes	R&D
DCBA	Nd-150	Nd foils & tracking chambers	30 kg	R&D

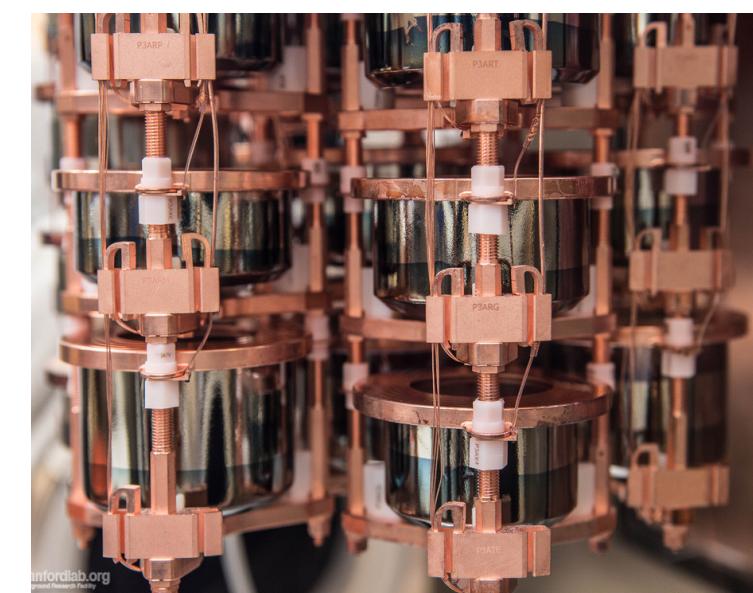
Complete

Construction

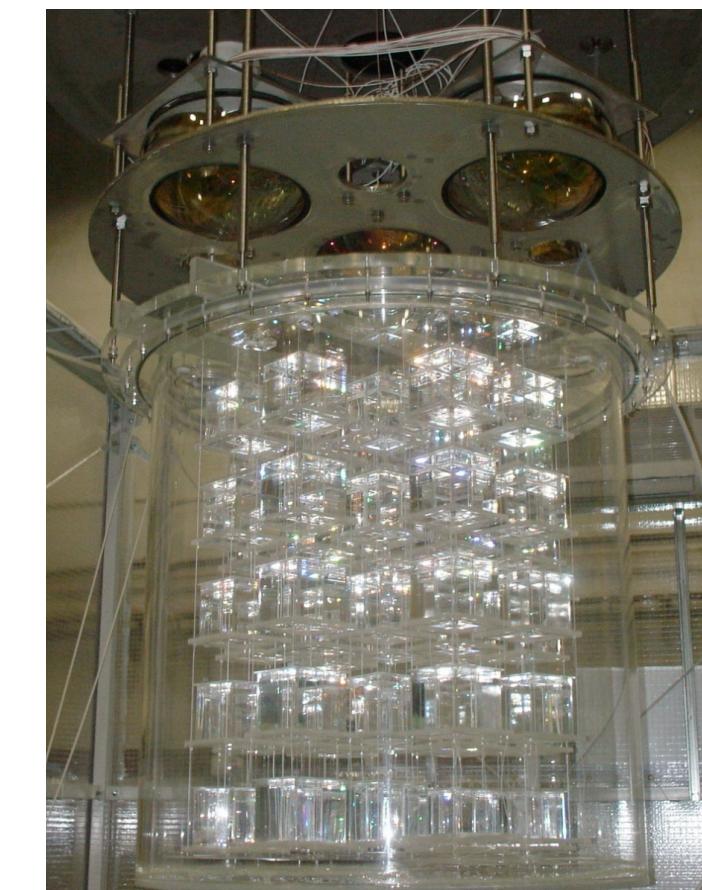
Operating



GERDA



MAJORANA



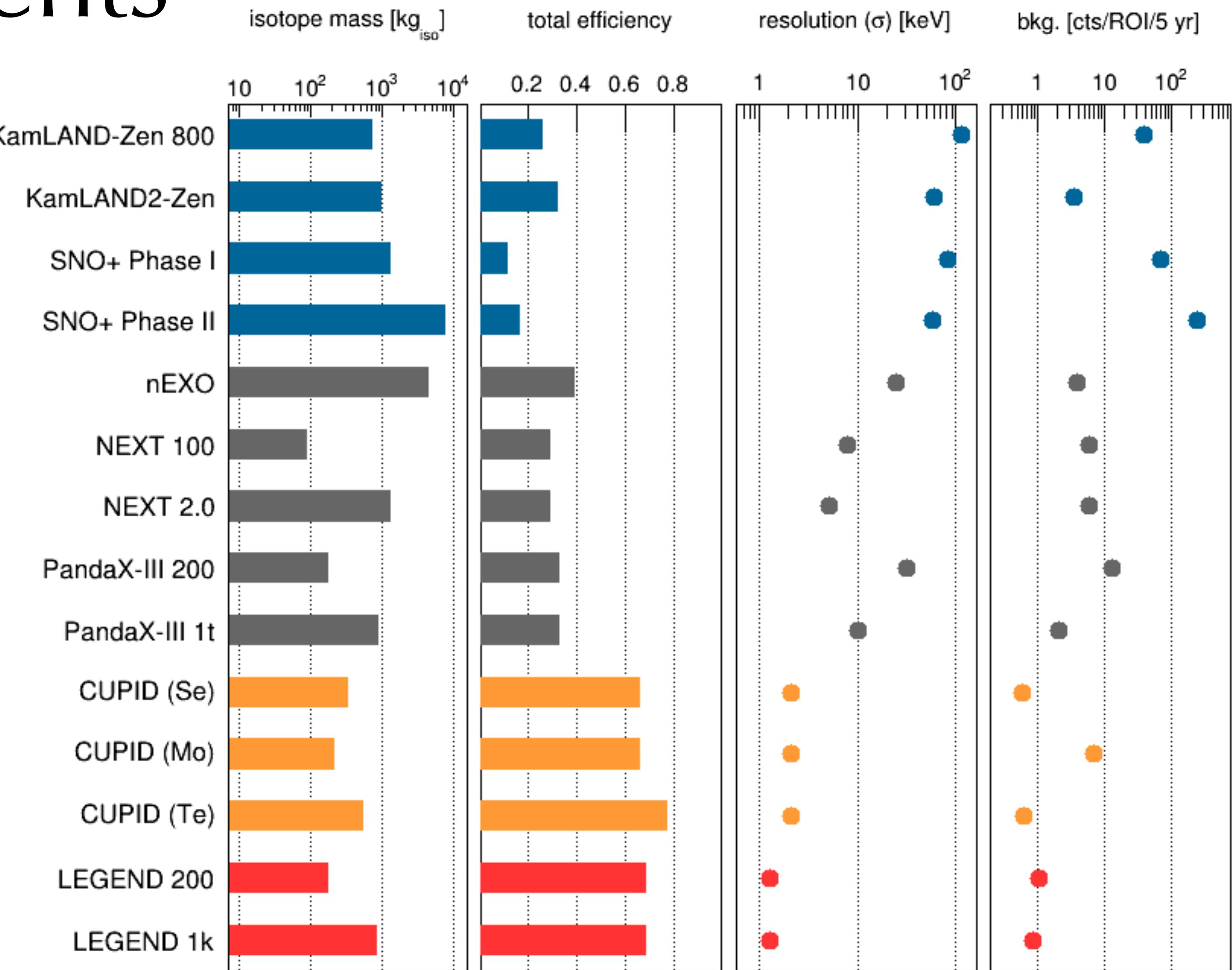
CANDLES

From J. Wilkerson

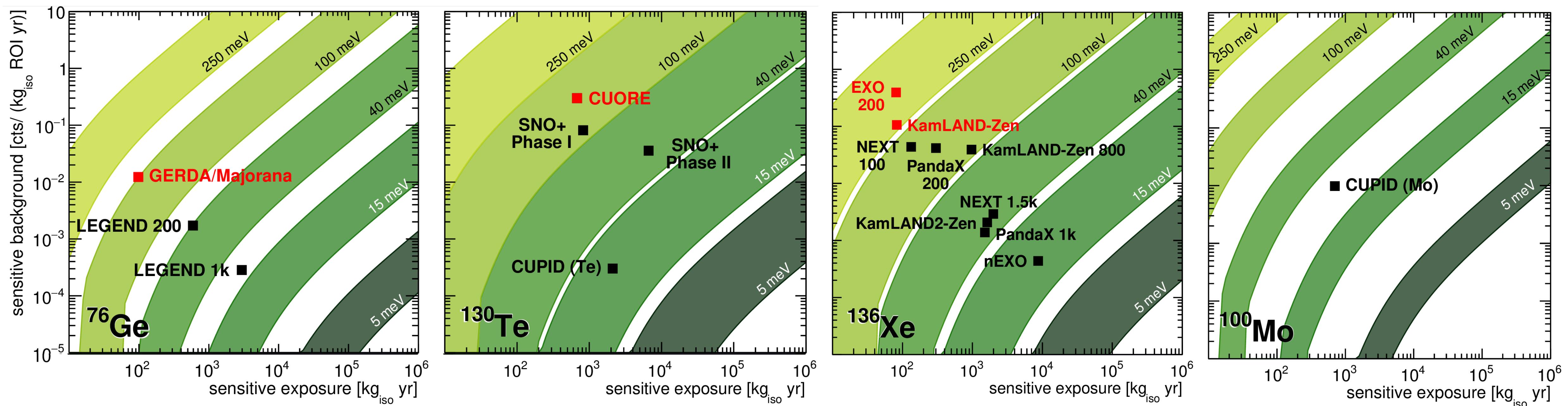
J. Detwiler

# Future Experiments

- Compiled using quoted stats in publications, presentations
- Tune sensitive exposure and sensitive background when necessary to match published sensitivities



# Discovery Sensitivity of Future Experiments



# Discovery Probability

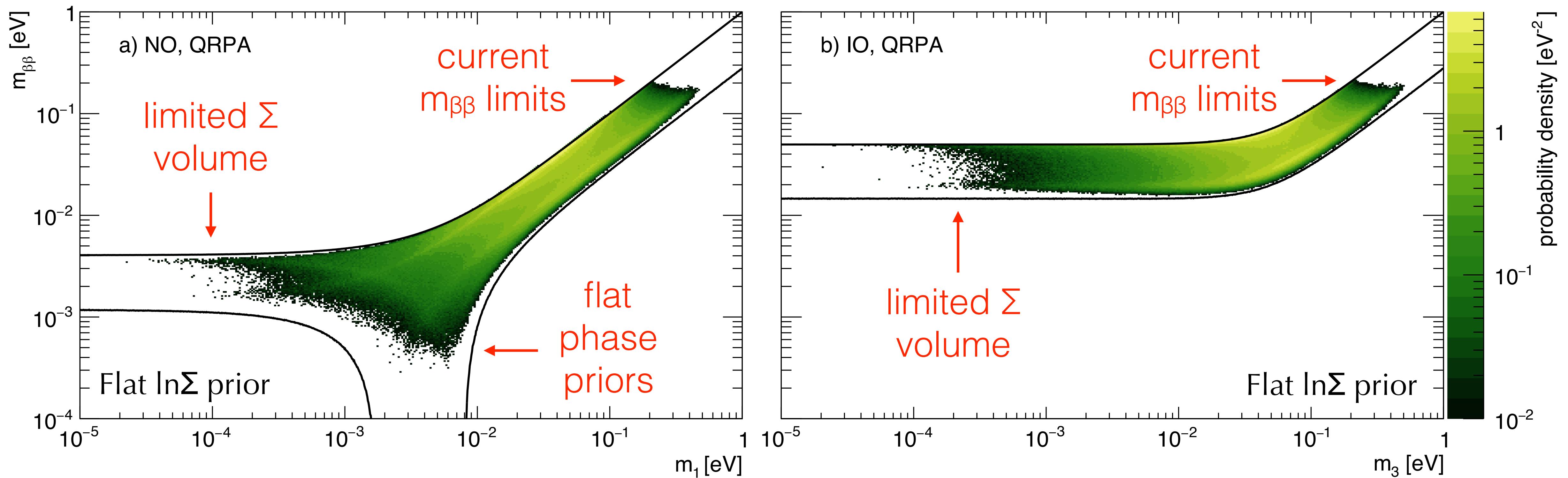
*What are the chances that these next-generation experiments will make a discovery?  
How much should humanity invest in  $0\nu\beta\beta$ ?*

- Bayesian methods are the only tools available by which such a “value” question can be approached:
  - Quantify the “volume” in the available parameter space (assign priors). Equal volumes = equal relative probability of discovery
  - Compute the amount of volume left to be explored (apply constraints from available measurements)
  - Compute the fraction of the remaining volume that will be explored by next-generation experiments. This is the “discovery probability” (DP).
- Equivalent / technical description:
  - Compute the posterior PDF for  $m_{\beta\beta}$  given all experiments to date, and use it as a prior for next-generation experiments
  - For each value of  $m_{\beta\beta}$ , compute the probability that a next-generation experiment will make a  $3\sigma$  discovery. Then sum up those probabilities weighted by the  $m_{\beta\beta}$  PDF.

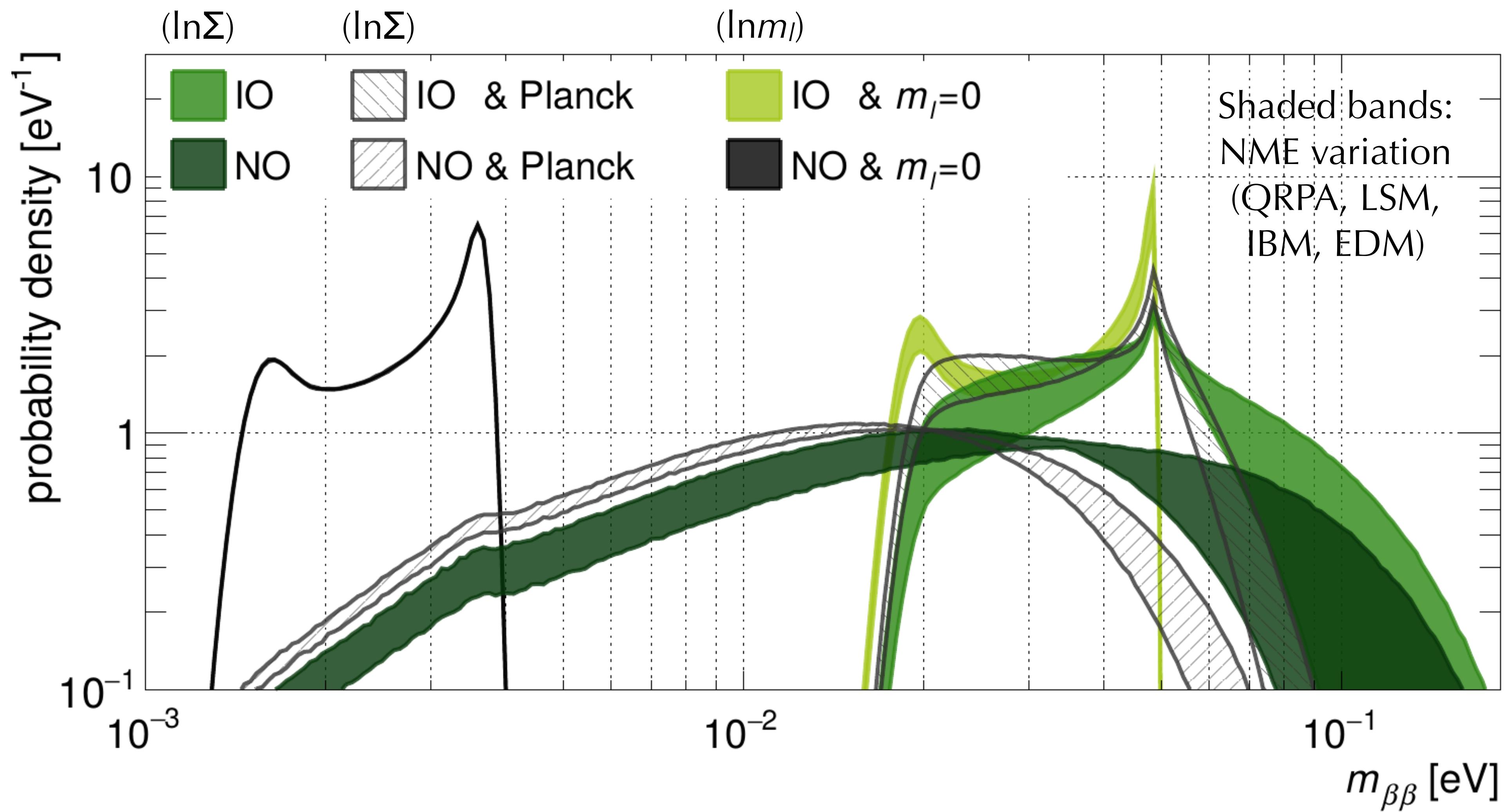
# Priors and Basis

- Neutrino mass scale is unknown: use log-flat prior for all mass parameters
- Angles and phases: use flat prior in  $[0, 2\pi]$
- Constrain with all available data: NuFit (osc.),  $\beta$ -decay,  $\beta\beta$ -decay
- Evaluate for multiple NME, with/without  $g_A$  quenching, with/without cosmological limits
- Basis choice:  $\Sigma$  vs.  $m_I$ 
  - $m_I$ : represents theoretical prejudice for the hierarchical scenario  $m_I \ll m_2$ . Results are trivial: DP  $\sim 100\%$  for IO, and  $< \sim\text{few}\%$  for NO
  - $\Sigma$ : represents theoretical prejudice that neutrino masses are generated by a different mechanism than the other SM fermions
  - We choose  $\Sigma$  as our “reference” basis. One can re-weight our results according to his or her own prejudice for this vs. extreme hierarchical scenarios

# $m_{\beta\beta}$ PDF

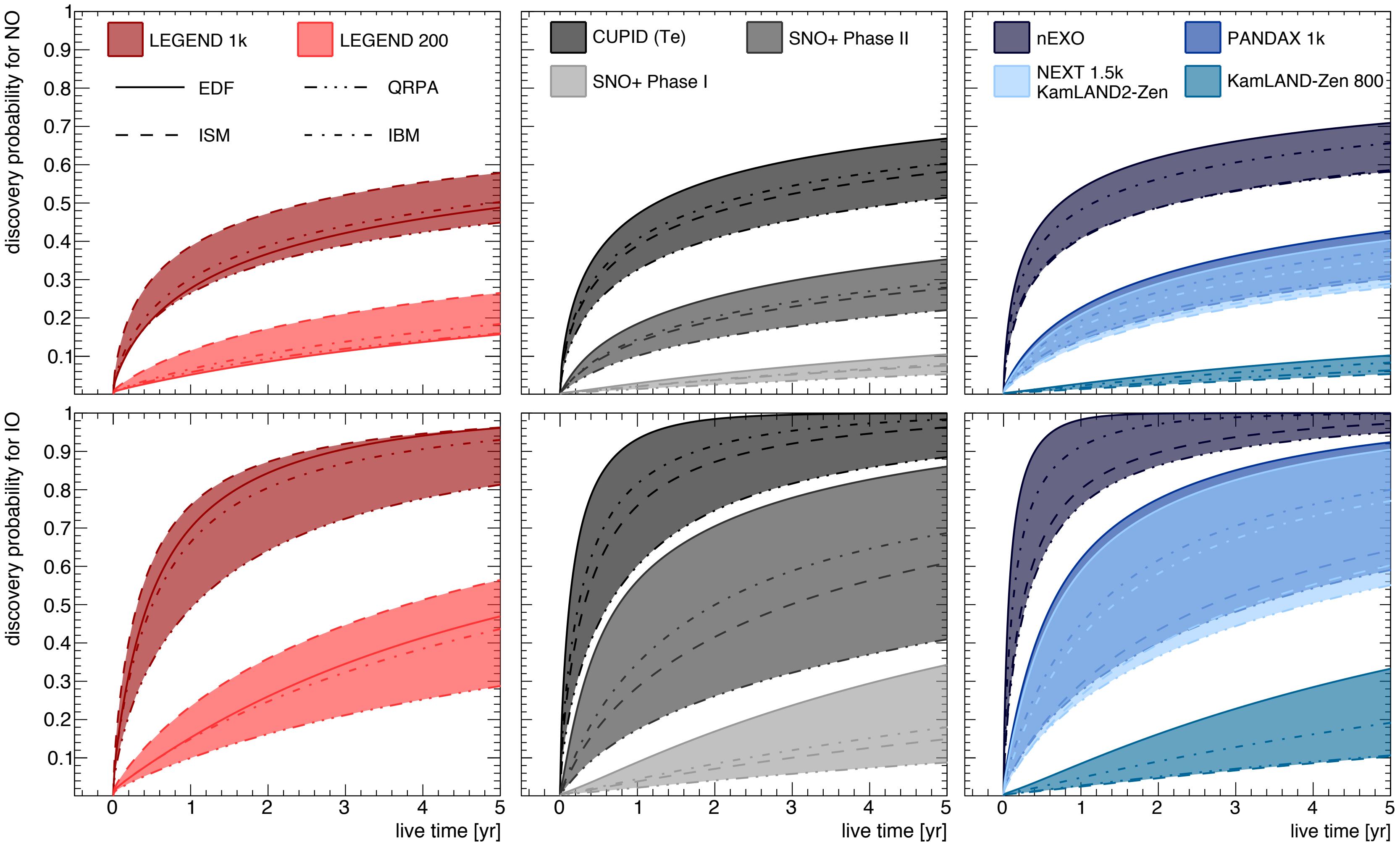


# $m_{\beta\beta}$ PDF



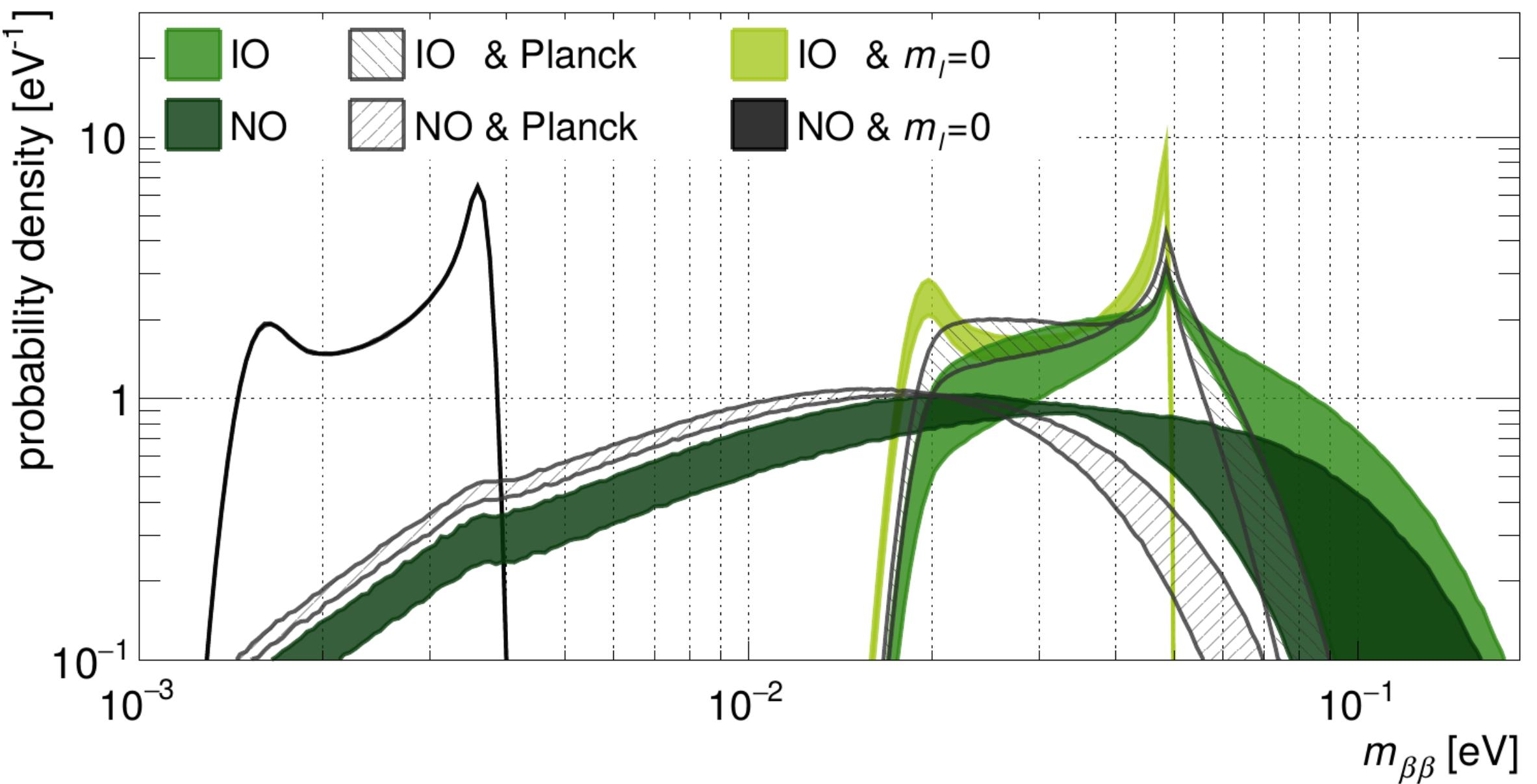
# Discovery Probabilities

- Fold  $m_{\beta\beta}$  PDF with discovery sensitivity
- These plots: flat  $\ln \Sigma$  prior
- Flat  $\ln m_l$  prior:
  - IO ~unchanged
  - NO  $\rightarrow$  ~few%



# Impact of $g_A$ Quenching

- $g_A$  quenching could be up to tens of percent: could suppress  $T_{1/2}$  by  $g_A^2$  or  $g_A^4$ , depending on the model
- Might be partially mitigated by higher  $q^2$  in virtual exchange loop
- Sensitivity is suppressed accordingly. But would also relax current  $0\nu\beta\beta$  limits
- Phase degeneracy gives larger posterior at higher  $m_{\beta\beta}$ : affect on discovery probability is weak until degradation reaches the main peak



# Alternative Analyses (flat $\ln \Sigma$ )

- Adding 30%  $g_A$  quenching: DP drops by only  $\sim 15\%$  ( $25\%$ ) for IO (NO)
- Adding cosmological constraints: NO DP reduced by  $\sim 30\%$ . No effect for IO.
- Both cosmological limits +  $g_A$  quenching: Planck rules out the region opened up at high  $m_{\beta\beta}$  from relaxed GERDA / KLZ limits. IO DP drops to  $\sim 50\%$ , NO DP drops to 10-20%.
- If KATRIN sees a positive signal: DP  $\rightarrow 100\%$  regardless of ordering, mass model, NME, quenching, cosmology.

Many scenarios have significant discovery probability for either mass ordering!

# Summary

- Promising future  $0\nu\beta\beta$  experiments must have high sensitive exposure with low sensitive background
- Proposed experiments balance exposure and background using different techniques in different nuclei with different systematics
- These experiments have good discovery probability: discovery may be just around the corner!

# Backup

