

$$S = \xi M \xi + \xi^\dagger M \xi^\dagger = \mathcal{O}(\phi^0) - \frac{1}{2f^2} (2\phi M \phi + \phi\phi M + M\phi\phi) + \mathcal{O}(\phi^4)$$