

# $\Lambda(1405)$ as a hadronic molecule



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# Contents



## Introduction

- Structure of “unstable” resonance?



## Structure of $\Lambda(1405)$ resonance

- Accurate  $\bar{K}N$  scattering amplitude

Y. Ikeda, T. Hyodo, W. Weise, PLB 706, 63 (2011); NPA 881, 98 (2012);

P.A. Zyla, et al. (Particle Data Group), PTEP 2020, 083C01 (2020)

Y. Kamiya, T. Hyodo, K. Morita, A. Ohnishi, W. Weise. PRL124, 132501 (2020)

T. Hyodo, M. Niijima, arXiv: 2010.07592 [hep-ph]

-  $\bar{K}N$  compositeness

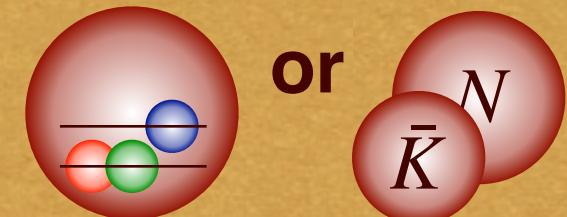
Y. Kamiya, T. Hyodo, PRC93, 035203 (2016); PTEP2017, 023D02 (2017)

T. Hyodo, JPS journal Vol. 75 No. 8, 478 (2020)

T. Kinugawa, T. Hyodo, in preparation



## Summary



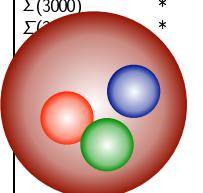
or

# Observed hadrons (2018)

## PDG 2018 edition

<http://pdg.lbl.gov/>

$p$	$1/2^+$	****	$\Delta(1232)$	$3/2^+$	****	$\Sigma^+$	$1/2^+$	****	$\Xi^0$	$1/2^+$	****	$\Lambda_c^+$	$1/2^+$	****
$n$	$1/2^+$	****	$\Delta(1600)$	$3/2^+$	***	$\Sigma^0$	$1/2^+$	****	$\Xi^-$	$1/2^+$	****	$\Lambda_c(2595)^+$	$1/2^-$	***
$N(1440)$	$1/2^+$	****	$\Delta(1620)$	$1/2^-$	***	$\Sigma^-$	$1/2^+$	****	$\Xi(1530)$	$3/2^+$	****	$\Lambda_c(2625)^+$	$3/2^-$	***
$N(1520)$	$3/2^-$	***	$\Delta(1700)$	$3/2^-$	***	$\Sigma(1385)$	$3/2^+$	***	$\Xi(1620)$	*		$\Lambda_c(2765)^+$	*	
$N(1535)$	$1/2^-$	***	$\Delta(1750)$	$1/2^+$	*	$\Sigma(1480)$	*		$\Xi(1690)$		***	$\Lambda_c(2880)^+$	$5/2^+$	***
$N(1650)$	$1/2^+$	***	$\Delta(1900)$	$1/2^-$	**	$\Sigma(1560)$	**		$\Xi(1820)$	$3/2^-$	***	$\Lambda_c(2940)^+$		***
$N(1675)$	$5/2^-$	***	$\Delta(1905)$	$5/2^+$	****	$\Sigma(1580)$	$3/2^-$	*	$\Xi(1950)$		***	$\Sigma_c(2455)$	$1/2^+$	****
$N(1680)$	$5/2^+$	***	$\Delta(1910)$	$1/2^+$	***	$\Sigma(1620)$	$1/2^-$	*	$\Xi(2030)$	$\geq \frac{5}{2}^?$	***	$\Sigma_c(2520)$	$3/2^+$	***
$N(1685)$	*		$\Delta(1920)$	$3/2^-$	***	$\Sigma(1660)$	$1/2^+$	***	$\Xi(2120)$	*		$\Sigma_c(2800)$		***
$N(1700)$	$3/2^-$	***	$\Delta(1930)$	$5/2^-$	***	$\Sigma(1670)$	$3/2^-$	***	$\Xi(2250)$	**		$\Xi_c^-(2645)$	$3/2^+$	***
$N(1710)$	$1/2^+$	***	$\Delta(1940)$	$3/2^-$	**	$\Sigma(1690)$	**		$\Xi(2370)$	**		$\Xi_c^-(2790)$	$1/2^-$	***
$N(1720)$	$3/2^+$	***	$\Delta(1950)$	$7/2^+$	****	$\Sigma(1730)$	$3/2^+$	*	$\Xi(2500)$	*		$\Xi_c^-(2815)$	$3/2^-$	***
$N(1860)$	$5/2^+$	**	$\Delta(2000)$	$5/2^+$	**	$\Sigma(1750)$	$1/2^-$	***	$\Xi(2500)$	*		$\Xi_c^-(2930)$	*	
$N(1875)$	$3/2^-$	***	$\Delta(2150)$	$1/2^-$	*	$\Sigma(1770)$	$1/2^+$	*	$\Omega^-$	$3/2^+$	****	$\Xi_c(2980)$		***
$N(1880)$	$1/2^+$	**	$\Delta(2200)$	$7/2^-$	*	$\Sigma(1775)$	$5/2^-$	***	$\Omega(2250)^-$		***	$\Xi_c(3055)$		***
$N(1895)$	$1/2^-$	**	$\Delta(2300)$	$9/2^+$	***	$\Sigma(1840)$	$3/2^+$	*	$\Omega(2380)^-$	**		$\Xi_c(3080)$		***
$N(1900)$	$3/2^+$	***	$\Delta(2350)$	$5/2^-$	*	$\Sigma(1880)$	$1/2^+$	**	$\Omega(2470)^-$	**		$\Xi_c(3123)$	*	
$N(1990)$	$7/2^+$	**	$\Delta(2390)$	$7/2^+$	*	$\Sigma(1900)$	$1/2^-$	*	$\Xi_c(2930)$	*		$\Omega_c^0(2770)^0$	$3/2^+$	***
$N(2000)$	$5/2^+$	**	$\Delta(2400)$	$9/2^-$	**	$\Sigma(1915)$	$5/2^+$	****	$\Xi_c(2980)$			$\Omega_c^0(2770)^0$	$3/2^+$	***
$N(2040)$	$3/2^+$	*	$\Delta(2420)$	$11/2^+$	*****	$\Sigma(1940)$	$3/2^+$		$\Xi_c(3055)$			$\Xi_{cc}^+$	*	
$N(2060)$	$5/2^-$	**	$\Delta(2750)$	$13/2^-$	**	$\Sigma(1940)$	$3/2^-$	***	$\Xi_c(3080)$			$\Xi_{cc}^0$		
$N(2100)$	$1/2^+$	*	$\Delta(2950)$	$15/2^+$	**	$\Sigma(2000)$	$1/2^-$	*	$\Xi_c(3123)$	*		$\Xi_{cc}^0$	$1/2^+$	***
$N(2120)$	$3/2^-$	**	$\Sigma(2030)$	$7/2^+$	****	$\Xi_c(2930)$			$\Xi_c(2980)$			$\Xi_{cc}^0(2770)^0$	$3/2^+$	***
$N(2190)$	$7/2^-$	****	$\Lambda$	$1/2^+$	****	$\Sigma(2070)$	$5/2^+$	*	$\Xi_c(2980)$			$\Xi_{cc}^0(2770)^0$		
$N(2220)$	$9/2^+$	****	$\Lambda(1405)$	$1/2^-$	***	$\Sigma(2080)$	$3/2^+$	**	$\Xi_c(3055)$			$\Xi_{cc}^0(2770)^0$		
$N(2250)$	$9/2^-$	****	$\Lambda(1520)$	$3/2^-$	***	$\Sigma(2100)$	$7/2^-$	*	$\Xi_c(3080)$			$\Xi_{cc}^0(2770)^0$		
$N(2300)$	$1/2^+$	**	$\Lambda(1600)$	$1/2^+$	***	$\Sigma(2250)$		***	$\Xi_c(3123)$	*		$\Xi_{cc}^0(2770)^0$		
$N(2570)$	$5/2^-$	**	$\Lambda(1670)$	$1/2^-$	***	$\Sigma(2455)$		**	$\Xi_c(2980)$			$\Xi_{cc}^0(2770)^0$		
$N(2600)$	$11/2^-$	***	$\Lambda(1690)$	$3/2^-$	***	$\Sigma(2620)$		**	$\Xi_c(3055)$			$\Xi_{cc}^0(2770)^0$		
$N(2700)$	$13/2^+$	**	$\Lambda(1710)$	$1/2^+$	*	$\Sigma(3000)$	*		$\Xi_c(3080)$			$\Xi_{cc}^0(2770)^0$		
$\Lambda(1800)$	$1/2^-$	***	$\Sigma(3000)$	*	*	$\Xi_c(3123)$	*		$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$		
$\Lambda(1810)$	$1/2^+$	***	$\Sigma(3000)$	*	*	$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$		
$\Lambda(1820)$	$5/2^+$	****	$\Sigma(3000)$	*	*	$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$		
$\Lambda(1830)$	$5/2^-$	***	$\Sigma(3000)$	*	*	$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$		
$\Lambda(1890)$	$3/2^+$	***	$\Sigma(3000)$	*	*	$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$		
$\Lambda(2000)$	*		$\Sigma(3000)$	*	*	$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$		
$\Lambda(2020)$	$7/2^+$	*	$\Sigma(3000)$	*	*	$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$		
$\Lambda(2050)$	$3/2^-$	*	$\Sigma(3000)$	*	*	$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$		
$\Lambda(2100)$	$7/2^-$	***	$\Sigma(3000)$	*	*	$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$		
$\Lambda(2110)$	$5/2^+$	***	$\Sigma(3000)$	*	*	$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$		
$\Lambda(2325)$	$3/2^-$	*	$\Sigma(3000)$	*	*	$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$		
$\Lambda(2350)$	$9/2^+$	***	$\Sigma(3000)$	*	*	$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$		
$\Lambda(2585)$	*		$\Sigma(3000)$	*	*	$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$			$\Xi_{cc}^0(2770)^0$		



155 baryons

LIGHT UNFLAVORED ( $S = C = B = 0$ )		STRANGE ( $S = \pm 1, C = B = 0$ )		CHARMED, STRANGE ( $C = S = \pm 1$ )		$\bar{c} \bar{c} f(f^C)$		
$\bullet \pi^\pm$	$1^-(0^-)$	$\bullet \phi(1680)$	$0^-(1^-)$	$\bullet K^\pm$	$1/2(0^-)$	$\bullet D_s^\pm$	$0(0^-)$	
$\bullet \pi^0$	$1^-(0^-)$	$\bullet \rho_3(1690)$	$1^+(3^-)$	$\bullet K^0$	$1/2(0^-)$	$\bullet D_s^\pm$	$0(?^?)$	
$\bullet \eta$	$0^+(0^-)$	$\bullet \rho(1700)$	$1^+(1^-)$	$\bullet K_S^0$	$1/2(0^-)$	$\bullet D_{s0}(2317)^\pm$	$0(0^+)$	
$\bullet f_0(500)$	$0^+(0^-)$	$\bullet \omega(1700)$	$2^+(2^-)$	$\bullet \rho_2(1700)$	$1/2(0^-)$	$\bullet D_3(2460)^\pm$	$0(1^-)$	
$\bullet \rho(770)$	$1^+(1^-)$	$\bullet f_0(1710)$	$0^+(1^-)$	$\bullet K'_0(800)$	$1/2(0^+)$	$\bullet D_2(2536)^\pm$	$0(1^+)$	
$\bullet \eta'(958)$	$0^+(0^-)$	$\bullet \eta(1760)$	$0^+(0^-)$	$\bullet K'(892)$	$1/2(1^-)$	$\bullet D_s(2700)^\pm$	$0(1^-)$	
$\bullet f_0(980)$	$0^+(0^-)$	$\bullet f_2(1810)$	$0^+(2^+)$	$\bullet K_1(1270)$	$1/2(1^+)$	$\bullet D_{s1}(2860)^\pm$	$0(?^?)$	
$\bullet \rho_0(980)$	$1^-(0^-)$	$\bullet \chi(1835)$	$?^-(?^-)$	$\bullet K_2(1400)$	$1/2(1^+)$	$\bullet D_s(3040)^\pm$	$0(?^?)$	
$\bullet \omega(1020)$	$0^-(0^-)$	$\bullet \chi(1840)$	$?^-(?^?)$	$\bullet K_3(1430)$	$1/2(2^+)$	<th data-cs="2" data-kind="parent">BOTTOM (<math>B = \pm 1</math>)</th> <th data-kind="ghost"></th>	BOTTOM ( $B = \pm 1$ )	
$\bullet h_1(1170)$	$0^-(1^-)$	$\bullet \phi_3(1850)$	$0^-(3^-)$	$\bullet K_4(1460)$	$1/2(0^-)$	$\bullet B^\pm$	$1/2(0^-)$	
$\bullet b_1(1235)$	$1^+(1^-)$	$\bullet \rho_3(1870)$	$0^+(2^-)$	$\bullet K_5(1530)$	$1/2(0^-)$	$\bullet B^0$	$1/2(0^2)$	
$\bullet a_1(1260)$	$1^-(1^-)$	$\bullet \rho_2(1900)$	$1^+(1^-)$	$\bullet K_6(1650)$	$1/2(1^+)$	$\bullet B^+ / \text{ADMIXTURE}$	$B^+ / B^-$	
$\bullet f_0(1280)$	$0^+(1^-)$	$\bullet f_2(1910)$	$0^+(2^+)$	$\bullet K_7(1680)$	$1/2(1^-)$	$\bullet B^0 / B^0$	$B^0 / B^-$	
$\bullet \omega(1420)$	$0^+(0^-)$	$\bullet f_2(1950)$	$0^+(2^+)$	$\bullet K_8(1700)$	$1/2(2^-)$	$\bullet B^+ / \text{ADMIXTURE}$	$B^+ / B^-$	
$\bullet f_0(1420)$	$0^+(1^-)$	$\bullet f_2(2100)$	$0^+(2^+)$	$\bullet K_9(1745)$	$1/2(4^+)$	$\bullet V_{cb}^0$	$V_{cb}^0$	
$\bullet f_0(1430)$	$0^-(1^-)$	$\bullet f_2(2150)$	$0^+(2^+)$	$\bullet K_10(1770)$	$1/2(2^-)$	$\bullet V_{ub}^0$	$V_{ub}^0$	
$\bullet a_0(1450)$	$1^-(0^-)$	$\bullet \rho_2(2170)$	$0^-(1^-)$	$\bullet K_11(1820)$	$1/2(2^-)$	$\bullet B^0$	$1/2(1^-)$	
$\bullet \rho_0(1450)$	$1^+(1^-)$	$\bullet f_2(2200)$	$0^+(2^+)$	$\bullet K_12(1830)$	$1/2(2^-)$	$\bullet B_1(5721)^\pm$	$1/2(1^-)$	
$\bullet f_0(1500)$	$0^+(0^-)$	$\bullet \eta(2225)$	$0^+(0^-)$	$\bullet K_13(1840)$	$1/2(4^-)$	$\bullet B_2(5732)^\pm$	$?^?(?)$	
$\bullet f_1(1510)$	$0^+(1^-)$	$\bullet \rho_2(2250)$	$1^+(3^-)$	$\bullet K_14(1880)$	$1/2(2^-)$	$\bullet B_3(5747)^\pm$	$1/2(2^+)$	
$\bullet f_0(1565)$	$0^+(2^+)$	$\bullet f_2(2300)$	$0^+(4^+)$	$\bullet K_15(1920)$	$1/2(2^-)$	$\bullet B_4(5749)^\pm$	$1/2(2^+)$	
$\bullet \omega(1570)$	$1^+(1^-)$	$\bullet f_2(2330)$	$0^+(4^+)$	$\bullet K_16(1955)$	$1/2(2^-)$	$\bullet B_5(5750)^\pm$	$0(2^+)$	
$\bullet h_1(1595)$	$0^-(1^-)$	$\bullet f_2(2340)$	$0^+(2^+)$	$\bullet K_17(1990)$	$1/2(2^-)$	$\bullet B_6(5850)^\pm$	$?^?(?)$	
$\bullet \omega_1(1600)$	$0^-(1^-)$	$\bullet \rho_2(2380)$	$1^+(5^-)$	<th data-cs="2" data-kind="parent">BOTTOM, CHARMED (<math>B = C = \pm 1</math>)</th> <th data-kind="ghost"></th>	BOTTOM, CHARMED ( $B = C = \pm 1$ )			
$\bullet a_1(1640)$	$1^-(1^-)$	$\bullet \rho_2(2450)$	$1^-(6^+)$	$\bullet D_1(2400)^\pm$	$1/2(0^+)$	$\bullet B_7^+$	$0(0^-)$	
$\bullet f_2(1640)$	$0^+(2^+)$	$\bullet \rho_2(2450)$	$0^+(5^+)$	$\bullet D_2(2420)^\pm$	$1/2(1^+)$	$\bullet B_8^+$	$0(2^+)$	
$\bullet \nu_2(1645)$	$0^+(2^+)$	$\bullet \rho_2(2450)$	$0^+(5^+)$	$\bullet D_3(2420)^\pm$	$1/2(2^+)$	$\bullet B_9^+$	$0(0^-)$	
$\bullet \omega_2(1650)$	$0^-(1^-)$	$\bullet \rho_2(2450)$	$0^+(5^+)$	$\bullet D_4(2420)^\pm$	$1/2(2^+)$	$\bullet B_{10}^+$	$?^?(?)$	
$\bullet \omega_3(1670)$	$0^-(1^-)$	$\bullet \rho_2(2450)$	$0^+(5^+)$	$\bullet D_5(2460)^\pm$	$1/2(2^+)$	$\bullet B_{11}^+$	$0(1^-)$	
$\bullet \omega_2(1670)$	$1^-(1^-)$			$\bullet D_6(2460)^\pm$	$1/2(2^+)$	$\bullet B_{12}^+$	$0(1^-)$	
				$\bullet D_7(2460)^\pm$	$1/2(2^+)$	$\bullet B_{13}^+$	$0(1^-)$	
				$\bullet D_8(2460)^\pm$	$1/2(2^+)$	$\bullet B_{14}^+$	$0(1^-)$	
				$\bullet D_9(2460)^\pm$	$1/2(2^+)$	$\bullet B_{15}^+$	$0(1^-)$	
				$\bullet D_{10}(2460)^\pm$	$1/2(2^+)$	$\bullet B_{16}^+$	$0(1^-)$	
				$\bullet D_{11}(2460)^\pm$	$1/2(2^+)$	$\bullet B_{17}^+$	$0(1^-)$	
				$\$				

# Observed hadrons (2020)

PDG 2020 edition

<http://pdg.lbl.gov/>

0	1/2+ ****	$\Lambda(1232)$	3/2+ ****	$\Sigma^+$	1/2+ ****	$\Xi^0$	1/2+ ****	$\Xi^{++}$	***
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LIGHT UNFLAVORED	STRANGE	CHARMED, STRANGE	c $\bar{c}$ continued
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Only color singlet states are observed.

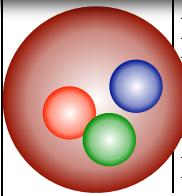
→ Color confinement problem

Flavor quantum numbers are described by  $qqq/q\bar{q}$ .

Why no  $qq\bar{q}\bar{q}$ ,  $qqqq\bar{q}\bar{q}$ , ... states (exotic hadrons)?

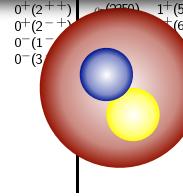
→ Exotic hadron problem, as nontrivial as confinement!

$\Lambda(1820)$	5/2+ ****	$\Xi_c^0(2645)$	3/2+ ***
$\Lambda(1830)$	5/2- ****	$\Xi_c^-(2790)$	1/2- ***
$\Lambda(1890)$	3/2+ ****	$\Xi_c^-(2815)$	3/2- ***
$\Lambda(2000)$	1/2- *	$\Xi_c^0(2930)$	**
$\Lambda(2050)$	3/2- *	$\Xi_c^0(2970)$	***
$\Lambda(2070)$	3/2+ *	$\Xi_c^0(3055)$	***
$\Lambda(2080)$	5/2- *	$\Xi_c^0(3080)$	***
$\Lambda(2085)$	7/2+ **	$\Xi_c^0(3123)$	*
$\Lambda(2100)$	7/2- ****	$\Xi_c^0(3270)$	1/2+ ***
$\Lambda(2110)$	5/2+ ***		
$\Lambda(2325)$	3/2- *		
$\Lambda(2350)$	9/2+ ***		
$\Lambda(2585)$	**		



162 baryons

$f_0(1640)^0$	0+(2+-)	$f_0(2050)^0$	1+(5-)	$D_0^*(2310)^0$	1/2(0+)	$B_{s2}^*(5360)^0$	0(2-)	$h_b(1P)$	0-(1+-)
$\star_{1/2}(1645)$	0+(2+-)	$D_s(2310)^0$	1/2(?)	$D_1(2420)^0$	1/2(1+)	$B_{s2}^*(5360)^0$	0(2-)	$\star_{1/2}(1P)$	0+(2++)
$\star_{3/2}(1650)$	0-(1-)	$D_s(2310)^{\pm}$	1/2(1+)	$D_1(2420)^{\pm}$	1/2(1+)	$\eta_b(2S)$	0+(0-+)	$\eta_b(2S)$	0-(1--)
$\star_{-3/2}(1670)$	0-(3-)	$D_s(2460)^0$	1/2(2+)	$D_1(2460)^0$	1/2(2+)	$\star_{3/2}(1D)$	0-(2-)	$\star_{3/2}(1D)$	0-(2-)
		$D_s(2460)^{\pm}$	1/2(2+)	$D_1(2460)^{\pm}$	1/2(2+)	$\chi_{bc}(2P)$	0+(0++)	$\chi_{bc}(2P)$	0+(1++)
		$D(2550)^0$	1/2(?)	$D_s(2550)^0$	1/2(?)	$\chi_{bc}(2S)^0$	0(0-)	$\chi_{bc}(2S)$	0(0-)
		$D(2640)^0$	1/2(?)	$D_s(2600)^0$	1/2(?)	$\chi_{bc}(2P)^0$	0+(1++)	$\chi_{bd}(2P)$	0+(1++)
		$D(2640)^{\pm}$	1/2(2+)	$D_s(2740)^0$	1/2(2?)	$\chi_{bd}(2S)^0$	0+(0++)	$\chi_{bd}(2S)$	0+(0++)
		$D(2740)^0$	1/2(?)	$D_s(2740)^0$	1/2(?)	$\chi_{bd}(2P)^0$	0+(1-)	$\chi_{bd}(2P)$	0+(1-)
		$D_s(2780)^0$	1/2(3-)	$D_s(2830)^0$	1/2(?)	$\chi_{bd}(3S)^0$	0+(1-)	$\chi_{bd}(3S)$	0+(1-)
		$D(3000)^0$	1/2(?)	$D_s(3000)^0$	1/2(?)	$\chi_{bd}(3P)^0$	0+(1++)	$\chi_{bd}(3P)$	0+(1++)



209 mesons

All ~ 370 hadrons emerge from single QCD Lagrangian.

# Unstable states via strong interaction

## Stable/unstable hadrons

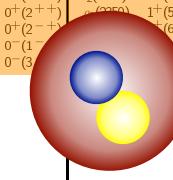
<http://pdg.lbl.gov/>

$p$	$1/2^+$ ****	$\Delta(1232)$	$3/2^+$ ****	$\Sigma^+$	$1/2^+$ ****	$\Xi^0$	$1/2^+$ ****	$\Xi_{cc}^{++}$	***
$n$	$1/2^+$ ***	$\Delta(1600)$	$3/2^-$ ***	$\Sigma^0$	$1/2^+$ ***	$\Xi^-$	$1/2^+$ ***	$\Lambda_b^0$	$1/2^+$ ***
$N(1440)$	$1/2^+$ ***	$\Delta(1620)$	$1/2^-$ ***	$\Sigma^-$	$1/2^+$ ***	$\Xi(1530)$	$3/2^+$ ***	$\Lambda_b^0$	$1/2^+$ ***
$N(1520)$	$3/2^-$ ***	$\Delta(1700)$	$3/2^-$ ***	$\Sigma(1885)$	$3/2^+$ ***	$\Xi(1620)$	*	$\Lambda_b(5912)^0$	$1/2^-$ ***
$N(1535)$	$1/2^-$ ***	$\Delta(1750)$	$1/2^+$ *	$\Sigma(1850)$	$3/2^-$ *	$\Xi(1690)$	***	$\Lambda_b(5920)^0$	$3/2^-$ ***
$N(1650)$	$1/2^-$ ***	$\Delta(1900)$	$1/2^-$ ***	$\Sigma(1620)$	$1/2^+$ ***	$\Xi(1820)$	$3/2^-$ ***	$\Lambda_b(6146)^0$	$3/2^+$ ***
$N(1675)$	$5/2^-$ ***	$\Delta(1905)$	$5/2^+$ ***	$\Sigma(1660)$	$1/2^+$ ***	$\Xi(1950)$	***	$\Lambda_b(6152)^0$	$5/2^+$ ***
$N(1680)$	$5/2^+$ ***	$\Delta(1910)$	$1/2^+$ ***	$\Sigma(1670)$	$3/2^-$ ***	$\Xi(2030)$	$\geq \frac{5}{2}?$ ***	$\Sigma_b^-$	$1/2^+$ ***
$N(1700)$	$3/2^-$ ***	$\Delta(1920)$	$3/2^+$ ***	$\Sigma(1750)$	$1/2^-$ ***	$\Xi(2120)$	*	$\Sigma_b^+$	$3/2^+$ ***
$N(1710)$	$1/2^+$ ***	$\Delta(1930)$	$5/2^-$ ***	$\Sigma(1775)$	$5/2^+$ ***	$\Xi(2250)$	**	$\Sigma_b(6097)^+$	***
$N(1720)$	$3/2^+$ ***	$\Delta(1940)$	$3/2^-$ **	$\Sigma(1780)$	$3/2^+$ *	$\Xi(2370)$	**	$\Xi_b(6097)^-$	***
$N(1860)$	$5/2^+$ **	$\Delta(1950)$	$7/2^+$ ***	$\Sigma(1880)$	$1/2^+$ **	$\Xi(2500)$	*	$\Xi_b^0, \Xi_b^-$	$1/2^+$ ***
$N(1875)$	$3/2^+$ ***	$\Delta(2000)$	$5/2^+$ **	$\Sigma(1900)$	$1/2^+$ **	$\Xi(2600)$	$\Xi_b(5935)^-$	$1/2^+$ ***	
$N(1880)$	$1/2^+$ ***	$\Delta(2150)$	$1/2^-$ *	$\Sigma(1910)$	$3/2^-$ ***	$\Omega^-$	$3/2^+$ ***	$\Xi_b(5945)^0$	$3/2^+$ ***
$N(1895)$	$1/2^-$ ***	$\Delta(2200)$	$7/2^-$ ***	$\Sigma(1915)$	$5/2^+$ ***	$\Omega(2012)^?$	***	$\Xi_b(5955)^-$	$3/2^+$ ***
$N(1900)$	$3/2^+$ ***	$\Delta(2300)$	$9/2^+$ **	$\Sigma(1940)$	$3/2^+$ *	$\Omega(2250)^-$	***	$\Xi_b(6227)^-$	***
$N(1990)$	$7/2^+$ **	$\Delta(2350)$	$5/2^-$ *	$\Sigma(2010)$	$3/2^+$ *	$\Omega(2380)^-$	**	$\Omega_b^-$	$1/2^+$ ***
$N(2000)$	$5/2^+$ **	$\Delta(2390)$	$7/2^+$ ***	$\Sigma(2030)$	$7/2^+$ ***	$\Omega(2470)^-$	**	$P_c(4312)^+$	*
$N(2040)$	$3/2^+$ *	$\Delta(2400)$	$9/2^-$ **	$\Sigma(2070)$	$5/2^+$ *	$\Lambda_c^+$	$1/2^+$ ***	$P_c(4380)^+$	*
$N(2060)$	$5/2^+$ ***	$\Delta(2420)$	$11/2^+$ ***	$\Sigma(2080)$	$3/2^+$ *	$\Lambda_c(2595)^+$	$1/2^-$ ***	$P_c(4440)^+$	*
$N(2100)$	$1/2^+$ ***	$\Delta(2750)$	$13/2^-$ **	$\Sigma(2100)$	$7/2^-$ *	$\Lambda_c(2625)^+$	$3/2^-$ ***	$P_c(4457)^+$	*
$N(2120)$	$3/2^-$ ***	$\Delta(2950)$	$15/2^+$ **	$\Sigma(2230)$	$3/2^+$ *	$\Lambda_c(2765)^+$	*		
$N(2190)$	$7/2^+$ ***	$\Lambda$	$1/2^+$ ***	$\Sigma(2250)$	***	$\Lambda_c(2860)^-$	$3/2^+$ ***		
$N(2220)$	$9/2^+$ ***	$\Lambda$	$1/2^+$ ***	$\Sigma(2455)$	***	$\Lambda_c(2880)^+$	$5/2^+$ ***		
$N(2250)$	$9/2^-$ ***	$\Lambda$	$1/2^-$ **	$\Sigma(2620)$	**	$\Lambda_c(2940)^+$	$3/2^-$ ***		
$N(2300)$	$1/2^+$ **	$\Lambda(1405)$	$1/2^-$ ***	$\Sigma(3000)$	*	$\Sigma_c(2455)$	$1/2^+$ ***		
$N(2570)$	$5/2^-$ **	$\Lambda(1520)$	$3/2^-$ ***	$\Sigma(3170)$	*	$\Sigma_c(2520)$	$3/2^-$ ***		
$N(2600)$	$11/2^-$ ***	$\Lambda(1600)$	$1/2^+$ ***	$\Sigma_c(2800)$	***	$\Sigma_c(2860)$	***		
$N(2700)$	$13/2^+$ **	$\Lambda(1670)$	$1/2^-$ ***	$\Xi_c^+$	$1/2^+$ ***	$\Xi_c^0$	$1/2^+$ ***		
		$\Lambda(1690)$	$3/2^-$ ***	$\Xi_c^-$	$1/2^+$ ***	$\Xi_c^0$	$1/2^+$ ***		
		$\Lambda(1710)$	$1/2^+$ *	$\Xi_c^0$	$1/2^+$ ***	$\Xi_c^-$	$1/2^+$ ***		
		$\Lambda(1800)$	$1/2^-$ ***	$\Xi_c^+$	$1/2^+$ ***	$\Xi_c^0$	$1/2^+$ ***		
		$\Lambda(1810)$	$1/2^+$ ***	$\Xi_c^0$	$1/2^+$ ***	$\Xi_c^0$	$1/2^+$ ***		
		$\Lambda(1820)$	$5/2^+$ ***	$\Xi_c(2645)$	$3/2^+$ ***	$\Xi_c(2790)$	$1/2^-$ ***		
		$\Lambda(1830)$	$5/2^-$ ***	$\Xi_c(2790)$	$1/2^-$ ***	$\Xi_c(2815)$	$3/2^-$ ***		
		$\Lambda(1890)$	$3/2^+$ ***	$\Xi_c(2915)$	$3/2^-$ ***	$\Xi_c(2930)$	**		
		$\Lambda(2000)$	$1/2^-$ *	$\Xi_c(2930)$	**	$\Xi_c(2970)$	***		
		$\Lambda(2050)$	$3/2^-$ *	$\Xi_c(3055)$	***	$\Xi_c(3080)$	***		
		$\Lambda(2070)$	$3/2^+$ *	$\Xi_c(3123)$	*	$\Xi_c(3123)$	*		
		$\Lambda(2080)$	$5/2^-$ *						
		$\Lambda(2085)$	$7/2^+$ **						
		$\Lambda(2100)$	$7/2^-$ ***						
		$\Lambda(2110)$	$5/2^+$ ***						
		$\Lambda(2325)$	$3/2^-$ *						
		$\Lambda(2350)$	$9/2^+$ ***						
		$\Lambda(2585)$	**						



162 baryons

LIGHT UNFLAVORED ( $S = C = B = 0$ )		STRANGE ( $S = \pm 1, C = B = 0$ )		CHARMED, STRANGE ( $C = S = \pm 1$ )		$c\bar{c}$ continued $F_c(f_c)$
$\bullet \pi^\pm$	$1^- (0^-)$	$\bullet \pi_2(1670)$	$1^- (2^-)$	$\bullet K^\pm$	$1/2(0^-)$	$\bullet D_s^\pm$
$\bullet \eta^0$	$1^- (0^-)$	$\bullet \phi(1680)$	$0^- (1^-)$	$\bullet K^0$	$1/2(0^-)$	$0(0^-)$
$\bullet f_0(500)$	$0^+(0^-)$	$\bullet \rho_3(1690)$	$1^+(3^-)$	$\bullet K_S^0$	$1/2(0^-)$	$D_{s0}(2317)^{\pm}$
$\bullet \eta(770)$	$1^+ (1^-)$	$\bullet \rho_2(1700)$	$1^- (2^+)$	$\bullet K_L^0$	$1/2(0^-)$	$D_{s1}(2460)^{\pm}$
$\bullet \omega(782)$	$0^- (1^-)$	$\bullet f_0(1710)$	$0^+(0^-)$	$\bullet K_0(700)$	$1/2(0^-)$	$D_{s1}(2536)^{\pm}$
$\bullet \eta'(958)$	$0^+(0^-)$	$\bullet \pi(1760)$	$0^+(0^-)$	$\bullet K_1(1400)$	$1/2(1^+)$	$D_{s2}(2573)^{\pm}$
$\bullet f_0(980)$	$0^+(0^-)$	$\bullet \pi(1800)$	$1^- (0^-)$	$\bullet K_2(1410)$	$1/2(0^-)$	$D_{s3}(2660)^{\pm}$
$\bullet \chi_0(980)$	$1^- (0^-)$	$\bullet f_2(1810)$	$0^+(2^+)$	$\bullet K_3(1780)$	$1/2(3^-)$	$D_{s4}(3040)^{\pm}$
$\bullet \omega(1020)$	$0^-(1^-)$	$\times \chi(1835)$	$?^+(0^-)$	$\bullet K_4(1430)$	$1/2(2^+)$	
$\bullet h_1(1170)$	$0^-(1^-)$	$\times \phi(1850)$	$0^-(3^-)$	$\bullet K_5(1430)$	$1/2(2^+)$	
$\bullet b_1(1235)$	$1^+ (1^-)$	$\bullet \pi(1870)$	$0^+(2^-)$	$\bullet K_6(1460)$	$1/2(2^-)$	
$\bullet f_2(1270)$	$0^+(2^-)$	$\bullet \pi(1900)$	$1^+ (1^-)$	$\bullet K_7(1530)$	$1/2(2^-)$	
$\bullet f_1(1285)$	$0^+(1^-)$	$\bullet f_2(1910)$	$0^+(2^-)$	$\bullet K_8(1650)$	$1/2(1^+)$	
$\bullet \omega(1295)$	$0^+(0^-)$	$\bullet \alpha_1(1950)$	$1^- (0^-)$	$\bullet K_9(1690)$	$1/2(1^+)$	$B_s^-, B^0$
$\bullet \chi_0(1300)$	$1^- (0^-)$	$\bullet f_2(1950)$	$0^+(2^-)$	$\bullet K_{10}(1770)$	$1/2(2^-)$	$B_s^+, B^0/B^0$ ADMIXTURE
$\bullet \omega_2(1320)$	$1^+ (2^+)$	$\bullet \alpha_1(1970)$	$1^- (4^-)$	$\bullet K_{11}(1780)$	$1/2(3^-)$	$Z_d(4200)$
$\bullet f_0(1370)$	$0^+(0^-)$	$\times \pi(1990)$	$1^+ (3^-)$	$\bullet K_{12}(1820)$	$1/2(2^+)$	$V_d$ and $V_u$ CKM Matrix Elements
$\bullet \pi_1(1400)$	$1^- (0^-)$	$\bullet \pi(2005)$	$1^- (2^-)$	$\bullet K_{13}(1830)$	$1/2(0^-)$	$\bullet B^*$
$\bullet h_1(1415)$	$0^-(1^-)$	$\bullet \pi(2020)$	$0^+(0^-)$	$\bullet K_{14}(1950)$	$1/2(0^+)$	$B_s(5721)^0$
$\bullet \alpha_1(1420)$	$1^- (1^-)$	$\bullet f_0(2050)$	$0^+(4^+)$	$\bullet K_{15}(1980)$	$1/2(2^+)$	$B_s(5721)^0$
$\bullet f_1(1420)$	$0^+(1^-)$	$\bullet \pi(2120)$	$1^- (2^-)$	$\bullet K_{16}(2045)$	$1/2(4^+)$	$\bullet B_s^*(5732)$
$\bullet \omega_1(1420)$	$0^-(1^-)$	$\bullet f_0(2100)$	$0^+(0^-)$	$\bullet K_{17}(2250)$	$1/2(2^-)$	$\bullet B_s^*(5747)$
$\bullet f_2(1430)$	$0^+(2^-)$	$\bullet f_2(2150)$	$0^+(2^-)$	$\bullet K_{18}(2320)$	$1/2(3^+)$	$\bullet B_s^*(5747)^0$
$\bullet \alpha_2(1450)$	$1^- (0^-)$	$\bullet \pi(2150)$	$1^+ (1^-)$	$\bullet K_{19}(2380)$	$1/2(5^-)$	$\bullet B_s(5840)^+$
$\bullet \chi_1(1475)$	$0^+(0^-)$	$\bullet \phi(2170)$	$0^-(1^-)$	$\bullet K_{20}(2500)$	$1/2(4^-)$	$\bullet B_s(5840)^0$
$\bullet f_0(1500)$	$0^+(0^-)$	$\bullet f_2(2200)$	$0^+(2^+)$	$\bullet K_{21}(3100)$	$1/2(4^+)$	$\bullet B_s(5970)^+$
$\bullet f_1(1510)$	$0^+(1^-)$	$\bullet f_2(2220)$	$0^+(0^-)$	$\bullet K_{22}(2250)$	$1^+ (0^-)$	$\bullet B_s(5970)^0$
$\bullet f_2'(1525)$	$0^+(2^+)$	$\eta(2225)$	$0^+(0^-)$	$\bullet K_{23}(2300)$	$1^+ (3^-)$	$\bullet B_s(5970)$
$\bullet f_2(1565)$	$0^+(2^+)$	$\pi(2250)$	$1^+ (3^-)$	$\bullet K_{24}(2330)$	$0^+(2^-)$	$\bullet B_s(6070)$
$\bullet \pi_1(1570)$	$1^+ (1^-)$	$\bullet f_2(2300)$	$0^+(2^+)$	$\bullet D_0(2007)^0$	$1/2(0^-)$	$\bullet B_s(6070)$
$\bullet h_1(1595)$	$0^+ (1^-)$	$\bullet f_2(2300)$	$0^+(4^+)$	$\bullet D_1(2010)^{\pm}$	$1/2(1^-)$	$\bullet B_s(6070)$
$\bullet \pi_1(1600)$	$1^- (1^-)$	$\bullet f_2(2330)$	$0^+(0^-)$	$\bullet D_2(2420)^0$	$1/2(1^-)$	$\bullet B_s(6070)$
$\bullet \alpha_1(1640)$	$1^- (1^-)$	$\bullet f_2(2340)$	$0^+(2^+)$	$\bullet D_3(2430)^0$	$1/2(1^-)$	$\bullet B_s(6070)$
$\bullet f_2(1640)$	$0^-(1^-)$	$\bullet f_2(2350)$	$0^+(1^-)$	$\bullet D_4(2420)^{\pm}$	$1/2(2^+)$	$\bullet B_s(6070)$
$\bullet \pi_2(1645)$	$0^+(2^-)$	$\bullet f_2(2350)$	$0^+(6^+)$	$\bullet D_5(2460)^0$	$1/2(2^+)$	$\bullet B_s(6070)$
$\bullet \omega_1(1650)$	$0^-(1^-)$	$\bullet f_2(2360)$	$0^+(1^-)$	$\bullet D_6(2740)^0$	$1/2(2^+)$	$\bullet B_s(6070)$
$\bullet \alpha_3(1670)$	$0^-(3^-)$			$\bullet D_7(2780)^0$	$1/2(3^-)$	$\bullet D(2460)^0$
				$\bullet D_8(2850)^0$	$1/2(2^+)$	$\bullet D(2550)^0$
				$\bullet D_9(2600)^0$	$1/2(2^+)$	$\bullet D(2640)^0$
				$\bullet D_10(2640)^0$	$1/2(2^+)$	$\bullet D(2740)^0$
				$\bullet D_11(2780)^0$	$1/2(2^+)$	$\bullet D(2740)^0$
				$\bullet D_12(2800)^0$	$1/2(2^+)$	$\bullet D(3000)^0$

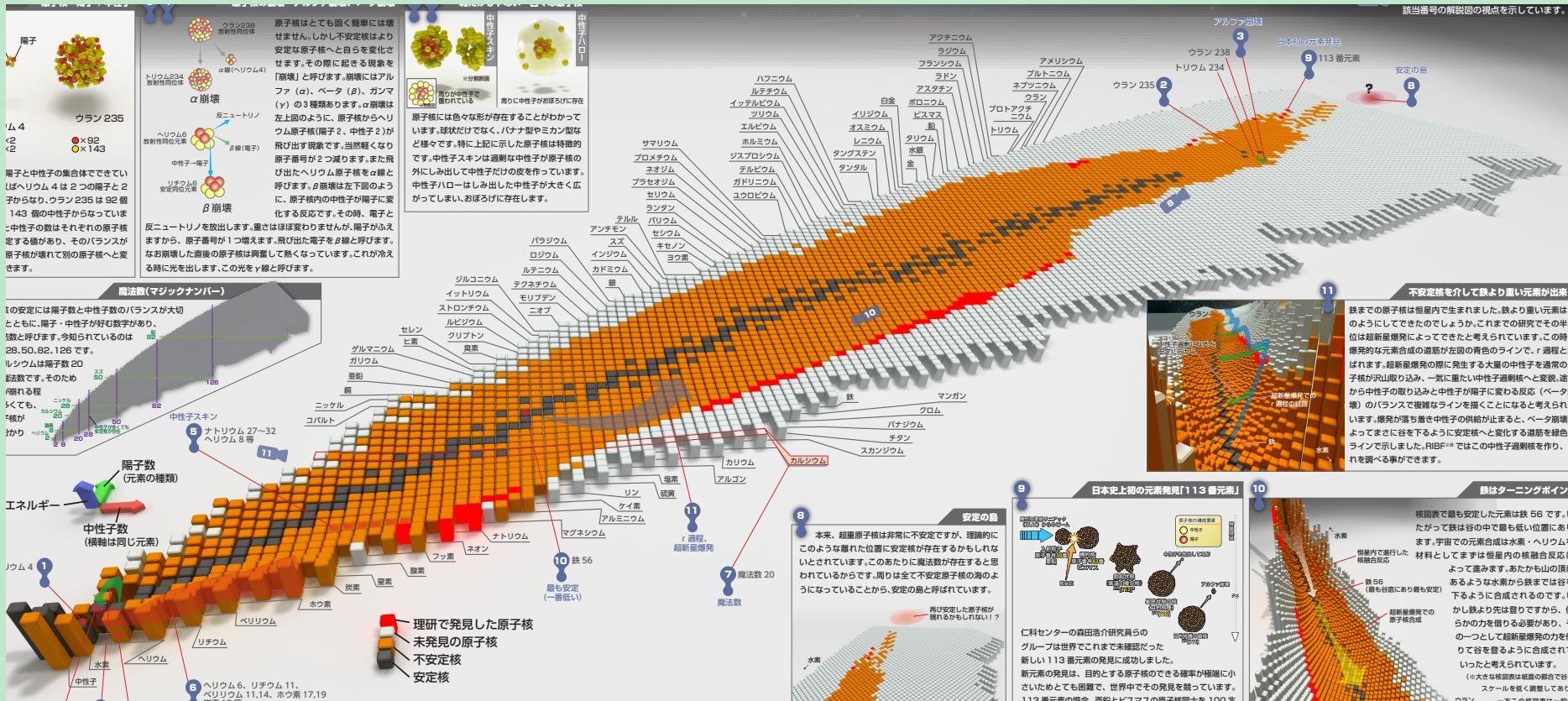


209 mesons

Most of hadrons are unstable (above two-hadron threshold)

# Relation to unstable nuclei

## Stable nuclei (~300), unstable nuclei (~2000)



<https://www.nishina.riken.jp/enjoy/kakuzu/index.html>

# Structure of unstable nuclei

- clustering, halo nuclei, Efimov effect, ...

# Nature of resonances

## Theoretical treatment for **unstable** hadrons

- **resonances** in hadron-hadron scattering
- **pole of the scattering amplitude**  $\longleftrightarrow$  “eigenstate”
- analytic continuation: unique

## Resonance as an “eigenstate” of Hamiltonian

- **complex energy**

**G. Gamow, Z. Phys. 51, 204 (1928)**

Zur Quantentheorie des Atomkernes.

Von G. Gamow, z. Zt. in Göttingen.

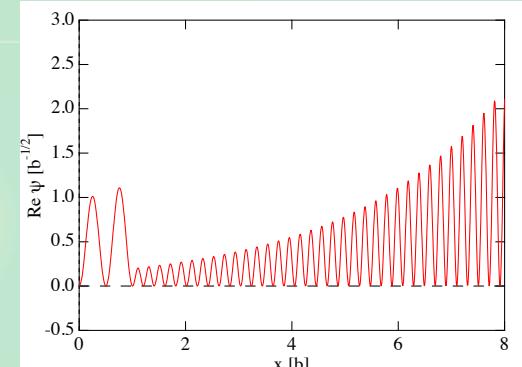
Mit 5 Abbildungen. (Eingegangen am 2. August 1928.)

Um diese Schwierigkeit zu überwinden, müssen wir annehmen, daß die Schwingungen gedämpft sind, und  $E$  komplex setzen:

$$E = E_0 + i \frac{\hbar \lambda}{4\pi},$$

wo  $E_0$  die gewöhnliche Energie ist und  $\lambda$  das Dämpfungsdekkrement (Zerfallskonstante). Dann sehen wir aber aus den Relationen (2a) und (2b),

- diverging wave function
- complex expectation value (norm,  $\langle r^2 \rangle$ )
- interpretation problem



# Contents



## Introduction

- Structure of “unstable” resonance?



## Structure of $\Lambda(1405)$ resonance

- Accurate  $\bar{K}N$  scattering amplitude

Y. Ikeda, T. Hyodo, W. Weise, PLB 706, 63 (2011); NPA 881, 98 (2012);

P.A. Zyla, et al. (Particle Data Group), PTEP 2020, 083C01 (2020);

Y. Kamiya, T. Hyodo, K. Morita, A. Ohnishi, W. Weise. PRL124, 132501 (2020);

T. Hyodo, M. Niiyama, arXiv: 2010.07592 [hep-ph]

-  $\bar{K}N$  compositeness

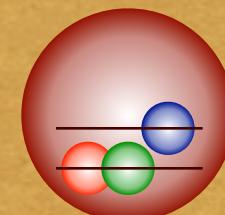
Y. Kamiya, T. Hyodo, PRC93, 035203 (2016); PTEP2017, 023D02 (2017)

T. Hyodo, JPS journal Vol. 75 No. 8, 478 (2020)

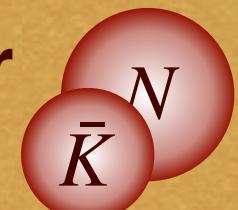
T. Kinugawa, T. Hyodo, in preparation



## Summary

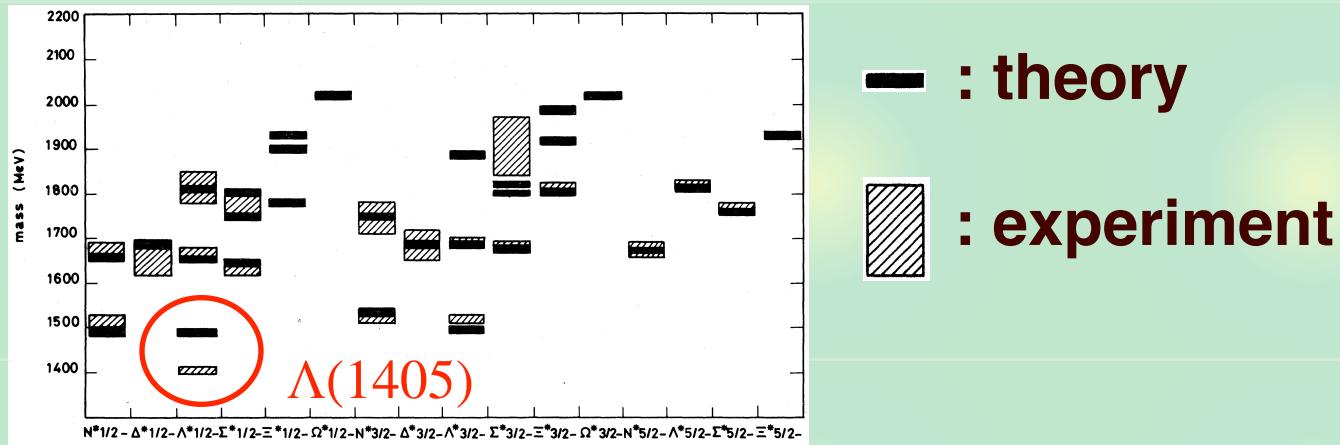
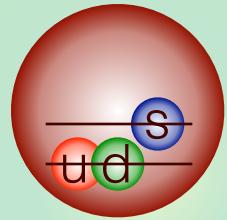


or



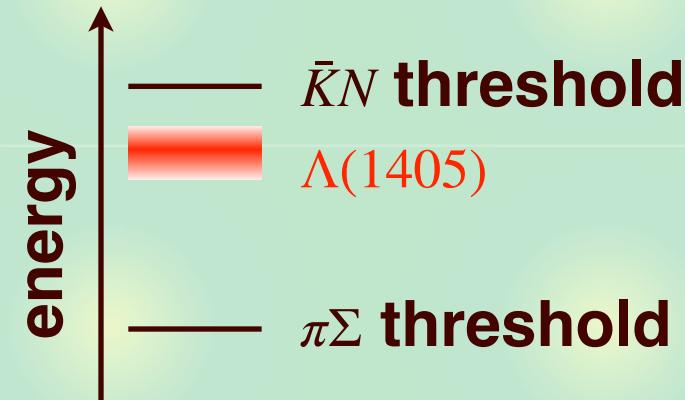
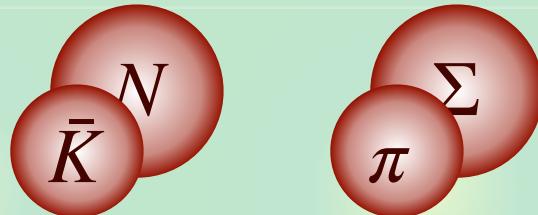
$\Lambda(1405)$  and  $\bar{K}N$  scattering $\Lambda(1405)$  does not fit in standard picture  $\rightarrow$  exotic candidate

N. Isgur and G. Karl, Phys. Rev. D18, 4187 (1978)



## Resonance in coupled-channel scattering

- coupling to MB states

Detailed analysis of  $\bar{K}N-\pi\Sigma$  scattering is necessary.

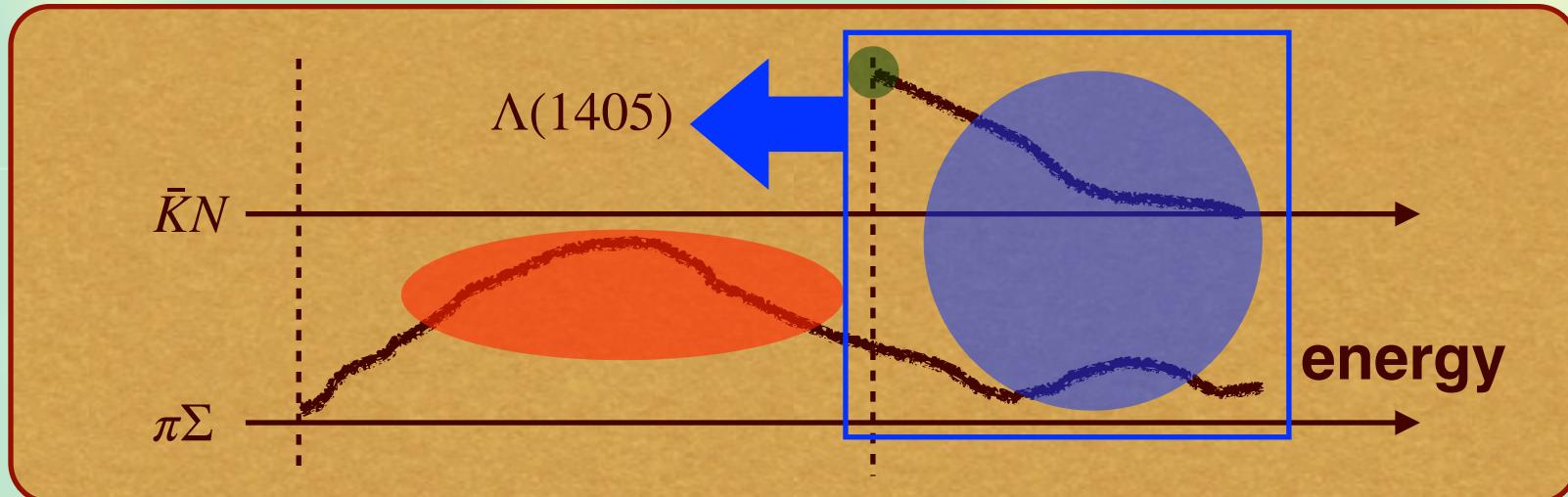
# Strategy for $\bar{K}N$ interaction

Above the  $\bar{K}N$  threshold : direct constraints

- $K^- p$  total cross sections (old data)
- $\bar{K}N$  threshold branching ratios (old data)
- $K^- p$  scattering length (new data : SIDDHARTA)

Below the  $\bar{K}N$  threshold: indirect constraints

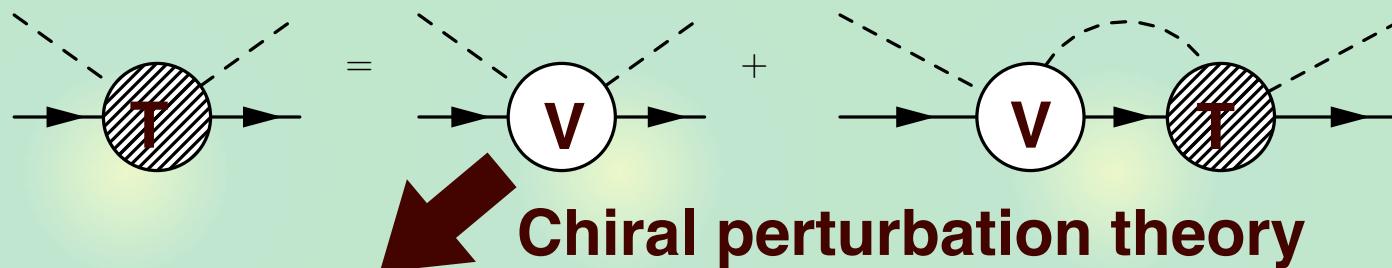
- $\pi\Sigma$  mass spectra (new data : LEPS, CLAS, HADES, ...)



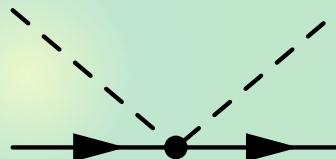
# Construction of the realistic amplitude

**Chiral SU(3) coupled-channels ( $\bar{K}N, \pi\Sigma, \pi\Lambda, \eta\Lambda, \eta\Sigma, K\Xi$ ) approach**

Y. Ikeda, T. Hyodo, W. Weise, PLB 706, 63 (2011); NPA 881 98 (2012)



1) TW term

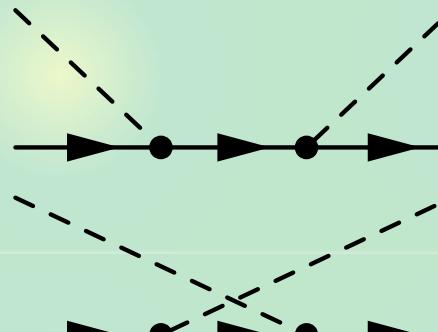


$$\mathcal{O}(p)$$

6 cutoffs

**TW model**

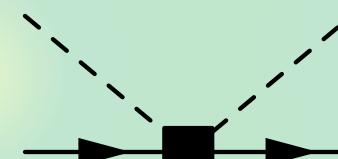
2) Born terms



$$\mathcal{O}(p)$$

**TWB model**

3) NLO terms



$$\mathcal{O}(p^2)$$

7 LECs

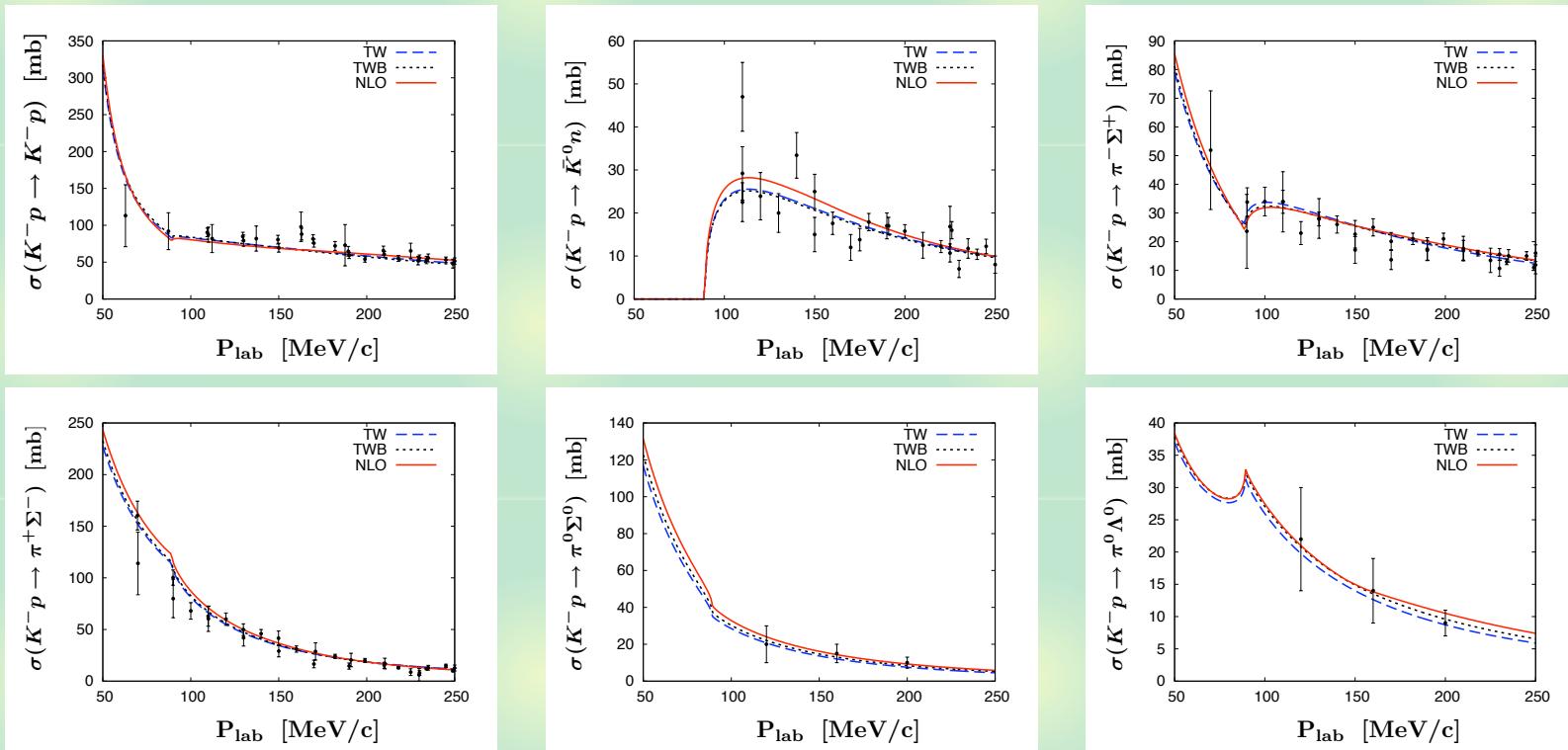
**NLO model**

## Best-fit results

 $K$  at rest

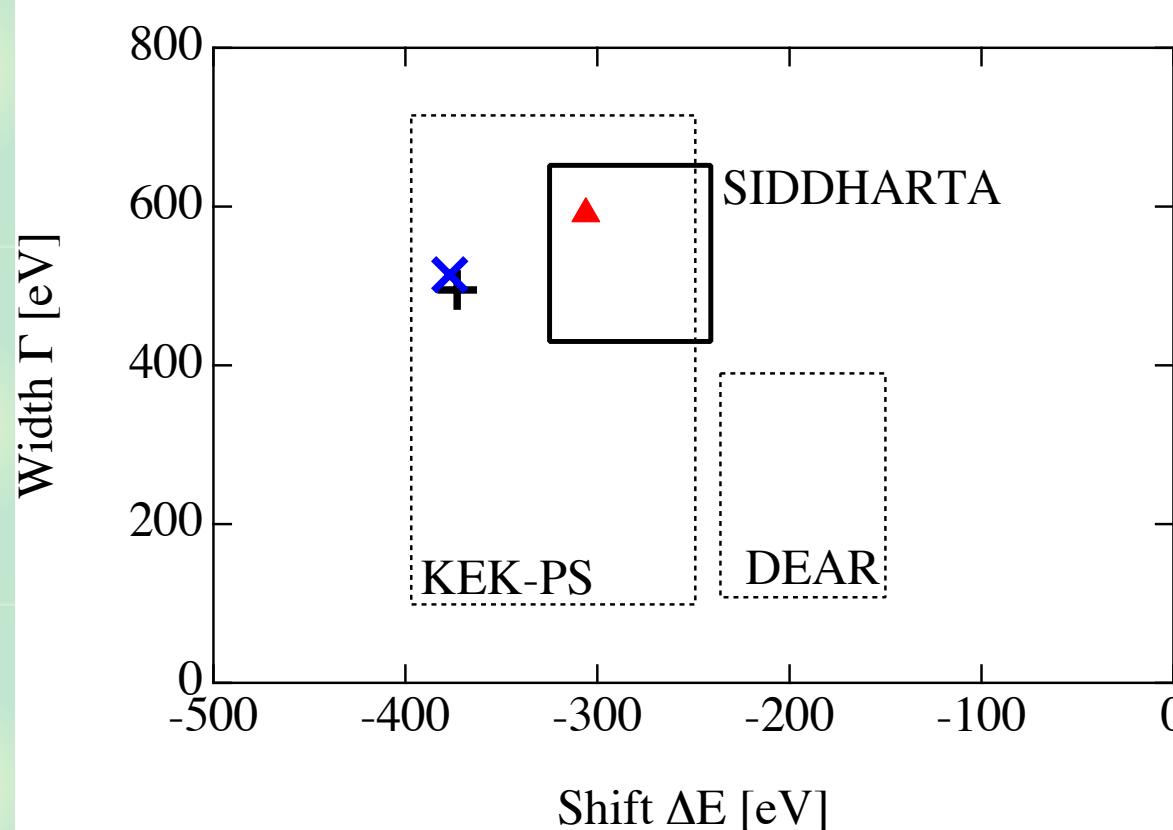
	TW	TWB	NLO	Experiment	
$\Delta E$ [eV]	373	377	306	$283 \pm 36 \pm 6$	[10]
$\Gamma$ [eV]	495	514	591	$541 \pm 89 \pm 22$	[10]
$\gamma$	2.36	2.36	2.37	$2.36 \pm 0.04$	[11]
$R_n$	0.20	0.19	0.19	$0.189 \pm 0.015$	[11]
$R_c$	0.66	0.66	0.66	$0.664 \pm 0.011$	[11]
$\chi^2/\text{d.o.f}$	1.12	1.15	0.96		

} SIDDHARTA  
} Branching ratios

 $K^- p$  cross sectionsAccurate description of all existing data ( $\chi^2/\text{d.o.f} \sim 1$ )

# Comparison with SIDDHARTA

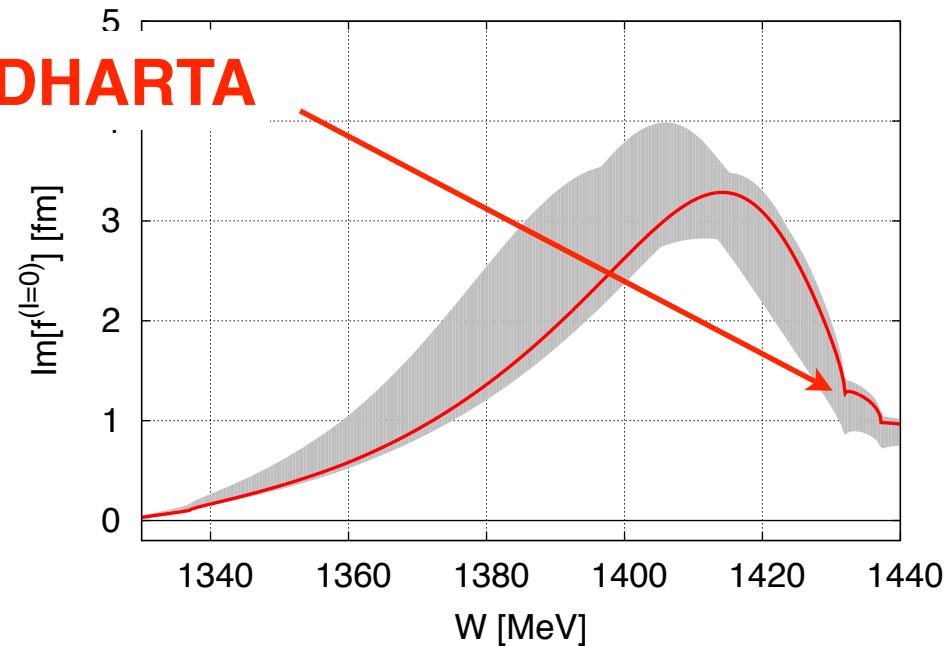
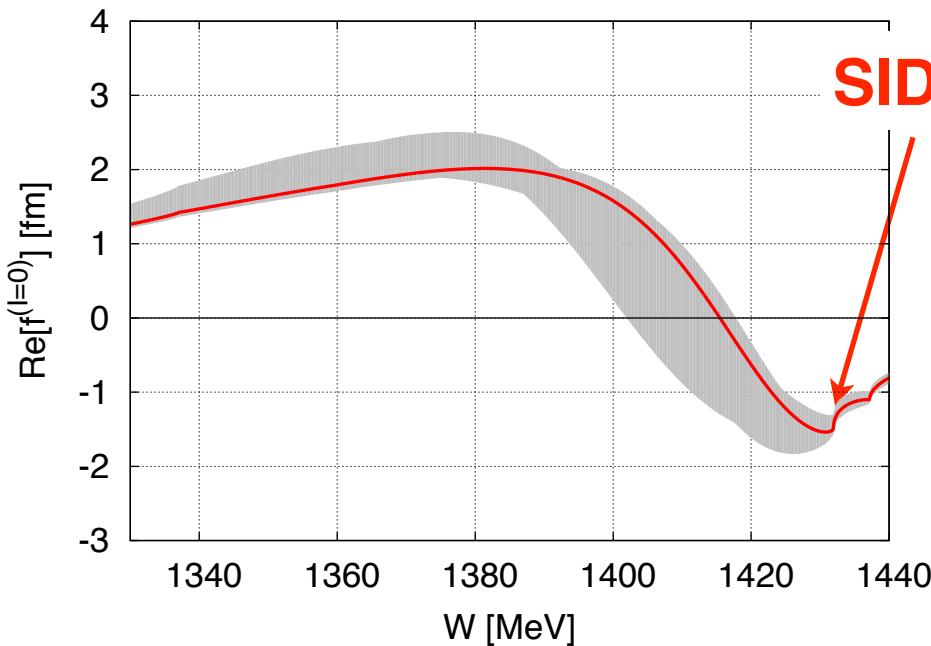
	TW	TWB	NLO
$\chi^2/\text{d.o.f.}$	1.12	1.15	0.957



**TW and TWB are reasonable, while best-fit requires NLO.**

# Subthreshold extrapolation

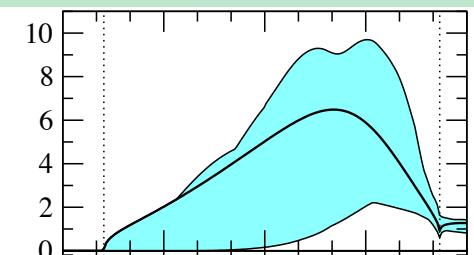
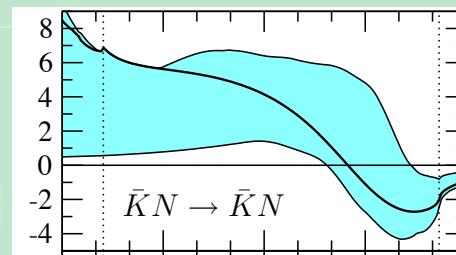
Uncertainty of  $\bar{K}N \rightarrow \bar{K}N(I = 0)$  amplitude below threshold



Y. Kamiya, K. Miyahara, S. Ohnishi, Y. Ikeda, T. Hyodo, E. Oset, W. Weise,  
NPA 954, 41 (2016)

- c.f. without SIDDHARTA

R. Nissler, Doctoral Thesis (2007)



SIDDHARTA is essential for subthreshold extrapolation.

# Extrapolation to complex energy: two poles

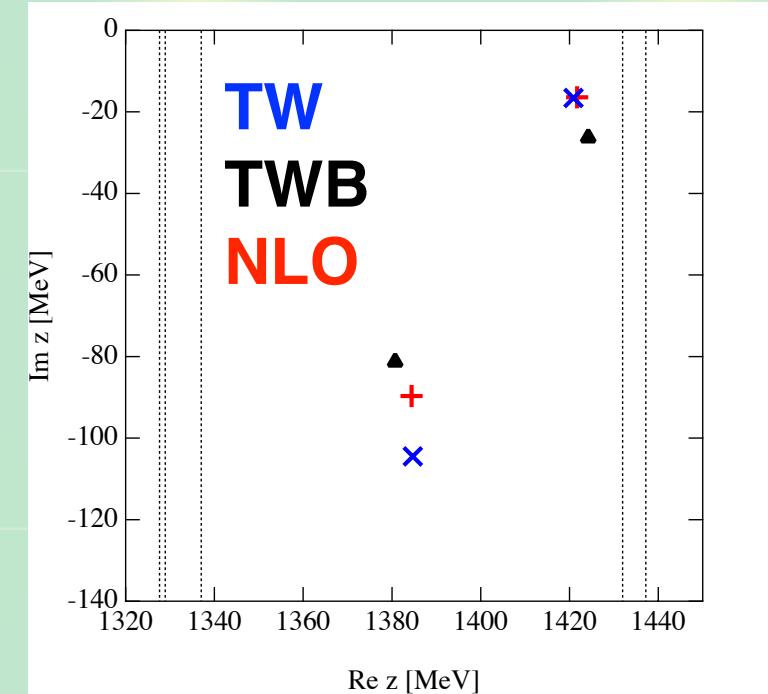
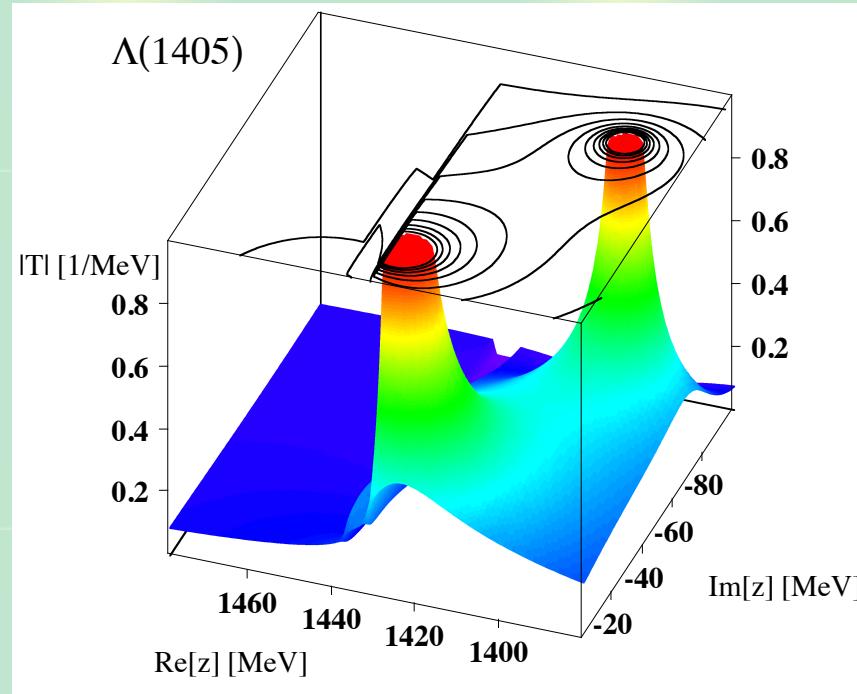
**Two poles : superposition of two eigenstates**

J.A. Oller, U.G. Meißner, PLB 500, 263 (2001);

D. Jido, J.A. Oller, E. Oset, A. Ramos, U.G. Meißner, NPA 723, 205 (2003);

U.G. Meißner, Symmetry 12, 981 (2020); M. Mai, arXiv: 2010.00056 [nucl-th];

T. Hyodo, M. Niiyama, arXiv: 2010.07592 [hep-ph]



T. Hyodo, D. Jido, Prog. Part. Nucl. Phys. 67, 55 (2012)

**NLO analysis confirms the two-pole structure.**

## PDG has changed

## 2020 update of PDG

P.A. Zyla, et al., PTEP 2020, 083C01 (2020); <http://pdg.lbl.gov/>

## - Particle Listing section:

Citation: P.A. Zyla et al. (Particle Data Group), Prog. Theor. Exp. Phys. **2020**, 083C01 (2020)

$\Lambda(1405) \frac{1}{2}^-$

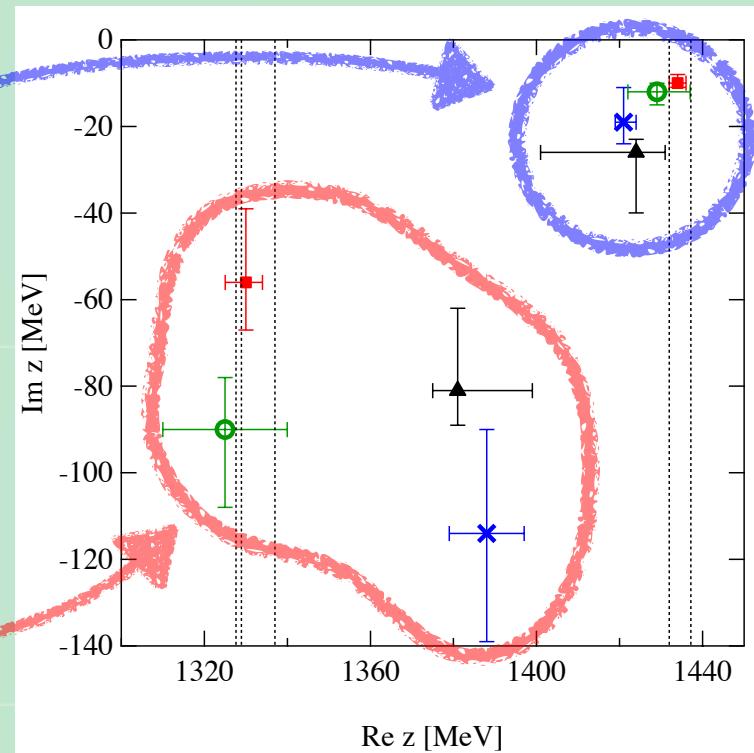
$I(J^P) = 0(\frac{1}{2}^-)$  Status: \*\*\*\*

Citation: P.A. Zyla et al. (Particle Data Group), Prog. Theor. Exp. Phys. **2020**, 083C01 (2020)

$\Lambda(1380) \frac{1}{2}^-$

$I^P = \frac{1}{2}^-$  new!

Status: \*\*



T. Hyodo, M. Niiyama, arXiv: 2010.07592 [hep-ph]

- $\Lambda(1405)$  is no longer at 1405 MeV but  $\sim 1420$  MeV.
- Lower pole: two-star resonance  $\Lambda(1380)$

# New data : $K^-p$ correlation function

## $K^-p$ total cross sections

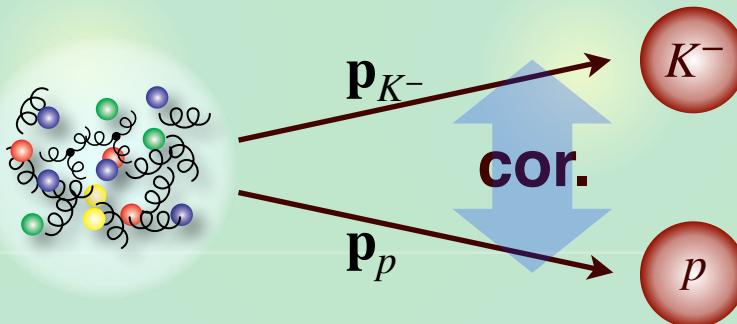
Y. Ikeda, T. Hyodo, W. Weise, PLB 706, 63 (2011)

### - Old bubble chamber data

## $K^-p$ correlation function

ALICE collaboration, PRL 124, 092301 (2020)

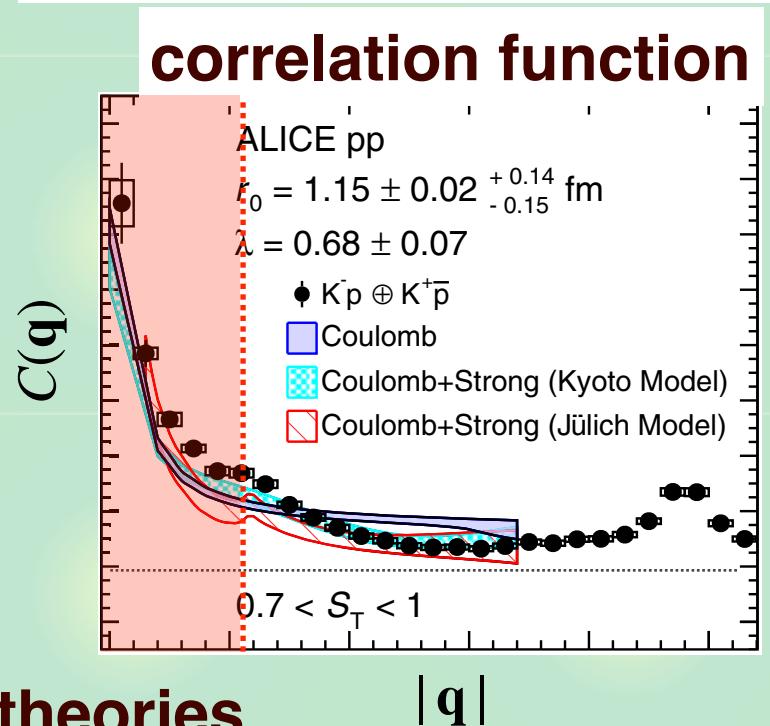
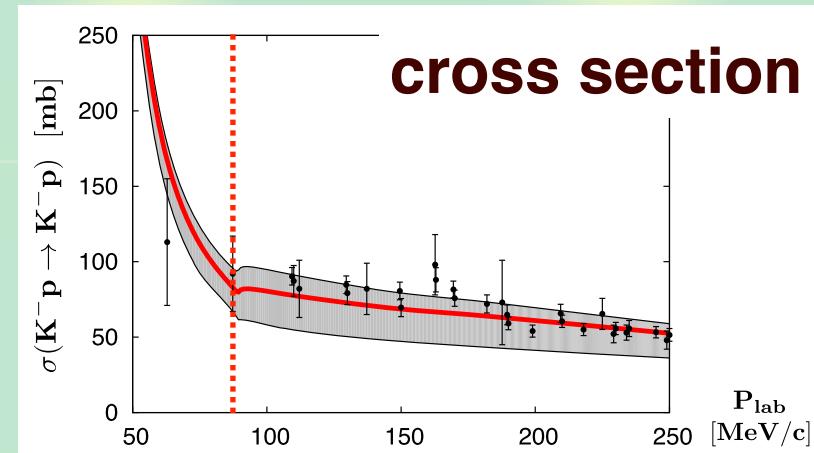
$$C(\mathbf{q}) = \frac{N_{K^-p}(\mathbf{p}_{K^-}, \mathbf{p}_p)}{N_{K^-}(\mathbf{p}_{K^-})N_p(\mathbf{p}_p)}$$



- Excellent precision ( $\bar{K}^0 n$  cusp)

- Low-energy data below  $\bar{K}^0 n$

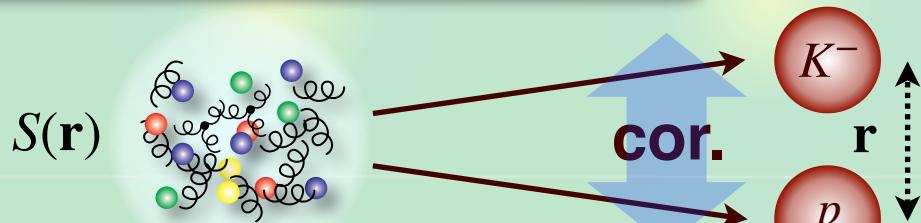
—> important constraint on  $\Lambda(1405)$  theories



# Prediction from chiral SU(3) dynamics

Theoretical calculation of  $C(q)$

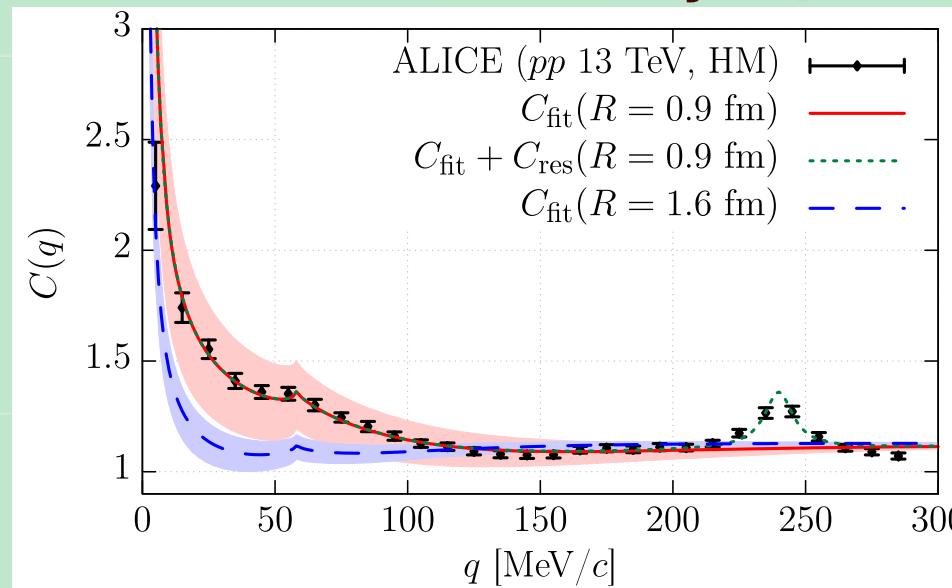
$$C(\mathbf{q}) \simeq \int d^3\mathbf{r} S(\mathbf{r}) |\Psi_{\mathbf{q}}^{(-)}(\mathbf{r})|^2$$



- wave function  $\Psi_{\mathbf{q}}^{(-)}(\mathbf{r})$  : coupled-channel  $\bar{K}N$ - $\pi\Sigma$ - $\pi\Lambda$  potential

K. Miyahara, T. Hyodo, W. Weise, PRC98, 025201 (2018)

- source function  $S(\mathbf{r})$  : determined by  $K^+p$  data



Y. Kamiya, T. Hyodo, K. Morita, A. Ohnishi, W. Weise. PRL124, 132501 (2020)

Correlation function is well reproduced.

# Contents



## Introduction

- Structure of “unstable” resonance?



## Structure of $\Lambda(1405)$ resonance

- Accurate  $\bar{K}N$  scattering amplitude

Y. Ikeda, T. Hyodo, W. Weise, PLB 706, 63 (2011); NPA 881, 98 (2012);

P.A. Zyla, et al. (Particle Data Group), PTEP 2020, 083C01 (2020)

Y. Kamiya, T. Hyodo, K. Morita, A. Ohnishi, W. Weise. PRL124, 132501 (2020)

T. Hyodo, M. Niiyama, arXiv: 2010.07592 [hep-ph]

- $\bar{K}N$  compositeness

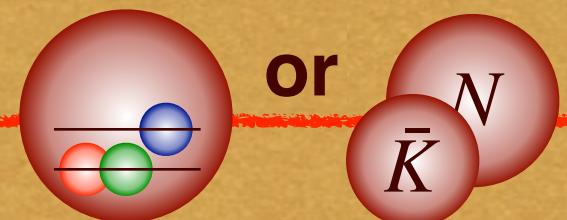
Y. Kamiya, T. Hyodo, PRC93, 035203 (2016); PTEP2017, 023D02 (2017)

T. Hyodo, JPS journal Vol. 75 No. 8, 478 (2020)

T. Kinugawa, T. Hyodo, in preparation



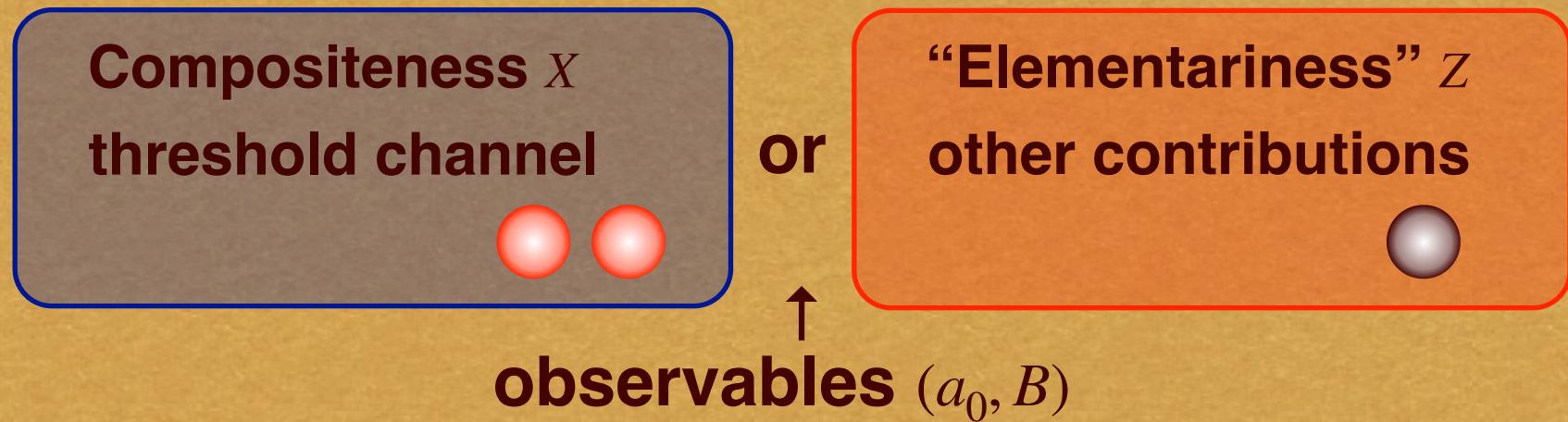
## Summary



# Compositeness of hadrons

- Structure of a given resonance (pole)?
- Weak binding relation for stable bound states

S. Weinberg, Phys. Rev. 137, B672 (1965)



- Effective field theory —> description of low-energy scattering amplitude, generalization to **unstable** resonances

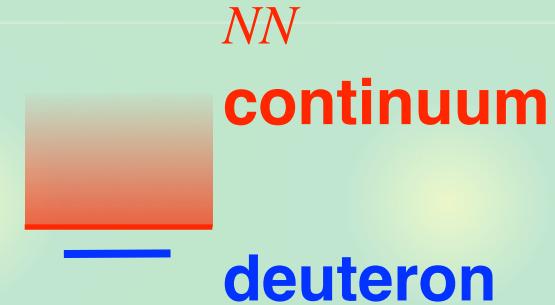
# Weak-binding relation for stable states

Compositeness  $X$  of s-wave **weakly bound state** ( $R \gg R_{\text{typ}}$ )

S. Weinberg, Phys. Rev. 137, B672 (1965);

T. Hyodo, Int. J. Mod. Phys. A 28, 1330045 (2013)

$$|d\rangle = \sqrt{X} |NN\rangle + \sqrt{1-X} |\text{others}\rangle$$



$$a_0 = R \left\{ \frac{2X}{1+X} + \mathcal{O}\left(\frac{R_{\text{typ}}}{R}\right) \right\}, \quad R = \frac{1}{\sqrt{2\mu B}}$$

- Deuteron is **NN composite** :  $a_0 \sim R \Rightarrow X \sim 1$
- Internal structure from **observable** ( $a_0, B$ )

Problem: applicable only for stable states

# Effective field theory

## Low-energy scattering with near-threshold bound state

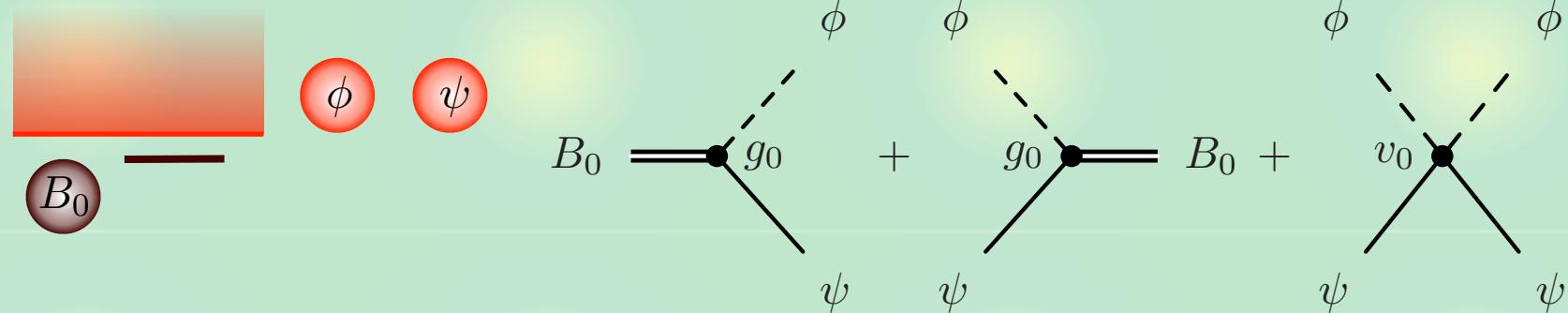
### - Nonrelativistic EFT with contact interaction

D.B. Kaplan, Nucl. Phys. B494, 471 (1997)

E. Braaten, M. Kusunoki, D. Zhang, Annals Phys. 323, 1770 (2008)

$$H_{\text{free}} = \int d\mathbf{r} \left[ \frac{1}{2M} \nabla \psi^\dagger \cdot \nabla \psi + \frac{1}{2m} \nabla \phi^\dagger \cdot \nabla \phi + \frac{1}{2M_0} \nabla B_0^\dagger \cdot \nabla B_0 + \omega_0 B_0^\dagger B_0 \right]$$

$$H_{\text{int}} = \int d\mathbf{r} \left[ g_0 (B_0^\dagger \phi \psi + \psi^\dagger \phi^\dagger B_0) + v_0 \psi^\dagger \phi^\dagger \phi \psi \right]$$



- **cutoff** :  $\Lambda \sim 1/R_{\text{typ}}$  (**interaction range of microscopic theory**)
- **At low momentum**  $p \ll \Lambda$ , **interaction  $\sim$  contact**

# Compositeness and “elementariness”

## Eigenstates

$$H_{\text{free}} |B_0\rangle = \omega_0 |B_0\rangle, \quad H_{\text{free}} |\mathbf{p}\rangle = \frac{\mathbf{p}^2}{2\mu} |\mathbf{p}\rangle$$

**free (discrete + continuum)**

$$(H_{\text{free}} + H_{\text{int}}) |B\rangle = -B |B\rangle$$

**full (bound state)**

- normalization of  $|B\rangle$  + completeness relation

$$\langle B | B \rangle = 1, \quad 1 = |B_0\rangle\langle B_0| + \int \frac{d\mathbf{p}}{(2\pi)^3} |\mathbf{p}\rangle\langle\mathbf{p}|$$

- projections onto free eigenstates

$$1 = Z + X, \quad Z \equiv |\langle B_0 | B \rangle|^2, \quad X \equiv \int \frac{d\mathbf{p}}{(2\pi)^3} |\langle \mathbf{p} | B \rangle|^2$$

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“elementarity”



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compositeness

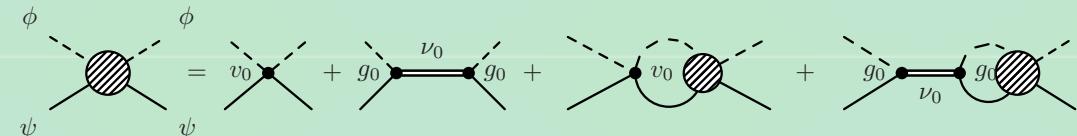


$Z, X$ : real and nonnegative  $\rightarrow$  interpreted as probability

# Weak binding relation

$\psi\phi$  scattering amplitude (exact result)

$$f(E) = -\frac{\mu}{2\pi} \frac{1}{[v(E)]^{-1} - G(E)}$$



$$v(E) = v_0 + \frac{g_0^2}{E - \omega_0}, \quad G(E) = \frac{1}{2\pi^2} \int_0^\Lambda dp \frac{p^2}{E - p^2/(2\mu) + i0^+}$$

**Compositeness**  $X \leftarrow v(E), G(E)$

$$X = \frac{G'(-B)}{G'(-B) - [1/v(-B)]'}$$

$1/R = \sqrt{2\mu B}$  expansion of scattering length  $a_0$

$$a_0 = -f(E=0) = R \underbrace{\left\{ \frac{2X}{1+X} + \overline{\mathcal{O}\left(\frac{R_{\text{typ}}}{R}\right)} \right\}}_{\text{renormalization independent}} \text{renormalization dependent}$$

If  $R \gg R_{\text{typ}}$ , correction terms neglected:  $X \leftarrow (a_0, B)$

# Inclusion of decay channel

## Introduce decay channel

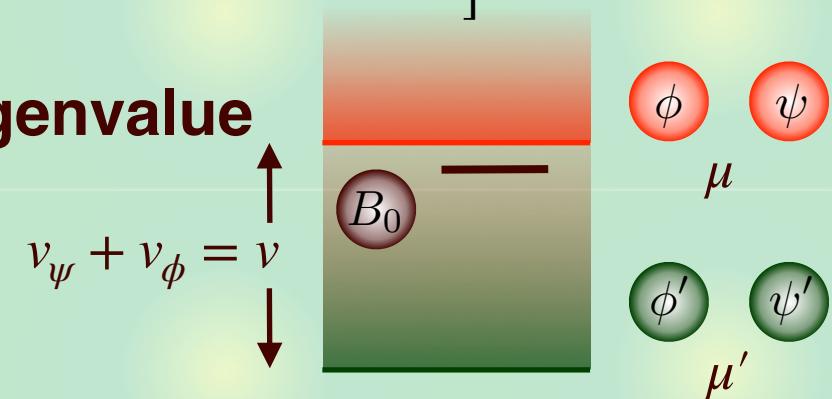
$$H'_{\text{free}} = \int d\mathbf{r} \left[ \frac{1}{2M'} \nabla \psi'^{\dagger} \cdot \nabla \psi' - \nu_{\psi} \psi'^{\dagger} \psi' + \frac{1}{2m'} \nabla \phi'^{\dagger} \cdot \nabla \phi' - \nu_{\phi} \phi'^{\dagger} \phi' \right]$$

$$H'_{\text{int}} = \int d\mathbf{r} \left[ g'_0 \left( B_0^{\dagger} \phi' \psi' + \psi'^{\dagger} \phi'^{\dagger} B_0 \right) + v'_0 \psi'^{\dagger} \phi'^{\dagger} \phi' \psi' + v'_0 (\psi'^{\dagger} \phi'^{\dagger} \phi' \psi' + \psi'^{\dagger} \phi'^{\dagger} \phi' \psi') \right]$$

## Quasi-bound state : complex eigenvalue

$$H = H_{\text{free}} + H'_{\text{free}} + H_{\text{int}} + H'_{\text{int}}$$

$$H|h\rangle = E_h |h\rangle, \quad E_h \in \mathbb{C}$$



## Generalized relation : correction from threshold difference

$$a_0 = R \left\{ \frac{2X}{1+X} + \mathcal{O}\left(\left|\frac{R_{\text{typ}}}{R}\right|\right) + \underline{\mathcal{O}\left(\left|\frac{\ell}{R}\right|^3\right)} \right\}, \quad R = \frac{1}{\sqrt{-2\mu E_h}}, \quad \ell \equiv \frac{1}{\sqrt{2\mu\nu}}$$

Y. Kamiya, T. Hyodo, PRC93, 035203 (2016); PTEP2017, 023D02 (2017)

If  $|R| \gg (R_{\text{typ}}, \ell)$ , correction terms neglected:  $X \leftarrow (a_0, E_h)$

# Complex compositeness

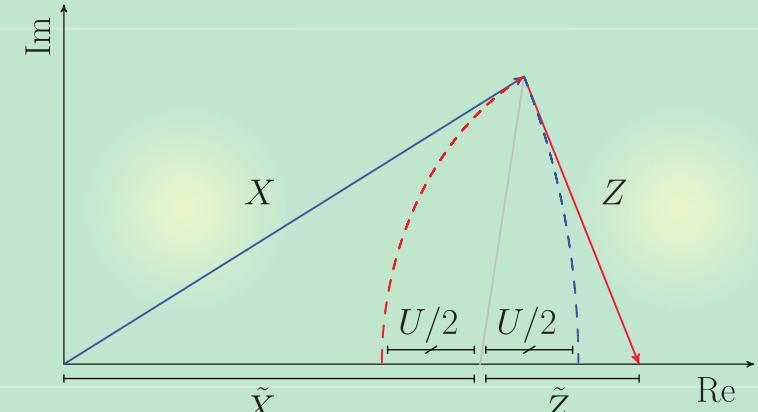
Unstable states  $\rightarrow$  complex  $Z$  and  $X$

$$Z + X = 1, \quad Z, X \in \mathbb{C}$$

- Probabilistic interpretation?

New definition

$$\tilde{Z} = \frac{1 - |X| + |Z|}{2}, \quad \tilde{X} = \frac{1 - |Z| + |X|}{2}$$



- interpreted as probabilities  $\tilde{Z} + \tilde{X} = 1, \quad \tilde{Z}, \tilde{X} \in [0, 1]$

- reduces to  $Z$  and  $X$  in the bound state limit

$U/2$ : uncertainty of interpretation

$$U = |Z| + |X| - 1$$

c.f. T. Berggren, Phys. Lett. 33B, 547 (1970)

- Sensible interpretation only for small  $U/2$  case

# Evaluation of compositeness

## Generalized weak-binding relation

$$a_0 = R \left\{ \frac{2X}{1+X} + \mathcal{O}\left(\left|\frac{R_{\text{typ}}}{R}\right|\right) + \mathcal{O}\left(\left|\frac{\ell}{R}\right|^3\right) \right\}, \quad R = \frac{1}{\sqrt{-2\mu E_h}}, \quad \ell \equiv \frac{1}{\sqrt{2\mu\nu}}$$

## $(a_0, E_h)$ determinations by several groups

- neglecting correction terms:

	$E_h$ [MeV]	$a_0$ [fm]	$X_{\bar{K}N}$	$\tilde{X}_{\bar{K}N}$	$U/2$
Set 1 [35]	$-10 - i26$	$1.39 - i0.85$	$1.2 + i0.1$	1.0	0.3
Set 2 [36]	$-4 - i8$	$1.81 - i0.92$	$0.6 + i0.1$	0.6	0.0
Set 3 [37]	$-13 - i20$	$1.30 - i0.85$	$0.9 - i0.2$	0.9	0.1
Set 4 [38]	$2 - i10$	$1.21 - i1.47$	$0.6 + i0.0$	0.6	0.0
Set 5 [38]	$-3 - i12$	$1.52 - i1.85$	$1.0 + i0.5$	0.8	0.3

- In all cases,  $X \sim 1$  with small  $U/2$  (complex nature)

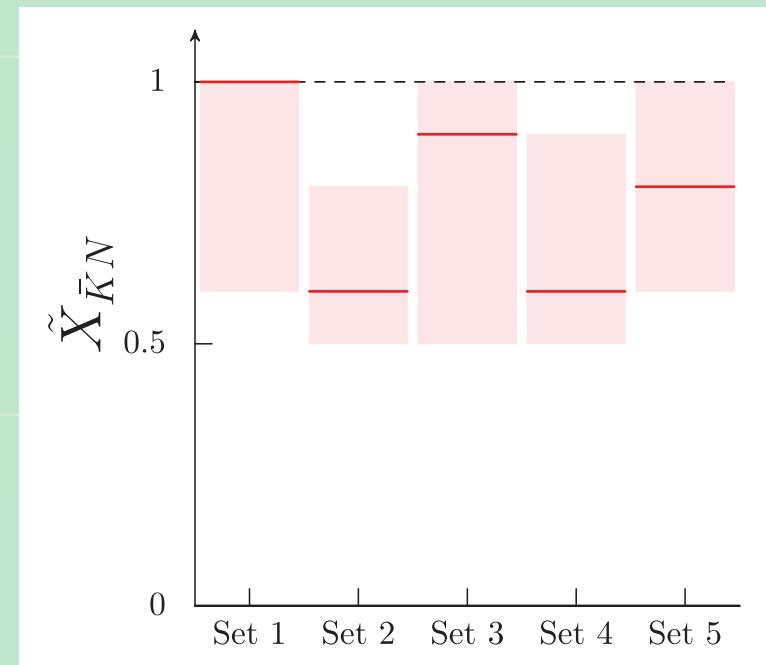
$\Lambda(1405)$ :  $\bar{K}N$  composite dominance  $\leftarrow$  observables

# Uncertainty estimation

Estimation of correction terms:  $|R| \sim 2$  fm

$$a_0 = R \left\{ \frac{2X}{1+X} + \mathcal{O}\left(\left|\frac{R_{\text{typ}}}{R}\right|\right) + \mathcal{O}\left(\left|\frac{\ell}{R}\right|^3\right) \right\}, \quad R = \frac{1}{\sqrt{-2\mu E_h}}, \quad \ell \equiv \frac{1}{\sqrt{2\mu\nu}}$$

- $\rho$  meson exchange picture:  $R_{\text{typ}} \sim 0.25$  fm
- energy difference from  $\pi\Sigma$ :  $\ell \sim 1.08$  fm



$\bar{K}N$  composite dominance holds even with correction terms.

## Correction term and zero range limit

What happens if  $R_{\text{typ}} \rightarrow 0$  ?

$$a_0 = R \frac{2X}{1 + X}$$

- Limit  $\Lambda \rightarrow \infty$  can be taken in renormalizable EFT
- EFT with only  $\psi, \phi$  fields should have  $X = 1$

$$\Rightarrow a_0 = R$$

- “effective range model” gives  $a_0 \neq R$  : contradiction?

E. Braaten, M. Kusunoki, D. Zhang, Annals Phys. 323, 1770 (2008)

$R_{\text{typ}}$  should be either  $R_{\text{int}}$  or length scale in the amplitude

$$a_0 = R \left\{ \frac{2X}{1 + X} + \mathcal{O}\left(\frac{R_{\text{typ}}}{R}\right) \right\}, \quad R_{\text{typ}} = \max(R_{\text{int}}, |r_e|, \dots)$$

- relevant to system with large  $|r_e|$

T. Kinugawa, T. Hyodo, in preparation

# Summary



**Structure of unstable resonance is nontrivial.**



**Pole structure of the  $\Lambda(1405)$  region is now well constrained by the experimental data.**

“ $\Lambda(1405)$ ”  $\rightarrow \Lambda(1405)$  and  $\Lambda(1380)$

Y. Ikeda, T. Hyodo, W. Weise, PLB 706, 63 (2011); NPA 881, 98 (2012);

P.A. Zyla, et al. (Particle Data Group), PTEP 2020, 083C01 (2020)

T. Hyodo, M. Niiyama, arXiv: 2010.07592 [hep-ph]



**Generalized weak-binding relation shows that (higher-energy)  $\Lambda(1405)$  is dominated by molecular  $\bar{K}N$  component.**

Y. Kamiya, T. Hyodo, PRC93, 035203 (2016); PTEP2017, 023D02 (2017)

T. Hyodo, JPS journal Vol. 75 No. 8, 478 (2020)