

# Femtoscscopy for the systems with strangeness and charm



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## Introduction — Femtoscopy



## Femtoscopy for strangeness

### - $\Lambda\alpha$ and $\Xi\alpha$ correlations

[A. Jinno, Y. Kamiya, T. Hyodo, A. Ohnishi, PRC110, 014001 \(2024\);](#)  
[Y. Kamiya, A. Jinno, T. Hyodo, A. Ohnishi, arXiv:2409.13207 \[nucl-th\]](#)



## Femtoscopy for charm

### - $DD^*$ and $D\bar{D}^*$ correlations

[Y. Kamiya, T. Hyodo, A. Ohnishi, EPJA58, 131 \(2022\)](#)

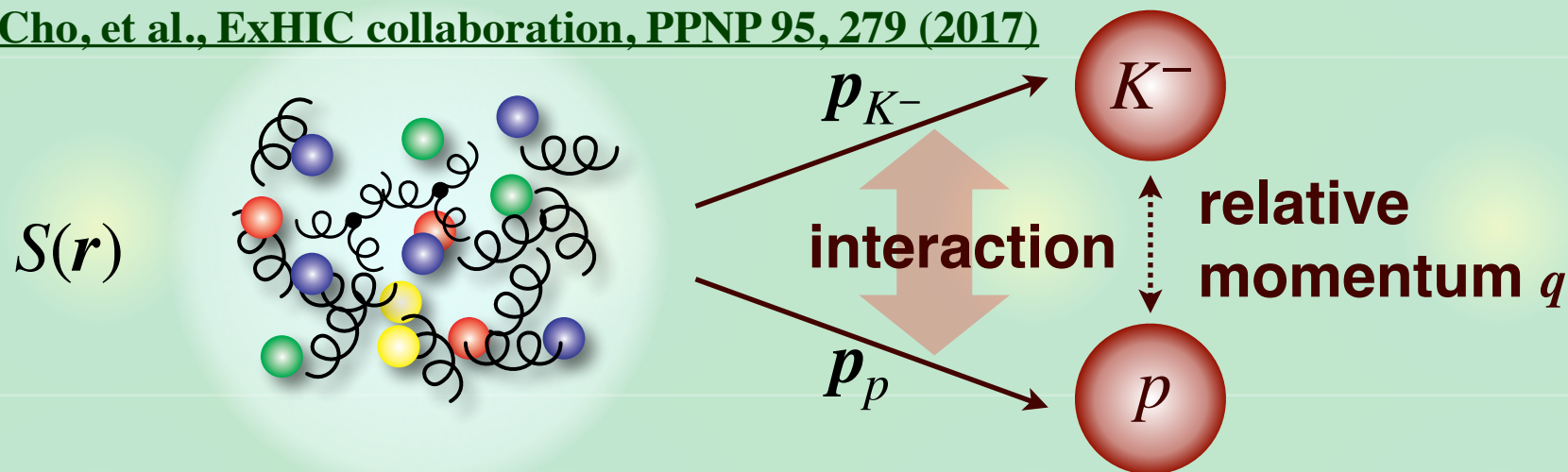


## Summary and future prospects

# Correlation function and KP formula

High-energy collision: chaotic source  $S(r)$  of hadron emission

S. Cho, et al., ExHIC collaboration, PPNP 95, 279 (2017)



## - Definition

$$C(q) = \frac{N_{K^-p}(p_{K^-}, p_p)}{N_{K^-}(p_{K^-})N_p(p_p)} \quad (= 1 \text{ in the absence of FSI/QS})$$

## - Theory (Koonin-Pratt formula)

incoming + outgoing

S.E. Koonin, PLB 70, 43 (1977); S. Pratt, PRD 33, 1314 (1986)

$$C(q) \simeq \int d^3r S(r) |\Psi_q^{(-)}(r)|^2, \quad \Psi_q^{(-)}(r) \propto S^\dagger e^{-iqr} - e^{+iqr} \quad (r \rightarrow \infty)$$

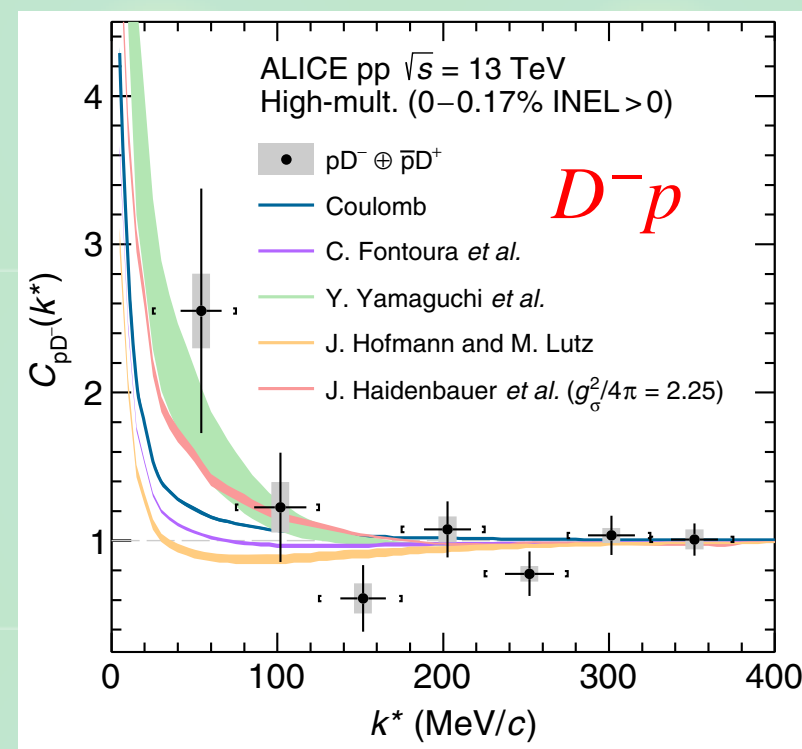
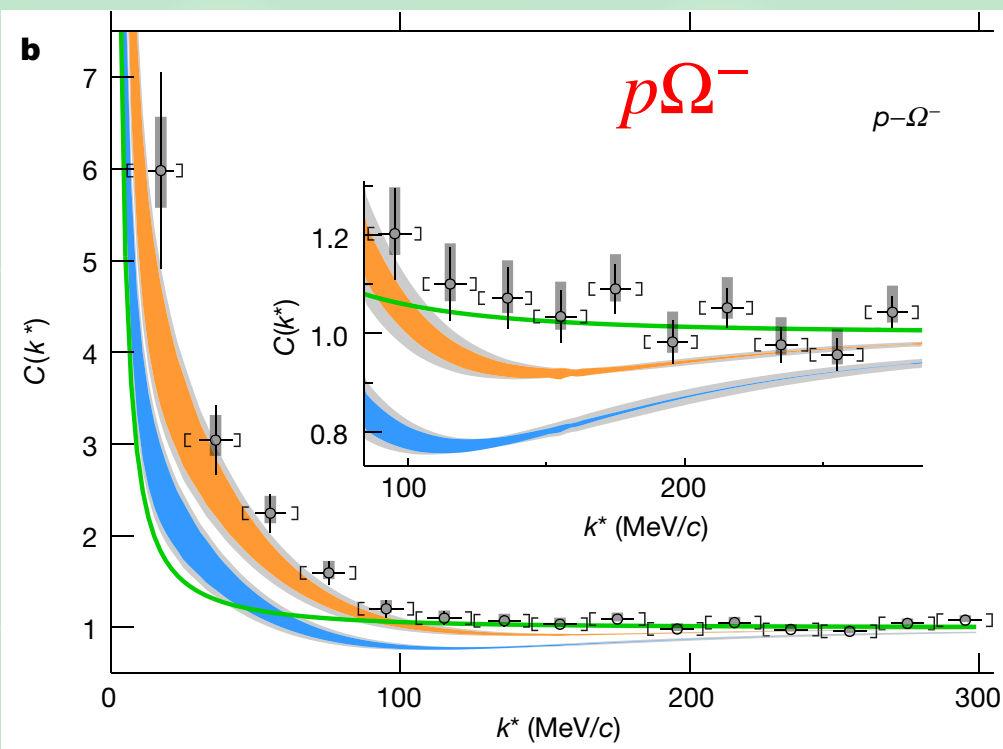
Source function  $S(r) \longleftrightarrow$  wave function  $\Psi_q^{(-)}(r)$  (interaction)

# Experimental data with strangeness and charm

## Correlation functions observed by ALICE@LHC

ALICE collaboration, Nature 588, 232 (2020);

ALICE collaboration, PRD 106, 052010 (2022)



$\Omega^- \sim sss$  : strangeness  $S = -3$ ,  $D^- \sim \bar{c}d$  : charm  $C = -1$

Almost **impossible** in scattering experiments



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## Summary and future prospects

## $\Lambda\alpha$ correlation: Motivation

### A solution to hyperon puzzle in neutron stars

- $\Lambda NN$  **three-body force** for repulsion at high density

D. Gerstung, N. Kaiser, W. Weise, EPJA 55, 175 (2020)

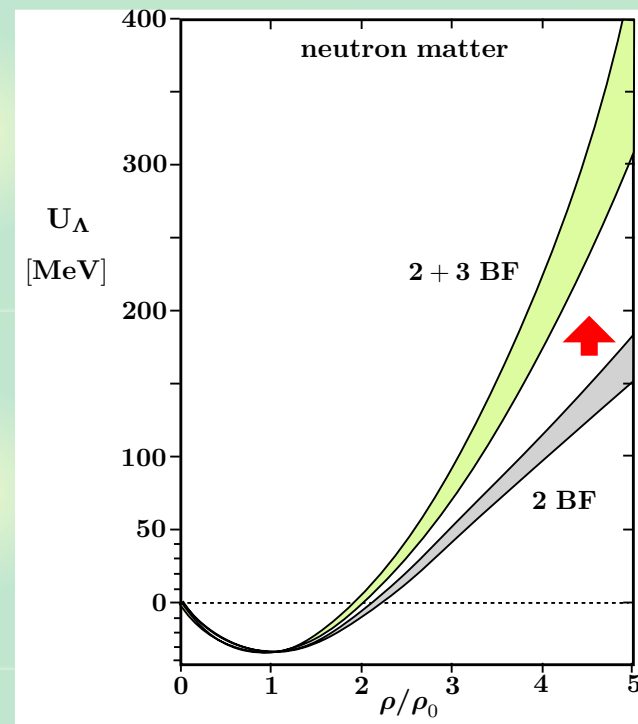
### How to verify this in experiments?

- $\Lambda$  **directed flow** in heavy ion collisions

Y. Nara, A. Jinno, K. Murase, A. Ohnishi,  
PRC 106, 044902 (2022)

### $\Lambda$ -nucleus correlation function?

- Heavy nuclei are difficult to produce
- Strong binding of  $\alpha$ : two-body treatment justified



$\Lambda\alpha$  correlation function  $\rightarrow$  **nature of  $\Lambda\alpha$  potential?**

# $\Lambda\alpha$ potentials

## Phenomenological $\Lambda\alpha$ potentials ( ${}^5_\Lambda\text{He}$ binding energy)

I. Kumagai-Fuse, S. Okabe, Y. Akaishi, PLB 345, 386 (1997)

- **SG**: single gaussian
- **Isle**: two gaussians (with core)

## Skyrme-Hartree Fock methods

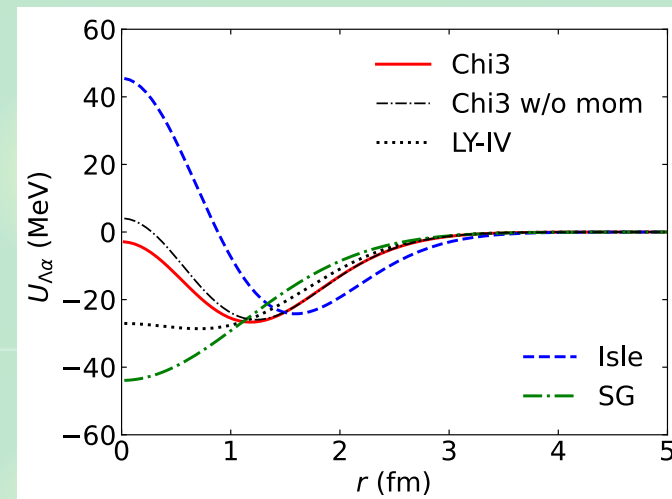
- **LY4**: phenomenorogical

D.E. Lanskoj, Y. Yamamoto, PRC 55, 2330 (1997)

- **Chi3**: based on chiral EFT with  $\Lambda NN$  force

A. Jinno, K. Murase, Y. Nara, A. Ohnishi, PRC 108, 065803 (2023)

- Both potentials reproduce hypernuclear data from C to Pb
- $\alpha$  density distribution  $\rightarrow \Lambda\alpha$  potentials

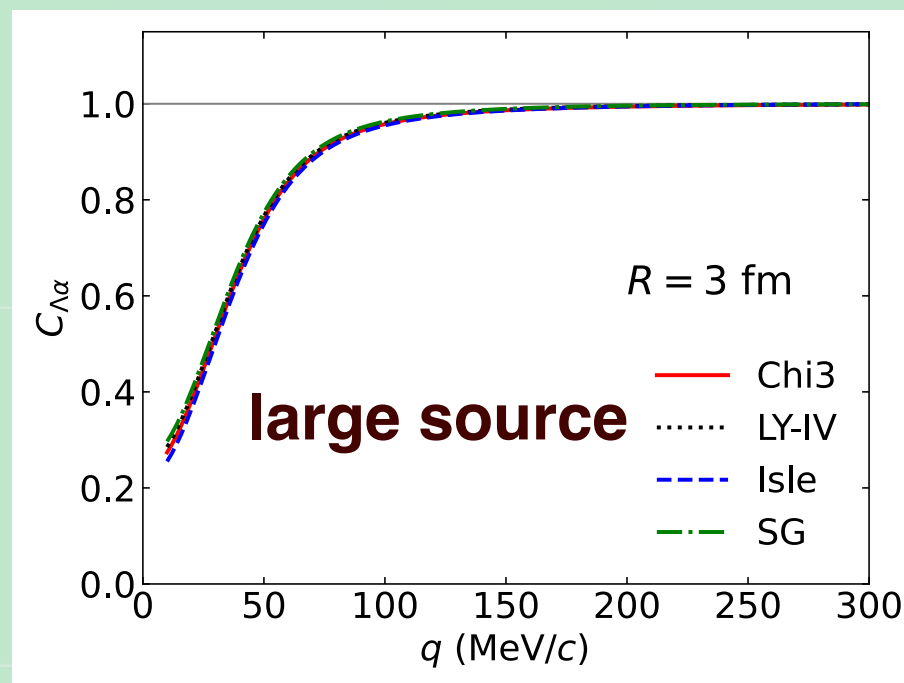
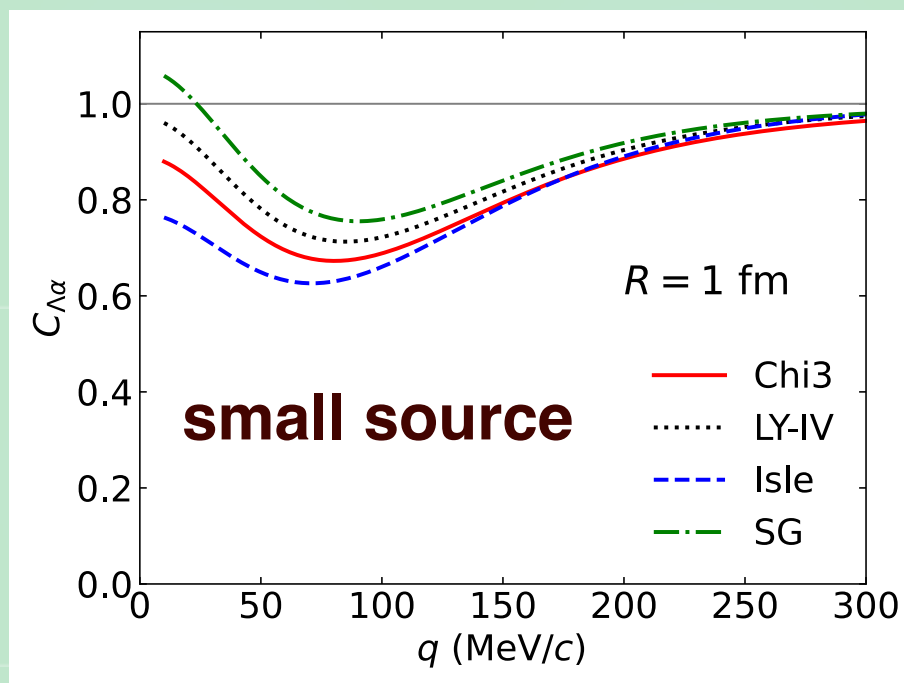


Effect of repulsive core  $\rightarrow$  correlation function?

# $\Lambda\alpha$ correlation: source size dependence

## Correlation functions from small and large sources

A. Jinno, Y. Kamiya, T. Hyodo, A. Ohnishi, PRC110, 014001 (2024)



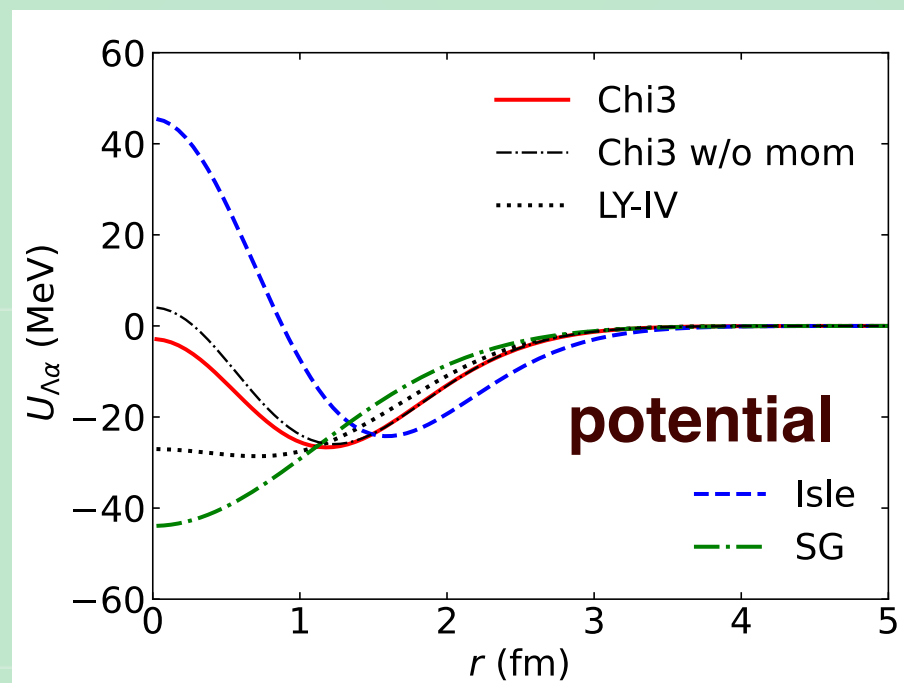
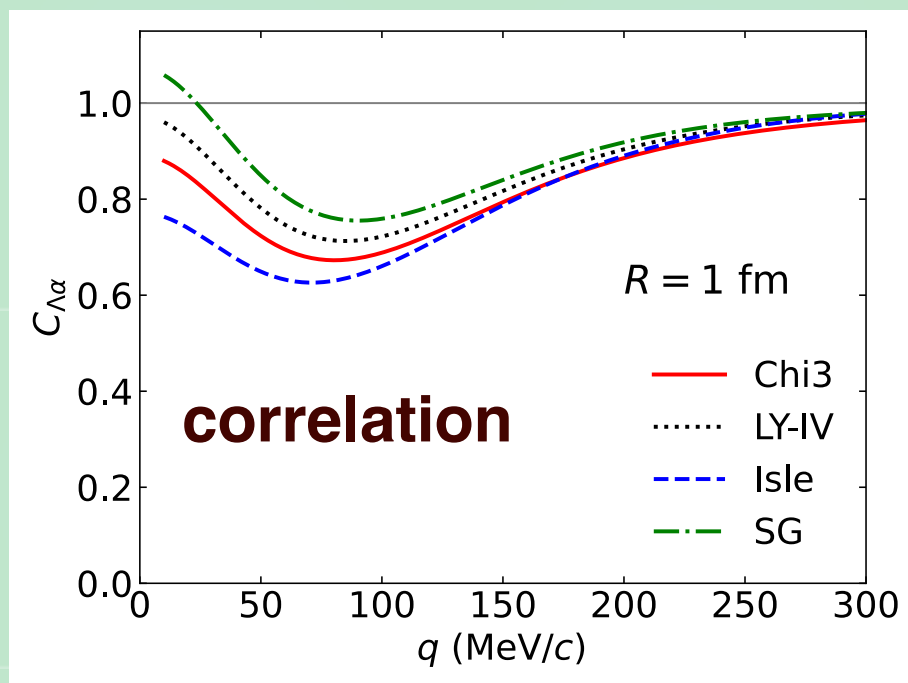
- Bound state signature (dip at low  $q$  in small source)
- No difference in large source ( $R \sim 3$  fm)
- **Interaction dependence** in small source ( $R \sim 1$  fm)



# $\Lambda\alpha$ correlation: interaction dependence

## Correlation functions and $\Lambda\alpha$ potentials

A. Jinno, Y. Kamiya, T. Hyodo, A. Ohnishi, PRC110, 014001 (2024)



- $U_{\Lambda\alpha}(r = 0)$ : **Isle** > LY-IV > **Chi3** > **SG**
- $C_{\Lambda\alpha}(q = 0)$ : **Isle** < LY-IV < **Chi3** < **SG**
- Central repulsion **suppresses** correlation at low  $q$

# $\Xi\alpha$ correlation: Motivation

$\Xi N$  interactions ( $^{11}S_0$ ,  $^{31}S_0$ ,  $^{13}S_1$ ,  $^{33}S_1$ ) from lattice QCD and ChEFT

K. Sasaki, et al. (HAL QCD), NPA 998, 121737 (2020);

J. Haidenbauer, U.-G. Meißner, EPJA 55, 23 (2019)

—> Different predictions for  $\Xi^-\alpha$  and  $\Xi^0\alpha$  bound states

E. Hiyama, M. Isaka, T. Doi, T. Hatsuda, PRC 106, 064318 (2022)

H. Le, J. Haidenbauer, U.-G. Meißner, A. Nogga, EPJA 57, 339 (2021)

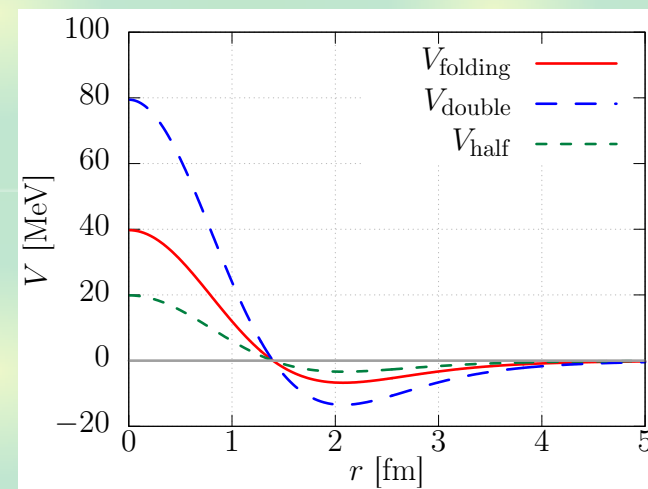
Three  $\Xi\alpha$  potentials (attraction plus core)

Y. Kamiya, A. Jinno, T. Hyodo, A. Ohnishi, arXiv:2409.13207 [nucl-th]

-  $V_{\text{folding}}$ : folding HAL QCD  $\Xi N$  potentials

-  $V_{\text{double}} = V_{\text{folding}} \times 2$ ,  $V_{\text{half}} = V_{\text{folding}}/2$

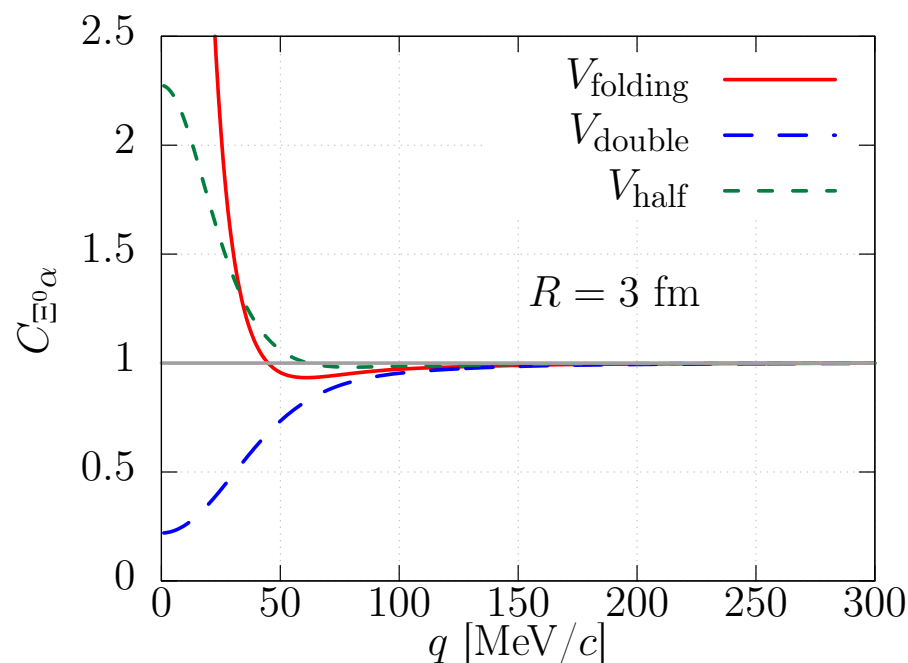
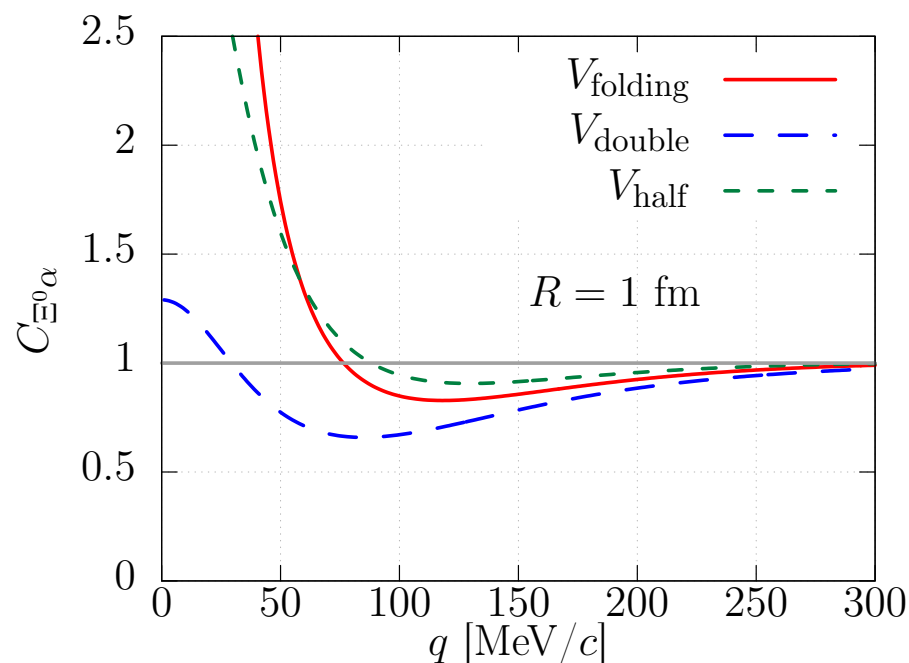
potential	$\Xi^-\alpha$ [MeV]	$\Xi^0\alpha$ [MeV]
$V_{\text{folding}}$	0.47	-
$V_{\text{double}}$	2.08	1.15
$V_{\text{half}}$	0.18	-



# $\Xi\alpha$ correlation: source size dependence

## $\Xi^0\alpha$ Correlation functions

Y. Kamiya, A. Jinno, T. Hyodo, A. Ohnishi, arXiv:2409.13207 [nucl-th]



- $V_{\text{double}}$ : strong source size dependence  $\leftarrow$  bound state
- Dip in  $V_{\text{folding}}$  and  $V_{\text{half}}$   $\leftarrow$  repulsive core?

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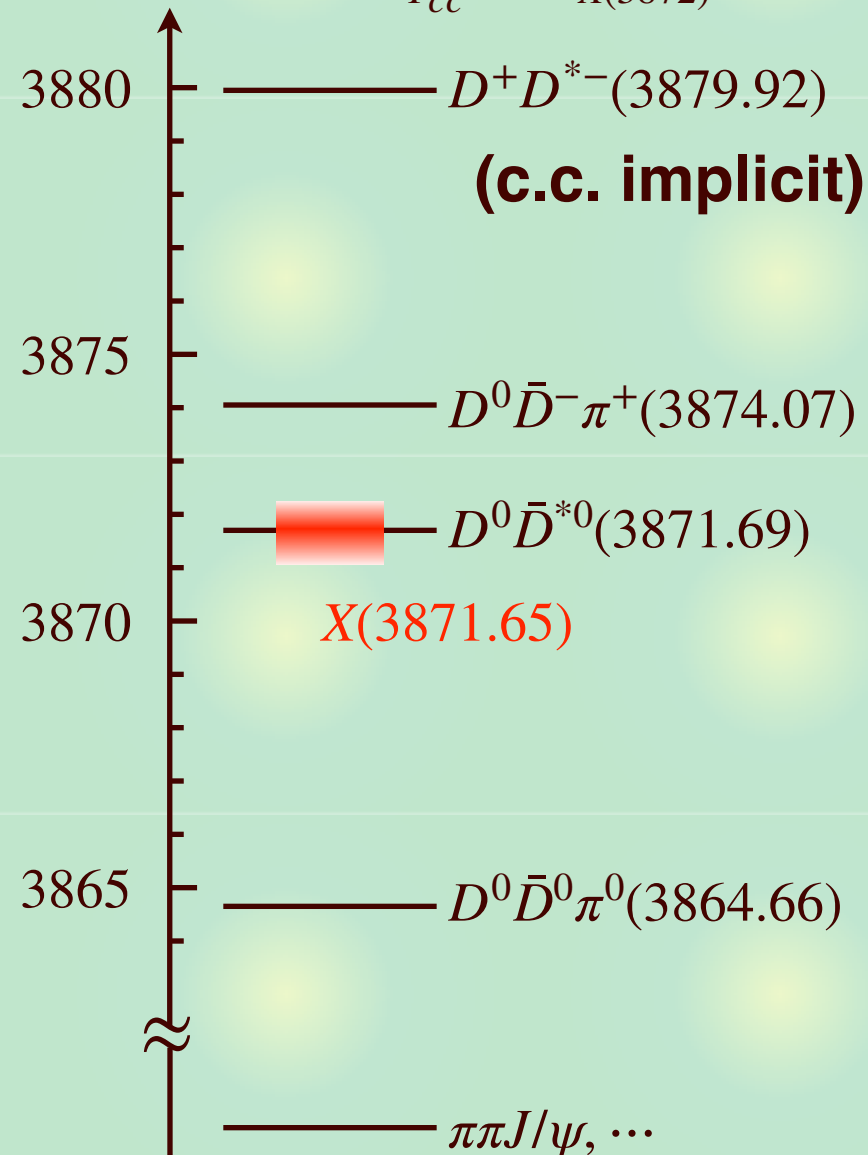
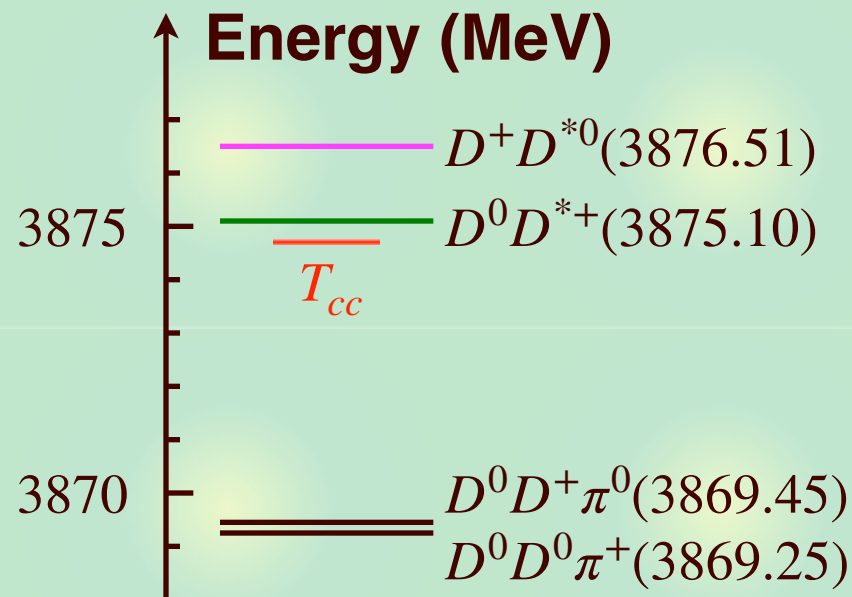


## Summary and future prospects

# $T_{cc}$ and $X(3872)$

$X(3872)$  : another near-threshold state with  $M_{T_{cc}} \sim M_{X(3872)}$

## - Masses from PDG Live



-  $T_{cc}/X(3872)$  near  $DD^*/D\bar{D}^*$

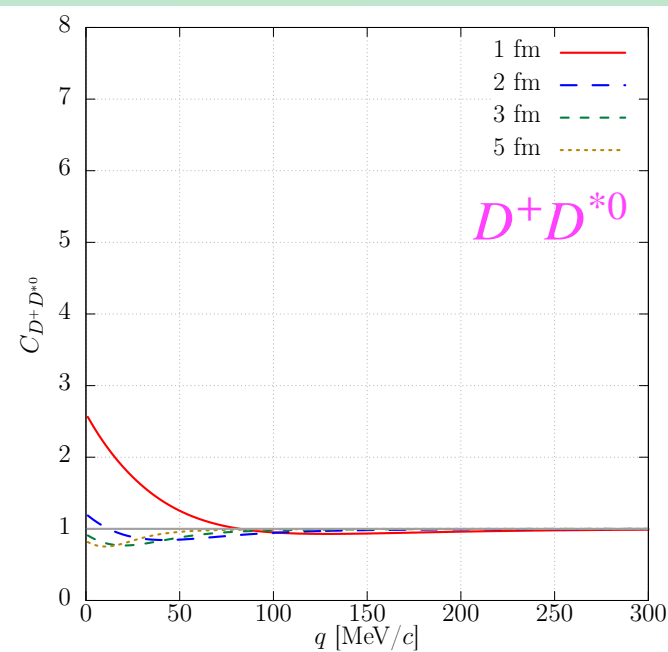
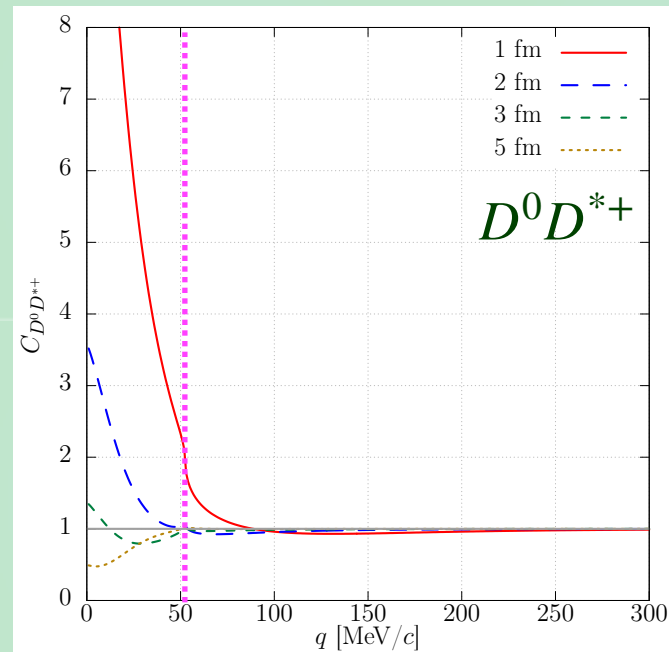
—> Molecule nature?

-  $X(3872)$  has decay channels

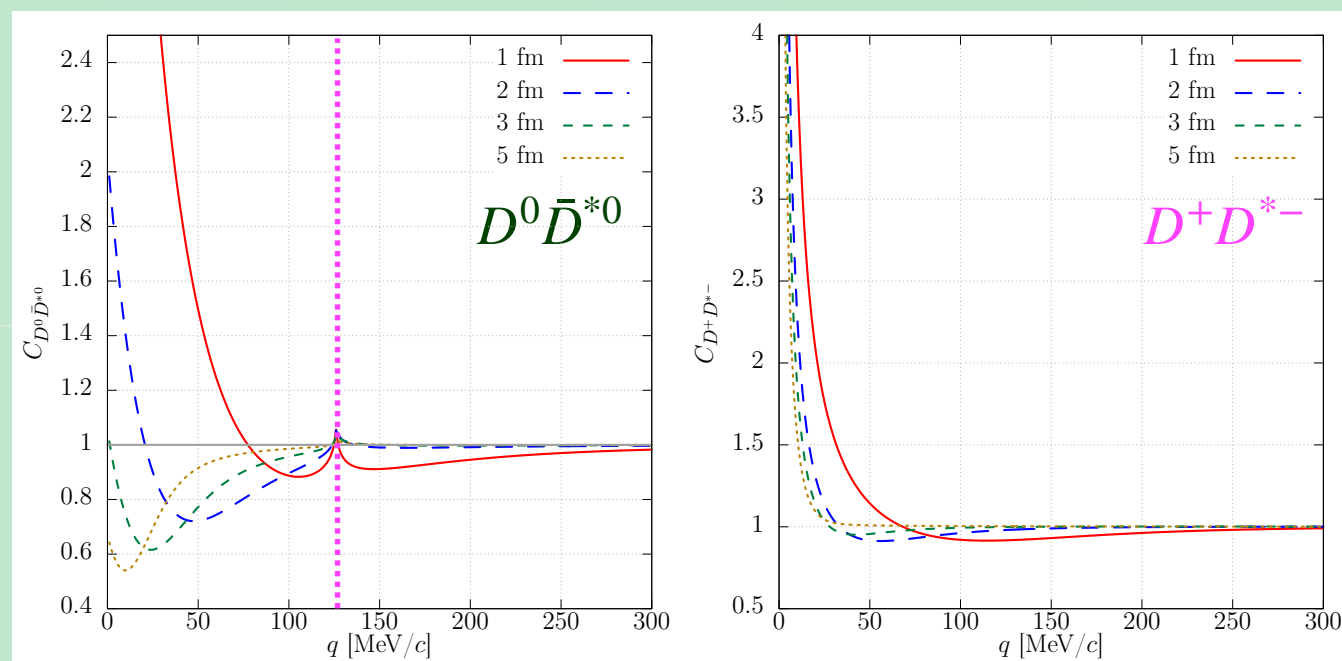


$DD^* \sim T_{cc}$  sector $D^0D^{*+}$  and  $D^+D^{*0}$  correlation functions ( $cc\bar{u}\bar{d}$ , exotic)Y. Kamiya, T. Hyodo, A. Ohnishi, EPJA58, 131 (2022)

$D^+D^{*0}$   
 $D^0D^{*+}$   
 $T_{cc}$



- Bound state feature (source size dep.) in both channels
- Strong signal in  $D^0D^{*+}$ , weaker one in  $D^+D^{*0}$
- $D^+D^{*0}$  cusp in  $D^0D^{*+}$  ( $q \sim 52$  MeV) is not very prominent

$D\bar{D}^* \sim X(3872)$  sector $D^0\bar{D}^{*0}$  and  $D^+\bar{D}^{*-}$  correlation functions ( $c\bar{c}q\bar{q}$ )Y. Kamiya, T. Hyodo, A. Ohnishi, EPJA58, 131 (2022) $D^+\bar{D}^{*-}$  $D^0\bar{D}^{*0}$  $X(3872)$ 

- Bound state feature in  $D^0\bar{D}^{*0}$  correlation
- Sizable  $D^+\bar{D}^{*-}$  cusp in  $D^0\bar{D}^{*0}$  ( $q \sim 126$  MeV)
- $D^+\bar{D}^{*-}$  correlation : Coulomb attraction dominance

## Summary



**Femtoscscopy: novel and useful method to study interactions of exotic hadrons and nuclei**



**$\Lambda\alpha$  correlations**

**- hint for repulsive core in  $\Lambda\alpha$  interaction**

[A. Jinno, Y. Kamiya, T. Hyodo, A. Ohnishi, PRC110, 014001 \(2024\)](#)



**$E\alpha$  correlations**

**- existence of bound state**

[Y. Kamiya, A. Jinno, T. Hyodo, A. Ohnishi, arXiv:2409.13207 \[nucl-th\]](#)



**$DD^*$  and  $D\bar{D}^*$  correlations**

**- (quasi-)bound nature of  $T_{cc}$  and  $X(3872)$**

[Y. Kamiya, T. Hyodo, A. Ohnishi, EPJA58, 131 \(2022\)](#)

## Future prospects



### New direction: femtoscopy with nuclei

- $\Lambda\alpha, \Xi\alpha$  **correlations: J-PARC HI, CBM@GSI,...**

[A. Jinno, Y. Kamiya, T. Hyodo, A. Ohnishi, PRC110, 014001 \(2024\);](#)  
[Y. Kamiya, A. Jinno, T. Hyodo, A. Ohnishi, arXiv:2409.13207 \[nucl-th\]](#)



### $K^\pm\alpha$ **correlation? (in preparation)**

- K nuclei, K atoms
- Folding potential, optical potential, ...



### $\Lambda\ ^3\text{He}, \Xi\ ^3\text{He}$ **correlations? (in preparation)**

- measurable at ALICE?