

Transitions of charm/bottom baryons with pion emissions

Ref. Phys. Rev. D91, 014031 (2015)

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Contents

1. Heavy quark symmetry
2. Decays of excited heavy baryons
3. Conclusion

1. Heavy quark symmetry

U



2 MeV

d



5 MeV



1300 MeV



100 MeV



4200 MeV

173,000 MeV

1. Heavy quark symmetry

Heavy quark symmetry (HQS)

Heavy baryon (Qqq)

Manohar, Wise, Luke, Grinstein, ...

$$\Psi(j)_J$$


Heavy quark spin 1/2

$$J=j\pm 1/2$$

“Brown Muck” : Light quarks and gluons
definite total spin j quark # = 2 and color $\bar{\textbf{3}}$



Mass spectrum

HQS doublet/singlet

(j \neq 0) (j=0)

1. Heavy quark symmetry

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Heavy baryon (Qqq)

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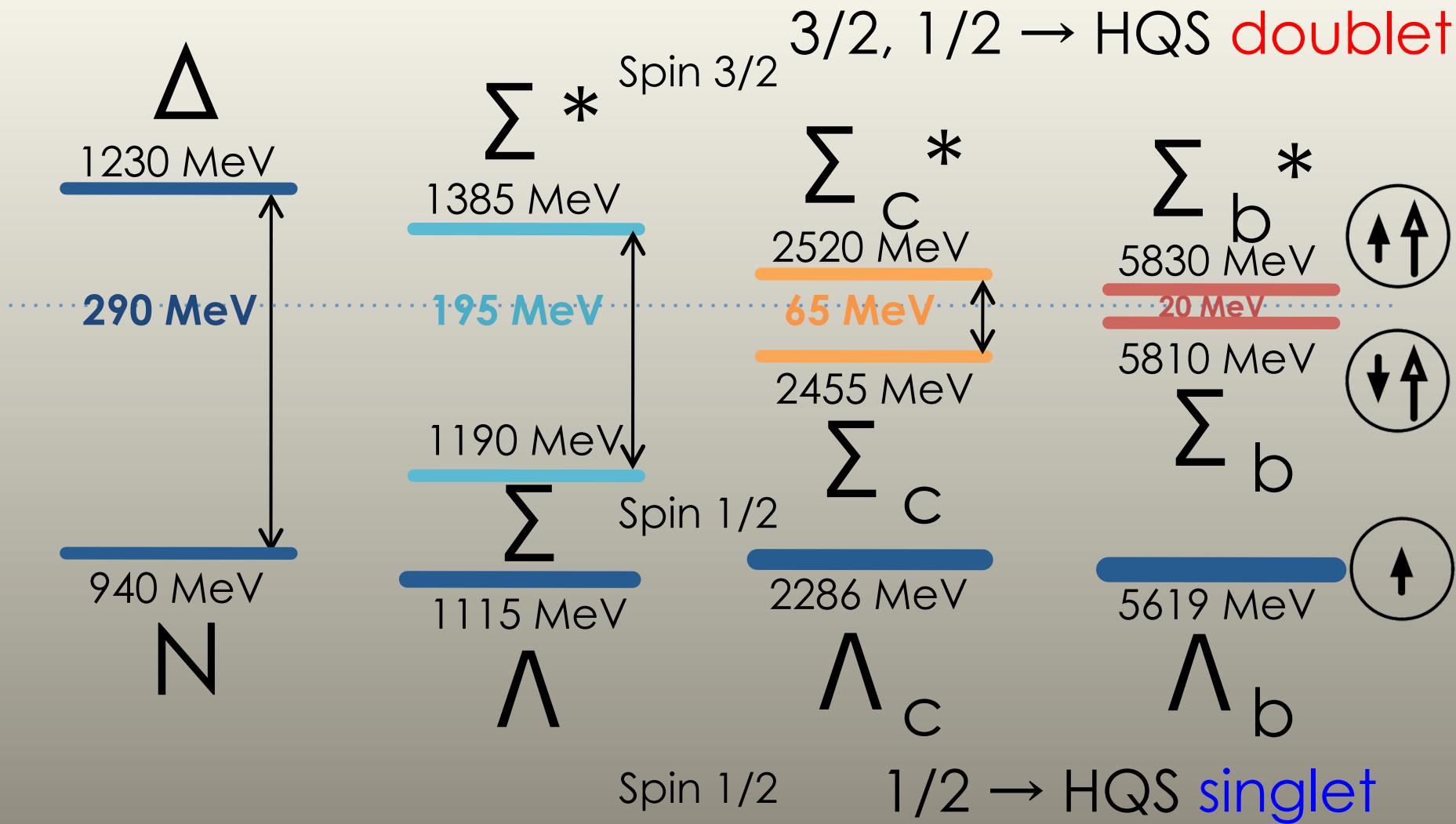
Mass spectrum

HQS doublet/singlet

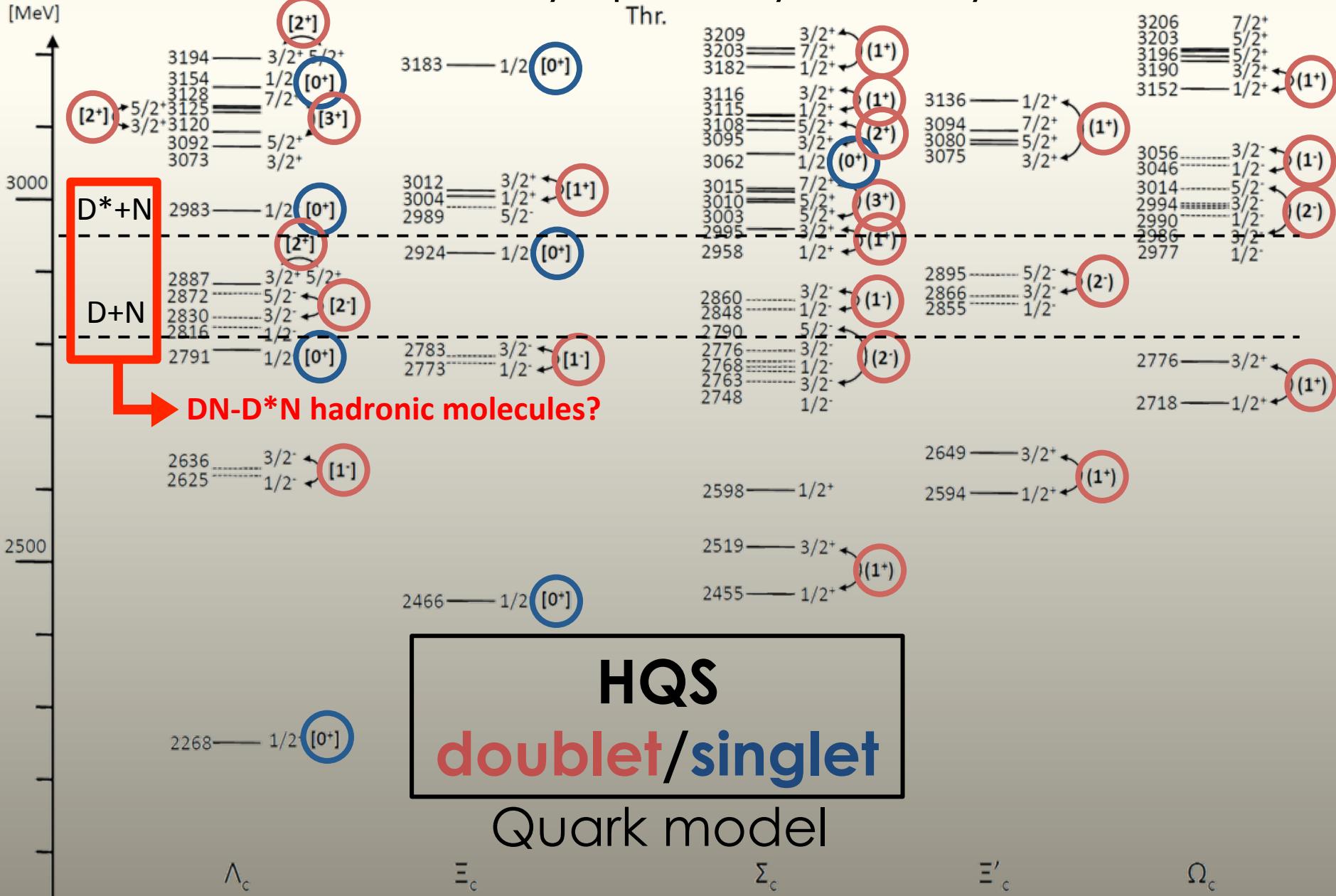
(j \neq 0) (j=0)

1. Heavy quark symmetry

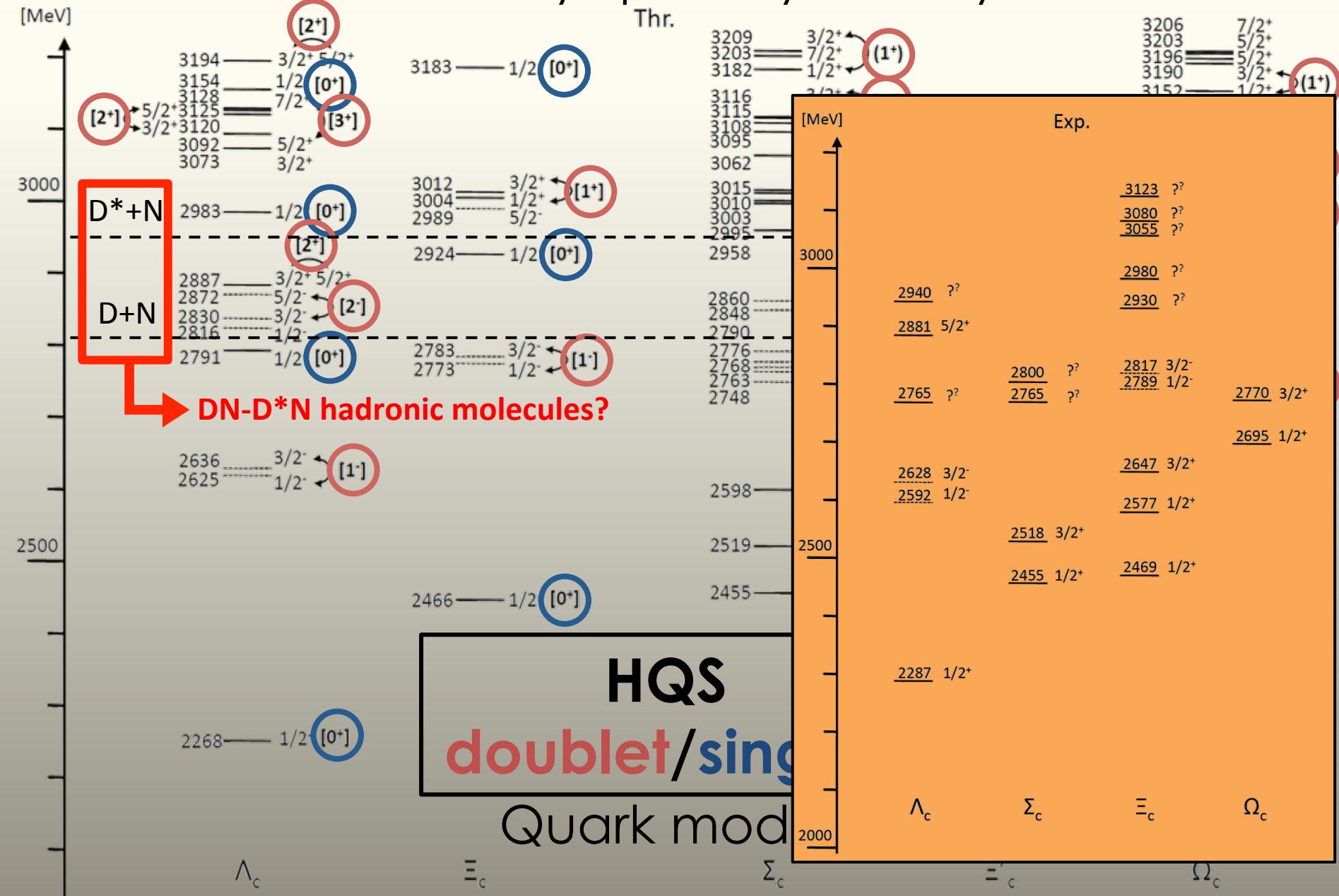
(1) Heavy Hadron Mass Spectrum



1. Heavy quark symmetry

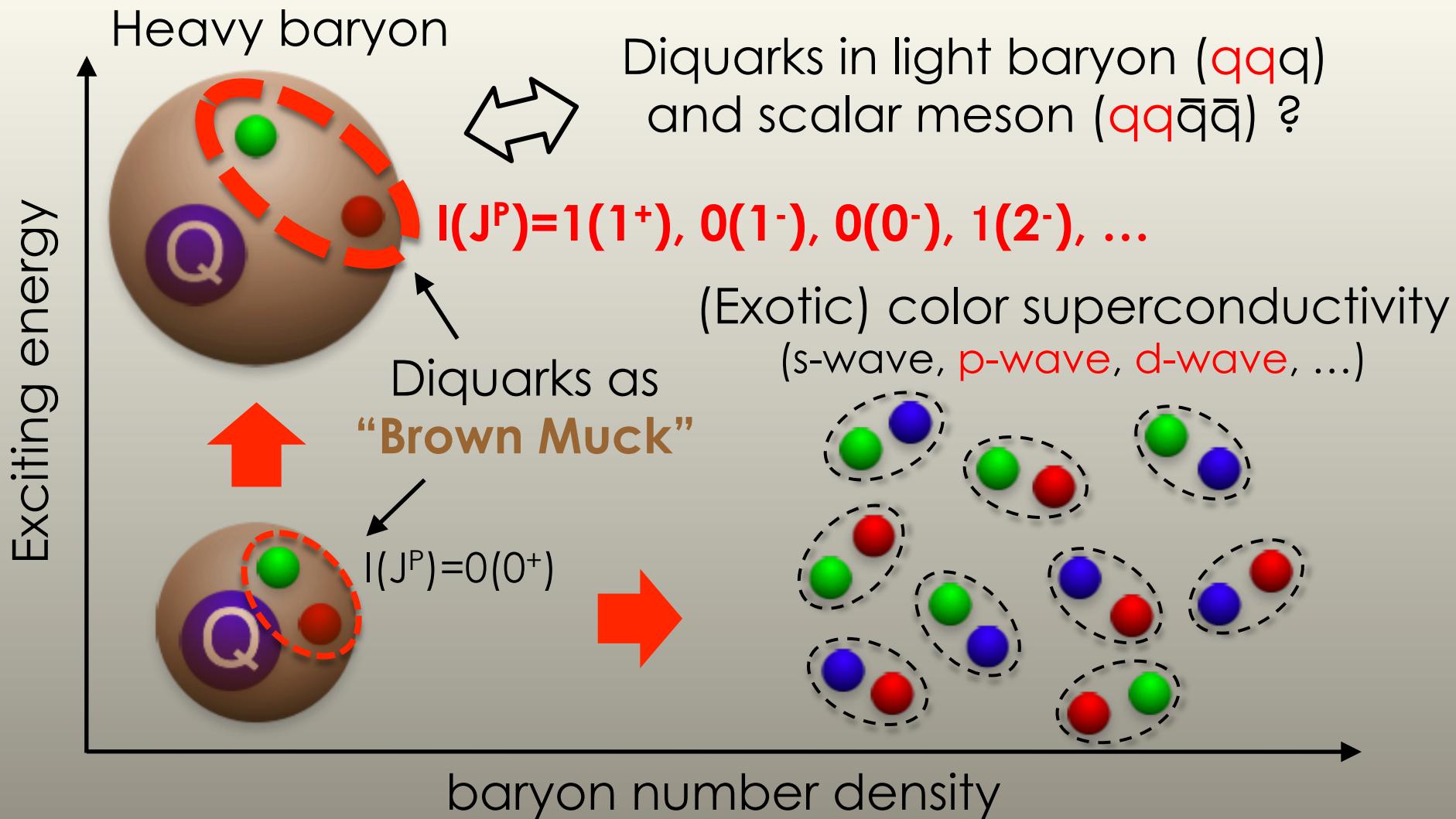


1. Heavy quark symmetry



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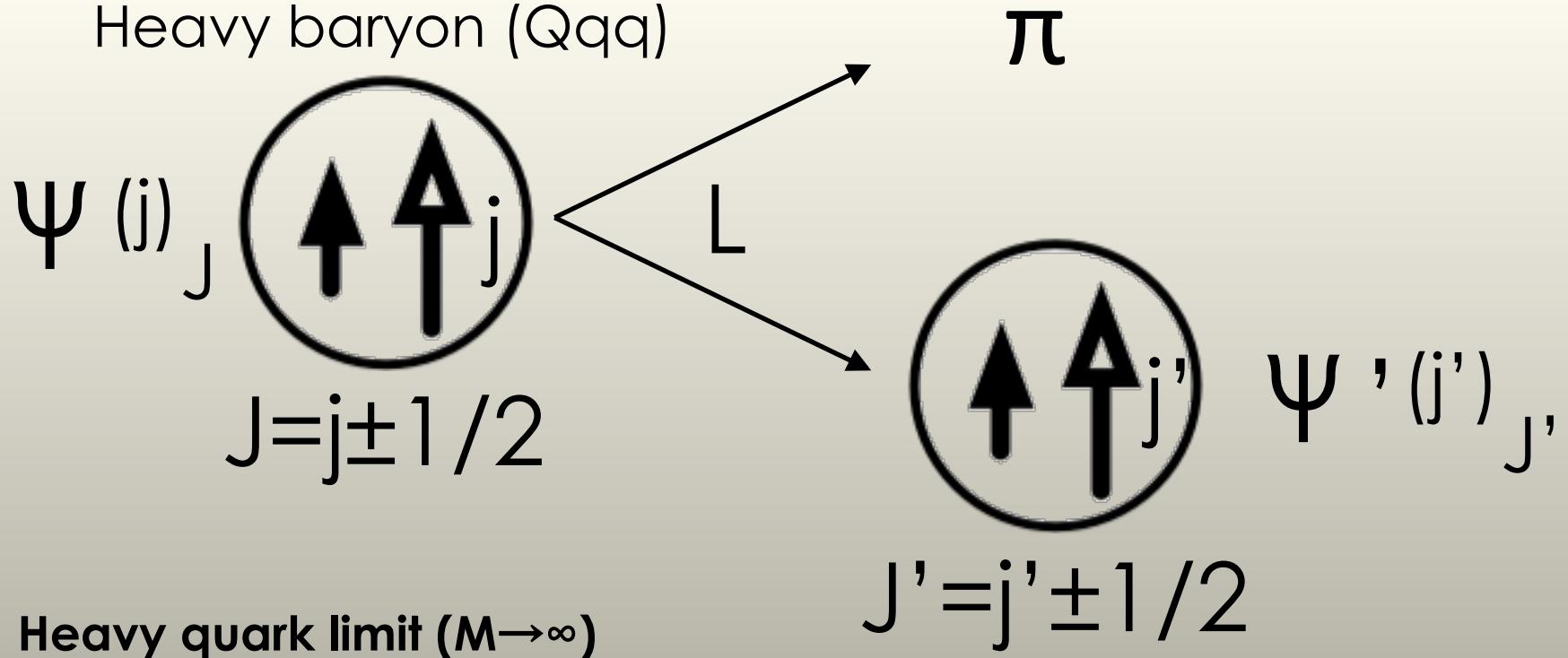
(2) Diquark Phase Diagram



2. Decays of excited heavy baryons

Transitions by strong decay

Heavy baryon (Qqq)



Heavy quark limit ($M \rightarrow \infty$)

$$\Gamma[\Psi_J^{(j)} \rightarrow \Psi'_{J'}^{(j')} \pi] \propto (2j+1)(2J'+1) \left| \left\{ \begin{array}{cccc} L & j' & j \\ 1/2 & J & J' \end{array} \right\} \right|^2 + \mathcal{O}(1/M)$$

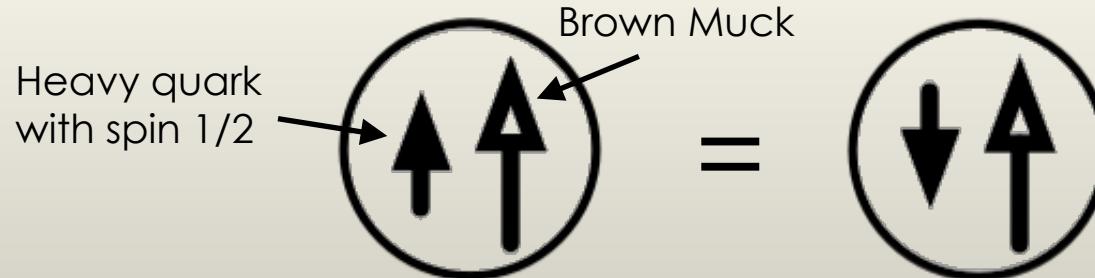
*Conservation of “spin” of brown muck: $j=j'+L$ Isgur and Wise, Phys. Rev. Lett. 66, 1130 (1991)

Question: what is $\mathcal{O}(1/M)$?

2. Decays of excited heavy baryons

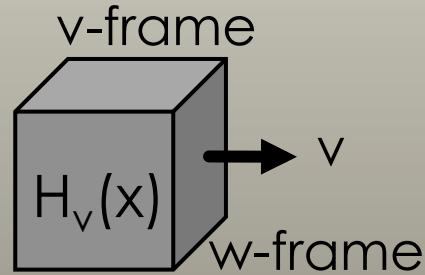
Heavy-baryon effective Lagrangian

1. Heavy quark symmetry is conserved at $\mathcal{O}(1)$.

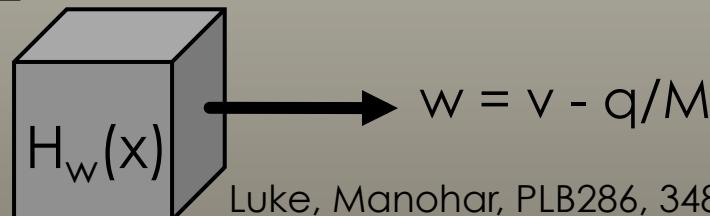


2. Inv. under velocity rearrangement at $\mathcal{O}(1) + \mathcal{O}(1/M)$.

$$v \rightarrow w = v + q/M \quad (q/M \ll 1)$$



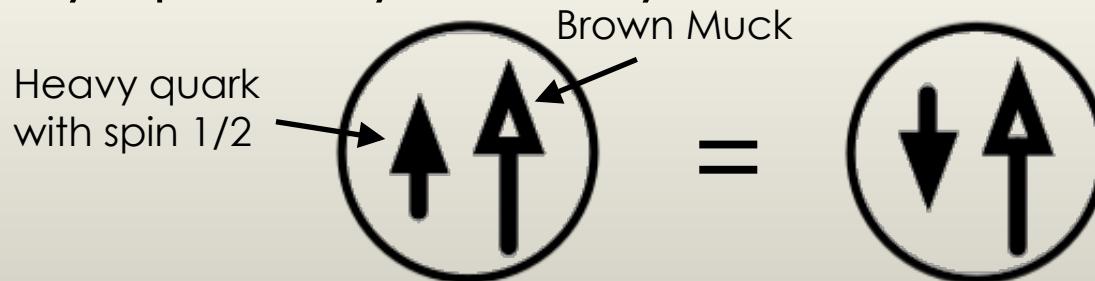
“Velocity rearrangement” :
Lorentz boost between v-frame and w-frame
up to $\mathcal{O}(1/M)$



2. Decays of excited heavy baryons

Heavy-baryon effective Lagrangian

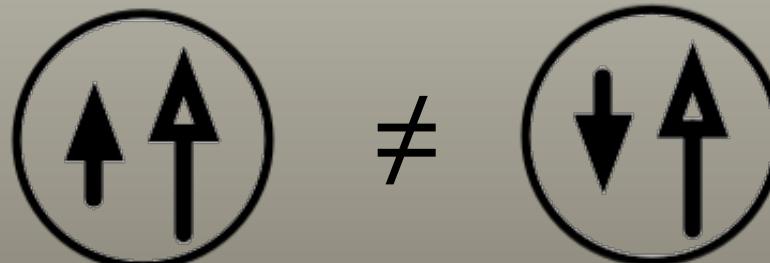
1. Heavy quark symmetry is conserved at $O(1)$.



2. Inv. under velocity rearrangement at $O(1)+O(1/M)$.

$$v \rightarrow w = v + q/M \quad (q/M \ll 1)$$

3. Heavy quark symmetry breaking terms at $O(1/M)$.



2. Decays of excited heavy baryons

(A part of) brief history of “Qqq baryon” effective theory

Brown Muck spin and parity	Heavy Mass Expansion	
$j^P = 0^+, 1^+$	LO: $\mathcal{O}(1)$	NLO: $\mathcal{O}(1/M)$
$j^P = 0^+, 1^+$	T-M. Yan, H-Y Cheng, C-Y. Cheung, G-L. Lin, Y-C. Lin,, H-L. Yu PRD46, 1148 (1992) (P-wave decay)	H-Y. Cheng, C-Y. Cheung, G-L. Lin, Y-C. Lin, T-M. Yan, H-L. Yu PRD49, 2490 (1994) (P-wave decay)
$j^P = 0^\pm, 1^\pm$ $(j^P, j^{P'})$ and $(j^P, j+1^{P'})$	H-Y. Cheng, C-K. Chua PRD75, 014006 (2007) (S-, P-, D-wave decay)	
Arbitrary j^P $(j,j)^P$ and $(j,j+1)^P$		SY. PRD91, 014031 (2015) (P-wave decay)

2. Decays of excited heavy baryons

Falk, Nucl. Phys. B378, 79 (1992)

Effective baryon field with brown muck spin j

$$\psi^{\mu_1 \dots \mu_j} = A^{\mu_1 \dots \mu_j} u_h$$

Brown muck Heavy quark
 with spin j spin 1/2
 Total spin $j \pm 1/2$

- Constraint conditions

$$\begin{aligned}
 \psi\psi^{\mu_1 \dots \mu_j} &= \psi^{\mu_1 \dots \mu_j} && \text{Positive-energy} \\
 &&& \text{heavy quark} \\
 \psi^{\mu_1 \dots \mu_k \dots \mu_\ell \dots \mu_j} &= \psi^{\mu_1 \dots \mu_\ell \dots \mu_k \dots \mu_j} \\
 v_{\mu_1} \psi^{\mu_1 \dots \mu_j} &= 0 \\
 g_{\mu_1 \mu_2} \psi^{\mu_1 \mu_2 \dots \mu_j} &= 0
 \end{aligned}
 \quad \left. \right\} \text{Cf. Rarita-Schwinger field} \\
 &&& \text{for spin 3/2}$$

- Projection to $j-1/2$ and $j+1/2$ states

$$\psi_{j-1/2}^{\mu_1 \dots \mu_{j-1}} = \sqrt{\frac{j}{2j+1}} \gamma_5 \gamma_{\mu_j} \psi^{\mu_1 \dots \mu_j}$$

$$\begin{aligned}
 \psi_{j+1/2}^{\mu_1 \dots \mu_j} &= \psi^{\mu_1 \dots \mu_j} - \frac{1}{2j+1} \left\{ (\gamma^{\mu_1} + v^{\mu_1}) \gamma_{\nu_1} g_{\nu_2}^{\mu_2} \dots g_{\nu_j}^{\mu_j} + \dots \right. \\
 &\quad \left. + g_{\nu_1}^{\mu_1} \dots g_{\nu_{j-1}}^{\mu_{j-1}} (\gamma^{\mu_j} + v^{\mu_j}) \gamma_{\nu_j} \right\} \psi^{\nu_1 \dots \nu_j}
 \end{aligned}$$

2. Decays of excited heavy baryons

SY. PRD91, 014031 (2015)

Interaction Lagrangian at LO+NLO

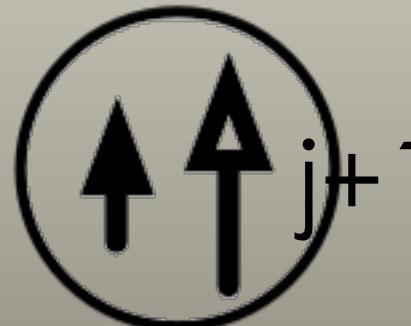
$(j, j+1)$ transitions -- different brown-muck spin $j, j+1$ in initial and final states --

$$\mathcal{L}_{\text{int}}^{(j,j+1)} = g^{(j,j+1)} \bar{\psi}_1^{\mu_1 \dots \mu_j} \mathcal{A}_{\rho_{j+1}} \psi_2^{\rho_1 \dots \rho_j \rho_{j+1}} g_{\mu_1 \rho_1} \dots g_{\mu_j \rho_j}$$

NLO (HQS breaking)

$$+ \frac{g_1^{(j,j+1)}}{M} \bar{\psi}_1^{\mu_1 \dots \mu_j} \varepsilon_{\rho_{j+1} \rho \sigma \tau} v^\rho \mathcal{A}^\sigma S_v^\tau \psi_2^{\rho_1 \dots \rho_j \rho_{j+1}} g_{\mu_1 \rho_1} \dots g_{\mu_j \rho_j} + \text{h.c.}$$

Pauli-Lubanski vector $S_v^\mu = -\frac{1}{2} \gamma_5 (\gamma^\mu \not{v} - v^\mu)$
(spin operator)



$$J=j\pm 1/2$$

$$J' = j+3/2, j+1/2$$

2. Decays of excited heavy baryons

SY. PRD91, 014031 (2015)

Constraint among decay widths

$(j, j+1)$ transitions -- different brown-muck spin $j, j+1$ in initial and final states --

$$2 \check{\Gamma}[\Psi_{3/2}^{(2)} \rightarrow \Psi_{1/2}^{(1)} \pi] - 4 \check{\Gamma}[\Psi_{3/2}^{(2)} \rightarrow \Psi_{3/2}^{(1)} \pi] = \check{\Gamma}[\Psi_{5/2}^{(2)} \rightarrow \Psi_{3/2}^{(1)} \pi] + \mathcal{O}(1/M^2)$$

$$\frac{3}{2} \check{\Gamma}[\Psi_{5/2}^{(3)} \rightarrow \Psi_{3/2}^{(2)} \pi] - 6 \check{\Gamma}[\Psi_{5/2}^{(3)} \rightarrow \Psi_{5/2}^{(2)} \pi] = \check{\Gamma}[\Psi_{7/2}^{(3)} \rightarrow \Psi_{5/2}^{(2)} \pi] + \mathcal{O}(1/M^2)$$

$$\frac{4}{3} \check{\Gamma}[\Psi_{7/2}^{(4)} \rightarrow \Psi_{5/2}^{(3)} \pi] - 8 \check{\Gamma}[\Psi_{7/2}^{(4)} \rightarrow \Psi_{7/2}^{(3)}] = \check{\Gamma}[\Psi_{9/2}^{(4)} \rightarrow \Psi_{7/2}^{(3)} \pi] + \mathcal{O}(1/M^2)$$



For any $j \geq 1$...

$$\frac{j+1}{j} \check{\Gamma}[\Psi_{j+1/2}^{(j+1)} \rightarrow \Psi_{j-1/2}^{(j)} \pi] - (2j+2) \check{\Gamma}[\Psi_{j+1/2}^{(j+1)} \rightarrow \Psi_{j+1/2}^{(j)} \pi] = \check{\Gamma}[\Psi_{j+3/2}^{(j+1)} \rightarrow \Psi_{j+1/2}^{(j)} \pi] + \mathcal{O}(1/M^2)$$

A constraint on different decay channels at $\mathcal{O}(1/M)$.

This is a “weaker” constraint to Isgur-Wise’s constraint.

2. Decays of excited heavy baryons

SY. PRD91, 014031 (2015)

Analogy

Gell-Mann, Okubo relation

$$4m_K^2 = 3m_\eta^2 + m_\pi^2$$

Flavor SU(3) symmetry breaking
(Gell-Mann, Oaks, Renner relation)

$$m_\pi^2 = 2B_0\hat{m},$$

$$m_K^2 = B_0(\hat{m} + m_s),$$

$$m_\eta^2 = \frac{2}{3}B_0(\hat{m} + 2m_s),$$

2. Decays of excited heavy baryons

SY. PRD91, 014031 (2015)

Some numerical studies ...

(1,0) transitions

$$\sum_{j=1}^Q (*) \rightarrow \Lambda_Q \pi$$

Charm

Belle, arXiv:1404.5389

$$\Gamma[\Sigma_c^{++} \rightarrow \Lambda_c^+ \pi^+] \simeq 1.84 \pm 0.04^{+0.07}_{-0.20} \text{ MeV}$$

$$\Gamma[\Sigma_c^0 \rightarrow \Lambda_c^+ \pi^-] \simeq 1.76 \pm 0.04^{+0.09}_{-0.21} \text{ MeV}$$

$$\Gamma[\Sigma_c^{*++} \rightarrow \Lambda_c^+ \pi^+] \simeq 14.77 \pm 0.25^{+0.18}_{-0.30} \text{ MeV}$$

$$\Gamma[\Sigma_c^{*0} \rightarrow \Lambda_c^+ \pi^-] \simeq 15.41 \pm 0.41^{+0.20}_{-0.32} \text{ MeV}$$

\simeq : p-wave π transition assumed

2. Decays of excited heavy baryons

SY. PRD91, 014031 (2015)

Some numerical studies ...

(1,0) transitions

$$\sum_{j=1} \Sigma_Q^{(*)} \rightarrow \Lambda_Q \pi$$

$$\Gamma[\Psi_{1/2}^{(1)} \rightarrow \Psi_{1/2}^{(0)} \pi] = \frac{1}{3} \left(g^{(1,0)^2} - \frac{2g^{(1,0)}g_1^{(1,0)}}{M} \right) K_{1/2,1/2}^{(1,0)}$$

$$\Gamma[\Psi_{3/2}^{(1)} \rightarrow \Psi_{1/2}^{(0)} \pi] = \frac{1}{3} \left(g^{(1,0)^2} + \frac{g^{(1,0)}g_1^{(1,0)}}{M} \right) K_{3/2,1/2}^{(1,0)}$$

$$g^{(0,1)} = 0.83 \quad g_1^{(0,1)}/M = 0.048 \quad \sim 6\% (?)$$

$$M = (M_{1/2}^{(1)} + 2M_{3/2}^{(1)})/3$$

2. Decays of excited heavy baryons

SY. PRD91, 014031 (2015)

Some numerical studies ...

(1,0) transitions

$$\sum_{j=1} \Sigma_Q^{(*)} \rightarrow \Lambda_Q \pi$$

Bottom PDG2014

$$\Gamma[\Sigma_b^+ \rightarrow \Lambda_b^0 \pi^+] \simeq 9.7_{-3.0}^{+4.0} \text{ MeV}$$

$$\Gamma[\Sigma_b^- \rightarrow \Lambda_b^0 \pi^-] \simeq 4.9_{-2.4}^{+3.3} \text{ MeV}$$

← **5.1 MeV**
(present theory)

$$\Gamma[\Sigma_b^{*+} \rightarrow \Lambda_b^0 \pi^+] \simeq 11.5 \pm 2.8 \text{ MeV}$$

$$\Gamma[\Sigma_b^{*-} \rightarrow \Lambda_b^0 \pi^-] \simeq 7.5 \pm 2.3 \text{ MeV}$$

← **9.6 MeV**
(present theory)

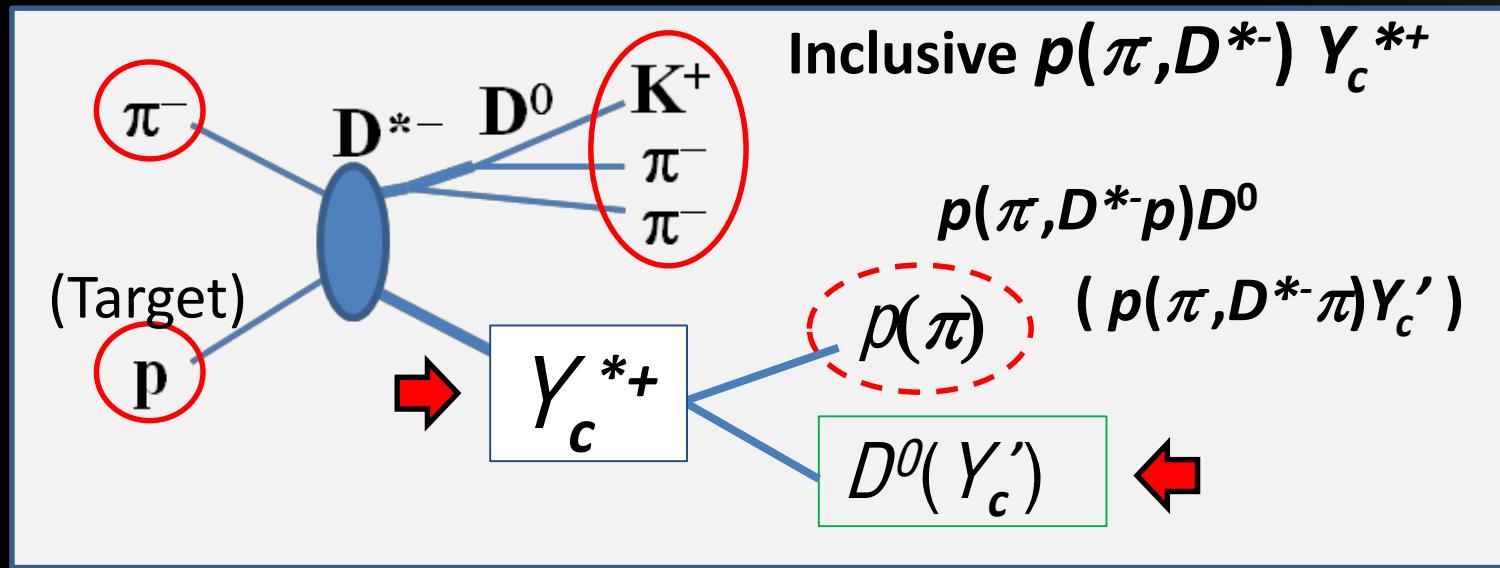
\simeq : p-wave transition supposed

3. Conclusion

1. Strong decays of one-pion emission from excited heavy baryons are discussed.
2. Heavy quark symmetry (HQS) at LO+NLO in $1/m_Q$ expansion is considered.
3. Relations for decay widths in several channels are obtained model-independently.
4. They will be useful for identifications of HQS doublet/singlet in experimental analysis.
5. Other contributions except for $1/m_Q$?
(isospin breaking, chiral expansion, etc.)

Charmed Baryon Spectroscopy

Using Missing Mass Techniques



Conducted by the E50 experiment at J-PARC

Missing Mass Spectrum (Sim.)

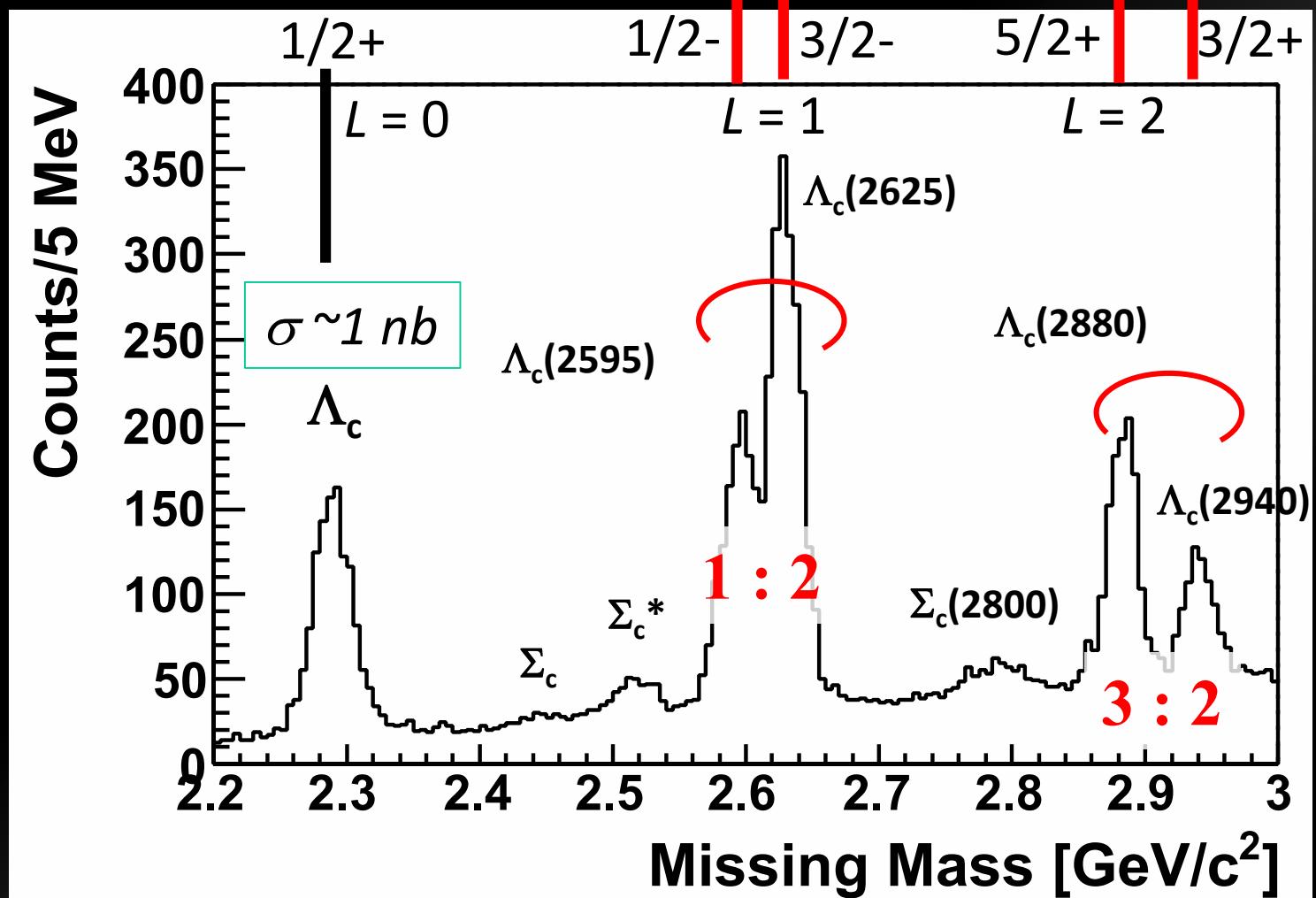
Noumi 2014

- $\sim 1000 Y_c^*/\text{nb}/100 \text{ days}$
- Sensitivity: $\sigma \sim 0.1 \text{ nb}$

for Y_c^* w/ $\Gamma = 100 \text{ MeV}$

HQS doublet

HQS doublet?



1. Heavy quark symmetry

$$\mathcal{L}_{\text{heavy quark}} = \bar{Q}(iD - m_Q)Q \quad D_\mu = \partial_\mu - igA_\mu^a T^a$$



1/m_Q expansion
(positive energy state Q_v with velocity v)

Manohar, Wise, Luke, Grinstein, ...

$$\mathcal{L}_{\text{HQET}} = \boxed{\bar{Q}_v v \cdot iD Q_v} + \bar{Q}_v \frac{(iD_\perp)^2}{2m_Q} Q_v - g_s \bar{Q}_v \frac{\sigma_{\mu\nu} G^{\mu\nu}}{4m_Q} Q_v + \mathcal{O}(1/m_Q^2)$$

LO



Heavy quark spin in $m_Q \rightarrow \infty$ is
conserved.

Heavy quark symmetry (HQS)

2. Decays of excited heavy baryons

SY. PRD91, 014031 (2015)

Interaction Lagrangian at LO+NLO

(j,j) transitions -- same brown-muck spin j in initial and final states --

$$\boxed{j \geq 1} \quad \mathcal{L}_{\text{int}}^{(j,j)} = g^{(j,j)} \bar{\psi}_1^{\mu_1 \dots \mu_j} i\varepsilon_{\mu_1 \rho_1 \alpha \beta} v^\alpha \mathcal{A}^\beta \psi_2^{\rho_1} {}_{\mu_2 \dots \mu_j}$$

NLO (velocity-rearrangement)

$$+ \frac{g^{(j,j)}}{2M} \bar{\psi}_1^{\mu_1 \dots \mu_j} i\varepsilon_{\mu_1 \rho_1 \alpha \beta} i D_\perp^\alpha(\psi_2) \mathcal{A}^\beta \psi_2^{\rho_1} {}_{\mu_2 \dots \mu_j}$$

$$- \frac{g^{(j,j)}}{2M} \bar{\psi}_1^{\mu_1 \dots \mu_j} i\varepsilon_{\mu_1 \rho_1 \alpha \beta} i \overleftarrow{D}_\perp^\alpha(\psi_1) \mathcal{A}^\beta \psi_2^{\rho_1} {}_{\mu_2 \dots \mu_j}$$

$$+ \frac{g_1^{(j,j)}}{2M} \bar{\psi}_1^{\mu_1 \dots \mu_j} S_v \cdot \mathcal{A} \psi_2^{\rho_1} {}_{\mu_1 \dots \mu_j}$$

NLO (HQS breaking)

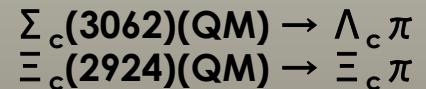
$$+ \frac{g_2^{(j,j)}}{2M} \bar{\psi}_1^{\mu_1 \dots \mu_j} (S_{v\mu_1} \mathcal{A}_{\rho_1} + S_{v\rho_1} \mathcal{A}_{\mu_1}) \psi_2^{\rho_1} {}_{\mu_2 \dots \mu_j}$$

$$+ \text{h.c.} + \mathcal{O}(1/M^2)$$

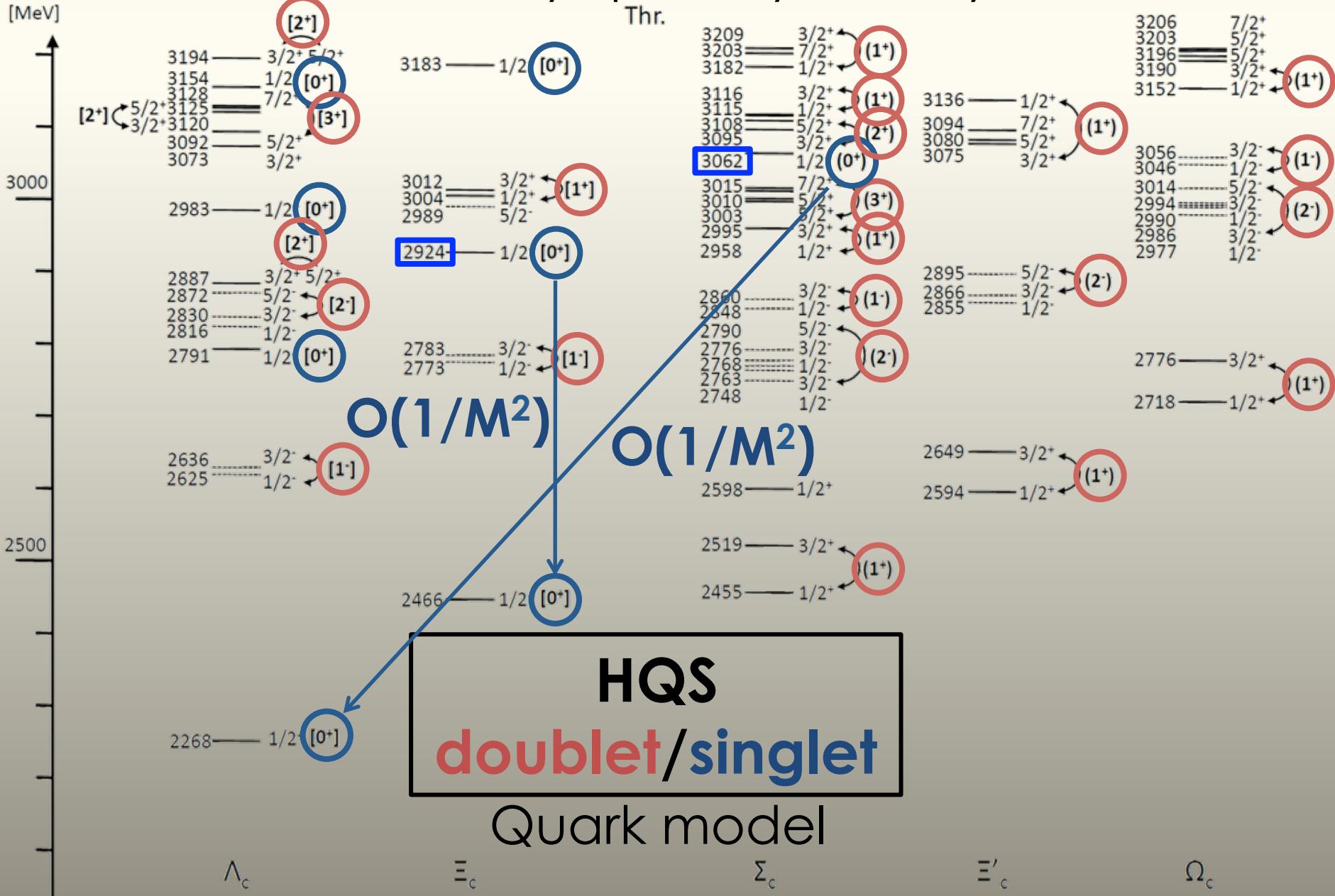
$$\boxed{j = 0}$$

$$\mathcal{L}_{\text{int}}^{(0,0)} = \frac{g_1^{(0,0)}}{M} \bar{\psi}_1 S_v \cdot \mathcal{A} \psi_2 + \text{h.c.} + \mathcal{O}(1/M^2)$$

$1/2^\pm \rightarrow 1/2^\pm$ transition
is very small, $\mathcal{O}(1/M^2)$.



1. Heavy quark symmetry



2. Decays of excited heavy baryons

SY. PRD91, 014031 (2015)

Interaction Lagrangian at LO+NLO

(j,j) transitions -- same brown-muck spin j in initial and final states --

$$\check{\Gamma}(\Psi_{1/2}^{(1)} \rightarrow \Psi'_{3/2}^{(1)} \pi) = 2 \check{\Gamma}(\Psi_{3/2}^{(1)} \rightarrow \Psi'_{1/2}^{(1)} \pi) + \mathcal{O}(1/M^2)$$

$$\check{\Gamma}(\Psi_{3/2}^{(2)} \rightarrow \Psi'_{5/2}^{(2)} \pi) = \frac{3}{2} \check{\Gamma}(\Psi_{5/2}^{(2)} \rightarrow \Psi'_{3/2}^{(2)} \pi) + \mathcal{O}(1/M^2)$$

$$\check{\Gamma}(\Psi_{5/2}^{(3)} \rightarrow \Psi'_{7/2}^{(3)} \pi) = \frac{4}{3} \check{\Gamma}(\Psi_{7/2}^{(3)} \rightarrow \Psi'_{5/2}^{(3)} \pi) + \mathcal{O}(1/M^2)$$

↓ For any $j \geq 1$...

$$\check{\Gamma}[\Psi_{j-1/2}^{(j)} \rightarrow \Psi'_{j+1/2}^{(j)} \pi] = \frac{j+1}{j} \check{\Gamma}[\Psi_{j+1/2}^{(j)} \rightarrow \Psi'_{j-1/2}^{(j)} \pi] + \mathcal{O}(1/M^2)$$

This holds not only at $\mathcal{O}(1/M)$ but also at $\mathcal{O}(1)$.

2. Decays of excited heavy baryons

SY. arXiv:1408.3703

Constraint among decay widths

$(j, j+1)$ transitions

$$2 \check{\Gamma}[\Psi_{3/2}^{(2)} \rightarrow \Psi_{1/2}^{(1)} \pi] - 4 \check{\Gamma}[\Psi_{3/2}^{(2)} \rightarrow \Psi_{3/2}^{(1)} \pi] = \check{\Gamma}[\Psi_{5/2}^{(2)} \rightarrow \Psi_{3/2}^{(1)} \pi] + \mathcal{O}(1/M^2)$$

$$\frac{3}{2} \check{\Gamma}[\Psi_{5/2}^{(3)} \rightarrow \Psi_{3/2}^{(2)} \pi] - 6 \check{\Gamma}[\Psi_{5/2}^{(3)} \rightarrow \Psi_{5/2}^{(2)} \pi] = \check{\Gamma}[\Psi_{7/2}^{(3)} \rightarrow \Psi_{5/2}^{(2)} \pi] + \mathcal{O}(1/M^2)$$

$$\frac{4}{3} \check{\Gamma}[\Psi_{7/2}^{(4)} \rightarrow \Psi_{5/2}^{(3)} \pi] - 8 \check{\Gamma}[\Psi_{7/2}^{(4)} \rightarrow \Psi_{7/2}^{(3)}] = \check{\Gamma}[\Psi_{9/2}^{(4)} \rightarrow \Psi_{7/2}^{(3)} \pi] + \mathcal{O}(1/M^2)$$



For any $j \geq 1$...

$$\frac{j+1}{j} \check{\Gamma}[\Psi_{j+1/2}^{(j+1)} \rightarrow \Psi_{j-1/2}^{(j)} \pi] - (2j+2) \check{\Gamma}[\Psi_{j+1/2}^{(j+1)} \rightarrow \Psi_{j+1/2}^{(j)} \pi] = \check{\Gamma}[\Psi_{j+3/2}^{(j+1)} \rightarrow \Psi_{j+1/2}^{(j)} \pi] + \mathcal{O}(1/M^2)$$

A constraint on different decay channels at $\mathcal{O}(1/M)$.

This is a “weaker” constraint to Isgur-Wise’s constraint.

2. Decays of excited heavy baryons

SY. arXiv:1408.3703

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$$\frac{3}{2} \check{\Gamma}[\Psi_{5/2}^{(3)} \rightarrow \Psi_{3/2}^{(2)} \pi]$$

Example: $j=1$

$$\frac{4}{3} \check{\Gamma}[\Psi_{3/2}^{(2)} \rightarrow \Psi_{1/2}^{(1)} \pi] = \frac{5}{18} \left(g^{(1,2)2} - \frac{g^{(1,2)} g_1^{(1,2)}}{M} \right) K_{3/2,1/2}^{(2,1)}$$

$$\Gamma[\Psi_{3/2}^{(2)} \rightarrow \Psi_{3/2}^{(1)} \pi] = \frac{1}{18} \left(g^{(1,2)2} - \frac{4g^{(1,2)} g_1^{(1,2)}}{M} \right) K_{3/2,3/2}^{(2,1)}$$

$$\frac{j+1}{j} \check{\Gamma}[\Psi_j^{(2)} \rightarrow \Psi_{j-1}^{(1)} \pi] = \frac{1}{3} \left(g^{(1,2)2} + \frac{g^{(1,2)} g_1^{(1,2)}}{M} \right) K_{5/2,3/2}^{(2,1)}$$

$$K_{J_2,J_1}^{(j+1,j)} = \frac{1}{2\pi f_\pi^2} \left(\Delta_{J_2,J_1}^{(j+1,j)2} - m_\pi^2 \right)^{3/2}$$

$$\Delta_{J_2,J_1}^{(j+1,j)} = m_\pi^2 / 2M_{J_2}^{(j+1)} + M_{J_2}^{(j+1)} - M_{J_1}^{(j)}$$

$\mathcal{O}(1/M^2)$

$\mathcal{O}(1/M^2)$

$\pi] + \mathcal{O}(1/M^2)$

$\mathcal{O}(1/M)$.

A cons.

1. Heavy quark symmetry

Heavy quark symmetry (HQS)

