

Solar Neutrinos, the physics gold mine

Hamish Robertson, NDM12, Nara, June 2012

Solar gold

- Neutrino oscillations, mass, explain the solar neutrino problem.
- Θ_{12} and Θ_{13} accurately known now.
- Solar models very accurate (metals abundance remains in doubt, but minor).



What is the future for solar neutrinos?

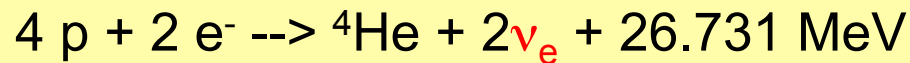
- Our challenge is a 1% measurement of the TOTAL neutrino luminosity. Comparison with the electromagnetic luminosity will test for sterile neutrinos and whether there is solar variability, with climate consequences.

1%

Can we DO that?

Simplicity of the luminosity test:

Energy from Hydrogen Burning:



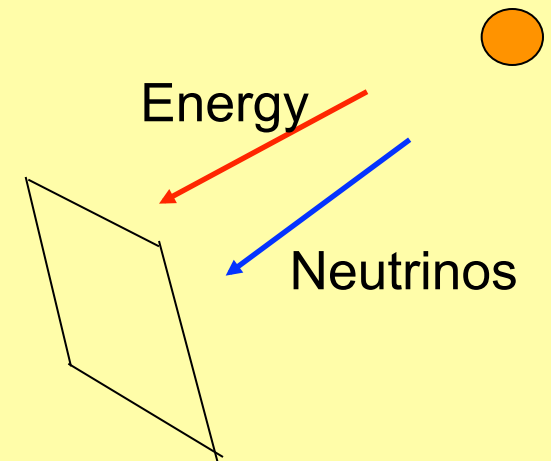
Measured power reaching Earth:

$$137 \text{ mW cm}^{-2} = 8.53 \times 10^{11} \text{ MeV cm}^{-2} \text{ s}^{-1}$$

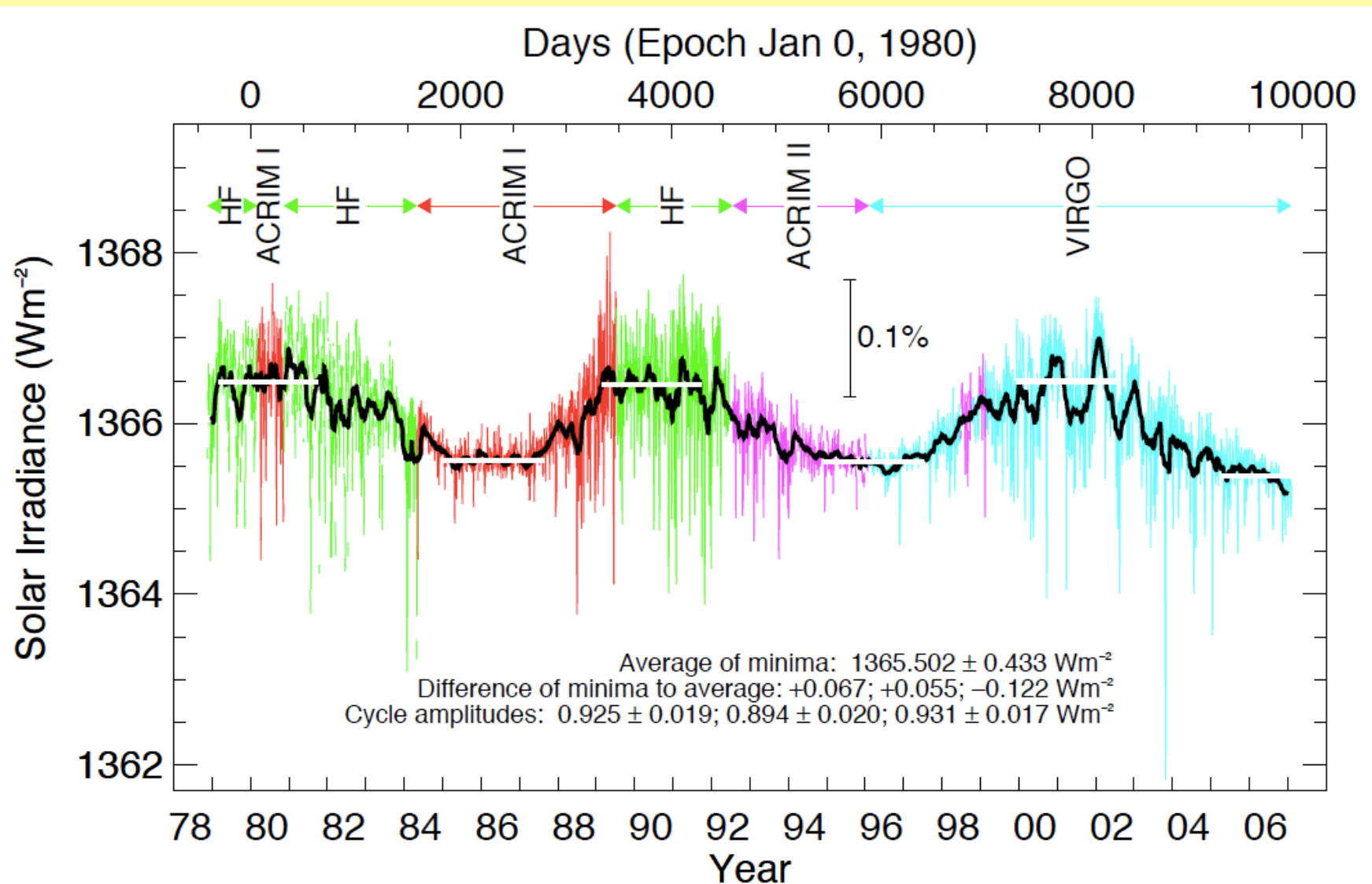
So... the neutrino flux is

$$\frac{2 \times 8.53 \times 10^{11}}{26.731}$$

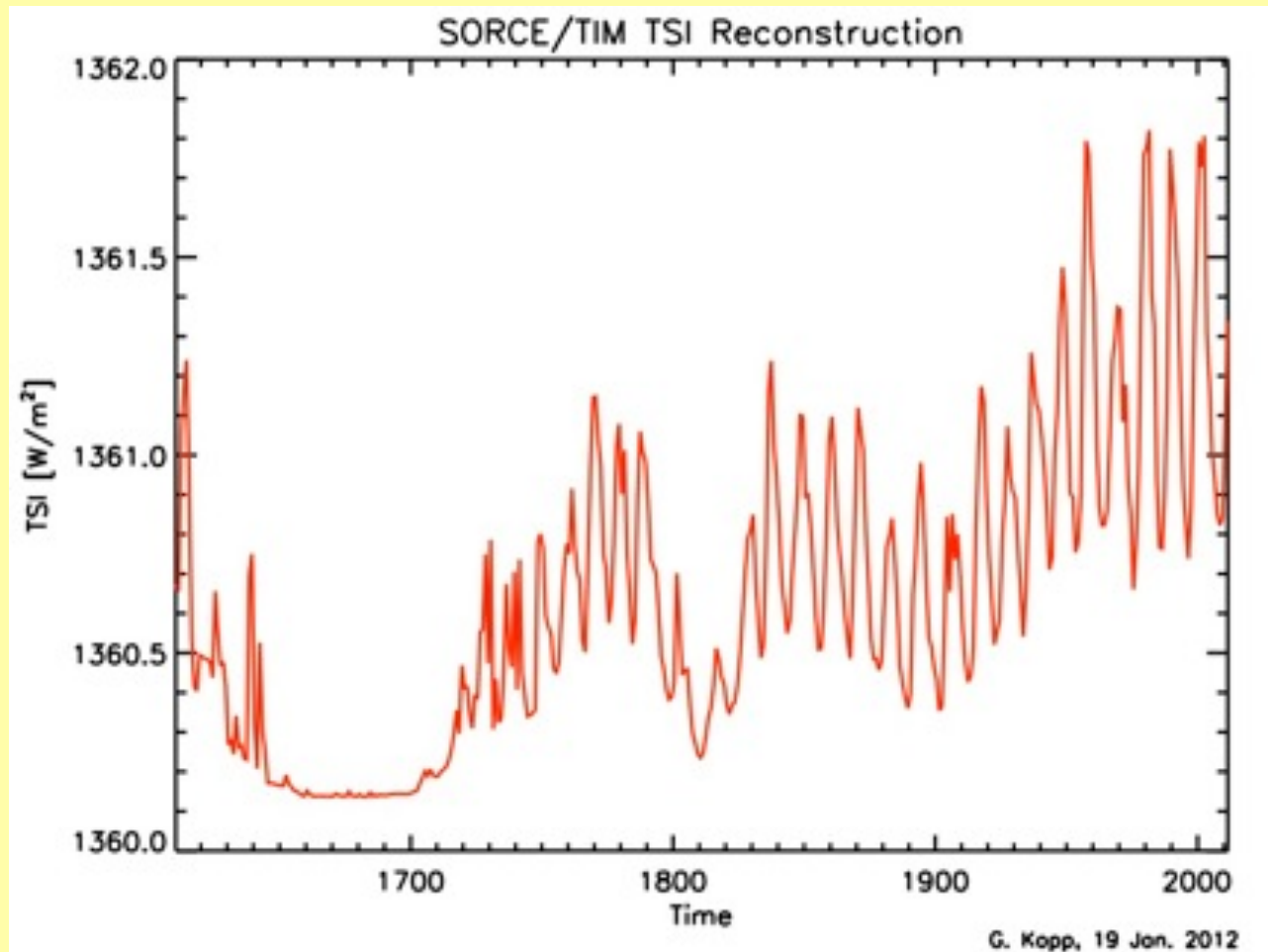
$$= 6.38 \times 10^{10} \nu_e \text{ cm}^{-2} \text{ s}^{-1}$$



Solar Irradiance



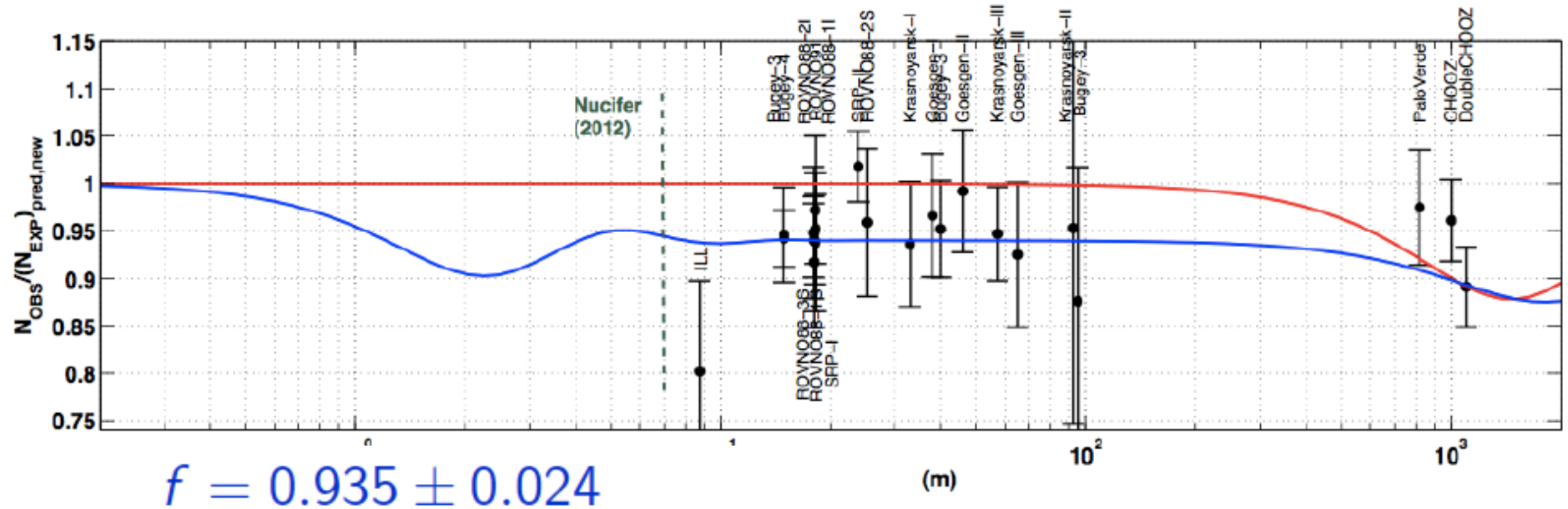
Solar Irradiance from Sunspot Numbers



Kopp & Lean; Geophys. Res. Lett., **38**, L01706 (2011).

Reactor anomaly

Mention et al., 1101.2755



$$\chi^2_{\min} = 15.7/18 \quad (P = 61\%)$$

$$\chi^2_{f=1} = 23.0/19 \quad (P = 2.4\%)$$

$$\Delta\chi^2_{f=1} = 7.25 \quad (2.7\sigma)$$

T. Schwetz, Nu2012

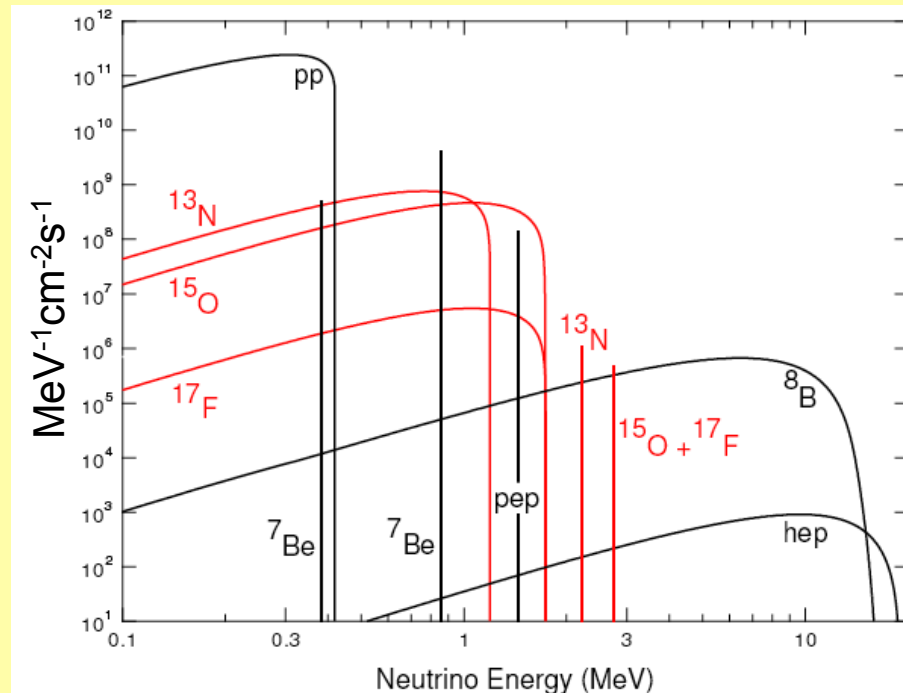
The Neutrino Luminosity

Some corrections and assumptions:--

Residual heat from formation
(gravitation, deuterium burning)
<<1%

Quasi-static burning (^3He , CNO)

The practical problem $\rightarrow$



The Luminosity Constraint:

$$\sum_i \eta_i \Phi_i = \frac{2I}{Q}$$

$$I = 85.31(34) \times 10^{10} \text{ MeV cm}^{-2} \text{ s}^{-1} \text{ (solar irradiance)}$$

What do we need?

Source	η_i
pp	0.9799
pep	0.8917
${}^7\text{Be}$	0.9352
${}^8\text{B}$	0.4979
CNO (${}^{13}\text{N} + {}^{15}\text{O}$)	0.9363
hep	0.7609

DATA:

SAGE, Gallex/GNO:

Borexino: $1.6(3) \times 10^8 \text{ cm}^{-2}\text{s}^{-1}$

Borexino: $4.89(24) \times 10^9 \text{ cm}^{-2}\text{s}^{-1}$

SNO: $5.25(19) \times 10^6 \text{ cm}^{-2}\text{s}^{-1}$

Borexino: $<3.7 \times 10^8 \text{ cm}^{-2}\text{s}^{-1}$

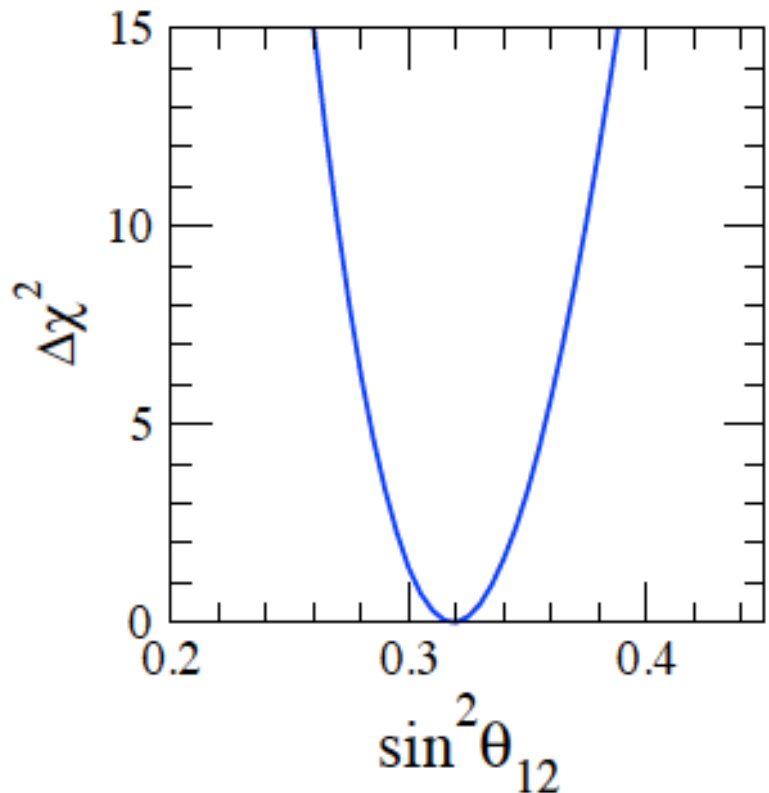
SNO: $<2 \times 10^4 \text{ cm}^{-2}\text{s}^{-1}$

θ_{12} SNO, SK, KamLAND

θ_{13} D-Chooz, Daya Bay, RENO

Recent global analyses

Forero et al. 1205.4018v2

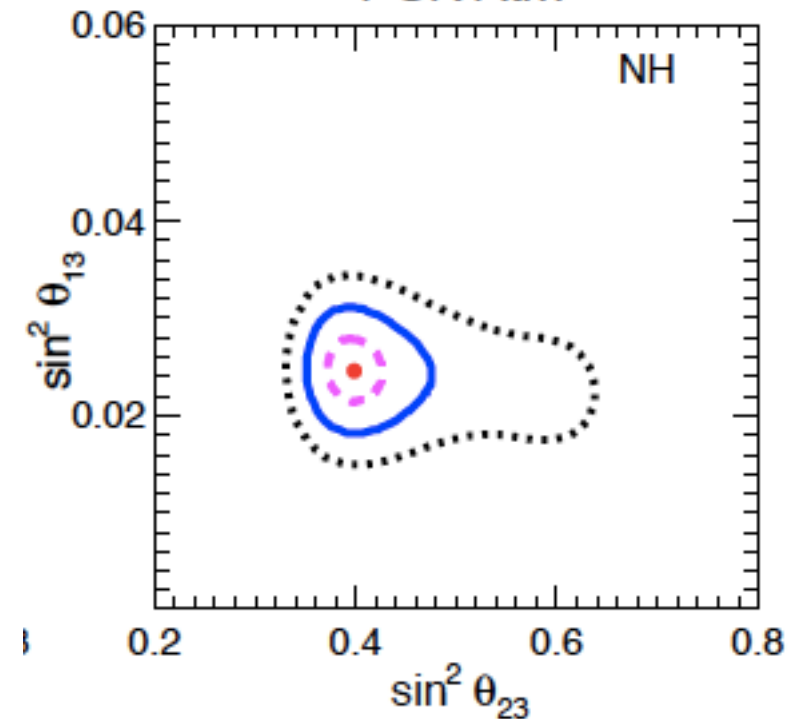


$$\sin^2 \theta_{12} = 0.320^{+0.015}_{-0.017}$$

$$\sin^2 \theta_{13} = 0.026^{+0.003}_{-0.004}$$

Fogli et al. 1205.5254v2

LBL + Solar + KamLAND
+ SBL Reactors
+ SK Atm



$$\sin^2 \theta_{12} = 0.307^{+0.018}_{-0.015}$$

$$\sin^2 \theta_{13} = 0.0245^{+0.0034}_{-0.0031}$$

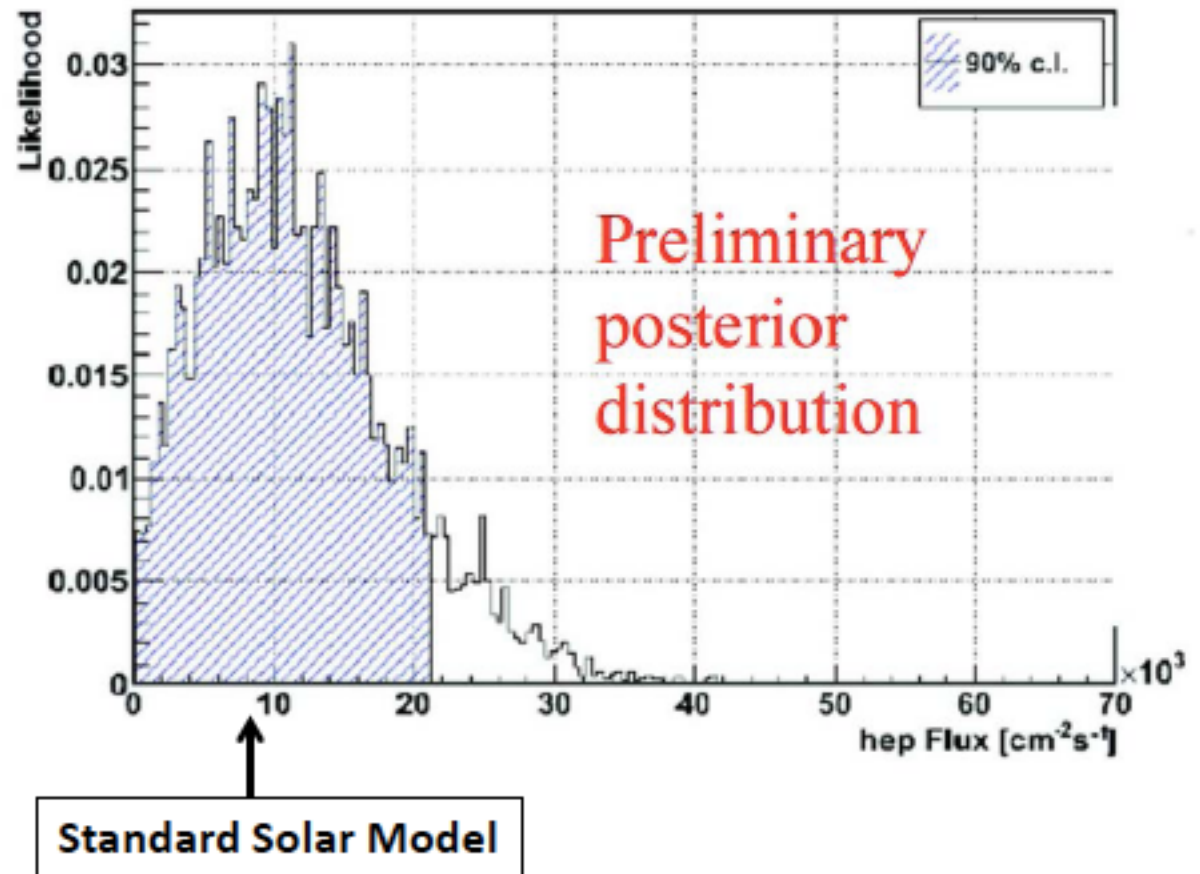
SNO *hep* limit

hep neutrino flux: Chris Howard SNO thesis, to be published

Preliminary MCMC fit to all SNO data.

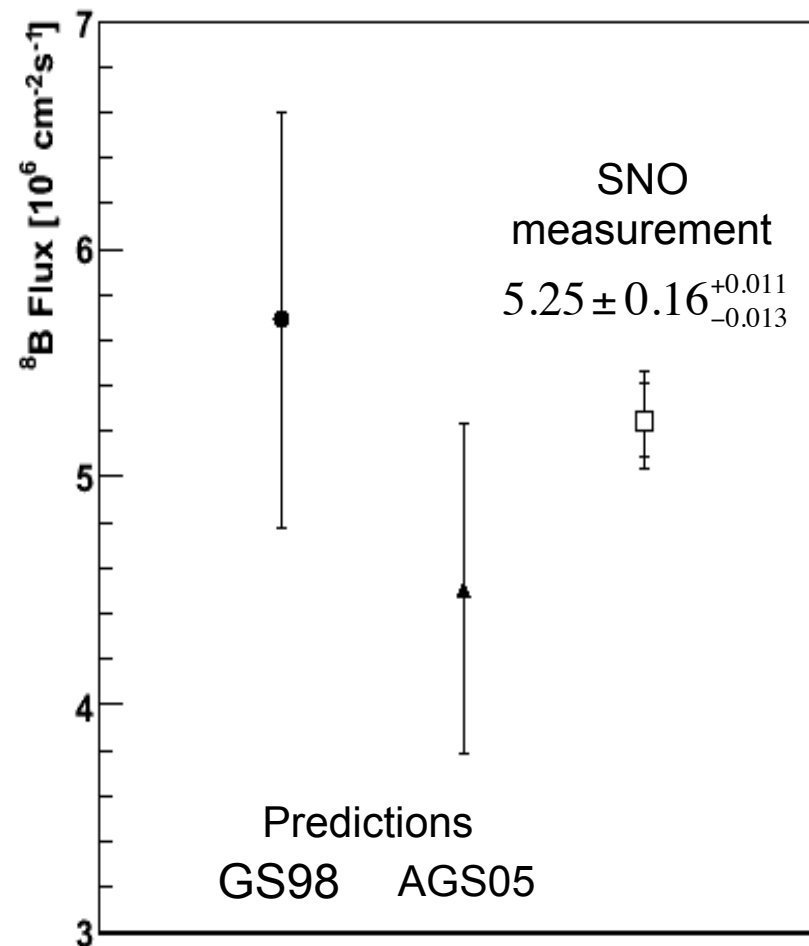
Limit of $22 \times 10^3 \text{ cm}^{-2}/\text{s}$ (90%)

Consistent with
SSM: $8 \times 10^3 \text{ cm}^{-2}/\text{s}$



^8B Solar Neutrino Flux

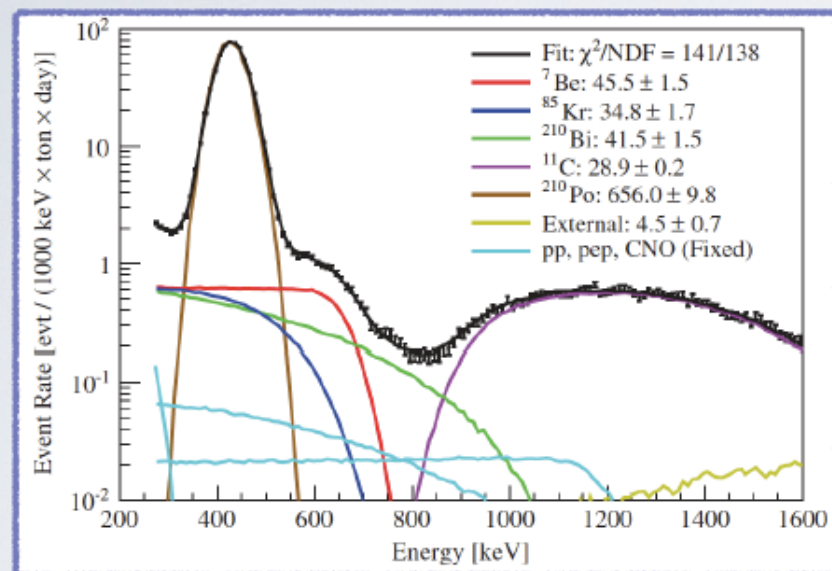
B. Aharmim et al. 1109.0763v1



^7Be RATE (II)

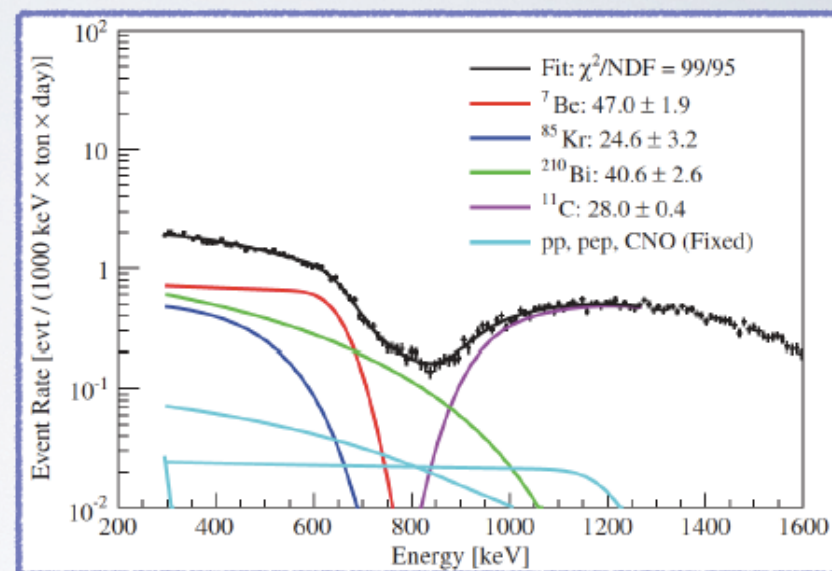
- Two approaches to control systematic errors due to analysis procedure:

Monte Carlo fit to the spectrum,
no α/β ^{210}Po peak subtraction



Phys. Rev. Lett. 107, 141302, 2011

Analytical fit to the spectrum,
after α/β ^{210}Po peak subtraction



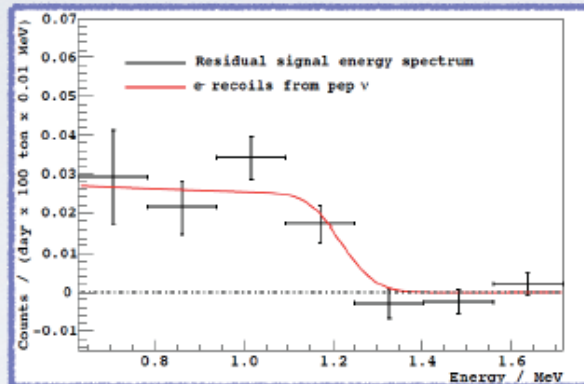
- Very Consistent results, small difference included in sys. uncertainty
- Rate for 100 t target:
 - 46.0 ± 1.5 (stat) ± 1.5 (sys) c d⁻¹**

Source	%
Trigger efficiency and stability	< 0.1
Live time	0.04
Scintillator density	0.05
Fiducial volume	+0.5 -1.3
Fit methods	2
Energy response	2.7
Sacrifice of cuts	0.1
Total	+3.4 -3.6

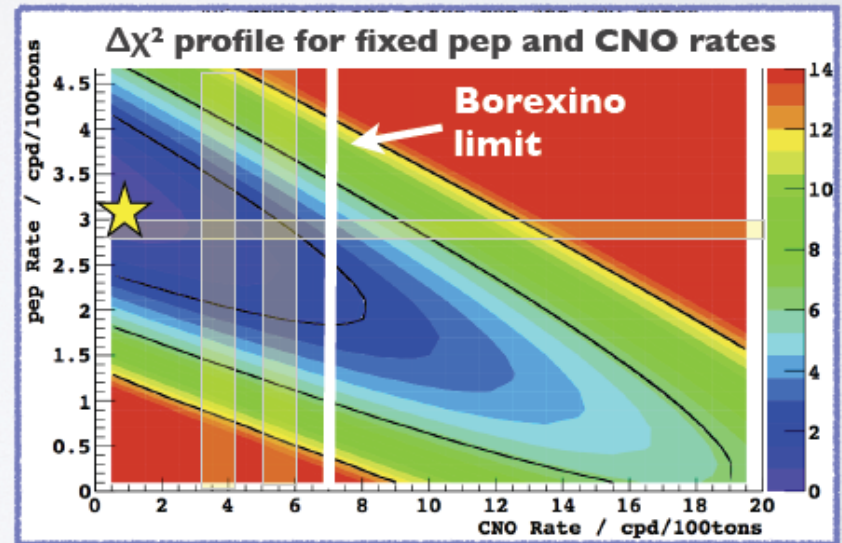
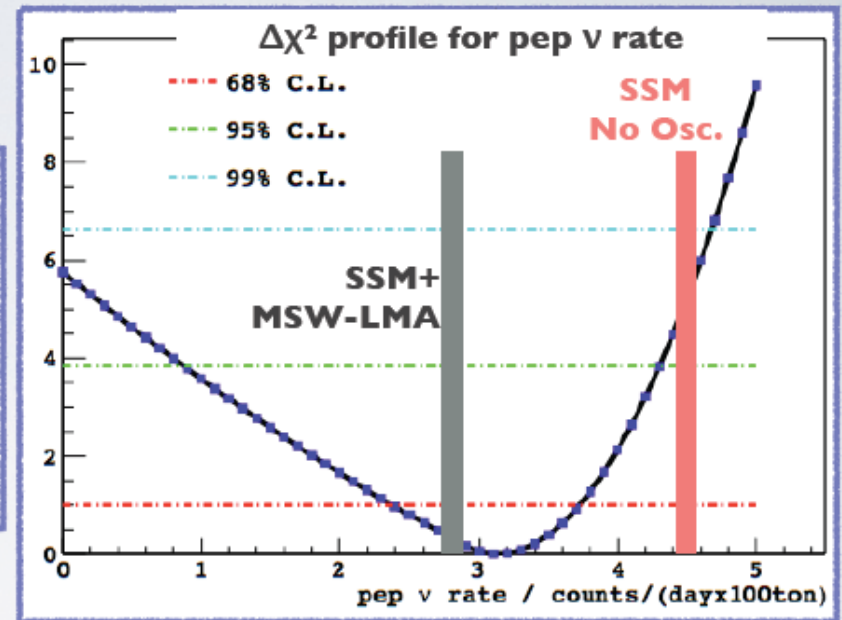
FIRST DETECTION OF **PEP** NEUTRINOS (ν)

- Rate: $3.1 \pm 0.6_{\text{(stat)}} \pm 0.3_{\text{(sys)}} \text{ cpd}/100 \text{ t}$
PRL 108, 051302 (2012)

- No oscillations excluded at **97% c.l.**
- Absence of pep solar ν excluded at 98%



- Assuming MSW-LMA:
 - $\Phi_{\text{pep}} = 1.6 \pm 0.3 \cdot 10^8 \text{ cm}^{-2} \text{ s}^{-1}$
- CNO limit obtained assuming pep @ SSM
 - CNO rate** $< 7.1 \text{ cpd}/100 \text{ t}$ (95% c.l.)



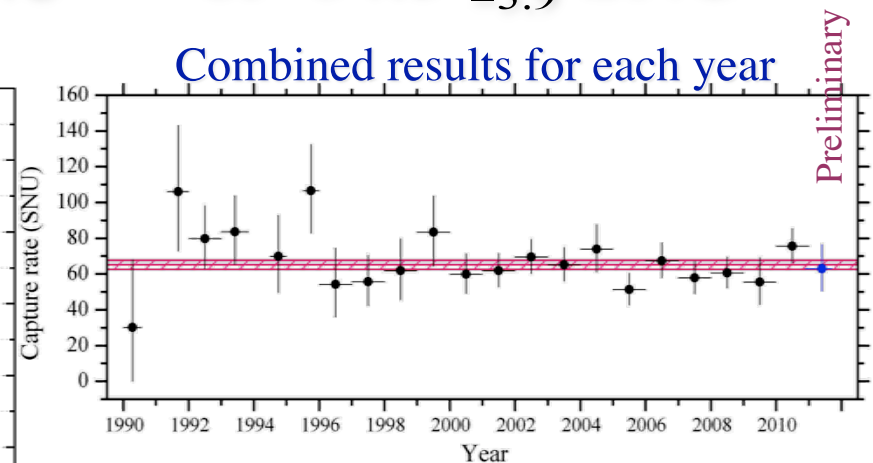
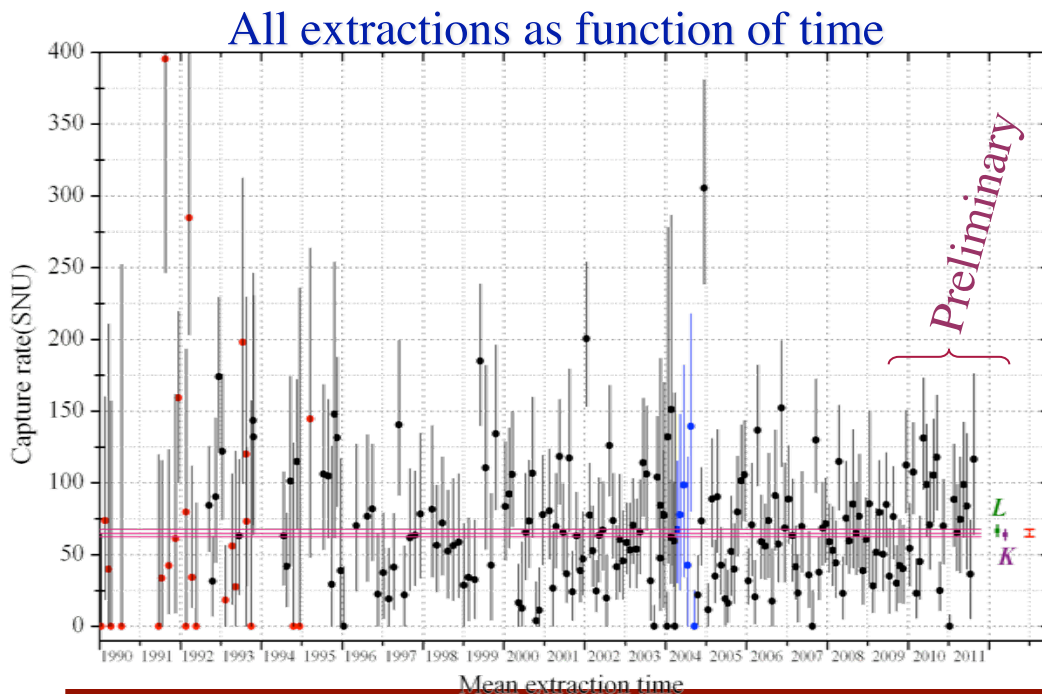


Presently **SAGE** is the only experiment sensitive to the *pp* neutrinos

It has the **longest almost uninterrupted time of measurements** among operating solar neutrino experiments

20.6 year period (1990 – 11.2011): 214 runs, 396 separate counting sets

Result : $64.5^{+2.7}_{-2.7}(\text{stat})^{+2.6}_{-2.8}(\text{syst}) \text{ SNU}$ or $64.5^{+3.7}_{-3.9} \text{ SNU}$



(1 SNU = 1 interaction/s in a target that contains 10^{36} atoms of the neutrino absorbing isotope).

SAGE continues to perform regular solar neutrino extractions every four weeks with ~50 t of Ga

Luminosity measurement plan

Only two fluxes are significant, pp and ${}^7\text{Be}$. Others are $\sim 1\%$ or less.

A neutral-current measurement at low energies seems out of reach for the foreseeable future.

Therefore we must use CC and/or ES measurements and oscillation parameters to deduce the total active flux.

For a 1% measurement:

- precisely known cross-sections

- precisely known oscillation parameters (we have 5%)

- high statistics

- low systematics

Four possible strategies

1. Make direct measurements of pp and ${}^7\text{Be}$ by ES.
2. Use pep measurement by ES to determine pp by calculation.
3. Use pep measurement by ES to normalize a CC measurement of pp and ${}^7\text{Be}$.
4. Use available data and validate the model.

Precise cross sections required

- Elastic scattering is very precisely known.
- CC reactions to ground states known by detailed balance.
- CC reactions can be calibrated with sources.
- Distribution is a continuum.
- Radiochemical rates include excited states.
- Intense sources, geometrical factors are complications.

Neutrino-electron scattering

't Hooft PLB37, 1971

$$\frac{d\sigma}{dT} = \frac{2G_F^2 m_e}{\pi} \left[g_L^2 + g_R^2 \left(1 - \frac{T}{E_\nu}\right)^2 - g_L g_R \frac{m_e T}{E_\nu^2} \right]$$

T is electron kinetic energy, and:

$$\frac{2G_F^2 m_e}{\pi} = 1.7233 \times 10^{-44} \text{ cm}^2$$

Electron neutrinos:

$$g_L = \sin^2 \theta_W + 1/2 = 0.73119(14)$$

$$g_R = \sin^2 \theta_W = 0.23119(14)$$

Mu, tau neutrinos:

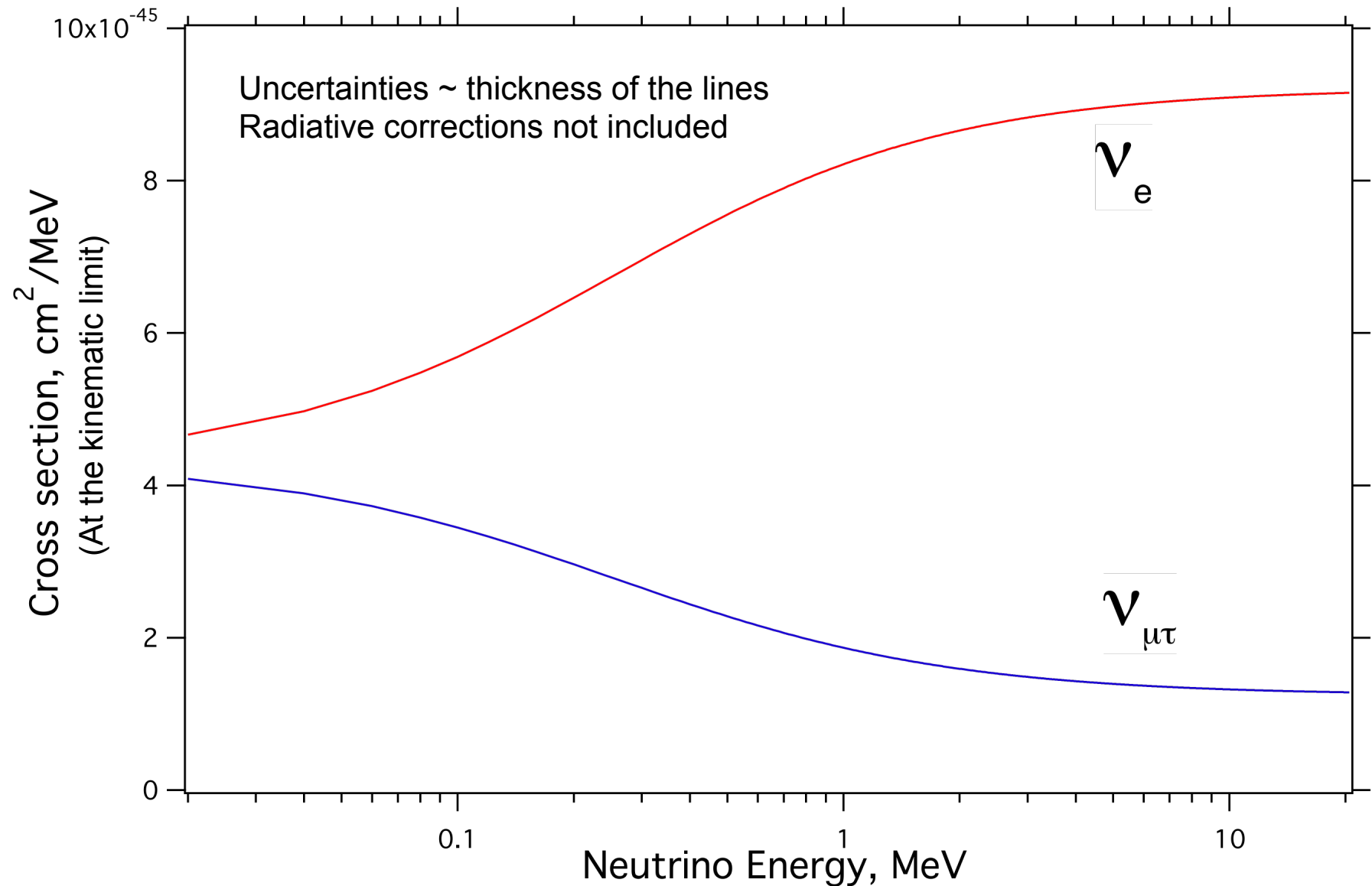
$$g_L = \sin^2 \theta_W - 1/2 = -0.26881(14)$$

$$g_R = \sin^2 \theta_W = 0.23119(14)$$

Kinematic limit:

$$T \leq \frac{2E_\nu^2}{2E_\nu + m_e}$$

Neutrino – electron scattering



The ES ‘miracle’

The rate observed in an experiment where both electron and non-electron flavors are present is

$$\begin{aligned} R &\sim [\sigma_e P_{ee} + \sigma_{\mu\tau}(1 - P_{ee})] \Phi \\ &= [P_{ee}(\sigma_e - \sigma_{\mu\tau}) + \sigma_{\mu\tau}] \Phi \end{aligned}$$

where P_{ee} is the electron neutrino survival probability, σ_α is the differential cross section for scattering of flavor α , and Φ is the active flux.

$$\frac{d\Phi}{\Phi} = - \left[1 + \frac{\sigma_{\mu\tau}}{P_{ee}(\sigma_e - \sigma_{\mu\tau})} \right]^{-1} \frac{dP_{ee}}{P_{ee}}$$

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Flux	E_ν	$\frac{d\Phi}{dP_{ee}} \frac{P_{ee}}{\Phi}$
	MeV	
<i>pp</i>	0.42 - 0.513	
${}^7\text{Be}$	0.86 - 0.616	
<i>pep</i>	1.44 - 0.651	

The ES 'miracle' 2

$$\begin{aligned} P_{ee} &= (1 - \sin^2 \theta_{13})^2 (1 - 2 \sin^2 \theta_{12} + 2 \sin^4 \theta_{12}) + \sin^4 \theta_{13} \\ &\equiv (1 - S_{13})(1 - 2S_{12} + 2S_{12}^2) + S_{13}^2 \end{aligned}$$

The survival probability depends on the oscillation parameters as follows:

$$\begin{aligned} \frac{dP_{ee}}{P_{ee}} &= \frac{-2S_{12} + 4S_{12}^2}{P_{ee}} \frac{dS_{12}}{S_{12}} \\ \frac{dP_{ee}}{P_{ee}} &= \frac{-S_{13}(1 - 2S_{12} + 2S_{12}^2) + 2S_{13}^2}{P_{ee}} \frac{dS_{13}}{S_{13}} \end{aligned}$$

With the current best-fit values, $S_{12} = 0.307(17)$ and $S_{13} = 0.0245(32)$, the logarithmic derivative ratios are,

$$\begin{aligned} \frac{dP_{ee}}{P_{ee}} &= -0.422 \frac{dS_{12}}{S_{12}} \\ \frac{dP_{ee}}{P_{ee}} &= -0.028 \frac{dS_{13}}{S_{13}} \end{aligned}$$

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 \end{aligned}$$

	Flux	E_ν	Flux Uncert.
		MeV	%
pp	0.42		1.22
${}^7\text{Be}$	0.86		1.45
pep	1.44		1.54

Determination of the neutrino luminosity

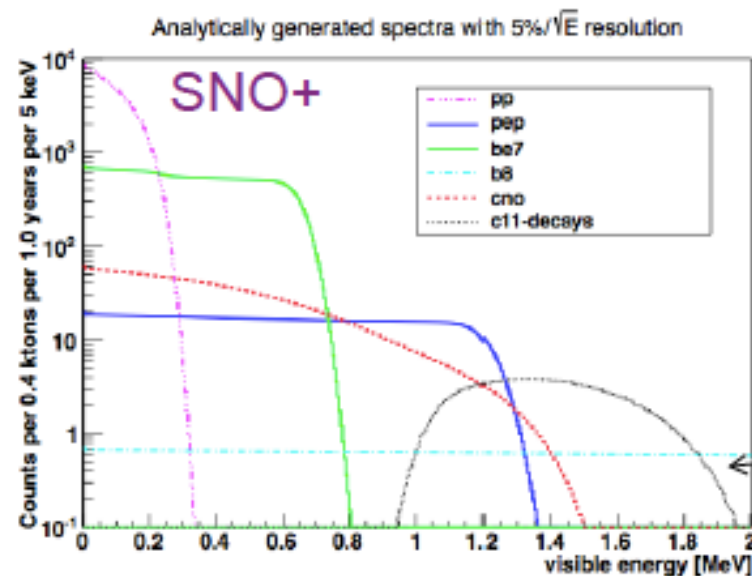
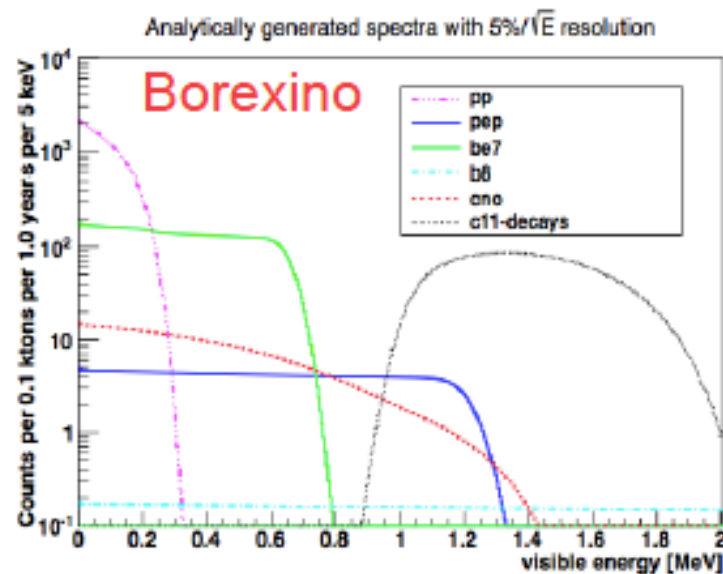
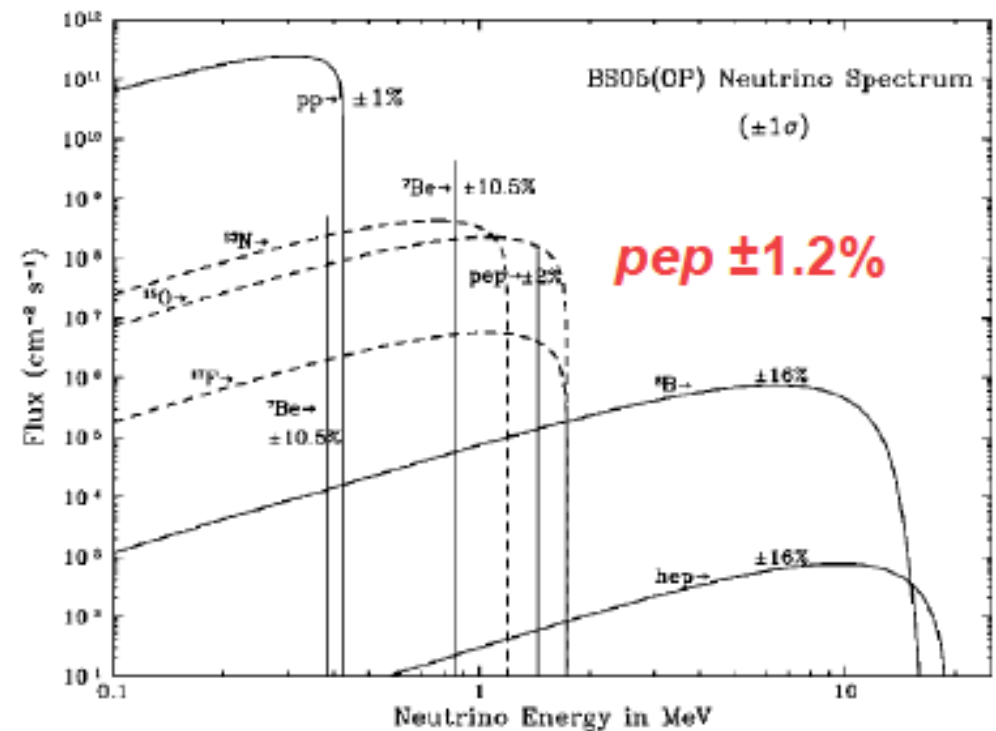
Gonzalez-Garcia et al. 0910.4584v4:

$$\frac{L_{\odot}(\text{neutrino-inferred})}{L_{\odot}} = 1.00 \pm 0.14 \left[{}^{+0.37}_{-0.34} \right] .$$



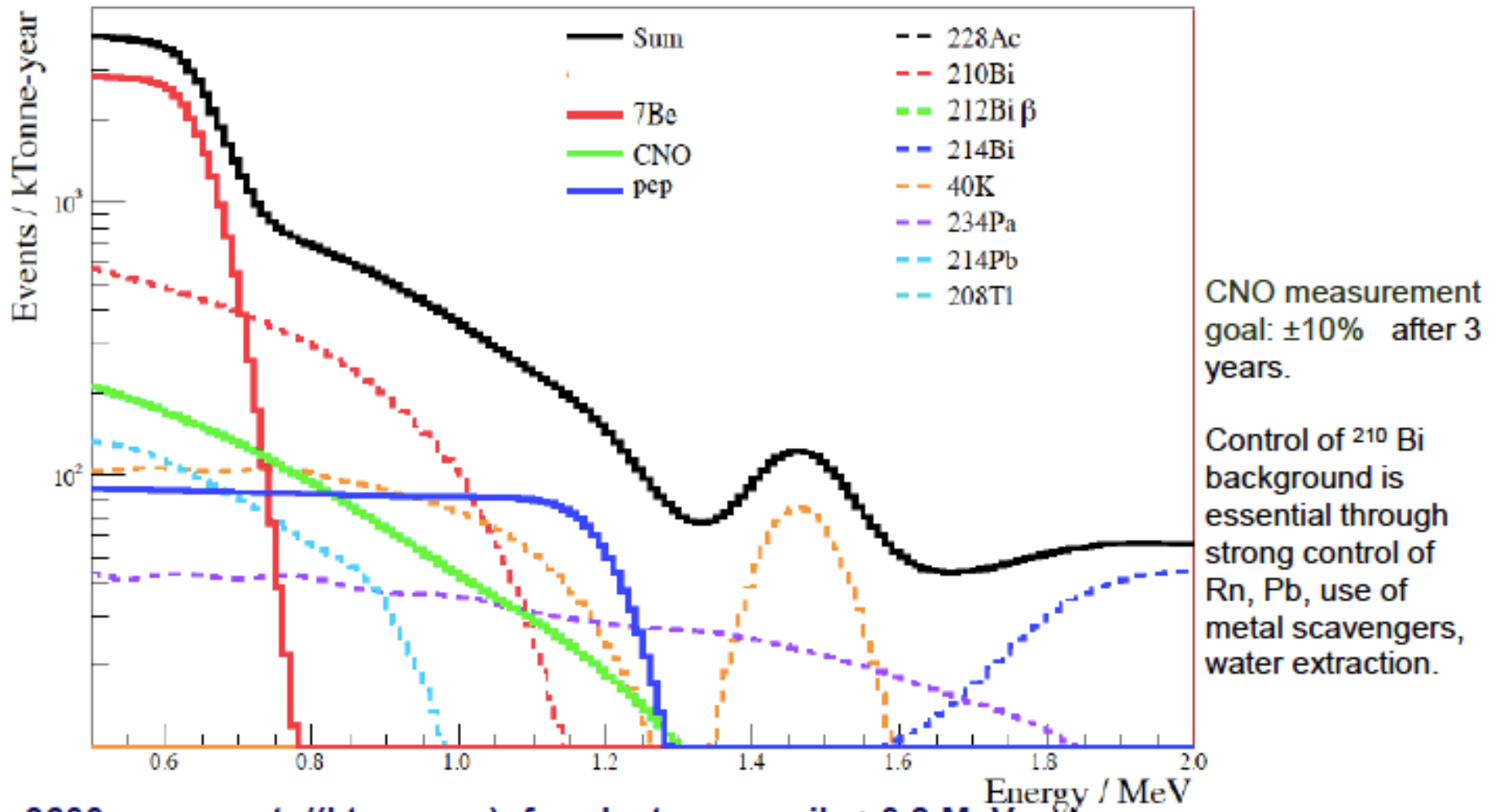
- will detect pep solar neutrinos without cosmogenic ^{11}C background (in Borexino and KamLAND)

- $R = \Phi P_{ee} \sigma$
- known flux, known cross section
- thus measurement probes the neutrino survival probability with few% precision



^{11}C background can be cut further using muon tracks.

SNO+ pep and CNO Solar Neutrino Signals



3600 *pep* events/(kton·year), for electron recoils >0.8 MeV

goal: $\pm 5\%$ total uncertainty after 3 years (including systematic and SSM)

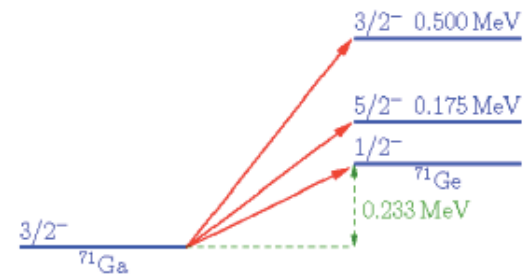
pep and *pp* closely related

$$R_{p+e+p} \cong 5.51 \times 10^{-5} \rho (1 + X) T_6^{-1/2} (1 + 0.02 T_6) R_{p-p}$$

Bahcall & May, Ap. J. 155 (1969)

The Gallium cross section

the reaction $\nu_e + {}^{71}\text{Ga} \rightarrow {}^{71}\text{Ge} + e^-$
can proceed to the ground state or
through excited states of ${}^{71}\text{Ge}$



$$\sigma^x = \sigma_{\text{g.s.}}^x \left(1 + a_x \frac{\text{BGT}_{175}}{\text{BGT}_{\text{g.s.}}} + b_x \frac{\text{BGT}_{500}}{\text{BGT}_{\text{g.s.}}} \right) \quad (x = \text{Cr, Ar})$$

previous calculations based on estimates of GT strengths

Bahcall hep-ph/9710491, Haxton nucl-th/9804011

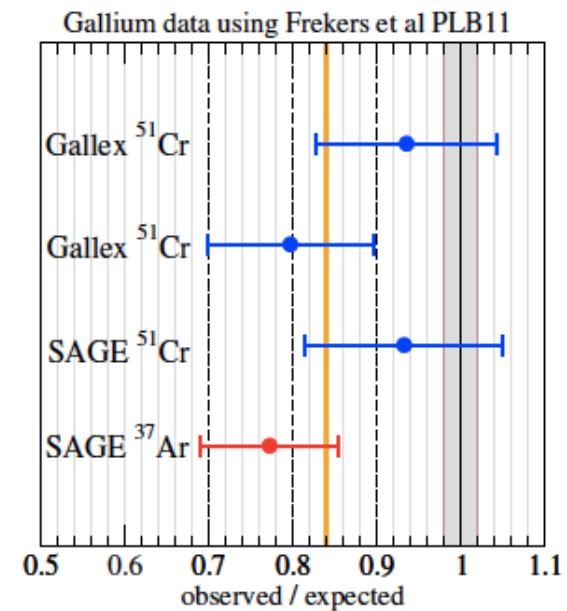
recent measurement of ${}^{71}\text{Ga}({}^3\text{He}, t){}^{71}\text{Ge}$ D. Frekers et al., PLB 706, 134 (2011):

$$\frac{\text{BGT}_{175}}{\text{BGT}_{\text{g.s.}}} = 0.0399 \pm 0.0305 \quad \frac{\text{BGT}_{500}}{\text{BGT}_{\text{g.s.}}} = 0.207 \pm 0.016$$

$\Rightarrow$ contribution of $7.2 \pm 2.0\%$ from excited states (for ${}^{51}\text{Cr}$)

Gallium data

D. Frekers et al., PLB 706, 134 (2011) BGT determinations lead to a correction of ratios relative to Bahcall expectation by factor 0.982 (0.977) for Cr (Ar) sources



combined fit: $\chi^2_{\min} = 2.3/3 \text{ dof}$ $r = 0.84^{+0.054}_{-0.051}$ $\Delta\chi^2_{r=1} = 8.7 (2.9\sigma)$

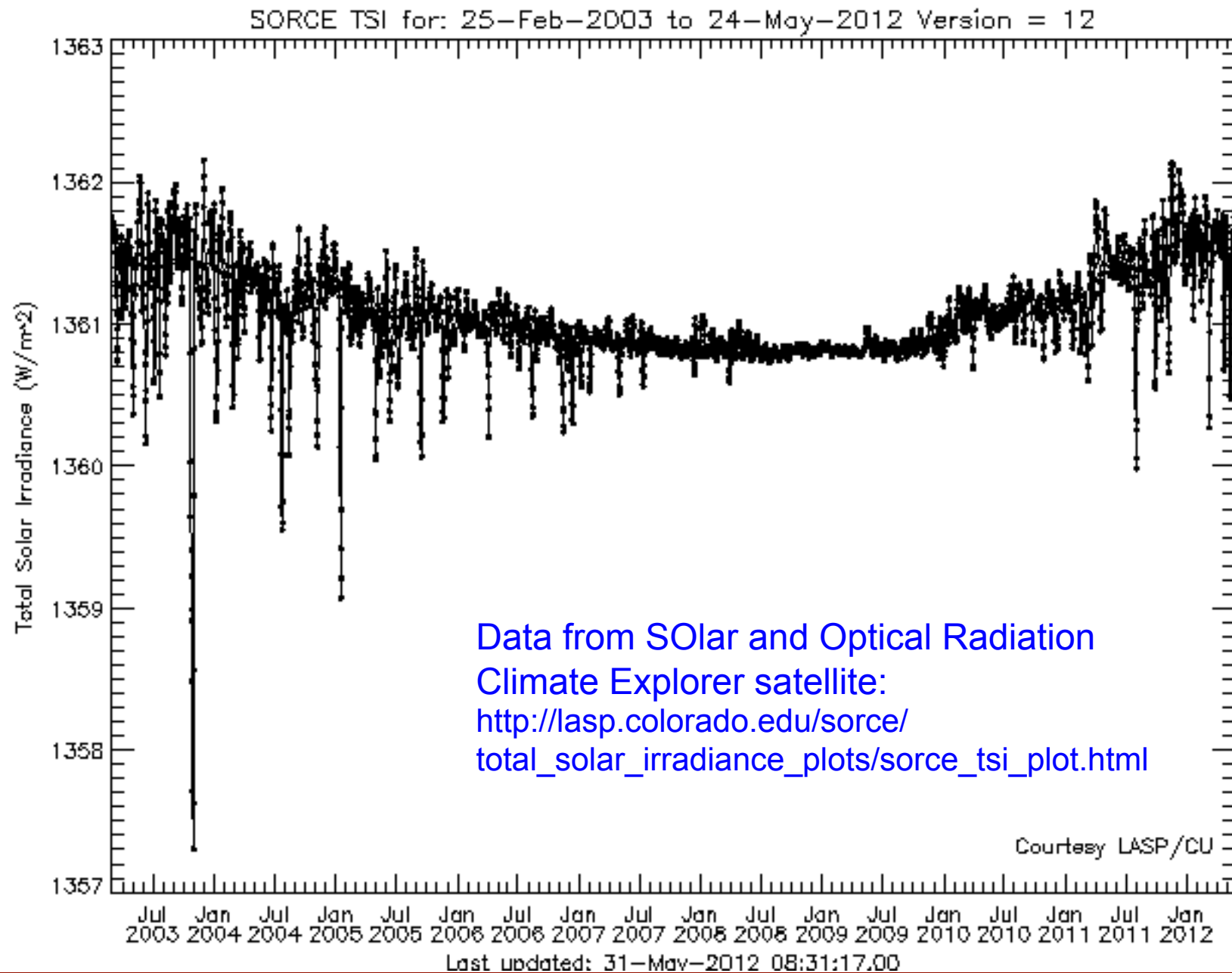
Using the neutrino luminosity

Electromagnetic Luminosity	85.35×10^{10}	$\text{MeV cm}^{-2} \text{ s}^{-1}$
Sum of known fluxes x η_i (not Ga)	4.89×10^9	$\text{cm}^{-2} \text{ s}^{-1}$
`Predicted' pp flux	$6.01(3) \times 10^{10}$	$\text{cm}^{-2} \text{ s}^{-1}$
GS98	5.98×10^{10}	$\text{cm}^{-2} \text{ s}^{-1}$
AGSS09	6.03×10^{10}	$\text{cm}^{-2} \text{ s}^{-1}$
Use Ga data	$6.30(47) \times 10^{10}$	$\text{cm}^{-2} \text{ s}^{-1}$
Neutrino Luminosity scaled by Reactor Anomaly	$79.8(20) \times 10^{10}$	$\text{MeV cm}^{-2} \text{ s}^{-1}$
`Predicted' pp ν_a flux	$5.59(15) \times 10^{10}$	$\text{cm}^{-2} \text{ s}^{-1}$
Difference	$0.71(49) \times 10^{10}$	$\text{cm}^{-2} \text{ s}^{-1}$

Summary

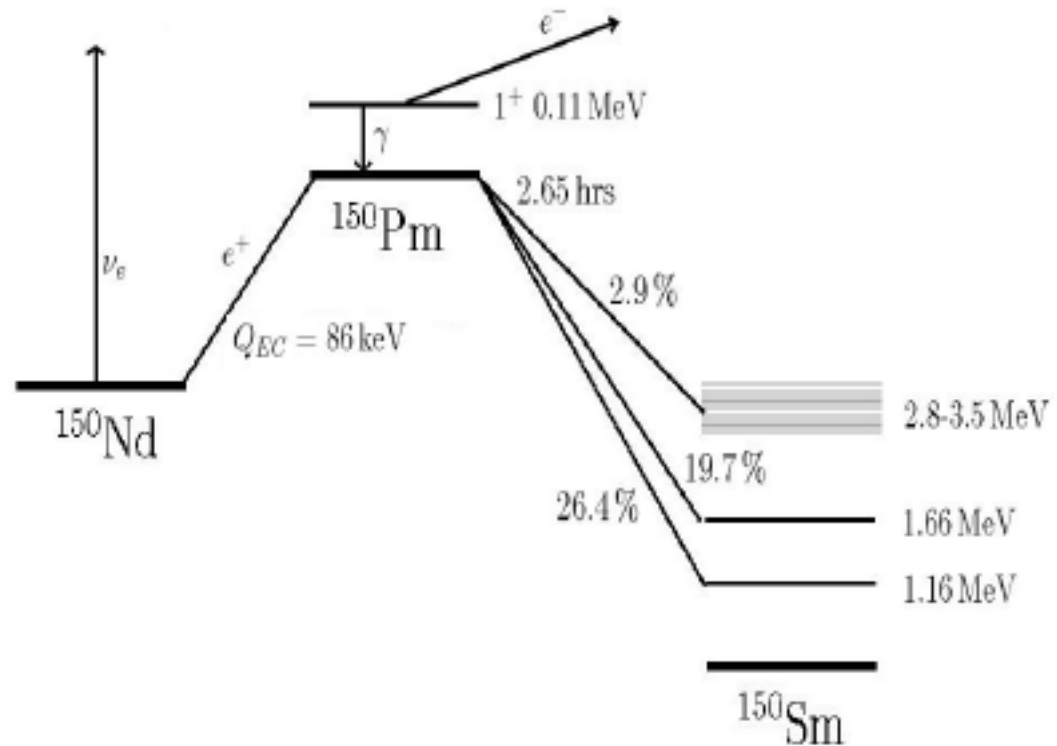
- A $\sim 1\%$ measurement of the ν luminosity **appears achievable**. We need a good pp or pep measurement by ES.
- Current data with Ga and no SSM **disfavors** reactor anomaly at $\sim 90\%$ CL.
- Strong tension between **solar** and **source** data for Ga experiments.

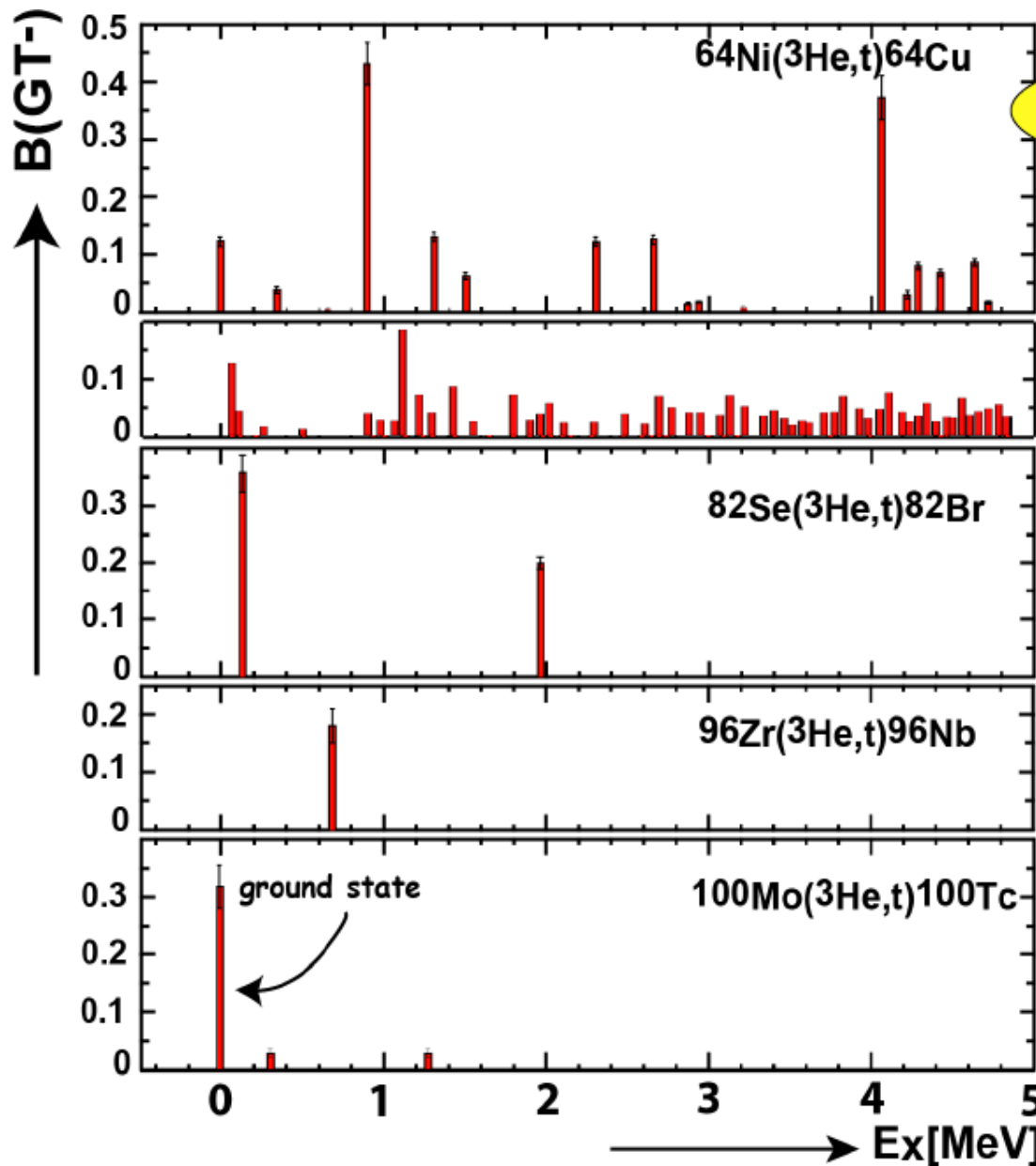
FIN



A Low-Threshold Solar Neutrino Target

K. Zuber PLB 709, 6 (2012).





$^{64}\text{Zn}(\epsilon\epsilon, \epsilon\beta^+)$

$^{76}\text{Ge}(\beta\beta^-)$

$^{82}\text{Se}(\beta\beta^-)$

$^{96}\text{Zr}(\beta\beta^-)$

$^{100}\text{Mo}(\beta\beta^-)$

reduced
spreading
of GT
strength

D. Frekers, 2011 (INT)

SAGE Baksan, Russia



50 tons of metallic Ga

1990-2011, running

214 runs (Jan 1990 – Dec 2011) give
the result: **$64.5^{+3.7}_{-3.8}$ SNU**

The weighted average of the results of all Ga experiments is now

GALLEX/GNO Gran Sasso, Italy



30 tons of Ga

(103 tons of GaCl_3 acidic solution)

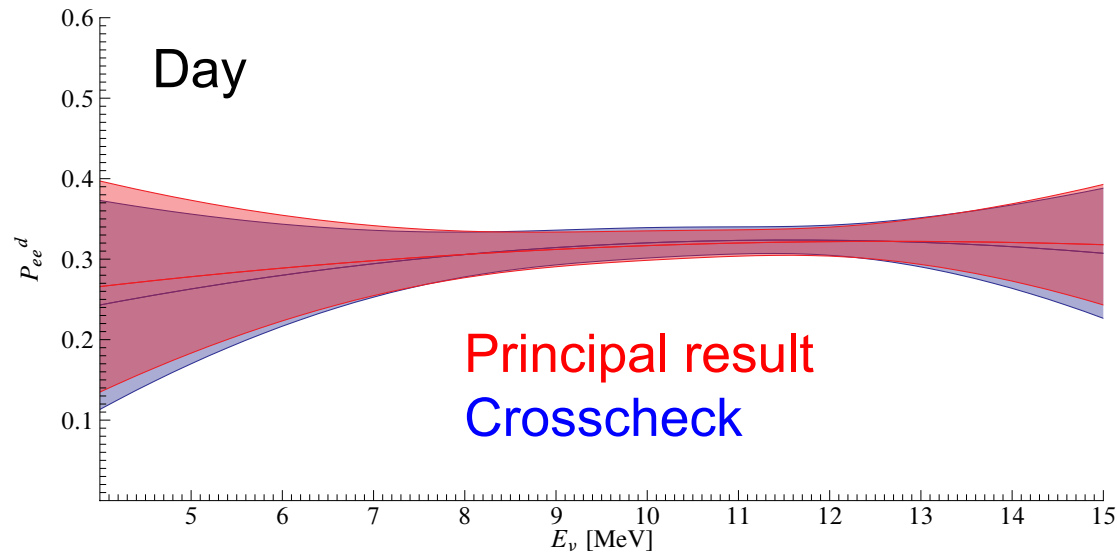
1991-2003

123 runs (May 1991 – Apr 2003) give
the result: **67.5 ± 5.1 SNU**

66.1 ± 3.1 SNU

NDM12 Nara June 10, 2012

Survival Probability



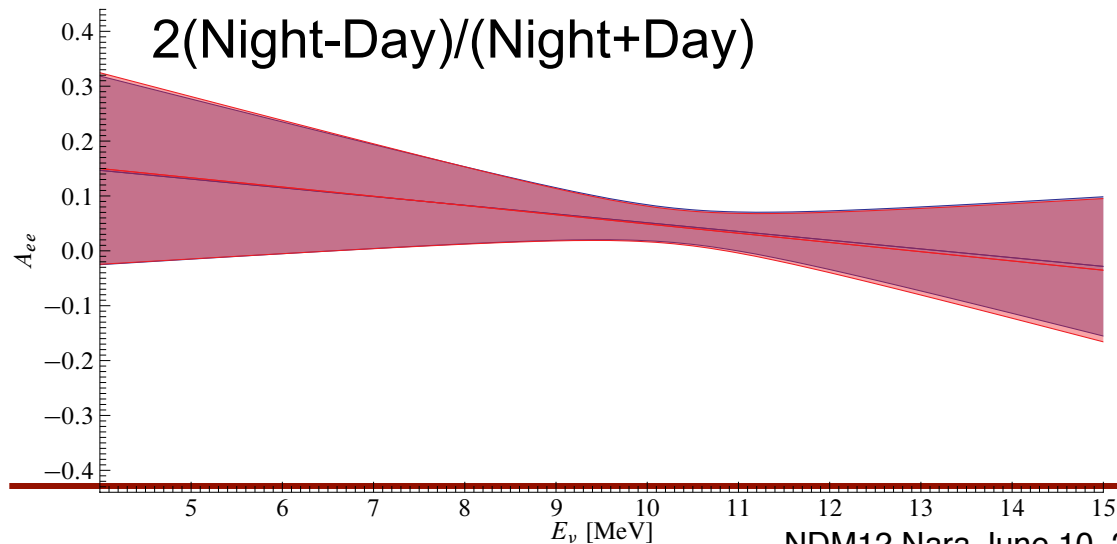
$$c_0 = 0.317 \pm 0.016 \pm 0.009$$

$$c_1 = 0.0039^{+0.0065}_{-0.0067} \pm 0.0045$$

$$c_2 = -0.0010 \pm 0.0029^{+0.0014}_{-0.0016}$$

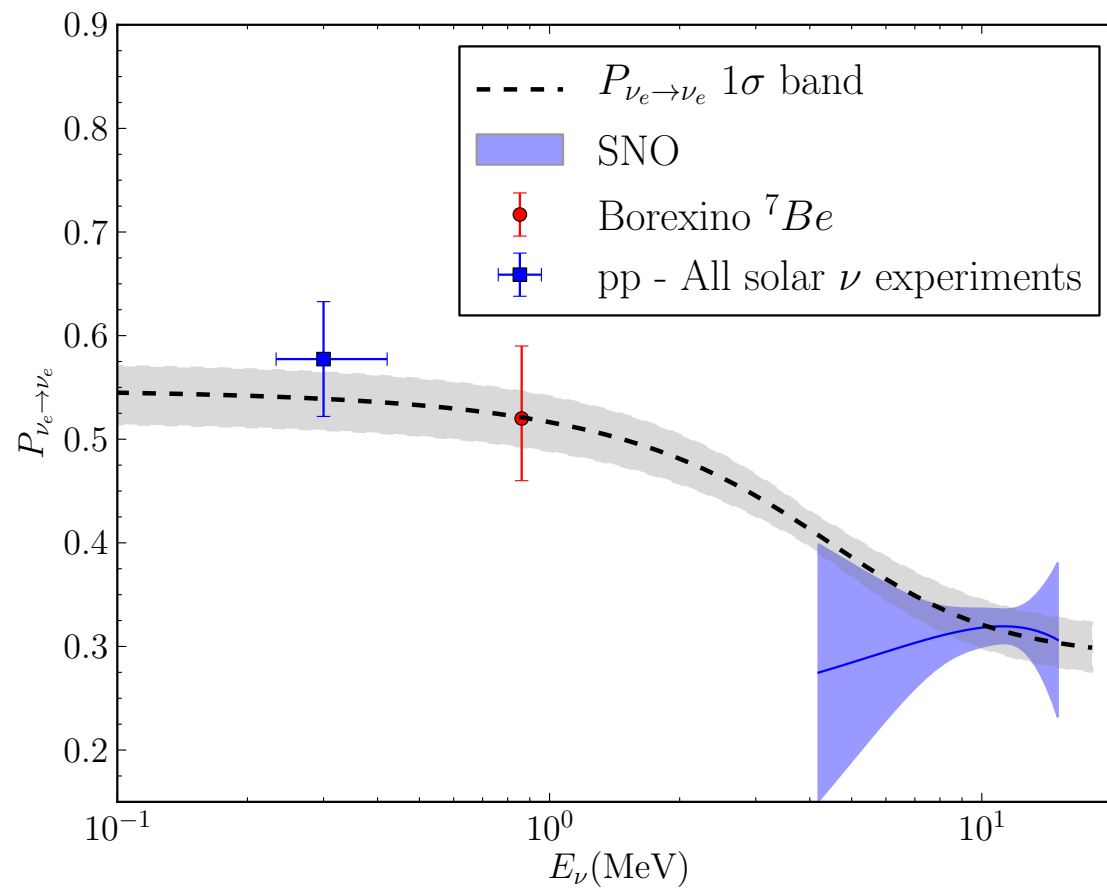
$$a_0 = 0.046 \pm 0.031^{+0.014}_{-0.013}$$

$$a_1 = -0.016 \pm 0.025^{+0.010}_{-0.011}$$

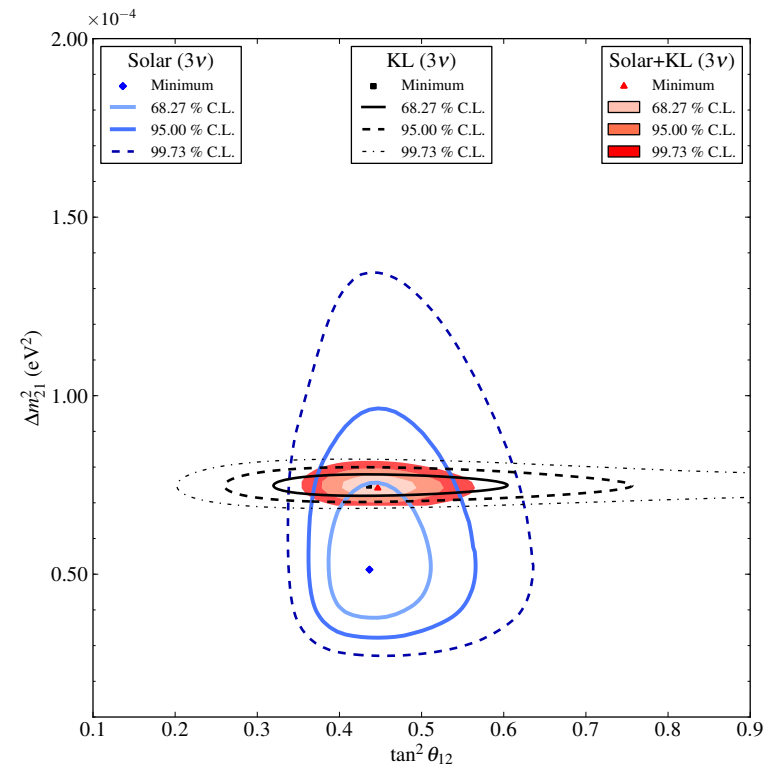
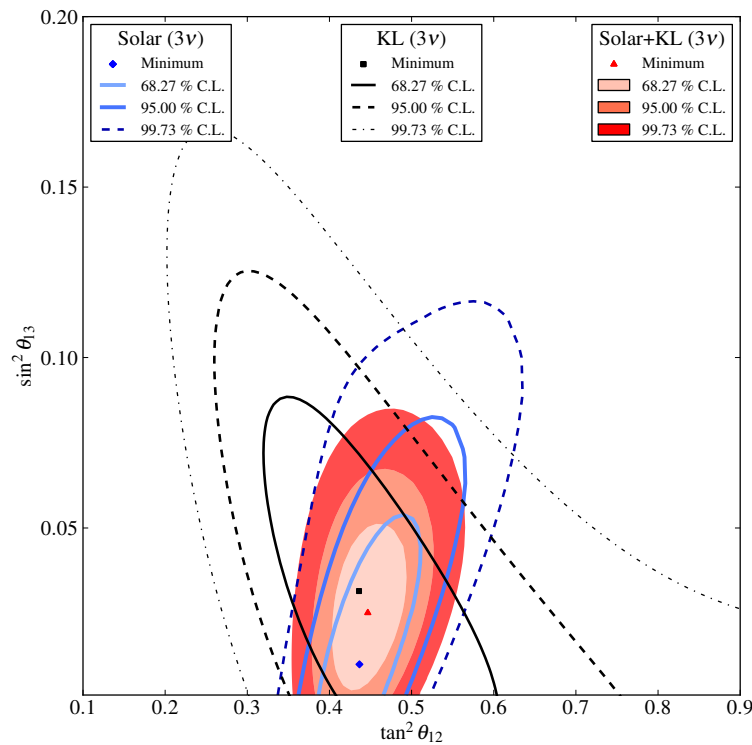


Approximately 20%
improvement over
previous analysis.

MSW Solution



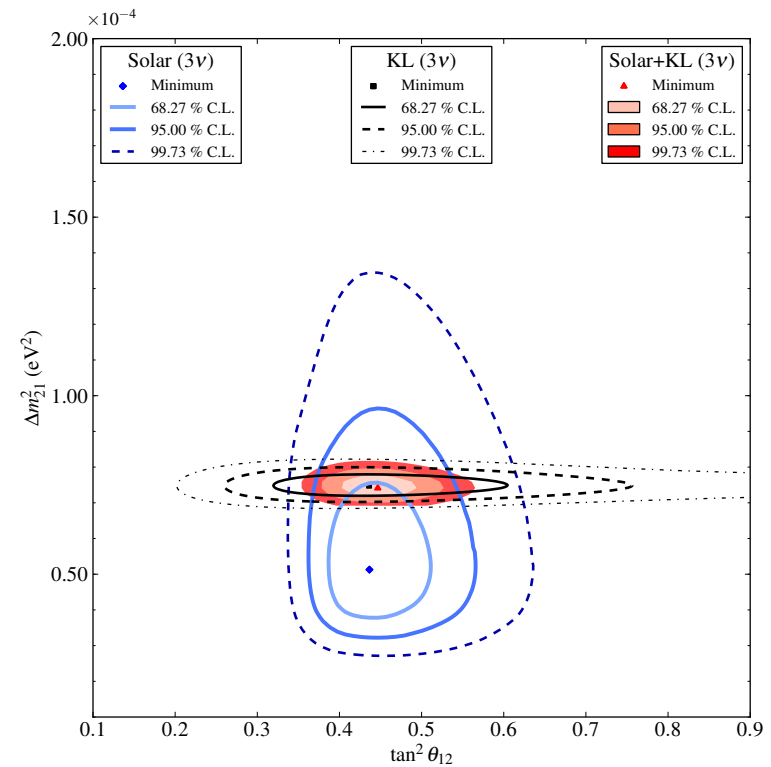
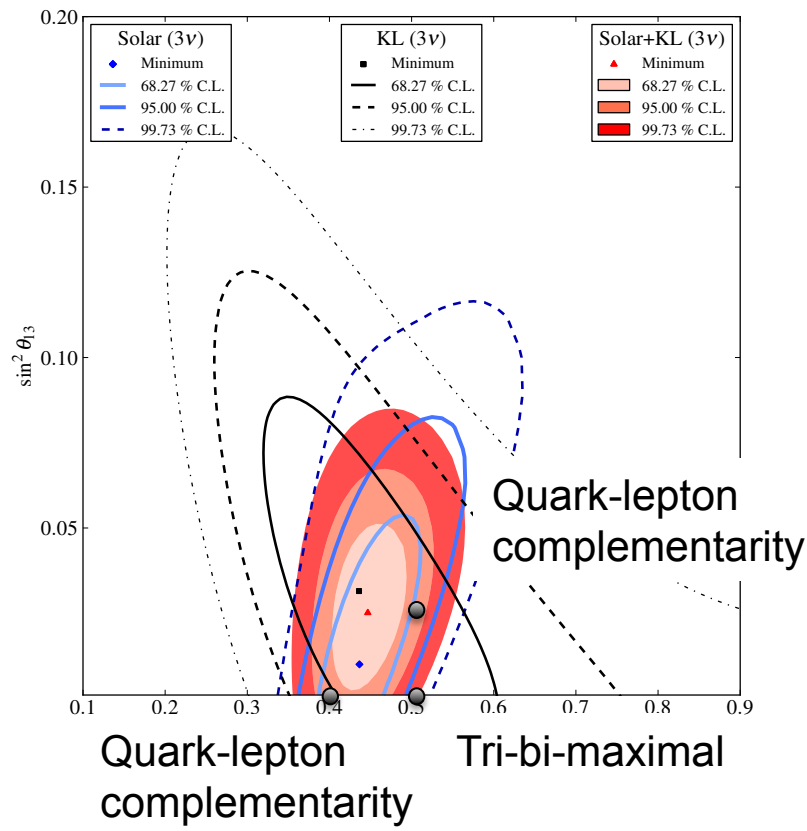
Oscillation Parameters



$$\tan^2 \theta_{12} = 0.446^{+0.030}_{-0.029} \quad \Delta m_{21}^2 = (7.41^{+0.21}_{-0.19}) \times 10^{-5} \text{ eV}^2 \quad \sin^2 \theta_{13} = 0.0251^{+0.0176}_{-0.0146}$$

$$< 0.0534 \text{ (95\%C.L.)}$$

Oscillation Parameters



Solar Neutrino Experiments ca. 2002

Solar Neutrino Experiments												
Expt.	Type	Fiducial	Mass	Threshold, keV			BP00 Rates per year				Event Eff. %	Start
		Tons	of	ES	CC	NC	pp + pep	⁷ Be	⁸ B	CNO		
<i>Cl-Ar</i>	Radioch.	135	³⁷ Cl		814		14	72	363	26	16	1968
<i>Kamioka</i>	Cerenkov	680	water	7000					120		100	1985
<i>SAGE</i>	Radioch.	23	⁷¹ Ga		233		181	86	31	22	25	1990
<i>Gallex</i>	Radioch.	12	⁷¹ Ga		233		94	45	16	11		1991
<i>SuperK</i>	Cerenkov	22000	water	5000					10200		100	1996
<i>GNO</i>	Radioch.	12	⁷¹ Ga		233		94	45	16	11		1998
<i>SNO</i>	Cerenkov	2000	water	5000					1100		100	1999
		200	² H		6400				10000		100	1999
		200	² H			2223			5000		50	1999
<i>KamLAND</i>	Scintillator	1000	scintillator									2001
<i>Borexino</i>	Scintillator	100	scintillator	250				20000				2002
<i>HERON</i>	L He rotons, Scintillator	5	He	100			3025	1500	2	125	80	
<i>TPC</i>	Gas TPC	7	He	180			4000					
<i>CLEAN</i>	Scintillator	12.5	Ne	100			9000					
<i>XMASS</i>	Scintillator		Xe									
<i>LENS</i>	Scintillator	5	¹⁷⁶ Yb		301,445		570	400	32	136		
<i>MOON</i>	Scintillator	3.3	¹⁰⁰ Mo		168		409	129	14	34	20	
<i>CI</i>	Hybrid	2200	³⁷ Cl		814		230	1200	5900	420	16	
<i>GaAs</i>	Ionization		⁷¹ Ga									
<i>LiF</i>	Bolometer	0.9	⁷ Li		862	487	27	29			100	