What can we learn about the "*K*NN" from the J-PARC E15 peak ?

- Relation between the Λp invariant mass spectrum and " $\overline{K}NN$ " -

Takayasu SEKIHARA *

(Research Center for Nuclear Physics, Osaka Univ.)

in collaboration with

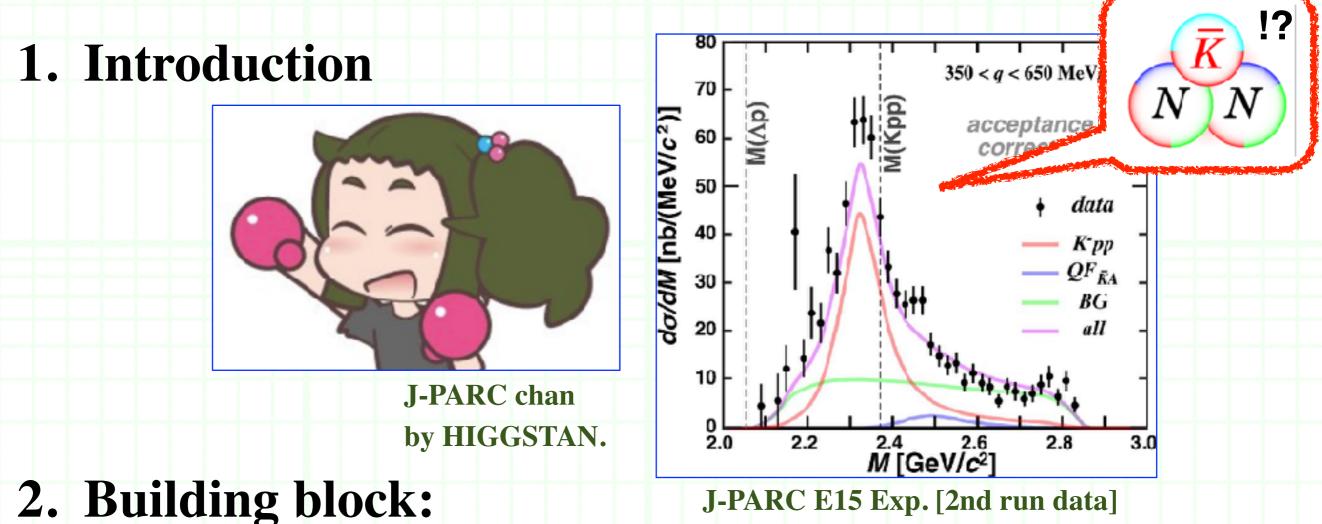
Eulogio OSET (Valencia Univ.)

and Angels RAMOS (Barcelona Univ.)

* Freelance science writer

- [1] T.S., E. Oset and A. Ramos, *PTEP* 2016 123D03.
- [2] <u>T. S.</u>, E. Oset and A. Ramos, *JPS Conf. Proc.* (2019), in press [arXiv:1903.10773].
- [3] T.S., E. Oset and A. Ramos, in preparation.

Contents



- The $\overline{K}N$ bound state / $\Lambda(1405)$
- **3.** Physics on the $\overline{K}NN$ bound state

4. Summary

++ Strangeness nuclear physics ++
 Strangeness nuclear physics / strange quark is interesting !
 In the transition region from chiral to heavy symmetry.
 --- Different viewpoint compared to usual nuclear physics (u & d).

- --- Dynamical part of constituent strange quark will still play an important role in the hadron spectroscopy. matter (fermions)
- It exists in "Nature".
 Possibly in neutron stars.
- Easier to produce in Exps.

 10^{2}

 10°

 10^{1}

AQCD $4\pi f_{\pi}$

 10^{3}



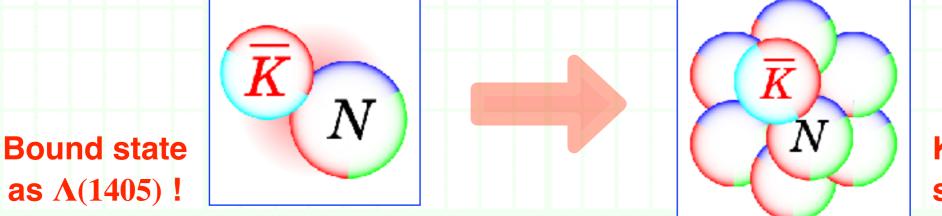
E [MeV]

 10^{4}

++ Kaonic nuclei ++

• Antikaon (\overline{K}) -nuclear systems are "attractive" !

- The $\overline{K}N$ interaction is strong enough to make a bound state as $\Lambda(1405)$.
- There should exist kaonic nuclei, which are bound states of <u>k</u> and nuclei via strong interaction between them.



Kaonic nuclei should exist !!

- There are several motivations to study kaonic nuclei themselves:
 - 1. Exotic states of many-body systems in strong interaction.
 - 2. Feedback to the *KN* interaction.
 - 3. <u>Kaons / strangeness in finite nuclear density</u>.

++ The "K-pp" state ++ The KNN (I=1/2) state --- so-called "K-pp" state ---- is the simplest state of the kaonic nuclei.

There have been many studies on this state.

<u>Theoretical studies</u>:

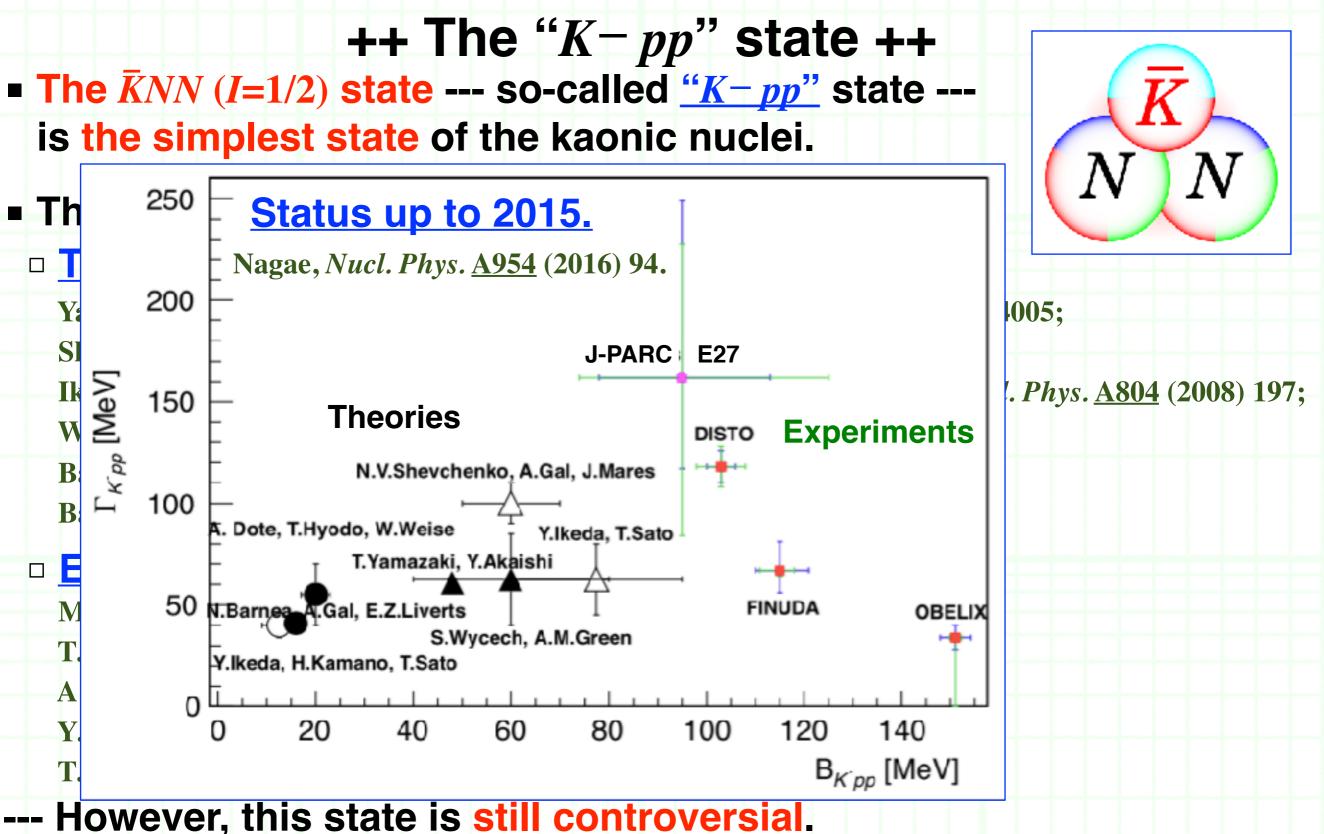
Yamazaki and Akaishi, *Phys. Lett.* <u>B535</u> (2002) 70; *Phys. Rev.* <u>C65</u> (2002) 044005; Shevchenko, Gal and Mares, *Phys. Rev. Lett.* <u>98</u> (2007) 082301; Ikeda and Sato, *Phys. Rev.* <u>C76</u> (2007) 035203; Dote, Hyodo and Weise, *Nucl. Phys.* <u>A804</u> (2008) 197; Wycech and Green, *Phys. Rev.* <u>C79</u> (2009) 014001; Bayar, Yamagata-Sekihara and Oset, *Phys. Rev.* <u>C84</u> (2011) 015209; Barnea, Gal and Liverts, *Phys. Lett.* <u>B712</u> (2012) 132; ...

Experimental studies:

M. Agnello et al. [FINUDA], Phys. Rev. Lett. 94 (2005) 212303;

- T. Yamazaki et al. [DISTO], Phys. Rev. Lett. 104 (2010) 132502;
- A. O. Tokiyasu et al. [LEPS], Phys. Lett. <u>B728</u> (2014) 616;
- Y. Ichikawa et al. [J-PARC E27], PTEP 2015 021D01; 061D01;
- T. Hashimoto et al. [J-PARC E15], PTEP 2015 061D01; ...

--- However, this state is still controversial.



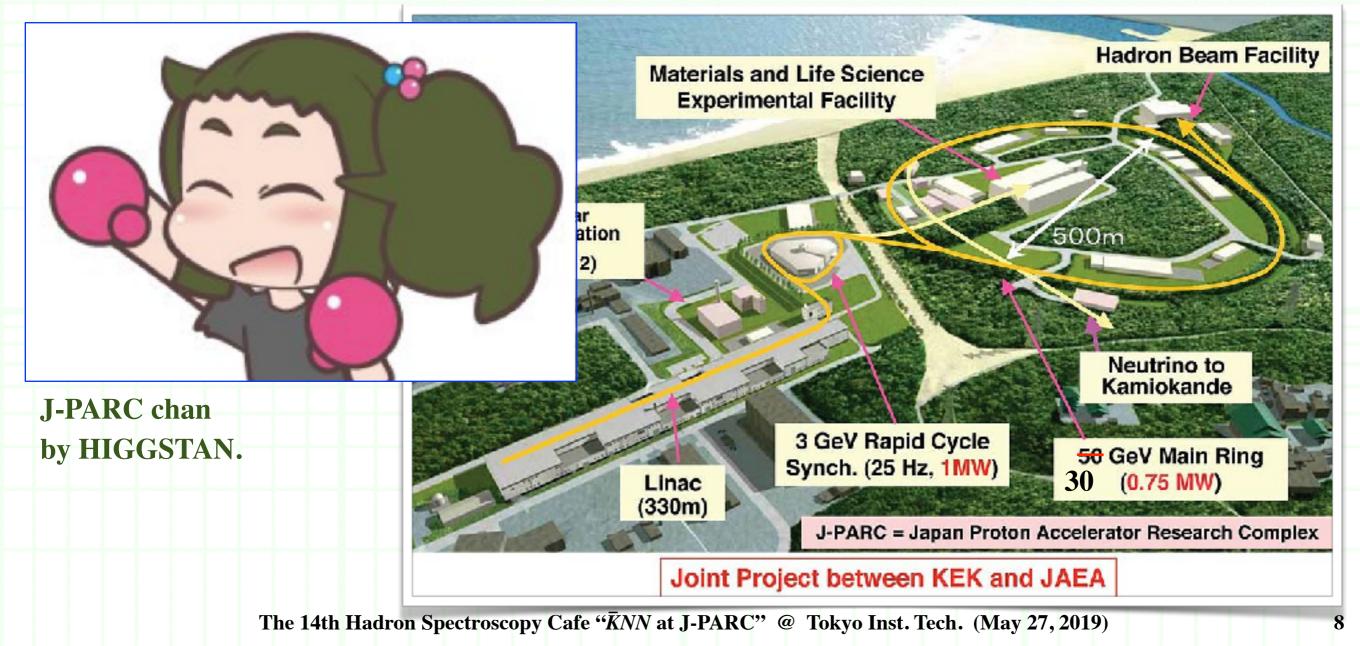
++ J-PARC ++

Recently, the J-PARC E15 Exp. was performed to search for

the $\overline{K}NN$ bond state with the in-flight $K - {}^{3}He -> \Lambda p n$ reaction.

Y. Sada et al., PTEP 2016 051D01; Ajimura et al., Phys. Lett. B789 (2019) 620.

J-PARC --- Japan Proton Accelerator Research Complex.



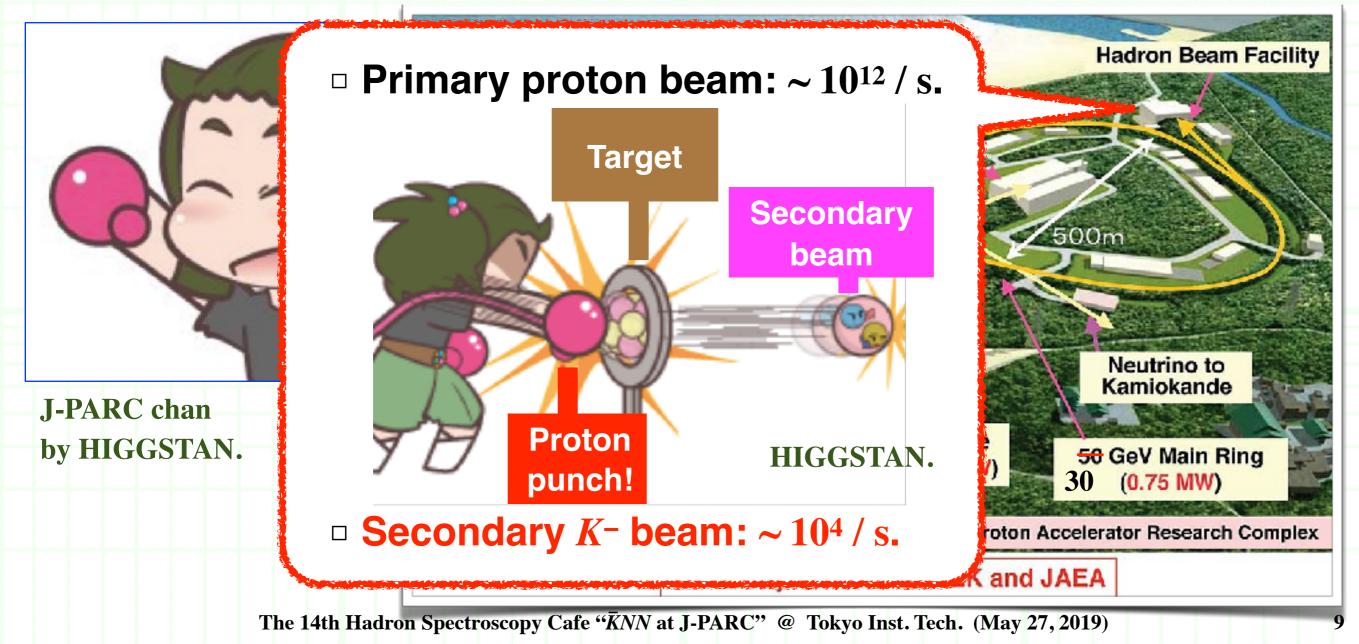
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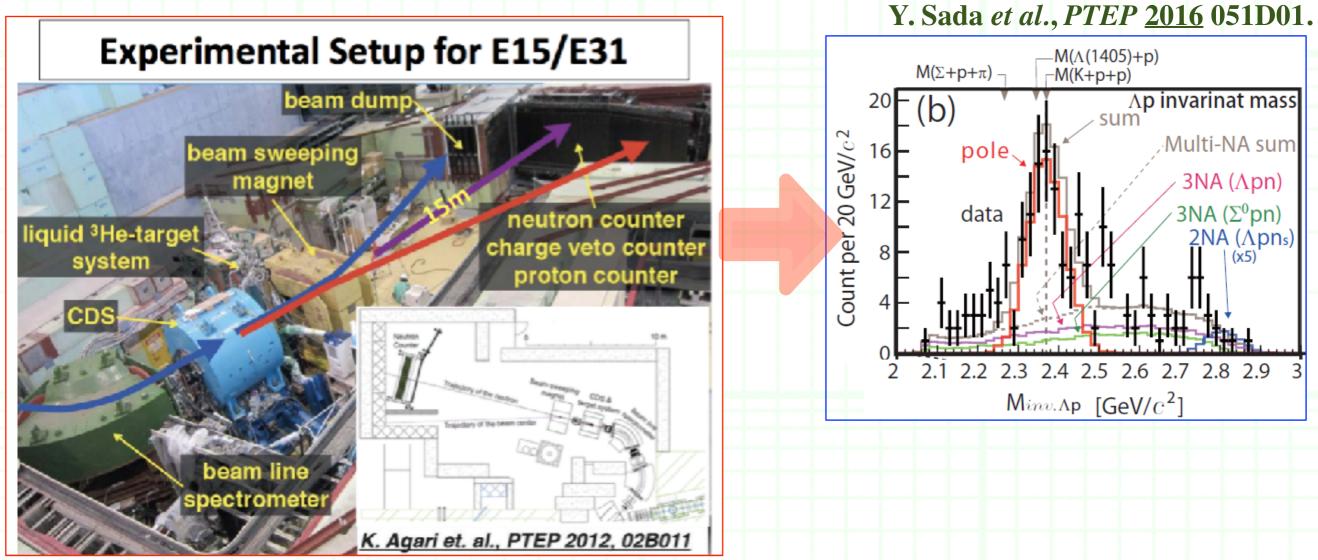
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Y. Sada et al., PTEP 2016 051D01; Ajimura et al., Phys. Lett. B789 (2019) 620.

J-PARC ---- Japan Proton Accelerator Research Complex.



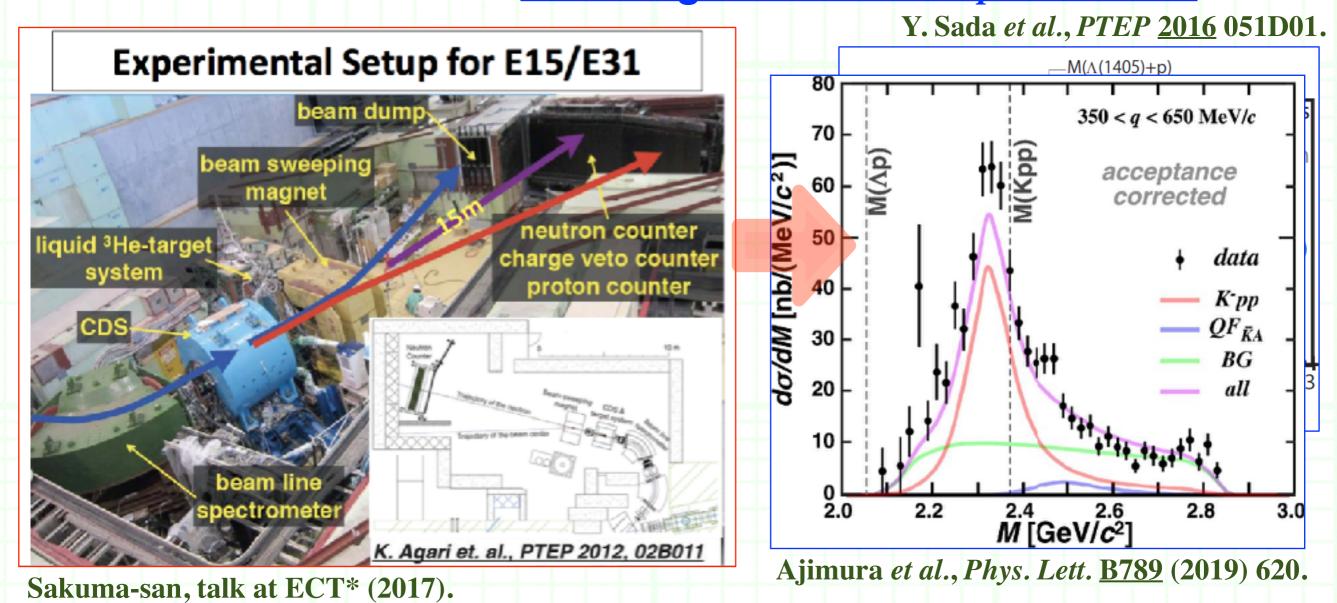
++ J-PARC E15 ++ ■ Recently, the J-PARC E15 Exp. was performed to search for the *K̄NN* bond state with the in-flight *K*- ³He -> Λ p n reaction.



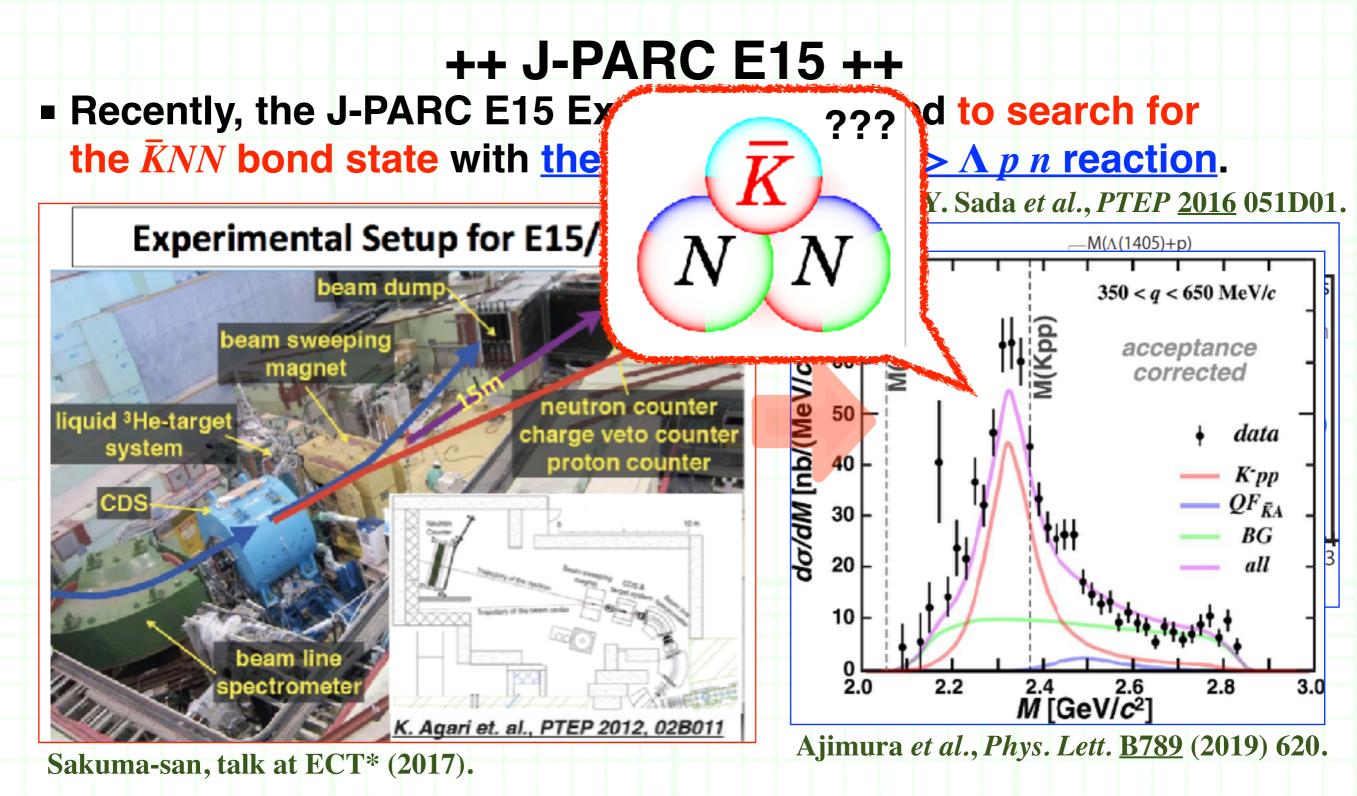
Sakuma-san, talk at ECT* (2017).

Big advantage: we can directly put kaon into the nucleus.

++ J-PARC E15 ++ Recently, the J-PARC E15 Exp. was performed to search for the *KNN* bond state with the in-flight *K*− ³He → Λ *p n* reaction.



Big advantage: we can directly put kaon into the nucleus.



Big advantage: we can directly put kaon into the nucleus.

++ Questions about *KNN* ++

From the J-PARC E15 data, what can we learn about the KNN ?

- □ **Does the** *K̄NN* **bound state really exist ?**
- Spin / parity ?
- Relation between the Exp. peak and the resonance pole ?
- Description Pole position ?

Box does the \overline{K} -nucleus interaction realize ?

 The same questions can arise for the *k̄*N bound state.
 We discuss how the same questions have been attacked in the *k̄*N bound-state case (as a building block of the *k̄*NN), and then extend it to the *k̄*NN bound-state case.

2. Building block: The *KN* bound state / Λ(1405)

++ About the $\overline{K}N$ bound state ++

	$\Lambda(1405)$ as $\overline{K}N$ bound state
Prediction	
Discovery	
Spin / parity	
Interaction	
Component	
Peak position	
Pole position	

++ Prediction ++

• [Theory] A resonance state [= $\Lambda(1405)$] was predicted in 1959.

Dalitz and Tuan, Phys. Rev. Lett. <u>2</u> (1959) 425; Ann. Phys. <u>10</u> (1960) 307.

• Spin / parity $\underline{J^p} = 1/2^-$, isospin $\underline{I} = 0$, strangeness $\underline{S} = -1$, below the \overline{KN} threshold and decays into the $\pi\Sigma$ channel.

 \square Based on <u>analysis of the Exp. data of the \overline{KN} scattering length</u>.

POSSIBLE RESONANT STATE IN PION-HYPERON SCATTERING*

R. H. Dalitz and S. F. Tuan

Enrico Fermi Institute for Nuclear Studies and Department of Physics, University of Chicago, Chicago, Illinois (Received April 27, 1959)

ANNALS OF PHYSICS: 3, 307-351 (1960)

With charge independence, describe the *s*-wave scatteri energy K^- -proton collisions tering lengths A_0 and A_1 , one and I=1 channels, related to shifts δ_I by

 $k \cot \delta_I = 1/A_I (i)$

where k denotes the center-c of the $K^- - p$ system. Since t is expected to have short ran

The Phenomenological Representation of K-Nucleon Scattering and Reaction Amplitudes^{*†}

R. H. DALITZ AND S. F. TUAN

Enrico Fermi Institute for Nuclear Studies and the Department of Physics, University of Chicago, Chicago, Illinois

The 14th

++ Discovery of $\Lambda(1405)$ ++

• [Exp.] The $\Lambda(1405)$ resonance was discovered in 1961.

Alston et al., Phys. Rev. Lett. <u>6</u> (1961) 698.

• Then, what is the structure of $\Lambda(1405)$?

Λ(1405) can be <u>naturally explained as a *KN* bound state</u>. But how can we "proof" that ? <-- Long-standing problem !

VOLUME 6, NUMBER 12

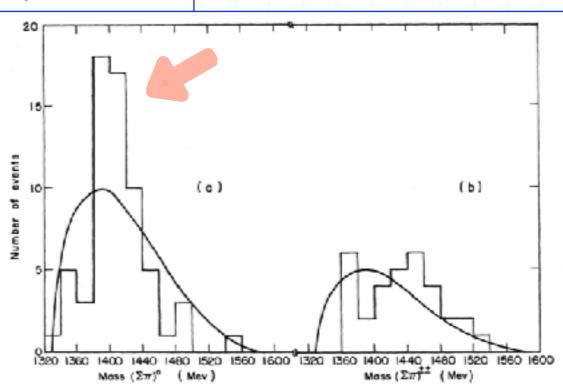
PHYSICAL REVIEW LETTERS

JUNE 15, 1961

STUDY OF RESONANCES OF THE $\Sigma -\pi$ SYSTEM^{*}

Margaret H. Alston, Luis W. Alvarez, Philippe Eberhard,[†] Myron L. Good,[‡] William Graziano, Harold K. Ticho,^{||} and Stanley G. Wojcicki Lawrence Radiation Laboratory and Department of Physics, University of California, Berke (Received May 8, 1961; revised manuscript received May 31, 1961)

Recently a T = 1 resonance in the $\Lambda - \pi$ system, called Y_1^* , has been observed with a mass of 1385 Mev.¹⁻⁶ Two types of resonances have been predicted that might relate this observation to other elementary-particle interactions: (1) $P_{3/2}$ resonances in the $\Lambda - \pi$ and $\Sigma - \pi$ systems predicted by global symmetry,^{7,8} corresponding to the $(\frac{3}{2}, \frac{3}{2})$ resonance of the π -N system, (2) a spin- $\frac{1}{2}Y - \pi$ resonance resulting from a bound state in the of $(\Sigma - \pi)^+$ and $(\Sigma - \pi)^-$ there appea of events in the region of M=138the number of $(\Lambda - \pi^+)$ and $(\Lambda - \pi^-)$ Mev $< M_{\Lambda - \pi} < 1415$ Mev from ref suming that all charged $\Sigma - \pi$ sys mass regions of Fig. 1 are Y_1^* , < 8%. This treatment yields an limit, since there is no evidence above background. The $\Sigma^{\pm} + \pi^{\mp}$

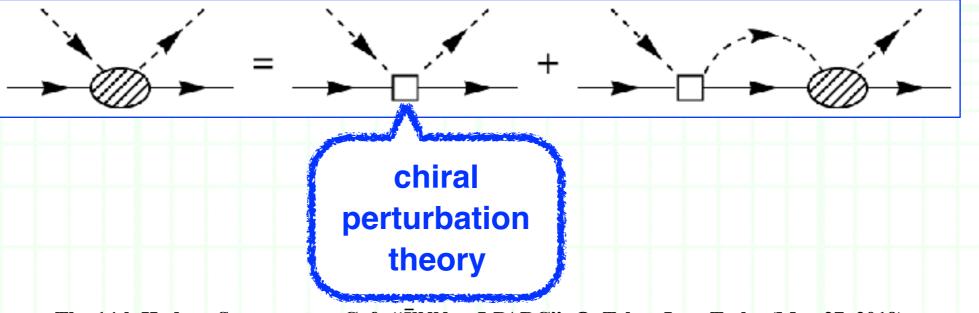


++ $\Lambda(1405)$ in chiral dynamics ++

• [Theory] $\Lambda(1405)$ is well described in chiral dynamics.

Kaiser, Siegel and Weise (1995); Oset and Ramos (1998); ...

- □ \overline{K} is a <u>Nambu-Goldstone boson</u> of spontaneous chiral symmetry breaking in QCD. $SU(3)_L \otimes SU(3)_R \rightarrow SU(3)_{\text{flavor}}$
- $\Box \overline{K}$ is massive by strange quark: $m_K \sim 495$ MeV.
- --> Interaction from chiral perturbation theory & its unitarization can dynamically generate $\Lambda(1405)$ in \overline{KN} coupled channels.
- ---- Chiral dynamics !



++ $\Lambda(1405)$ in chiral dynamics ++

• [Theory] $\Lambda(1405)$ is well described in chiral dynamics.

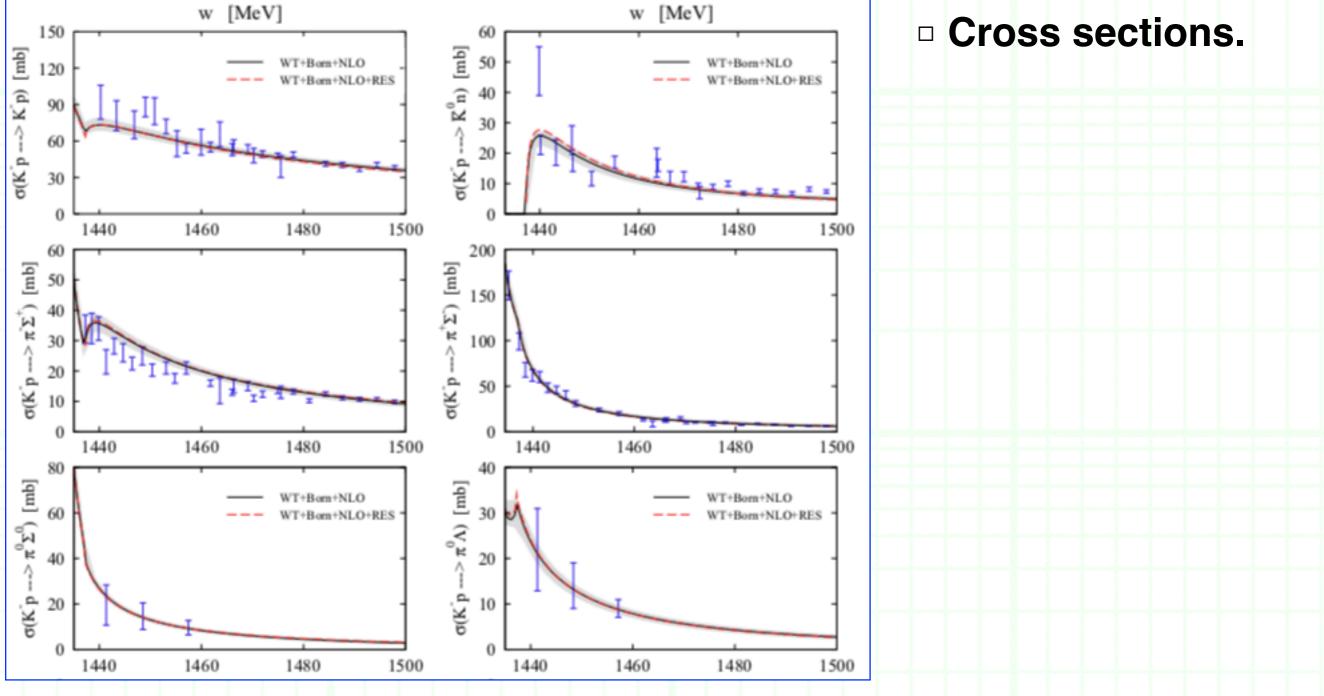
□ Observables at the K-p threshold.

	γ	R_n	R_c	$a_p(K^-p \to K^-p)$	ΔE_{1s}	Γ_{1s}
Ikeda-Hyodo-Weise (NLO) [23]	2.37	0.19	0.66	-0.70 + i0.89	306	591
Guo-Oller (fit I + II) [25]	$2.36^{+0.24}_{-0.23}$	$0.188^{+0.028}_{-0.029}$	$0.661^{+0.012}_{-0.011}$	$(-0.69 \pm 0.16) + i(0.94 \pm 0.11)$	308 ± 56	619 ± 73
Mizutani et al. (model s) [26]	2.40	0.189	0.645	-0.69 + i0.89	304	591
Mai-Meissner (fit 4) [29]	$2.38^{+0.09}_{-0.10}$	$0.191^{+0.013}_{-0.017}$	$0.667^{+0.006}_{-0.005}$		288^{+34}_{-32}	572^{+39}_{-38}
Cieply-Smejkal (NLO) [75]	2.37	0.191	0.660	-0.73 + i0.85	310	607
Shevchenko (two-pole model) [76]	2.36			-0.74 + i0.90	308	602
WT+Born+NLO	$2.36^{+0.03}_{-0.03}$	$0.188^{+0.010}_{-0.011}$	$0.659^{+0.005}_{-0.002}$	$-0.65^{+0.02}_{-0.08} + i0.88^{+0.02}_{-0.05}$	288^{+23}_{-8}	588^{+9}_{-40}
WT+NLO+Born+RES	2.36	0.189	0.661	-0.64 + i0.87	283	587
Expt.	2.36 ± 0.04	0.189 ± 0.015	0.664 ± 0.011	$(-0.66\pm 0.07)+i(0.81\pm 0.15)$	283 ± 36	541 ± 92

Feijoo, Magas and Ramos, Phys. Rev. C99 (2019) 035211.

++ $\Lambda(1405)$ in chiral dynamics ++

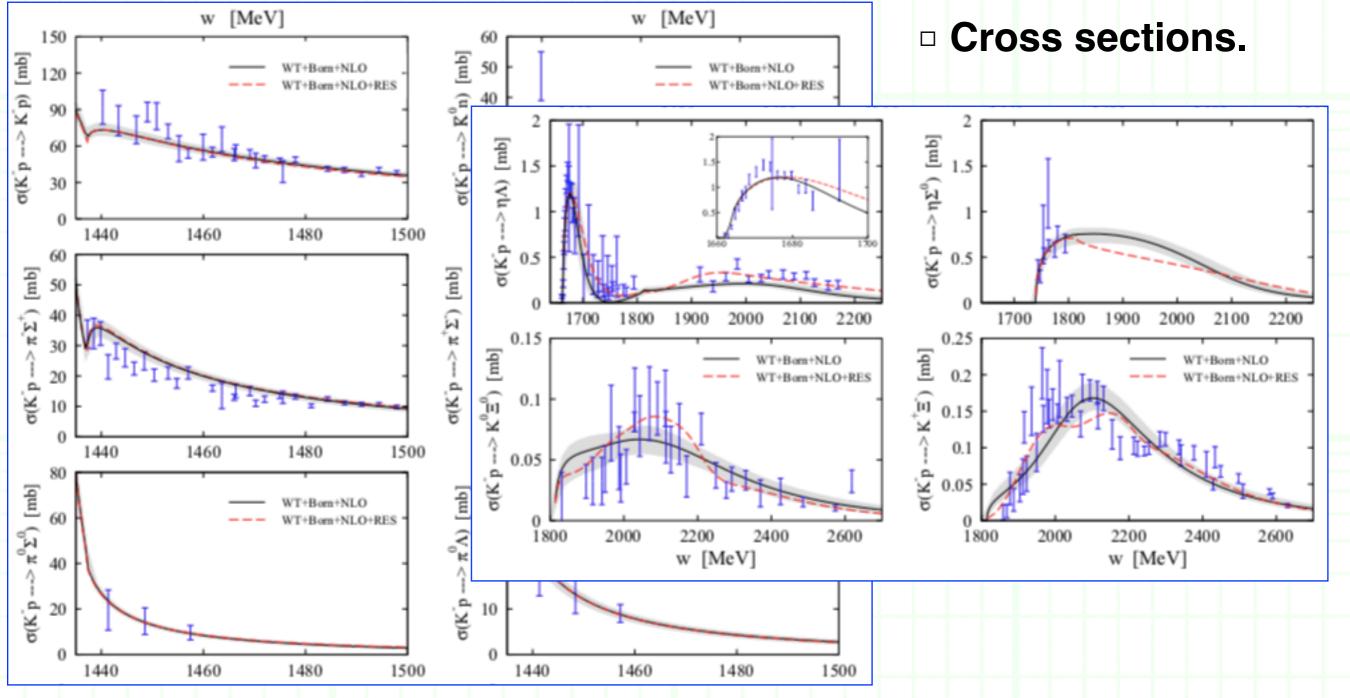
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Feijoo, Magas and Ramos, *Phys. Rev.* <u>C99</u> (2019) 035211.

++ $\Lambda(1405)$ in chiral dynamics ++

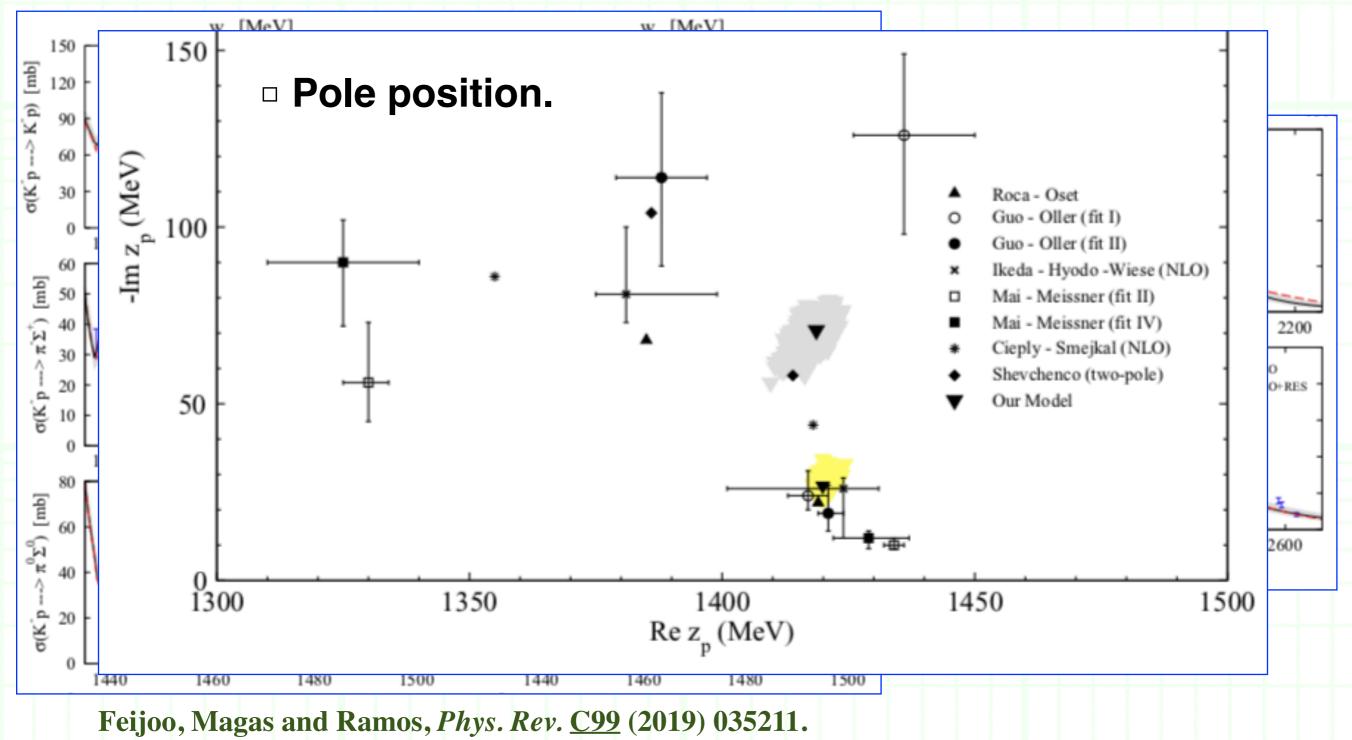
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Feijoo, Magas and Ramos, *Phys. Rev.* <u>C99</u> (2019) 035211.

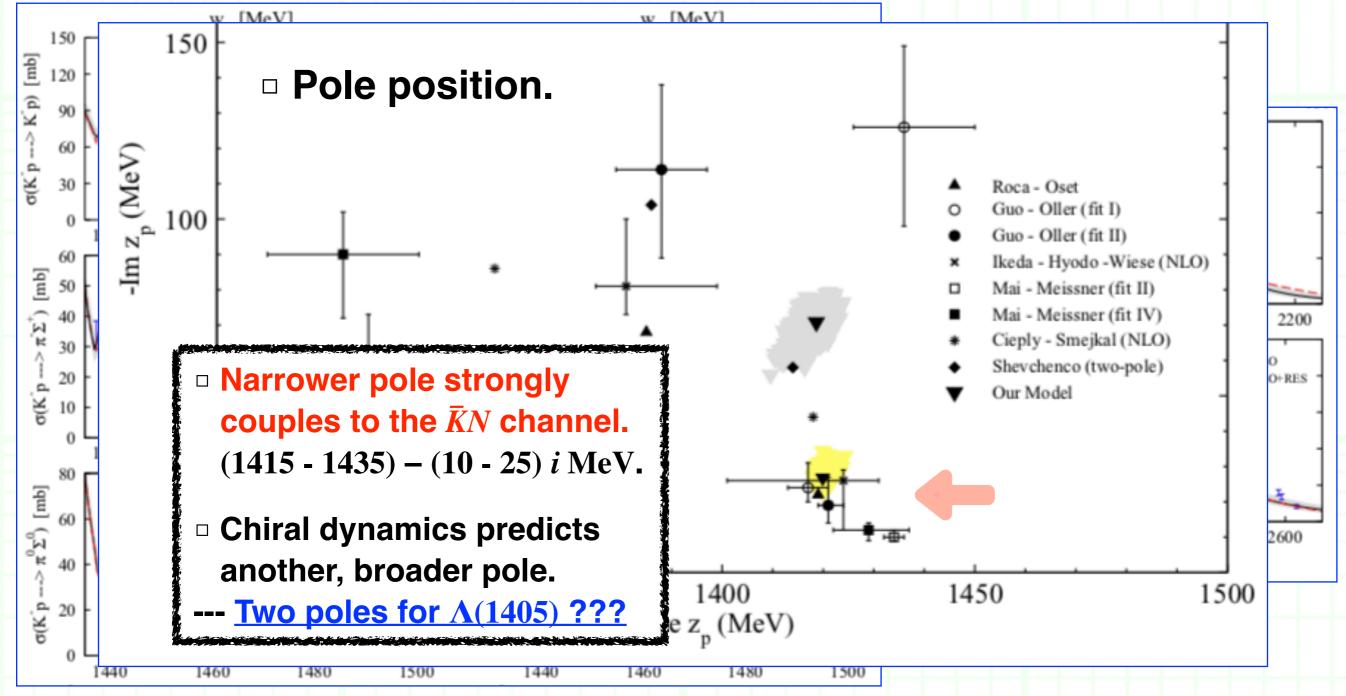
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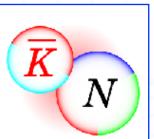


Feijoo, Magas and Ramos, *Phys. Rev.* <u>C99</u> (2019) 035211.

++ Structure of $\Lambda(1405)$ ++

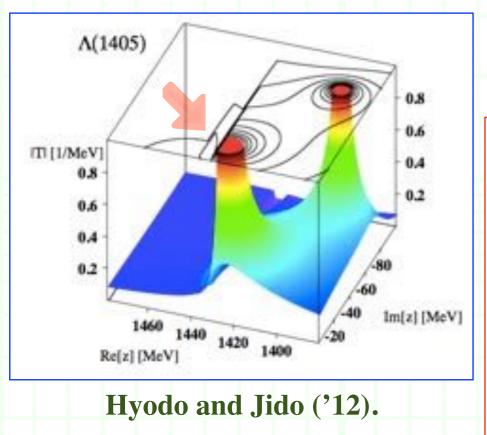
• [Theory] What is the structure of $\Lambda(1405)$?

--> To check how much Λ(1405) contains the *k̄*N component, the compositeness was calculated in chiral dynamics.
 □ Compositeness = Norm of the two-body wave function for each resonance pole.



How much ?

Uniquely determined once model space and parameters are fixed.



<u>T.S.</u>, Hyodo and Jido, *PTEP* <u>2015</u>, 063D04.

	$\Lambda(1405)$, higher pole	$\Lambda(1405)$, lower pole
$\sqrt{s_{ m pole}}$	$1424 - 26i { m ~MeV}$	1381 - 81i MeV
$\dot{X}_{\bar{K}N}$	1.14 + 0.01i	-0.39 - 0.07i
$X_{\pi\Sigma}$	-0.19 - 0.22i	0.66 + 0.52i
$X_{\eta\Lambda}$	0.13 + 0.02i	-0.04 + 0.01i
$X_{K\Xi}$	0.00 + 0.00i	-0.00 + 0.00i
Z	-0.08 + 0.19i	0.77 - 0.46i

++ Structure of $\Lambda(1405)$ ++

• [Theory] What is the structure of $\Lambda(1405)$?

- --> To check how much Λ(1405) contains the <u>*K*</u>N component, the compositeness was calculated in chiral dynamics.
 - One may evaluate the compositeness only from "observables" in model independent manner --- Pole position and Scatt. length.

$$a_0 = R\left\{\frac{2X}{1+X} + O\left(\left|\frac{R_{\text{typ}}}{R}\right|\right) + \sqrt{\frac{{\mu'}^3}{\mu^3}}O\left(\left|\frac{l}{R}\right|^3\right)\right\}, \quad R = \frac{1}{\sqrt{2\mu E_{QB}}}.$$

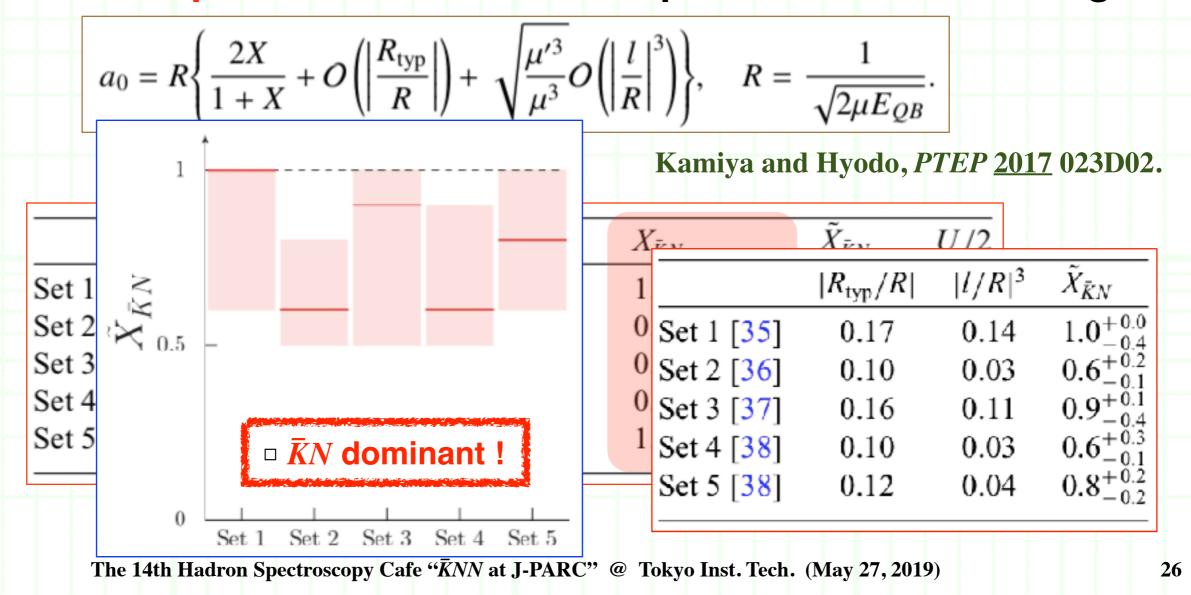
Kamiya and Hyodo, PTEP 2017 023D02.

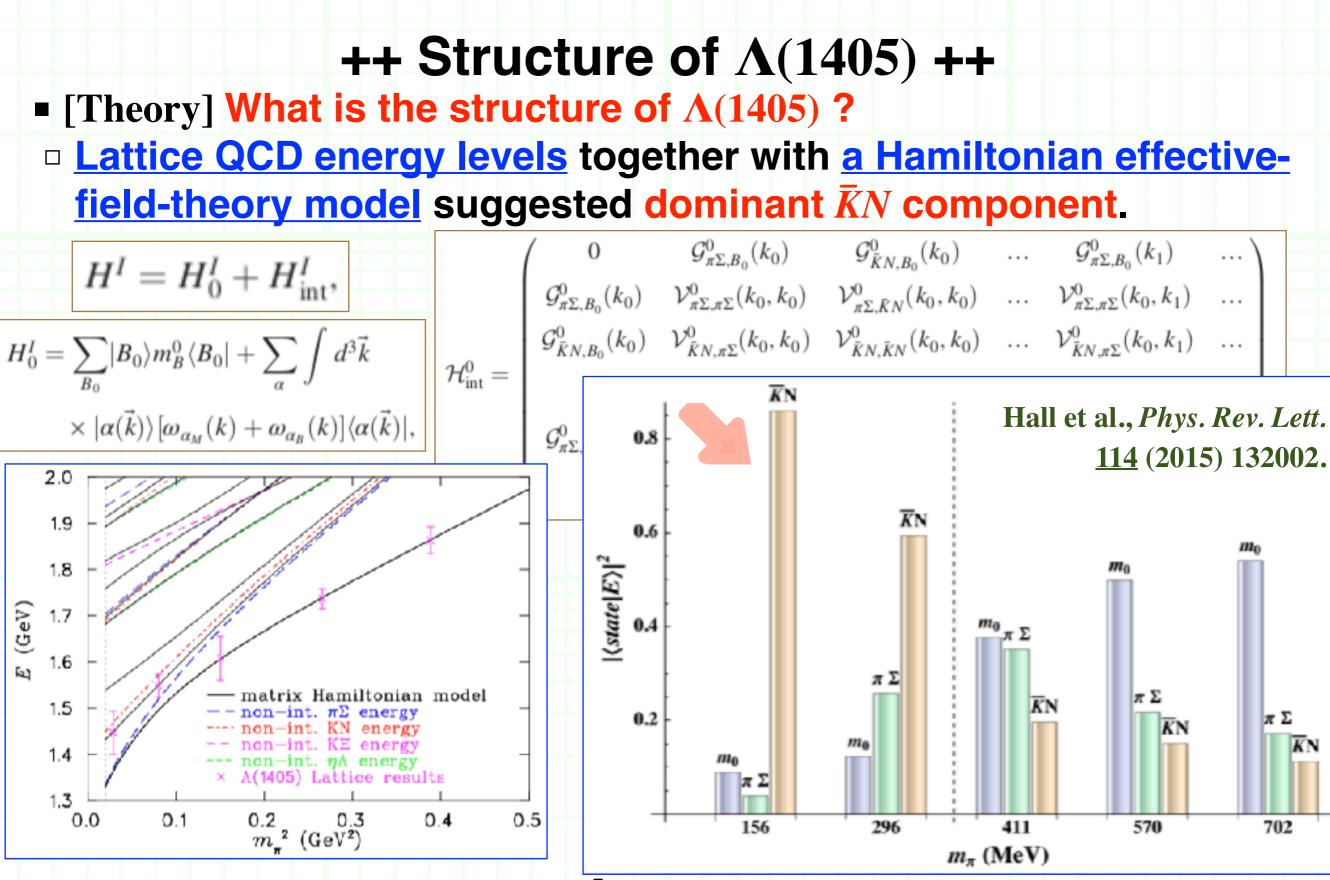
5,552		E_h [MeV]	a_0 [fm]	$X_{ar{K}N}$	$\tilde{X}_{\bar{K}N}$	U/2
	Set 1 [35]	-10 - i26	1.39 - i0.85	1.2 + i0.1	1.0	0.3
	Set 2 [36]	-4-i8	1.81 - i0.92	0.6 + i0.1	0.6	0.0
	Set 3 [37]	-13 - i20	1.30 - i0.85	0.9 - i0.2	0.9	0.1
	Set 4 [38]	2 - i10	1.21 - i1.47	0.6 + i0.0	0.6	0.0
	Set 5 [38]	-3-i12	1.52 - i1.85	1.0 + i0.5	0.8	0.3

++ Structure of $\Lambda(1405)$ ++

• [Theory] What is the structure of $\Lambda(1405)$?

- --> To check how much $\Lambda(1405)$ contains the \overline{KN} component, the compositeness was calculated in chiral dynamics.
 - One may evaluate the compositeness only from "observables" in model independent manner --- Pole position and Scatt. length.



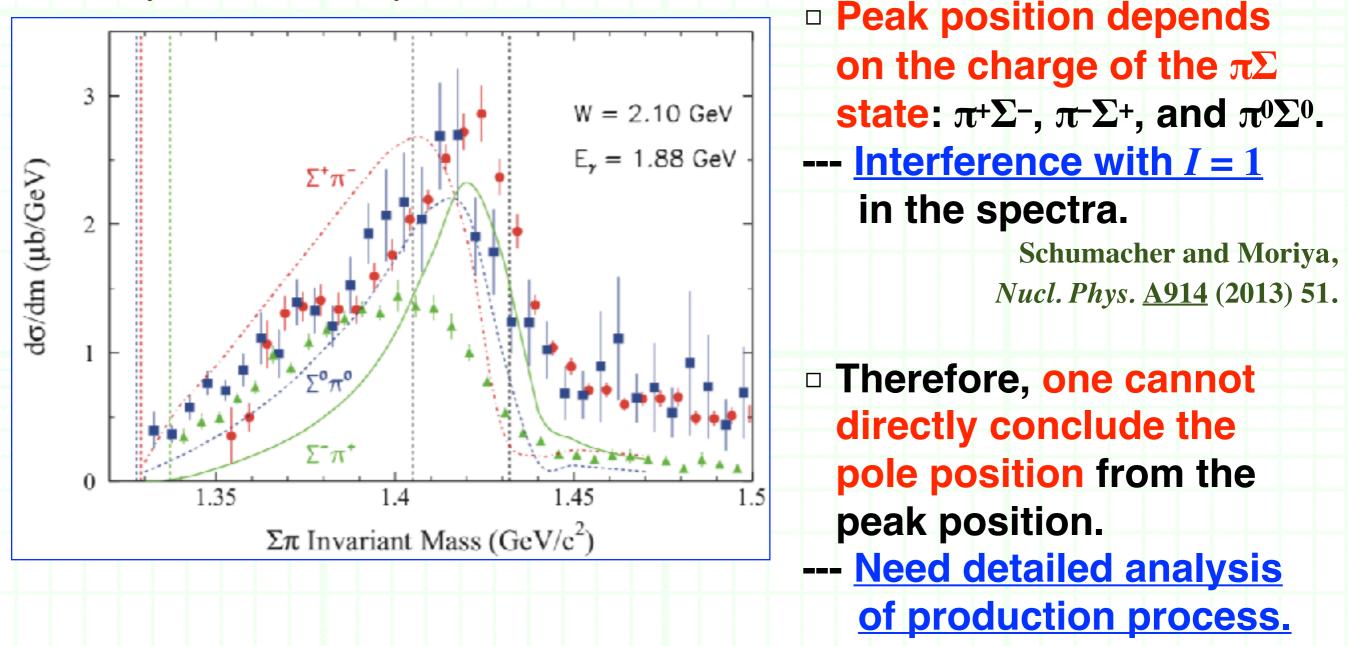


++ Observed peak(s) of $\Lambda(1405)$ ++

• [Exp.] How $\Lambda(1405)$ emerges in spectra ?

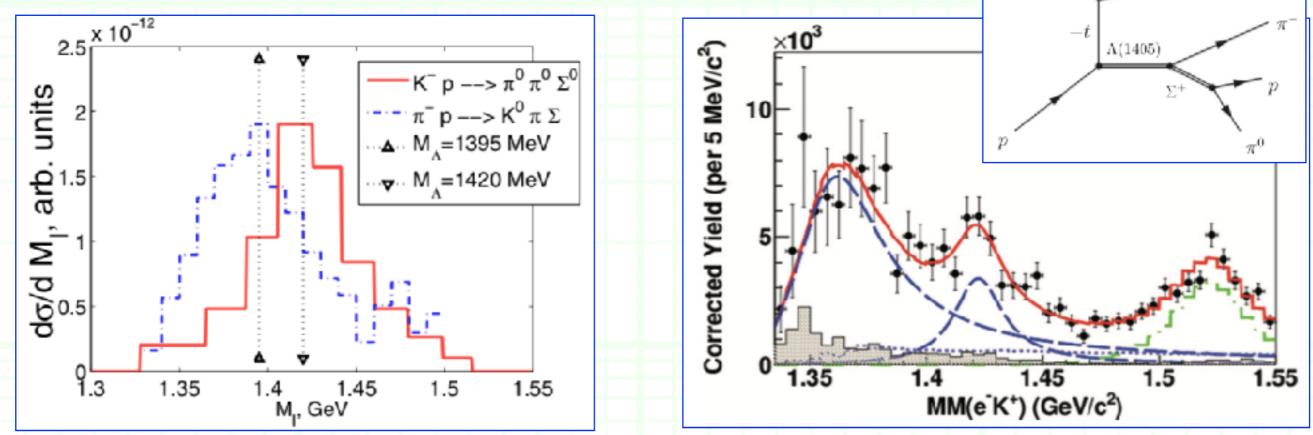
 $\Box \gamma p \longrightarrow K^+ (\pi \Sigma)^0 \text{ reaction.}$

Moriya et al. [CLAS], Phys. Rev. <u>C87</u> (2013) 035206.



++ Observed peak(s) of $\Lambda(1405)$ ++

[Exp.] How Λ(1405) emerges in spectra ?
 In addition, some reactions generate Λ(1405) with much lower peak position.



Magas, Oset and Ramos, *Phys. Rev. Lett.* <u>95</u> (2005) 052301; Prakhov *et al.* [Crystall Ball], *Phys. Rev.* <u>C70</u> (2004) 034605; Thomas *et al.*, *Nucl. Phys.* <u>B56</u> (1973) 15. $\Box e p \rightarrow e K^+ \pi^- \Sigma^+.$

Lu et al. [CLAS],

Phys. Rev. C88 (2013) 045202.

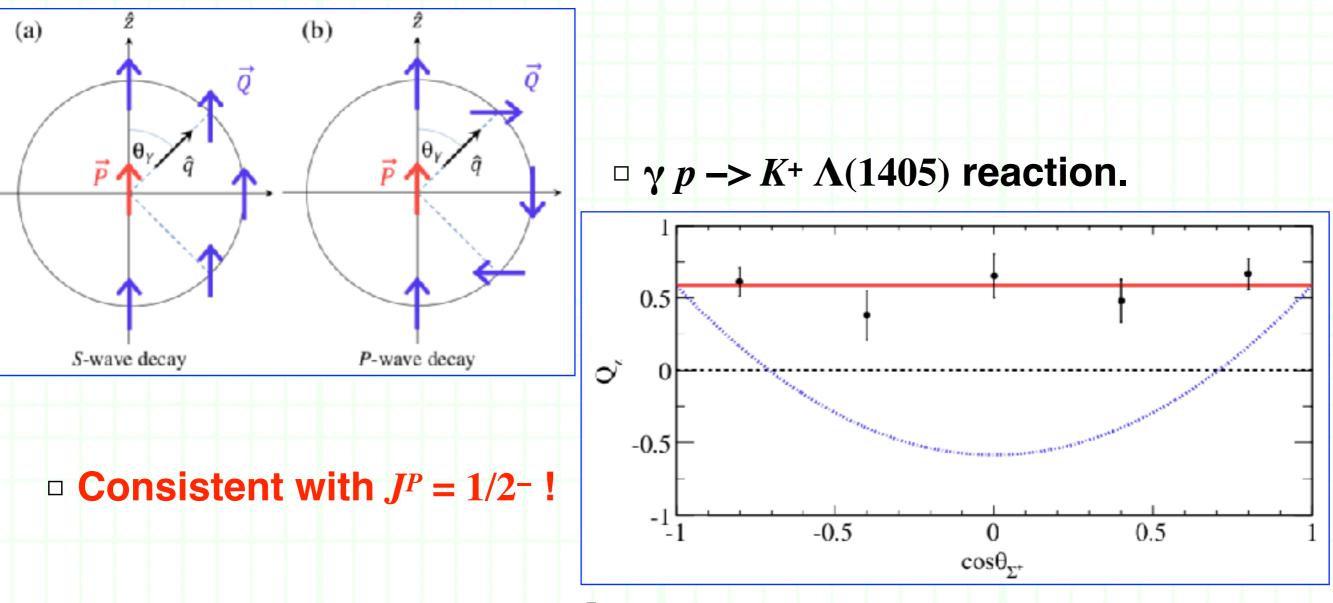
--- Effect of the two-pole nature for the $\Lambda(1405)$???

++ Spin / parity of $\Lambda(1405)$ ++

• [Exp.] What is the spin / parity of $\Lambda(1405)$?

Moriya et al. [CLAS], Phys. Rev. Lett. <u>112</u> (2014) 082004.

• Complete Exp. confirmation of the spin & parity of $\Lambda(1405)$ was done very recently.



++ Summary of the $\overline{K}N$ bound state ++

	$\Lambda(1405)$ as $\overline{K}N$ bound state
Prediction	1959
Discovery	1961
Spin / parity	1/2- (2014)
Interaction	Chiral dynamics
Component	$\overline{K}N$ dominant in chiral D (2015 ~)
Peak position	Depends on reaction
Pole position	(1415 - 1435) – (10 - 25) <i>i</i> MeV*
	* Assuming chiral dynamics.

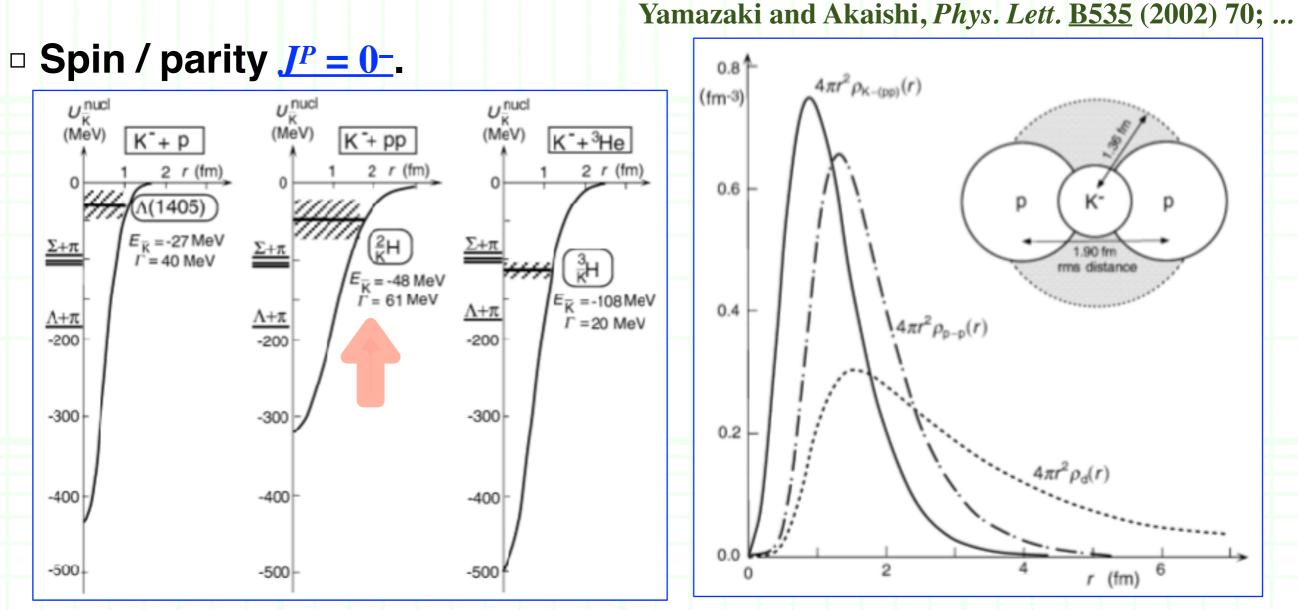
3. Physics on the KNN bound state

++ Extension to the $\overline{K}NN$ bound state ++

	$\Lambda(1405)$ as $\overline{K}N$ bound state	<i><u>KNN</u></i> bound state	
Prediction	1959		
Discovery	1961		
Spin / parity	1/2- (2014)		
Interaction	Chiral dynamics		
Component <i>K̄N</i> dominant in chiral D			
Peak position	Peak position Depends on reaction		
Pole position	Pole position (1415 - 1435) – (10 - 25) <i>i</i> MeV*		
* Assuming chiral dynamics.			

++ Prediction ++

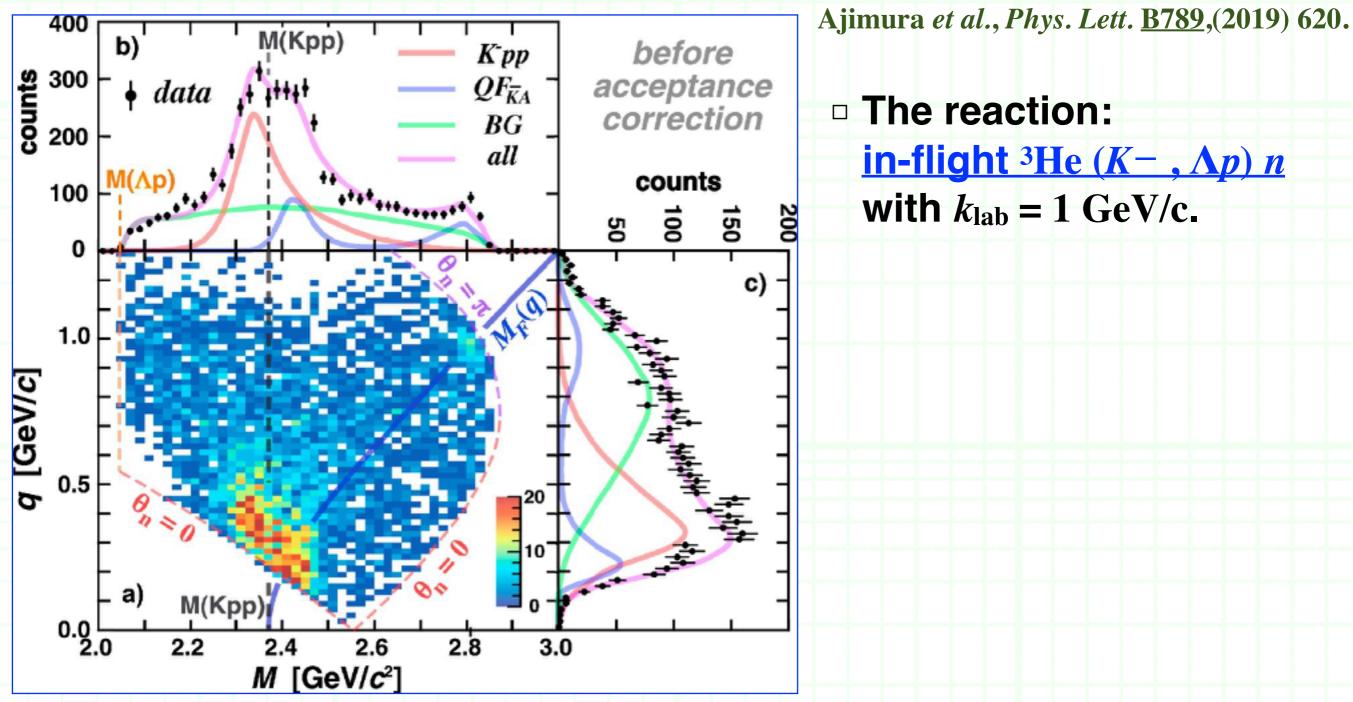
• [Theory] The *K*NN bound state was predicted in 2002.



• Sophisticated models followed, and it was found that \overline{KNN} system is bound as long as the \overline{KN} lnt. is strongly attractive.

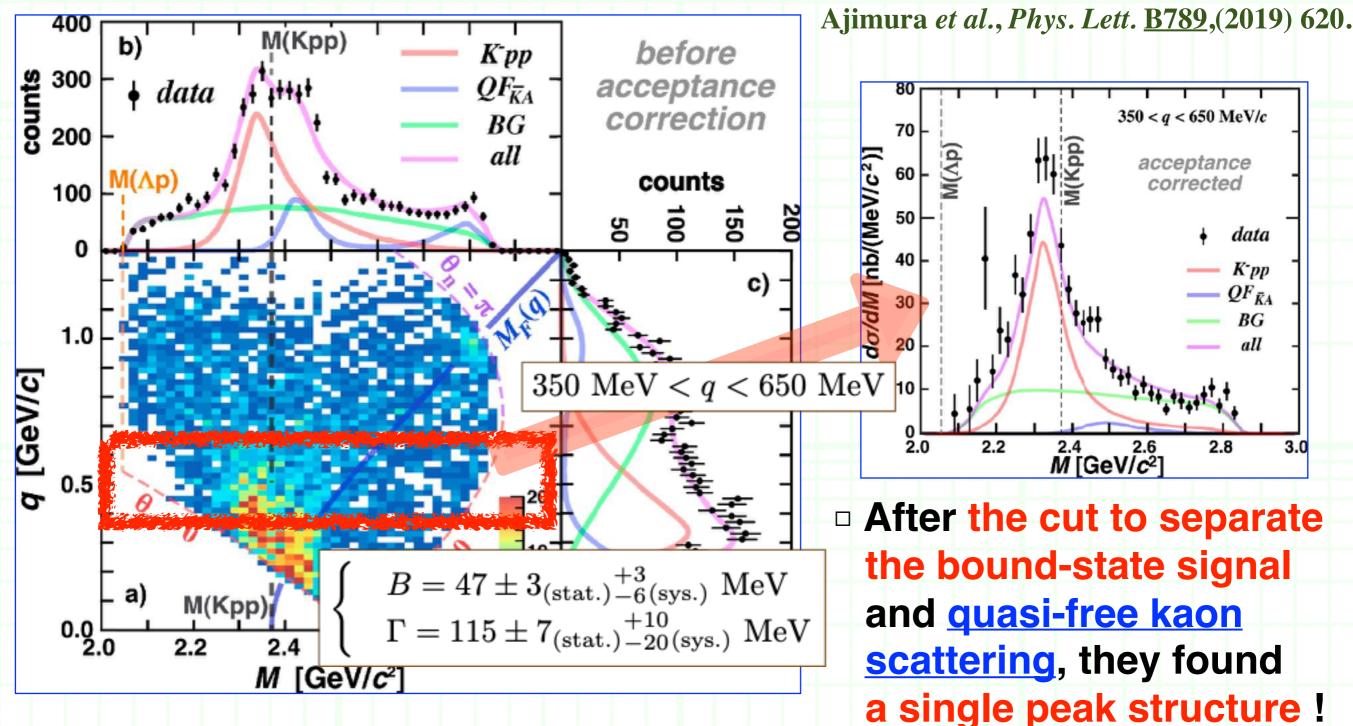
++ Discovery ??? ++

[Exp.] Beautiful data from the J-PARC E15 Exp. !



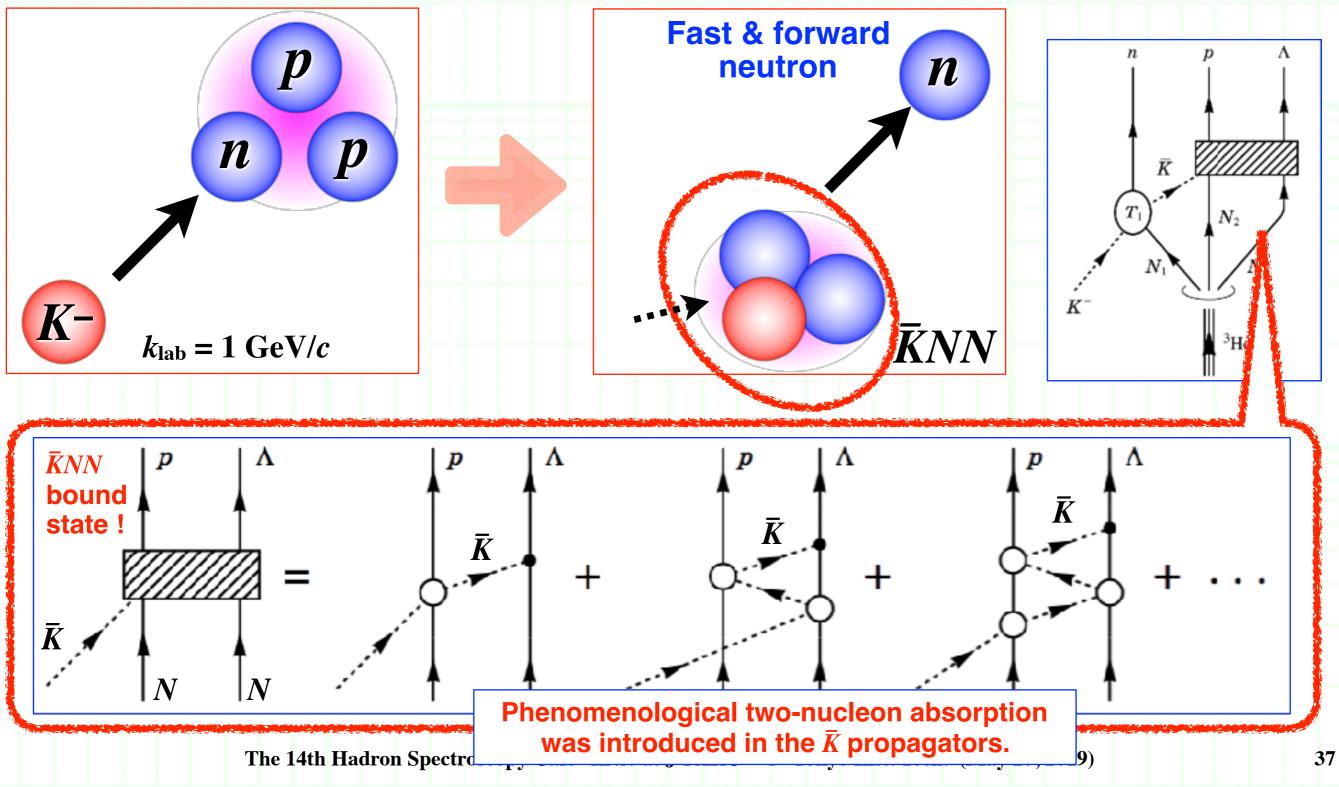
++ Discovery ??? ++

[Exp.] Beautiful data from the J-PARC E15 Exp. !



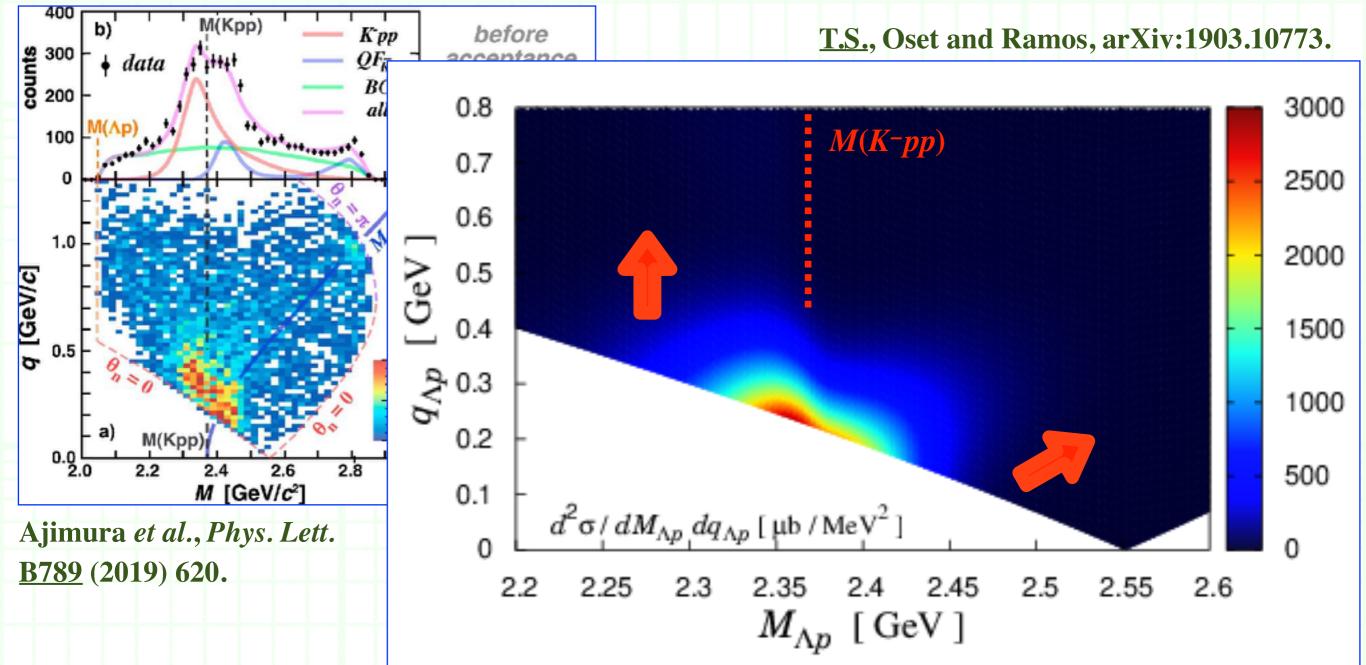
++ Discovery ??? ++

• [Theory.] <u>Calculate the spectrum</u> in the <u>*KNN*</u> bound state scenario.

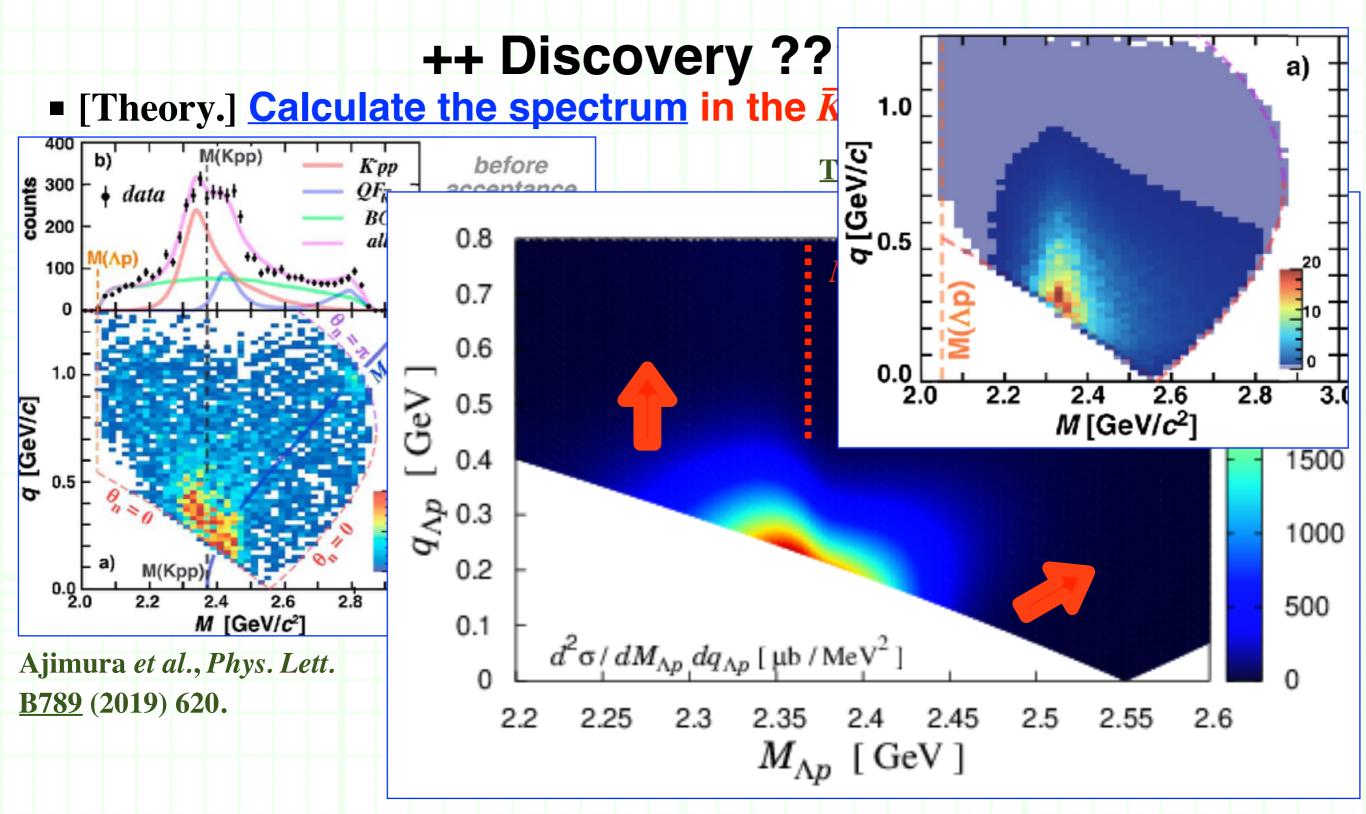


++ Discovery ??? ++

[Theory.] Calculate the spectrum in the KNN bound state scenario.



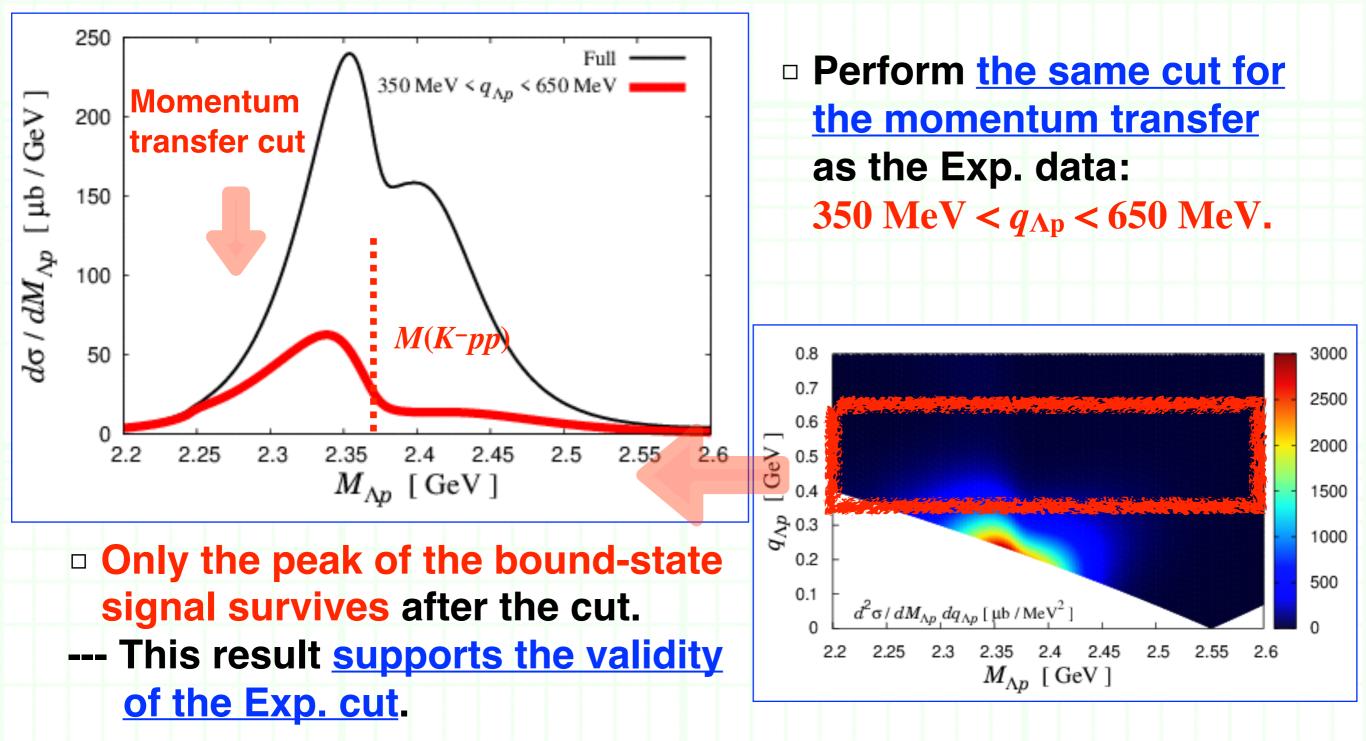
The same behavior for the differential cross section.



The same behavior for the differential cross section.

++ Discovery ??? ++

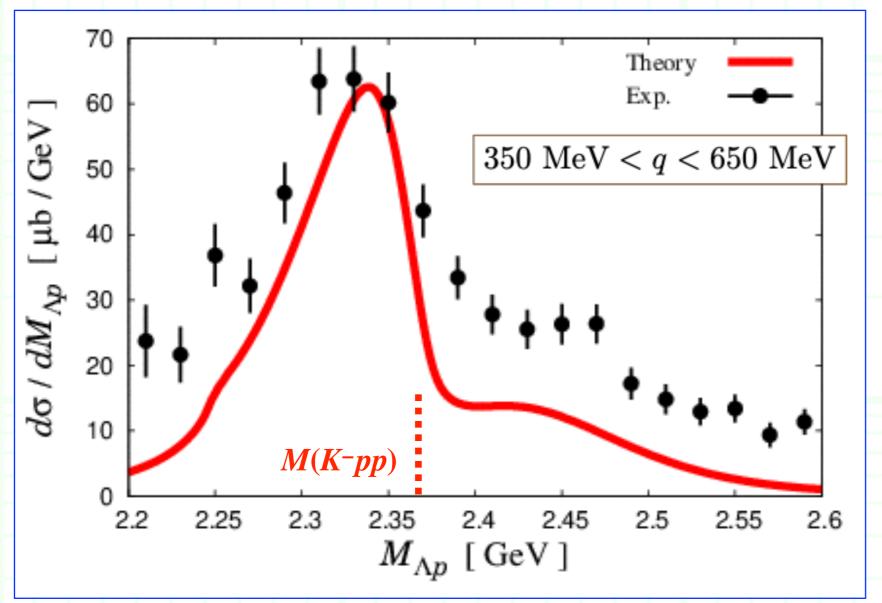
• [Theory.] <u>Calculate the spectrum</u> in the <u>*KNN*</u> bound state scenario.



++ Discovery ??? ++

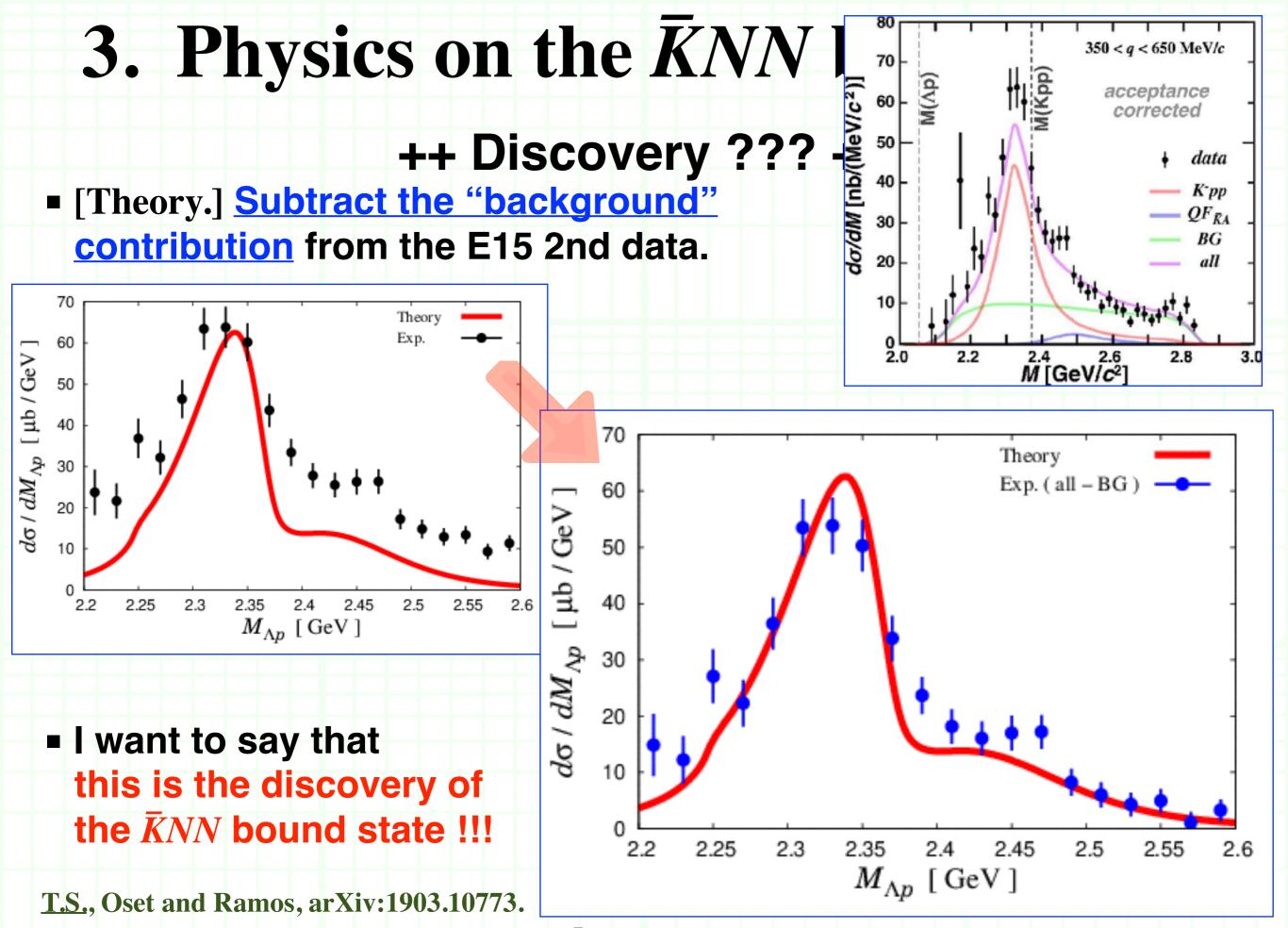
• [Theory.] <u>Calculate the spectrum</u> in the <u>*KNN*</u> bound state scenario.

T.S., Oset and Ramos, arXiv:1903.10773.



 With the cut 350 MeV < *q*_{Ap} < 650 MeV, *peak structures are similar to each other.*
 This supports the production of the *KNN* bound state.

Note: Exp. data contain background. <-- Absent in our model.</p>

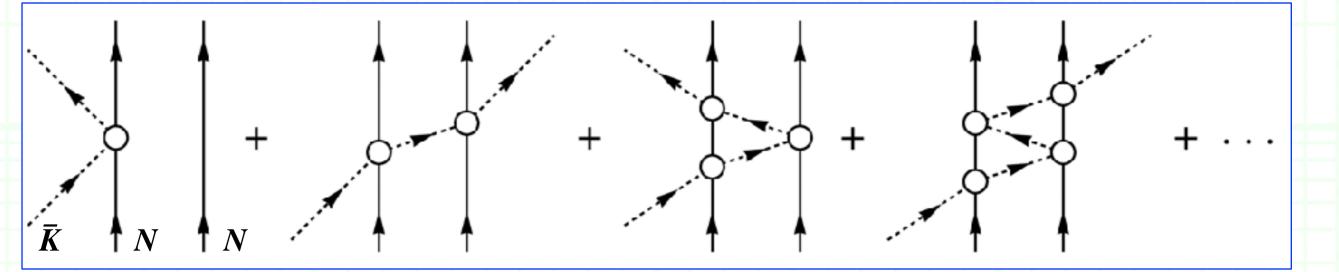


++ Interactions in the $\overline{K}NN$ bound state ++

• [Theory] The attraction to form the $\overline{K}NN$ bound state comes

from the two-body KN and NN interactions.
 Usually, theoretical calculations are done with the two-body KN and NN interactions.

□ In terms of the fixed-center approximation to the Faddeev Eq., the $\overline{K}NN$ three-body calculation JAEA press release. with the two-body $\overline{K}N$ Int. can be done:

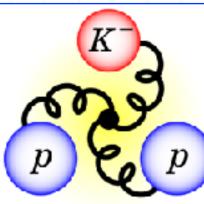


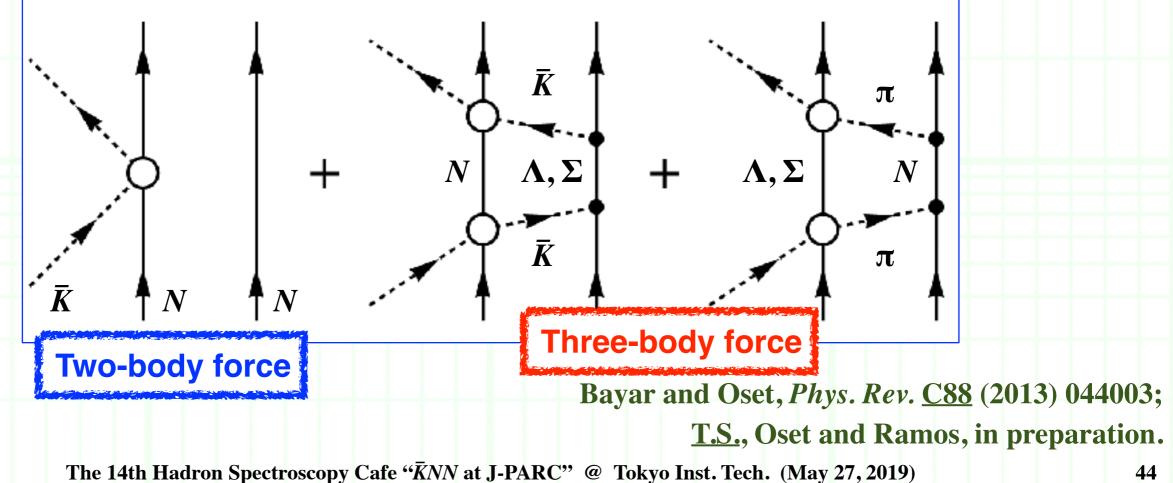
Bayar, Yamagata-Sekihara and Oset, *Phys. Rev.* <u>C84</u> (2011) 015209; <u>T.S.</u>, Oset and Ramos, *PTEP* <u>2016</u> 123D03.

--- NN interaction has been taken into account to form "NN center".

++ Interactions in the $\overline{K}NN$ bound state ++

- [Theory] However, there should exist KNN three-body force !
 - \Box The $\bar{K}NN$ three-body interaction reflects <u>non-conservation of</u> the meson number.
 - --- New type of three-body force.
 - \Box The $\overline{K}NN$ three-body interaction in this way is added to the two-body *KN* interaction as:



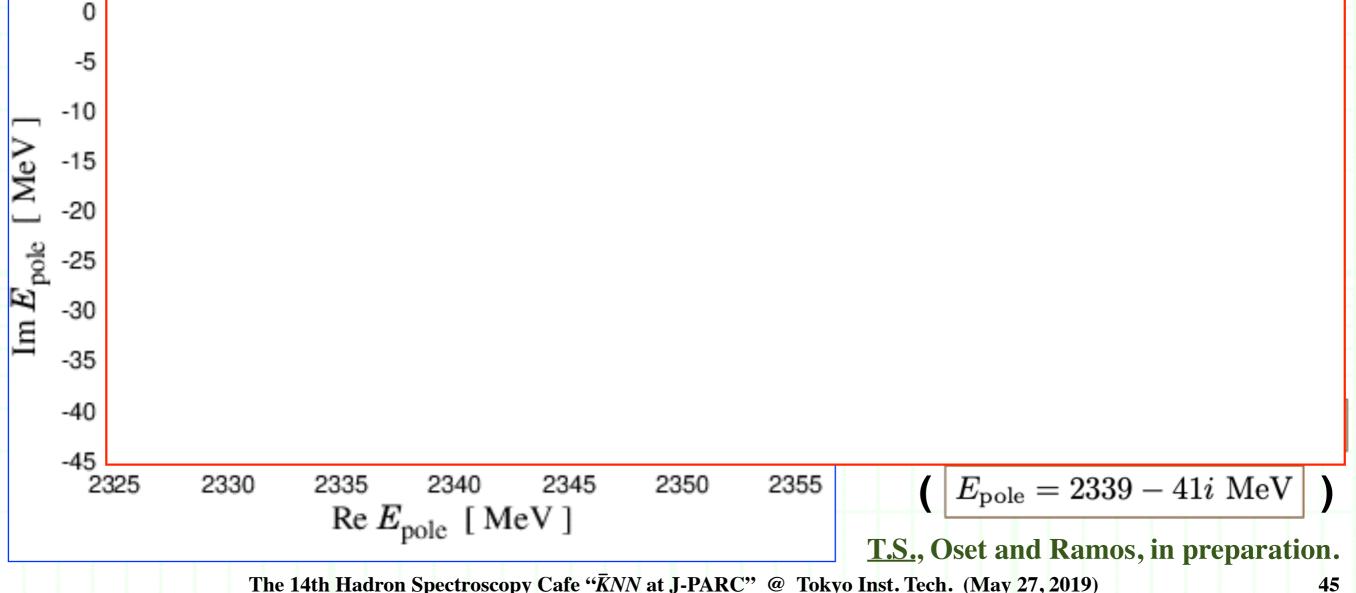


++ Interactions in the KNN bound state ++

[Theory] Only two-body force vs. including three-body force.

- \square Pole position of the $\overline{K}NN$ bound state in the fixed-center Approx.
- --- Parameter in the fixed-center approximation

d: <u>distance between *NN* as a "center"</u>.

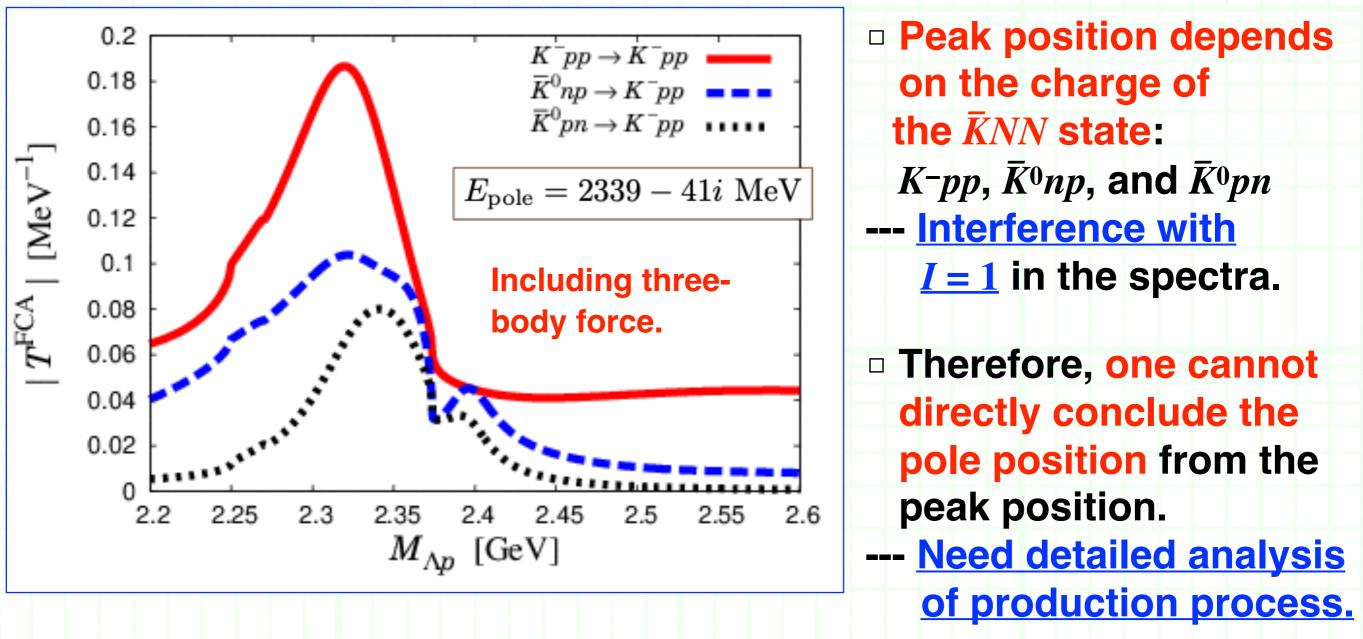


++ Observed peak(s) ++

[Theory / Exp.] How the *KNN* bound state emerges in spectra ?
 KNN -> KNN amplitude in the particle basis.

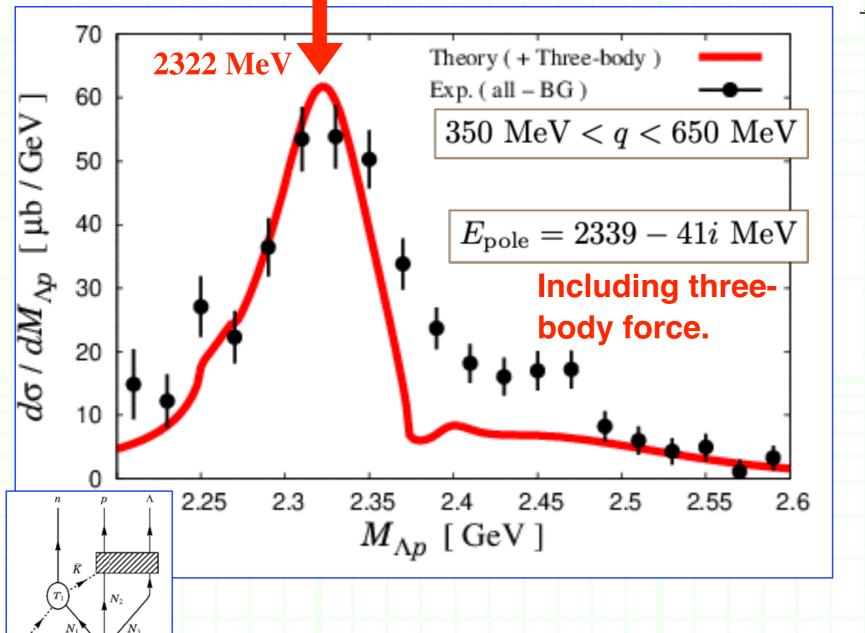
--- K-pp, $\overline{K}^0 np$, and $\overline{K}^0 pn \rightarrow \overline{K}NN$.

<u>T.S.</u>, Oset and Ramos, in preparation.



++ Observed peak(s) ++

• [Theory / Exp.] How the \overline{KNN} bound state emerges in spectra ? • Calculate the Λp invariant mass spectrum of K^{-3} He -> $\Lambda p n$.



T.S., Oset and Ramos, in preparation.

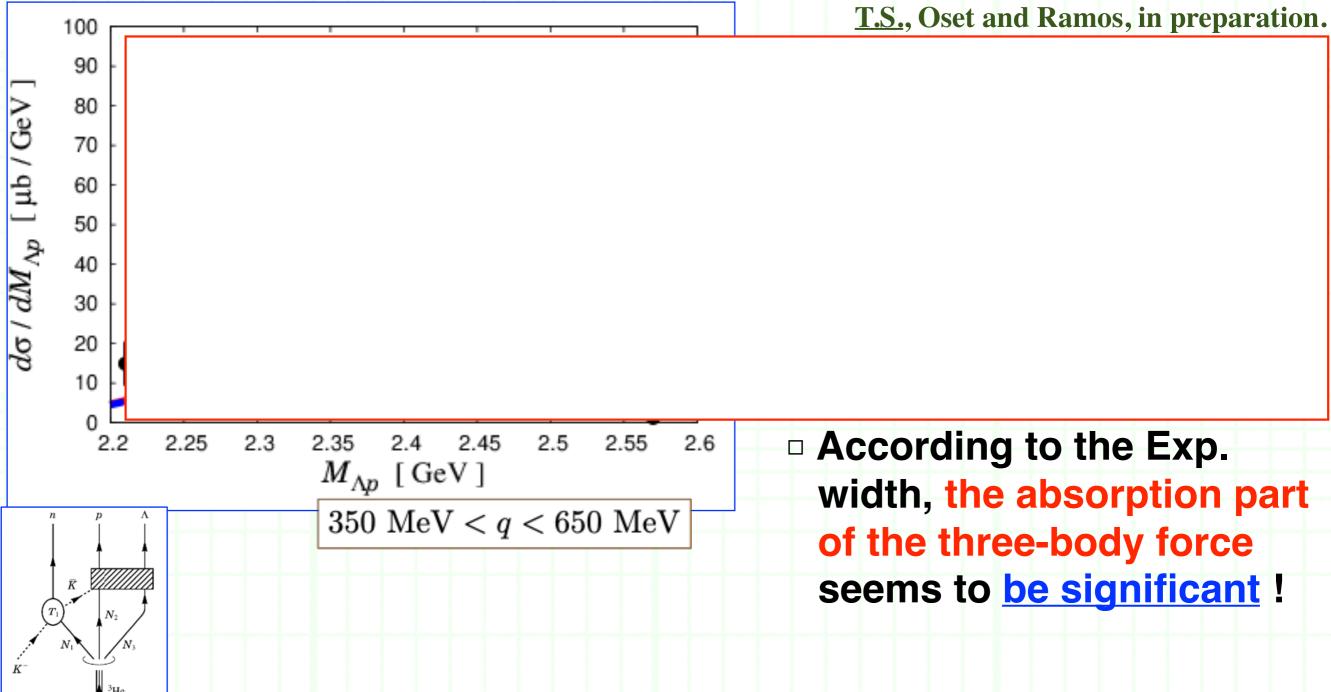
 Clearly, we see that the peak position 2322 MeV < Re(E_{pole}).
 --- About -17 MeV shift.

 Therefore, the Breit-Wigner parameters do not coincide with the pole position.

++ Observed peak(s) ++

• [Theory / Exp.] How the *K̄NN* bound state emerges in spectra ?

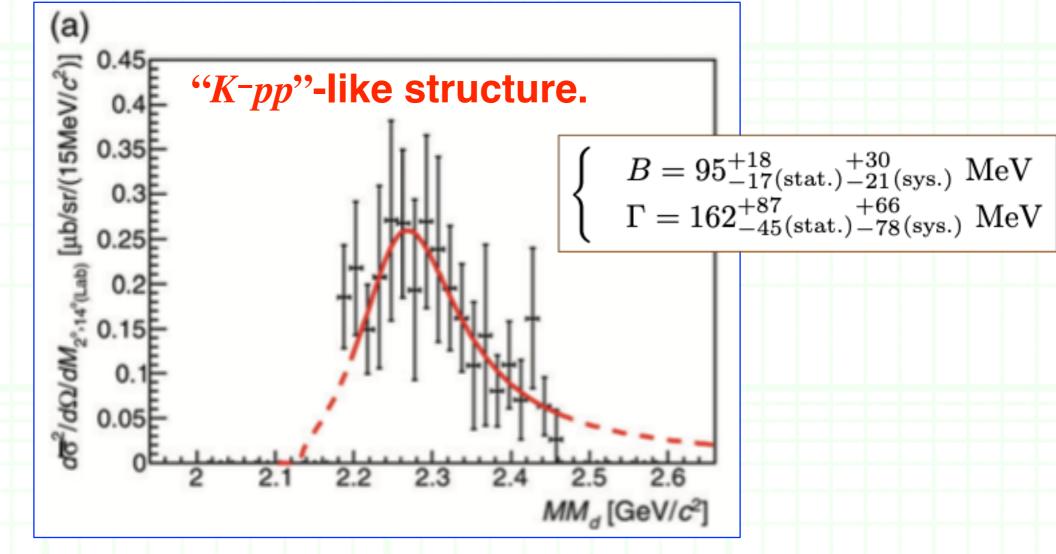
□ Calculate the Λp invariant mass spectrum of K^{-3} He -> $\Lambda p n$.



++ Observed peak(s) ++

• [Exp.] How about the peak in the J-PARC E27 data ?

 $\Box \text{ <u>The } \pi^+ d \longrightarrow K^+ \Sigma^0 p \text{ reaction.}$ </u>



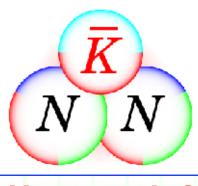
Ichikawa et al. [J-PARC E27], PTEP 2015 021D01.

--- Two-pole nature for the \overline{KNN} bound state, as $\Lambda(1405)$???

++ Structure ++

 [Theory / Exp.] What is the "structure" of the *KNN* bound state ?
 --- How much the resonance state discovered in J-PARC E15 contains the *KNN* fraction ?

□ For the moment, we can only say that there exist a resonance in the Λp spectrum of K^{-3} He -> $\Lambda p n$.



How much?

Because the resonance is generated by the k beam and decays into Λp,
 the resonance contains certain fractions of KNN and Λp.
 The resonance couples to the KNN and Λp channels.

We have to define three-body compositeness for the *KNN* bound state and establish how to evaluate it in theoretical models / from Exp. data.

++ Spin / parity ++

[Exp.] What is the spin / parity of the *KNN* bound state ?
 The Exp. signal of the *KNN* bound state <u>can be explained</u> by single Breit-Wigner form as:

$$f_{\{Kpp\}} = \frac{C_{Kpp} \left(\Gamma_{Kpp}/2\right)^2}{\left(M - M_{Kpp}\right)^2 + \left(\Gamma_{Kpp}/2\right)^2} \exp\left(-\left(\frac{q}{Q_{Kpp}}\right)^2\right)$$

--- Angular dependence of the Exp. data is consistent with the *KNN* state in *S* wave. --> Consistent with *J*^{*P*} = 0⁻. Ajimura *et al.*, *Phys. Lett.* <u>B789</u> (2019) 620.

□ To fix the spin / parity in Exp. in a model independent manner, we have to measure decay angle and polarizations of Λ and p. --- cf. $\gamma p \rightarrow K^+ \Lambda(1405)$ reaction. Moriva et al. [CLAS], Phys. Rev. Lett. 112 (2014) 082004.

The 14th Hadron Spectroscopy Cafe "*KNN* at J-PARC" @ Tokyo Inst. Tech. (May 27, 2019)

P-wave decay

S-wave decay

++ Spatial size ++

Exp.] From the analysis of Exp. data, they commented on

the "spatial size" of the $\overline{K}NN$ bound state.

$$f_{\{Kpp\}} = \frac{C_{Kpp} \left(\Gamma_{Kpp}/2\right)^2}{\left(M - M_{Kpp}\right)^2 + \left(\Gamma_{Kpp}/2\right)^2} \exp\left(-\left(\frac{q}{Q_{Kpp}}\right)^2\right) \frac{1}{8789} \text{ (2019) 620.}$$

--- With $Q_{Kpp} = 381 \pm 14 (stat.)^{+57}_{-0} (sys.)$ MeV/c , which is very large value, a very compact system was formed (~ 0.5 fm).

- Theory] However, there are several factors which generates q dependence of the cross section.
 - Spatial size of the <u>knn</u> bound state.
 - Angular dependence of the K-n -> K-n and K-p -> K
 0 amplitudes at the first collision. They should be off-shell !

--> Therefore, we cannot directly conclude the spatial size of the formed $\overline{K}NN$ bound state.

++ Summary of the *KNN* bound state ++

	<i>K</i> <i>NN</i> bound state	
Prediction	2002 ~	
Discovery	2019 ?	
Spin / parity	<i>J</i> ^{<i>P</i>} = 0 [−] ???	
Interaction	Two-body <i>K̄N and NN</i> + Three-body <i>K̄NN</i> ?	
Component	<i><u>KNN</u></i> dominant ???	
Peak position	Depends on reaction	
Pole position	???	

4. Summary

4. Summary

++ Summary ++

	$\Lambda(1405)$ as $\overline{K}N$ bound state	<i><u>KNN</u></i> bound state
Prediction	1959	2002 ~
Discovery	1961	2019 ?
Spin / parity	1/2- (2014)	<i>J</i> ^{<i>P</i>} = 0 [−] ???
Interaction	Chiral dynamics	Two-body <i>KN</i> and <i>NN</i> + Three-body <i>KNN</i> ?
Component	$\overline{K}N$ dominant in chiral D (2015 ~)	<i>Ī</i> <i>KNN</i> dominant ???
Peak position	Depends on reaction	Depends on reaction
Pole position	$(1415 - 1435) - (10 - 25) i MeV^*$???

Assuming chiral dynamics.

 [My guess] Without any excellent ideas, we need one-half century to pin down properties of the <u>KNN</u> bound state in Exps.

Thank you very much for your kind attention !