

# *Hadron-hadron correlation and interaction from high-energy nuclear collisions*

**Akira Ohnishi (YITP, Kyoto U.)**

*The 15th Hadron Spectroscopy Cafe*

*“Hadron interactions and Exotics in Heavy Ion collisions”,  
Jan. 10, 2020, Tokyo Institute of Technology*

*K. Morita, T. Furumoto, AO, PRC91('15)024916 ( $\Lambda\Lambda$ )*

*AO, K. Morita, K. Miyahara, T. Hyodo, NPA954 ('16)294 ( $\Lambda\Lambda$ ,  $K^-p$ )*

*K. Morita, AO, F. Etminan, T. Hatsuda, PRC94('16)031901(R) ( $\Omega N$ )*

*S. Cho et al. (ExHIC Collab.), Prog.Part.Nucl.Phys.95('17)279 ( $\Lambda\Lambda$ ,  $K^-p$ )*

*T. Hatsuda, K. Morita, AO, K. Sasaki, NPA967('17)856 ( $\Xi^-p$ )*

*K. Morita, S. Gongyo, T. Hatsuda, T. Hyodo, Y. Kamiya, AO,  
PRC101('20)015201 [1908.05414] ( $N\Omega$ ,  $\Omega\Omega$ )*

*Y. Kamiya, T. Hyodo, K. Morita, AO, W. Weise  
arXiv:1911.01041 [nucl-th] ( $K^-p$ )*



# Hadron Physics at High-Energy Colliders ?

- High-Energy Nuclear Collisions ( $\sqrt{s_{NN}}=40 \text{ GeV} - 14 \text{ TeV}$ ) as a Hadron Factory
  - Higgs, BSM, SUSY, QGP, ...
  - $dN/dy \sim 1000$  (RHIC, Au+Au)  $\rightarrow 10^3-10^5$  hadrons in one event
  - Various hadrons, nuclei ( $A \leq 4$ ) and anti-nuclei are formed.
  - Yield  $\sim$  Stat. Model calc.  
(Formation processes are too complicated to be out of statistical.)

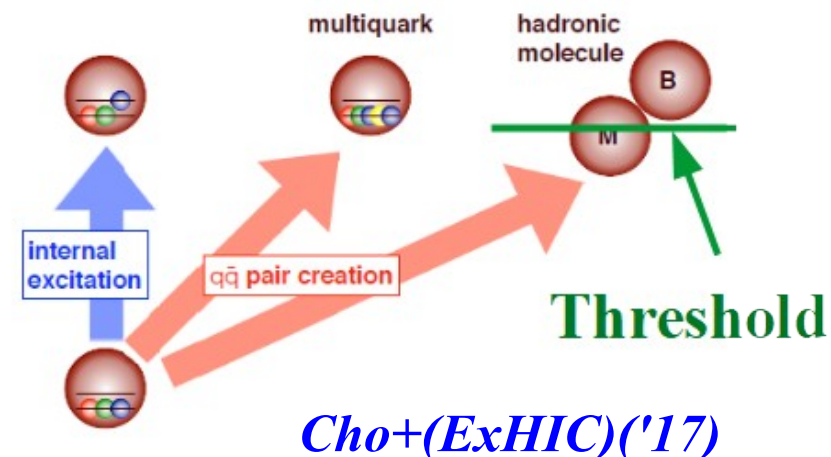
- Trend in Hadron physics

- Quark-gluon structure of hadrons (Multi-quark or Hadronic molecule)

- Hadrons with heavy-quarks

- Hadron-Hadron interaction  $\Lambda N, \Sigma N, \Lambda\Lambda, \Xi N, \bar{K}N, \dots$

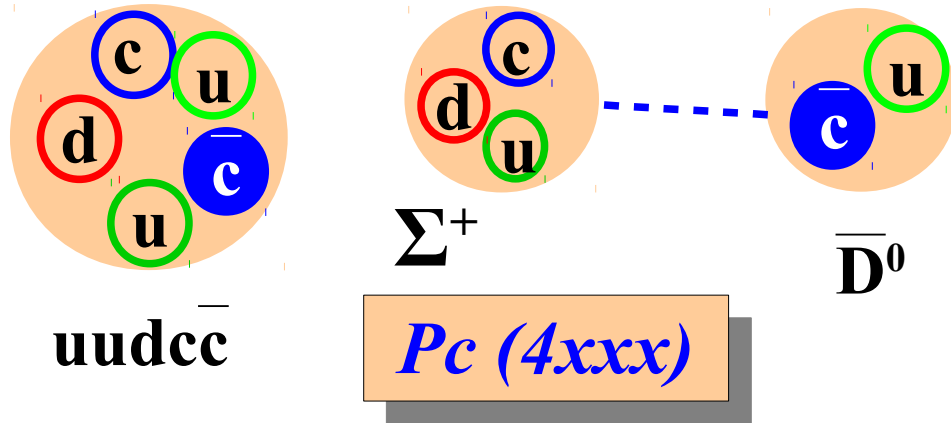
- Hadrons in nuclear matter / EOS of nuclear matter



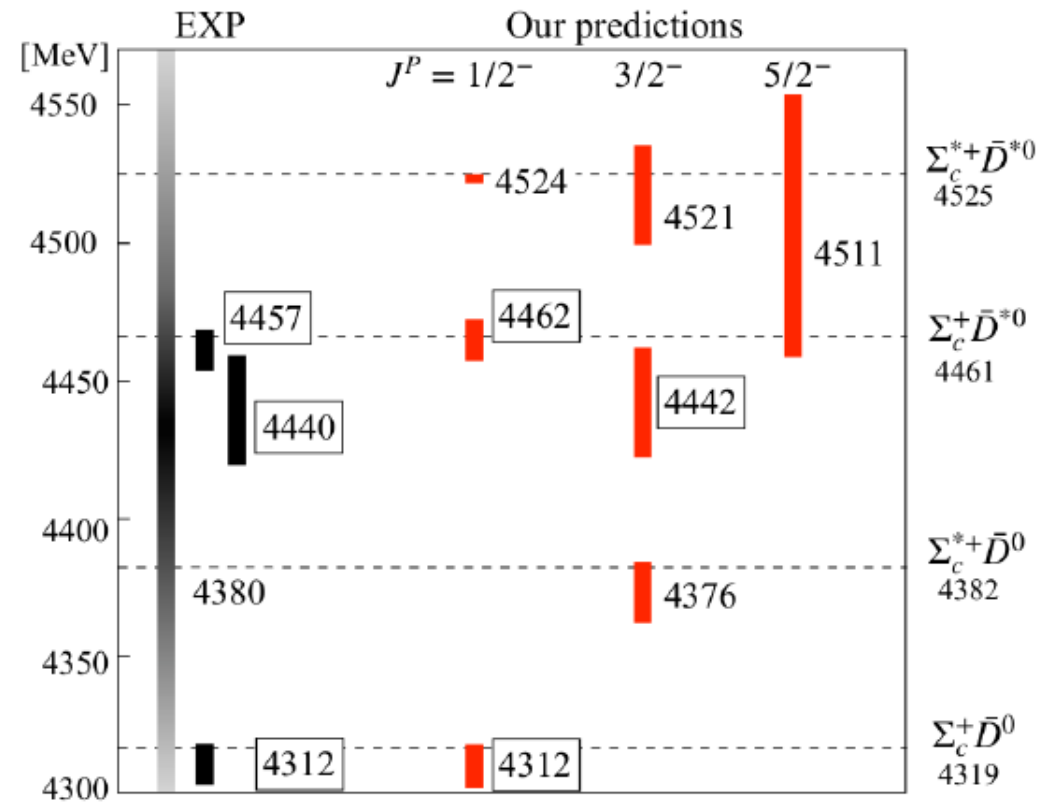
# Compact Multiquark State or Hadronic Molecule

- The answer may be “the superposition” (for pentaquarks) !

*Y. Yamaguchi, H. García-Tecocoatzi, A. Giachino, A. Hosaka, E. Santopinto, S. Takeuchi, M. Takizawa, arXiv:1907.04684*



*To confirm the structure, we need to understand scatt. amp. or potential via inv. mass spec. or corr. fn. !*



*E.g. Y. Ikeda et al. (HAL QCD), PRL117('16)242001 (Zc(3900))*

# Hadron Physics at High-Energy Colliders ?

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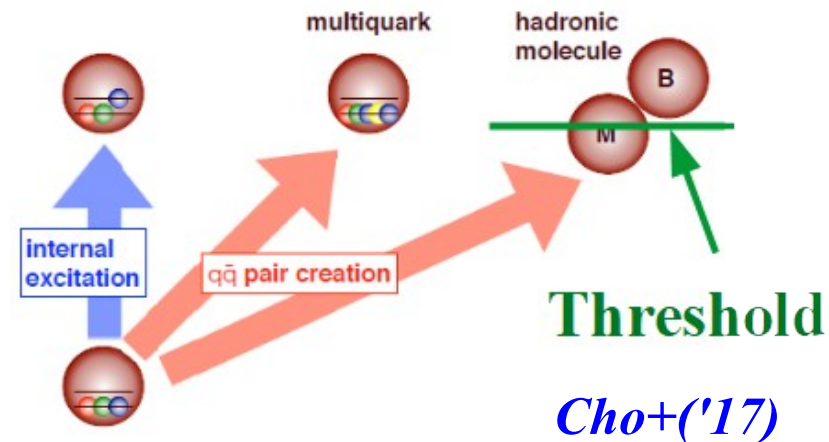
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Corr. Fn.

# Outline

- **Generic introduction: Hadron physics at Colliders ?**
- **Correlation function and interaction**
  - Two ways to use the correlation function
  - Scattering length dependence of the correlation function
- **Baryon-Baryon Interaction and Correlation Function**
  - Where is dibaryon ?
  - $p\Omega$  correlation from lattice QCD potential, STAR and ALICE.
  - ( $\Lambda\Lambda$ ,  $p\Xi$  and  $\Omega\Omega$  correlations)
- **Kaon-Nucleon Interaction and Correlation Function**
  - Coupled Channels Effects on Corr. Fn.
  - $\bar{K}N$  potential and correlation from chiral SU(3) dynamics and  $K^-p$  correlation from ALICE
- **Summary**

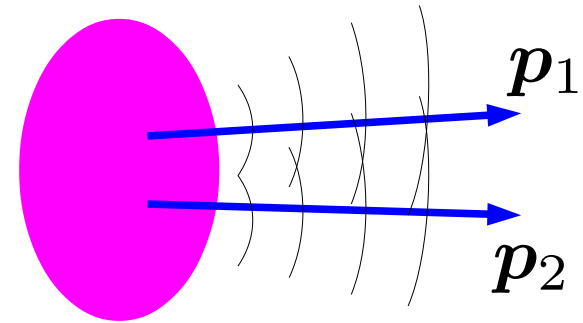
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# *Correlation Function and Interaction*

# Correlation Function

- Emitting source function

$$N_i(\mathbf{p}) = \int d^4x S_i(x, \mathbf{p})$$



- Two-particle momentum dist.

- Assumption: Two particles are produced independently, and the correlation is generated by the final state int.

*Koonin('77), Pratt+('86), Lednicky+('82)*

$$N_{12}(\mathbf{p}_1, \mathbf{p}_2) \simeq \int d^4x d^4y S_1(x, \mathbf{p}_1) S_2(y, \mathbf{p}_2) \underbrace{|\Psi_{\mathbf{p}_1, \mathbf{p}_2}(x, y)|^2}_{\text{two-body w.f.}}$$

$$\simeq \int d^4x d^4y S_1(x, \mathbf{p}_1) S_2(y, \mathbf{p}_2) \underbrace{|\varphi_q(\mathbf{r})|^2}_{\text{relative w.f.}}$$

- Correlation function

$$C(\mathbf{p}_1, \mathbf{p}_2) = \frac{N_{12}(\mathbf{p}_1, \mathbf{p}_2)}{N_1(\mathbf{p}_1)N_2(\mathbf{p}_2)} \simeq \int d\mathbf{r} S_{12}(\mathbf{r}) |\varphi_q(\mathbf{r})|^2$$

# Correlation Function

- **Example: Free identical bosons (spin 0, non-relativistic), Gaussian source (static, simultaneous, spherical)**

$$S(\mathbf{x}, \mathbf{p}) \propto \exp \left[ -\frac{\mathbf{x}^2}{2R^2} - \frac{\mathbf{p}^2}{2MT} \right]$$

$$S(\mathbf{x}, \mathbf{p}_1) S(\mathbf{y}, \mathbf{p}_2) \propto \exp \left[ -\frac{R_{\text{cm}}^2}{R^2} - \frac{\mathbf{r}^2}{4R^2} - \frac{\mathbf{P}^2}{4MT} - \frac{\mathbf{q}^2}{2\mu T} \right]$$

$$\begin{aligned} \Psi_{\mathbf{p}_1, \mathbf{p}_2}(\mathbf{x}, \mathbf{y}) &\propto \frac{1}{\sqrt{2}} \left[ e^{i\mathbf{p}_1 \cdot \mathbf{x} + i\mathbf{p}_2 \cdot \mathbf{y}} + e^{i\mathbf{p}_1 \cdot \mathbf{y} + i\mathbf{p}_2 \cdot \mathbf{x}} \right] \\ &= e^{i\mathbf{P} \cdot \mathbf{R}_{\text{cm}}} \times \sqrt{2} \cos \mathbf{q} \cdot \mathbf{r} \end{aligned}$$

- **Correlation function**

$$\begin{aligned} C(\mathbf{q}) &= (4\pi R^2)^{-3/2} \int d\mathbf{r} \exp \left[ -\frac{\mathbf{r}^2}{4R^2} \right] 2 \cos^2 \mathbf{q} \cdot \mathbf{r} \\ &= 1 + \exp(-4q^2 R^2) \end{aligned}$$

**Correlation Function  $\rightarrow$  Source Size**



# How can we measure the radius of a star ?

## Two photon intensity correlation

*Hanbury Brown & Twiss, Nature 10 (1956), 1047.*

- Simultaneous two photon observation probability is enhanced from independent emission cases  
 → angular diameter of Sirius=6.3 msec

**Recent data (Wikipedia)**  
**5.936±0.016 msec**

A TEST OF A NEW TYPE OF STELLAR INTERFEROMETER ON SIRIUS

By R. HANBURY BROWN

Jodrell Bank Experimental Station, University of Manchester

AND

DR. R. Q. TWISS

Services Electronics Research Laboratory, Baldock

NATURE November 10, 1956 VOL. 178

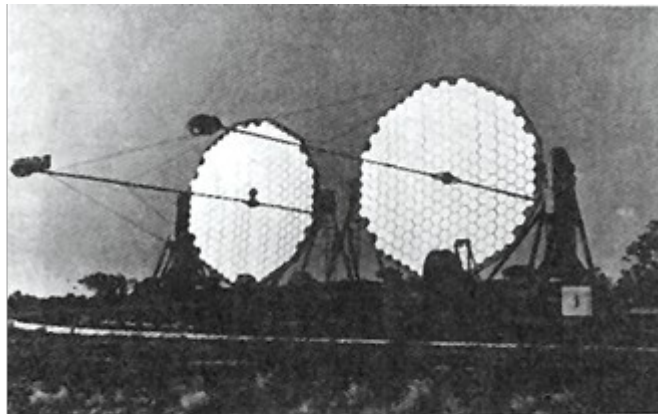


Figure 2. Picture of the two telescopes used in the HBT experiments. The figure was extracted from Ref.[1].

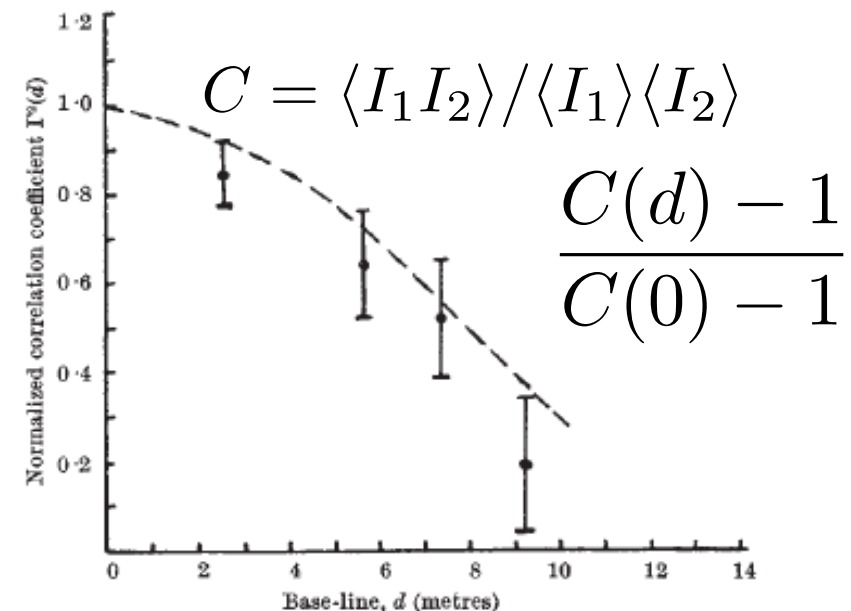


Fig. 2. Comparison between the values of the normalized correlation coefficient  $\Gamma^2(d)$  observed from Sirius and the theoretical values for a star of angular diameter  $0.0063''$ . The errors shown are the probable errors of the observations

*HBT telescope (from Goldhaber, ('91))*

*HBT ('56)*

# Two particle intensity correlation

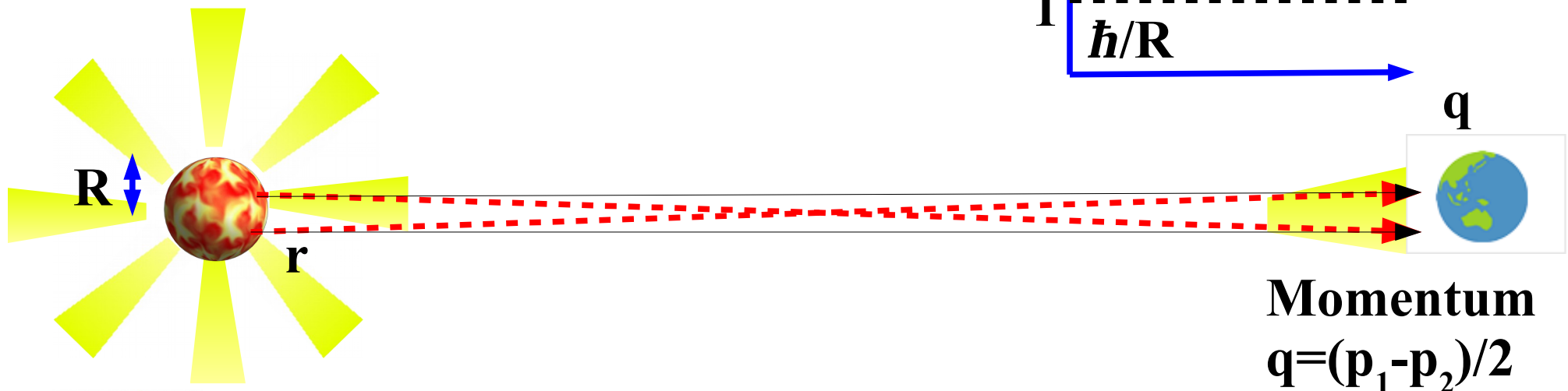
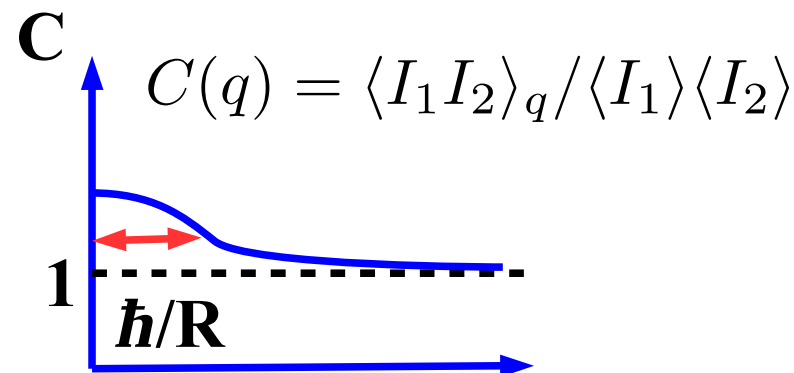
- Wave function symmetrization from quantum statistics

$$C(\mathbf{q}) = \int d^3r S(\mathbf{q}, \mathbf{r}) \left| \frac{1}{\sqrt{2}} (e^{i\mathbf{q}\cdot\mathbf{r}} + e^{-i\mathbf{q}\cdot\mathbf{r}}) \right|^2 \simeq \underline{1 + \exp(-4q^2 R^2)}$$

Source fn.  
( $\mathbf{r}$ =relative coordinate)  
(symmetrized w.f.)<sup>2</sup>

Static spherical source case

→ Small relative momenta are favored due to symmetrization of the relative wave function.



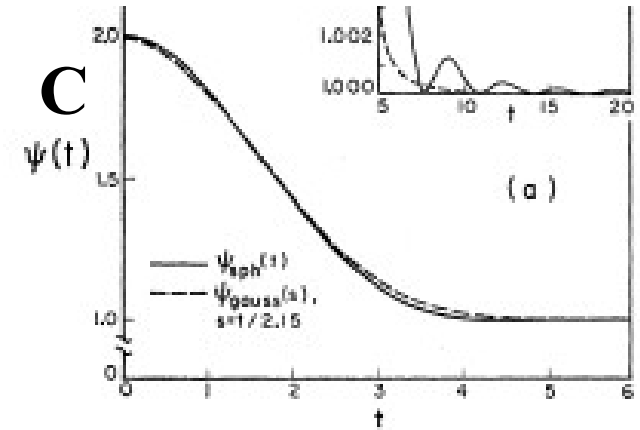
# How can we measure source size in nuclear reactions ?

## ■ Two pion interferometry

*G. Goldhaber, S. Goldhaber, W. Lee, A. Pais, Phys. Rev. 120 (1960), 300*

- Two pion emission probability is enhanced at small relative momenta

→ Pion source size  $\sim 0.75 \hbar / \mu c$



$q$  (relative momentum)

PHYSICAL REVIEW

VOLUME 120, NUMBER 1

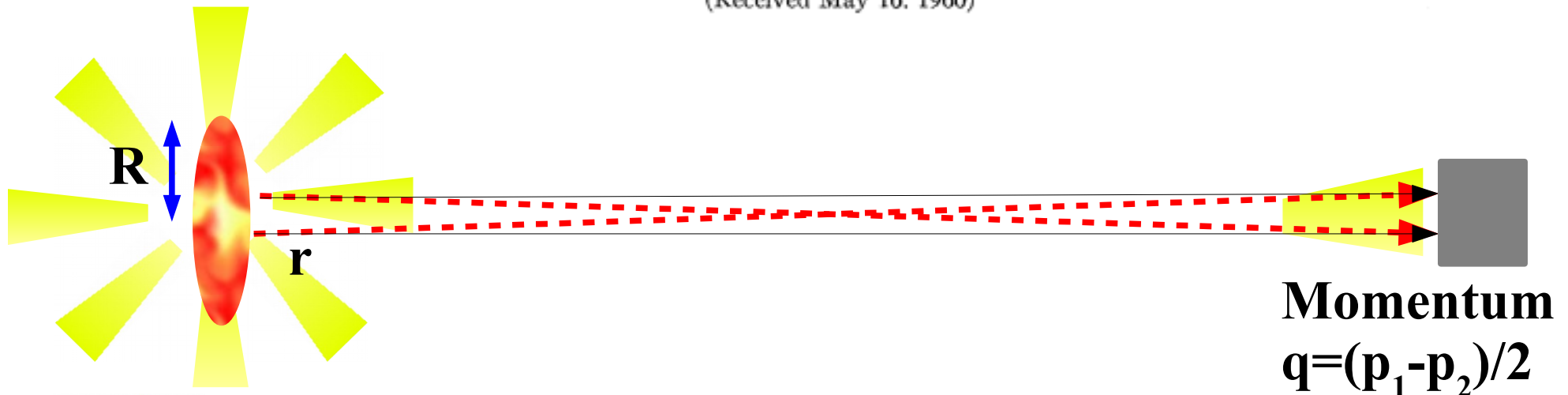
OCTOBER 1, 1960

## Influence of Bose-Einstein Statistics on the Antiproton-Proton Annihilation Process\*

GERSON GOLDHABER, SULAMITH GOLDHABER, WONYONG LEE, AND ABRAHAM PAIS†

*Lawrence Radiation Laboratory and Department of Physics, University of California, Berkeley, California*

(Received May 16, 1960)



# Femtoscopic Study of Hadron-Hadron Interaction

- **HBT, GGLP: Corr. Fn. + w.f. → Source Size**  
**Another way: Corr. Fn. + Source Size**  
→ wave function → hadron-hadron interaction
- **Effect of hadron-hadron interaction on the wave function**
  - Assumption: Only s-wave (L=0) is modified.
  - Non-identical particle pair, Gauss source.

$$\varphi_{\mathbf{q}}(\mathbf{r}) = e^{i\mathbf{q}\cdot\mathbf{r}} - j_0(qr) + \chi_q(r)$$

$$\rightarrow C(\mathbf{q}) = \int d\mathbf{r} S(r) |\varphi_{\mathbf{q}}(\mathbf{r})|^2$$

$$= 1 + \int d\mathbf{r} S(r) \{ |\chi_q(r)|^2 - |j_0(qr)|^2 \}$$

*K. Morita, T. Furumoto, AO, PRC91('15)024916*

*Corr. Fn. shows how much squared w. f. is enhanced  
→ Large CF is expected with attraction*

# Wave function around threshold (S-wave, attraction)

## Low energy w.f. and phase shift

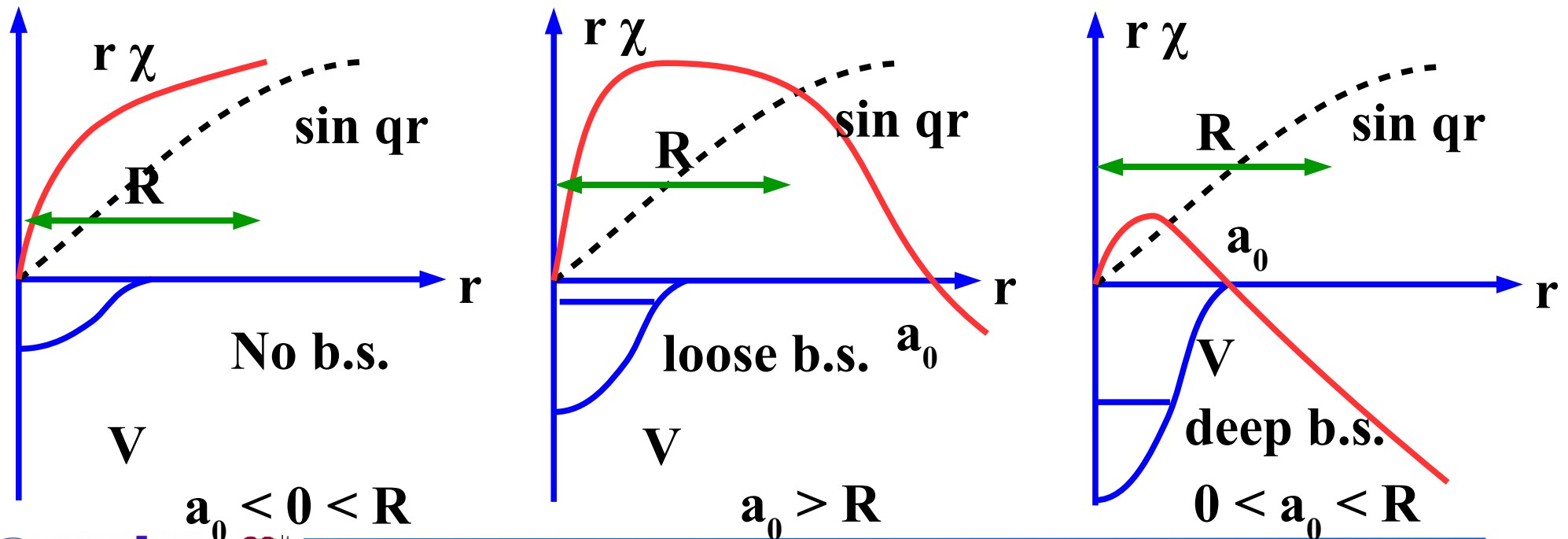
$$u(r) = qr\chi_q(r) \rightarrow \sin(qr + \delta(q)) \sim \sin(q(r - a_0))$$

$$q \cot \delta = -\frac{1}{a_0} + \frac{1}{2}r_{\text{eff}}q^2 + \mathcal{O}(q^4) \quad (\delta \sim -a_0q)$$

$a_0$  = scatt. length

$r_{\text{eff}}$  = eff. range

- Wave function grows rapidly at small  $r$  with attraction.
- With a bound state ( $a_0 > 0$ ), a node appears around  $r = a_0$



# Lednický-Lyuboshits (LL) model

## ■ Lednický-Lyuboshits analytic model

- **Asymp. w.f. + Eff. range corr. +  $\psi^{(-)} = [\psi^{(+)}]^*$**

$$\psi_0(r) \rightarrow \psi_{\text{asy}}(r) = \frac{e^{-i\delta}}{qr} \sin(qr + \delta) = \mathcal{S}^{-1} \left[ \frac{\sin qr}{qr} + f(q) \frac{e^{iqr}}{r} \right]$$

$$\begin{aligned} \Delta C_{\text{LL}}(q) &= \int dr S_{12}(r) (|\psi_{\text{asy}}(r)|^2 - |j_0(qr)|^2) \\ &= \frac{|f(q)|^2}{2R^2} F_3\left(\frac{r_{\text{eff}}}{R}\right) + \frac{2\text{Re}f(q)}{\sqrt{\pi}R} F_1(x) - \frac{\text{Im}f(q)}{R} F_2(x) \end{aligned}$$

( $x = 2qR$ ,  $R = \text{Gaussian size}$ ,  $F_1, F_2, F_3$  : Known functions)

## ■ Phase shifts

$$q \cot \delta = -\frac{1}{a_0} + \frac{1}{2} r_{\text{eff}} q^2 + \mathcal{O}(q^4) \rightarrow \delta \simeq -a_0 q + \mathcal{O}(q^3)$$

$$\sin(qr + \delta) \simeq \sin(q(r - a_0) + \dots) \quad \text{Node at } \mathbf{r} \sim \mathbf{a}_0$$

**for small  $q$**

# $C(q)$ in the low momentum limit

- Correlation function at small  $q$  (and  $r_{\text{eff}}=0$ )  $\rightarrow F_1=1, F_2=0, F_3=1$

$$\Delta C_{\text{LL}}(q) \rightarrow \frac{|f(0)|^2}{2R^2} + \frac{2\text{Re}f(0)}{\sqrt{\pi}R} \quad (q \rightarrow 0)$$

$$f(q) = (q \cot \delta - iq)^{-1} \simeq \left( -\frac{1}{a_0} + \frac{1}{2}r_{\text{eff}}q^2 - iq \right)^{-1} \rightarrow -a_0$$

$$C_{\text{LL}}(q \rightarrow 0) = 1 + \frac{a_0^2}{2R^2} - \frac{2a_0}{\sqrt{\pi}R} = 1 - \frac{2}{\pi} + \frac{1}{2} \left( \frac{a_0}{R} - \frac{2}{\sqrt{\pi}} \right)^2$$

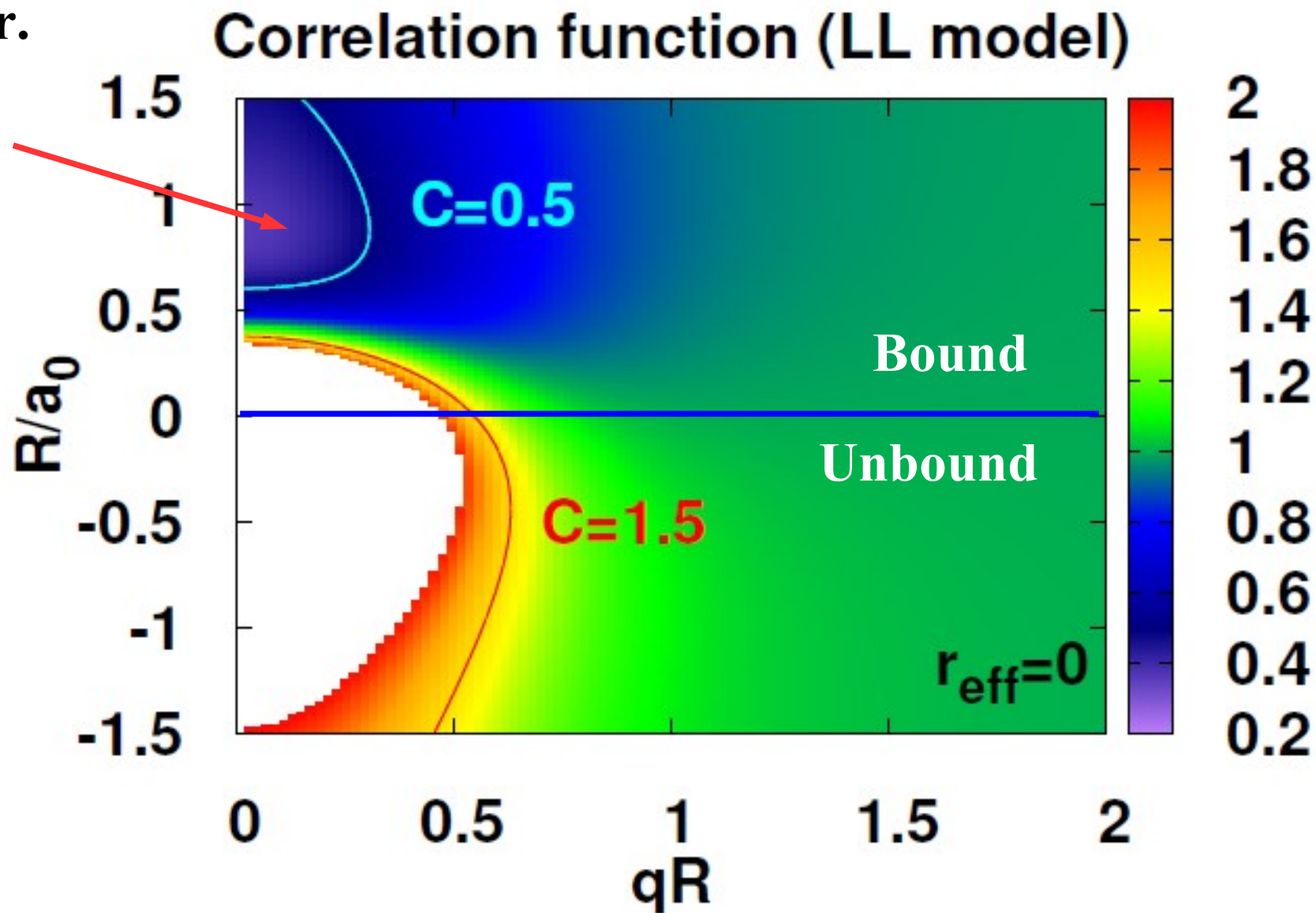
$$1 - 2/\pi \simeq 0.36, \quad \sqrt{\pi}/2 \simeq 0.89$$

$C(q \rightarrow 0)$  takes a minimum of **0.36** at  $R/a_0 = 0.89$  in the LL model.



# Correlation Function in LL model

Suppr.  
from  
node



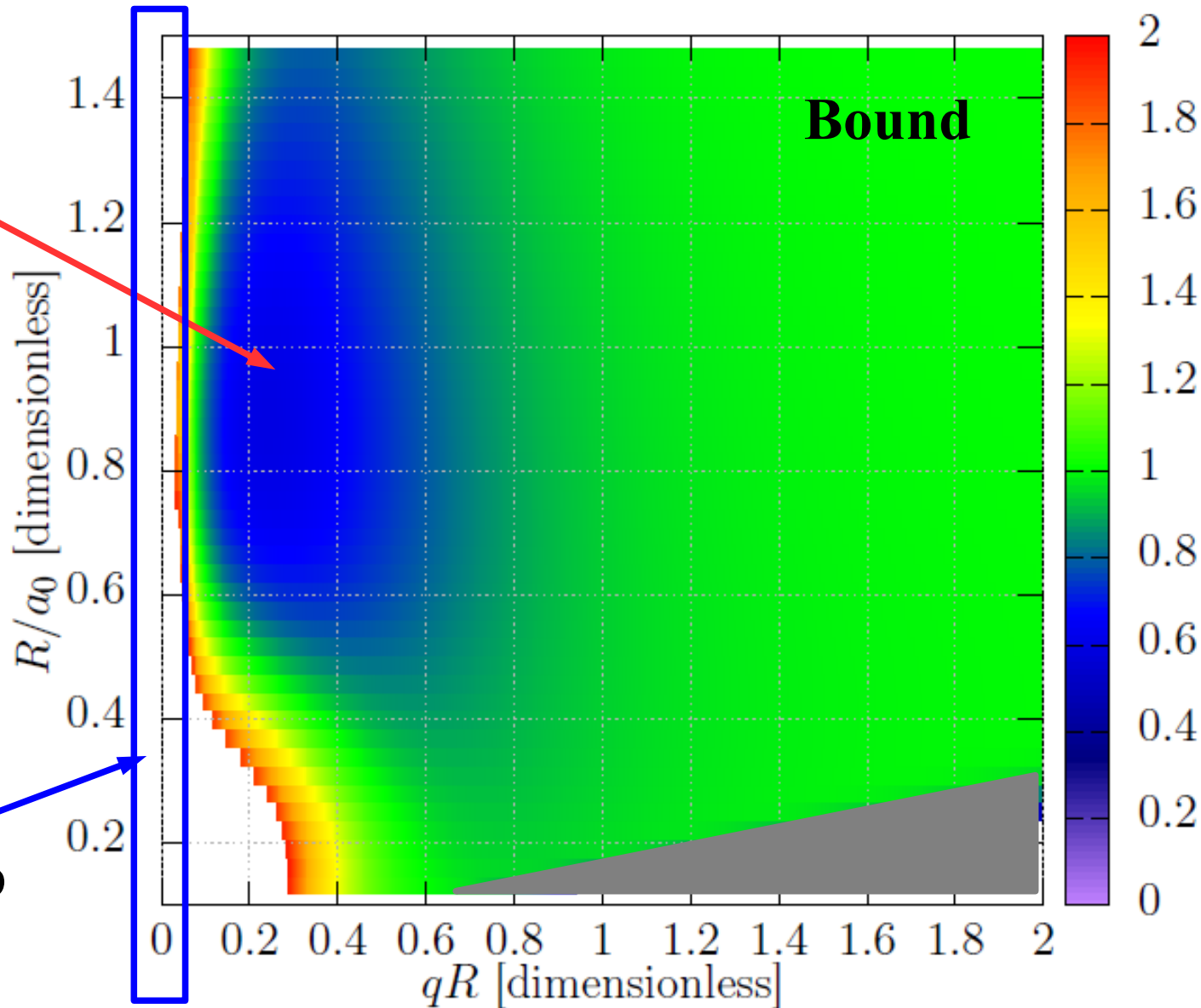
*LL model: R. Lednicky, V. L. Lyuboshits ('82)*

*Similar Fig. is shown in AO, K. Morita, K. Miyahara, T. Hyodo, NPA954('16), 294.*



# Correlation Function with Gaussian source

Suppr.  
from  
node



Coulomb  
enh.

$N\Omega$  potential ( $J=2$ , HAL QCD,  $a_0=3.4$  fm) + Coulomb

# *Femtoscopic study of Hadron-Hadron Interaction*

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- **Correlation Function is sensitive to interaction and source (size).**
  - **If you know the source (size), it is possible to constrain the interaction parameters such as scattering length ( $a_0$ ) and effective range ( $r_{\text{eff}}$ ).**
- **Source size dependence of the Correlation Function**
  - **Corr. Fn. is enhanced at any  $R$  for negative  $a_0$ . (w/o bound state)**
  - **Corr. Fn. is enhanced at  $R < a_0$  and suppressed at  $R \sim a_0$  for positive  $a_0$ . (w/ bound state or repulsive int.)**
  - **With repulsive int.,  $a_0 \sim r_c$  (hard core radius), and cannot be large, and coupled channels effects generally enhances corr. fn.**
- **And many experimental data are coming...**

# Recent Measurement of Hadron-Hadron Corr. Fn.

## ■ $\Lambda\Lambda$

*Adamczyk et al. (STAR Collaboration), PRL 114 ('15) 022301.*

*S. Achara et al. (ALICE), PRC99('19), 024001; arXiv:1905.07209*

*Th: K.Morita, T.Furumoto, AO, PRC91('15)024916;*

*AO, K.Morita, K.Miyahara, T.Hyodo, NPA954 ('16), 294 ( $\Lambda\Lambda$ ,  $K^-p$ )*

*S. Cho et al. (ExHIC Collab.), Prog.Part.Nucl.Phys.95('17)279 ( $\Lambda\Lambda$ ,  $K^-p$ )*

*J. Haidenbauer, NPA981 ('19) 1 ( $\Lambda\Lambda$ ,  $\Xi^-p$ ,  $K^-p$ ); Greiner,Muller('89); AO+('98)*

## ■ $\Omega^-p$

*J. Adam et al. (STAR), PLB790 ('19) 490 [1808.02511]*

*O. Vázquez Doce et al. (ALICE preliminary), Hadrons 2019*

*Th: K. Morita, AO, F. Etminan, T. Hatsuda, PRC94('16)031901(R)*

*K. Morita, S. Gongyo, T. Hatsuda, T. Hyodo, Y. Kamiya, AO, PRC101('20)015201*

## ■ $\Xi^-p$

*S. Acharya et al. (ALICE), PRL123 ('19)112002*

*Th: T. Hatsuda, K. Morita, AO, K. Sasaki, NPA967('17)856; J. Haidenbauer ('19)*

## ■ $K^-p$

*S. Acharya et al. (ALICE), arXiv:1905.13470*

*Th: AO+('16), S. Cho+(ExHIC)('17), J. Haidenbauer ('19)*

*Y. Kamiya, T. Hyodo, K. Morita, AO, W. Weise, arXiv:1911.01041*

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# *Baryon-Baryon Correlation Function (mainly on $p\Omega$ correlation)*

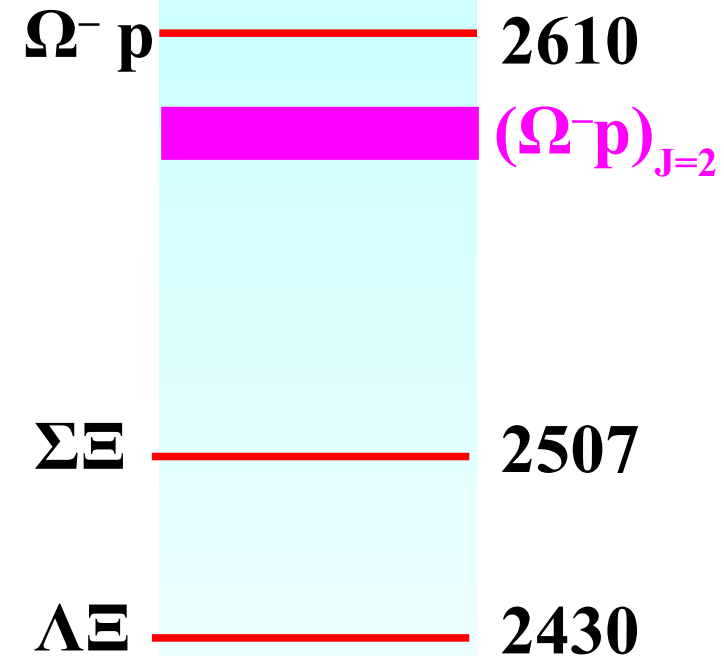
# Where is dibaryon ?

- Deuteron = First dibaryon (pn bound state)
  - H-particle: 6-quark state (uuddss)
    - Predicted (*Jaffe ('77)*), Ruled-out ( $\Lambda\Lambda$  nucl., *Takahashi+('01)*), Suggested as a resonance in exp. (*Yoon+ ('07)*) or as a bound state of  $\Xi N$  (*HAL QCD ('16)*)
  - Dibaryon would appear in channels, where *Oka ('88)*, *Gal ('16)*
    - The Pauli blocking of quarks does not operate,
    - and the Color-magnetic interaction is attractive
- Examples:  $H(=\Lambda\Lambda-N\Xi-\Sigma\Sigma)$ ,  $N\Omega$ ,  $N\Sigma^*$ ,  $d^*(=\Lambda\Lambda)$ .

*Let us examine the existence of dibaryon states by using the correlation function !*

# $\Omega N$ dibaryon

- $\Omega$  : sss,  $J\pi=3/2^+$ ,  $M=1672$  MeV
- Is there an  $\Omega N$  bound state ( $S=-3$  dibaryon) ?
  - Predicted as a dibaryon candidate  
*Goldman+ ('87), Oka ('88), Gal ('16)*
  - Lattice QCD predicts a bound state with narrow width for  $J=2$  ( ${}^5S_2$ )  
(Coupling to octet-octet with  $L=2$ )  
*Etminan+ (HAL QCD)('14), Iritani+ (HAL QCD) ('19)*
  - Meson exchange potential is also proposed  
*T. Sekihara, Y. Kamiya, T. Hyodo, PRC98 ('18) 015205*
  - Correlation function is measurable !  
*Adam+ (STAR)('19), ALICE, in prep.*



# $\Omega N$ potential from lattice QCD

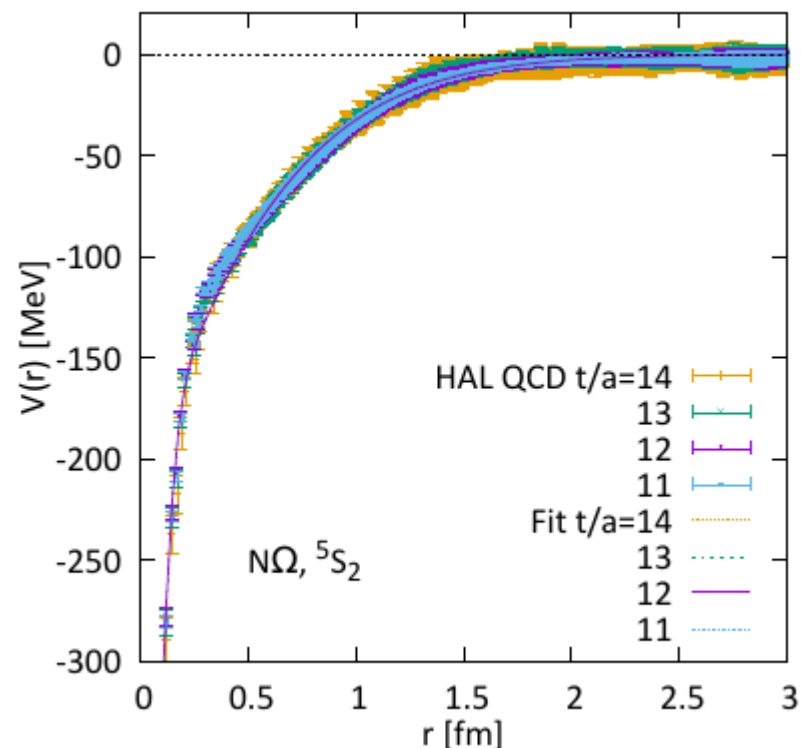
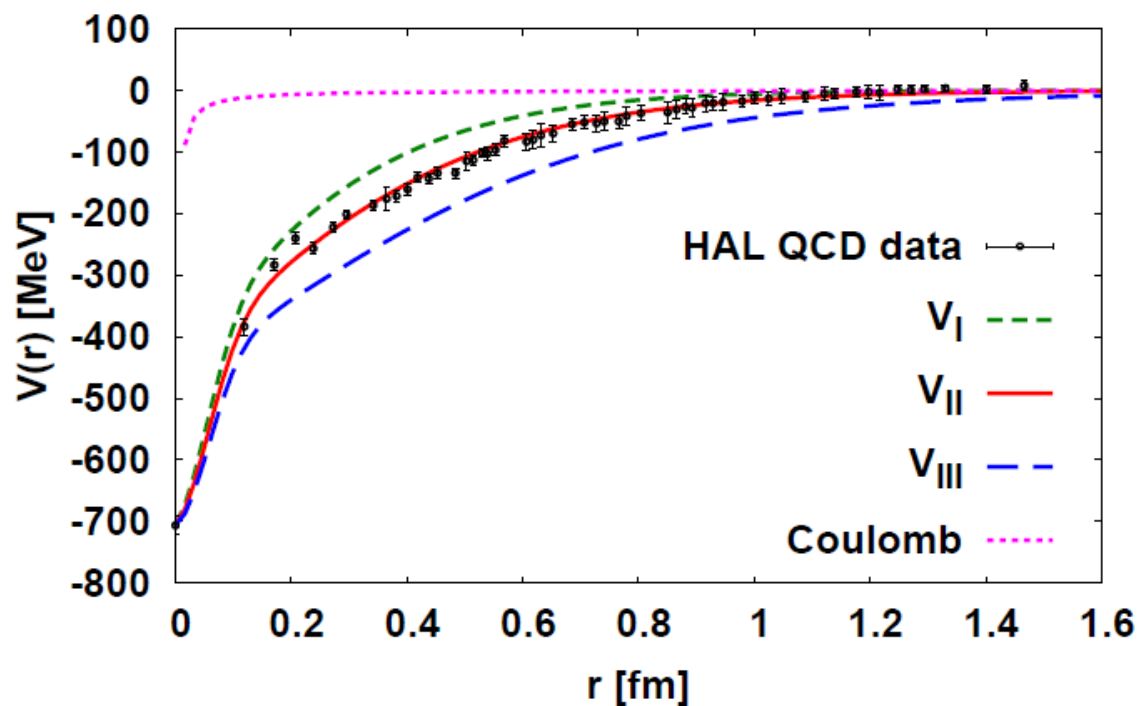
## ■ $\Omega N$ potential by HAL QCD Collab. ( $J=2$ )

- $m_\pi=875$  MeV, B.E.~ 0.63 MeV

*F. Etminan et al. (HAL QCD Collab.), NPA928('14)89.*

- $m_\pi=146$  MeV, B.E.~ 2.2 MeV

*T. Iritani et al. (HAL QCD Collab.), PLB 792('19)284.*

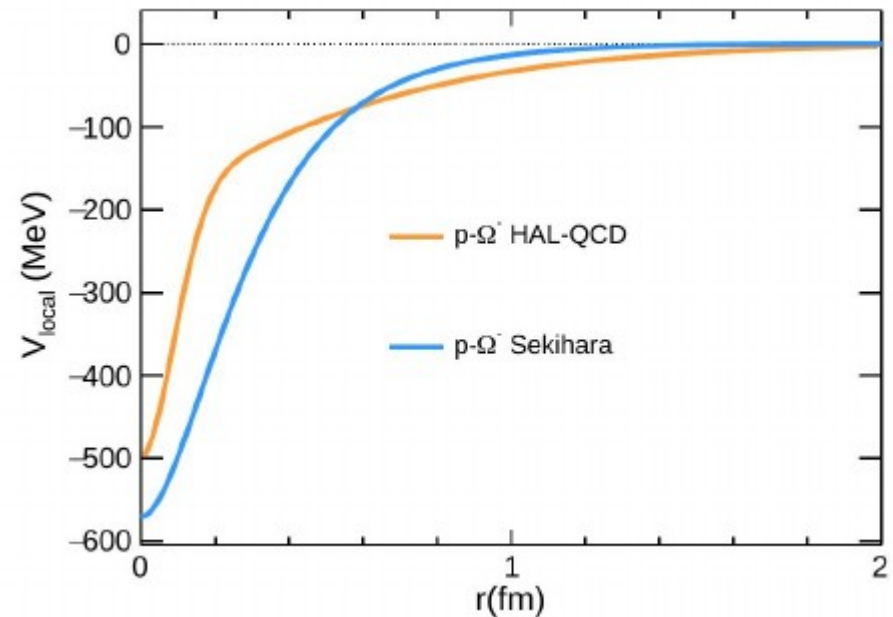
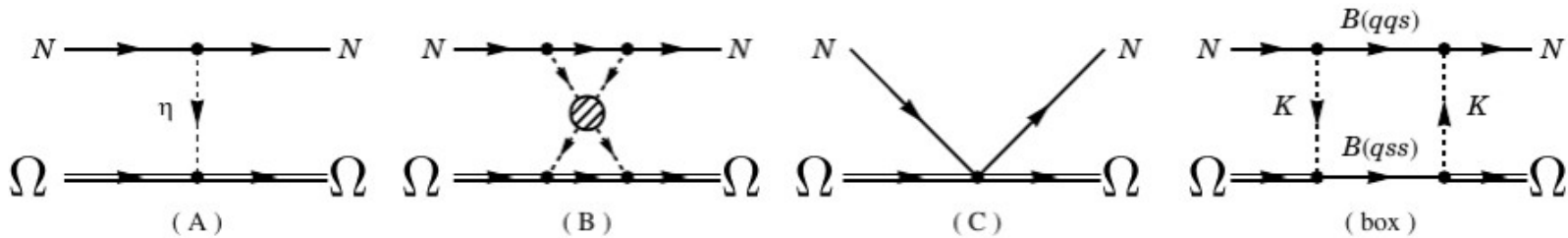


# Meson Exchange Potential

## ■ Meson exchange $N\Omega$ potential

*T. Sekihara, Y. Kamiya, T. Hyodo, PRC98 ('18) 015205*

- $\eta$  meson exchange,  $\sigma$  exchange, contact term, box diagram.
- Contact term is fitted to **the scatt. length** of HAL QCD potential.





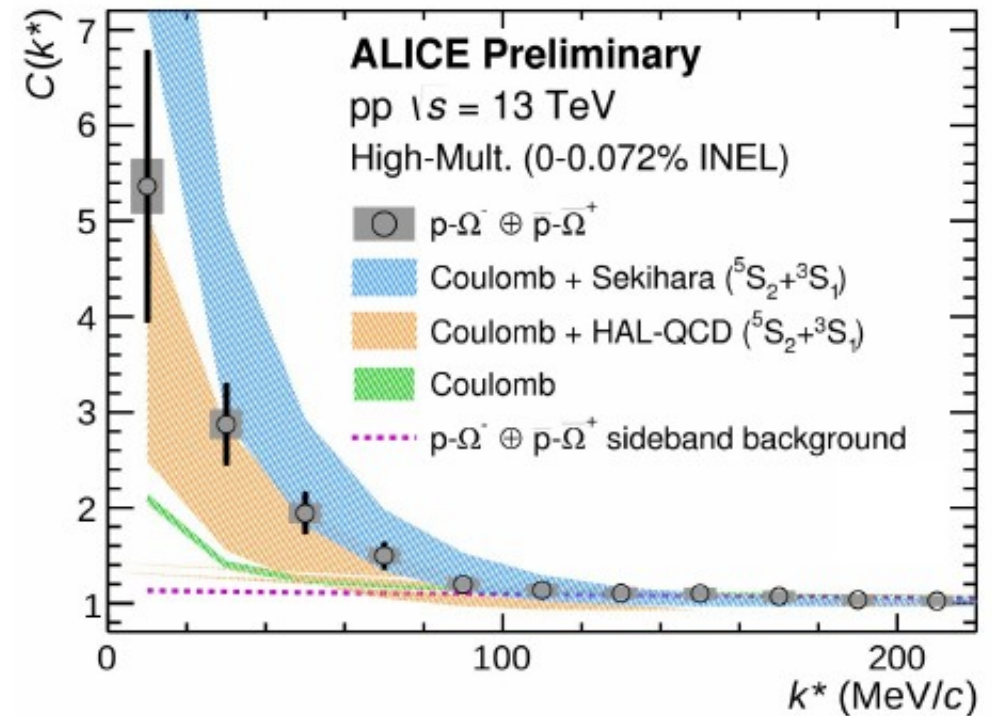
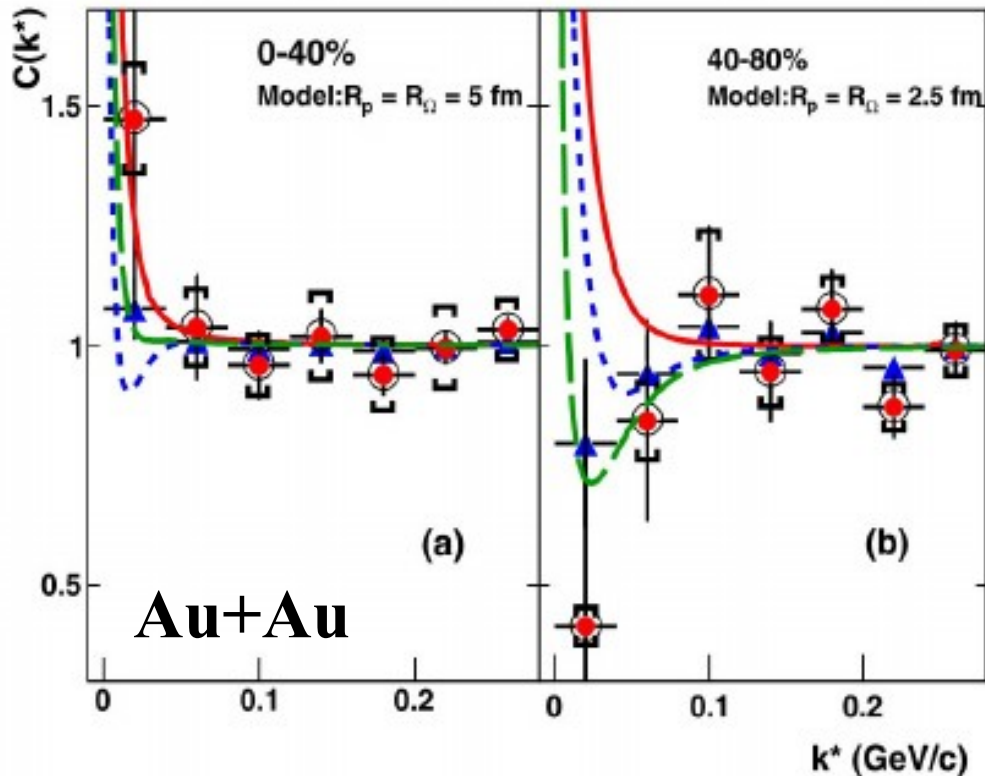
# $\Omega^- p$ correlation function data

## RHIC-STAR Collaboration

*J. Adam et al. (STAR), PLB790 ('19)  
490 [1808.02511]*

## LHC-ALICE Collaboration

*O. Vázquez Doce et al. (ALICE,  
preliminary), Hadrons 2019*



*Suppressed & Enhanced Corr. Fn. at RHIC & LHC, resp.  
Can we understand this difference?  
or Is one (or both) of them wrong?*

# PHYSICAL REVIEW C

covering nuclear physics

Highlights

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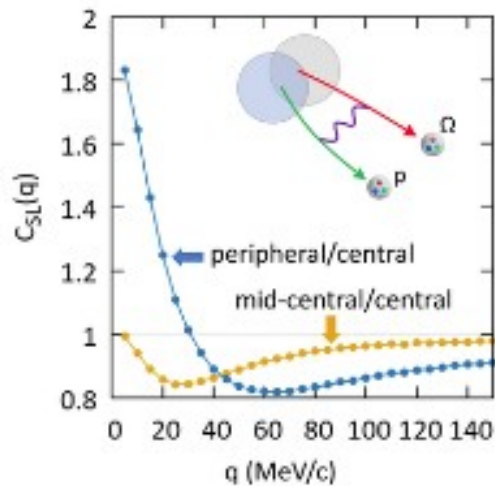
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## EDITORS' SUGGESTION

### Probing $\Omega\Omega$ and $p\Omega$ dibaryons with femtoscopy correlations in relativistic heavy-ion collisions

The authors investigate correlations between protons and  $\Omega$  baryons, and between two  $\Omega$  baryons, in heavy-ion collisions at RHIC and LHC. Given sufficient statistics in upcoming experiments, such measurements could provide valuable information on the existence of strange dibaryons and on the equation of state relevant to neutron stars.

Kenji Morita *et al.*

Phys. Rev. C **101**, 015201 (2020)

***K. Morita, S. Gongyo, T. Hatsuda, T. Hyodo, Y. Kamiya, AO, PRC101('20)015201***

# Calculation Details

*K. Morita, S. Gongyo, T. Hatsuda, T. Hyodo, Y. Kamiya, AO, PRC101('20)015201*

## ■ $N\Omega$ potential from HAL QCD Collab.

*Etminan+(HAL QCD) ('14), Iritani+ (HAL QCD)('19)*

- $J=1$  potential is uncertain  $\rightarrow$  Three models

Strong abs. at  $r < r_0$  ( $r_0 \sim 2$  fm) (*Morita+('16)*) (Standard)

Complete absorption  $\chi(J=1) = 0$  (Minimum)

Same w.f. as that with  $J=2$ ,  $\chi(J=1) = \chi(J=2)$  (Reference)

- Statistical Error can be evaluated by using Jackknife potentials.

## ■ Coulomb potential enhances CF even without strong int.

$\rightarrow$  Small-Large ratio of CF (*Morita+('16)*)

- Large source  $\rightarrow$  Coulomb force dominate

Small source  $\rightarrow$  Visible strong interaction effects

## ■ Source function: Blast wave, Gaussian source

# Emission Source Function

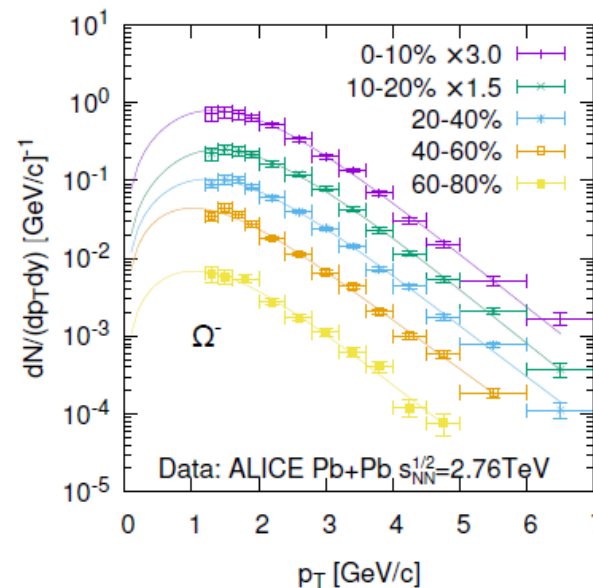
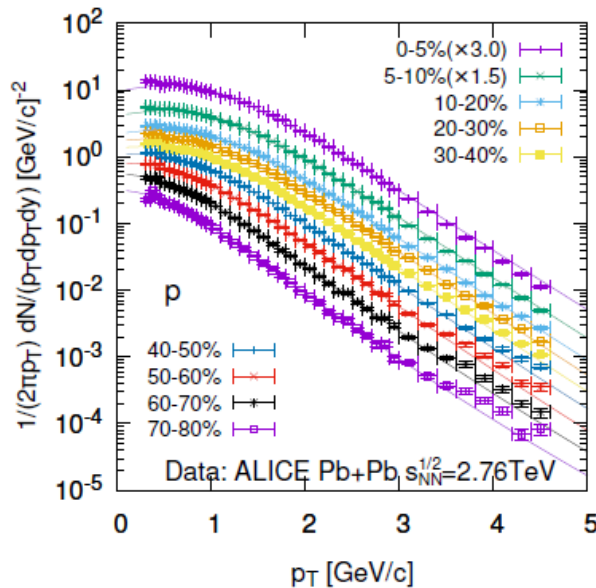
- Gaussian Source  $\propto \exp(-r^2/4R^2)$ ,  $R=(0.8-4)$  fm [Simple and convenient]

- Expanding source model [Reasonably realistic]  $u_\mu(x)$

Flow velocity

$$d^4x S_i(x, p) = \tau_0 d\eta_s d^2r_T \frac{d}{(2\pi)^3} \underline{n_f(u \cdot p, T)} \exp\left(-\frac{r_T^2}{2R_T^2}\right)$$

Fermi dist.



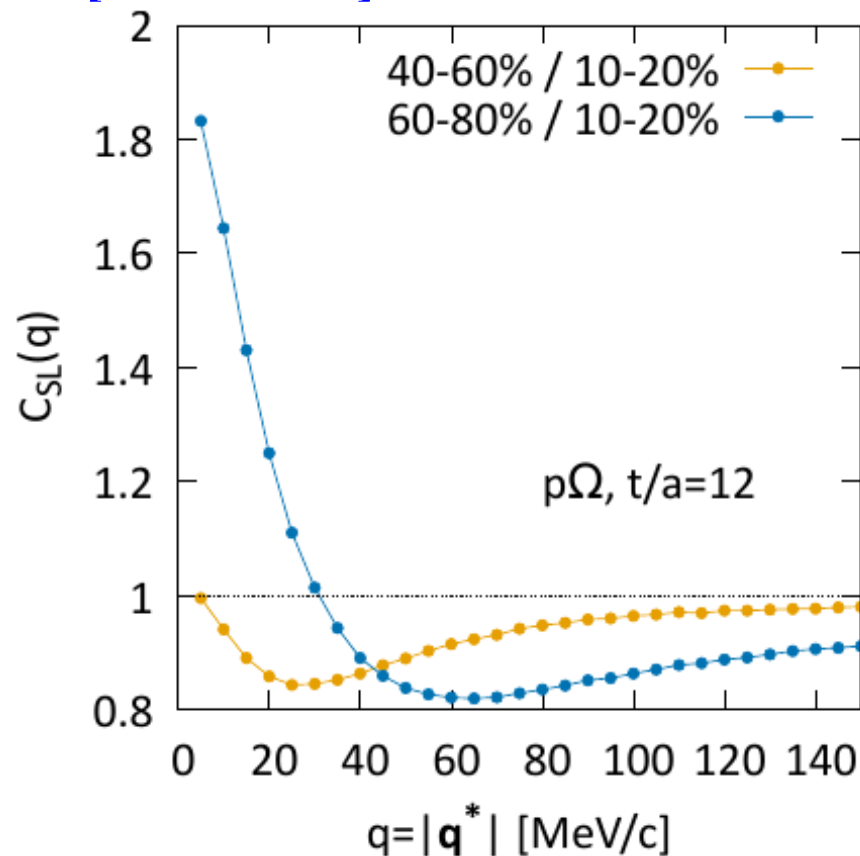
Morita+('20)

- Transport model result [should be realistic] → Future work

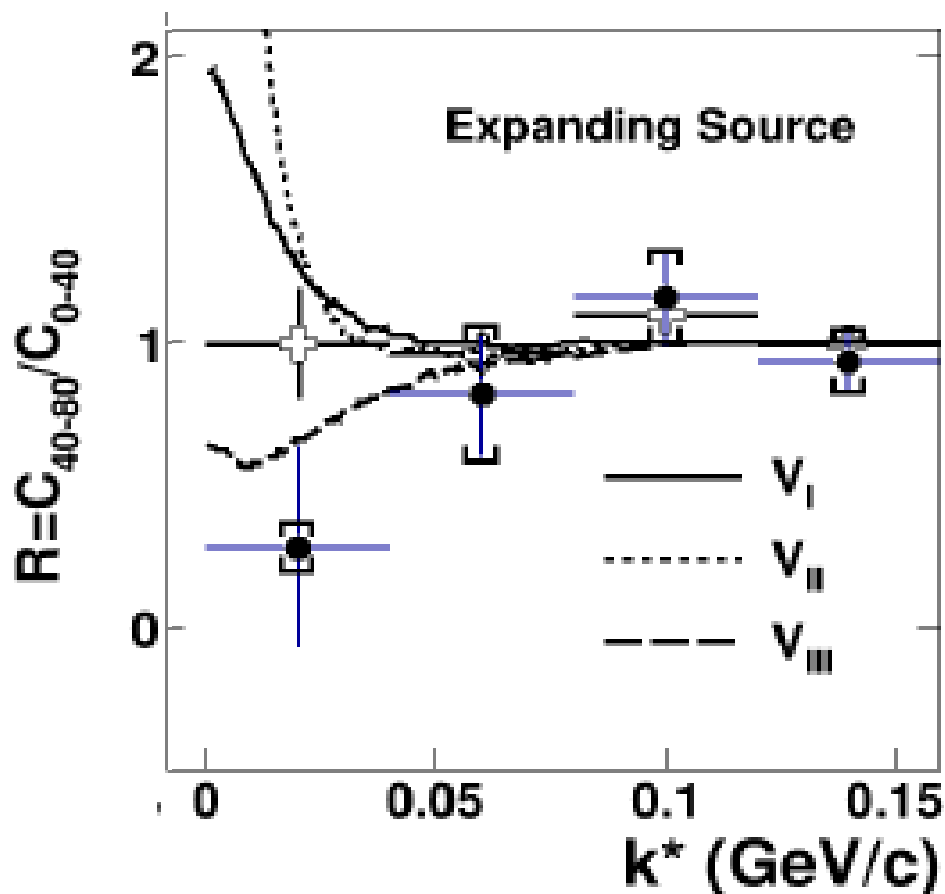
# Comparison with STAR data

- Results with potential at nearly physical quark mass (= between  $V_{II}$  and  $V_{III}$ )
- Dip is seen but is not deep enough to explain STAR data.

Morita, Gongyo, Hatsuda, Hyodo, Kamiya, AO, PRC101('20)015201 [1908.05414]



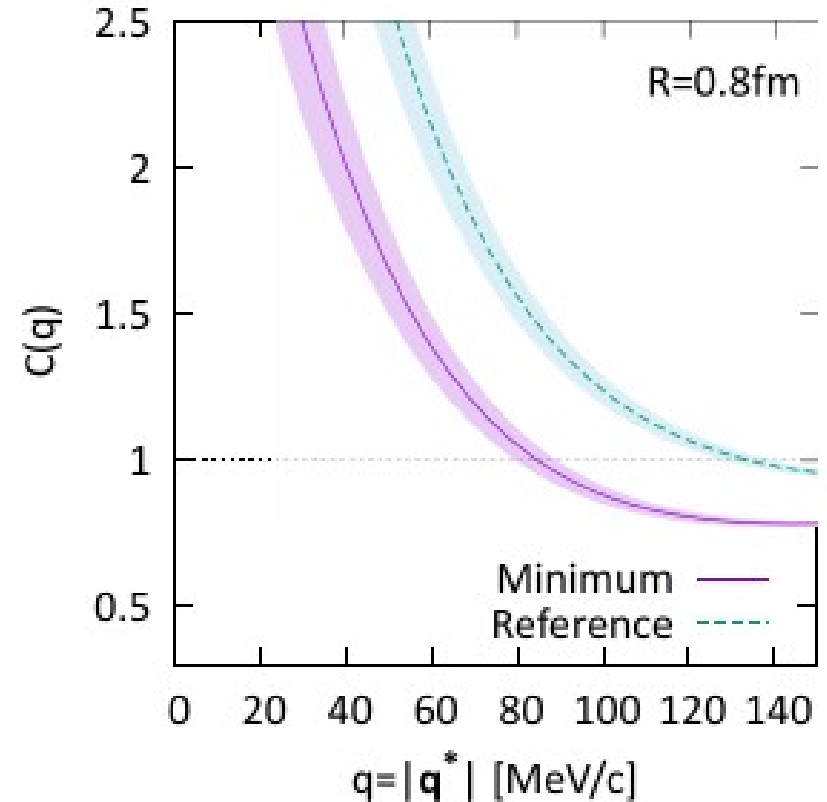
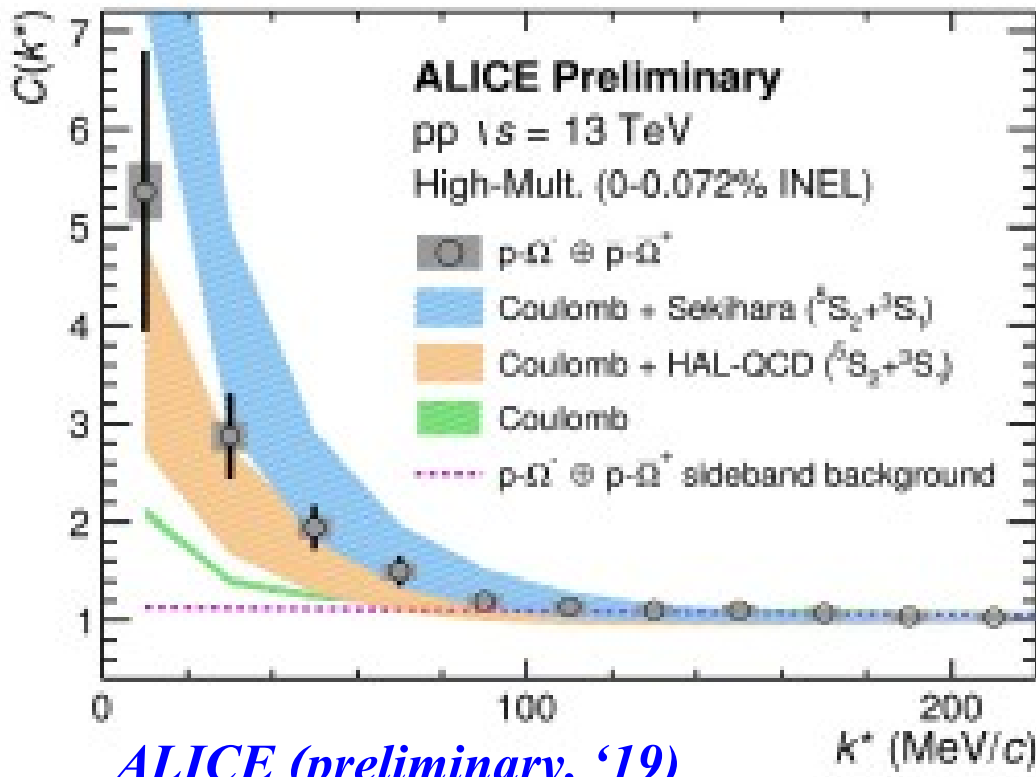
STAR (1808.02511, PLB790 ('19) 490)



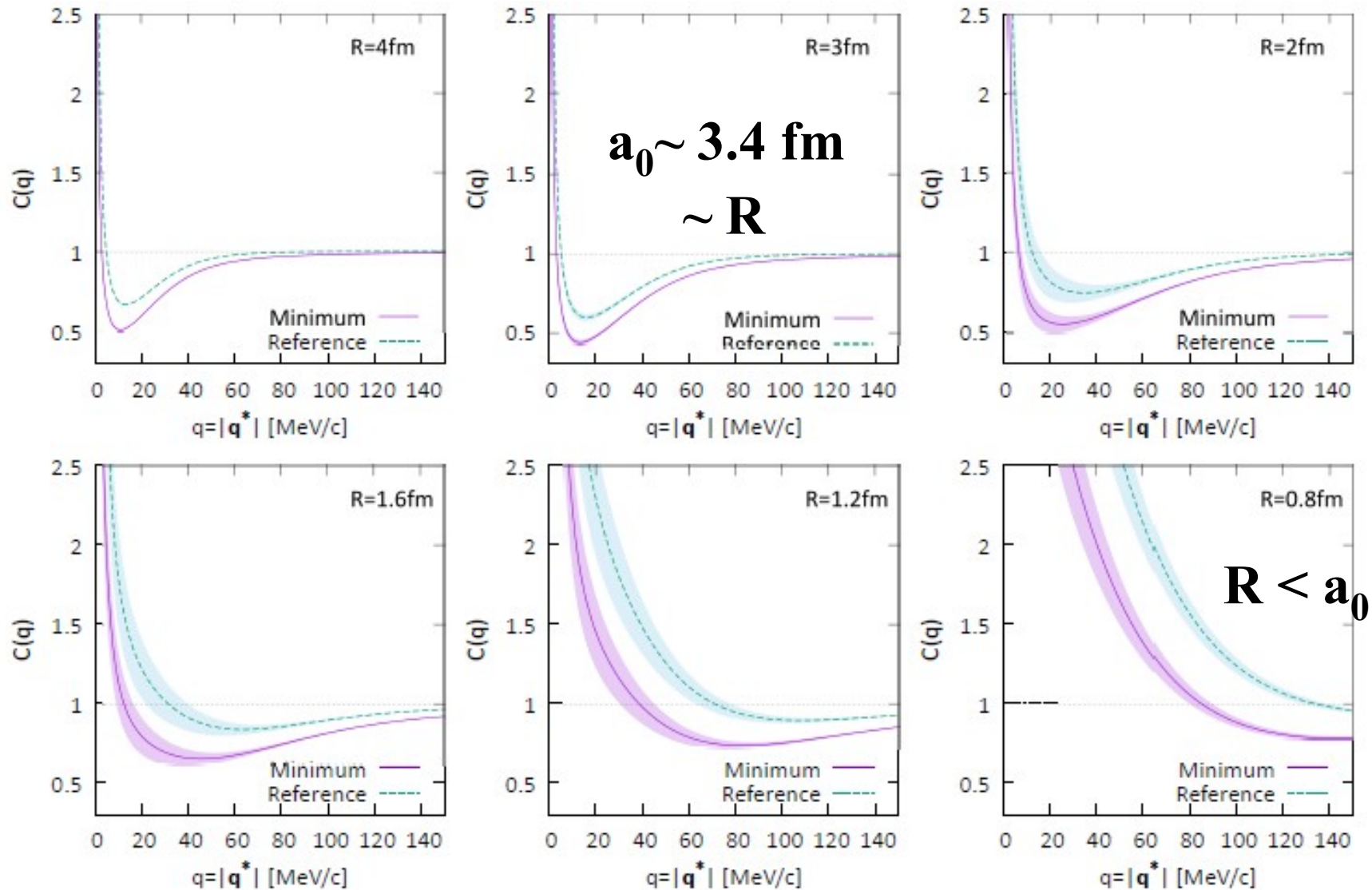


# ALICE Preliminary

- pp 13 TeV high-multiplicity events in ALICE  
→ Strong enhancement of CF at small  $q$   
*O. Vázquez Doce et al. (ALICE), Hadrons 2019*
- Lattice QCD potential roughly explains the data.



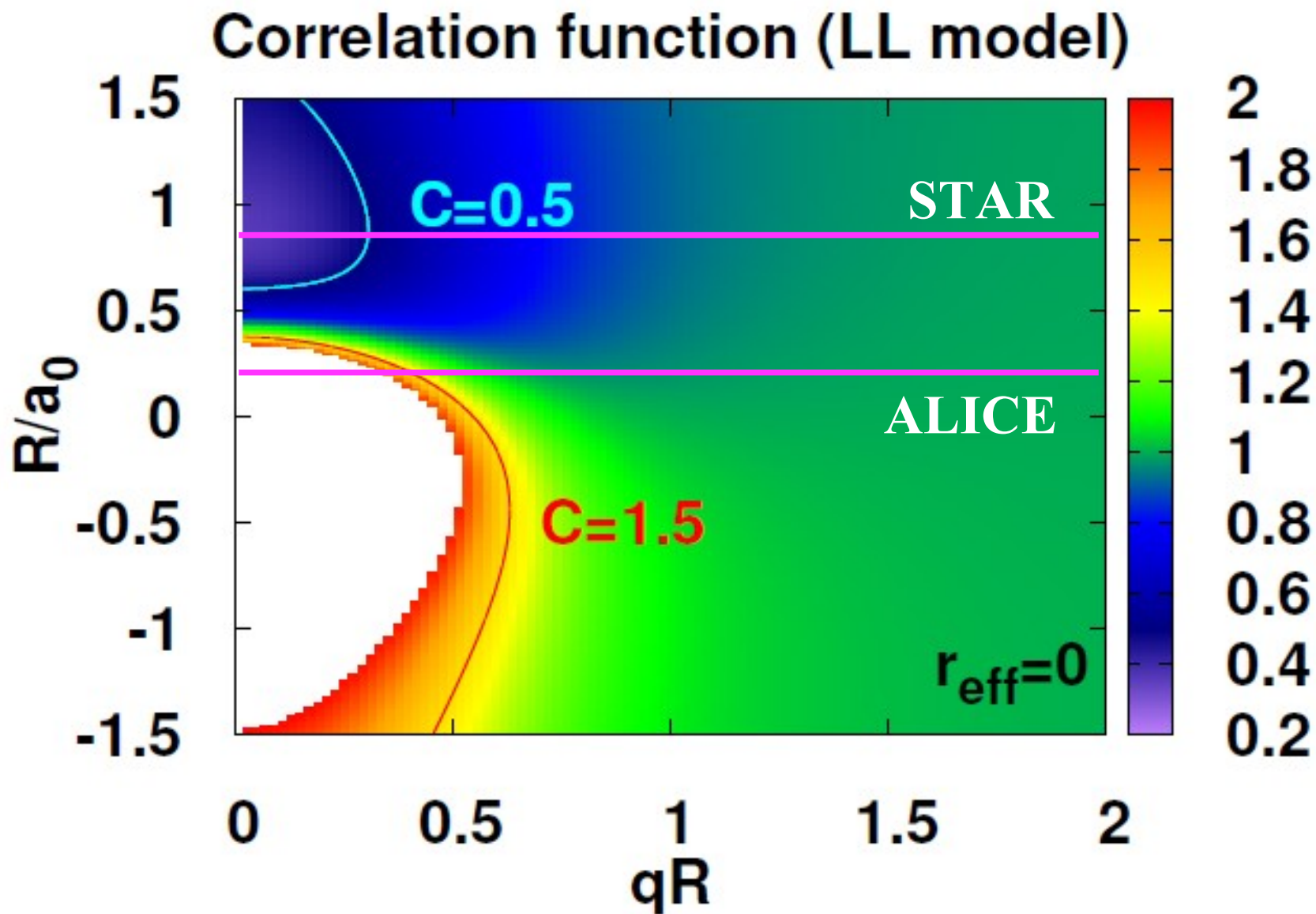
# Source Size Dependence of Correlation Function



Gaussian Source

*K. Morita, S. Gongyo, T. Hatsuda,  
T. Hyodo, Y. Kamiya, AO ('20)*

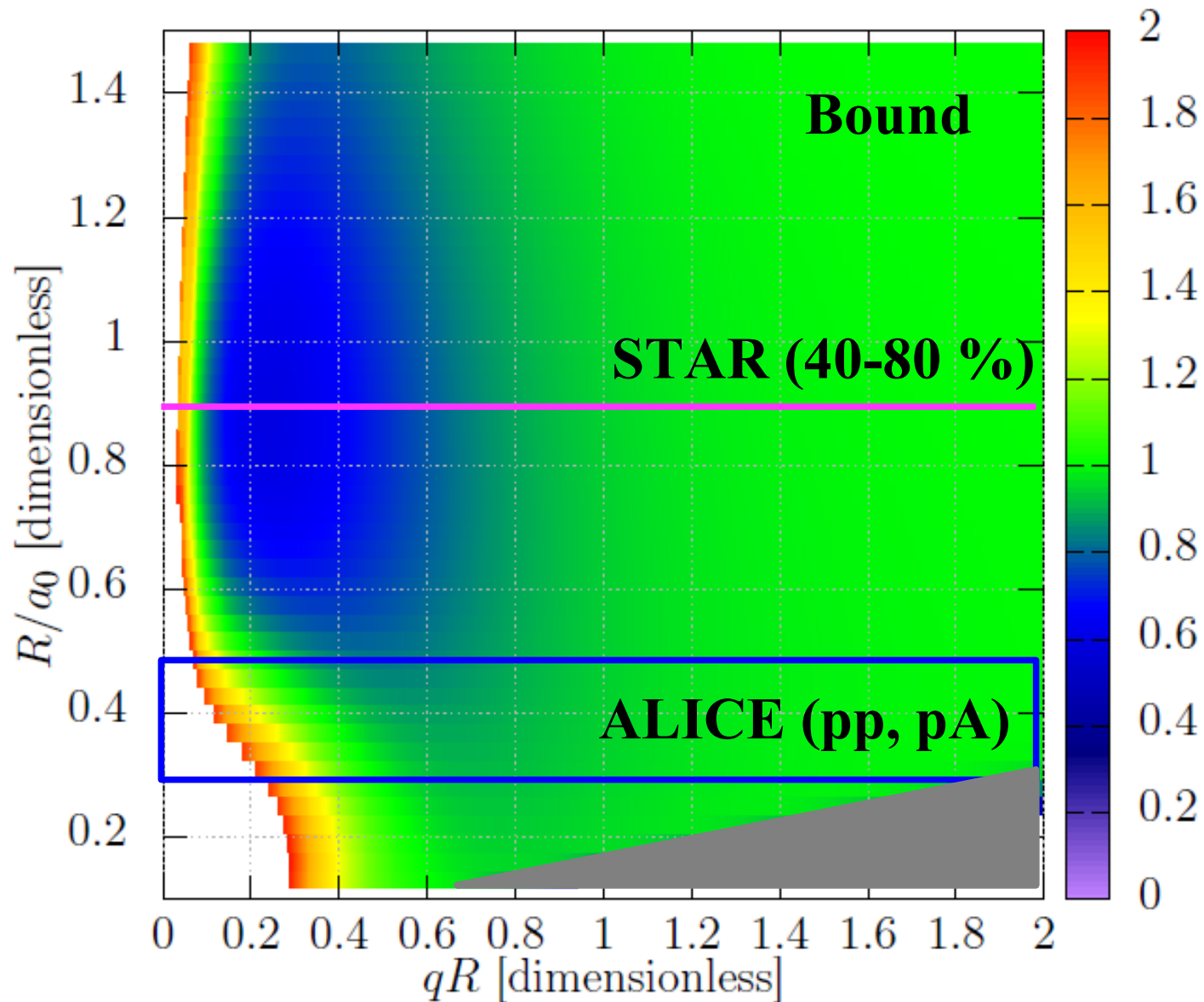
# Correlation Function in LL model



$a_0$  ( $p\Omega$ ) $\sim 3.4$  fm,  $R(\text{ALICE})\sim 0.7$  fm,  $R(\text{STAR})\sim 3$  fm

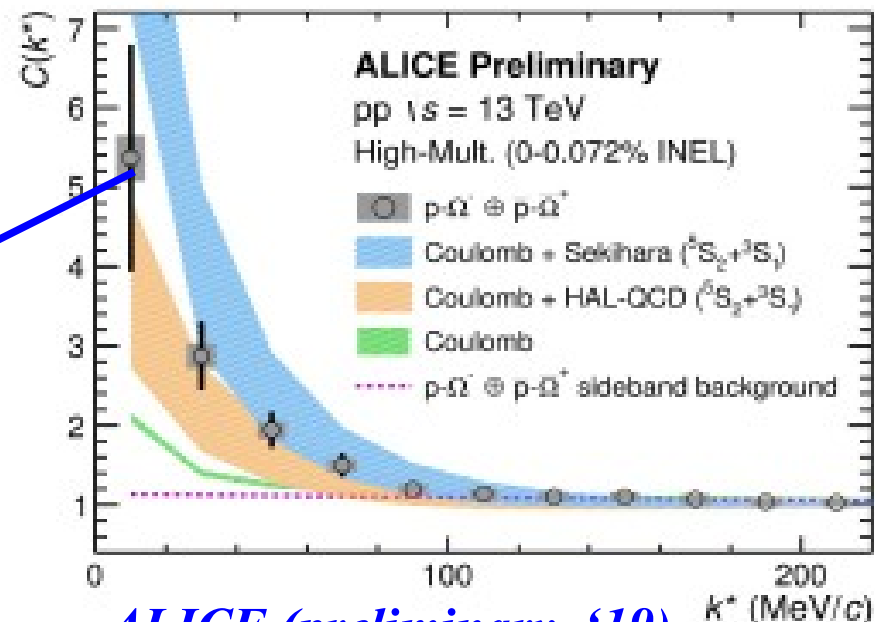
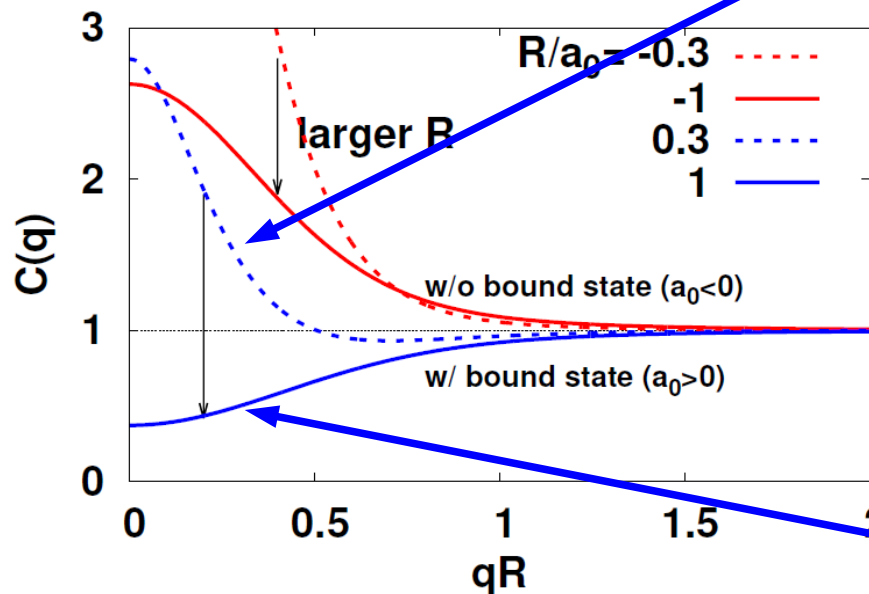


# Correlation Function with Gaussian source

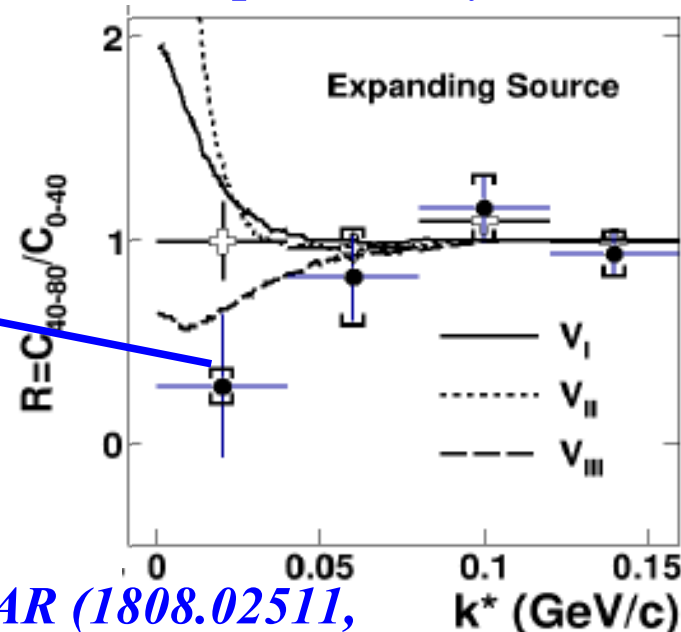


$N\Omega$  potential ( $J=2$ , HAL QCD,  $a_0=3.4$  fm) + Coulomb

# STAR + ALICE = $N\Omega$ Dibaryon



ALICE (preliminary, '19)



STAR (1808.02511, PLB790 ('19) 490)

# *STAR + ALICE = $N\Omega$ Dibaryon*

## ■ Theory

- Corr. Fn. is enhanced at any  $R$  for negative  $a_0$ . (w/o bound state)
- Corr. Fn. is enhanced at  $R < a_0$  and *suppressed* at  $R \sim a_0$  for positive  $a_0$ . (w/ bound state or repulsive int.)
- With repulsive int.,  $a_0 \sim r_c$  (hard core radius), and cannot be large, and coupled channels effects generally enhances corr. fn.

## ■ Experiment

- $p\Omega$  corr. fn. is *suppressed* at small  $q$  in HIC at RHIC.
- $p\Omega$  corr. fn. is strongly enhanced in high mult. pp events at LHC.

*There should be (a) bound state(s) in  $p\Omega$ , whose scatt. length is around the source size of HIC. Any other possibility ?*

---

# *$K^- p$ correlation*

# $K^- p$ interaction

- $\Lambda(1405)$   $\bar{K}N$  quasi-bound state

*Dalitz, Tuan ('60); Koch ('94); Kaiser, Siegel, Weise ('95); AO, Nara, Koch ('97); Jido+('03)*

- Positive scattering length in  $K^-$  atoms

*M.Iwasaki et al. PRL78('97)3067;  
M.Bazzi et al. [SIDDHARTA Collab.],  
PLB704('11)113.*

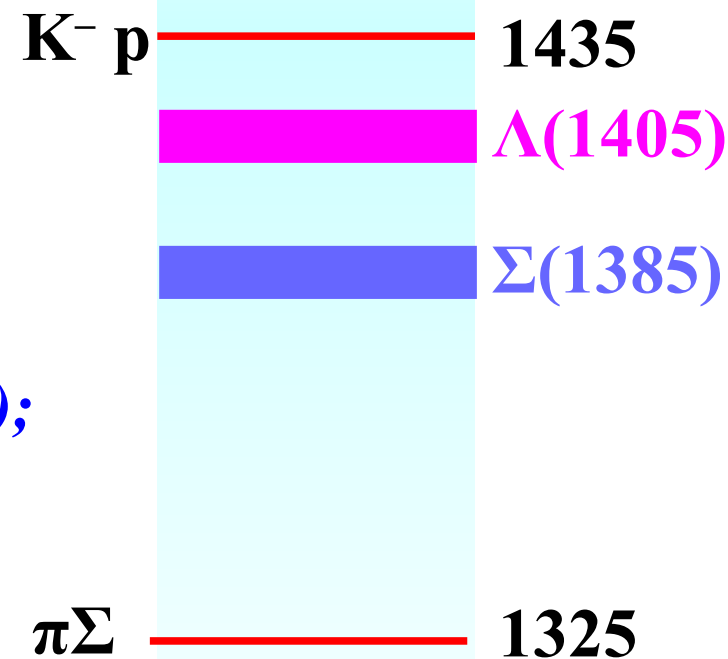
- Kaonic nuclei ?

*Nogami ('63); Akaishi, Yamazaki ('02);  
Shevchenko, Gal, Mares ('07); Ikeda, Sato ('07);  
Dote, Hyodo, Weise ('09)*

→ Needs precise info. on  $\bar{K}N$  int.

- Scattering amplitude and Potential fitting scattering and SIDDARTA data in chiral approach

*Ikeda, Hyodo, Weise ('11,'12),  
Miyahara, Hyodo ('16)*



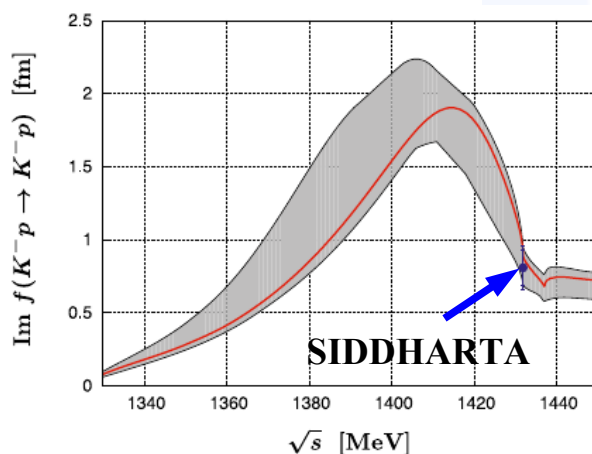
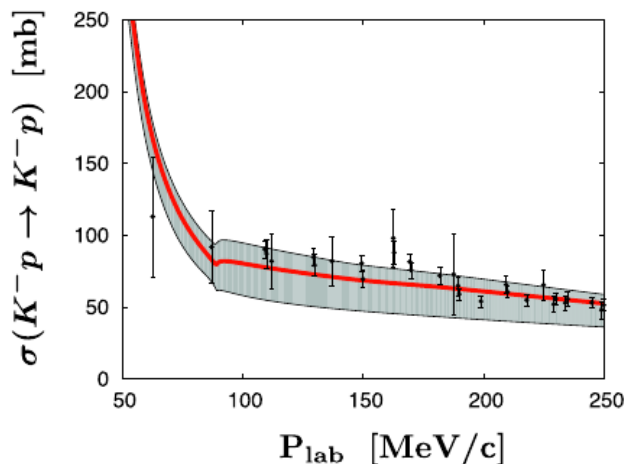
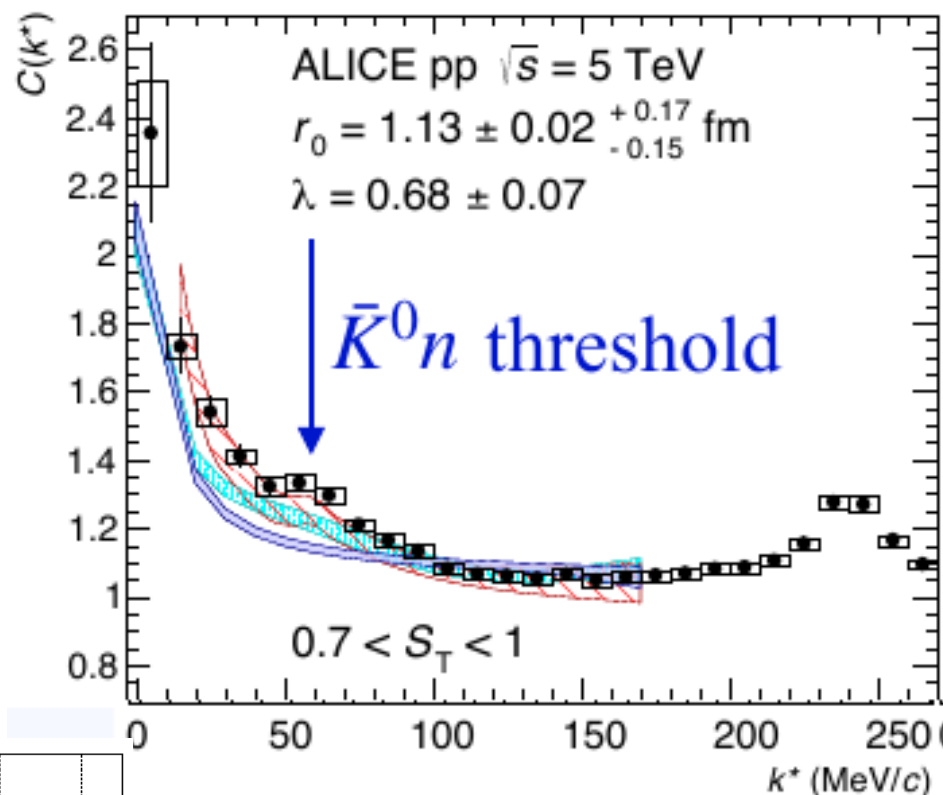
*How about  $K^- p$  correlation ?*

# $K^-p$ correlation function data

## ■ $K^-p$ correlation function from high-multiplicity events of pp collisions

*S. Acharya et al. (ALICE), arXiv:1905.13470*

- High precision data from low to high momentum ! c.f. Previous scatt. data & Kaonic atom data.
- Enhanced at low  $k$ , cusp,  $\Lambda(1520)$ , ...



Red: Kyoto model  
 Blue: Julich model  
 grey: Coulomb

*Y. Ikeda, T. Hyodo, W. Weise, NPA881 ('12) 98*

# $\bar{K}N-\pi\Sigma-\pi\Lambda$ Scattering Amplitude and Potential

## ■ Amplitude in chiral SU(3) coupled-channels dynamics

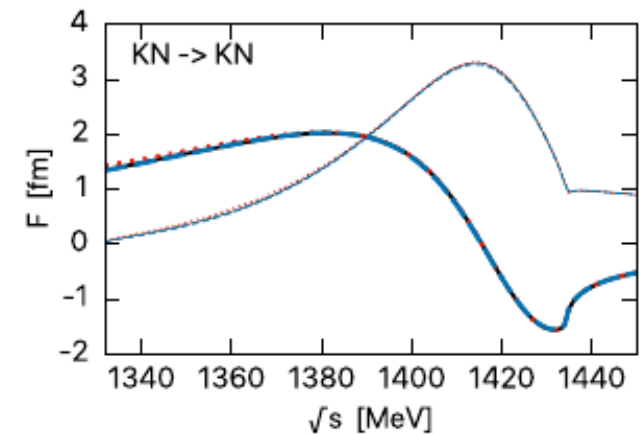
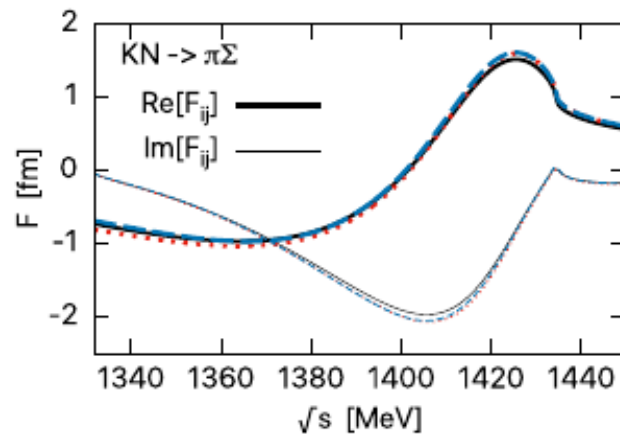
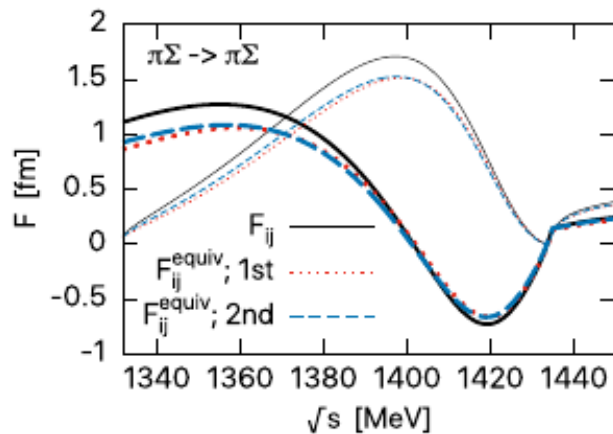
*Y. Ikeda, T. Hyodo, W. Weise, NPA881 ('12) 98*

- NLO meson-baryon effective Lagrangian ( $\bar{K}N-\pi\Sigma-\pi\Lambda$ )  
+ fit of Kaonic Hydrogen, Cross Section, Threshold branching ratio

## ■ Coupled-channels potential

*K. Miyahara, T. Hyodo, W. Weise, PRC98('18)025201*

- Potential fitted to IHW amplitude



*Y. Ikeda, T. Hyodo, W. Weise, NPA881 ('12) 98*

*K. Miyahara, T. Hyodo, W. Weise, PRC98('18)025201*

# Correlation Function with Coupled-Channels Effects

*J. Haidenbauer, NPA 981('19)1; R. Lednicky, V. V. Lyuboshits, V. L. Lyuboshits, Phys. At. Nucl. 61('98)2950.*

## ■ Single channel, w/o Coulomb (non-identical pair)

$$C(\mathbf{q}) = \underline{1} + \int d\mathbf{r} S(\mathbf{r}) \left[ \underline{|\chi^{(-)}(r, q)|^2} - \underline{|j_0(qr)|^2} \right]$$

## ■ Single channel, w/ Coulomb

$$C(\mathbf{q}) = \int d\mathbf{r} S(\mathbf{r}) \left[ \underline{|\varphi^{C,\text{full}}(\mathbf{q}, \mathbf{r})|^2} + \underline{|\chi^{C,(-)}(r, q)|^2} - \underline{|j_0^C(qr)|^2} \right]$$

**Full free**

**Coulomb w.f.**

**s-wave w.f.**

**with Coul.**

**s-wave**

**Coul. w.f.**

## ■ Coupled channel, w/ Coulomb

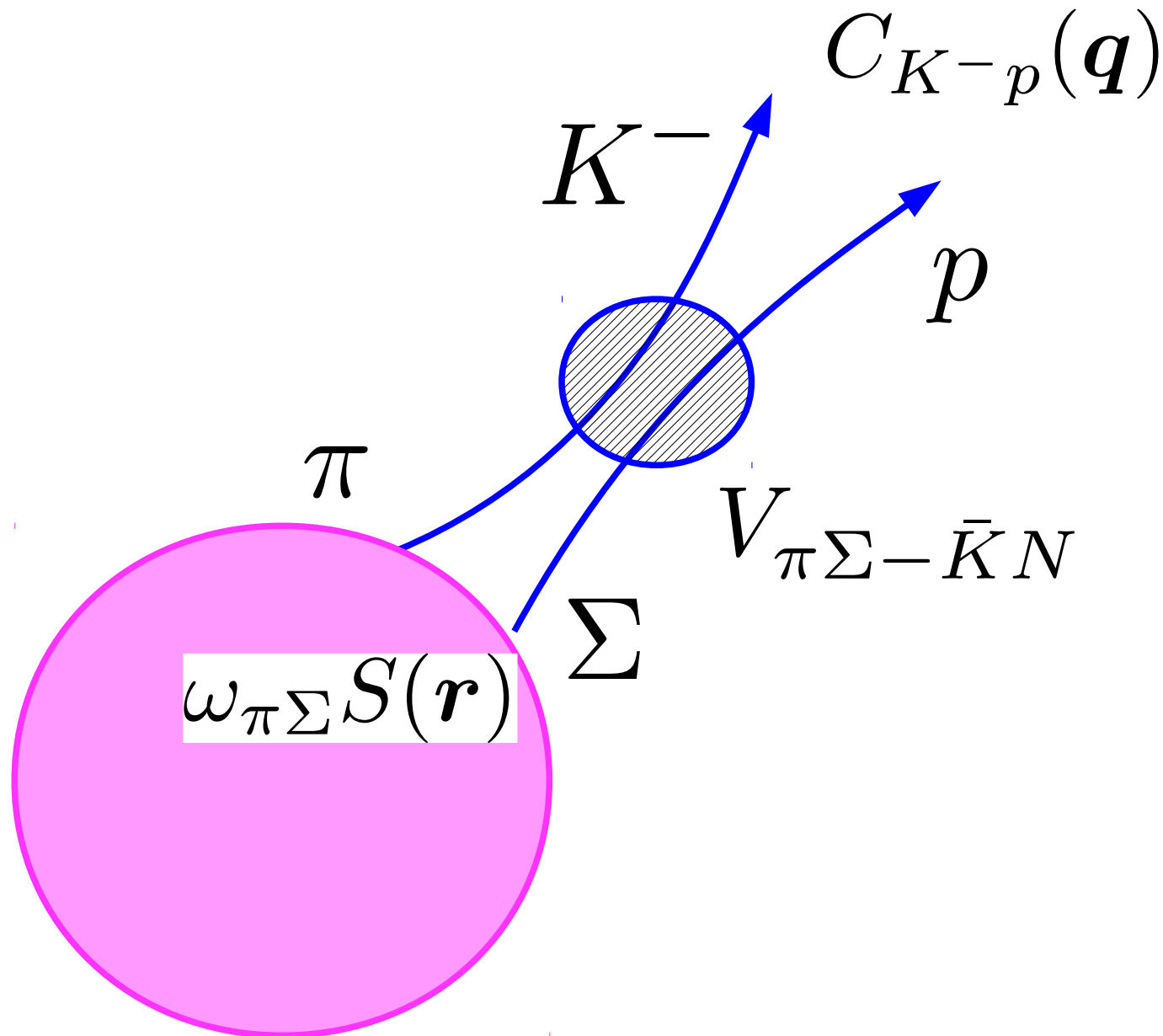
$$C_i(\mathbf{q}) = \int d\mathbf{r} S_i(\mathbf{r}) \left[ \underline{|\varphi^{C,\text{full}}(\mathbf{q}, \mathbf{r})|^2} + \underline{|\chi_i^{C,(-)}(r, q)|^2} - \underline{|j_0^C(qr)|^2} \right]$$

$$+ \sum_{j \neq i} \omega_j \int d\mathbf{r} S_j(\mathbf{r}) \underline{|\chi_j^{C,(-)}(r, q)|^2} \quad \text{s-wave w.f. in j-th channel}$$

**Outgoing B.C. in the i-th channel,  $\omega_j = \text{Source weight } (\omega_j=1)$**



# Correlation Function with Coupled-Channels Effects



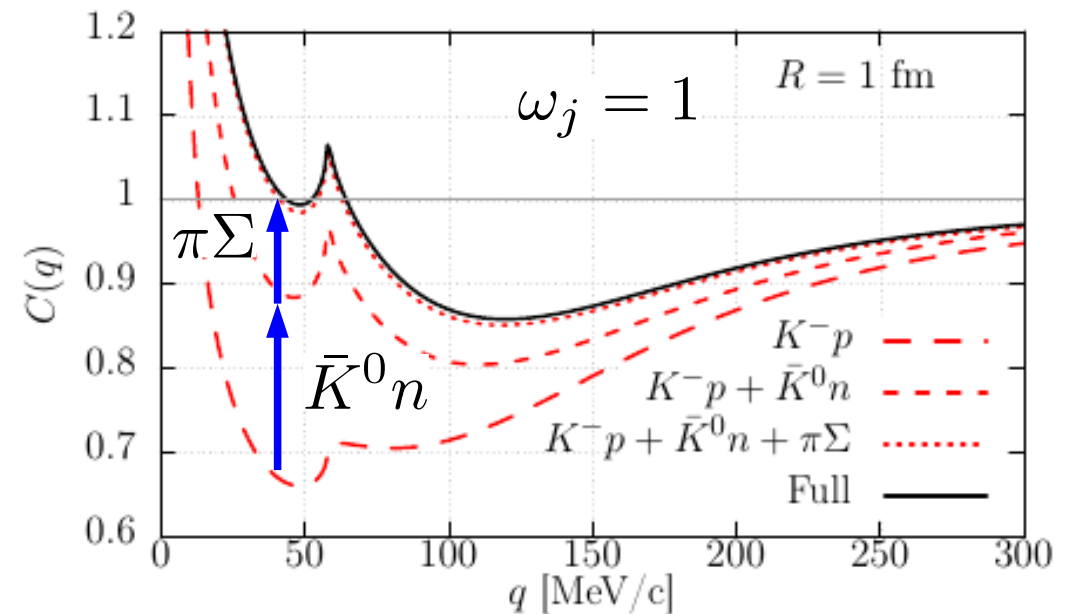
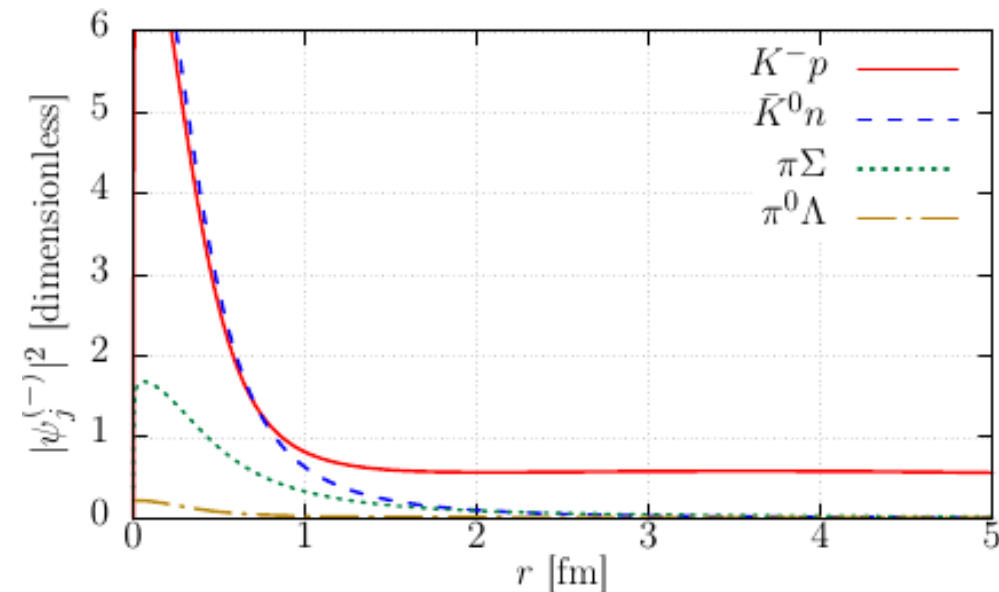
# Correlation Function from Chiral SU(3) Potential (1)

- **Corr. Fn. from Chiral SU(3) coupled-channels potential + Coulomb + threshold difference (for the first time !)**

*Y. Kamiya, T. Hyodo, K. Morita, AO, W. Weise, arXiv:1911.01041*

- **Coupled-channels effect**

- **W.f. of other channels than  $K^- p$  decay in  $r < 1$  fm.**
- **But they contribute to corr. fn. meaningfully.**



# Correlation Function from Chiral SU(3) Potential (2)

- “Free” parameters

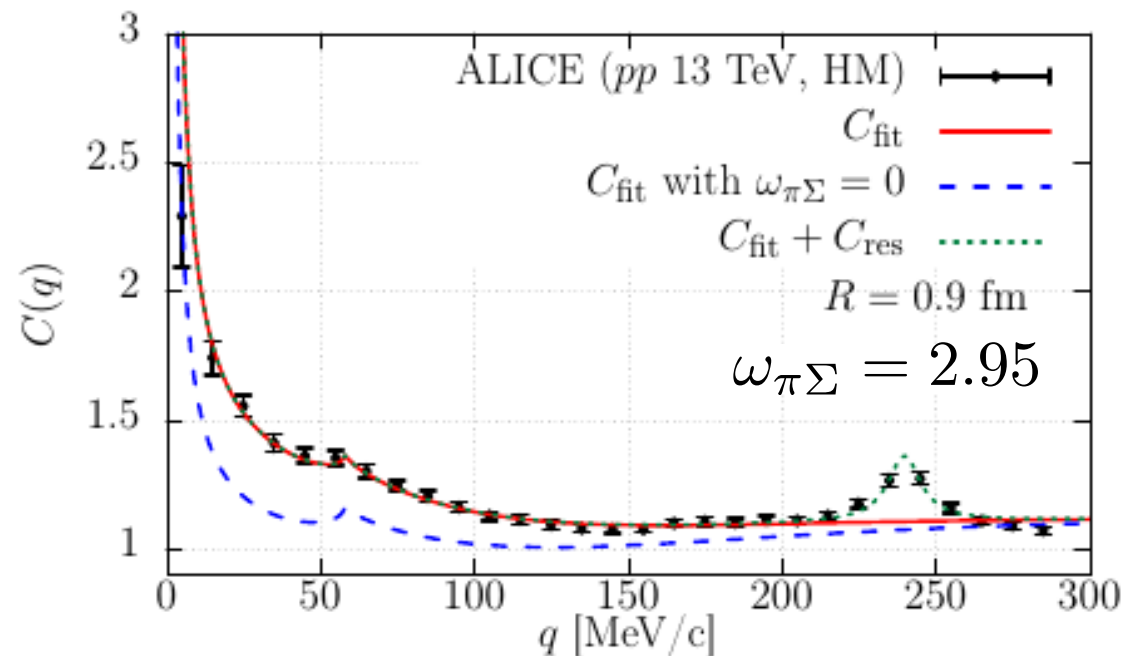
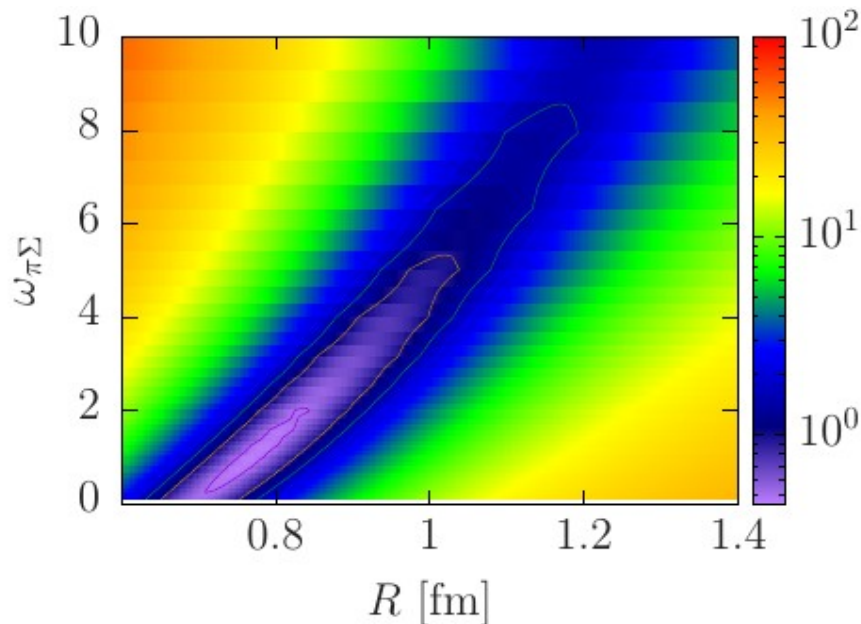
= Source Size  $R$ , Source Weight  $\omega_j$  ← Th+Exp.

+ Normalization + Pair purity ( $\lambda$ ) ← Exp.

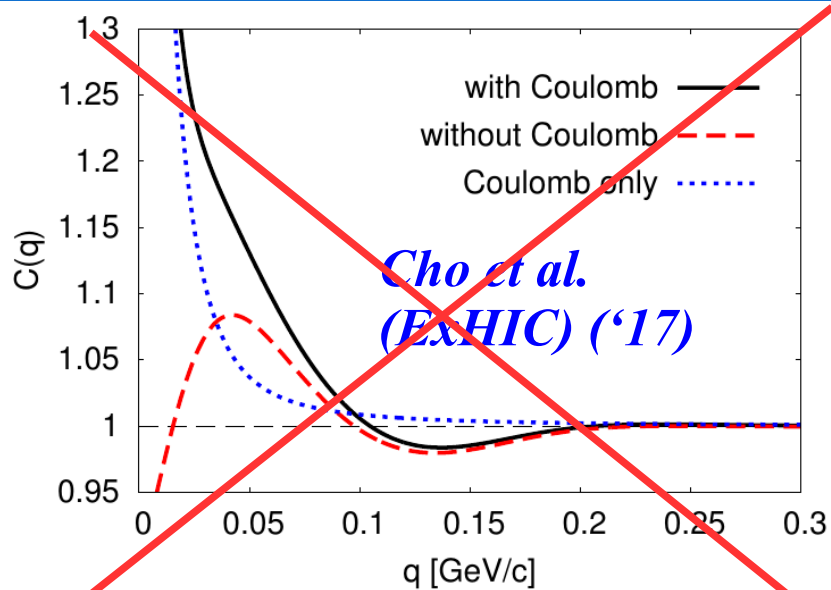
- Larger  $R \rightarrow$  Smaller couple-channels effect from  $\pi\Sigma$  (Favorable values of  $R$  and  $\omega_j$  are correlated)

- Simple statistical model estimate

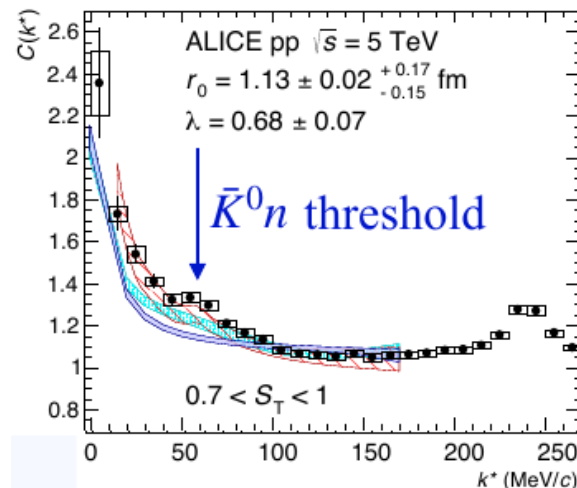
$$\omega_{\pi\Sigma} \sim \exp[(m_K + m_N - m_\pi - m_\Sigma)/T] \sim 2.$$



# Comparison with other estimates

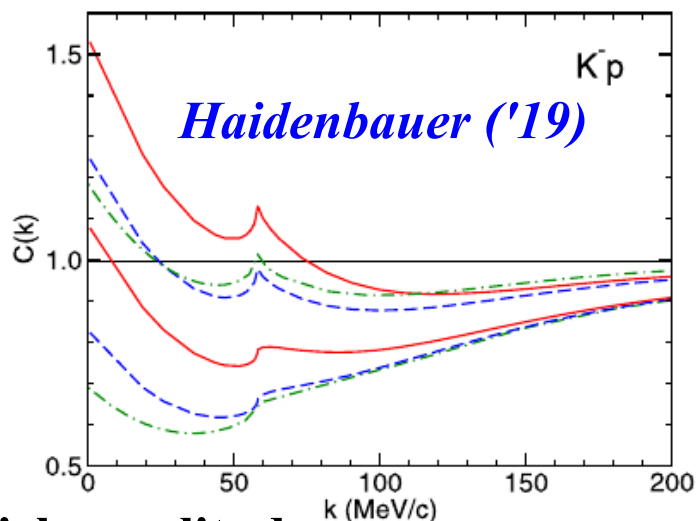


**Cho et al.  
(ExHIC) ('17)**  
No  $\bar{K}^0n, \pi\Sigma$  source  
No threshold diff.



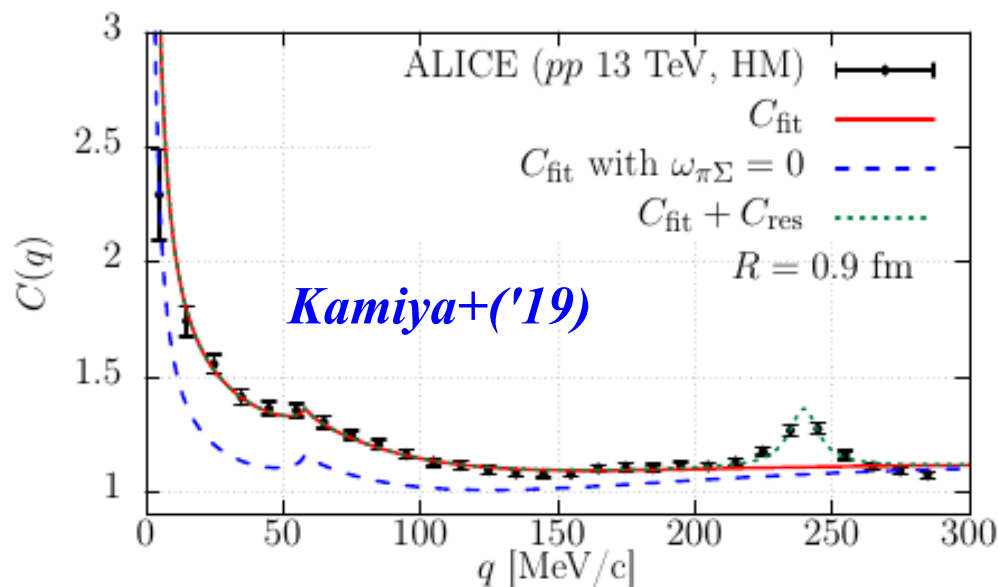
**ALICE**

**Kyoto model (~Cho+('17)) → accident  
Julich model (Blue) Gamow corr. for Coulomb**



**Haidenbauer ('19)**

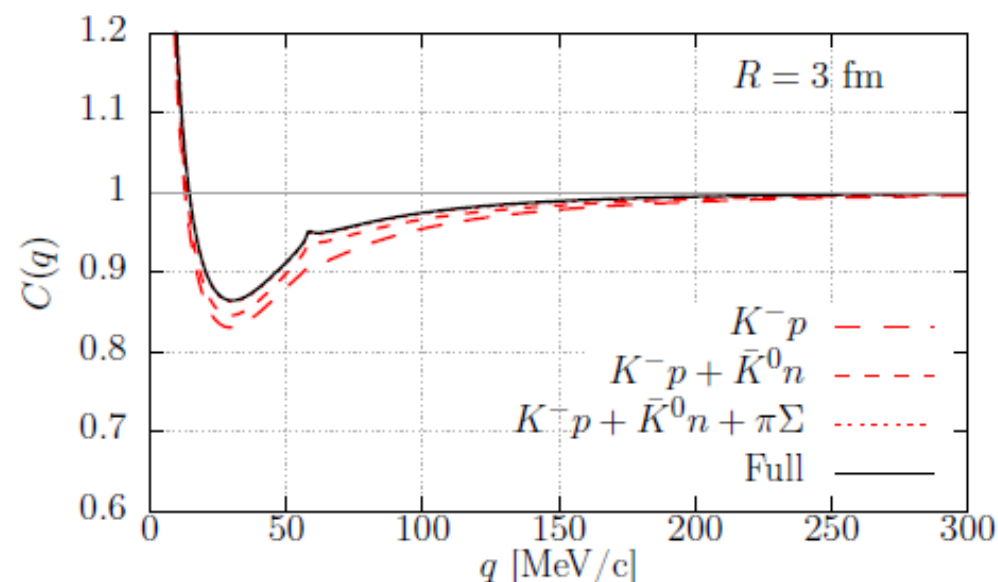
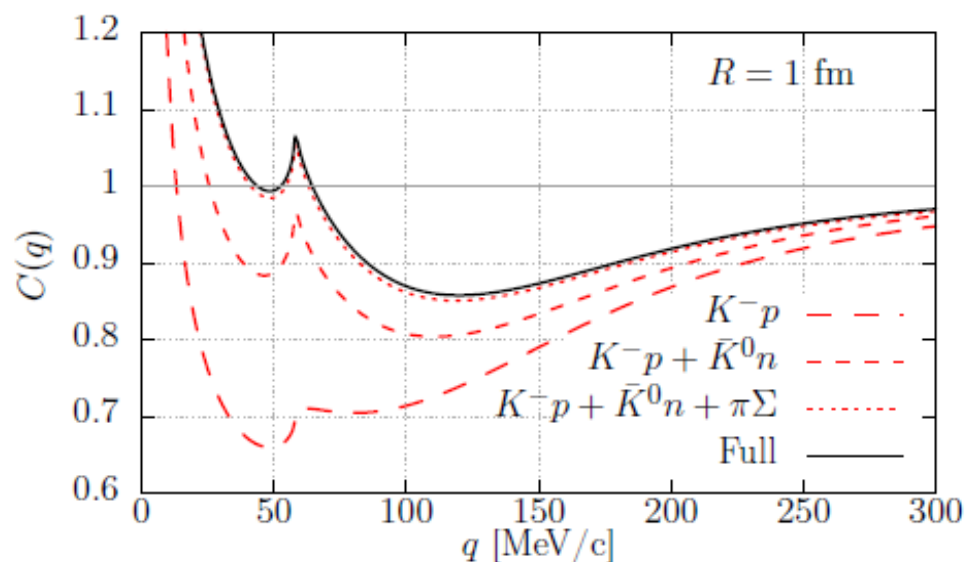
**Julich amplitude  
Consistent with Kamiya+('19) w/o Coulomb**



**Kamiya+('19)**

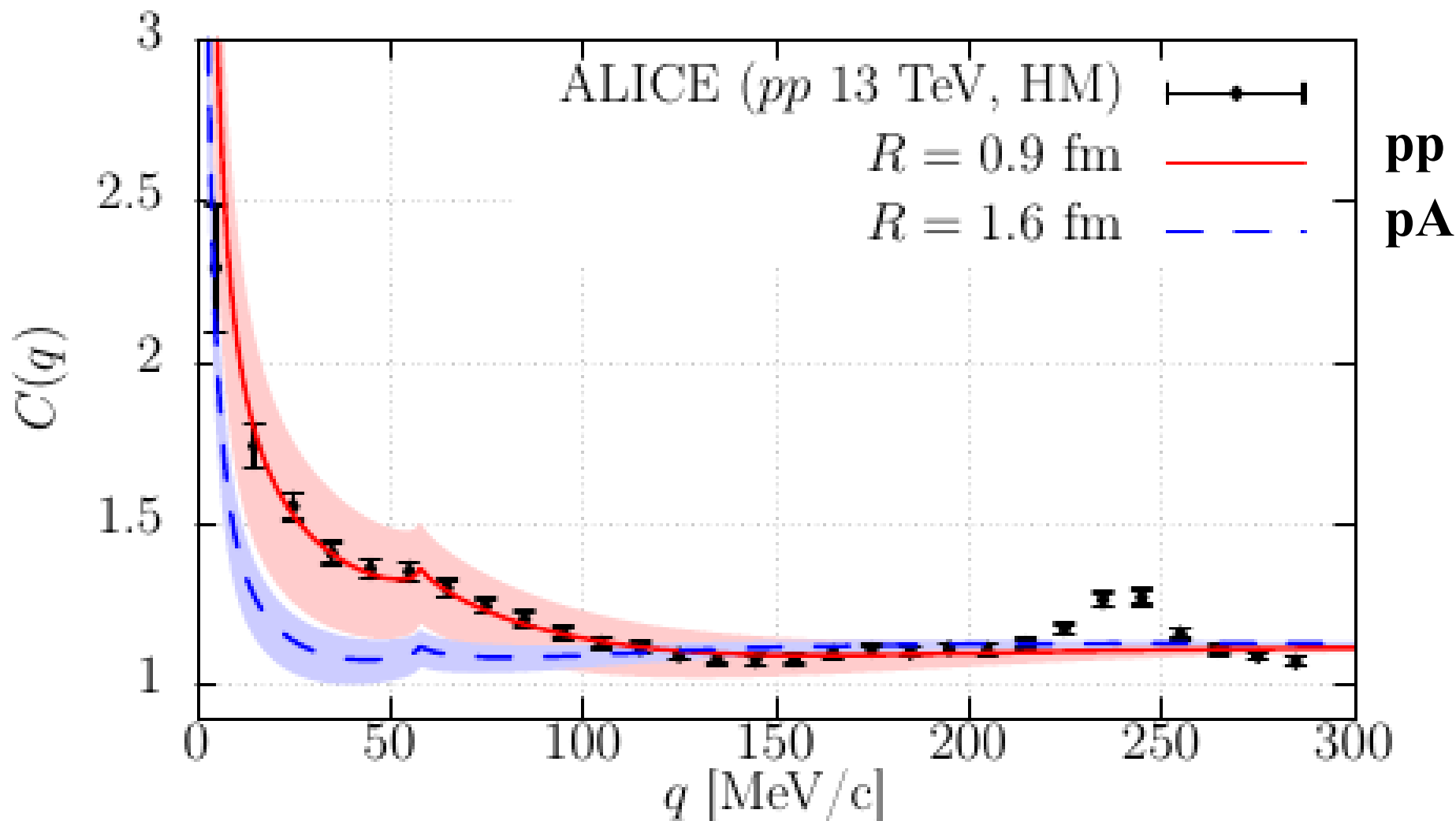
## Source Size Dependence (2)

- Experimental confirmation of coupled-channels contribution  
→ Source size dependence
  - Channel w.f. other than  $K^-p$  are localized at around  $r=0$ .  
(Outgoing boundary condition for  $K^-p$ )
  - Contribution of  $\pi\Sigma$  source is suppressed for larger  $R$ .



## Source Size Dependence (2)

- Corr. Fn. from pA & AA collisions will elucidate the role of  $\pi\Sigma$ 
  - $R \sim 1.6$  fm  $\rightarrow$   $\pi\Sigma$  effects are suppressed.



# Summary

- High-energy nuclear collisions can be utilized as a hadron factory.
- Two-hadron correlation functions are useful to get knowledge of hadron-hadron interaction.  
E.g. Large corr. fn. at small  $q$  implies large  $|a_0|/R$ , and the source size dependence may show the sign of  $a_0$ , to be or not to be bound.
- Measured corr. fn. tell us many things !
  - ALICE and STAR data strongly suggest the existence of  $S=-3$  dibaryon as a bound state of  $N\Omega$ .
  - ALICE data are consistent with chiral  $SU(3)$   $\bar{K}N-\pi\Sigma-\pi\Lambda$  amplitudes.
  - STAR and ALICE data confirm weakly attractive  $\Lambda\Lambda$  int.
  - ALICE data of  $\Xi^- p$  implies large  $|a_0|/R$ , and the existence of some kind of pole (b.s., res., virtual) around the threshold.

# Future works and challenges

## ■ To do

- $\Xi^-$  p corr. fn. with updated HAL QCD potential  
*K. Sasaki et al. (HAL QCD), arXiv:1912.08630*
- Corr. Fn. of  $S=-1$  BB pair, especially  $\Sigma^0$  p,  
using Lattice QCD BB potential.  
*S. Acharya et al. (ALICE), arXiv:1910.14407*
- $\pi\Sigma$  corr. fn. ( $\pi\Sigma$  interaction is not constrained !)
- $\pi^\pm Y$ ,  $K^\pm Y$  ( $Y=\Lambda, \Xi^-, \Omega^-$ ) will be measurable. Interesting physics ?

## ■ Challenges

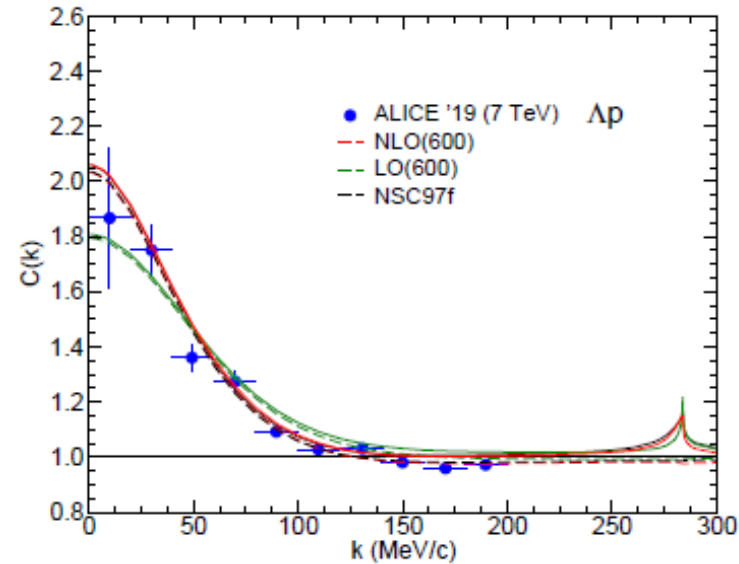
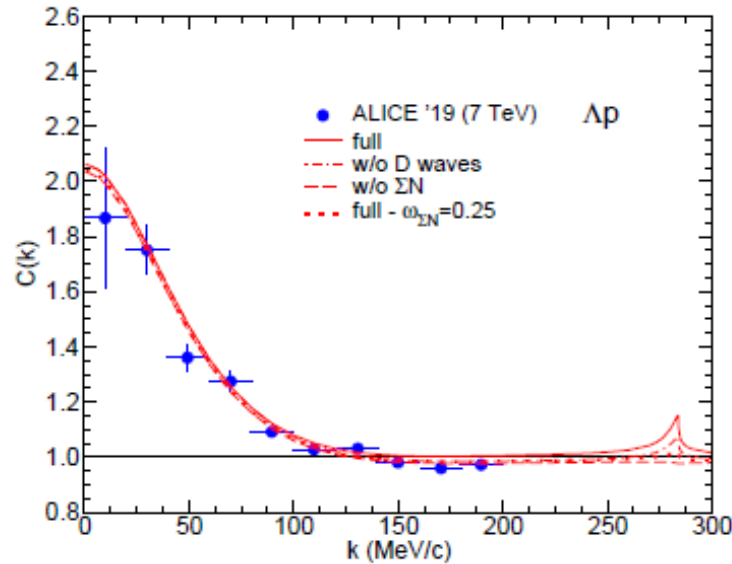
- $\Omega\Omega$  (experimentally challenging)
- Deuteron:  $K^- d$  ( $T=1$  ampl.),  $\Lambda d$  ( $3\Lambda H$  lifetime,  $\Lambda NN$  3BF),  
 $\Xi^- d$  (already measured (analyzed) ?), ...  
→ Break up effects of deuteron via CDCC would be helpful  
(Ogata, ...)



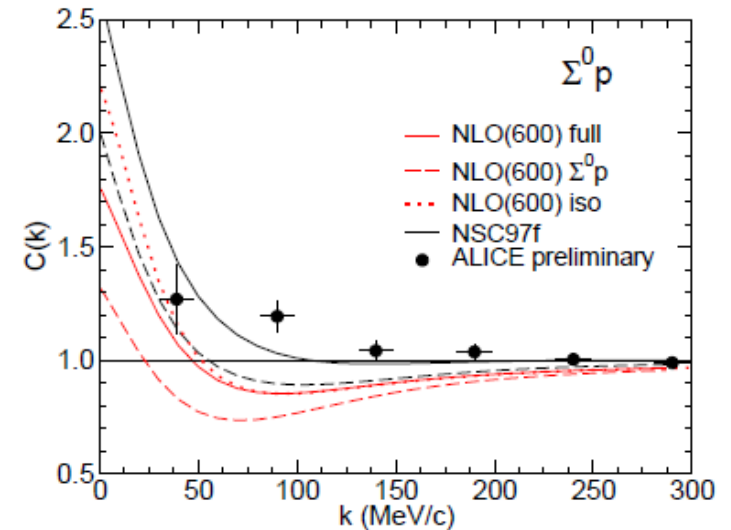
# Correlation Function Studies by Jülich Group

## ■ $\Lambda p$ correlation (chiral EFT, NLO)

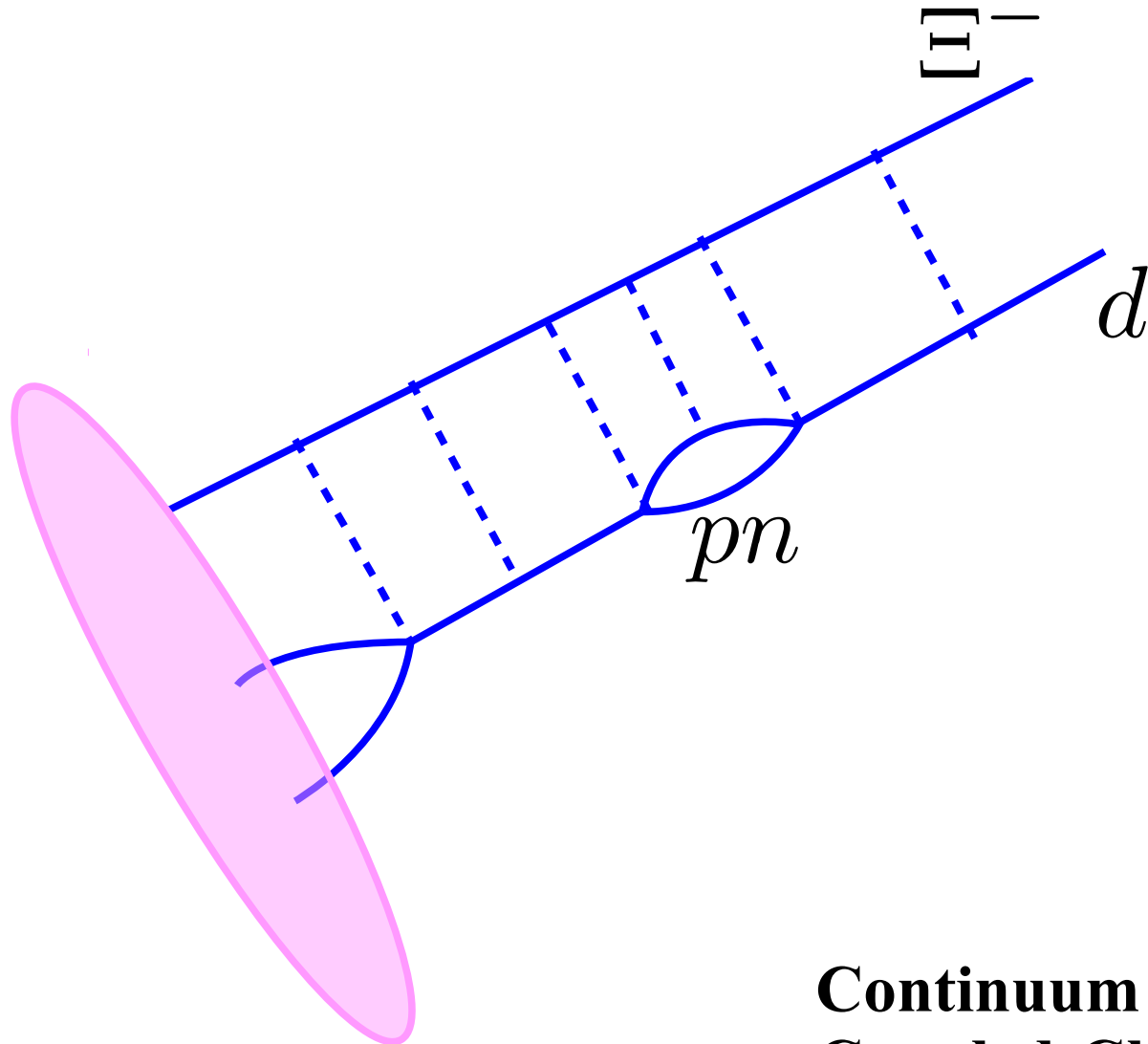
*J. Haidenbauer, FemTUM2019*



## ■ $\Sigma^0 p$ correlation



# Break up effect of deuteron



$$S_{\Xi pn}(r, r_{pn})$$

**Continuum Discretized  
Coupled-Channel (CDCC)  
would work**

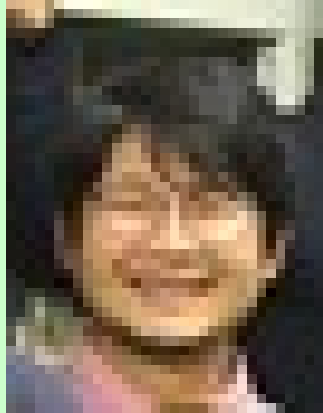
# Thank you for attention !

## Coauthors of arXiv:1908.05414

**K. Morita**



**S. Gongyo**



**T. Hatsuda**

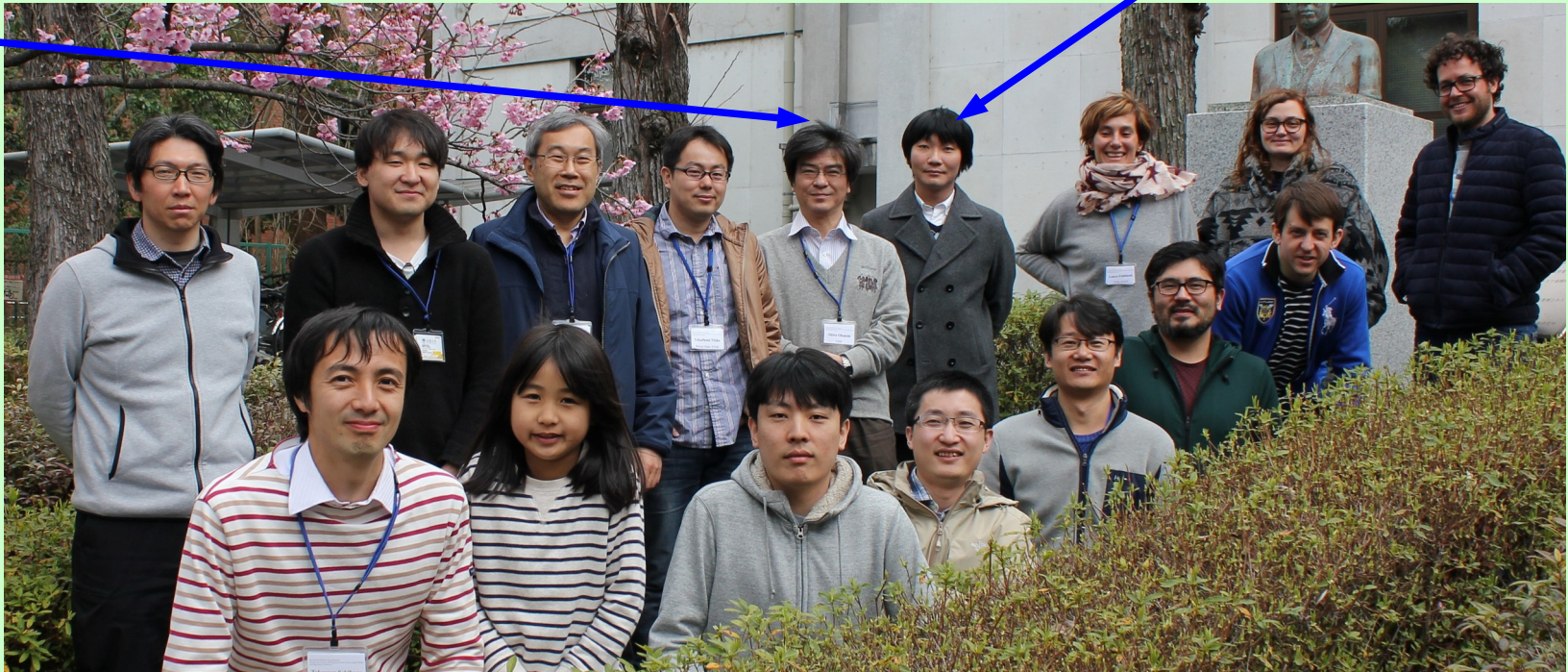


**T. Hyodo**



**Y. Kamiya**

**AO**



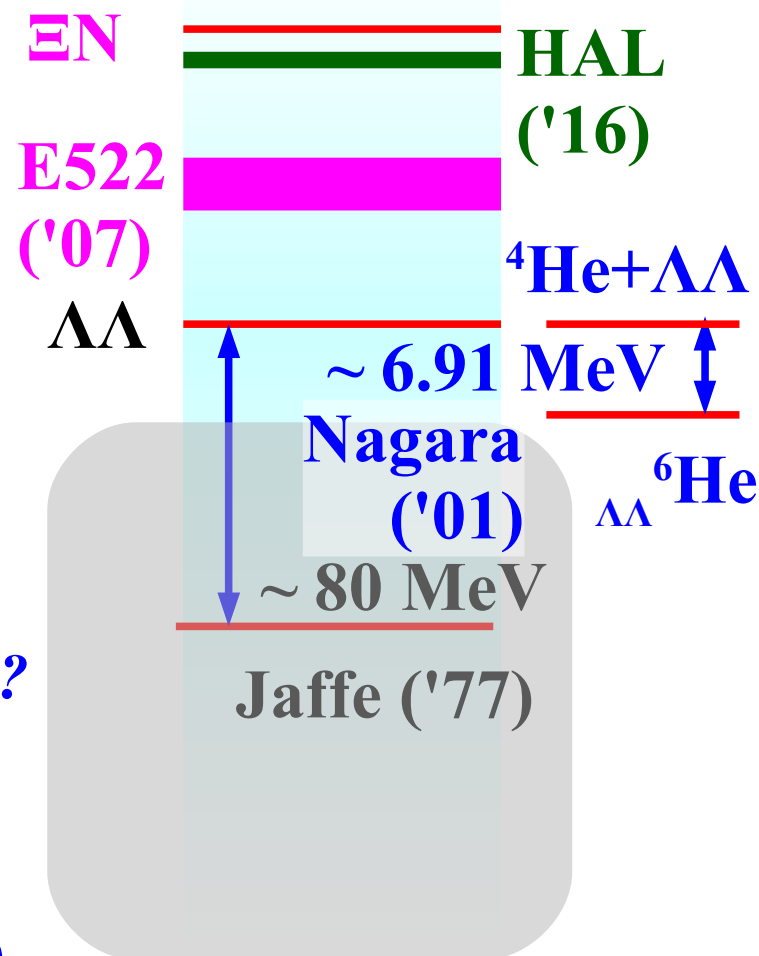
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*Do I have time ?*

# Relevance of $\Lambda\Lambda$ interaction to physics

## ■ H-particle: 6-quark state (uuddss)

- Prediction: *R.L.Jaffe, PRL38(1977)195*
- Ruled-out by double  $\Lambda$  hypernucleus  
*Takahashi et al., PRL87('01) 212502*
- Resonance or Bound “H” ?  
*Yoon et al.(KEK-E522)+AO ('07)*
- Lattice QCD  
*HAL QCD & NPLQCD ('11)*  
*HAL QCD ('16): H as a loosely bound EN ?*



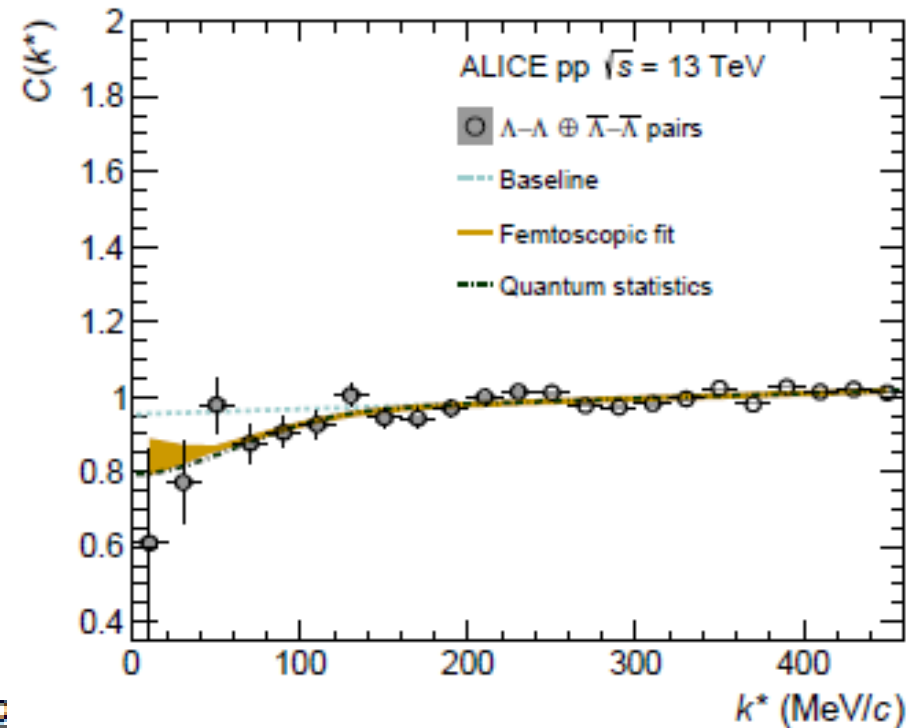
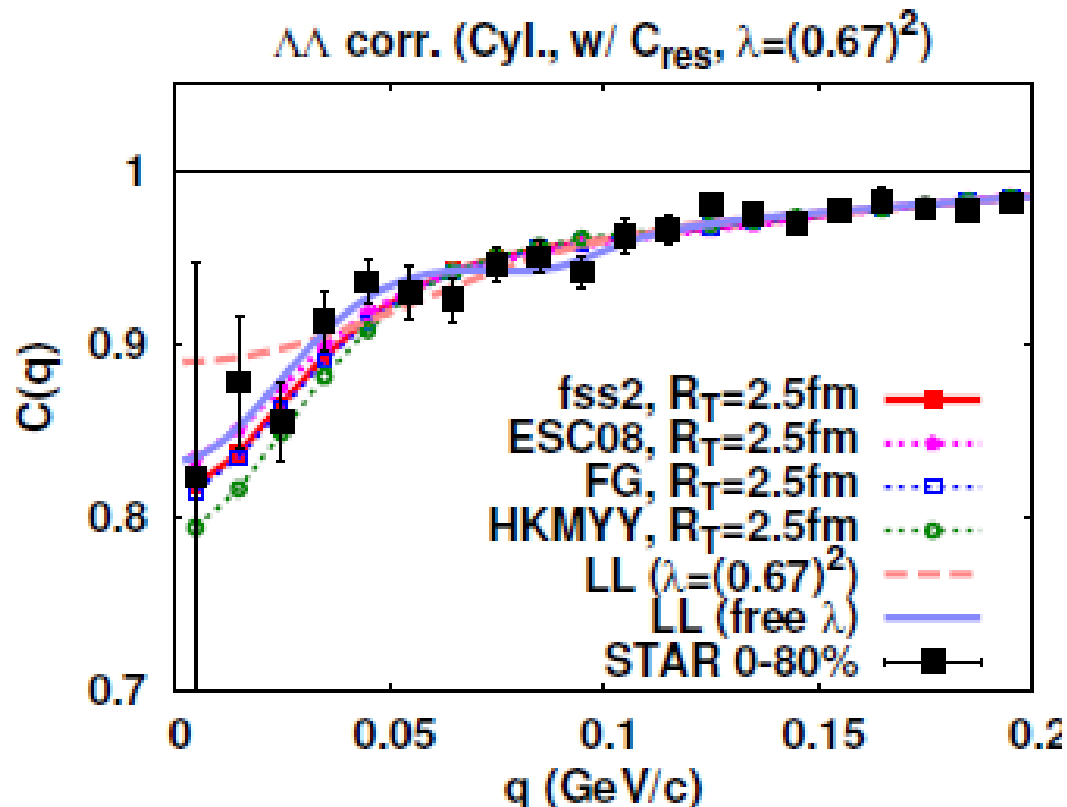
## ■ Neutron Star Matter EOS

- Hyperon Puzzle  
*Demorest et al. ('10), Antoniadis et al. ('13)*
- Cooling Puzzle ( $\Lambda\Lambda$  superfluidity)  
*T. Takatsuka, R. Tamagaki, PTP 112('04)37*



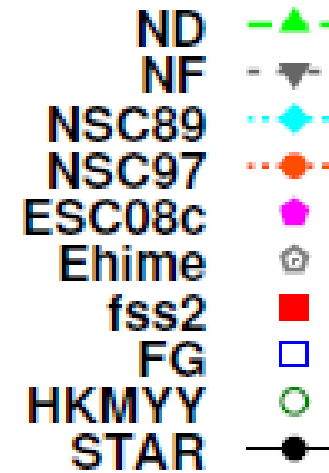
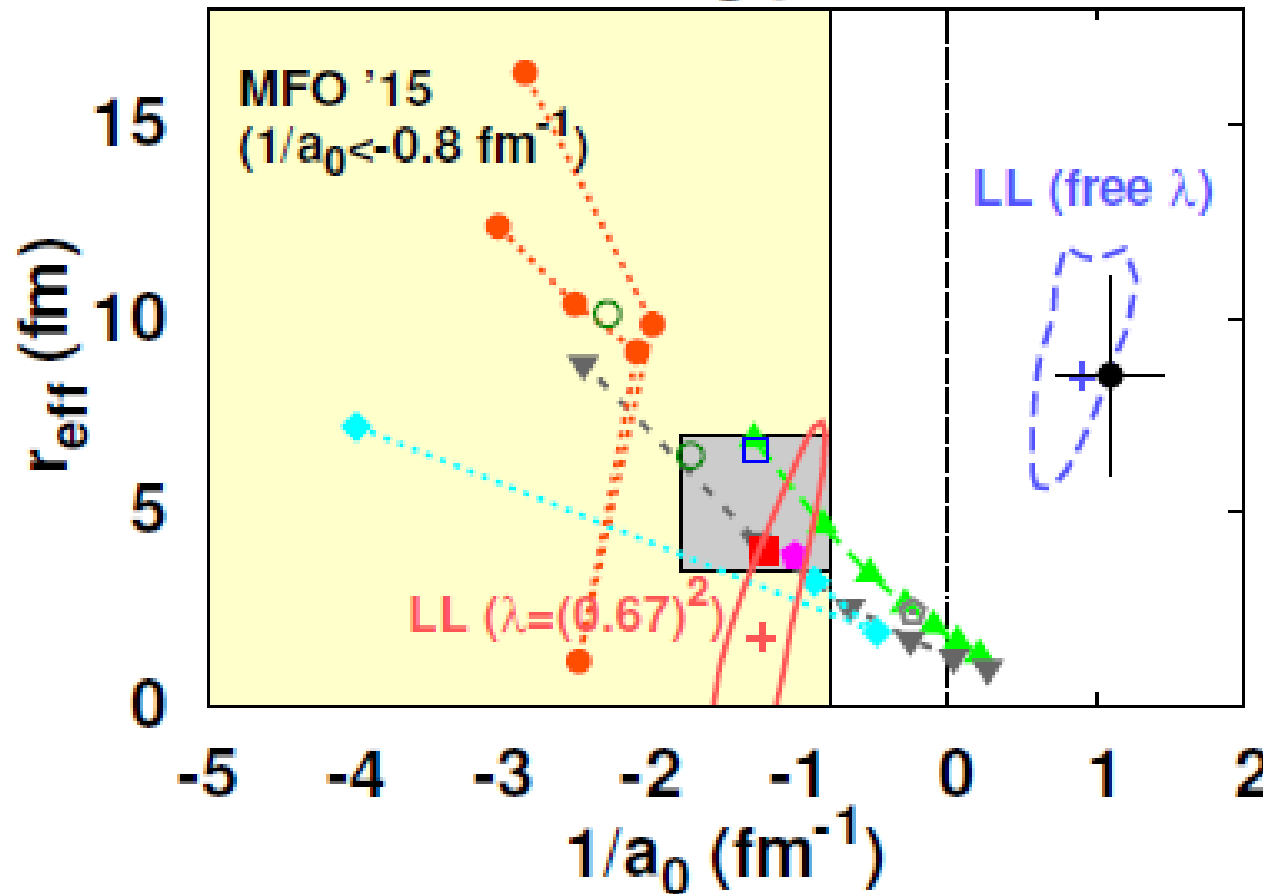
# $\Lambda\Lambda$ correlation at RHIC

- STAR collaboration at RHIC measured  $\Lambda\Lambda$  correlation !  
*Adamczyk et al. (STAR Collaboration), PRL 114 ('15) 022301.*
- Theoretical Analysis well explains the data  
*K.Morita et al., T.Furumoto, AO, PRC91('15)024916;*  
*AO, K.Morita, K.Miyahara, T.Hyodo, NPA954 ('16), 294.*
- New Data from ALICE  
*S. Achara+(ALICE), PRC99('19), 024001; arXiv:1905.07209*



# $\Lambda\Lambda$ interaction from $\Lambda\Lambda$ correlation

## $\Lambda\Lambda$ scattering parameters

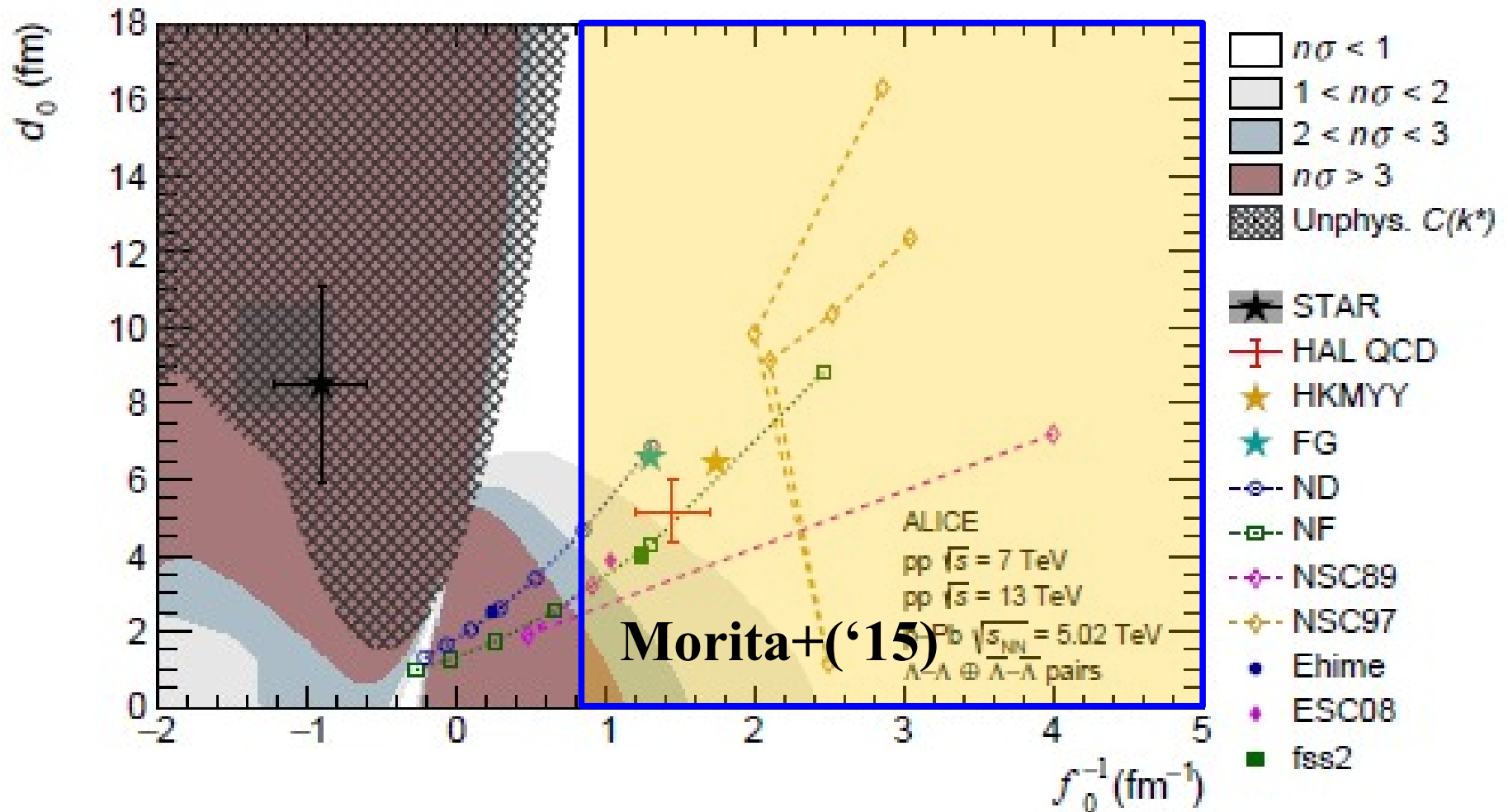


- Nijmegen potentials  
(ND, NF, NSC89, NSC97, ESC08)  
*Nagels+('77, '79), Maessen+('89),  
Rijken+('99, '10)*
- Ehime *Ueda et al. ('98)*
- Quark model interaction:  
fss2 *Fujiwara et al.('07)*
- Potential fitted to Nagara  
*Filikhin, Gal ('02) (FG),  
Hiyama et al. ('02, '10)(HKMYY)*

$$q \cot \delta = -1/a_0 + r_{\text{eff}} q^2/2 + \mathcal{O}(q^4)$$

# New Data from LHC-ALICE

ALICE (arXiv:1905.07209)



*Weakly attractive  $V_{\Lambda\Lambda}$*

*Large  $re_{\Lambda\Lambda}$   $\rightarrow$  Becomes repulsive at low relative density.*



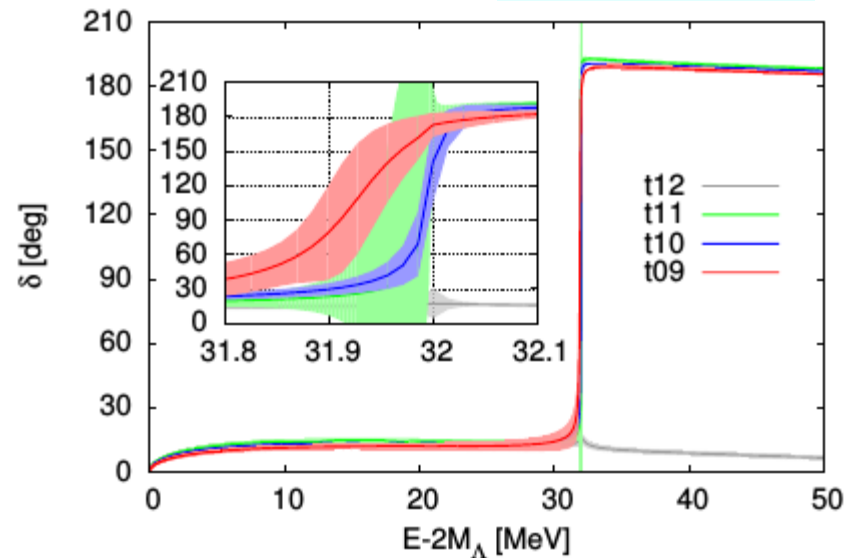
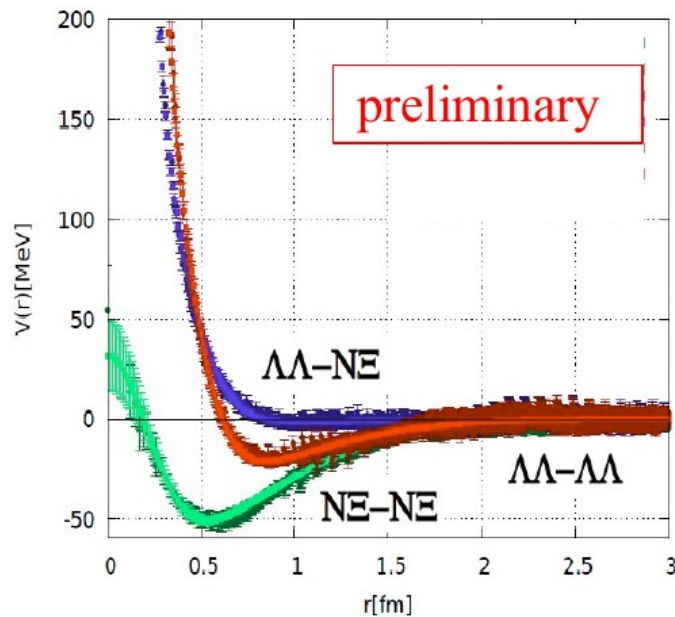
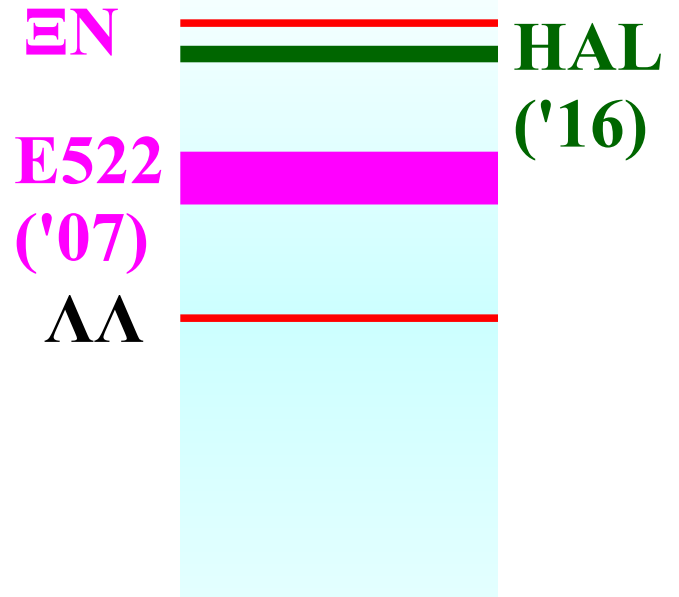
# Relevance of $\Xi N$ interaction to physics

- H-particle: 6-quark state (uuddss) may be realized as a loosely bound state of  $\Xi N$  ( $I=0$ )

*K. Sasaki et al. (HAL QCD, '16, '17)*

- Repulsive  $\Xi N$  interaction ( $I=1$ ) may help to support  $2 M_{\odot}$  Neutron Star

*Weissborn et al., NPA881 ('12) 62.*



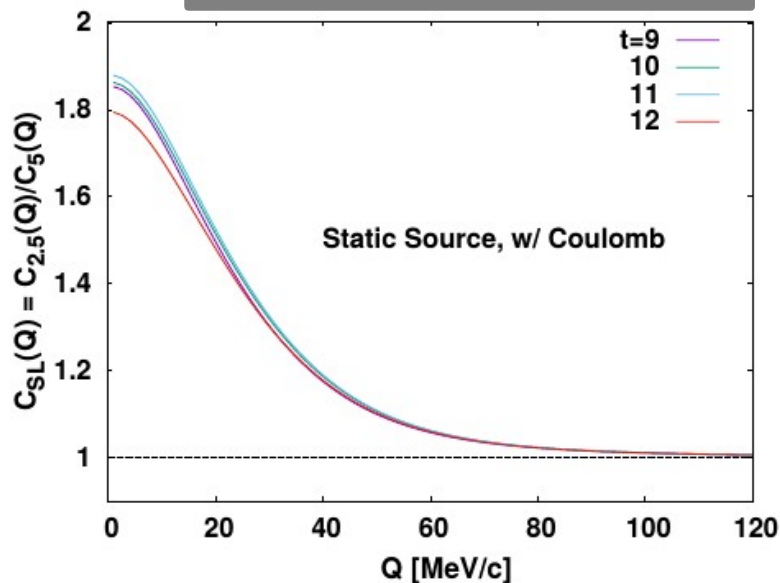
*K. Sasaki et al. (HAL QCD Collab.), EPJ Web Conf. 175 ('18) 05010.*

# $E^- p$ correlation

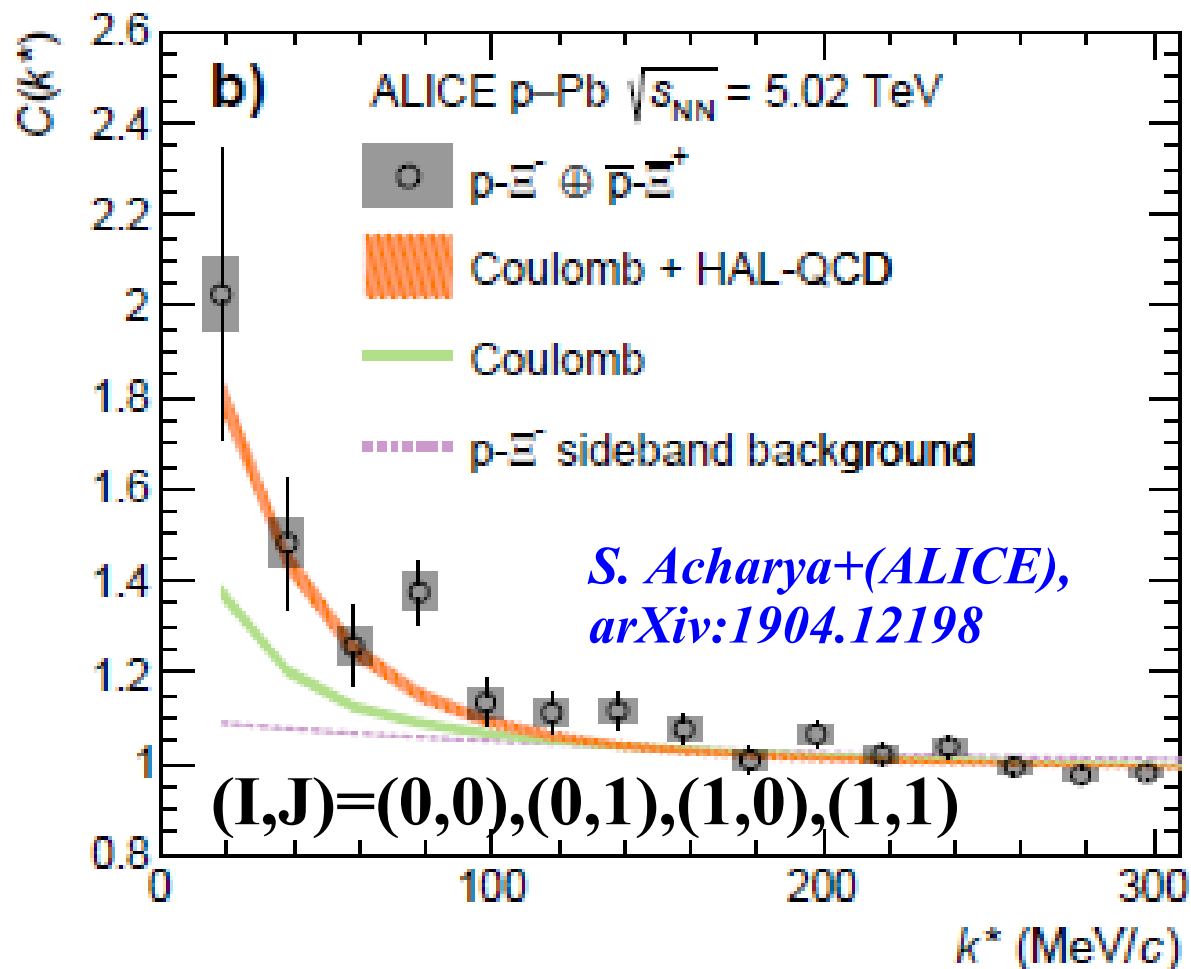
- Prediction of the correlation function by using  $\Xi N$  potential (HAL QCD Collab.) + Coulomb potential

$$|\psi|_{\text{spin av.}}^2 = \frac{1}{2} \sum_{I=0,1} \left[ \frac{1}{4} |\psi_I^{J=0}|^2 + \frac{3}{4} |\psi_I^{J=1}|^2 \right]$$

*HAL prediction is examined!*

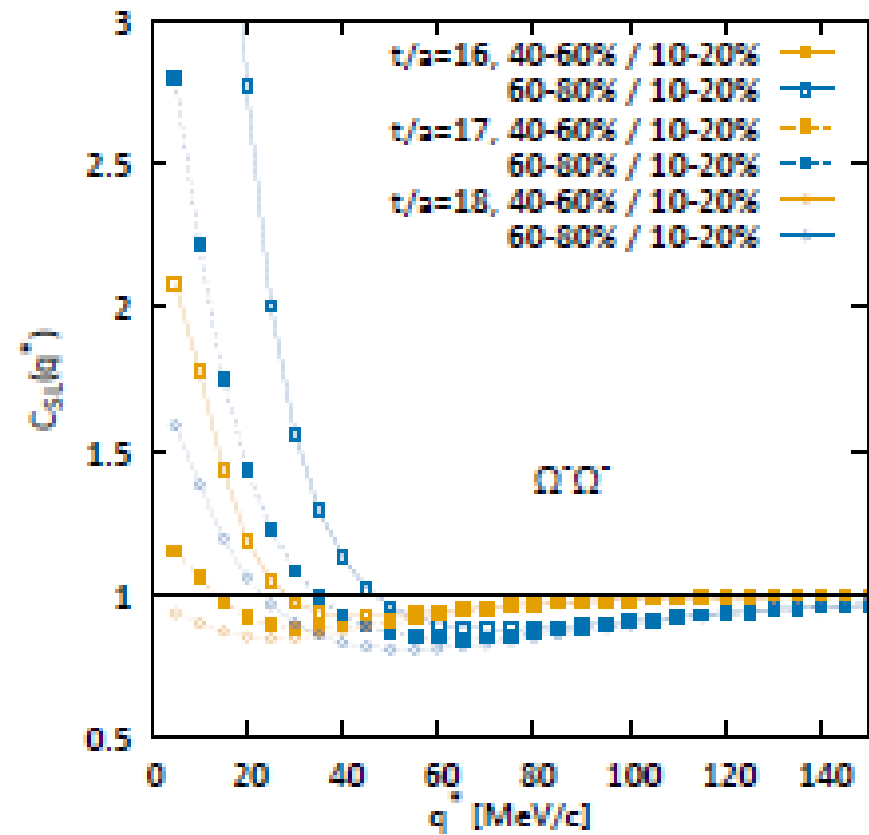
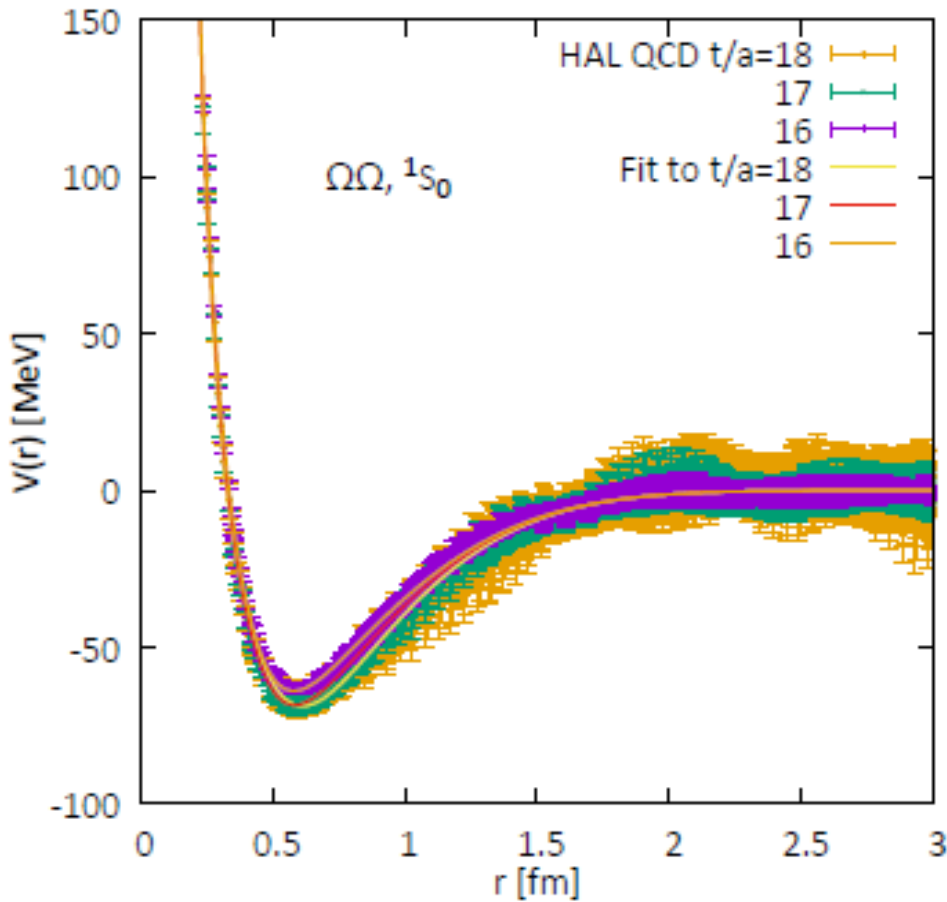


*T. Hatsuda, K. Morita, AO, K. Sasaki, NPA967('17), 856.*



# $\Omega\Omega$ correlation

$\Omega\Omega$  potential: S. Gongyo et al. (HAL QCD Collab),  
Phys. Rev. Lett. 120, 212001 (2017), 1709.00654.



K. Morita, S. Gongyo, T. Hatsuda, T. Hyodo,  
Y. Kamiya, AO, PRC101('20)015201 [1908.05414]

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*Thank you for your attention !*