

Pionic atom unveils hidden structure of QCD vacuum

—Deduction of chiral condensate at nuclear density—

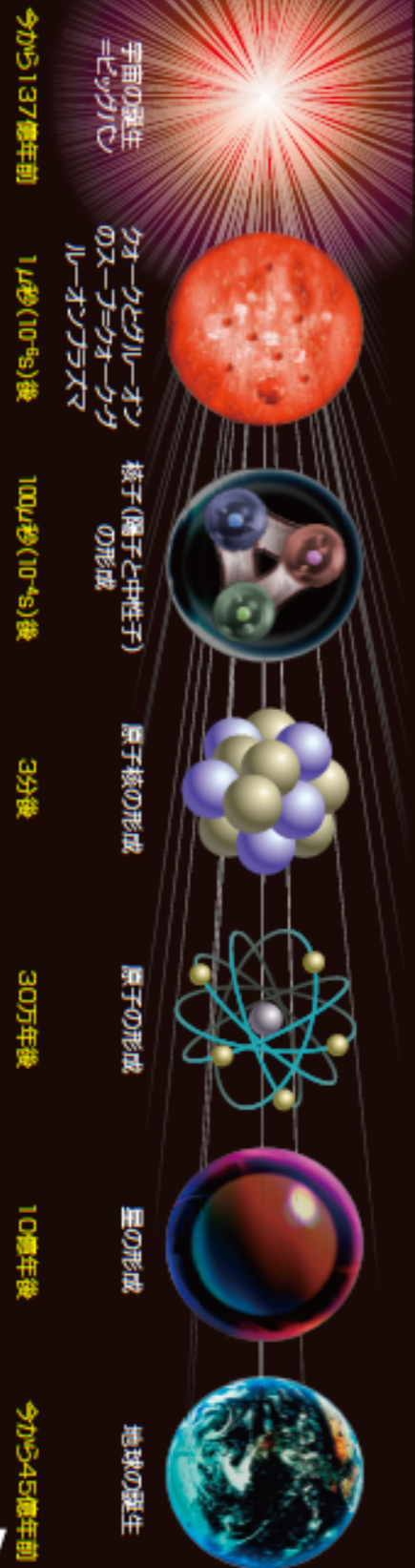
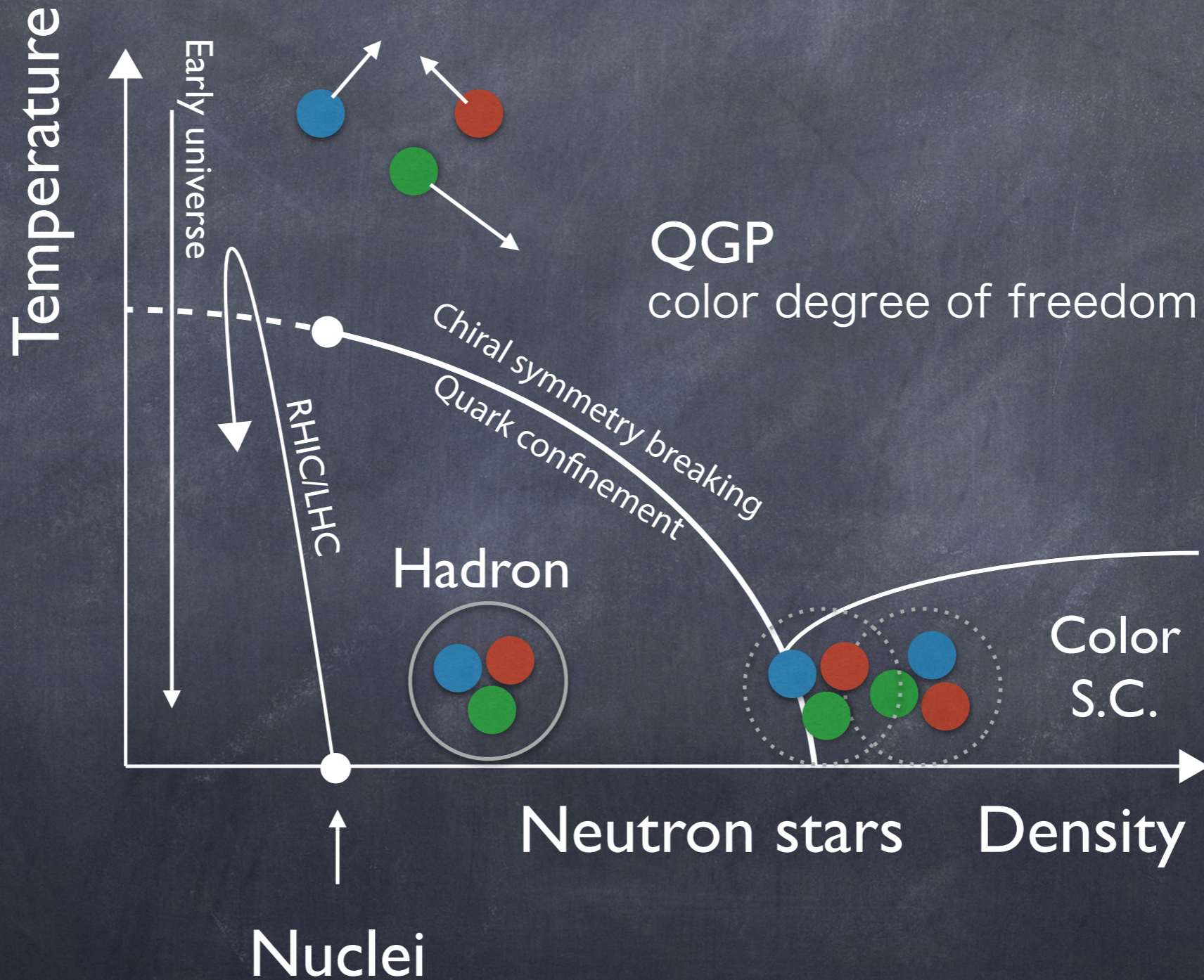
RIKEN Nishina Center
Kenta Itahashi

Pionic atom unveils hidden structure of QCD vacuum

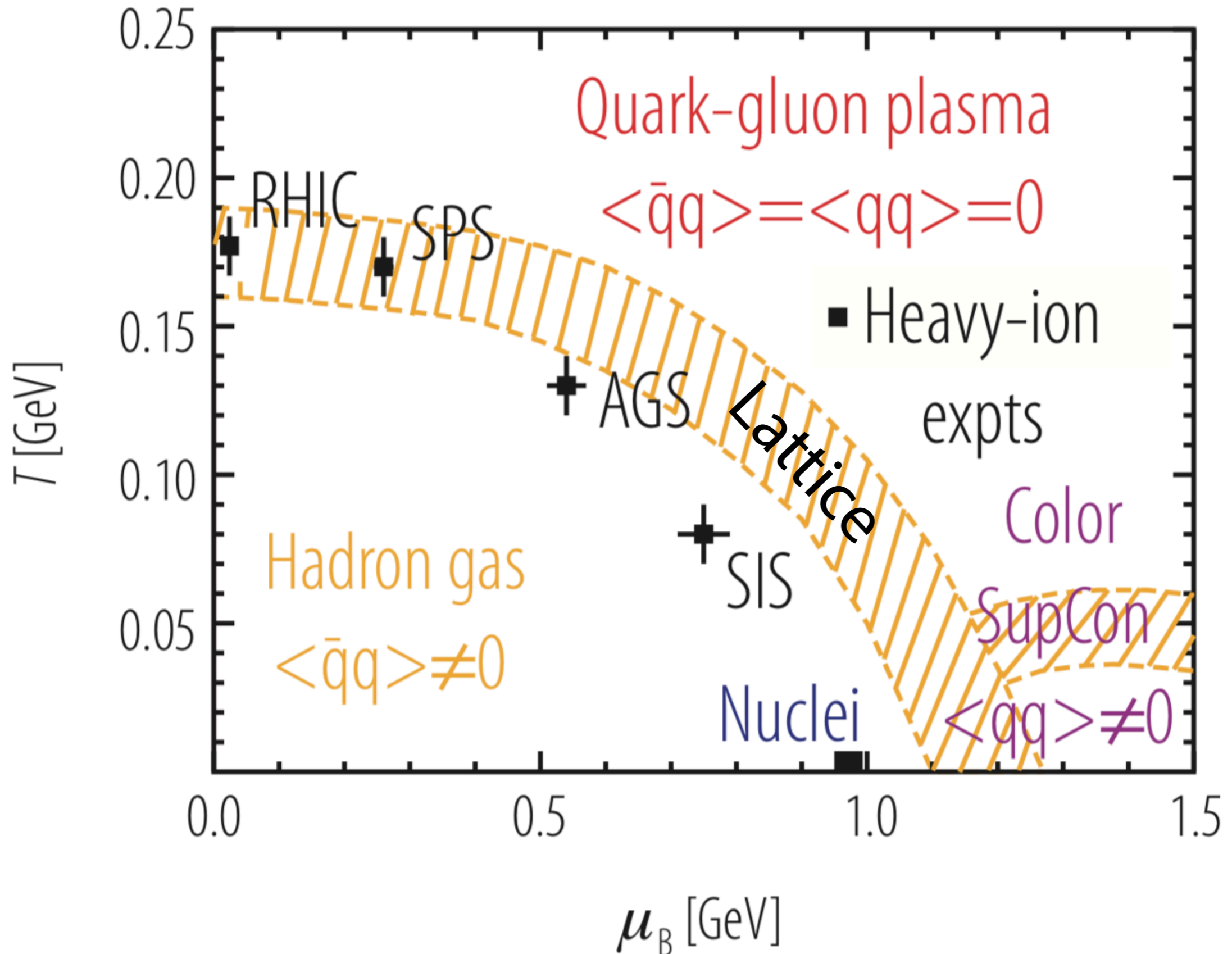
Takahiro Nishi¹, Kenta Itahashi^{1,*}, DeukSoon Ahn^{1,2}, Georg P.A. Berg³, Masanori Dozono¹, Daijiro Etoh⁴, Hiroyuki Fujioka⁵, Naoki Fukuda¹, Nobuhisa Fukunishi¹, Hans Geissel⁶, Emma Haettner⁶, Tadashi Hashimoto¹, Ryugo S. Hayano⁷, Satoru Hirenzaki⁸, Hiroshi Horii⁷, Natsumi Ikeno⁹, Naoto Inabe¹, Masahiko Iwasaki¹, Daisuke Kameda¹, Keichi Kisamori¹⁰, Yu Kiyokawa¹⁰, Toshiyuki Kubo¹, Kensuke Kusaka¹, Masafumi Matsushita¹⁰, Shin'ichiro Michimasa¹⁰, Go Mishima⁷, Hiroyuki Miya¹, Daichi Murai¹, Hideko Nagahiro⁸, Megumi Niikura⁷, Naoko Nose-Togawa¹¹, Shinsuke Ota¹⁰, Naruhiko Sakamoto¹, Kimiko Sekiguchi⁴, Yuta Shiokawa⁴, Hiroshi Suzuki¹, Ken Suzuki¹², Motonobu Takaki¹⁰, Hiroyuki Takeda¹, Yoshiki K. Tanaka¹, Tomohiro Uesaka¹, Yasumori Wada⁴, Atomu Watanabe⁴, Yuni N. Watanabe⁷, Helmut Weick⁶, Hiroki Yamakami⁵, Yoshiyuki Yanagisawa¹, and Koichi Yoshida¹

Material properties of vacuum

Properties of QCD vacuum depend on temperature and matter-density



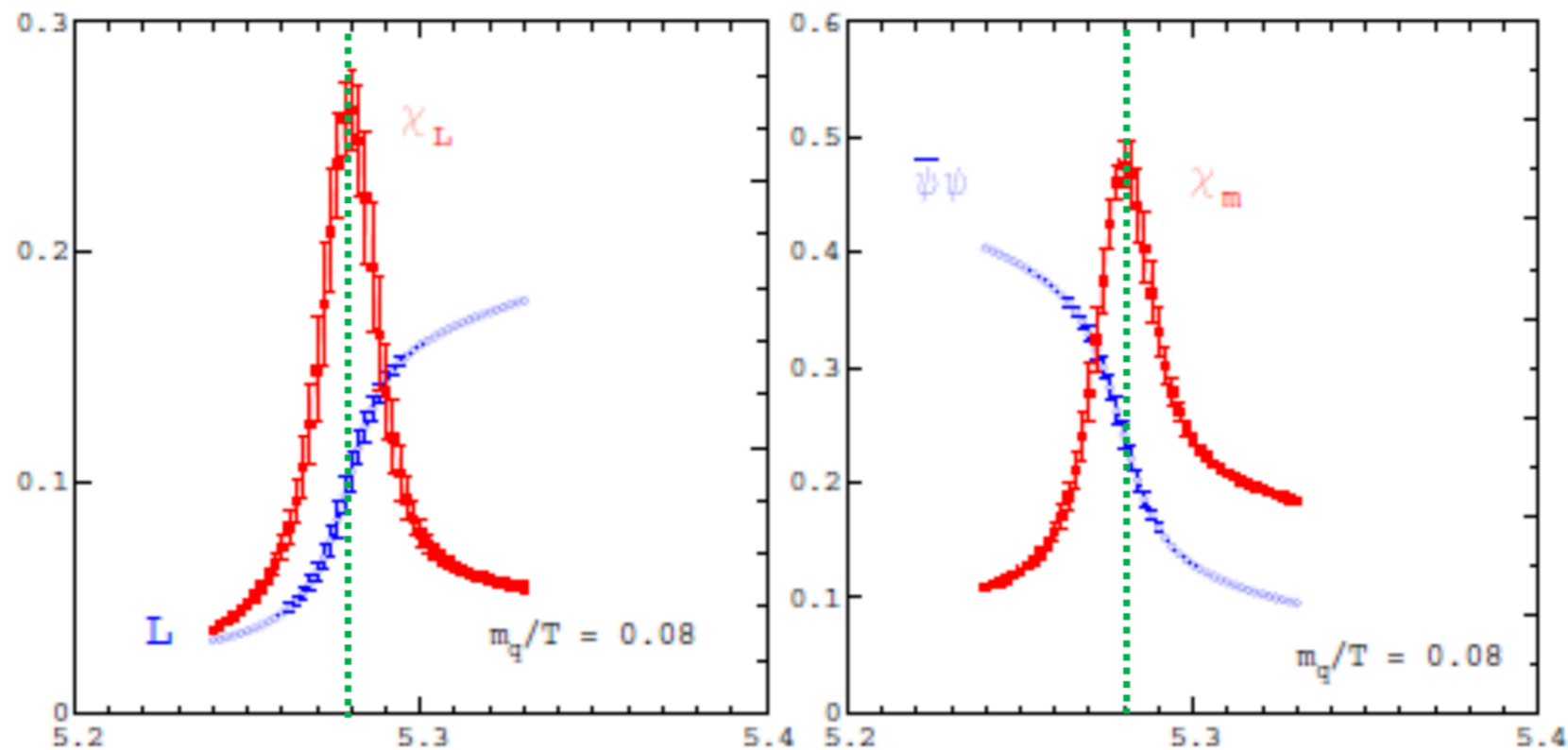
QCD phase and chemical freezeout points



Chiral transition & Quark confinement

Correlation between Confinement and CSB is suggested by
**Simultaneous Phase Transition of
 Deconfinement and Chiral Restoration.**

Lattice QCD results at finite temperature F. Karsch, Lect. Notes Phys. (2002)



Polyakov Loop $\langle L \rangle$
 Color Confinement

Chiral Condensate $\langle \bar{q}q \rangle$
 Chiral Symmetry Breaking

Fig. 2. Deconfinement and chiral symmetry restoration in 2-flavour QCD: Shown is $\langle L \rangle$ (left), which is the order parameter for deconfinement in the pure gauge limit ($m_q \rightarrow \infty$), and $\langle \bar{\psi}\psi \rangle$ (right), which is the order parameter for chiral symmetry breaking in the chiral limit ($m_q \rightarrow 0$). Also shown are the corresponding susceptibilities as a function of the coupling $\beta = 6/g^2$.

Chiral transition & Quark confinement

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Simultaneous Phase Transition of
Deconfinement and Chiral Restoration.

Lattice QCD results at finite temperature F. Karsch, Lect. Notes Phys. (2002)

0.3 0.6

Confinement と Chiral Symmetry Breaking の相関

有限温度や有限体積効果でのQCD相転移の様相などから、
両者には密接な対応関係があるのは明らか
～ Deconfinement と Chiral Symmetry Restoration の一致

ただし、両者の関係はあまり良く分かっていないのが現状

Polyakov Loop $\langle P \rangle$

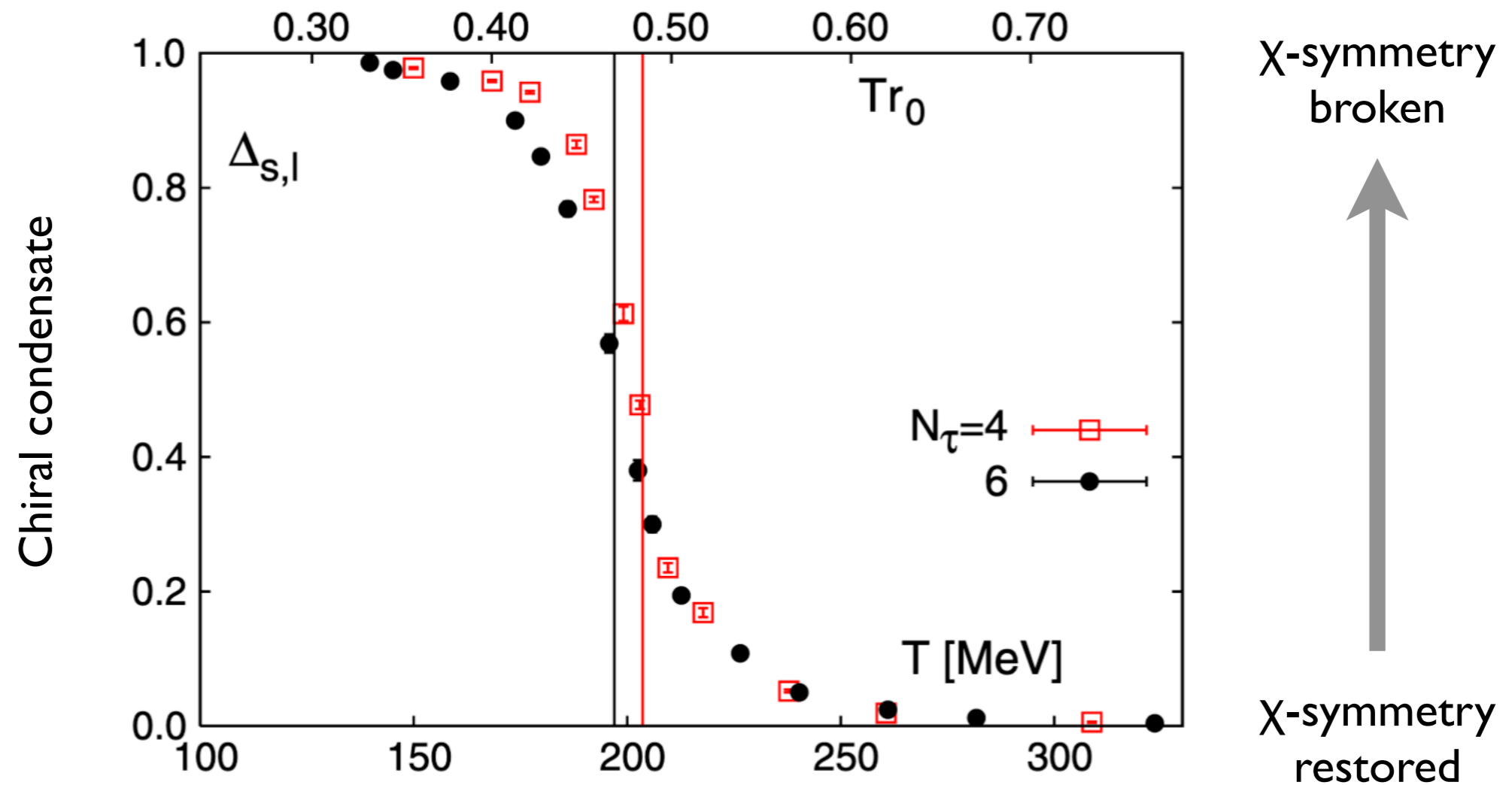
Color Confinement

Chiral Condensate $\langle \bar{q}q \rangle$

Chiral Symmetry Breaking

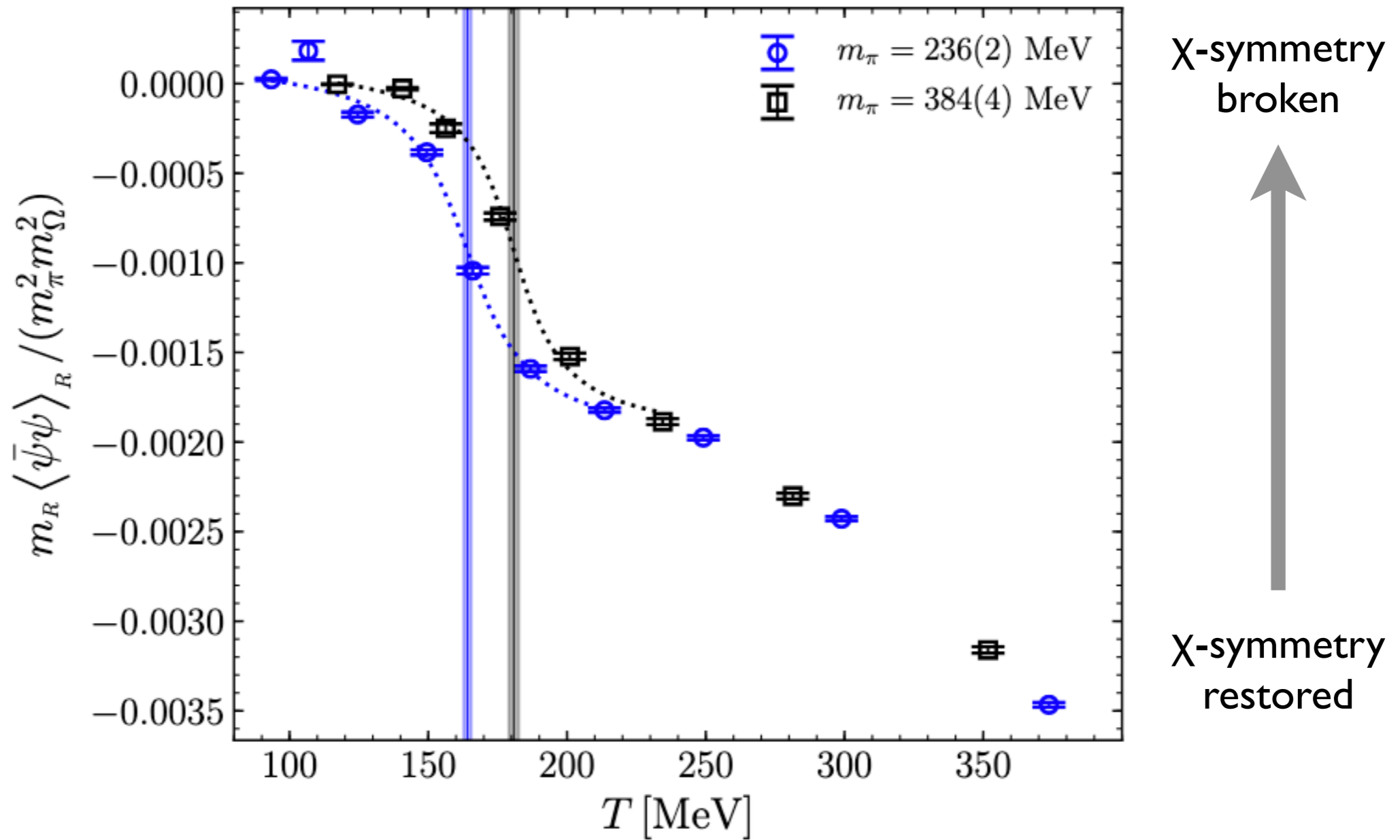
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Lattice QCD calculated T dependence of chiral condensate



Temperature dependence of the chiral condensate from lattice QCD with 2 + 1 quark flavours and almost physical quark masses

Lattice QCD calculated T dependence of chiral condensate



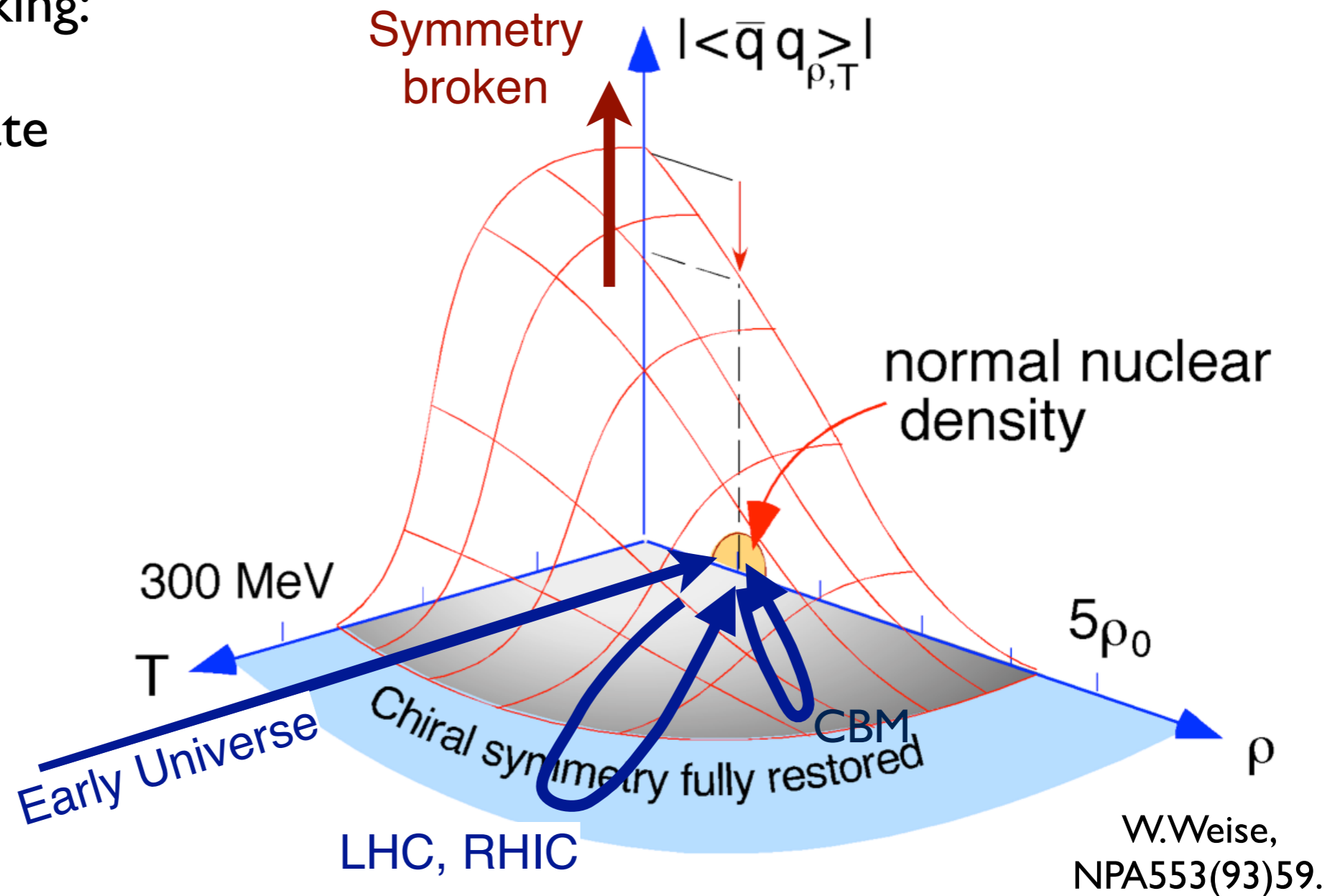
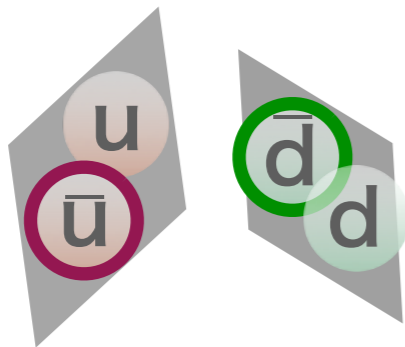
Remark: sign problem makes it difficult for lattice to approach non-zero ρ region

Jon-Ivar Skullerud
PRD105(2022)034504

Chiral condensate, order parameter of chiral symmetry

One of order parameters of χ -symmetry breaking:

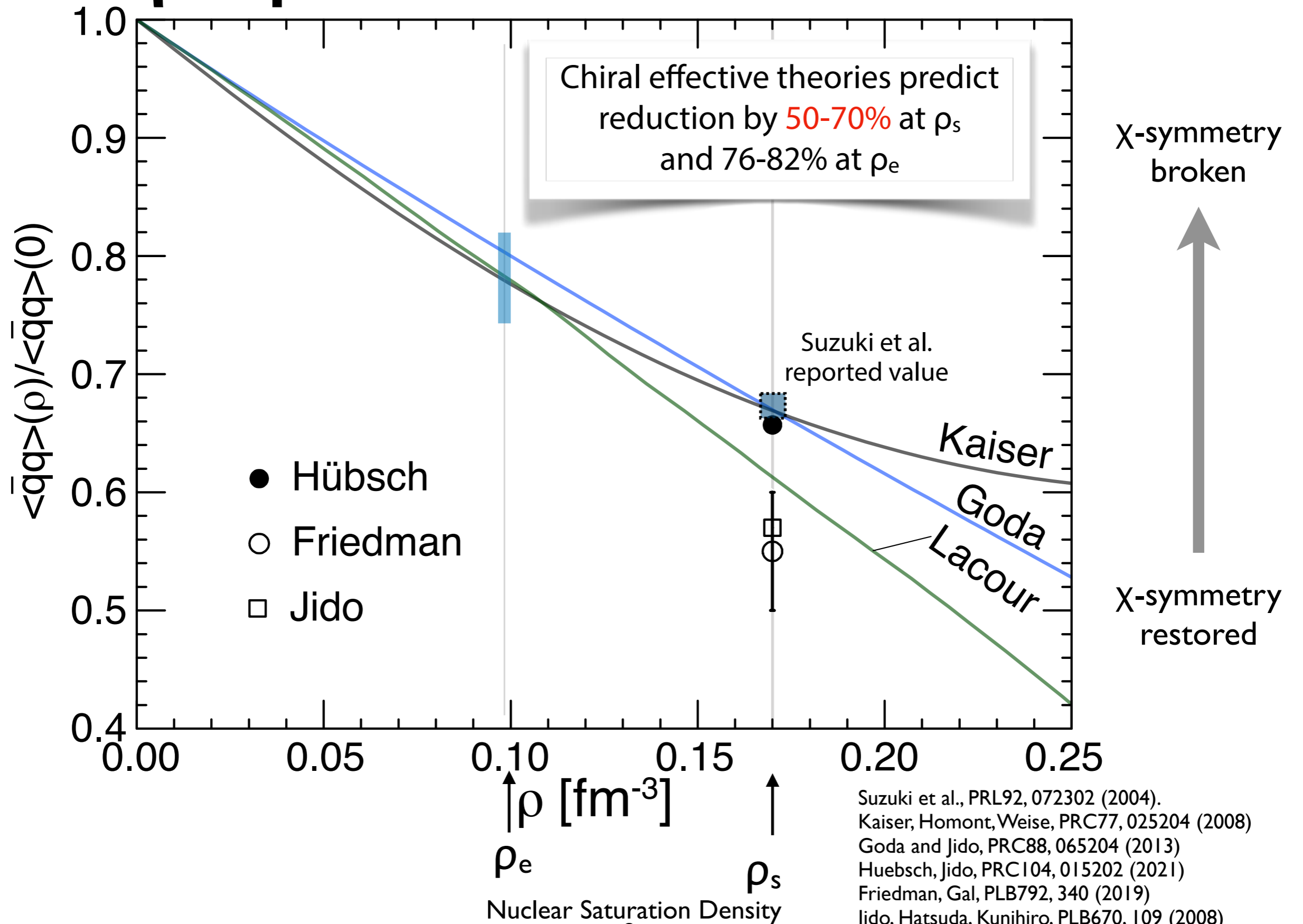
Chiral condensate



Remark: sign problem makes it difficult for lattice to approach non-zero ρ region

Analysis of material properties of QCD vacuum

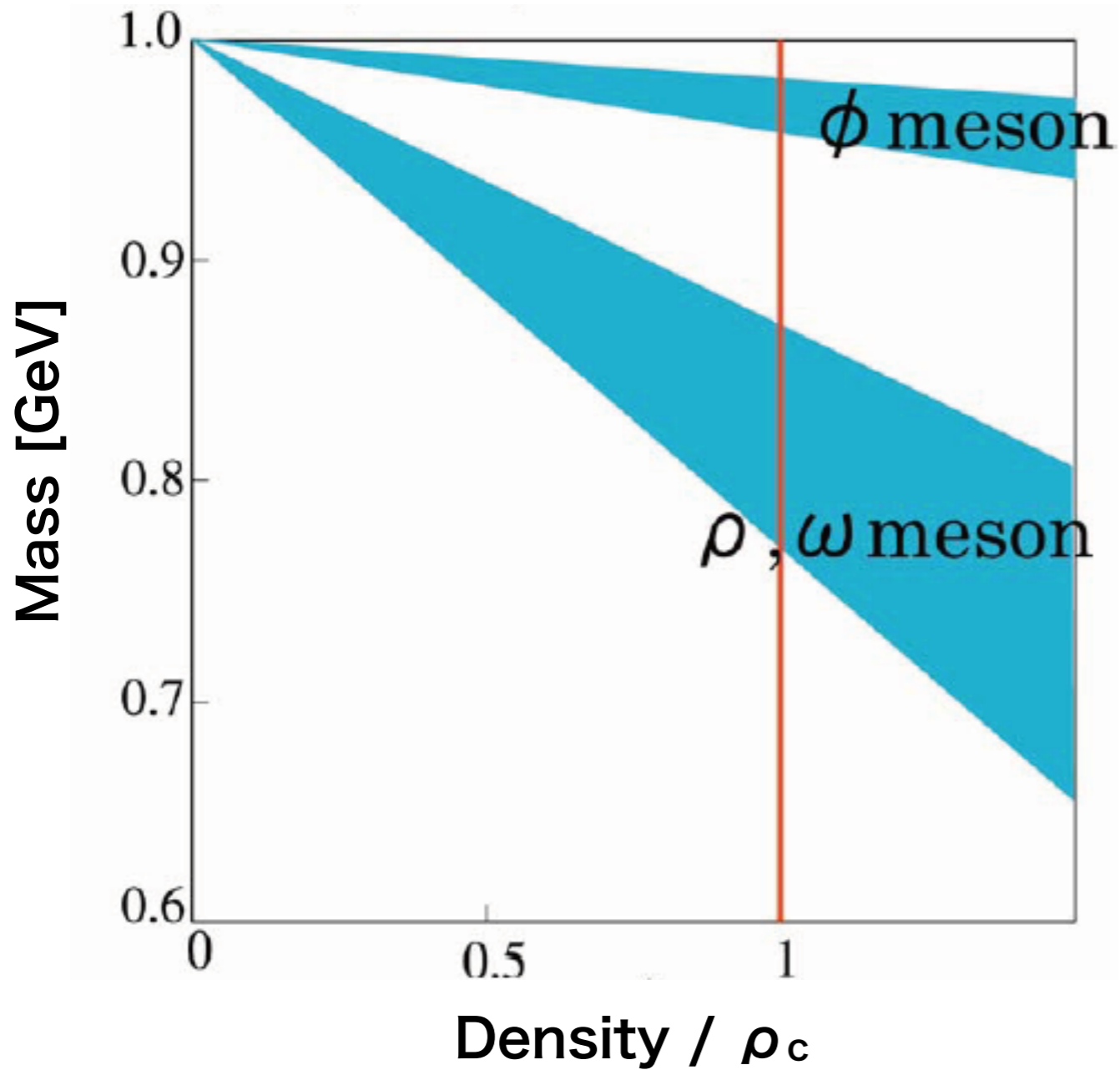
ρ dependence of chiral condensate



Suzuki et al., PRL92, 072302 (2004).
 Kaiser, Homont, Weise, PRC77, 025204 (2008)
 Goda and Jido, PRC88, 065204 (2013)
 Huebsch, Jido, PRC104, 015202 (2021)
 Friedman, Gal, PLB792, 340 (2019)
 Jido, Hatsuda, Kunihiro, PLB670, 109 (2008)
 Lacour, Oller, Meissner, J. Phys. G. 37, 125002 (2010)

Meson masses and QCD medium effect

Vector meson mass modification



$\phi(1020)$

$$J^{PC} = 0^-(1^{--})$$

Mass $m = 1019.455 \pm 0.020$ MeV (S = 1.1)

Full width $\Gamma = 4.26 \pm 0.04$ MeV (S = 1.4)

$\phi(1020)$ DECAY MODES	Fraction (Γ_i/Γ)	Scale factor/ Confidence level	ρ (MeV/c)
K^+K^-	(48.9 \pm 0.5) %	S=1.1	127
$K_L^0 K_S^0$	(34.2 \pm 0.4) %	S=1.1	110
$\ell^+ \ell^-$	—		510
$e^+ e^-$	(2.954 \pm 0.030) $\times 10^{-4}$	S=1.1	510
$\mu^+ \mu^-$	(2.87 \pm 0.19) $\times 10^{-4}$		499

$\rho(770)$ ^[h]

$$J^{PC} = 1^+(1^{--})$$

Mass $m = 775.49 \pm 0.34$ MeV

Full width $\Gamma = 149.1 \pm 0.8$ MeV

$\Gamma_{ee} = 7.04 \pm 0.06$ keV

$\omega(782)$

$$J^{PC} = 0^-(1^{--})$$

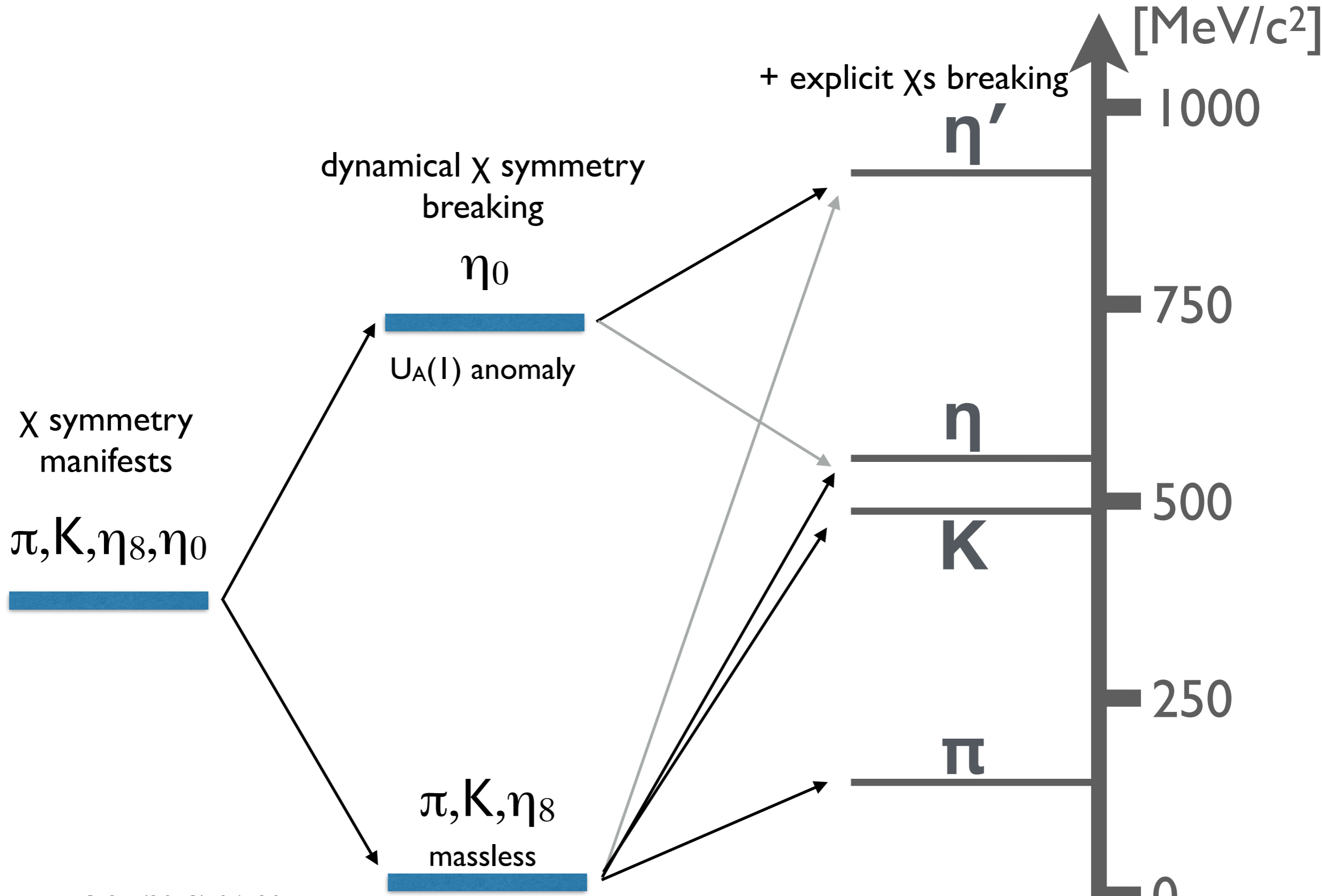
Mass $m = 782.65 \pm 0.12$ MeV (S = 1.9)

Full width $\Gamma = 8.49 \pm 0.08$ MeV

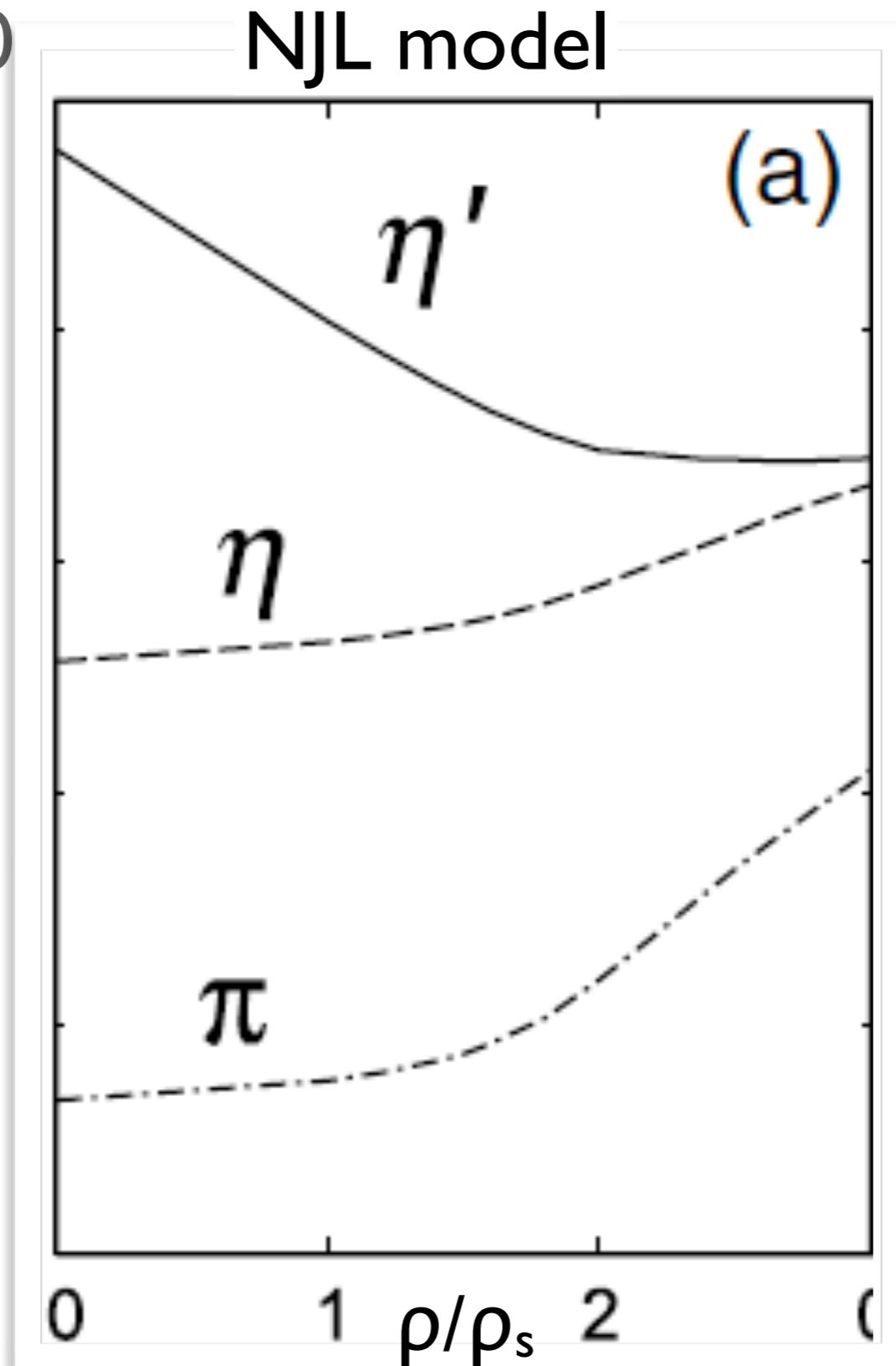
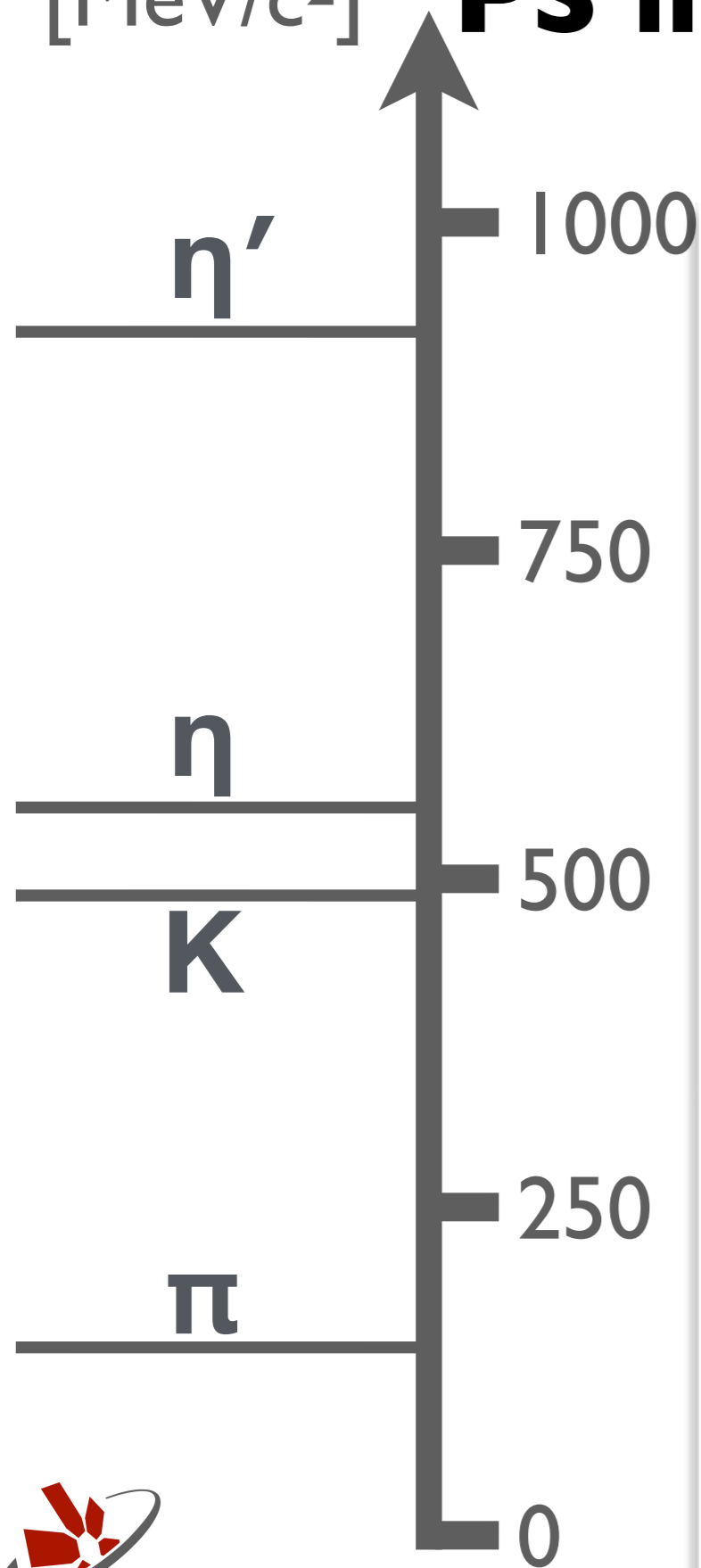
$\Gamma_{ee} = 0.60 \pm 0.02$ keV

Masses of Pseudo-Scalar Mesons

with various symmetry breaking patterns



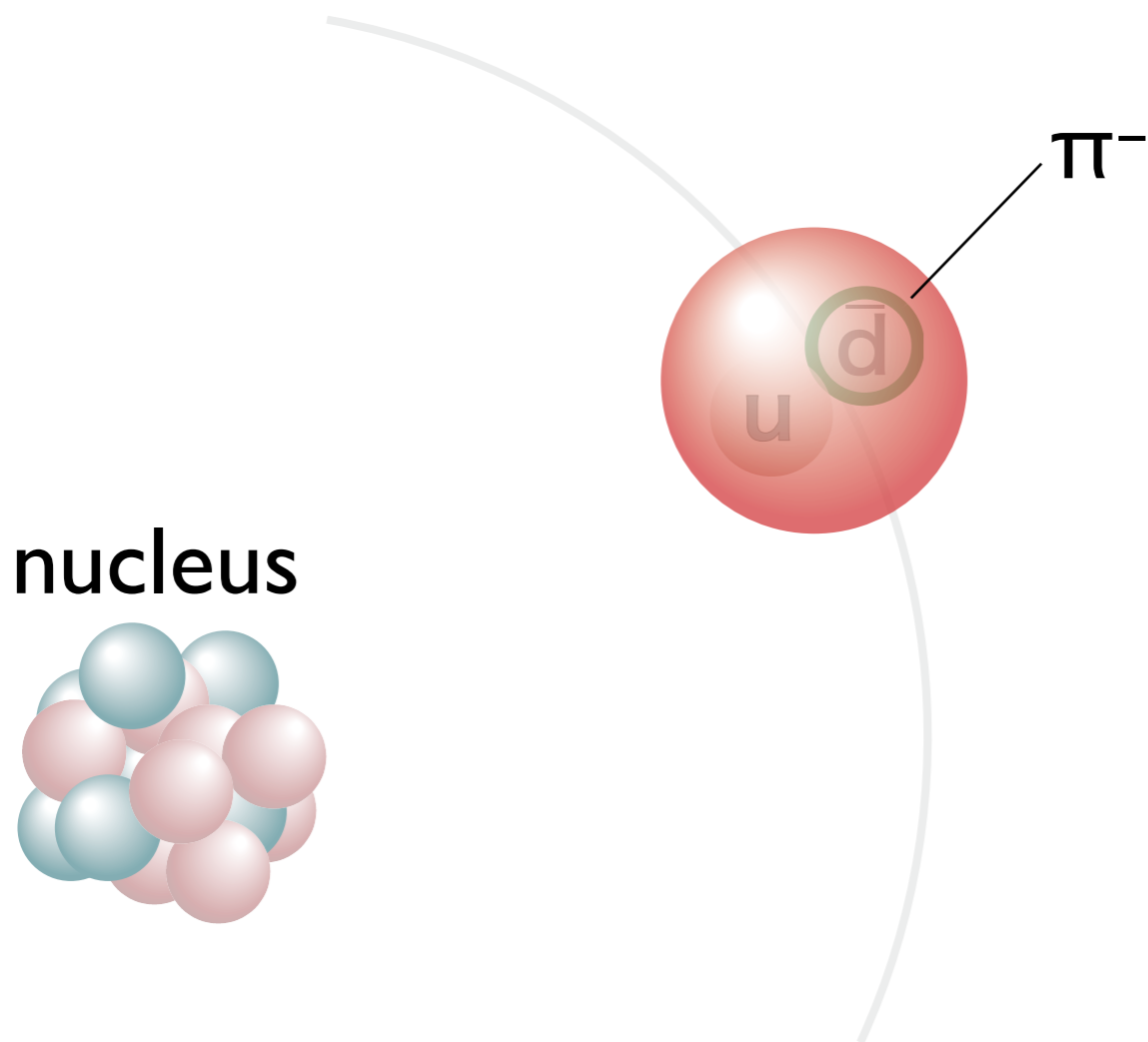
[MeV/c²] PS in high density medium



REMARK

Δm between η - η' , (σ , π) (ρ , a_1) are important

Pionic atoms

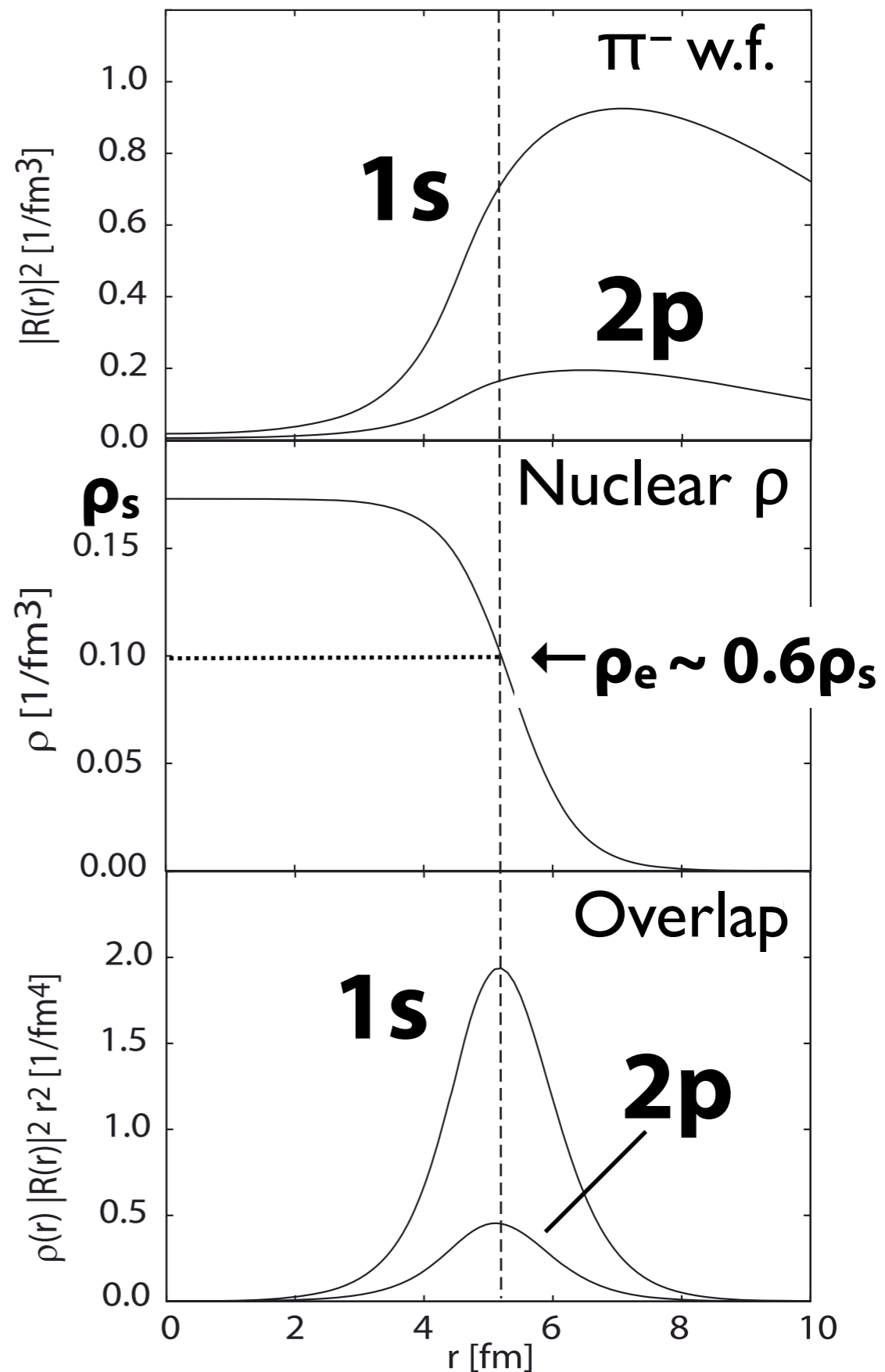


Ericson-Ericson potential

$$U_{\text{opt}}(r) = U_s(r) + U_p(r),$$

$$U_s(r) = b_0 \rho + \mathbf{b}_1 (\rho_n - \rho_p) + B_0 \rho^2$$

$$U_p(r) = \frac{2\pi}{\mu} \vec{\nabla} \cdot [c(r) + \varepsilon_2^{-1} C_0 \rho^2(r)] L(r) \vec{\nabla}$$



Pion-nucleus interaction

Overlap between
pion w.f. and nucleus
→ π works as a probe
at $\rho_e \sim 0.6\rho_s$



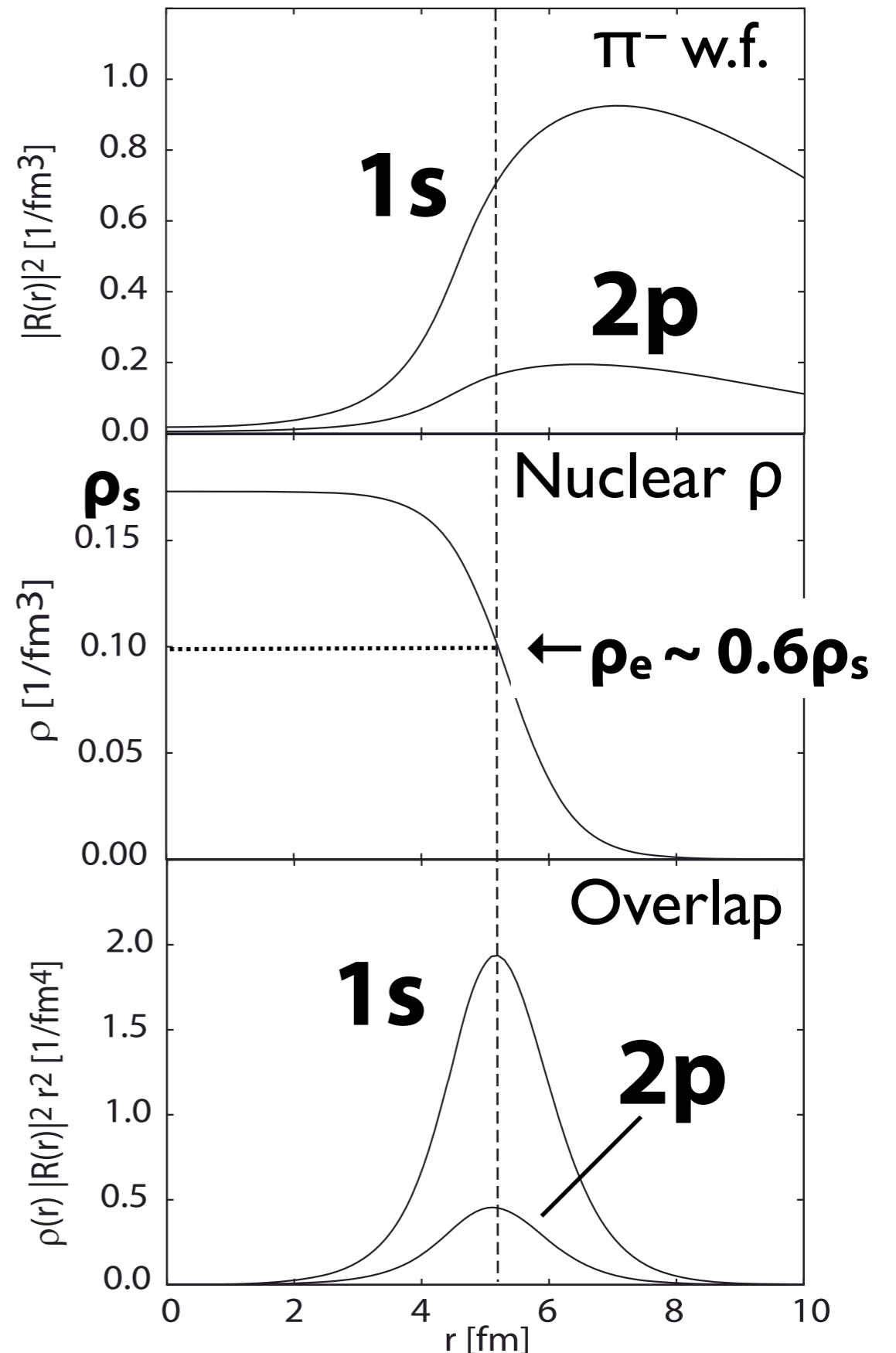
π -nucleus interaction is changed
for wavefunction renormalization
of medium effect

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Pion-nucleus interaction and chiral condensate

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In-medium Glashow-Weinberg relation

$$\frac{\langle \bar{q}q \rangle^*}{\langle \bar{q}q \rangle} \simeq \left(\frac{b_1^v}{b_1} \right)^{1/2} \left(1 - \gamma \frac{\rho}{\rho_0} \right)$$

$$\gamma = 0.184 \pm 0.003$$

Jido, Hatsuda, Kunihiro, PLB670, 109 (2008)

Pion-nucleus interaction and chiral condensate

Gell-Mann-Oakes-Renner relation

$$f_{\pi}^2 m_{\pi}^2 = -2m_q \langle \bar{q}q \rangle$$

Tomozawa-Weinberg relation

$$b_1 = -\frac{m_{\pi}}{8\pi f_{\pi}^2}$$

$$\frac{\langle \bar{q}q \rangle_{\rho}}{\langle \bar{q}q \rangle_0} \approx \frac{b_1^{\text{free}}}{b_1(\rho)}$$

M. Gell-Mann et al., PR175(1968)2195.
Y. Tomozawa, NuovoCimA46(1966)707.
S. Weinberg, PRL17(1966)616.

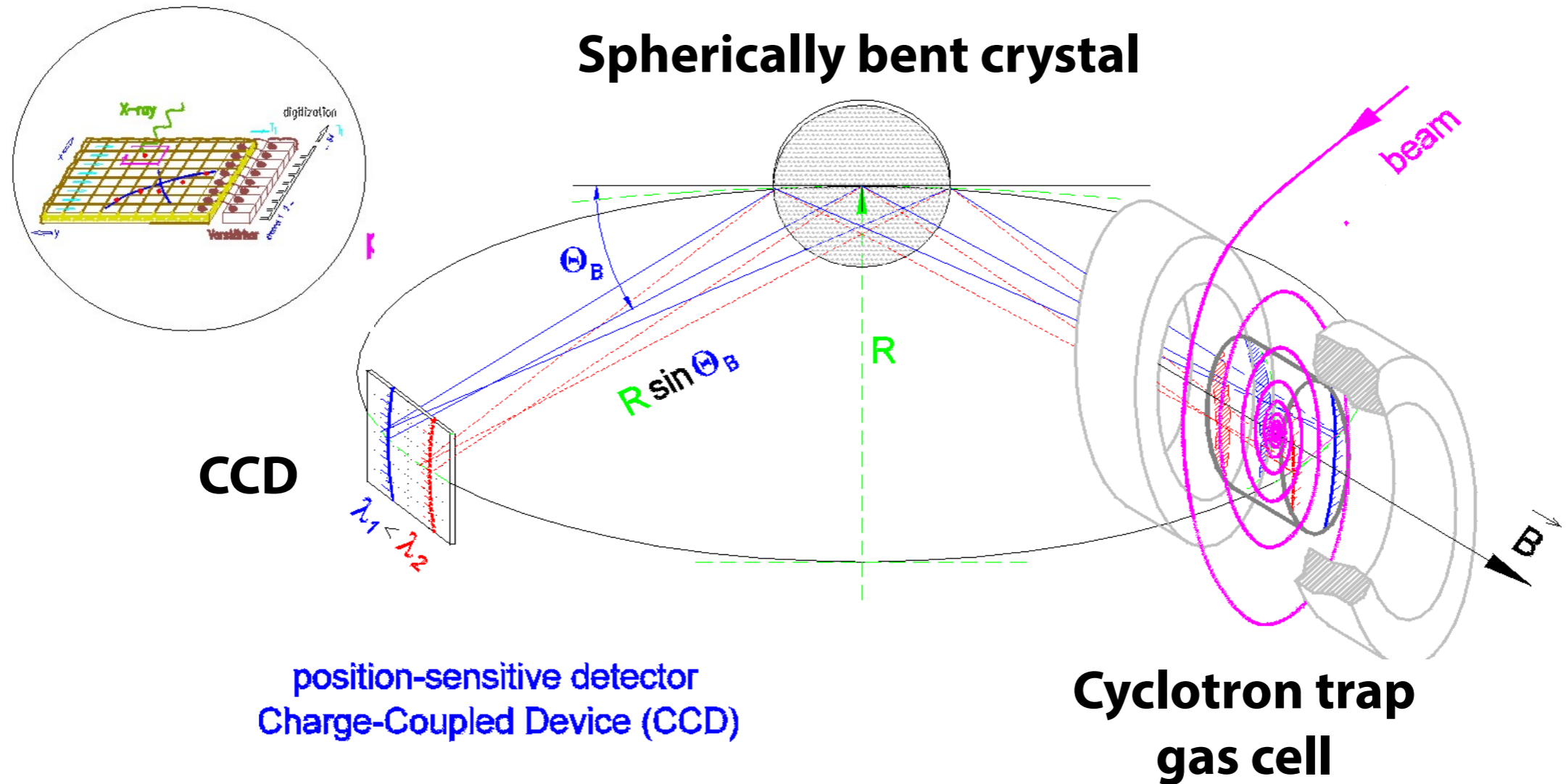
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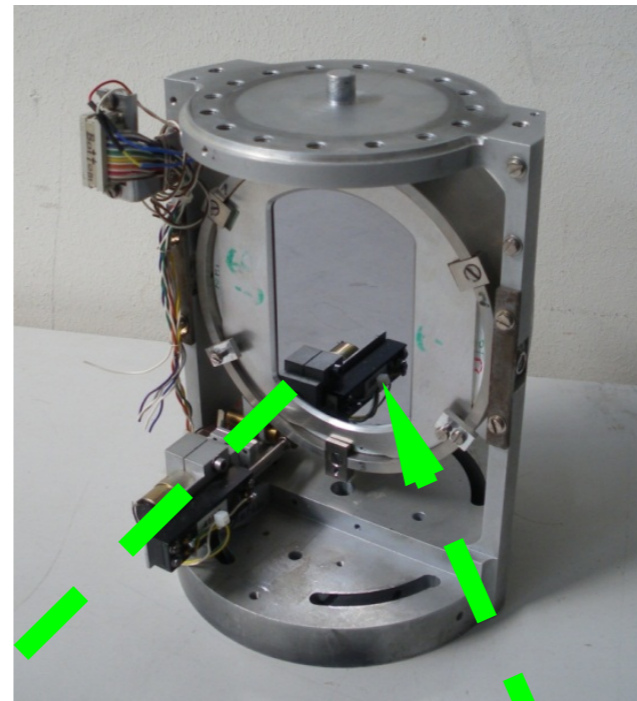
High precision pionic hydrogen/deuterium measurement at PSI



Bragg reflection
 $n\lambda = 2d \times \sin \theta_B$

High precision pionic hydrogen/deuterium measurement at PSI

X線凹面鏡



BRAGG CRYSTAL

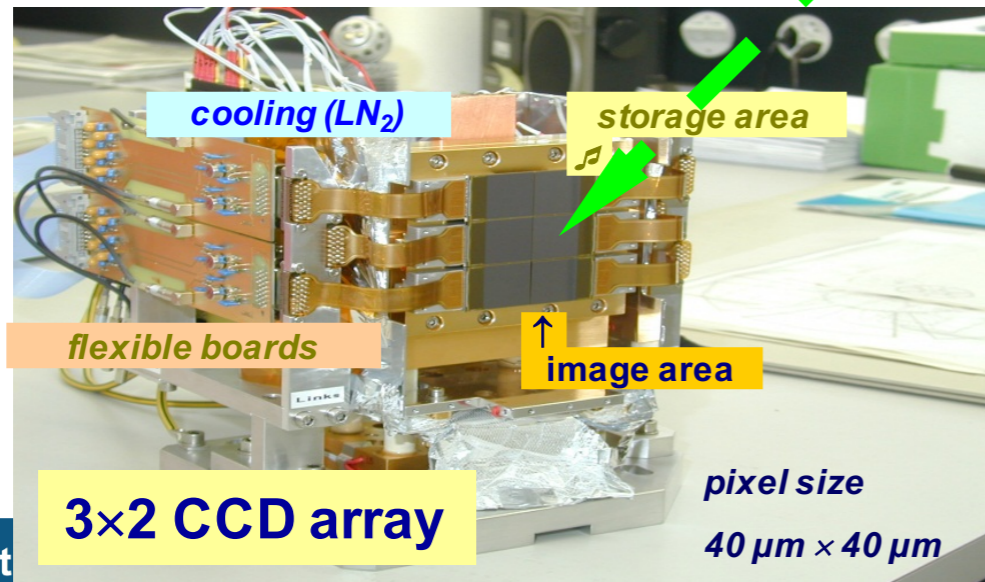
Si 111

spherically curved

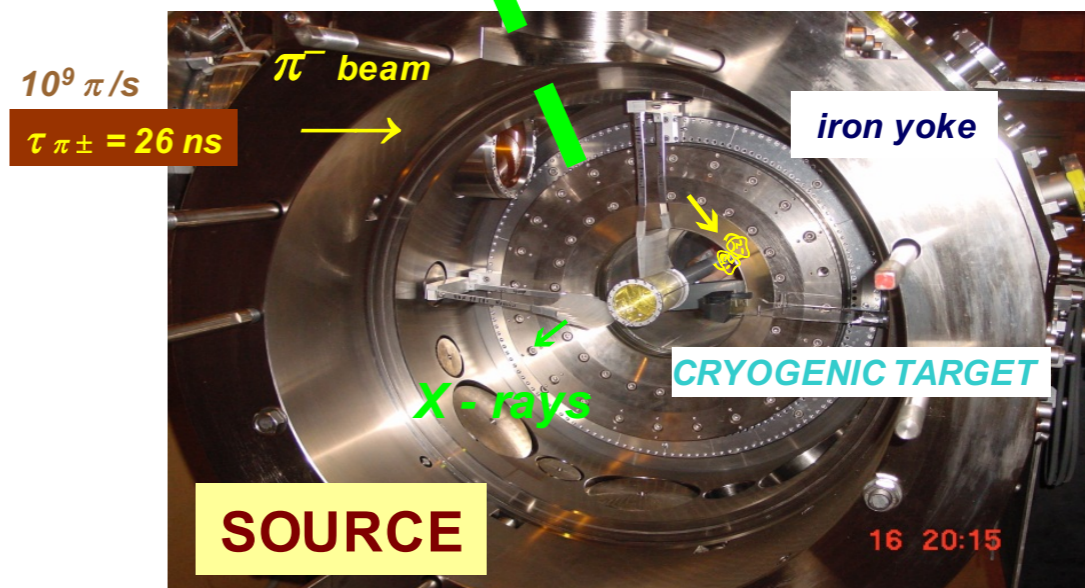
$R = 3\text{ m}$
 $\Phi = 10\text{ cm}$

CCD検出器

Large - Area Focal Plane Detector



CYCLOTRON TRAP
one coil removed



サイクロトロントラップ

Ultimate spectroscopy of hadronic atoms

N. Nelms et al., Nucl. Instr. Meth 484 (2002) 419

Detlev Gotta
Institut für Kernphysik, Forschungszentrum Jülich / Universität zu Köln

GGSWBS'14, Tbilisi, Georgia see talk by M. Jabua

6th Georgian - German School and Workshop in Basic Science - lecture

July 10, 2014

Pion-nucleus interaction and chiral condensate

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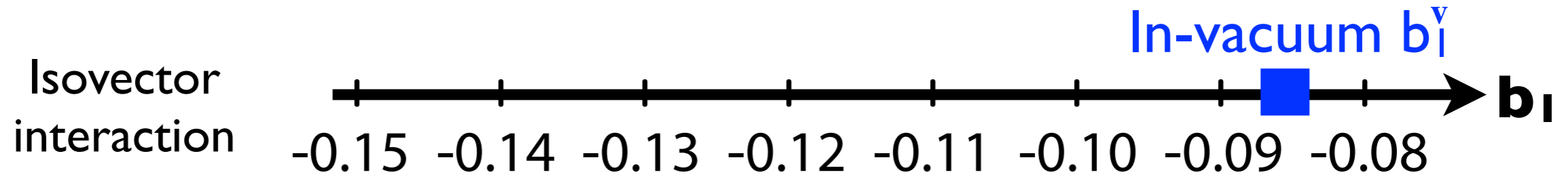
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Jido, Hatsuda, Kunihiro, PLB670, 109 (2008)

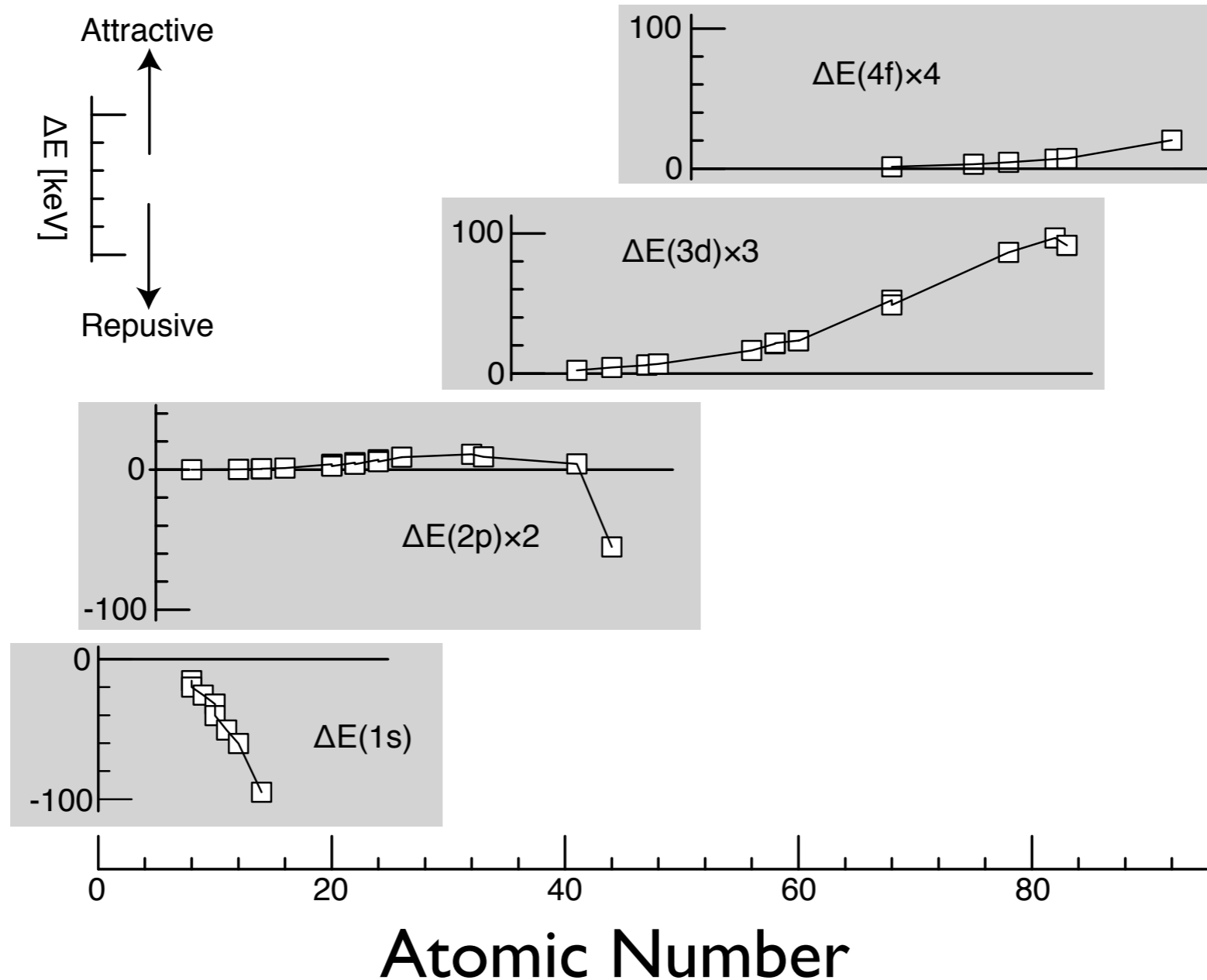
Pionic hydrogen and deuterium

$$b_1^{\text{v}} = 0.0866 \pm 0.0010$$

Hirtl et al., EPJA57, 70 (2021)



Level shifts in pionic X-ray measurements



Ericson-Ericson potential

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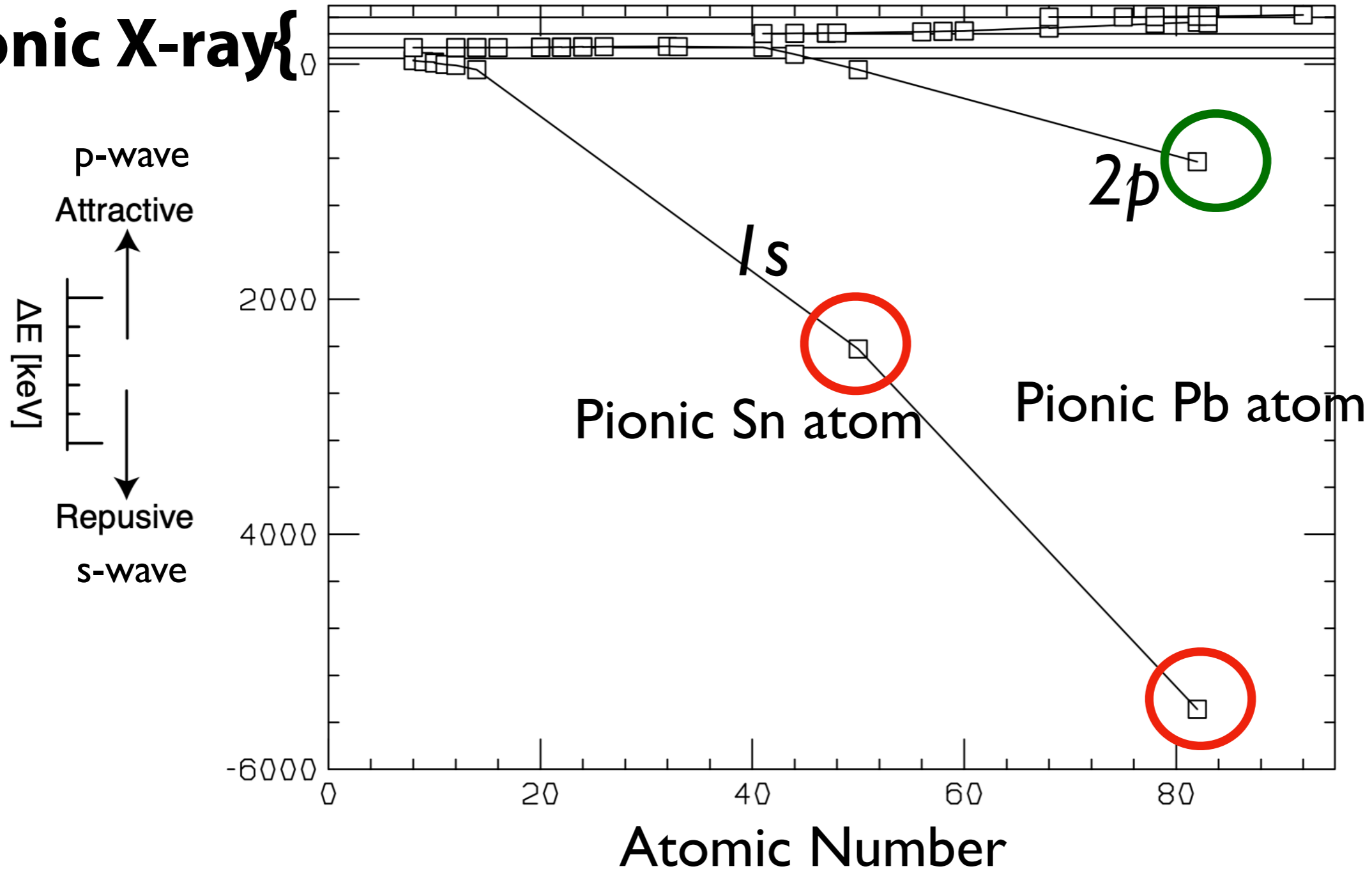
$$U_p(r) = \frac{2\pi}{\mu} \vec{\nabla} \cdot [c(r) + \varepsilon_2^{-1} C_0 \rho^2(r)] L(r) \vec{\nabla}$$

————→ **s-wave = repulsive = negative shift**

————→ **p-wave = attractive = positive shift**

Deeply bound pionic atoms Level shifts

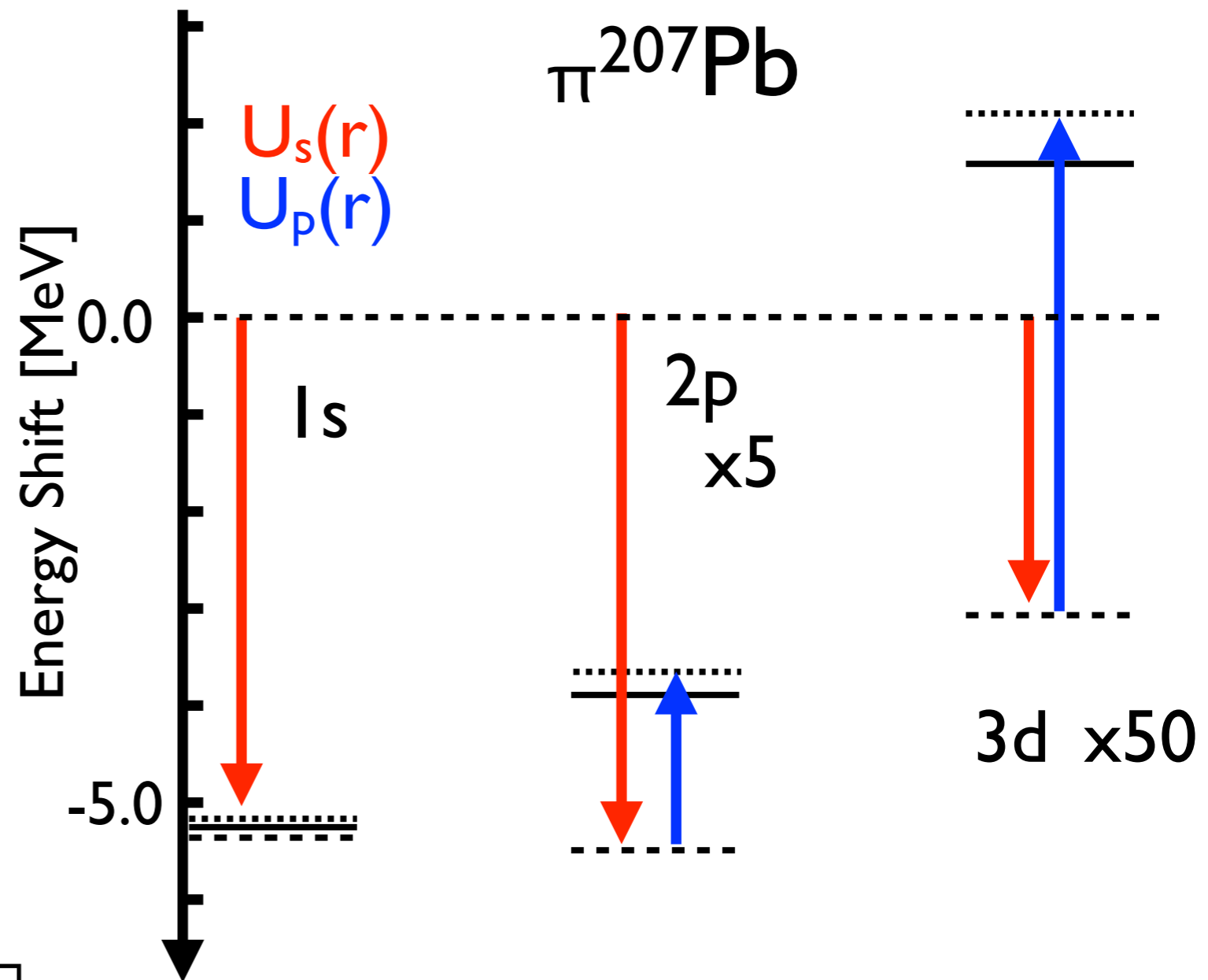
Pionic X-ray



Deeply bound atoms have "super" repulsive shifts and provide s-wave information

πA and π -nucleus interaction

Deeply bound states are sensitive to s-wave cf. Pionic X-rays are to p-wave



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s-wave interaction is dominant in **1s shift**, whereas p-wave is larger in 3d

PHYSICAL REVIEW C, VOLUME 62, 024606

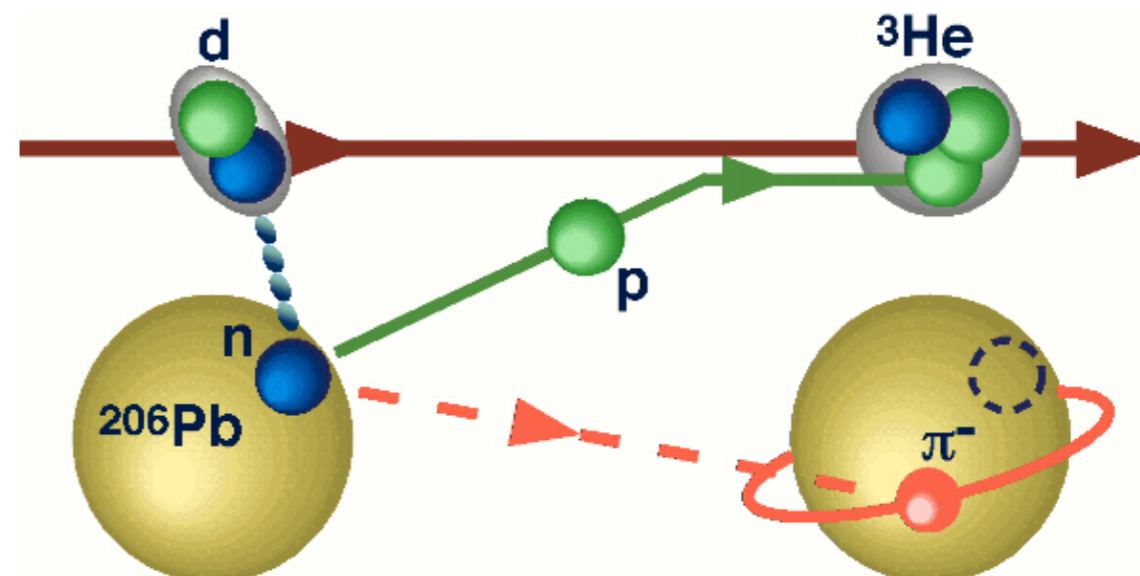
Isotope dependence of deeply bound pionic states in Sn and Pb

Y. Umemoto,¹ S. Hirenzaki,¹ K. Kume,¹ and H. Toki²

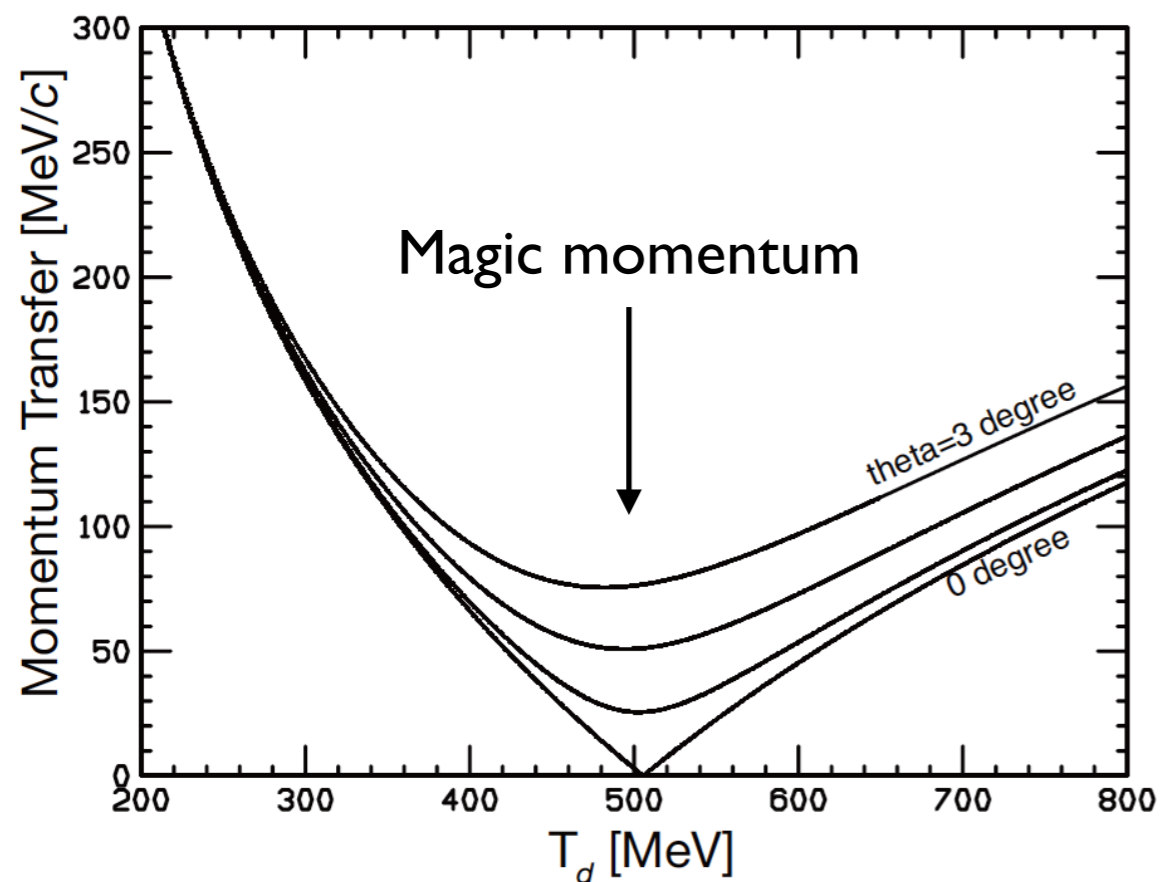
Spectroscopy of pionic atoms in $(d, {}^3\text{He})$ reactions

Missing mass spectroscopy to measure excitation spectrum of pionic atoms

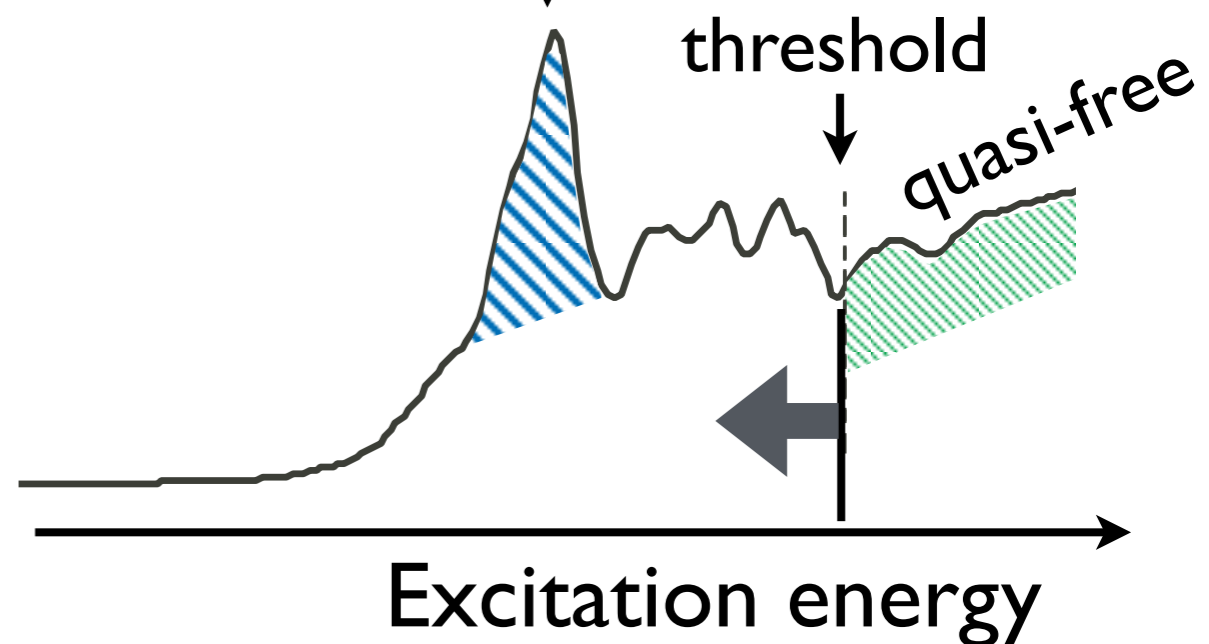
Direct production of pionic atoms



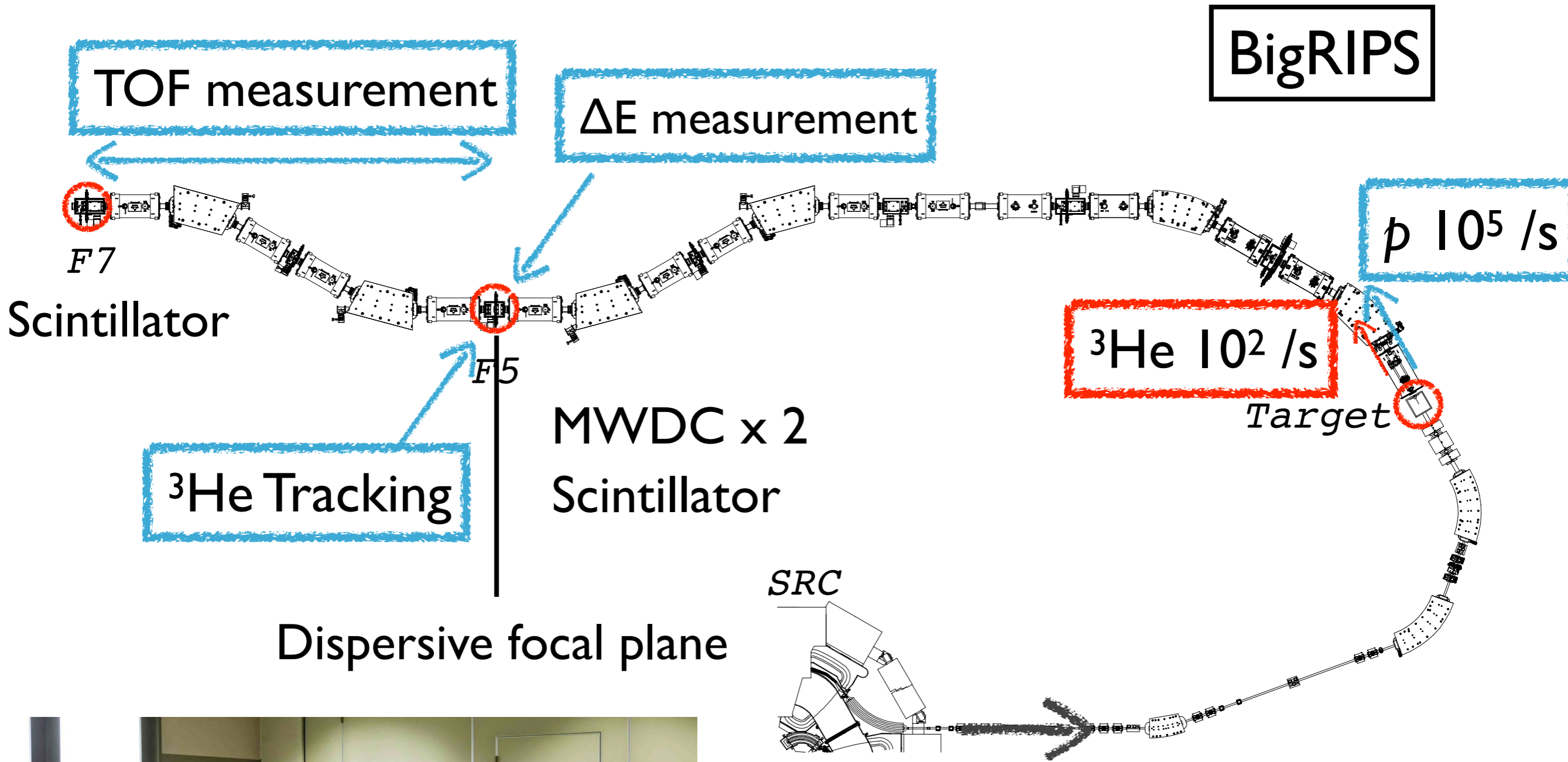
Momentum transfer



Pion bound state (coupled with n hole)



(d,³He) Reaction Spectroscopy in RIBF



d beam $> 10^{12}$ /s, 500 MeV



Wakohashi, RIKEN

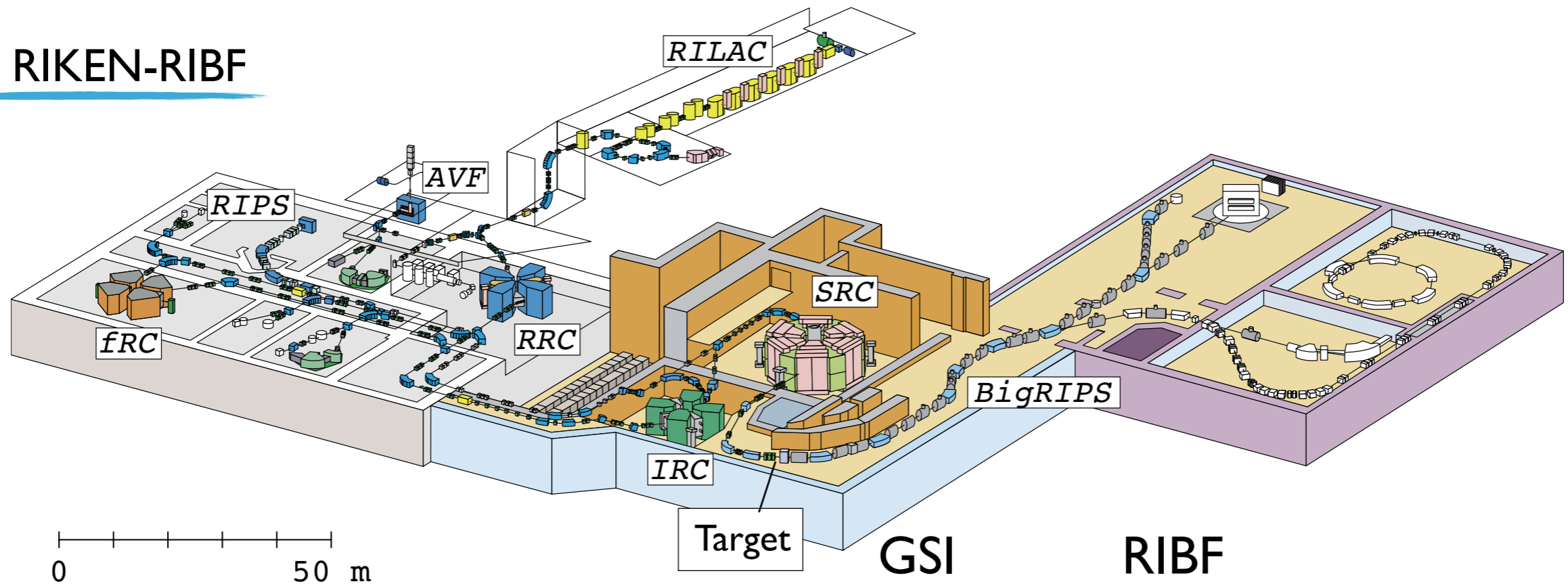
Reaction spectroscopy of pionic atom

Search for pionic atoms GSI-S160	1996	$^{208}\text{Pb}(d,^3\text{He})$
1s measurement GSI-S160	1998	$^{206}\text{Pb}(d,^3\text{He})$
Systematic run with Sn GSI-S236	2002	$^{116-124}\text{Sn}(d,^3\text{He})$
Pilot run at RIBF RIBF-27	2010	$^{122}\text{Sn}(d,^3\text{He})$
Production RIBF-54R1	2014	$^{117,122}\text{Sn}(d,^3\text{He})$
Systematic Measurement RIBF-135	2021	$^{112-124}\text{Sn}(d,^3\text{He})$
Inverse (pilot) RIBF-214		$\text{D}(^{136}\text{Xe},^3\text{He})$
Inverse		$\text{D}(\text{X}, ^3\text{He})$

$(p,2\text{He}), (p,2p)$ in RCNP

RI Beam Factory

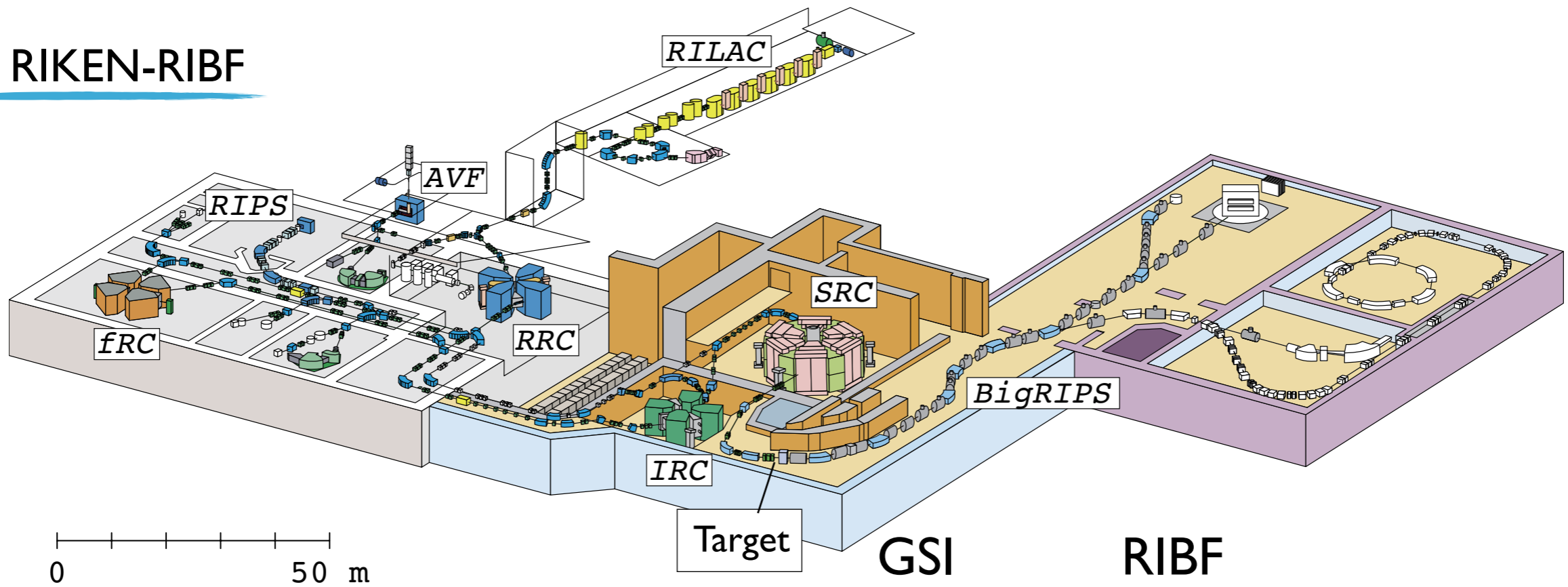
RIKEN-RIBF



	GSI	RIBF
d beam Intensity	$10^{11}/\text{spill}$	$> 10^{12}/\text{s}$
Target	$20 \text{ mg}/\text{cm}^2$	$10 \text{ mg}/\text{cm}^2$
$\Delta p_d/p_d$ (FWHM)	0.02%	0.06%
Resolution (FWHM)	400 keV	$\sim 1000 \text{ keV}$
Acceptance (mrad)	15H, 10V	40H, 60V

RI Beam Factory

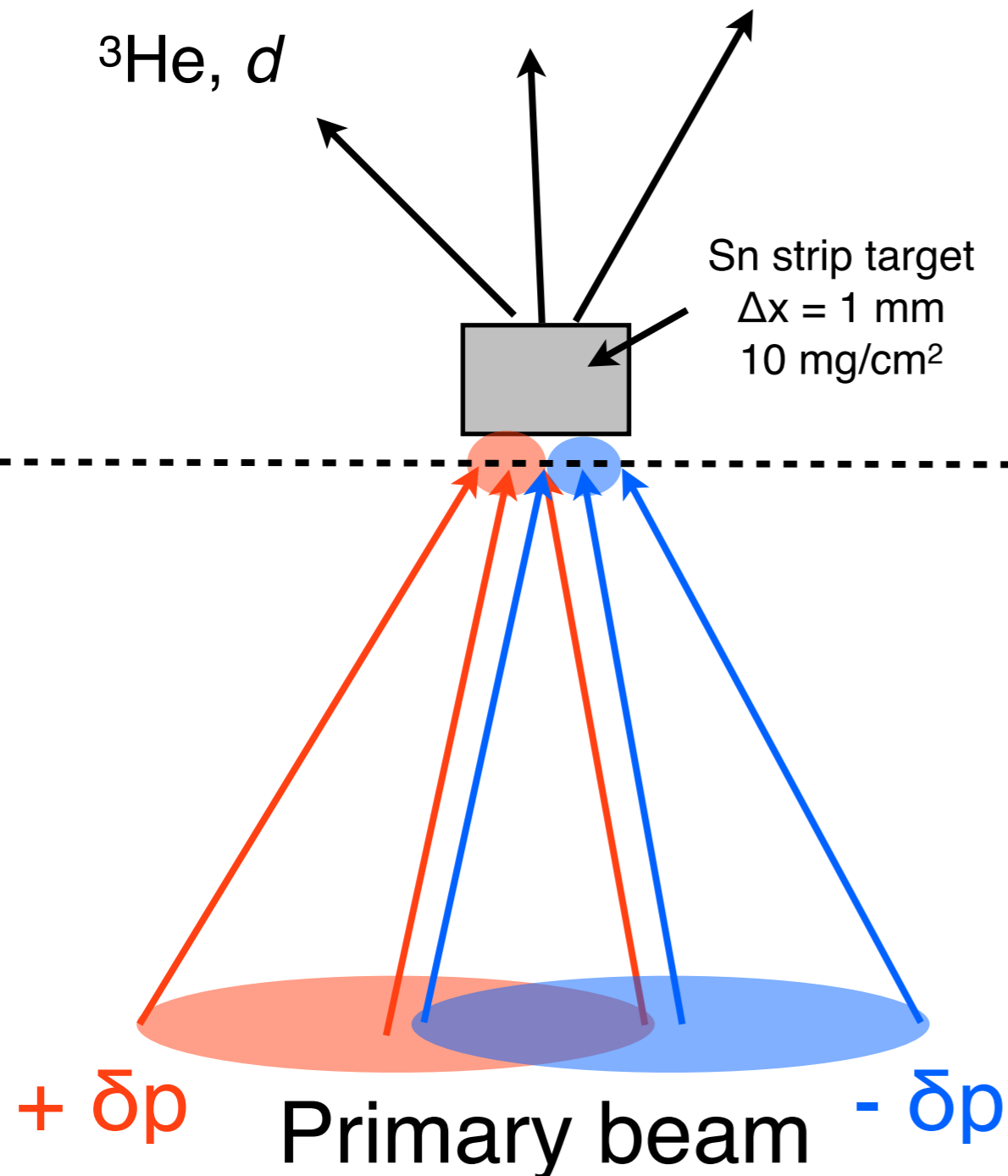
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Acceptance (mrad)	15H, 10V	40H, 60V

Dispersion matching

Resolution improvement technique



Dispersion matching

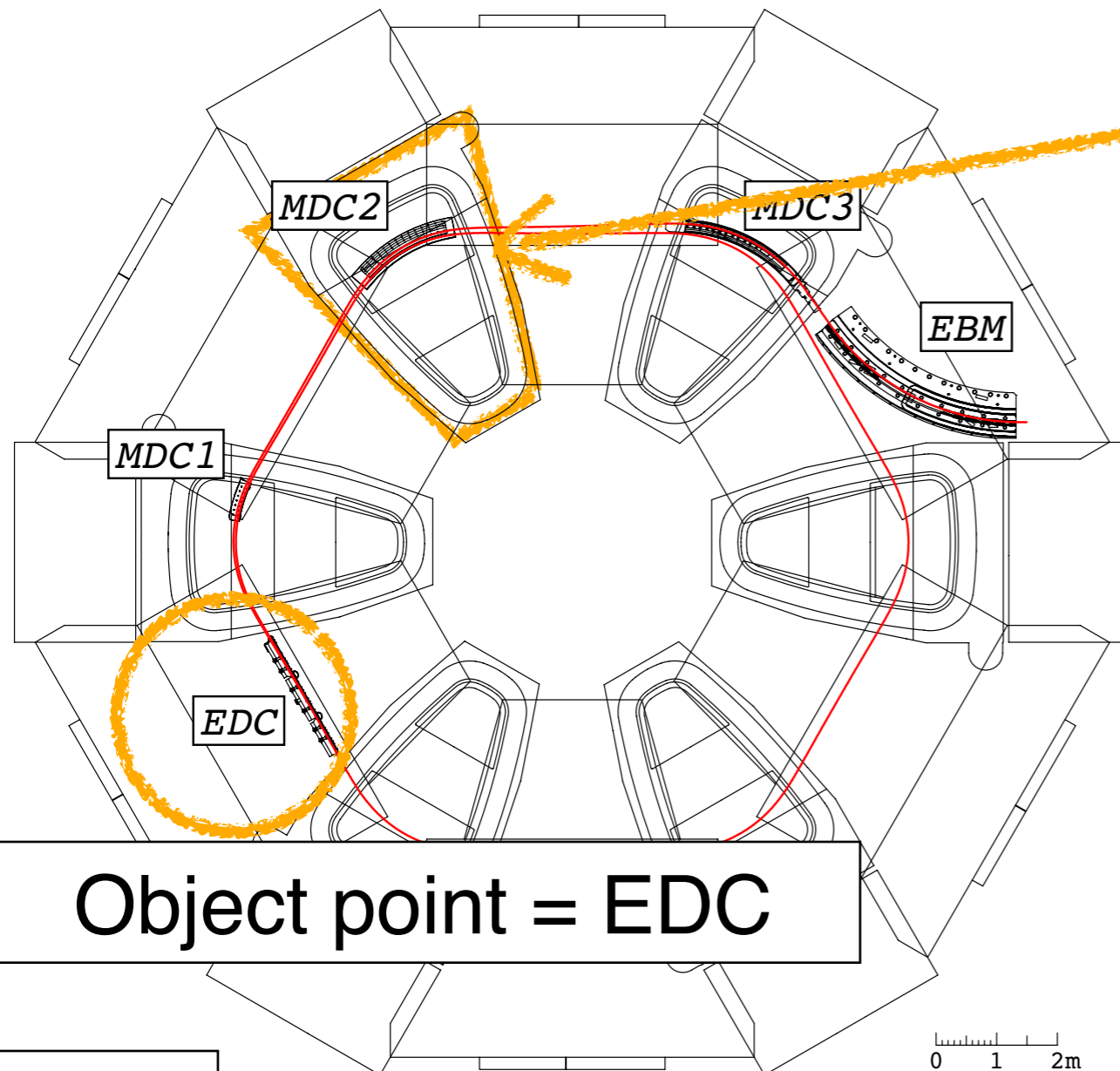
Analysis of beam energy in the beam line

← F0 (dispersive target position)
 $45 \text{ mm}/\%$

	pilot (2010)	2014
$\sigma_{p_{\text{primary}}} [\%]$	0.04	0.03
$\sigma_{X_{F0}} [\text{mm}]$	0.7	0.2
resolution _{exp} [keV]	500	280

Resolution improvement technique

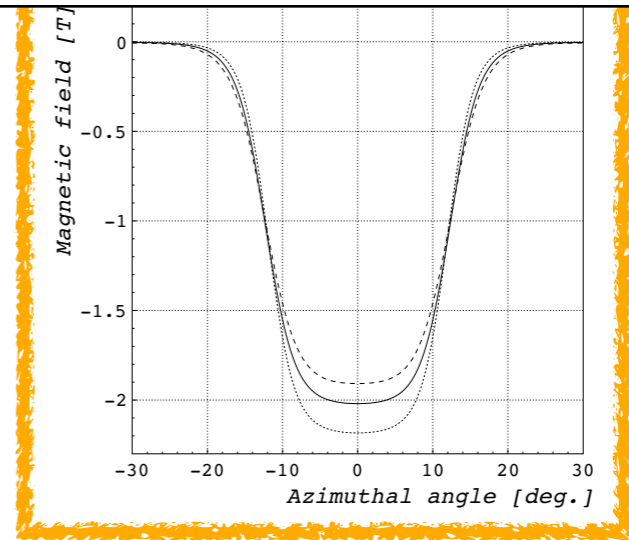
Dispersion matching using **primary beam**



Object point = EDC

SRC

magnetic field in the magnet



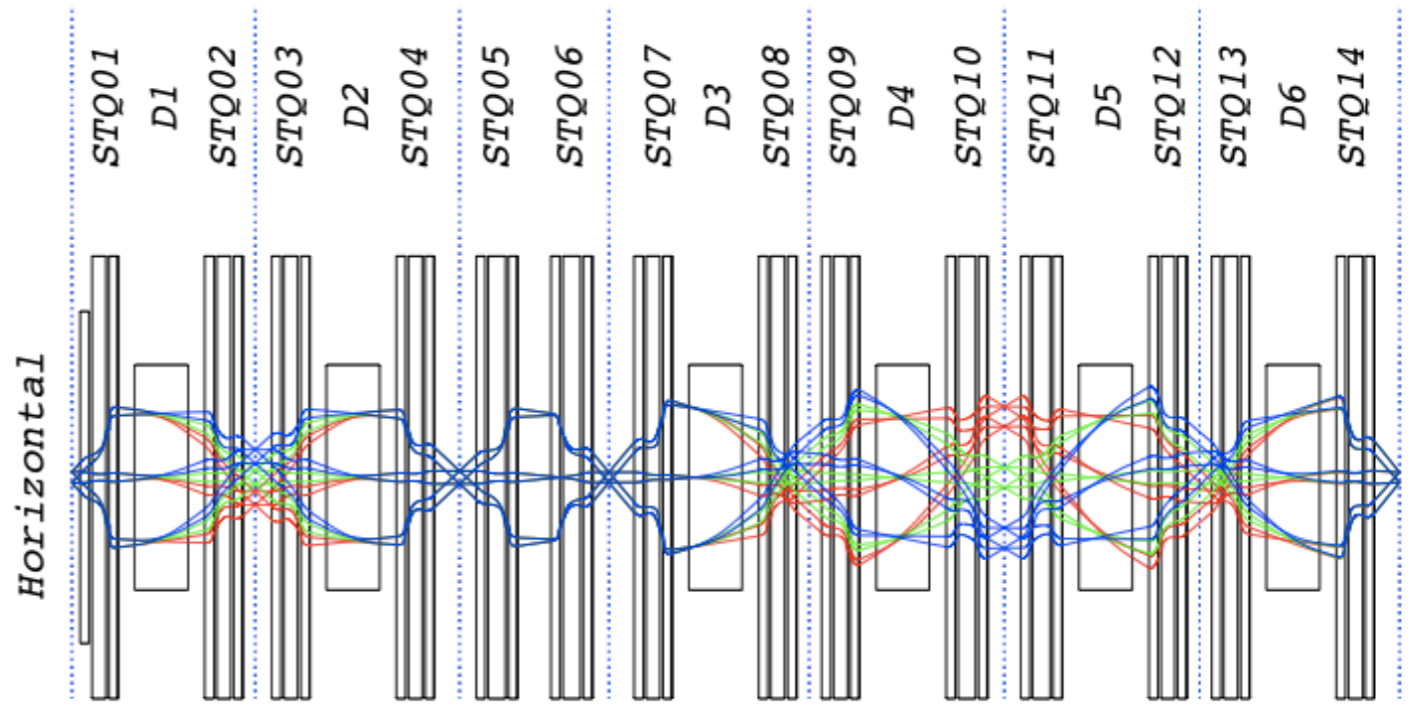
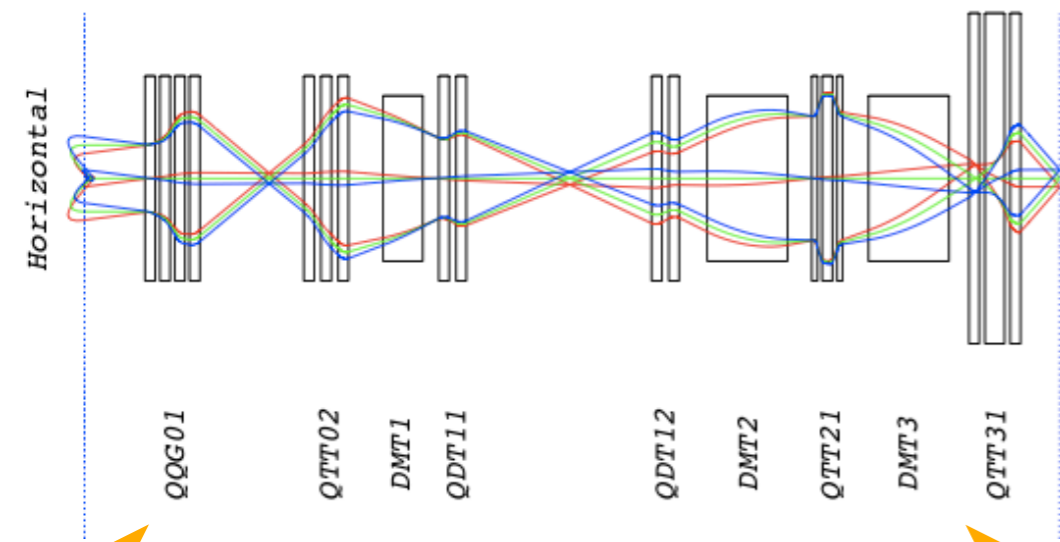
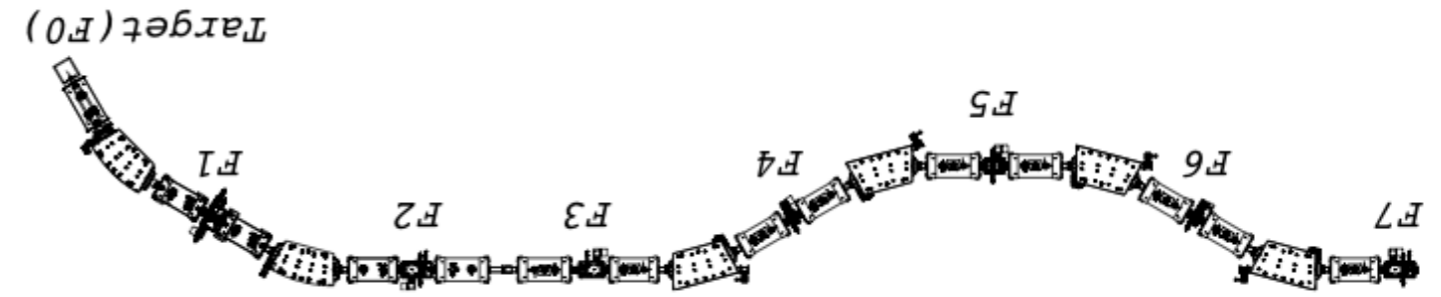
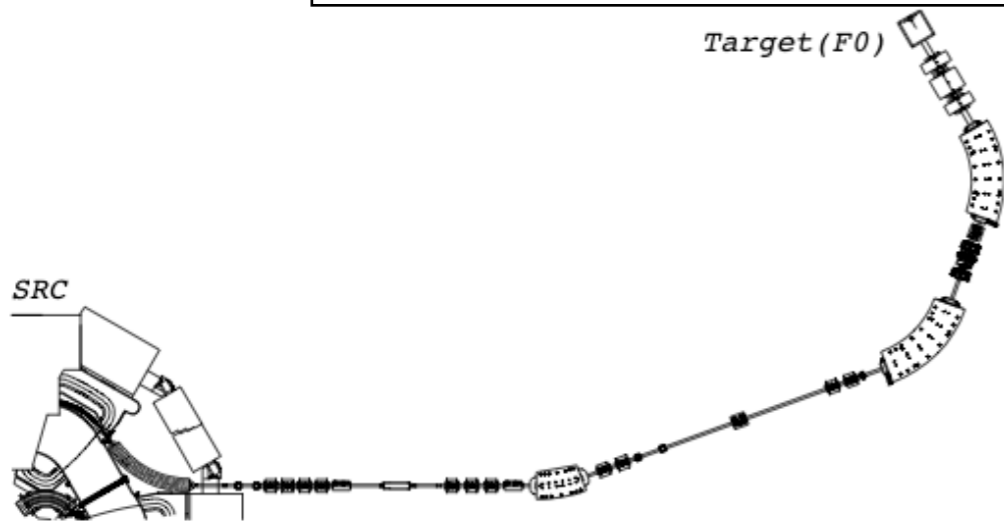
calculate the transfer matrix using Runge-Kutta method

$$\begin{pmatrix} (x|x) & (x|a) & (x|y) & (x|b) & (x|\delta) \\ (a|x) & (a|a) & (a|y) & (a|b) & (a|\delta) \\ (y|x) & (y|a) & (y|y) & (y|b) & (y|\delta) \\ (b|x) & (b|a) & (b|y) & (b|b) & (b|\delta) \end{pmatrix}_{\text{EDC} \rightarrow \text{EBM}} = \begin{pmatrix} -1.00 & -3.35 & 0.0 & 0.0 & 76.9 \\ 0.30 & -0.01 & 0.0 & 0.0 & -25.4 \\ 0.0 & 0.0 & -1.03 & -1.75 & 0.0 \\ 0.0 & 0.0 & -0.09 & -1.12 & 0.0 \end{pmatrix}$$

Resolution improvement technique

Beam Transfer line

BigRIPS



dispersion matching

Q analysis

pID

dispersion: 62 mm/%

Measured observable (= position at focal plane) reflects only Q-value

Resolution estimation

FWHM [keV]	2014	2021
Target thickness	110	30
Multiple scattering	120	45
Beam & optics	200	85
Total	~280	~100?

cf. 400 keV in GSI and in 2010

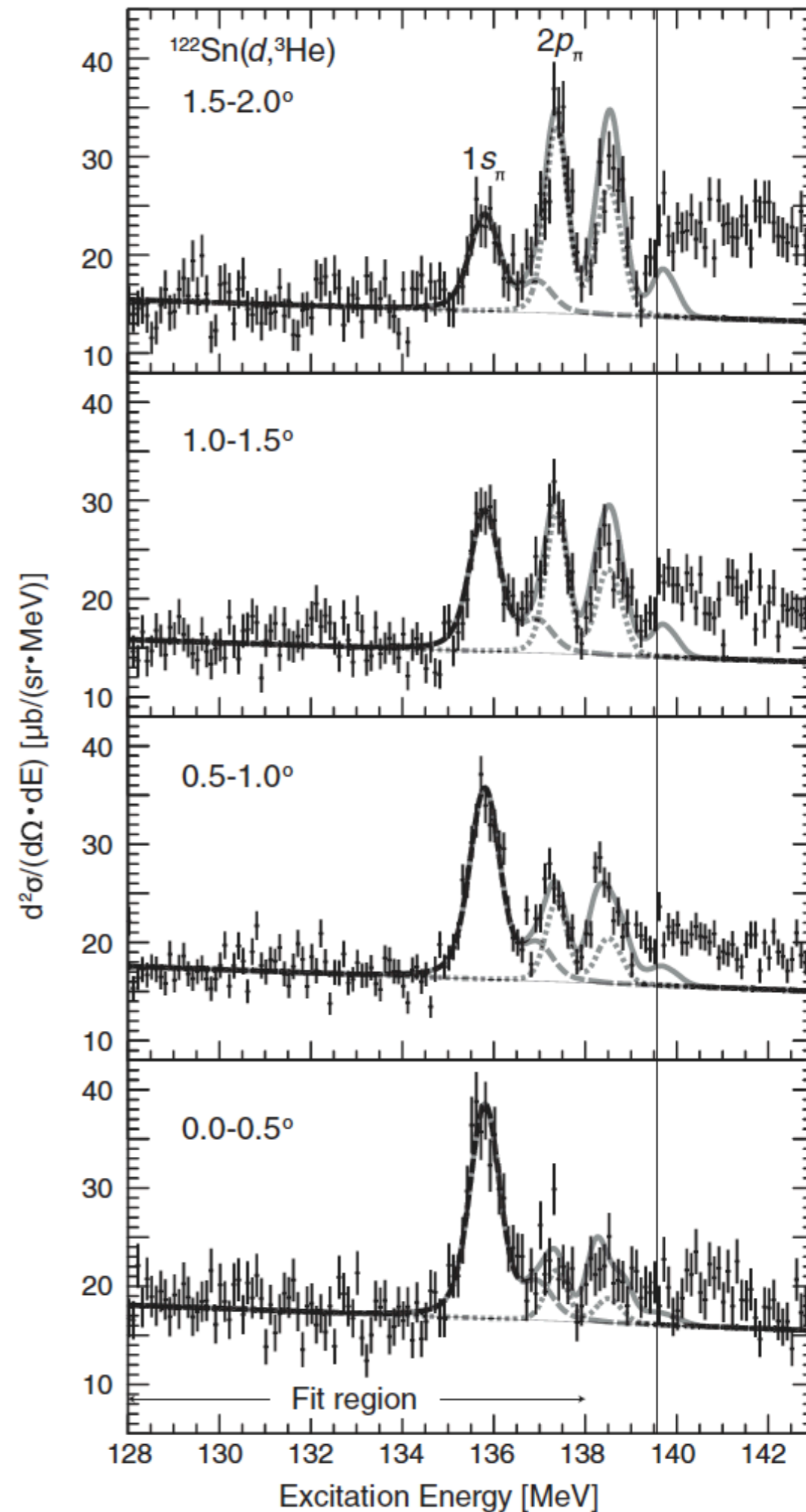
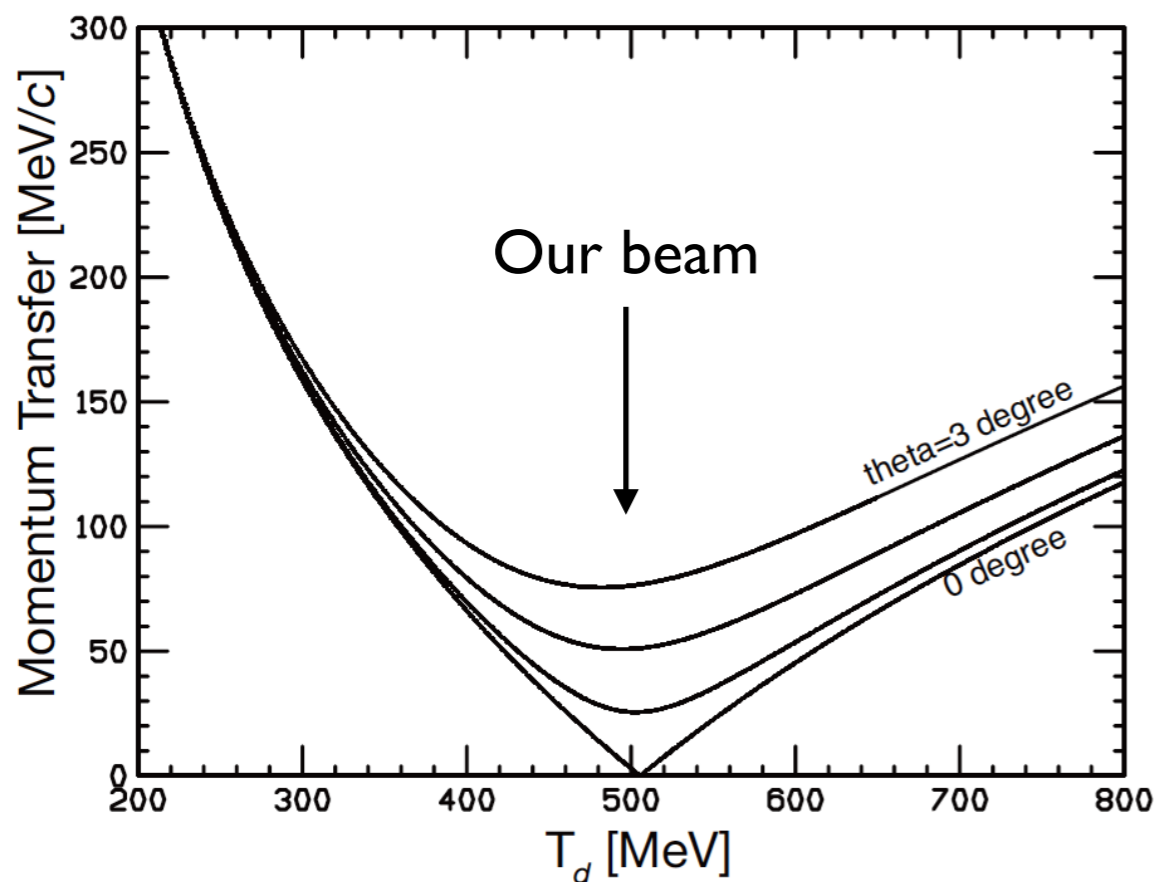
Pionic ^{121}Sn atom

Pilot run

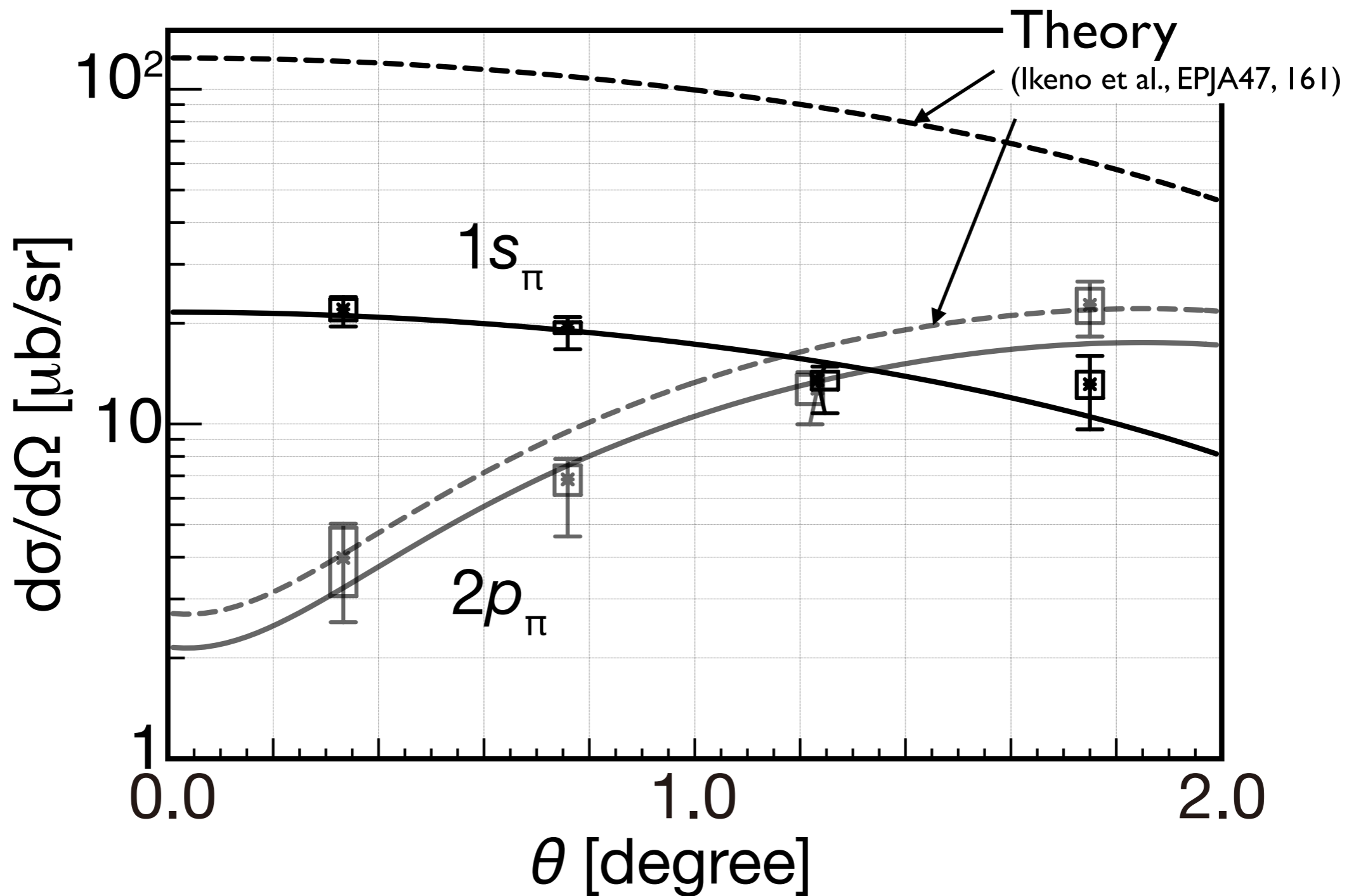
15 hours DAQ in 2010

First observation of
 θ dependence of
 π atom cross section

$$\Delta L \sim R \times q$$



1s and 2p pionic atom cross sections in (d, ³He)



θ dependence is well reproduced.
Theory calculates 5x larger cross section for 1s

Pionic ^{121}Sn atom

Pilot run

15 hours DAQ in 2010

First simultaneous $1s$ and $2p$ observation

$$B_{1s} = 3.828 \pm 0.013(\text{stat})_{-0.033}^{+0.036}(\text{syst}) \text{ MeV}$$

$$\Gamma_{1s} = 0.252 \pm 0.054(\text{stat})_{-0.070}^{+0.053}(\text{syst}) \text{ MeV}$$

$$B_{2p} = 2.238 \pm 0.015(\text{stat})_{-0.043}^{+0.046}(\text{syst}) \text{ MeV}$$

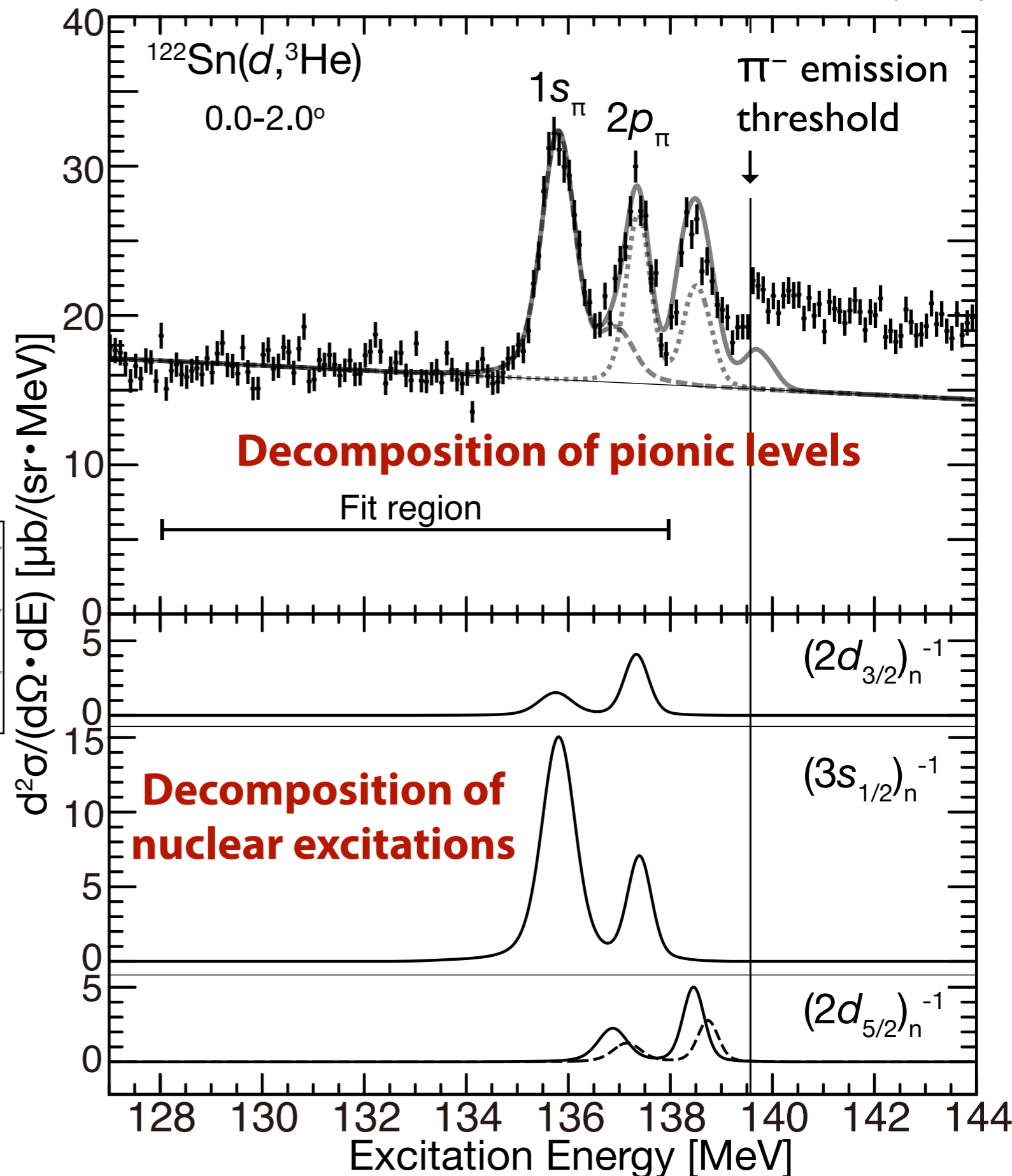
Resolution 394 keV (FWHM)

Theories

$$B_{1s} = 3.787\text{--}3.850 \text{ MeV}$$

$$\Gamma_{1s} = 0.306\text{--}0.324 \text{ MeV}$$

$$B_{2p} = 2.257\text{--}2.276 \text{ MeV}$$

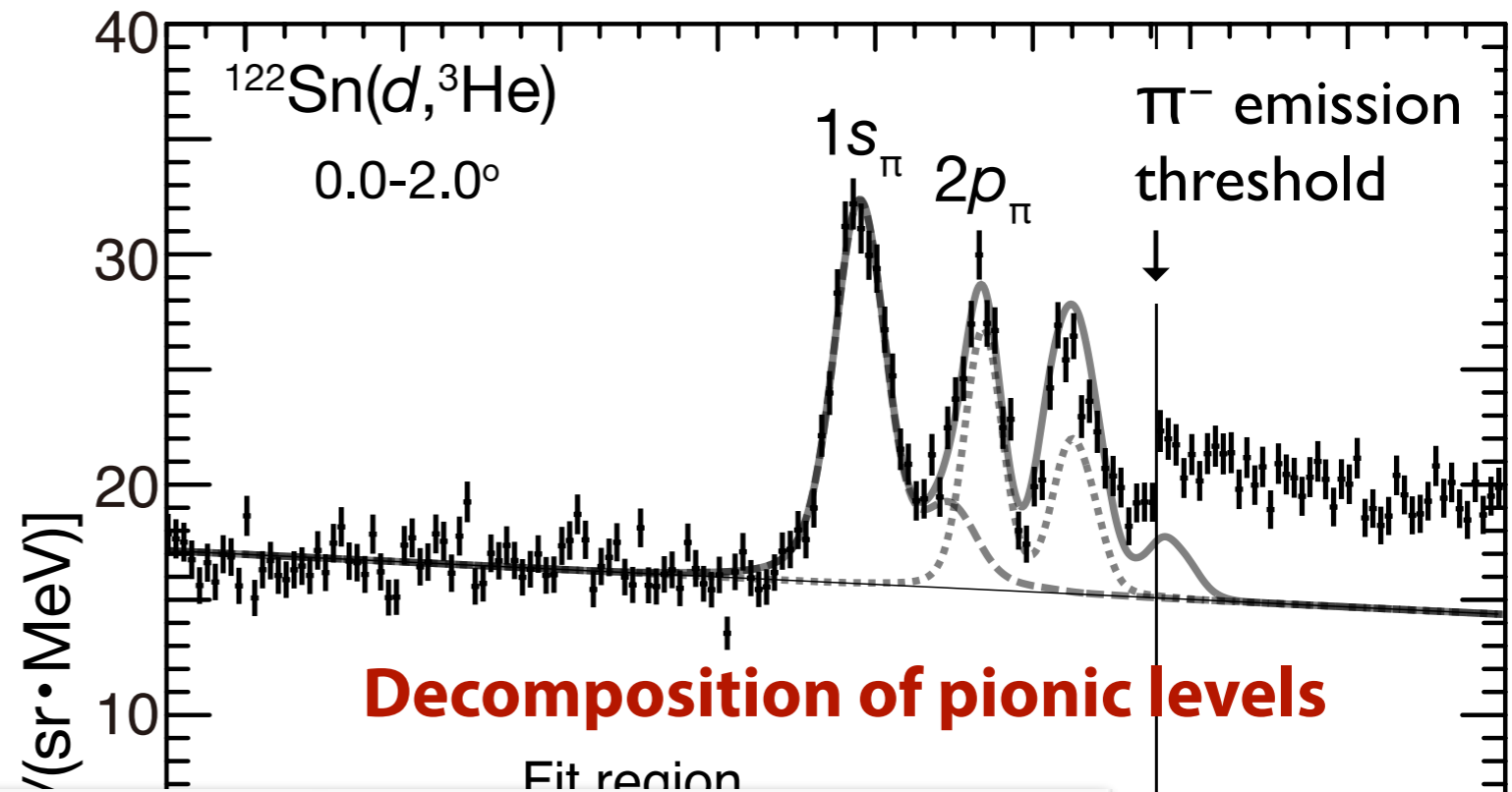


Pionic ^{121}Sn atom

Pilot run

15 hours DAQ in 2010

First simultaneous $1s$ and $2p$ observation



$$B_{1s} = 3.828 \pm 0.0$$

$$\Gamma_{1s} = 0.252 \pm 0.0$$

$$B_{2p} = 2.238 \pm 0.015(\text{stat})^{+0.046}_{-0.043}(\text{syst}) \text{ MeV}$$

However, precision was not enough...

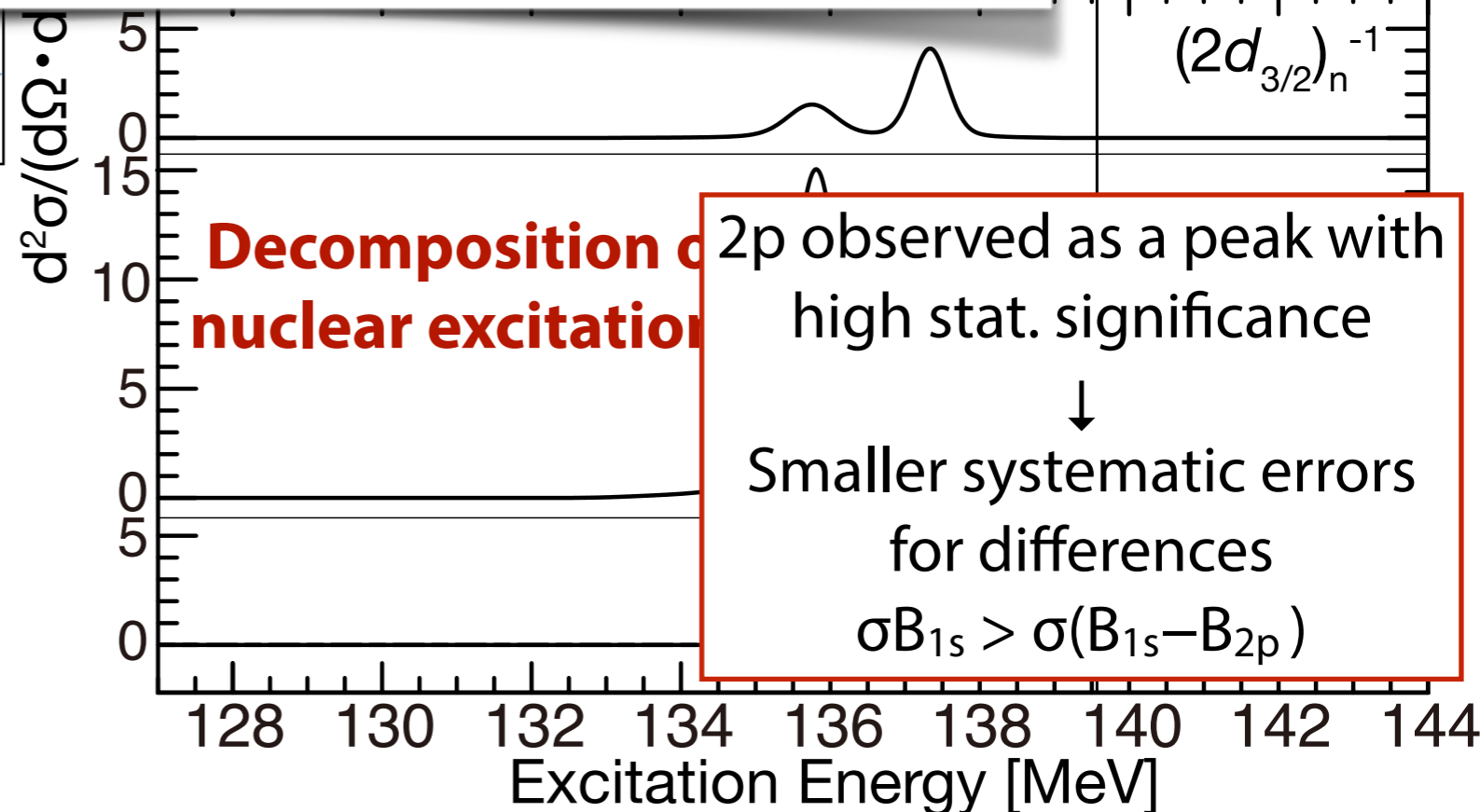
Resolution 394 keV (FWHM)

Theories

$$B_{1s} = 3.787\text{--}3.850 \text{ MeV}$$

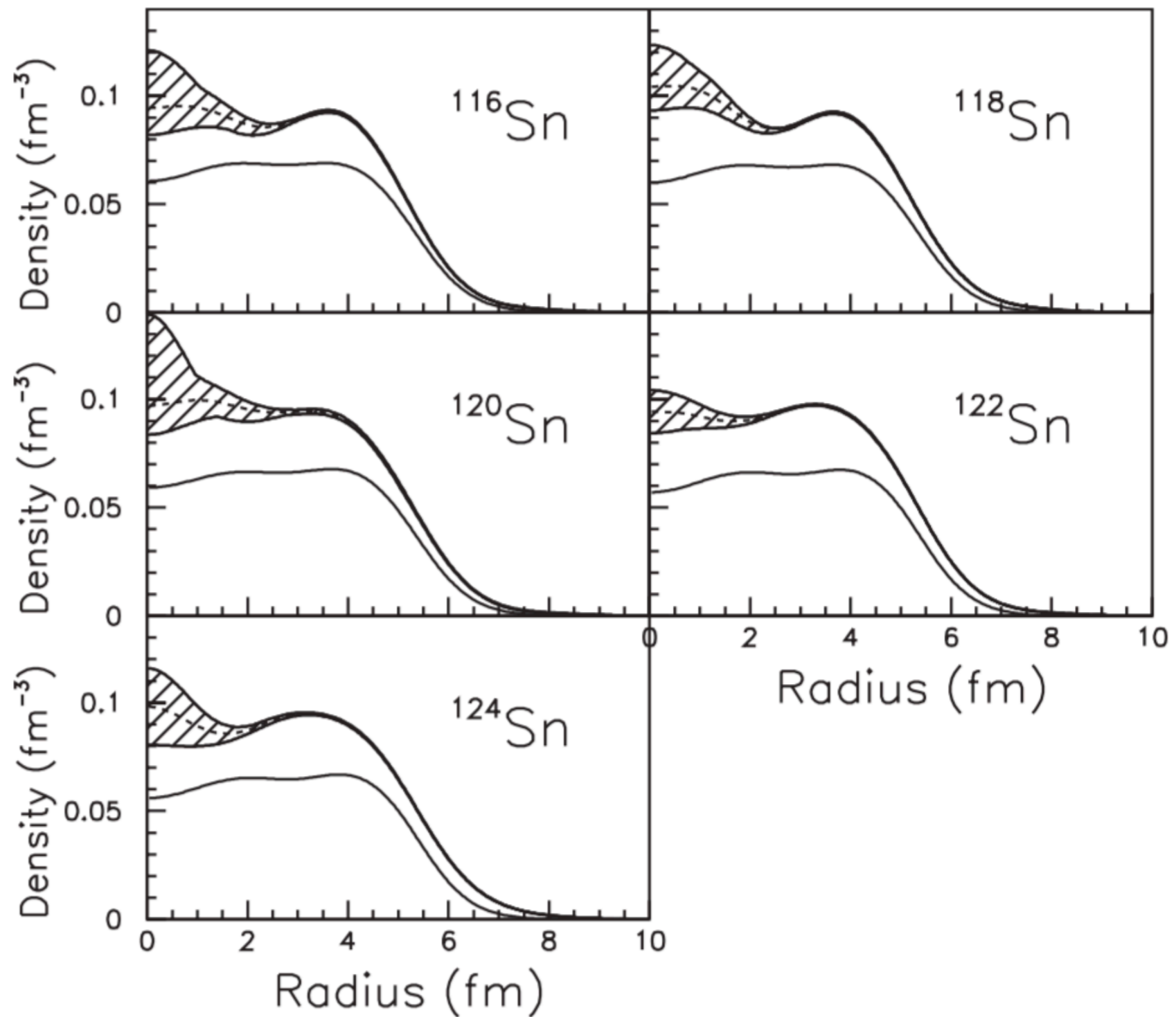
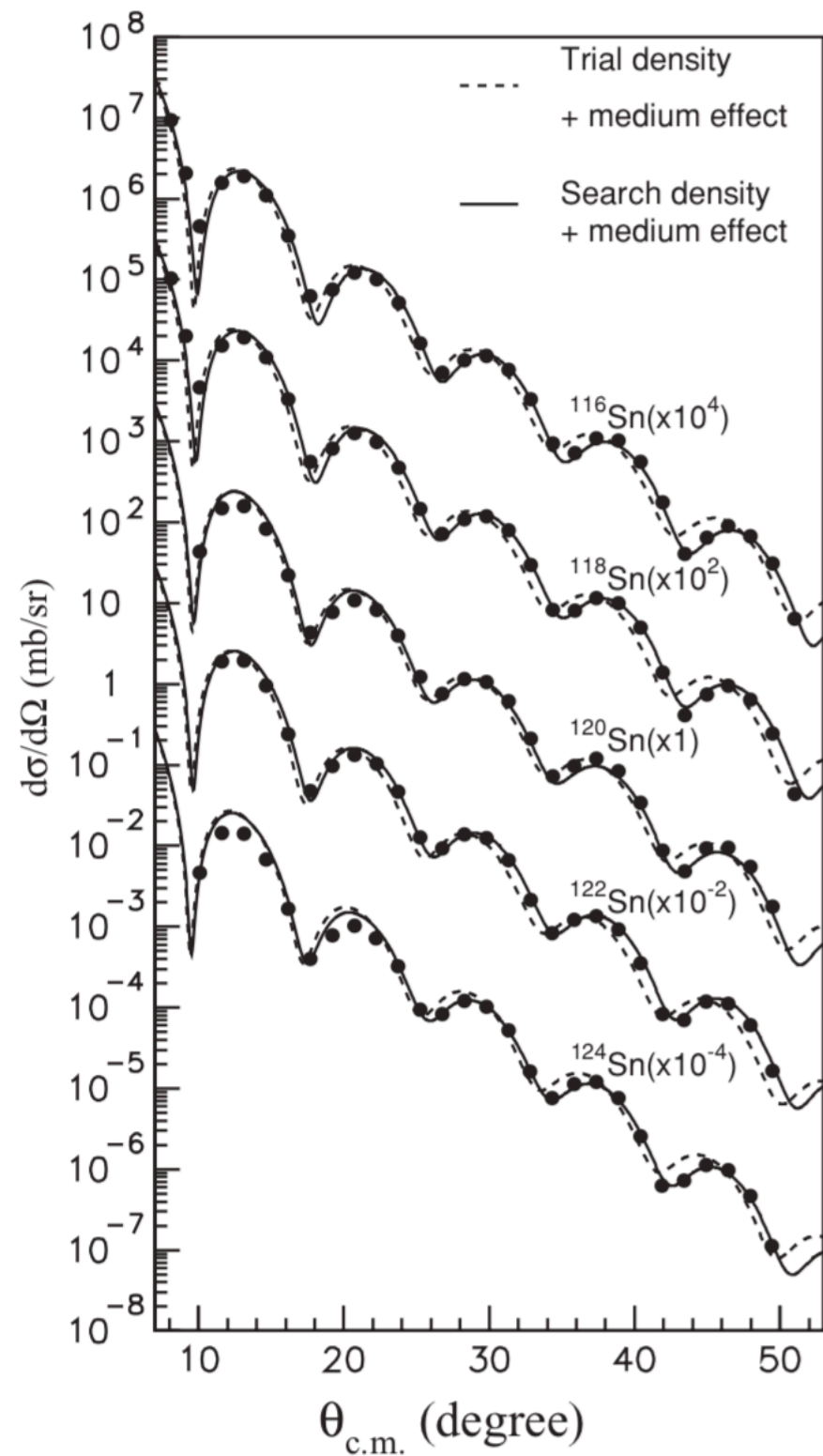
$$\Gamma_{1s} = 0.306\text{--}0.324 \text{ MeV}$$

$$B_{2p} = 2.257\text{--}2.276 \text{ MeV}$$



Measured nuclear density distribution of Sn isotopes

Sn(p,p') reaction at RCNP, Osaka



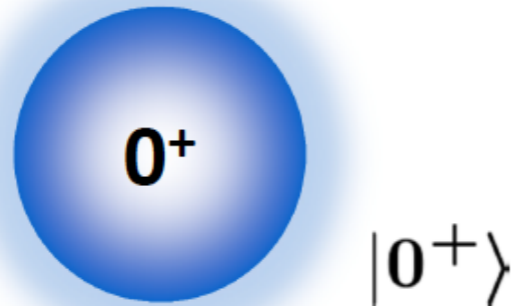
Residual interaction

Formulation: Even vs. Odd target

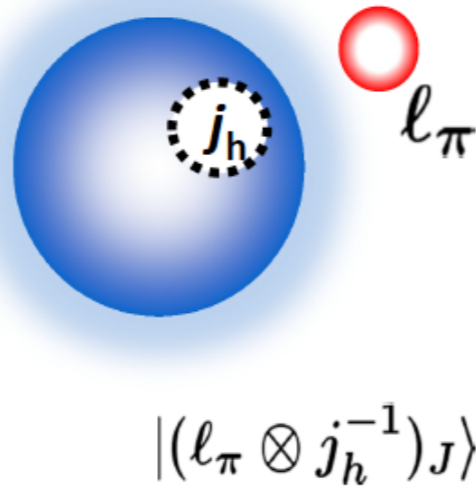
➤ Effective Number

Even target: $^{122}\text{Sn} (0^+)$

Initial:

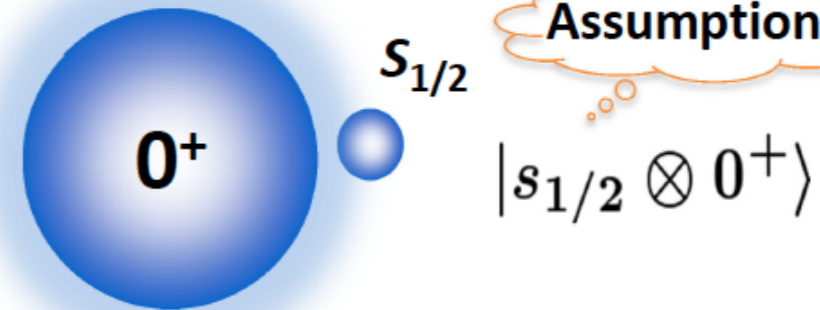


Final:



Odd target: $^{117, 119}\text{Sn} (1/2^+)$

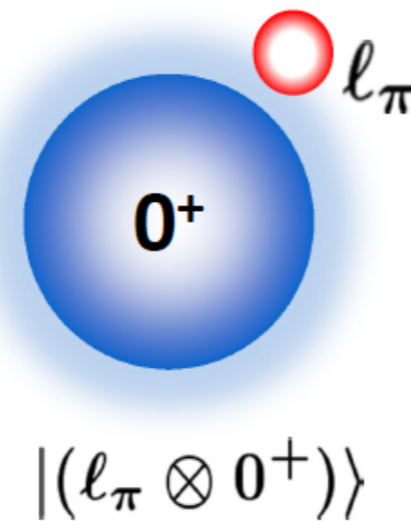
Initial:



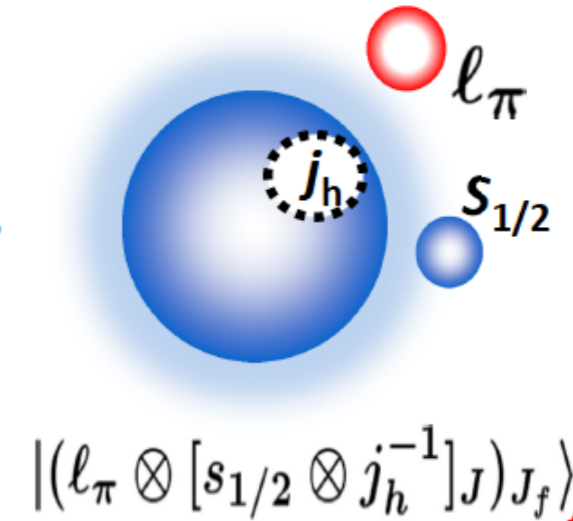
Final:

(1) neutron pick-up from $s_{1/2}$ orbit

(2) neutron pick-up j_h orbit from other than $s_{1/2}$



+



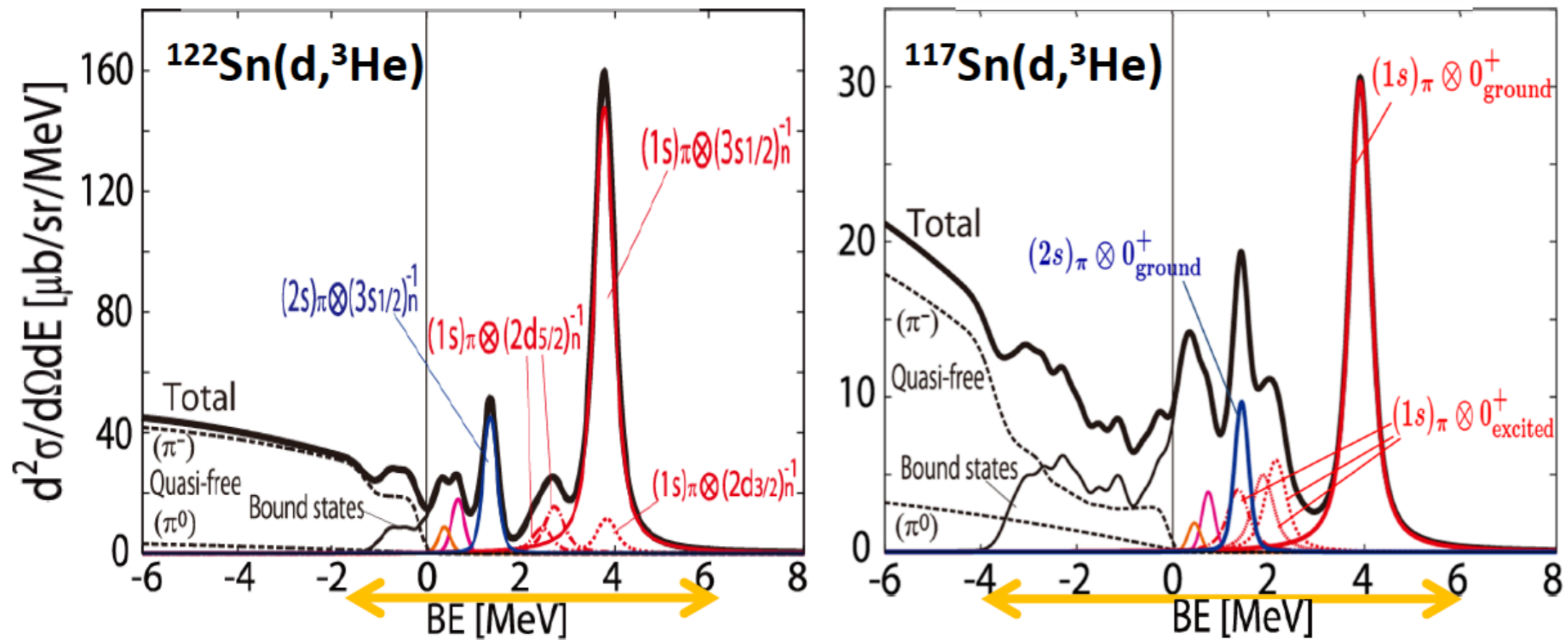
Theoretical predictions

Numerical Results: Even vs. Odd target

0 degrees

Even target: $^{122}\text{Sn} (0^+)$

Odd target: $^{117}\text{Sn} (1/2^+)$



- Pionic 1s state formation with neutron s-hole state is large in both spectra.
- Bound pionic state formation spectra in $^{117}\text{Sn}(d,^3\text{He})$ are spread over wider energy range.
- Absolute value of cross section in $^{117}\text{Sn}(d,^3\text{He})$ is smaller.

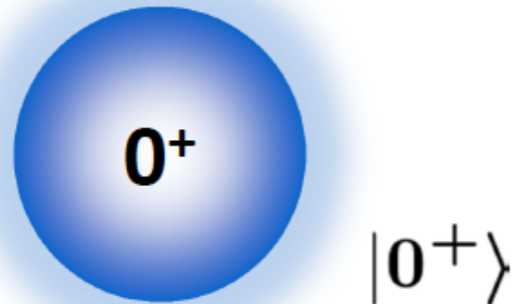
Residual interaction

Formulation: Even vs. Odd target

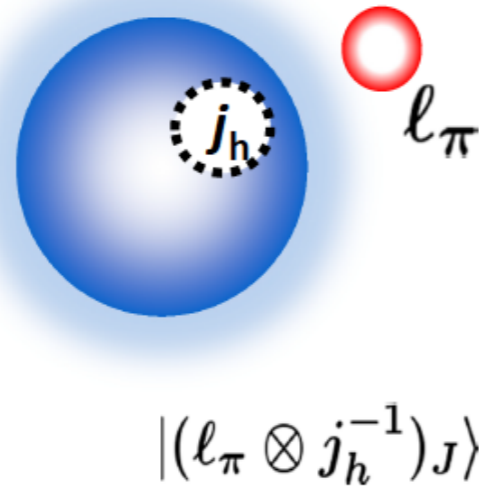
➤ Effective Number

Even target: $^{122}\text{Sn} (0^+)$

Initial:



Final:



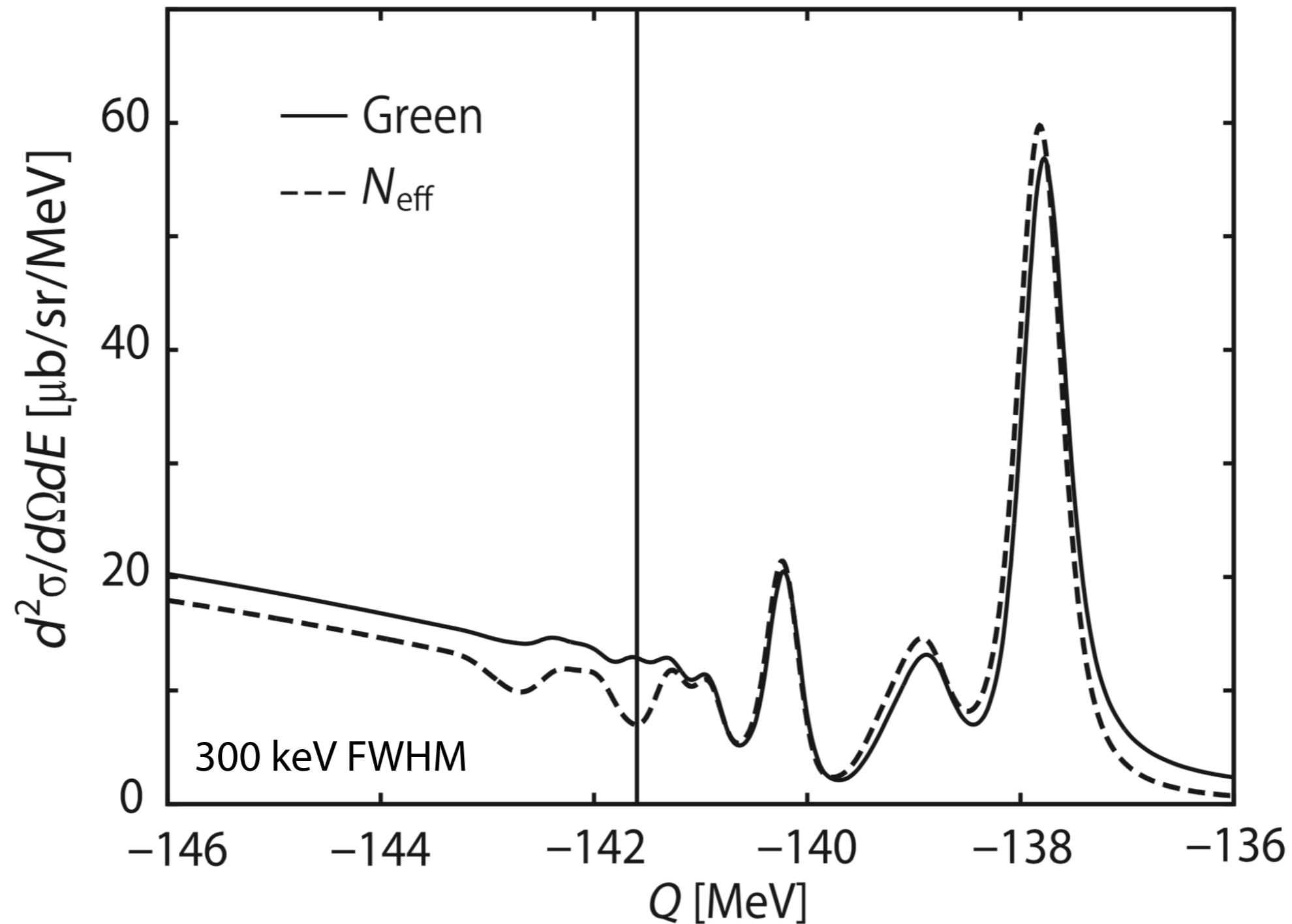
Nose-Togawa et al., PRC71, 061601(R) (2005)

TABLE V. Calculated complex energy shifts because of the residual interaction in ^{131}Sn . The results are shown in units of kilo-electron-volts for $[(1s)_\pi \otimes j_n^{-1}]_J$ and $[(2p)_\pi \otimes j_n^{-1}]_J$, including the s -wave and the p -wave parts of the pion neutron-hole residual interaction.

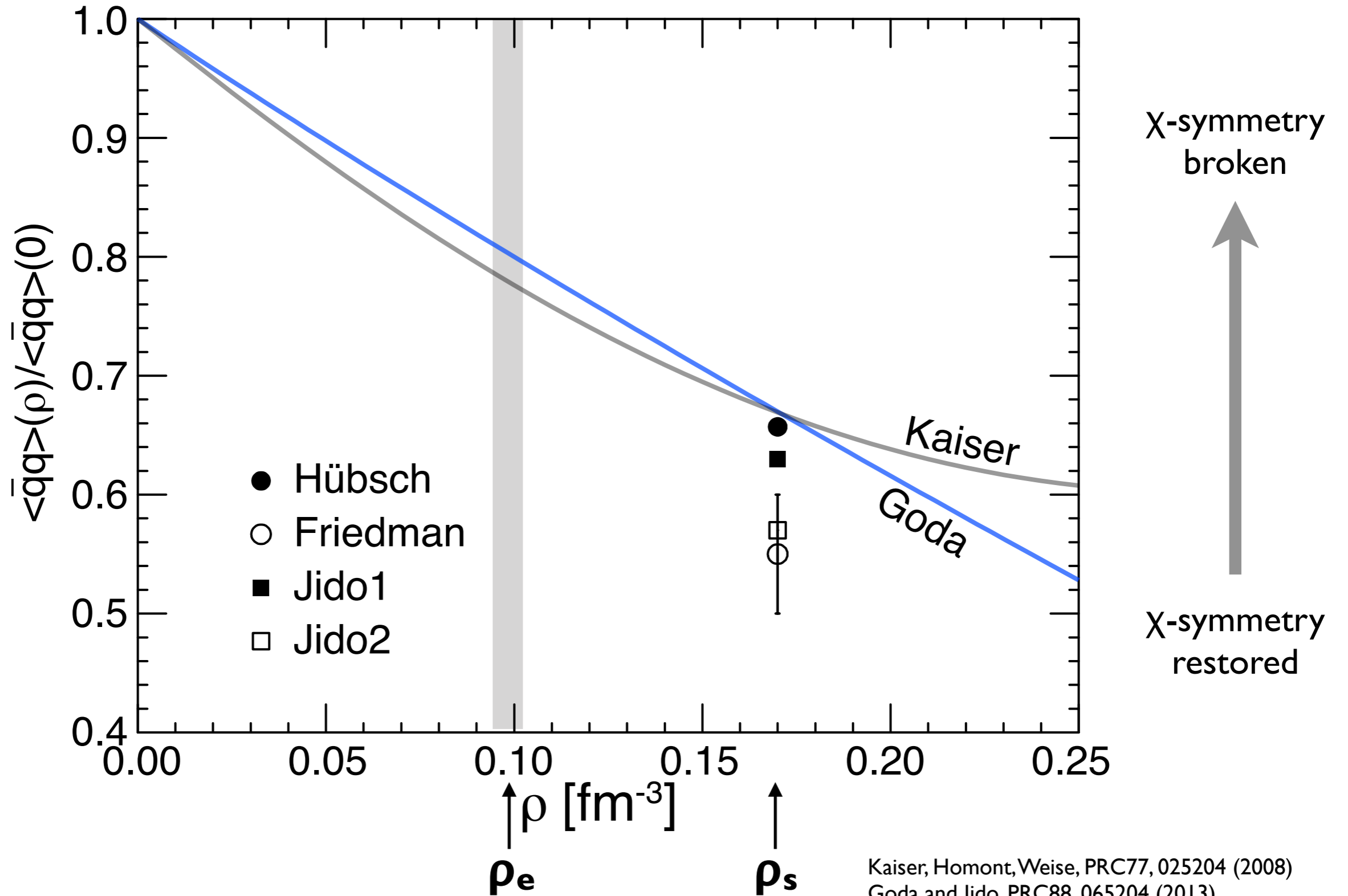
	$1s$		$2p$
$s_{1/2}^{-1}$	$-10.5 - 1.3i$	$J = 1/2$	$-3.2 - 0.6i$
		$J = 3/2$	$-3.3 - 0.6i$
$d_{3/2}^{-1}$	$-10.4 - 2.1i$	$J = 1/2$	$-7.1 - 2.0i$
		$J = 3/2$	$0.2 + 0.0i$
		$J = 5/2$	$-3.8 - 1.1i$
$g_{7/2}^{-1}$	$-6.5 - 1.6i$	$J = 5/2$	$-3.0 - 1.2i$
		$J = 7/2$	$0.9 + 0.4i$
		$J = 9/2$	$-2.1 - 0.8i$
$h_{11/2}^{-1}$	$-9.6 - 2.6i$	$J = 9/2$	$-4.6 - 1.8i$
		$J = 11/2$	$1.1 + 0.4i$
		$J = 13/2$	$-3.7 - 1.4i$
$d_{5/2}^{-1}$	$-9.9 - 1.9i$	$J = 3/2$	$-5.8 - 1.5i$
		$J = 5/2$	$0.6 + 0.2i$
		$J = 7/2$	$-3.9 - 1.1i$

Effect of $\sim 10\text{keV}$

$^{122}\text{Sn}(d,^3\text{He})$ spectra calculated with Neff and Green's function methods



ρ dependence of chiral condensate



Kaiser, Homont, Weise, PRC77, 025204 (2008)
 Goda and Jido, PRC88, 065204 (2013)
 Huebsch, Jido, PRC104, 015202 (2021)
 Friedman, Gal, PLB792, 340 (2019)
 Jido, Hatsuda, Kunihiro, PLB670, 109 (2008)
 Lacour, Oller, Meissner, J. Phys. G. 37, 125002 (2010)

Summary

- The binding energies and widths of the $1s$ and $2p$ states in $\text{Sn}121$ were determined with very high precision. Difference between the $1s$ and $2p$ values reduces the systematic errors drastically.
- Recent theoretical progress was adopted for the $\langle \bar{q}q \rangle$ evaluation, which directly relates the chiral condensate and the pion-nucleus interaction.
- We calculated various corrections for the first time and applied them. The application made a jump of the deduced chiral condensate. After the corrections, the chiral condensate ratio was deduced with much higher reliability.
- We conducted measurement of ρ dependence of chiral condensate in systematic study. We plan measurement with “inverse kinematic” reactions for pionic xenon, which leads to future experiments for pionic unstable nuclei.