

# Mesic Nuclei Formation by $(\gamma, p)$ reactions

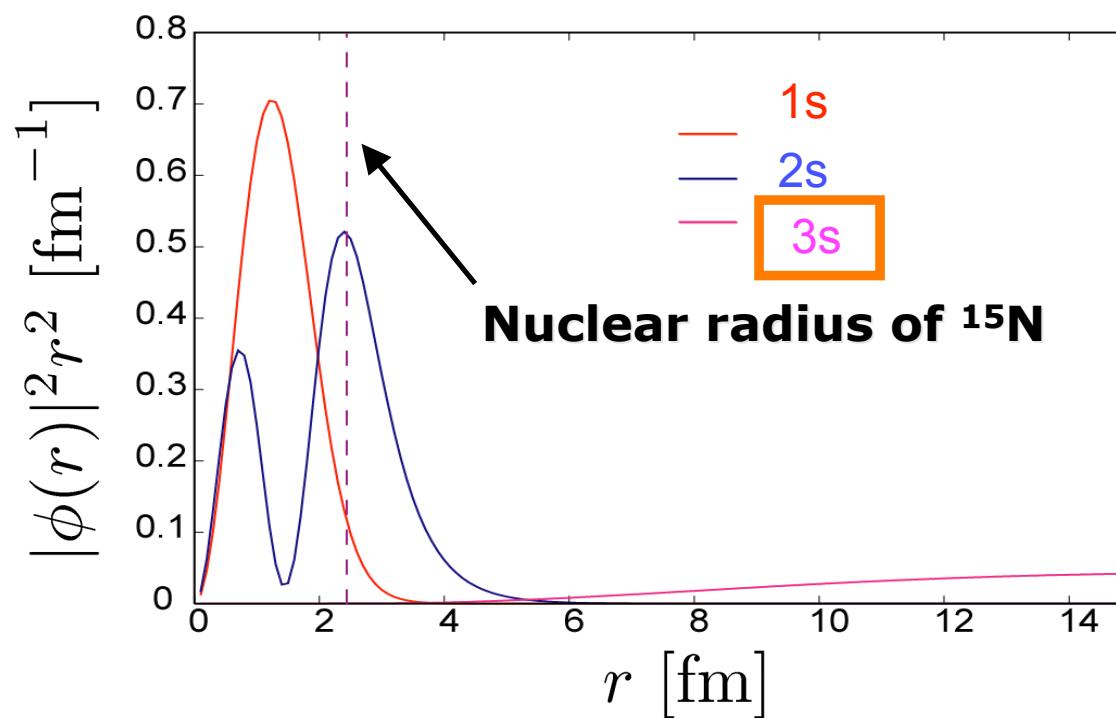
Satoru Hirenzaki  
(Nara Women's Univ.)

- 1. Introduction and Motivation
- 2. Missing Mass Spectroscopy (ex.  $\pi$  atoms)
- 3. Recent Topics  
 $(\eta, \omega, \eta')$
- 4. Summary

# 1. Introduction and Motivation

## ➤ Object

- Hadron – Nucleus bound systems.
    - Coulomb + Strong ⋯ Exotic Atoms  
(Deeply Bound)  $\pi$  atom, Kaonic Atom,  $\bar{p}$  atom ...
    - Strong ⋯ Exotic Nuclei  
Mesic Nuclei, Hypernuclei, ...

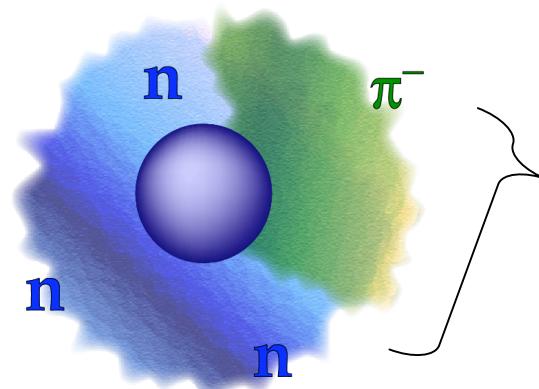


# Kaonic Atoms And Kaonic Nuclei

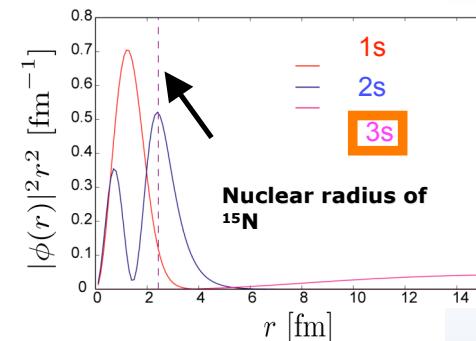
# 1. Introduction and Motivation

## ➤ 1. Exotic Many Body Physics

Ex.)



Pionic Atoms in halo nuclei  
Co-existence of Pion-Neutron-halo



## ➤ 2. Hadron Physics at finite density

Fundamental theory (QCD)

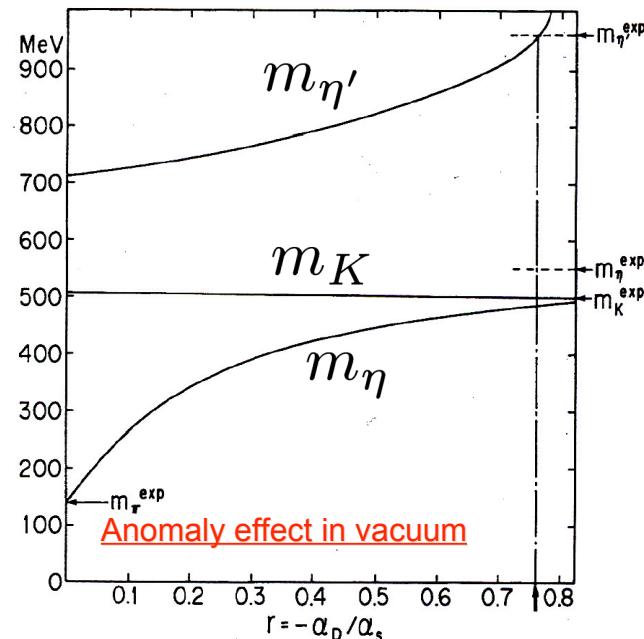
( $\longleftrightarrow$  Effective theory)

$\longleftrightarrow$  Hadron property at finite  $\rho$

$\longleftrightarrow$  Infinite System  $\longleftrightarrow$  Finite System

$\longleftrightarrow$  Mesic Atoms and Mesic Nuclei

Kunihiro, Hatsuda, PLB206(88)385, Fig.3



- Higgs mechanism
- Spontaneous Chiral Symmetry Breaking
- $U_A(1)$  Anomaly Effect

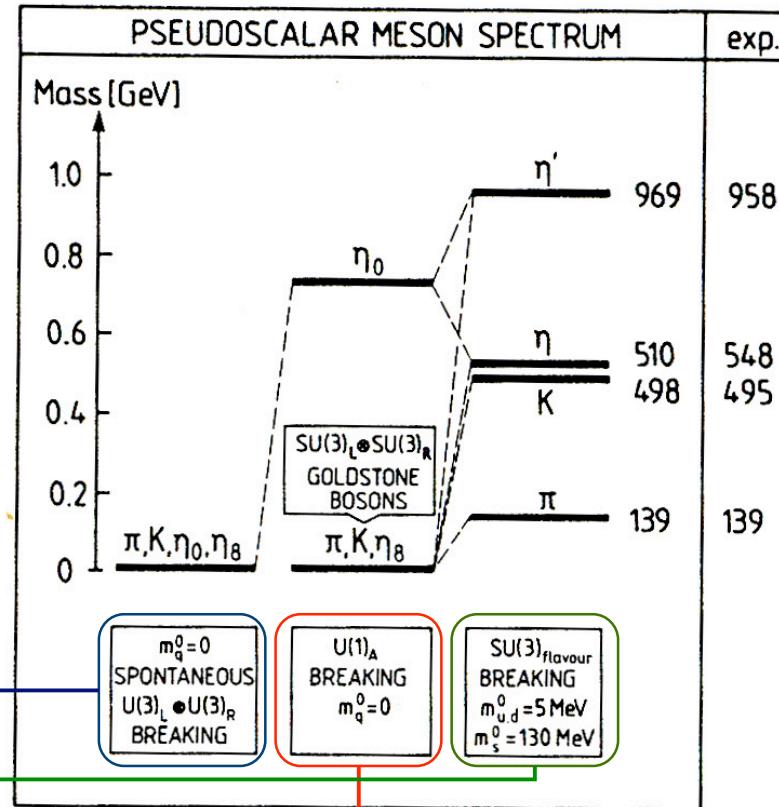
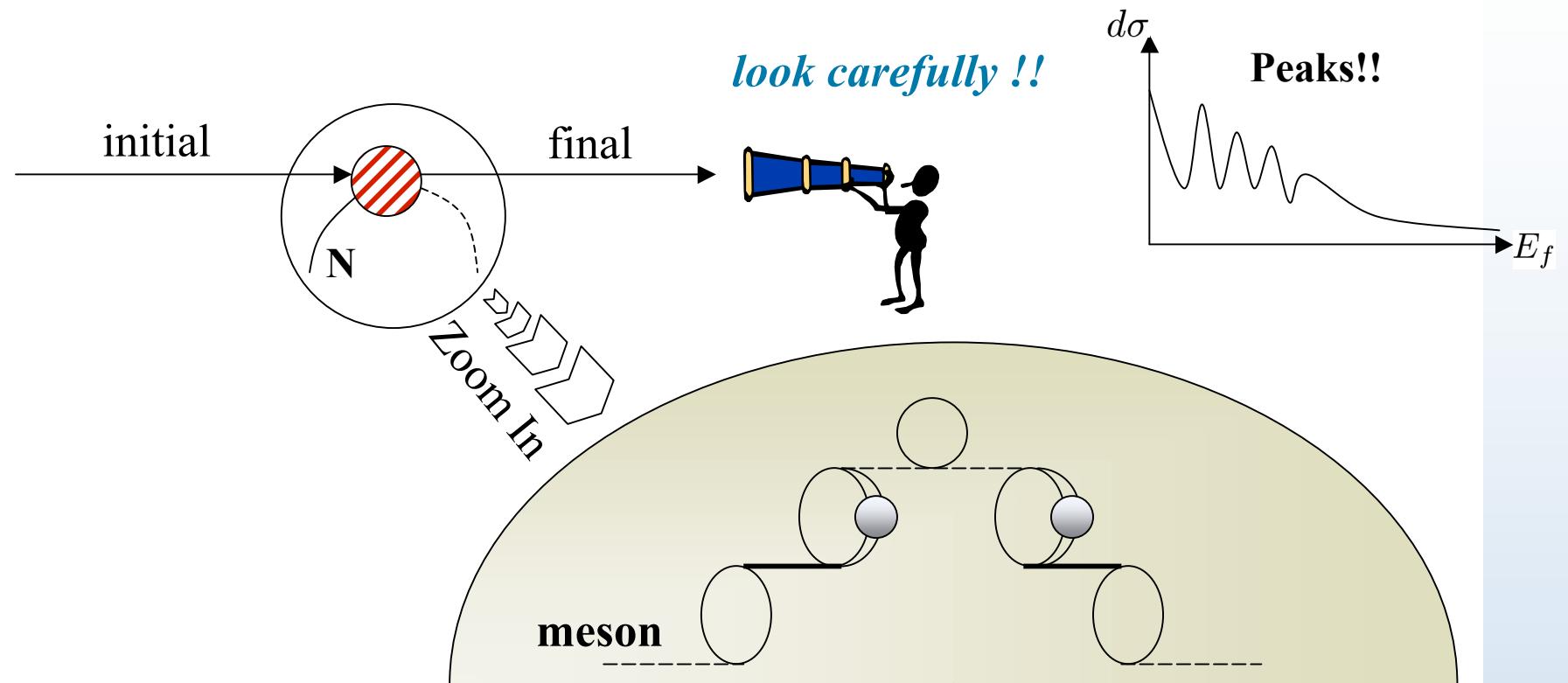
The NJL Model :  $J^p = 0^-$ 

Fig. 10. Pseudoscalar meson spectrum from the NJL model (Klimt et al. 1990), showing the chiral and flavour symmetry breaking pattern. Calculated and experimental masses are given in MeV.

## 2. Missing Mass Spectroscopy

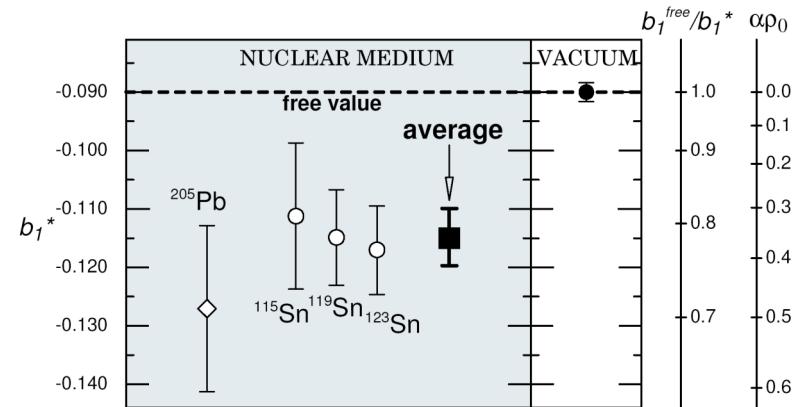
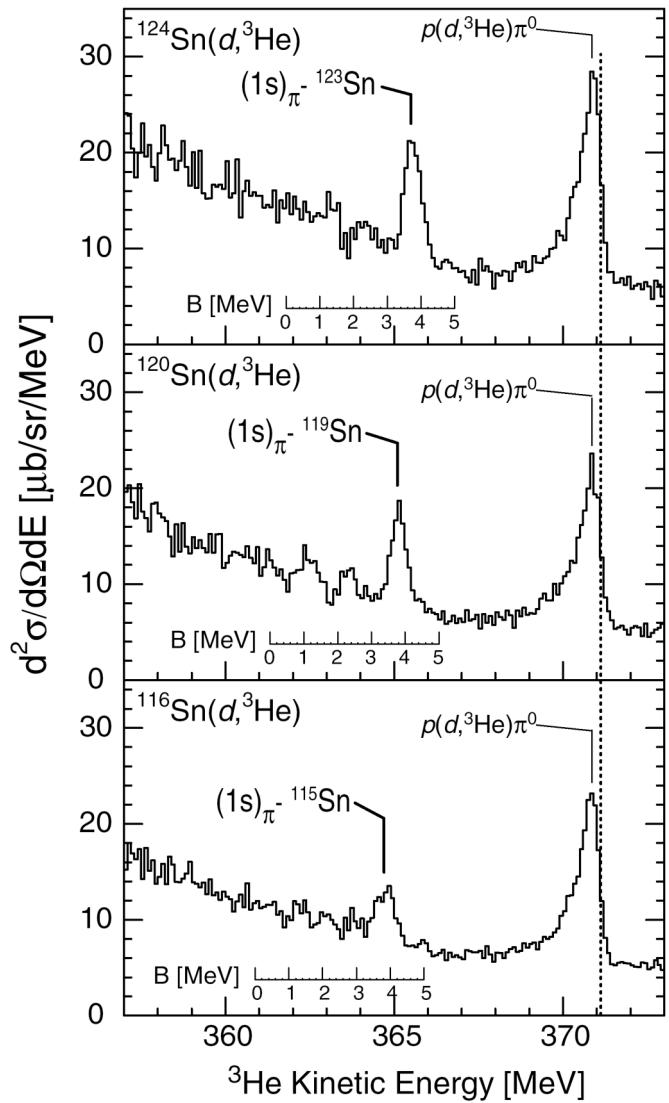


In-Medium Dispersion Relation

Medium Effects

$$[-\nabla^2 + m^2 + \Pi(\rho(r), \omega)]\phi = \omega^2 \phi$$

# Deeply Bound Pionic Atom by ( $d, {}^3\text{He}$ )



Umemoto et al., PRC62 (2000) (Theory Spectra)

K. Suzuki *et al.* Phys. Rev. Lett. 92(2004) 072302

**GOR relation + Tomozawa-Weinberg Relation**

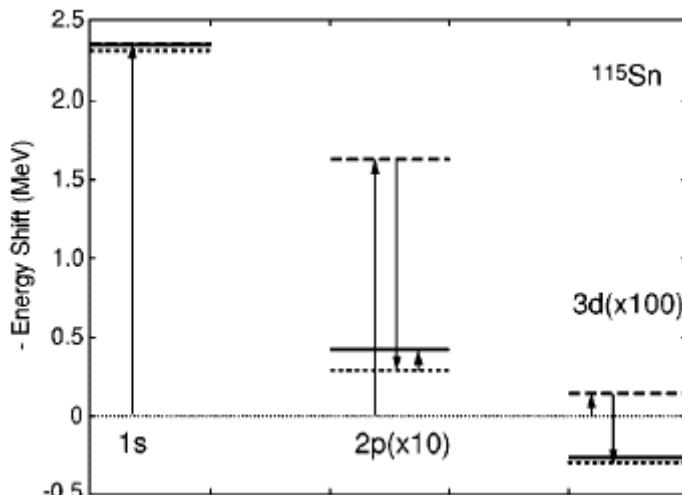
$$\frac{\langle \bar{q}q \rangle_\rho}{\langle \bar{q}q \rangle_0} \simeq \frac{f_\pi^{*2}}{f_\pi^2} \simeq \frac{b_1^{\text{free}}}{b_1^*(\rho)} = 0.78 \pm 0.05 \text{ @ } \rho \simeq 0.6\rho_0$$



$$\sim 0.64 \text{ @ } \rho = \rho_0$$

- Information on  $\Pi$  at finite  $\rho \sim \rho_0$ , ( $T \sim 0$ )

- Eigen state observation  $\iff$  Invariant Mass Method
- Quantum number fixed  $\implies$  Selective information



Umemoto et al., PRC62 (2000)

FIG. 1. The binding energies with finite-size Coulomb potential only  $B_{\text{Coul}}$  and Coulomb plus optical potential  $B_{\text{full}}$ , are calculated. The energy shifts  $B_{\text{Coul}}, B_{\text{full}}$  are shown as the solid bars for pionic  $1s$ ,  $2p$ , and  $3d$  states for  $^{115}\text{Sn}$  and  $^{207}\text{Pb}$ . The shifts due to the real local terms in the potential are shown by dashed bars. Dotted bars are the results with all real terms (local plus nonlocal) in the optical potential.

$$\begin{aligned} \Pi &= 2\mu V_{\text{opt}} \\ &= -4\pi[b(r) + \varepsilon_2 B_0 \rho^2(r)] \\ &\quad + 4\pi \nabla \cdot [c(r) + \varepsilon_2^{-1} C_0 \rho^2(r)] L(r) \nabla \end{aligned}$$

Ericson-Ericson, Ann. Phys. **36** (66) 323  
Seki-Masutani, Phys. Rev. **C27**(83)2799

with  $b(r) = \varepsilon_1 \{ b_0 \rho(r) + \textcolor{blue}{b_1} [\rho_n(r) - \rho_p(r)] \}$

$$c(r) = \varepsilon_1^{-1} \{ c_0 \rho(r) + c_1 [\rho_n(r) - \rho_p(r)] \}$$

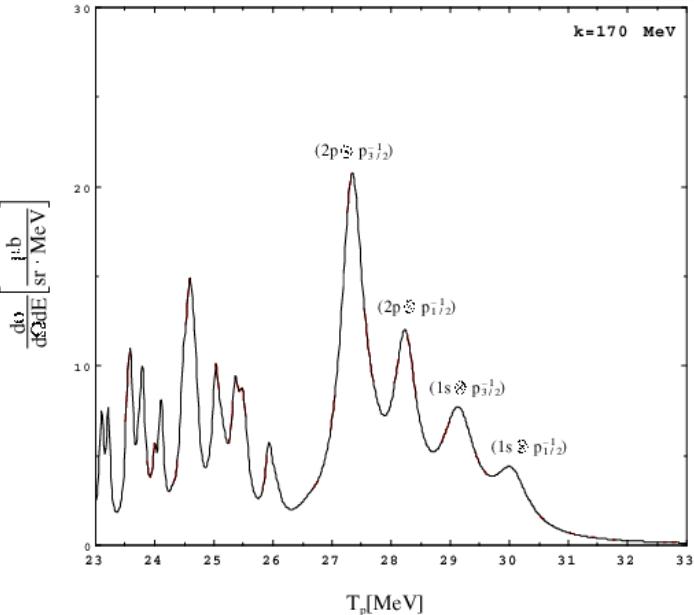
$$L(r) = \{1 + \frac{4}{3}\pi\lambda[c(r) + \varepsilon_2^{-1} C_0 \rho^2(r)]\}^{-1}$$

# A( $\gamma$ , N) reaction

- Mesic-Atom ... It's another Method.

S. Hirenzaki, E. Oset

Phys. Lett. **B527**(2002)69

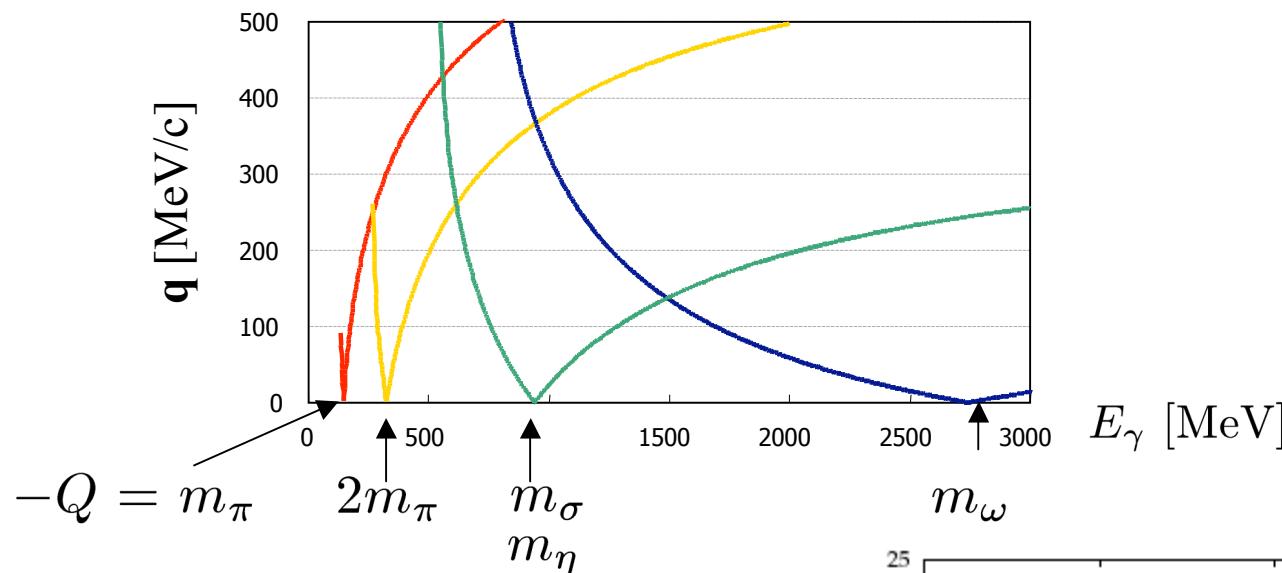


- Mesic-Nuclei ... It has an Advantage

➡ TRANSPARENCY cf. (d,  $^3\text{He}$ )

- ◆  $t \sim \int \chi_f^* \phi_M^* \psi_N \chi_i d^3 r$
- ◆ Substitutional vs. Quasi-Substitutional at recoilless kinematics.
- ◆ Deep Mesic State needs Deep Nuclear State !

# Kinematics $(\gamma, N)$ forward

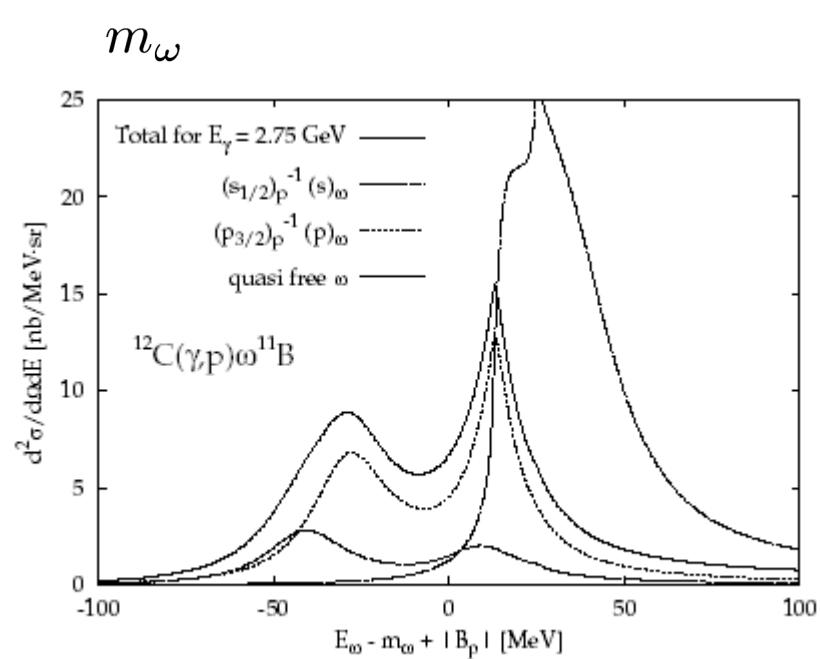


$\omega$  mesic Nuclei by  $(\gamma, p)$

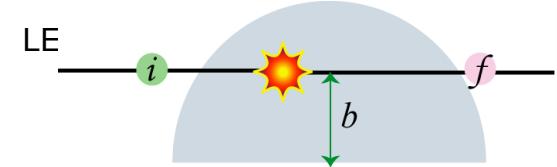
E. Marco, W. Weise

$E_\gamma = 2.75$  [GeV]

Phys. Lett. B502 (2001) 59



# Distortion factor

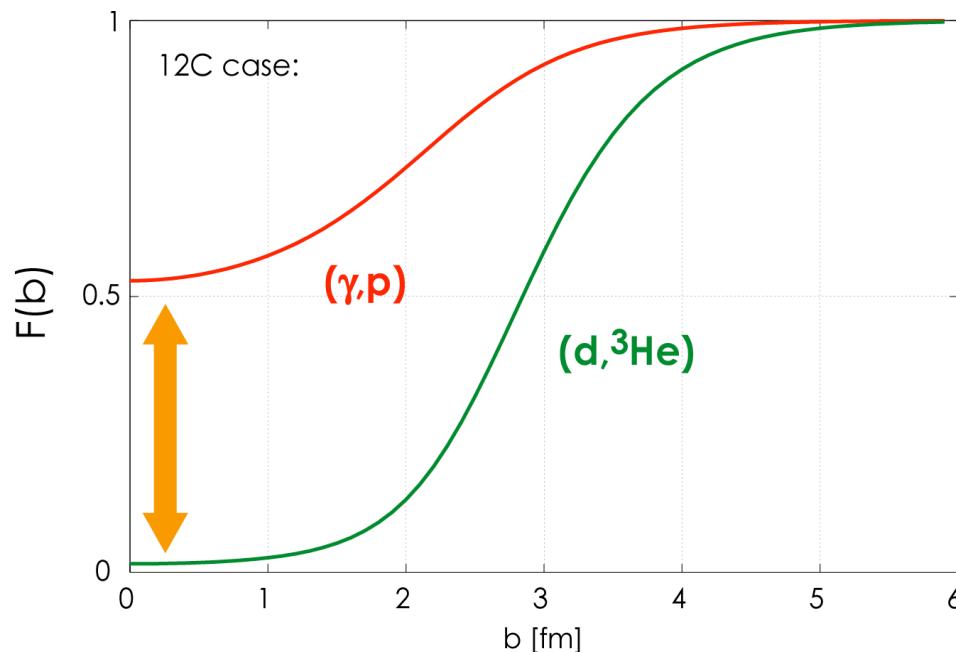


[Eikonal approx.]

$$\chi_f^*(\vec{r}) \chi_i(\vec{r}) = \exp[i\vec{q} \cdot \vec{r}] F(\vec{b})$$

**distortion Factor** reduction of the flux due to the absorption

$$F(b) = \exp \left[ -\frac{1}{2} \sigma_{iN} \int_{-\infty}^z dz' \rho_A(z', b) - \frac{1}{2} \sigma_{fN} \int_z^\infty dz' \rho_{A-1}(z', b) \right]$$



**(γ,p) case:**

more sensitive to the Center of the nucleus.

# 3-1. $\eta$ – Nucleus system : Nature of Baryon Resonance

## eta-mesic nuclei

- »  $(\pi^+, p)$ 
  - \* Liu, Haider, PRC34(1986)1845
  - \* Chiang, Oset, and Liu, PRC44(1988)738
  - Chrien *et al.*, PRL60(1988)2595
  - Kohno, Tanabe, Phys.Lett.B231:219-223,1989.
- »  $(d, {}^3He)$ 
  - \* Hayano, Hirenzaki, Gillitzer, Eur.Phys.J.A6(1999)99
  - \* D. Jido, H.Nagahiro, S.Hirenzaki PRC66(2002)045202

H. Nagahiro and D. Jido

## properties of eta meson

### $\eta$ meson

- »  $m_\eta = 547.3$  [MeV]
- »  $I = 0, J^P = 0^-$
- »  $\Gamma = 1.18$  [keV] ( $2\gamma, 3\pi^0, \pi^+\pi^-\pi^0, \dots$ )

### $\eta$ -N system

- Strong Coupling to  $N^*(1535)$ ,  $J^P = \frac{1}{2}^-$
- »  $\Gamma_{\pi N} \sim \Gamma_{\eta N} \sim 75$  [MeV]

### $\eta NN^*$ system

- No  $I = \frac{3}{2}$  baryon contamination
- Large coupling constant
- no suppression at threshold
- (s-wave coupling)  
 $\mathcal{L}_{\eta NN^*} = g_\eta \bar{N} \eta N^* + h.c.$

eta-Nucleus system



Doorway to  $N^*(1535)$

# Chiral model for N and N\*

## Chiral doublet model

DeTar, Kunihiro, PRD39 (89)2805  
 Jido, Oka, Hosaka, Nemoto, NPA671(00)471, PTP106(01)873  
 Jido, Hatsuda, Kunirhiro, PRL84(00)3252

Extended SU(2) Linear Sigma Model  
 for N and N\*

## Lagrangian

$$\mathcal{L} = \sum_{j=1,2} [\bar{N}_j i \not{\partial} N_j - g_j \bar{N}_j (\sigma + (-)^{j-1} i \gamma_5 \vec{\tau} \cdot \vec{\pi}) N_k] - m_0 (\bar{N}_1 \gamma_5 N_2 - \bar{N}_2 \gamma_5 N_1)$$

## Physical fields

$$\begin{pmatrix} N \\ N^* \end{pmatrix} = \begin{pmatrix} \cos \theta & \gamma_5 \sin \theta \\ -\gamma_5 \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} N_1 \\ N_2 \end{pmatrix}$$

N\* : chiral partner of nucleon

## Mass difference

$$m_N^*(\rho) - m_{N^*}^*(\rho) = (1 - C \frac{\rho}{\rho_0})(m_N - m_{N^*})$$

\* C~0.2 :the strength of the Chiral restoration  
 at the nuclear saturation density

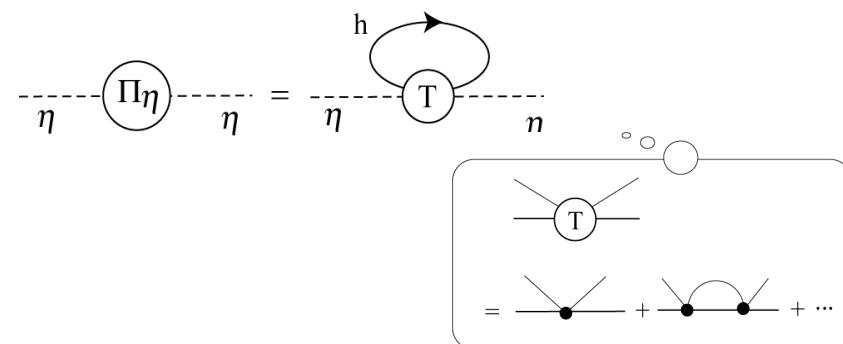
\* reduction of mass difference

## Chiral unitary model

Kaiser, Siegel, Weise, PLB362(95)23  
 Waas, Weise, NPA625(97)287  
 Garcia-Recio, Nieves, Inoue, Oset, PLB550(02)47  
 Inoue, Oset, NPA710(02) 354

\* In this study, we directly take the eta-self-energy in the ref.NPA710(02)354  
 A coupled channel Bethe-Salpeter eq.

$$\{\pi^- p, \pi^0 n, \eta n, K^0 \Lambda, K^+ \Sigma^-, K^0 \Sigma^0, \pi^0 \pi^- p, \pi^+ \pi^- n\}$$



\* the N\* is introduced as a resonance generated dynamically from meson-baryon scattering.

\* No mass shift of N\* is expected in the nuclear medium.

# $\eta$ -nucleus interaction $\sim N^*$ dominance

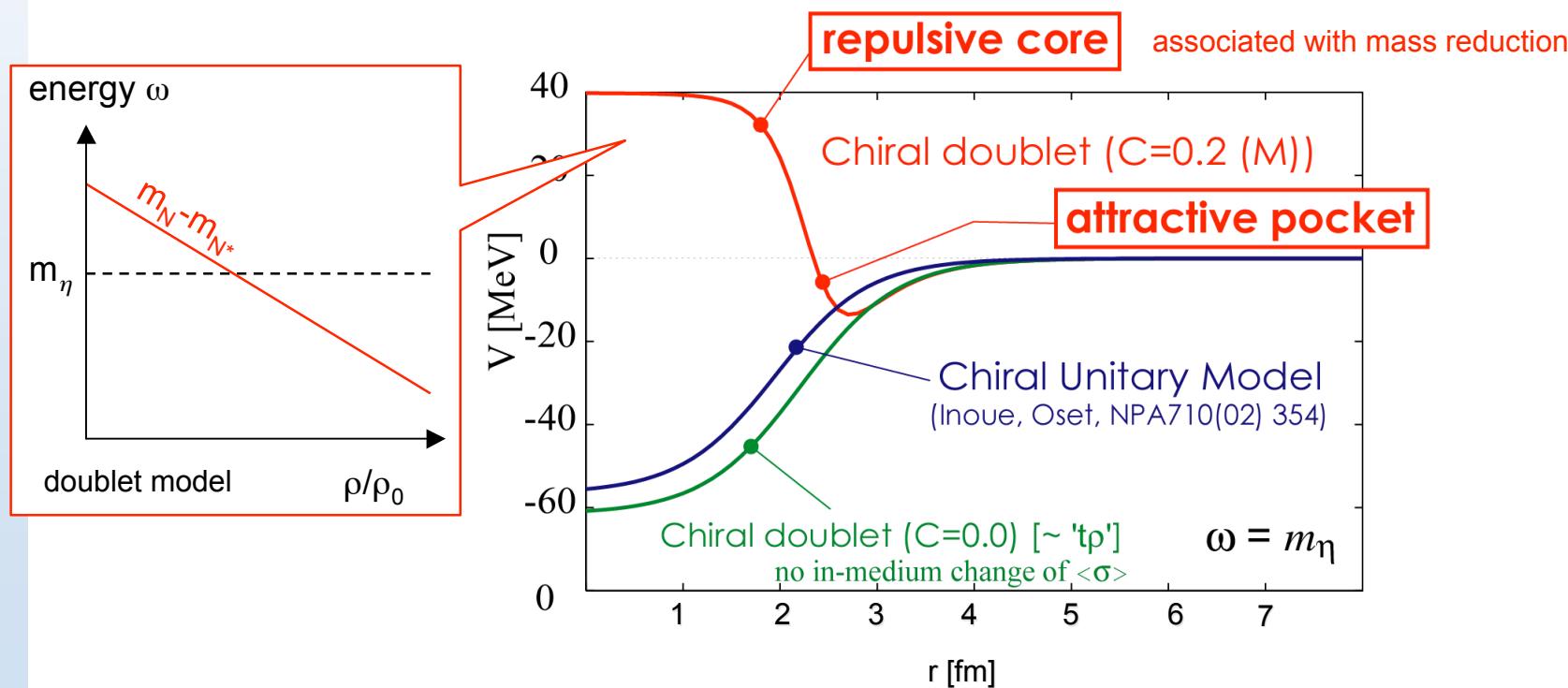
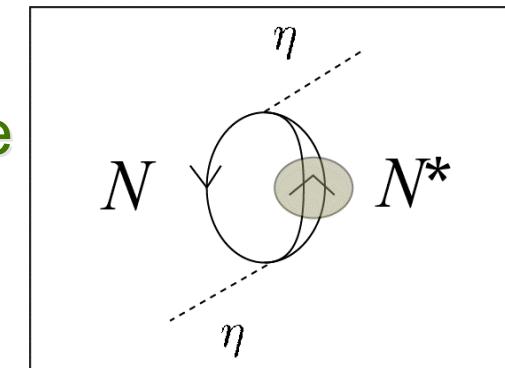
## optical potential

$$V_{\text{opt}} = \frac{g_\eta^2}{2\mu} \frac{\rho}{\omega - (m_{N^*}(\rho) - m_N(\rho)) + i\Gamma_N^*(s; \rho)/2}$$

(Chiang, Oset, Liu PRC44(1991)738)

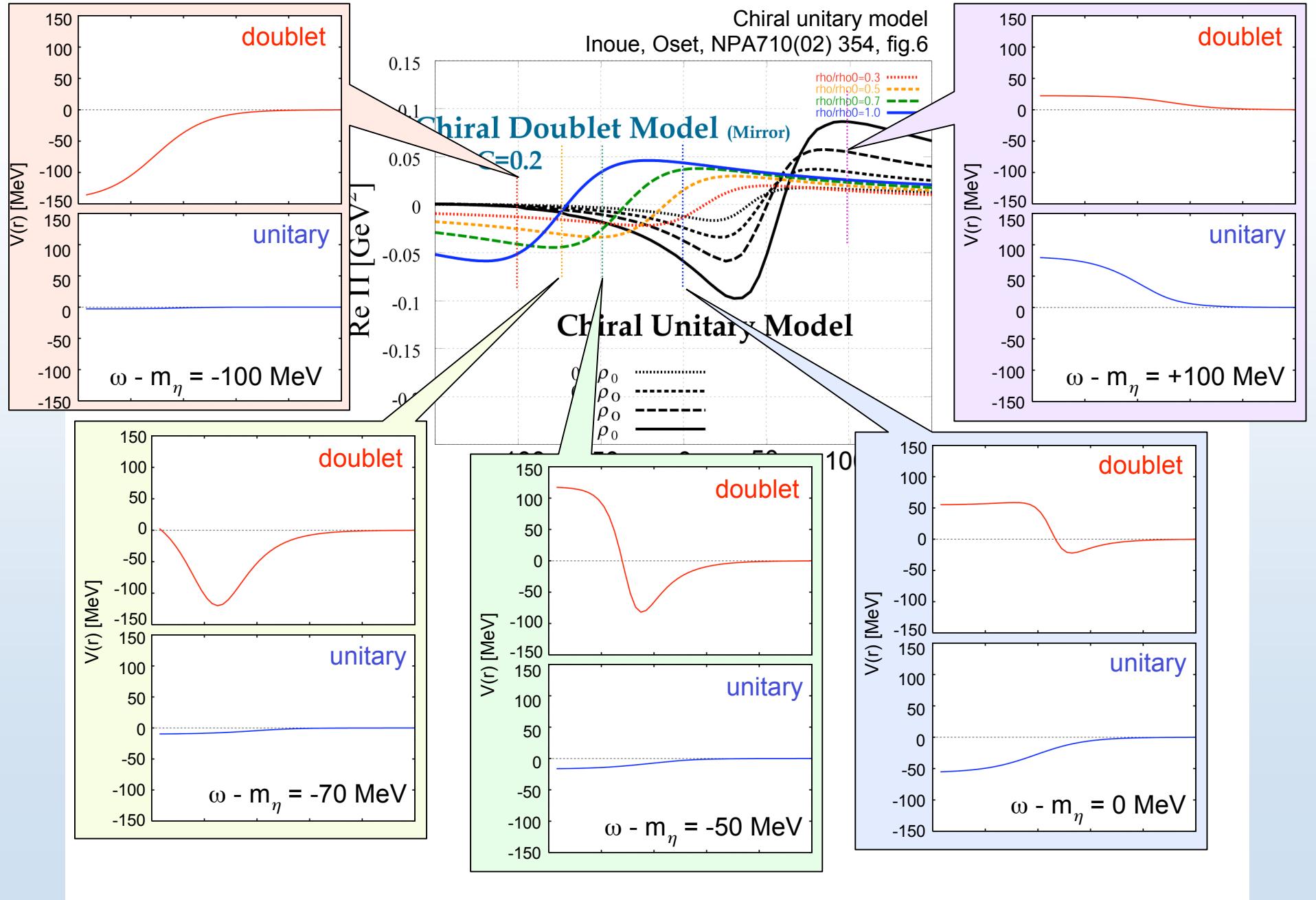
(D.Jido, H.N., S.Hirenzaki, PRC66(2002)045202)

$g_\eta \simeq 2.0$  to reproduce the partial width  $\Gamma_{N^* \rightarrow \eta N} \simeq 75$  MeV at tree level.



$\eta$ -nucleus optical potential  $\rightarrow$  sensitive to the in-medium properties of  $N$  and  $N^*$

# Energy dependence of the optical potentials



# Spectra of $^{12}\text{C}$ target

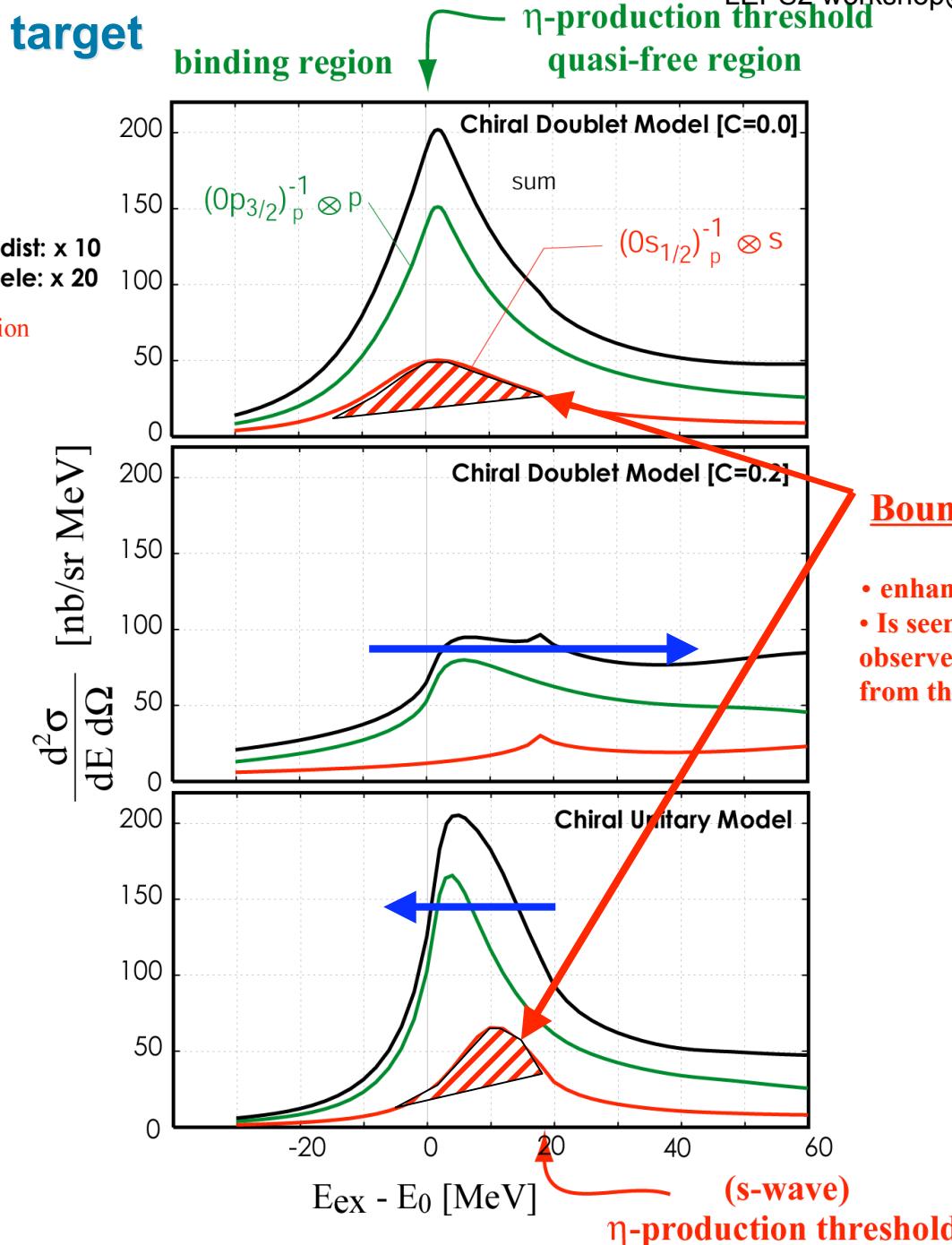
$T_d = 3.5 \text{ [GeV]}$

$E_\gamma = 950 \text{ [MeV]}$

recoilless condition for the eta production

$(\gamma, p)$

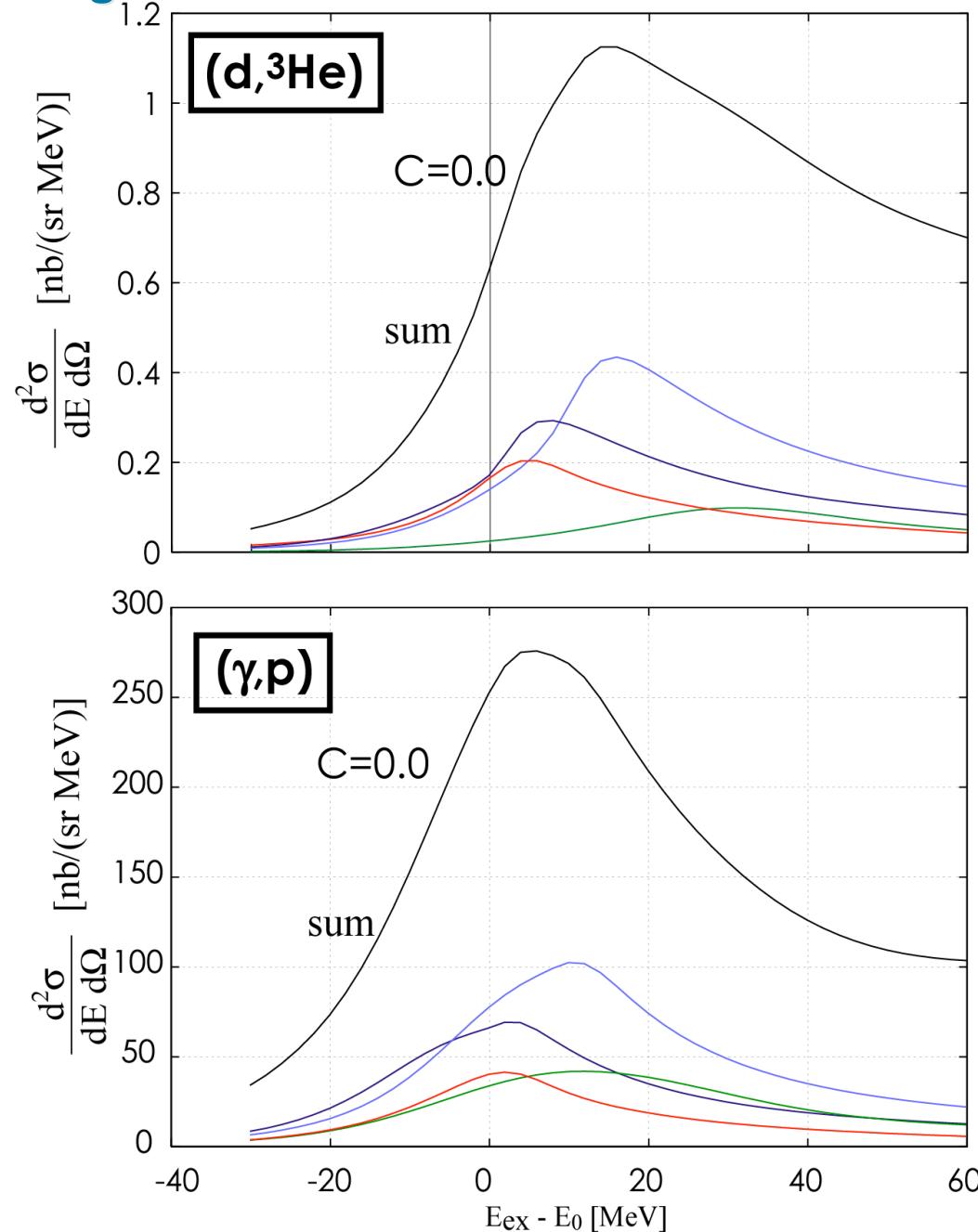
We can see the difference between two models more clearly.



# Spectra of $^{40}\text{Ca}$ target

$$\begin{aligned} & (1s_{1/2})_p^{-1} \otimes s_\eta \\ & (0d_{3/2})_p^{-1} \otimes d_\eta \\ & (0d_{5/2})_p^{-1} \otimes d_\eta \\ & (0p_{3/2})_p^{-1} \otimes p_\eta \end{aligned}$$

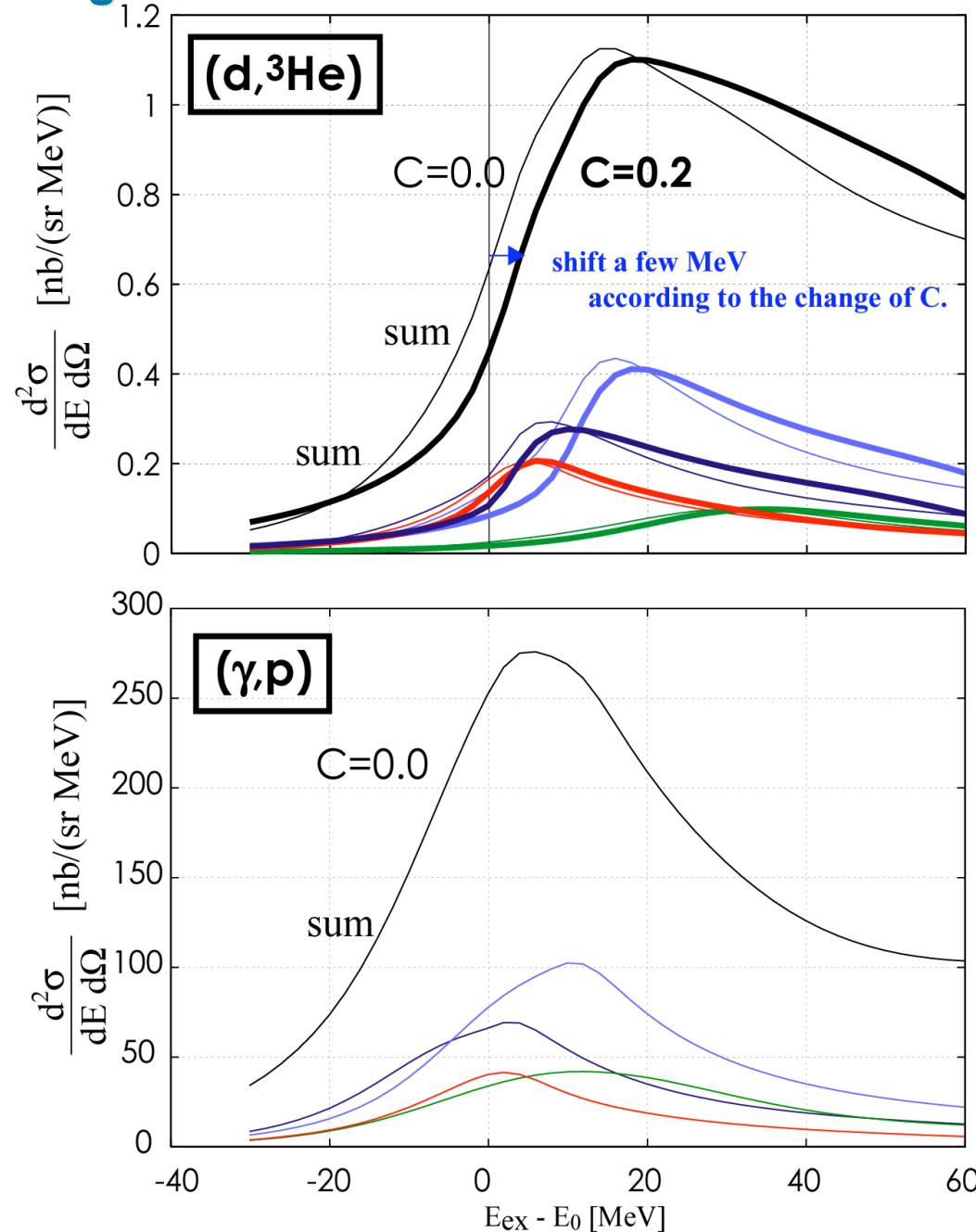
- heavy target case
- Chiral doublet model  
 $C=0.0$  vs.  $C=0.2$



# Spectra of $^{40}\text{Ca}$ target

$$\begin{aligned} & (1s_{1/2})_p^{-1} \otimes s_\eta \\ & (0d_{3/2})_p^{-1} \otimes d_\eta \\ & (0d_{5/2})_p^{-1} \otimes d_\eta \\ & (0p_{3/2})_p^{-1} \otimes p_\eta \end{aligned}$$

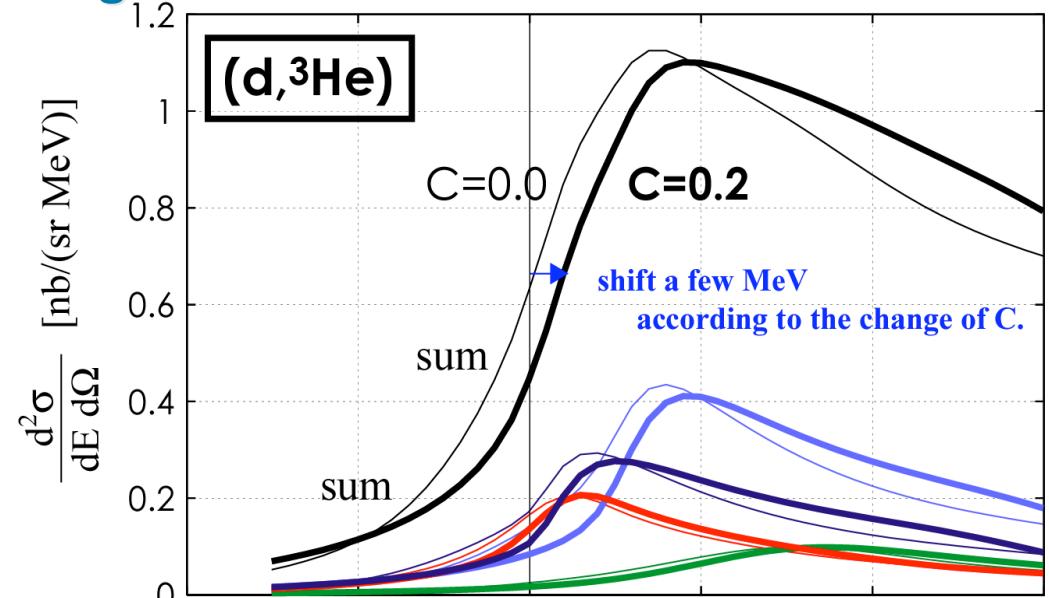
- heavy target case
- Chiral doublet model  
 $C=0.0$  vs.  $C=0.2$



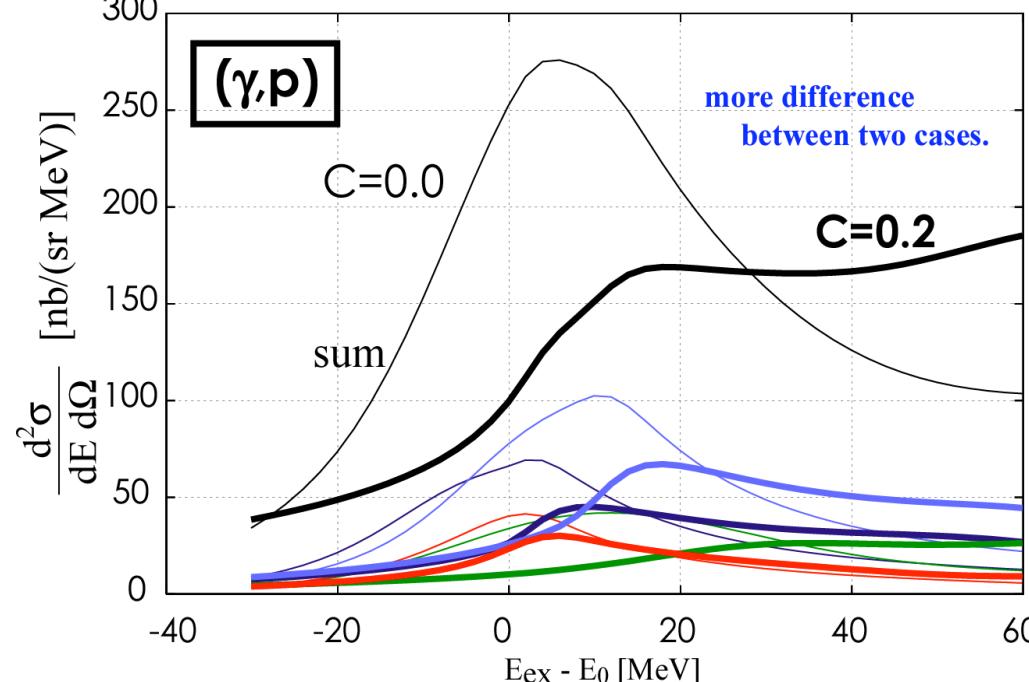
## Spectra of $^{40}\text{Ca}$ target

$$\begin{aligned} & (1s_{1/2})_p^{-1} \otimes s_\eta \\ & (0d_{3/2})_p^{-1} \otimes d_\eta \\ & (0d_{5/2})_p^{-1} \otimes d_\eta \\ & (0p_{3/2})_p^{-1} \otimes p_\eta \end{aligned}$$

- heavy target case
- Chiral doublet model  
 $C=0.0$  vs.  $C=0.2$



• Whole spectra change reflecting the reduction of mass difference of  $N$  and  $N^*$  !!



## 3-2. $\eta$ and $\eta'(958)$ mesic nuclei with NJL model

- quark picture of mesons -

H. Nagahiro, S. Hirenzaki, PRL(2005)

H. Nagahiro, M. Takizawa, S. Hirenzaki, PRC(2006)

### ➤ $\eta'(958)$ meson ... close connections with $U_A(1)$ anomaly

- some theoretical works
  - the effects of the  $U_A(1)$  anomaly on  $\eta'$  properties
  - at finite temperature/density
    - T. Kunihiro, PLB219(89)363
    - R.D.Pisarski, R.Wilczek, PRD29(84)338
    - K.Fukushima, K.Onishi, K.Ohta, PRC63(01)045203
    - P. Costa *et al.*, PLB560(03)171, hep-ph/0408177
    - S. D. Bass and A. W. Thomas, PLB634(06)368
  - the possible character changes of  $\eta'$
- a poor experimental information  
on the  $U_A(1)$  anomaly at finite density

Nagahiro and  
Takizawa

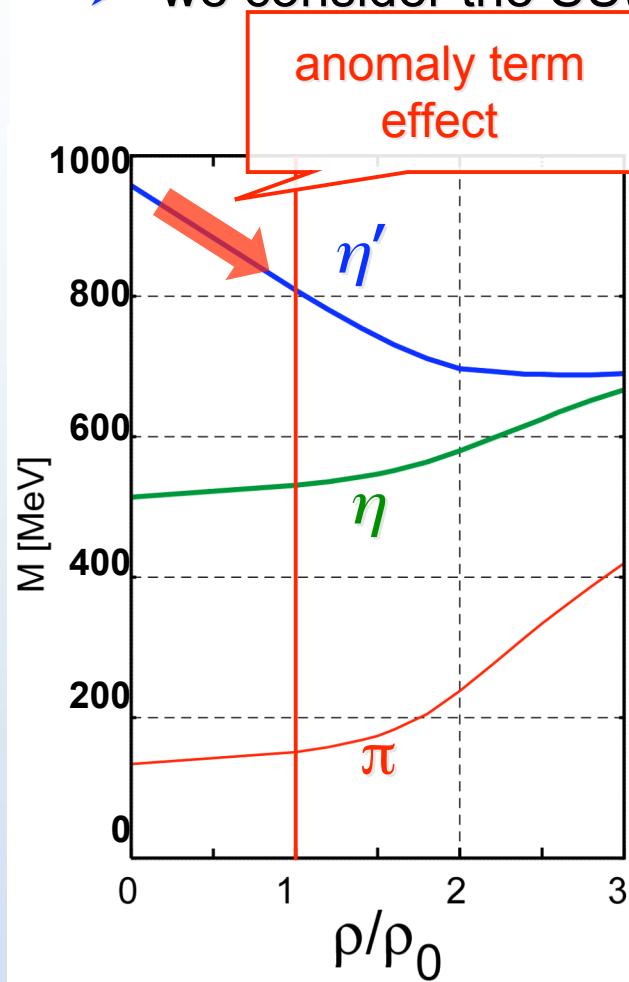
### ➤ proposal for the formation reaction of the $\eta'$ -mesic nuclei

(inspired by discussion with T. Hatsuda)

- discuss the possibility of the  $\eta'$ -nucleus bound states  
(Previous estimation of b.s. by K.Tushima, NPA670(00)198c : But,  $\Gamma$  is fixed to be 0)
- the  $\eta'$  properties, especially mass shift, at finite density

## SU(2) symmetric matter $\rho_u = \rho_d, \rho_s = 0$

- we consider the SU(2) sym. matter as the sym. nuclear matter.



parameters (in vacuum)

$$\begin{aligned}\Lambda &= 602.3 \text{ [MeV]} \\ g_S \Lambda^2 &= 3.67 \\ g_D \Lambda^5 &= -12.36 \\ m_{u,d} &= 5.5 \text{ [MeV]} \\ m_s &= 140.7 \text{ [MeV]}\end{aligned}$$

P. Rehberg, et al., PRC53(96)410.

$$\begin{aligned}M_{u,d} &= 367.6 \text{ [MeV]} \\ M_s &= 549.5 \text{ [MeV]} \\ \langle \bar{u}u \rangle^{1/3} &= -241.9 \text{ [MeV]} \\ \langle \bar{s}s \rangle^{1/3} &= -257.7 \text{ [MeV]} \\ m_{\eta'} &= 958 \text{ [MeV]} \\ m_\eta &= 514 \text{ [MeV]} \\ m_\pi &= 135 \text{ [MeV]}\end{aligned}$$

$\eta$  and  $\eta'$  mass shifts @  $\rho_0$

$$\Delta m_{\eta'} \sim -150 \text{ MeV} @ \rho_0$$

$$\Delta m_\eta \sim +20 \text{ MeV} @ \rho_0$$

Large mass sift at **normal nuclear density**

# $\eta$ - & $\eta'$ -Nucleus optical potential

~ potential description

## Real Part $V_0$

- evaluated by possible  $\eta, \eta'$  mass shift at  $\rho_0$

$$U(r) = (V_0 + iW_0) \frac{\rho(r)}{\rho_0}$$

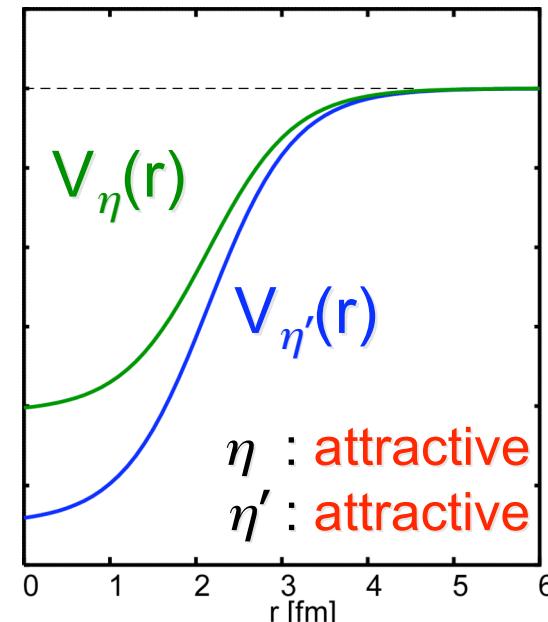
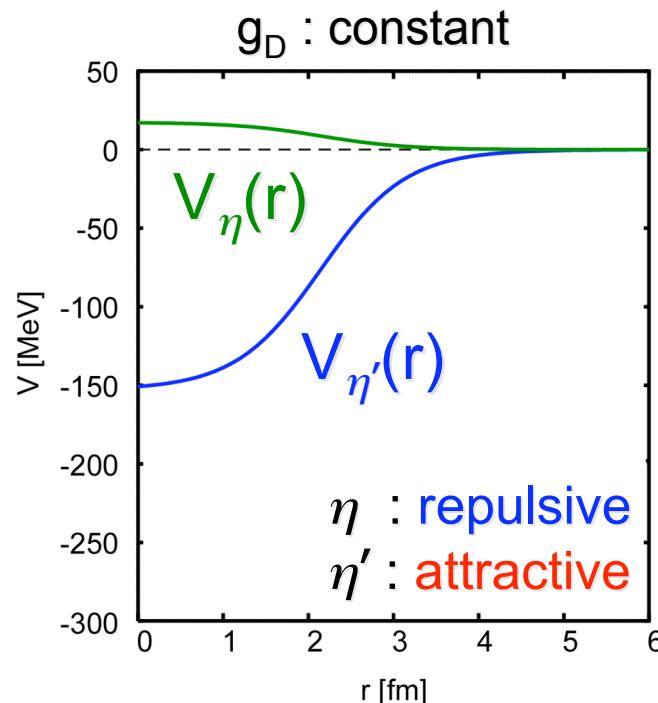
$$m_{\eta'}^2 \rightarrow m_{\eta'}^2(\rho) = (m_{\eta'} + \Delta m_{\eta'}(\rho))^2 \sim m_0^2 + 2m_0 \Delta m(\rho)$$

$$\Delta m(\rho) \rightarrow V(\rho(r)) = V_0 \frac{\rho(r)}{\rho_0}$$

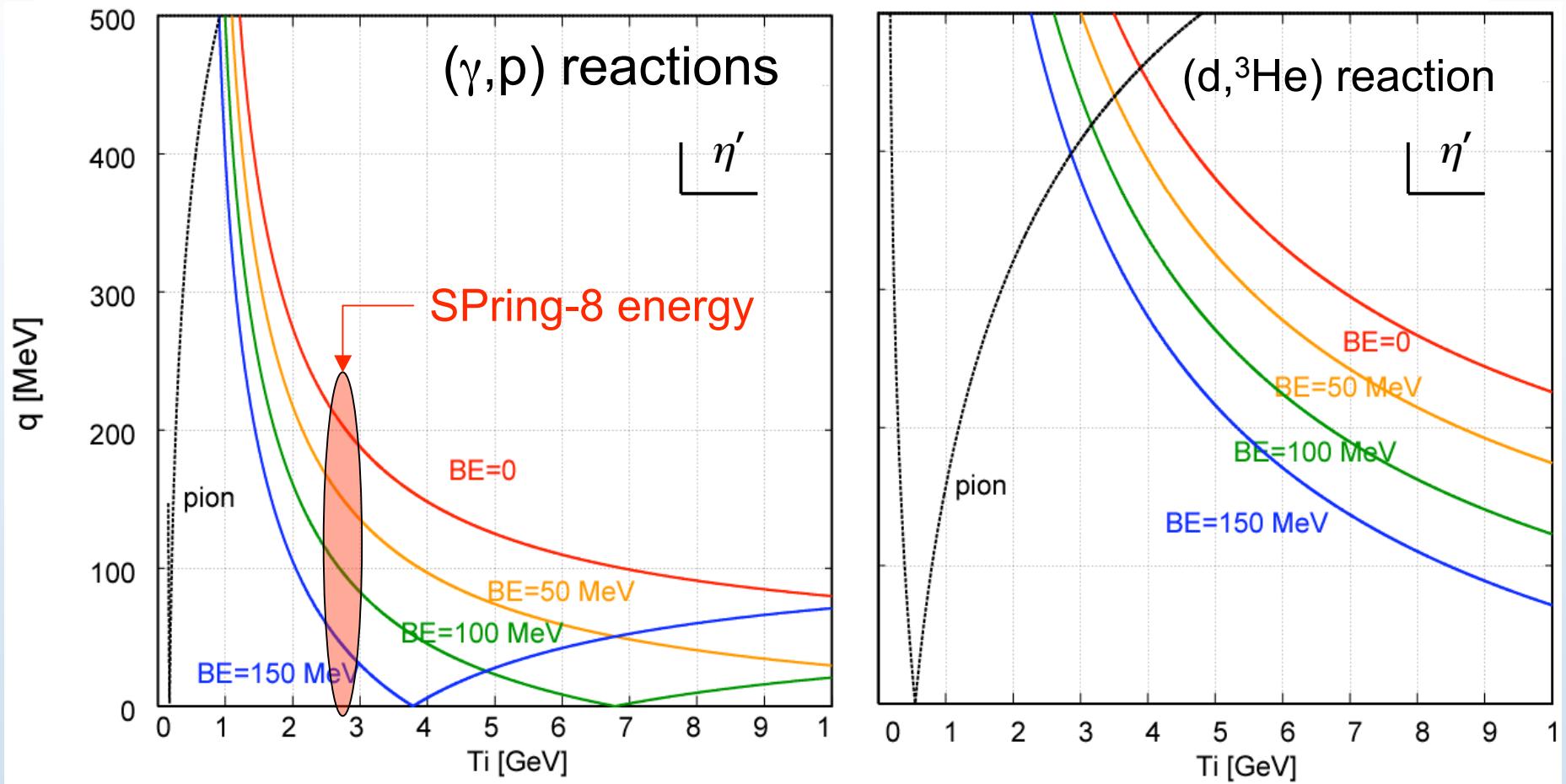
G.W.Carter, D.Diakonov,  
NPA642(98) c78;

Possible density dependence of  
 $g_D(\rho)$

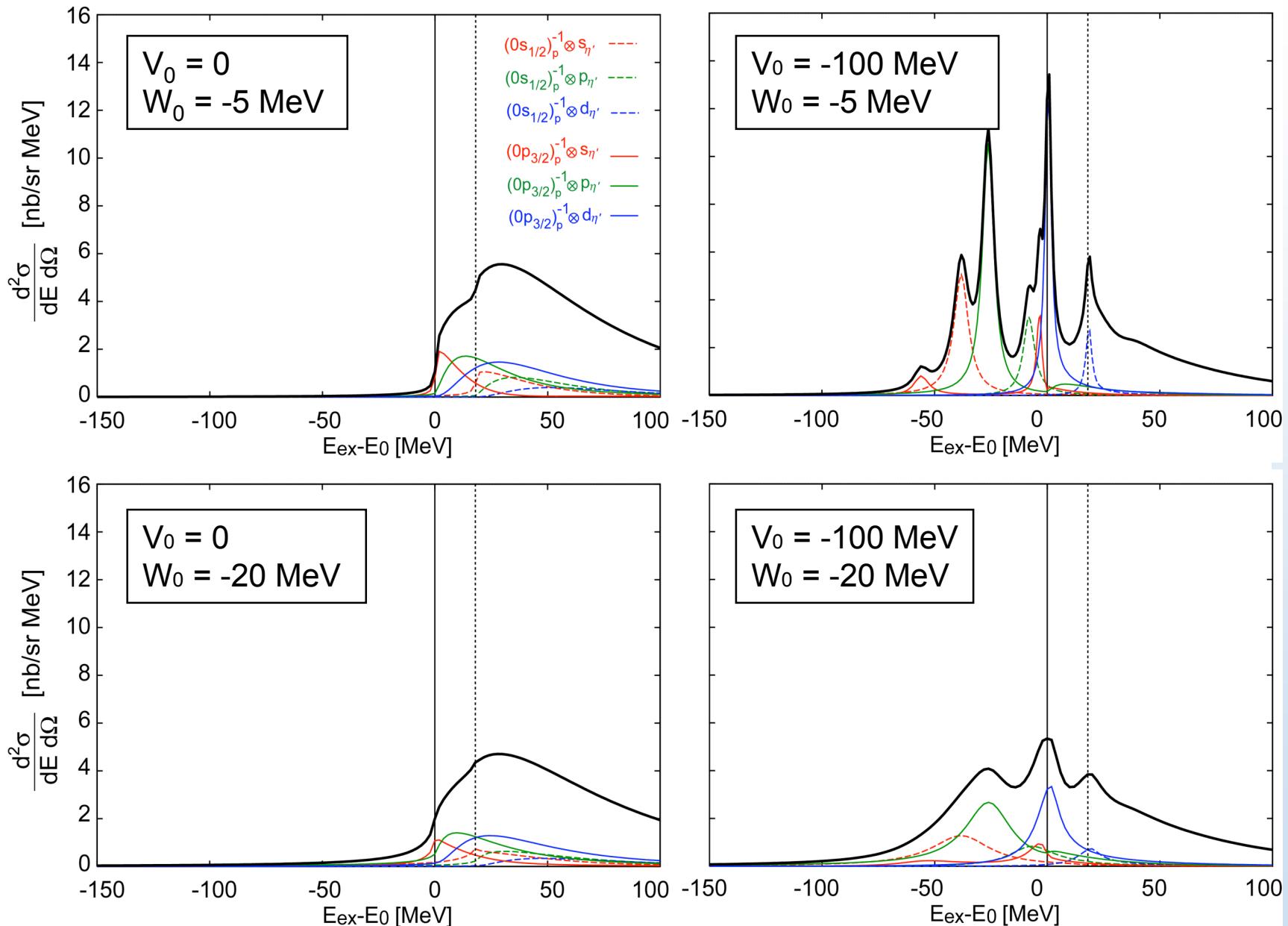
PRD60(99)016004.  
H. Kiuchi, M. Oka, PTP114, 813,  
(2005)



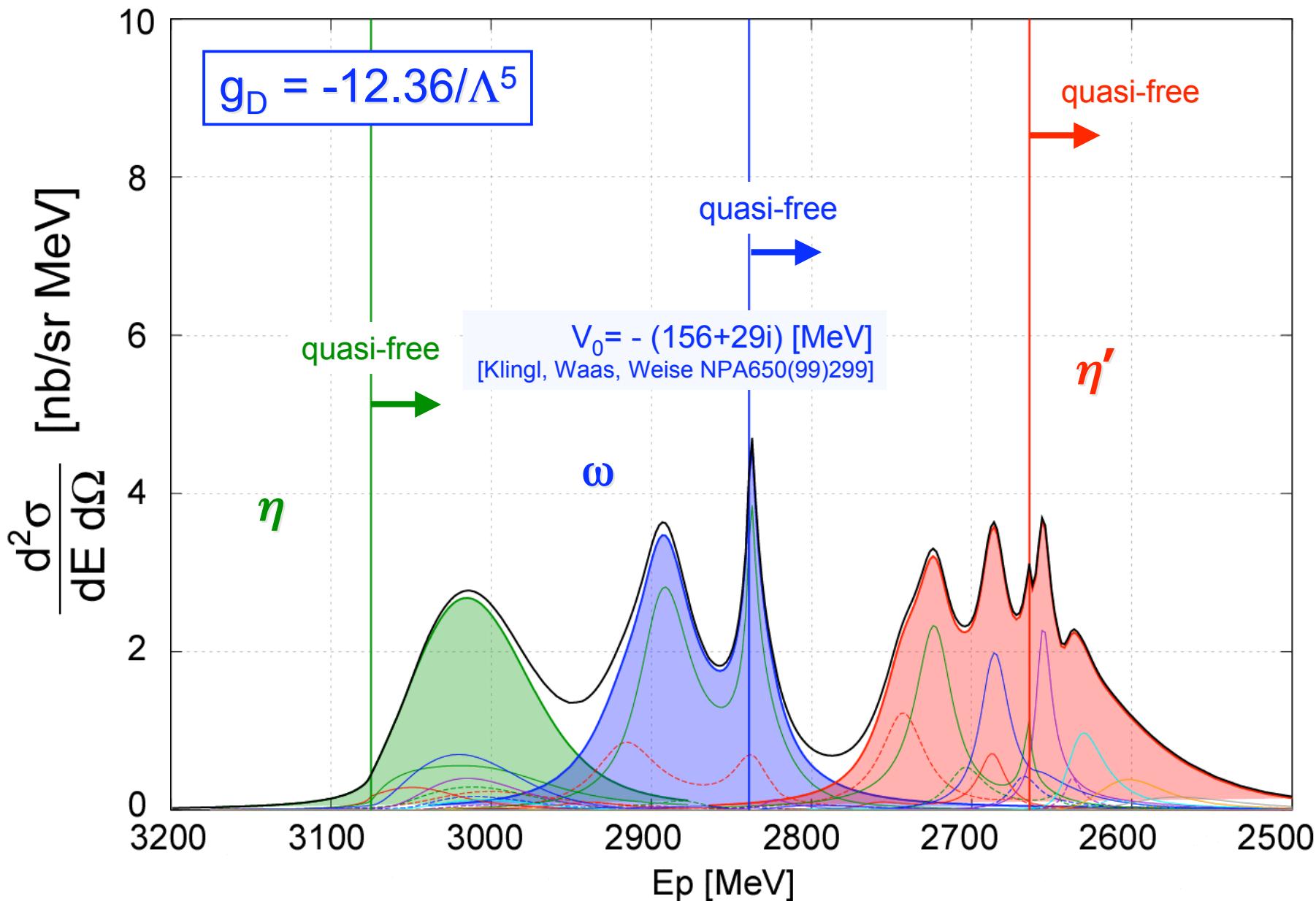
# Momentum transfer



# Numerical Results : $^{12}\text{C}(\gamma, \text{p})^{11}\text{B}_{\eta'}$



# Numerical results : $^{12}\text{C}(\gamma, \text{p})^{11}\text{B}_{\eta, \omega, \eta'}$



## 3-3. Omega Mesic Nuclei

➤ nucl-th/0610085

Study of possible  $\omega$  bound states in nuclei with the  
 $(\gamma, p)$  reaction

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Institutos de Investigación de Paterna, Aptd. 22085, 46071 Valencia, Spain

<sup>b</sup>Research Center for Nuclear Physics, Osaka University, Ibaraki, Osaka 567-0047 Japan

<sup>c</sup>Department of Physics, Nara Women's University, Nara 630-8506 Japan

October 21, 2006

➤ Momentum transfer at 0 deg. and 10 deg.

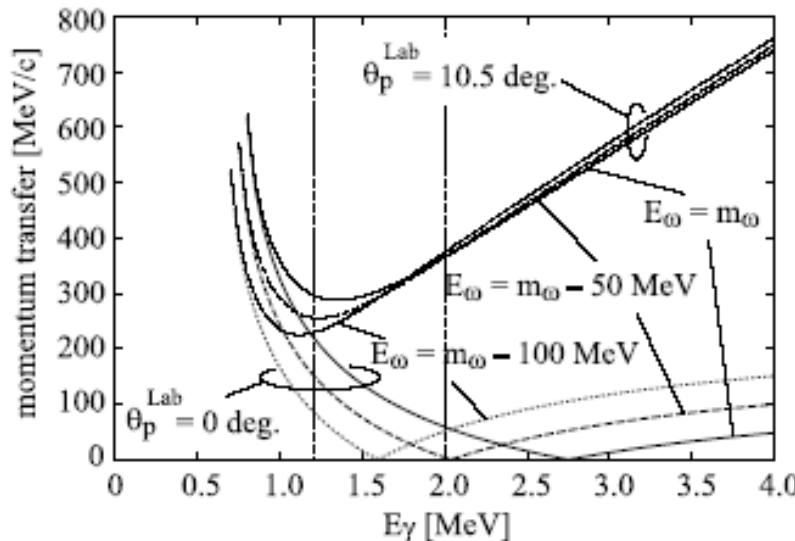


Figure 1: Momentum transfers are shown as a function of the incident photon energy  $E_\gamma$  in the  $(\gamma, p)$  reaction. The solid, dashed and dotted lines show the momentum transfers at  $\omega$  energy  $E_\omega = m_\omega$ ,  $E_\omega = m_\omega - 50$  MeV and  $E_\omega = m_\omega - 100$  MeV, respectively. The thick lines indicate the forward reaction cases and the thin lines the cases for the ejected proton in the final state with the finite angle  $\theta_p^{\text{Lab}} = 10.5$  degree. The vertical dashed lines show the incident energies  $E_\gamma = 1.2$  GeV and 2.0 GeV.

## ➤ E=2.0 GeV, 0 deg & 10 deg, 3 potentials

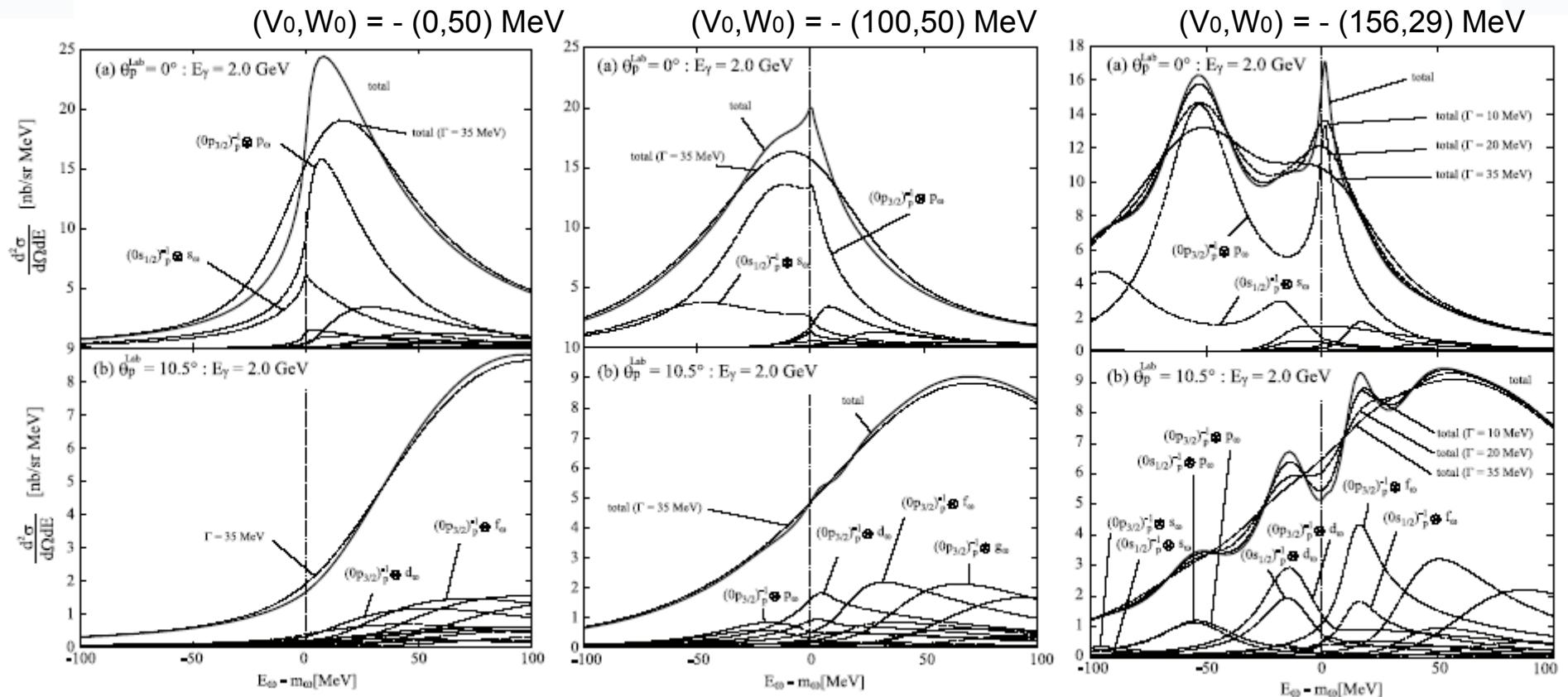


Figure 2: Formation spectra of the  $\omega$  mesic nucleus in  $^{12}\text{C}(\gamma, \text{p})$  reaction at emitted proton angle (a)  $\theta_p^{\text{Lab}} = 0$  degree and (b)  $\theta_p^{\text{Lab}} = 10.5$  degree calculated with the potential depth  $(V_0, W_0) = -(156, 29)$  MeV as in Eq. (2c). The incident photon energy is  $E_\gamma = 2.0$  GeV. The thick solid lines show the total spectra and the dashed lines the subcomponents as indicated in the figures. The assumed experimental resolutions are also indicated in the figures.

➤ E=1.2 GeV, 0 deg & 10 deg, 3 potentials

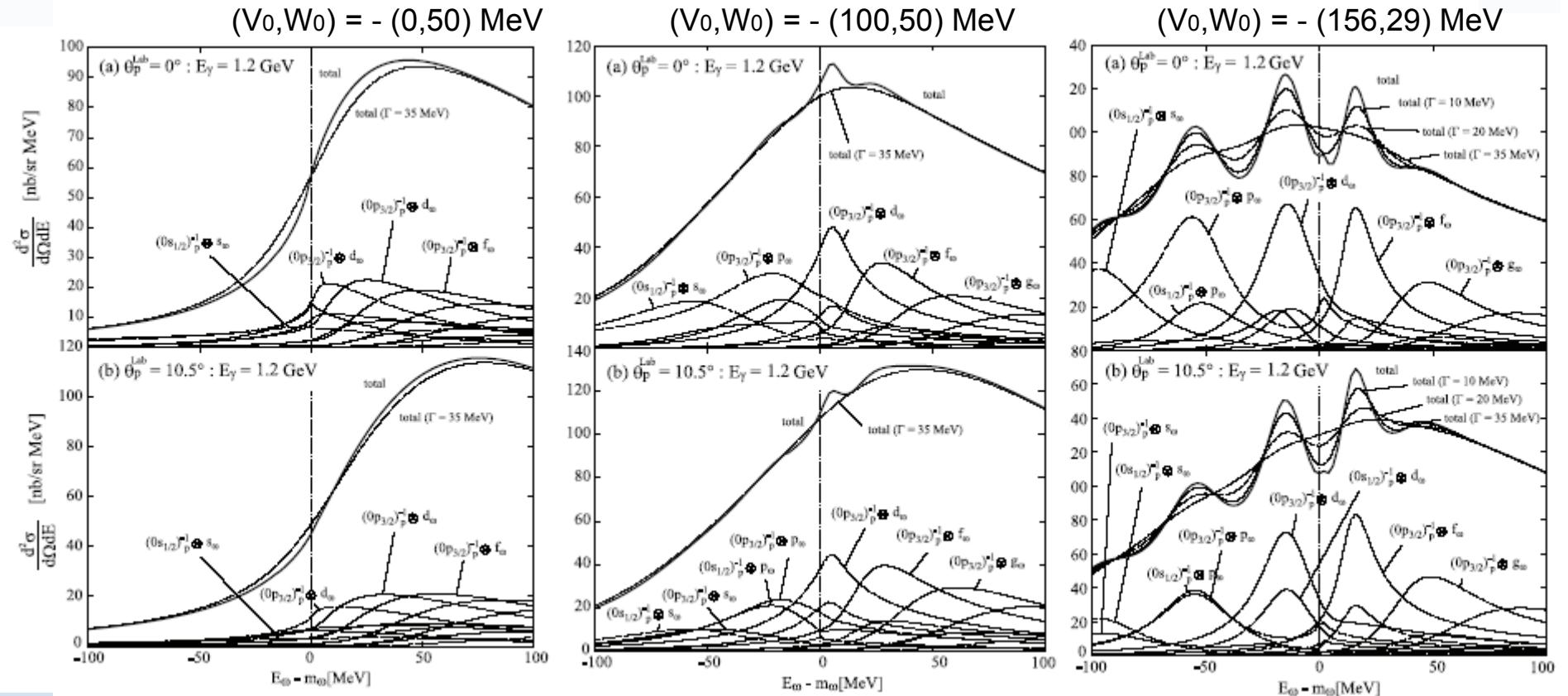


Figure 5: Formation spectra of the  $\omega$  mesic nucleus in  $^{12}\text{C}(\gamma, \text{p})$  reaction at emitted proton angle (a)  $\theta_p^{\text{Lab}} = 0$  degrees and (b)  $\theta_p^{\text{Lab}} = 10.5$  degrees calculated with the potential depth  $(V_0, W_0) = -(156, 29)$  MeV as in Eq. (2c). The incident photon energy is  $E_\gamma = 1.2$  GeV. The thick solid lines show the total spectra and the dashed lines the subcomponents as indicated in the figures. The assumed experimental resolutions are also indicated in the figures.

## (3.4 Penta hypernuclei formation)



Available online at [www.sciencedirect.com](http://www.sciencedirect.com)



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PHYSICS LETTERS B

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Physics Letters B 620 (2005) 125–130

[www.elsevier.com/locate/physletb](http://www.elsevier.com/locate/physletb)

### Production of $\Theta^+$ hypernuclei with the $(K^+, \pi^+)$ reaction

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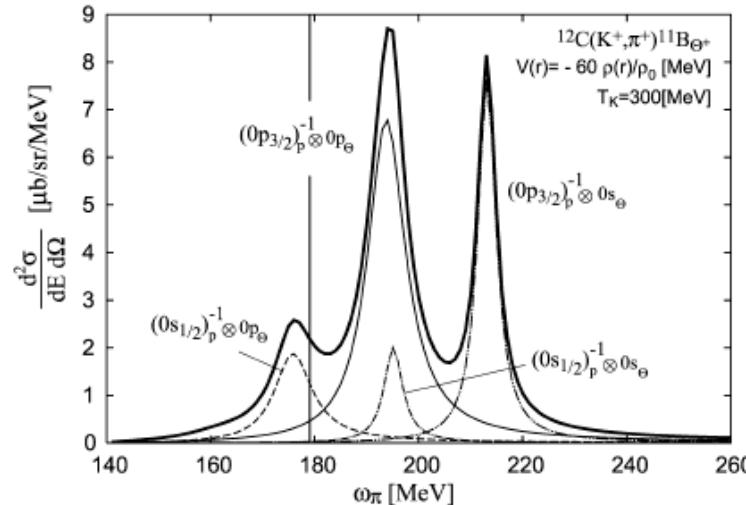


Fig. 2. Calculated  $\Theta$  bound states formation cross section shown as a function of the emitted pion energy  $\omega_\pi$  at forward angles for a  $^{12}\text{C}$  target. The incident kaon kinetic energy,  $T_K$ , is 300 MeV, and the shallow  $\Theta$  nuclear potential  $V(r) = -60\rho(r)/\rho_0$  MeV is used. The total spectrum is shown by the thick-solid line and the dominant subcomponents are also shown by the thin lines as indicated in the figures. The  $\Theta$  production threshold leaving the residual nucleus in its ground state is shown by the vertical line.

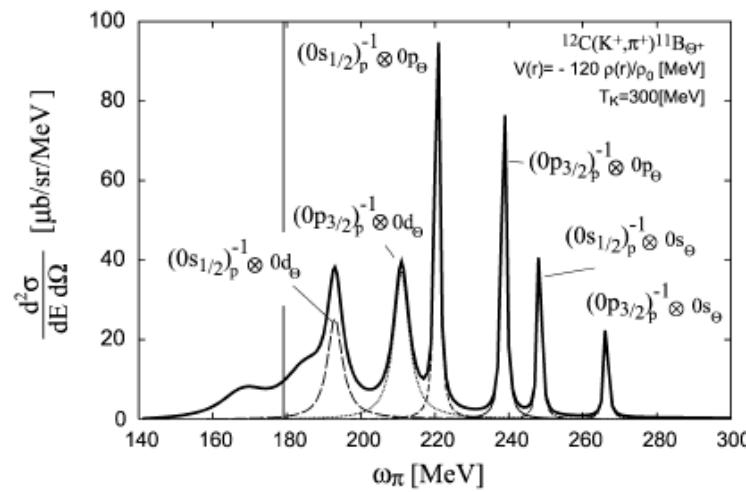


Fig. 3. Calculated  $\Theta$  bound states formation cross section shown as a function of the emitted pion energy  $\omega_\pi$  at forward angles for a  $^{12}\text{C}$  target. The incident kaon kinetic energy,  $T_K$ , is 300 MeV, and the deep  $\Theta$  nuclear potential  $V(r) = -120\rho(r)/\rho_0$  MeV is used. The total spectrum is shown by the thick-solid line and the dominant subcomponents are also shown by the thin lines as indicated in the figure. The  $\Theta$  production threshold leaving the residual nucleus in its ground state is shown by the vertical line.

## 4. Summary

### Mesic Atoms and Mesic Nuclei

- = Nucleus as Finite Density Laboratory
- = Exotic Nuclei with Meson impurities

We are interested in ...

- = how to connect to the fundamental theory
- = how to get reliable experimental information

Several Attempts : Not satisfactory in both sense !!

(gamma,p) reaction is interesting