

# Pentaquark hypernucleus and multi-quark states beyond 5

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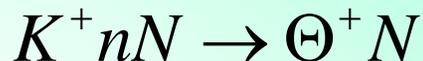
- Motivation
- Theoretical predictions for the  $\Theta^+$  hypernucleus
- What is the suitable reaction ?
  - momentum transfer for several candidate reactions
  - ‘magic momentum’ in one baryon knockout reaction
- Experimental setup
- Summary

# Motivation

- Another confirmation for the  $\Theta^+$  existence or at least existence of  $S=+1$  nucleus
- $\Theta$ -N interaction:  ~~$\Theta$ -N scattering~~  
only studied through  $\Theta$ -bound states  
→ feedback to  $\Theta^+$  properties and internal structure
- Medium modification of  $\Theta^+$   
very low  $M^*(\Theta)$  :  ~~$\Theta \rightarrow KN$~~ , stable for the strong decay!
- Pentaquarks in neutron star  
If  $U(\Theta^+) = -100$  MeV, 5% fraction of  $\Theta$  in the core of compact star at  $\rho = 4\rho_0$  → limit of  $M_{\text{nstar}}$  is reduced

# Need more reactivity in $K^+$ -Nucleus dynamics $\rightarrow$ more $\Theta^+$ in $K^+A$ ?

- $t\rho$  optical potential did not explain  $K$ - $A$  scattering and  $\sigma_R$  data at low energy in spite of weak  $K$ - $N$  interaction.
- if add density dependent term
 
$$t\rho \rightarrow t\rho(r) + B\bar{\rho}\rho(r)$$
 good fit is taken.
- assume this  $\Delta V_{\text{opt}}$  term is due to



process, the absorption cross section is  $\sim$ mb !

Gal, Friedman, PRL94,072301(2005)

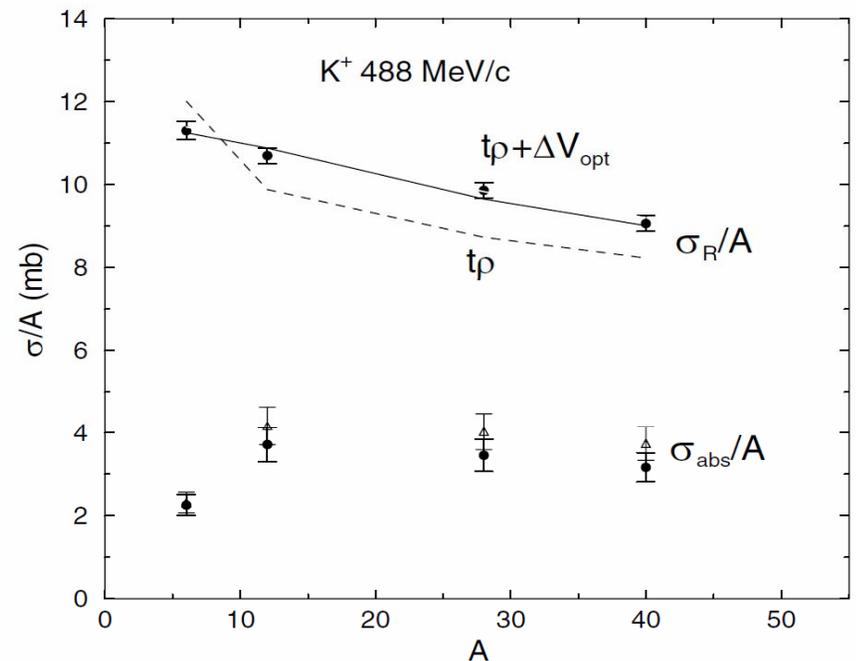


FIG. 1. Data and calculations for  $K^+$  reaction cross sections per nucleon ( $\sigma_R/A$ ) at  $p_{\text{lab}} = 488$  MeV/c are shown in the upper part. Calculated  $K^+$  absorption cross sections per nucleon ( $\sigma_{\text{abs}}/A$ ) are shown in the lower part; see text.

# Schematic model by Miller

Miller, PRC70,022202(2004)

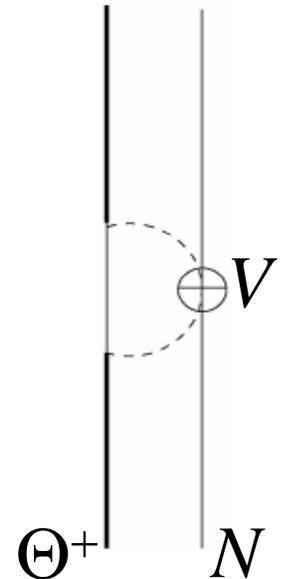
- $\Theta$  is treated as a nucleon vibration due to the coherent  $q\bar{s}$  excitation (like giant dipole resonance)

$q\bar{s}$  : pseudoscalar,  $L=1$  (positive parity of  $\Theta$ )

number of states:  $3(\text{color}) \times 3(L_z) \times 2(u\bar{s} \text{ or } d\bar{s}) = 18$

- determine the  $V$ (interaction between  $q\bar{s}$  and  $N$ ) and  $\mu$  (mass of  $q\bar{s}$ ) to reproduce  $M_\Theta$
- In  $\Theta N$  system, coherent cloud also interacts with another  $N$  via  $V$
- $\rightarrow$  Very large attractive  $\Theta N$  potential

$U(r) \sim -490 \text{ MeV}$  at  $\rho = \rho_0$  !



# Selfenergy of $\Theta^+$ associated with decay loops

H-C. Kim et al., J. Kor. Phys. Soc.46, 393(2005)  
Cabrera et al., PLB608, 231(2005)

- Selfenergy of  $\Theta$  in nuclei is evaluated with decay channels
- Only with KN channel  $\rightarrow$  too weak to bind  $\Theta$
- Add  $K\pi N$  channel

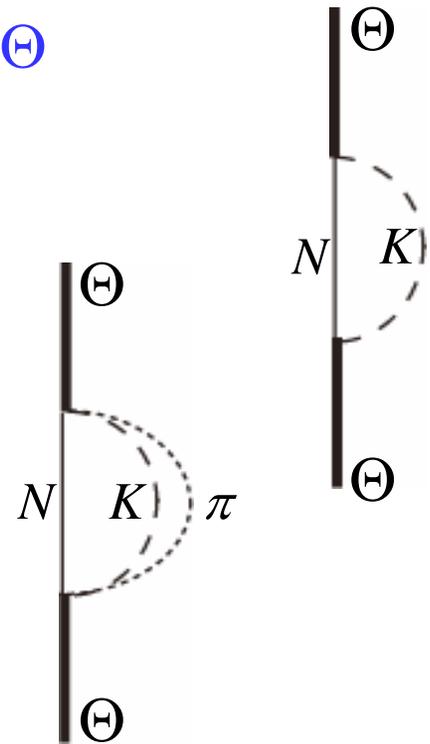
$\rightarrow$  strong attractive potential

Assume  $\Theta$  is  $\frac{1}{2}^+$ . SU(3) antidecouplet

Couplings are chosen to reproduce

$N^*(1710) \rightarrow N\pi\pi$  and SU(3) symmetry

- $U(r) = -60 \sim -120$  MeV, width:  
Pauli blocking and binding  $\rightarrow$  reduce  
 $K\pi N$  channel  $\rightarrow$  broaden, but not large



# Mean field approach

QMC model: Panda et al., PRC72,058201(2005)

Ryu et al., PRC72,045206

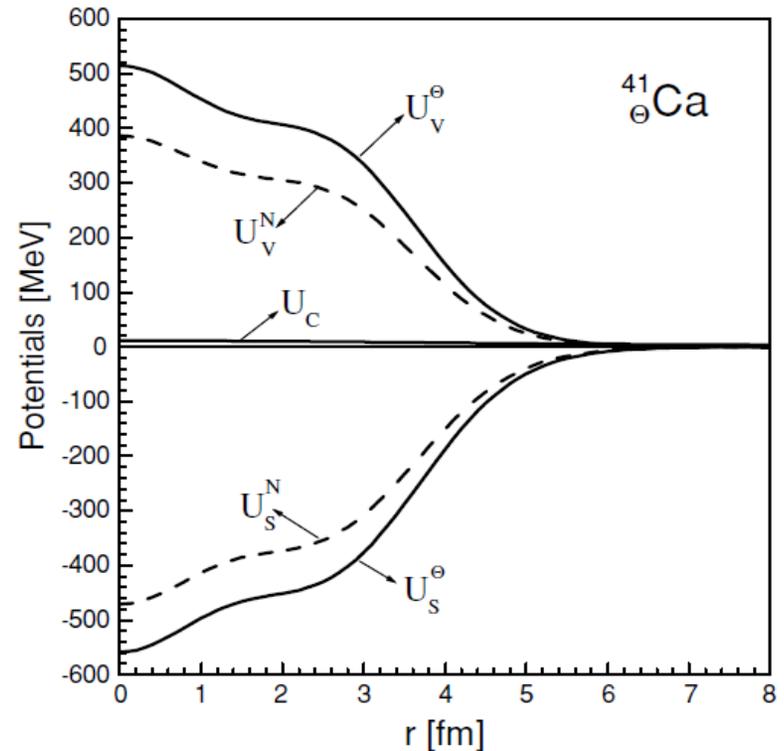
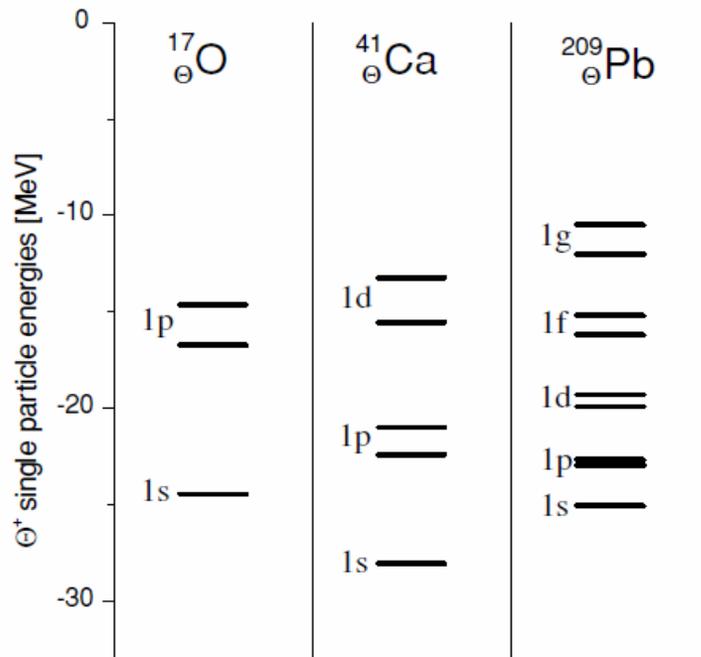
RMF model: Zhong et al., PRC71,015206; PRC72,065212

QMF model: Shen, Toki, PRC71,065208

- Baryons in nuclear medium interact through the scalar ( $\sigma$ ) and vector meson ( $\omega, \rho$ ) fields
- Coupling constants in nuclear sector ( $g_\sigma^N, g_\omega^N, g_\rho^N$ ) and  $m_\sigma$  are determined to produce nuclear saturation properties
- For  $\Theta$ , assume  $g_\sigma^\Theta = 4/3 g_\sigma^N$ ,  $g_\omega^\Theta = 4/3 g_\omega^N$ , ( $g_\rho^\Theta = 0$  if  $\Theta(I=0)$ ) because  $\sigma$ ,  $\omega$  and  $\rho$  couple only to  $u$  and  $d$  quarks  
(for  $\Lambda$ ,  $g_\sigma^\Lambda = 2/3 g_\sigma^N$ ,  $g_\omega^\Lambda = 2/3 g_\omega^N$ )
- $U = U_s + U_v \sim g_\sigma^\Theta \sigma_0 + g_\omega^\Theta \omega_0$

# Mean field approach

- RMF:  $U = -50 \sim -90 \text{ MeV}$  for the point-like  $\Theta$   
but  $-90 \text{ MeV} \rightarrow -37.5 \text{ MeV}$  for  $\Theta$  as a  $K\pi N$  bound state
- QMF:  $U = -50 \text{ MeV}$



# QCD sum rule of $\Theta^+$ in nuclear matter

Navarra et al., PLB606,335(2005)

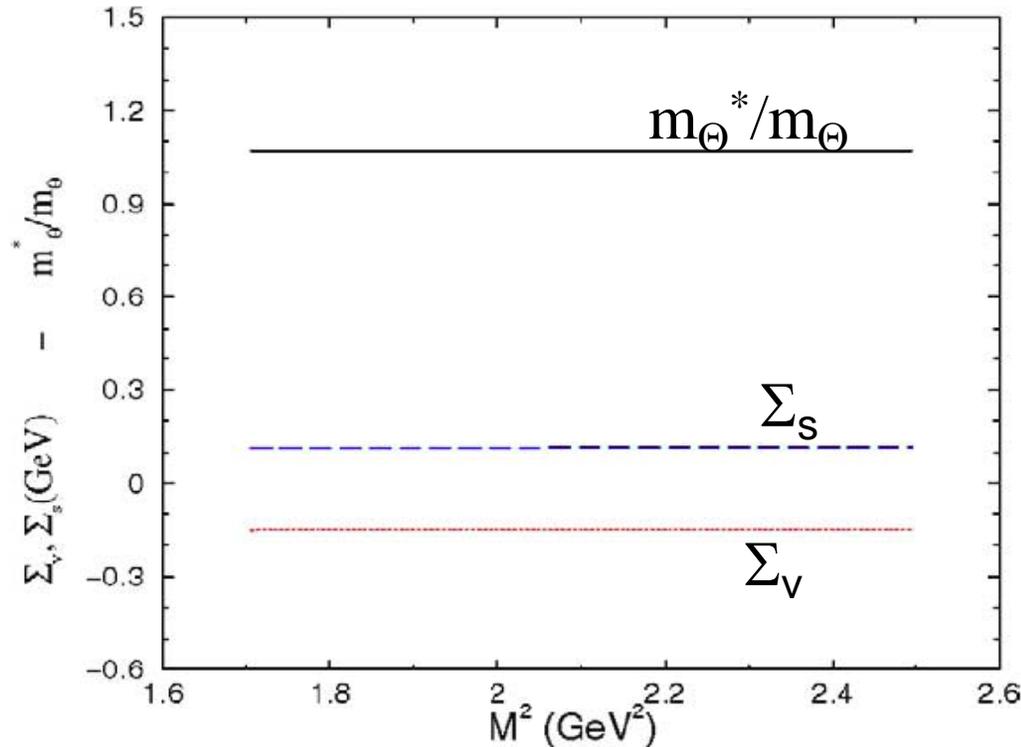


Fig. 2. The ratio  $m_{\Theta}^*/m_{\Theta}$  (solid line), the vector and scalar self-energies (dotted and dashed lines, respectively) as functions of the Borel parameter  $M^2$ , for  $y = 0.3$ .

- $\Sigma_S$ : positive and  $\Sigma_V$ : negative !
- But  $U = \Sigma_S + \Sigma_V$ : is still negative :  
 $U = -40 \sim -90$  MeV  
strongly depends on the value of the gluon condensate

# Summary of the theoretical predictions for $\Theta^+(1/2^+)$

- Miller's schematic model:  $U(\Theta^+) < -100$  MeV
- Hadronic SU(3) approach:  $U(\Theta^+) = -60 \sim -120$  MeV  
(selfenergy associated with  $KN$  and  $K\pi N$  decays )
- Mean field theory  
RMF model:  $U(\Theta^+) = -37.5 \sim -90$  MeV  
QMF model:  $U(\Theta^+) \sim -50$  MeV
- QCD sum rule:  $U(\Theta^+) = -40 \sim -90$  MeV

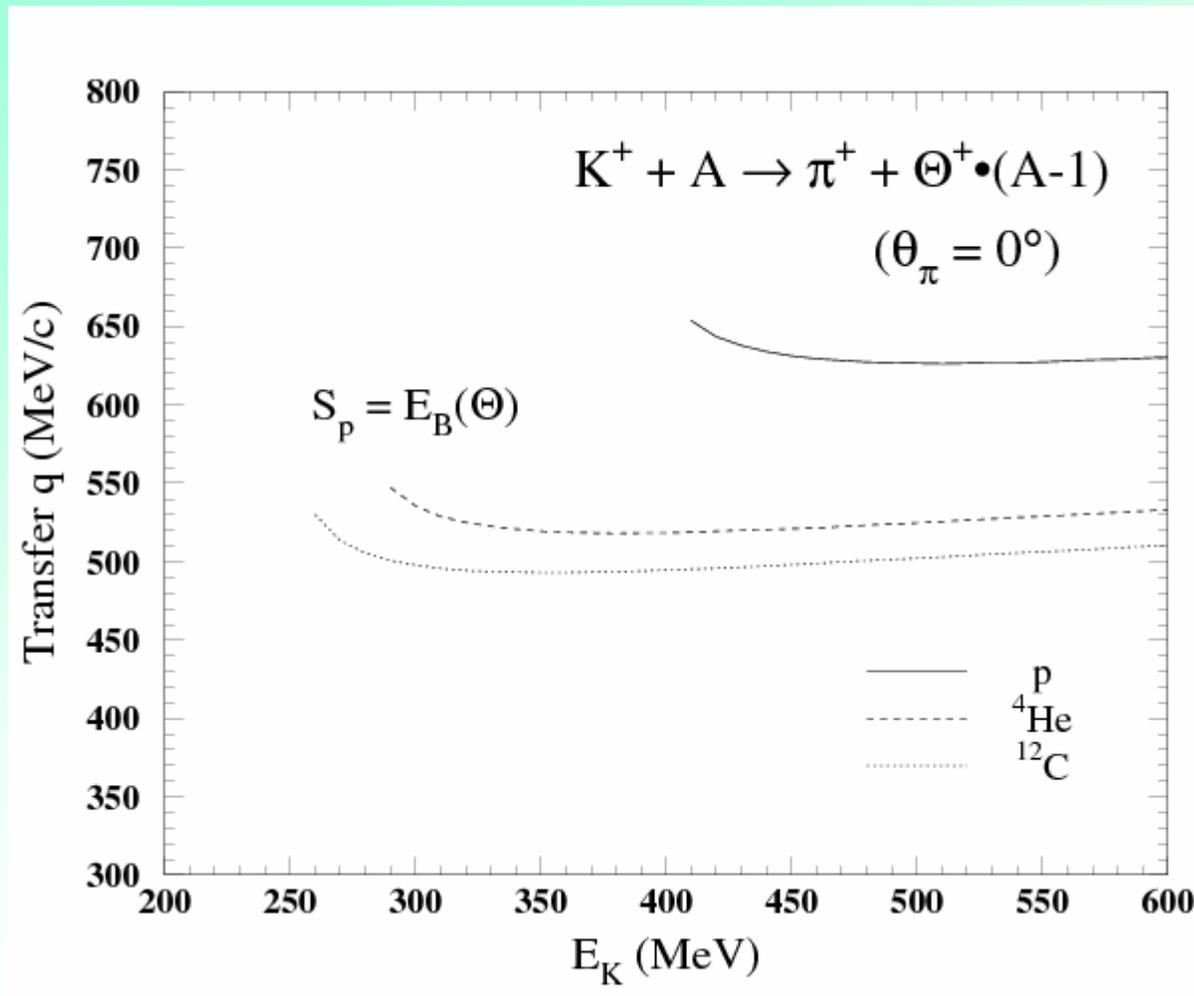
All give sufficiently large attractive potentials to bind  $\Theta^+$  in nucleus, but what is the bridge between different models ?

# What is the suitable reaction for producing $\Theta^+$ hypernucleus ?

- Elementary one-nucleon or two-nucleon process can produce  $\Theta^+$  with reasonable cross sections
- Two-body reaction process is preferable to the missing mass spectroscopy
- Momentum difference between the produced  $\Theta^+$  and the recoil nucleus should be small
  - small momentum transfer  $q$  in Lab system
- Small background (BG) process or some BG reduction methods should exist :
  - coincidence with backward decay products

# Momentum transfer in $(K^+, \pi^+)$ reaction

( $\Theta^+$  has still not been found in  $p(K^+, \pi^+)X$ )



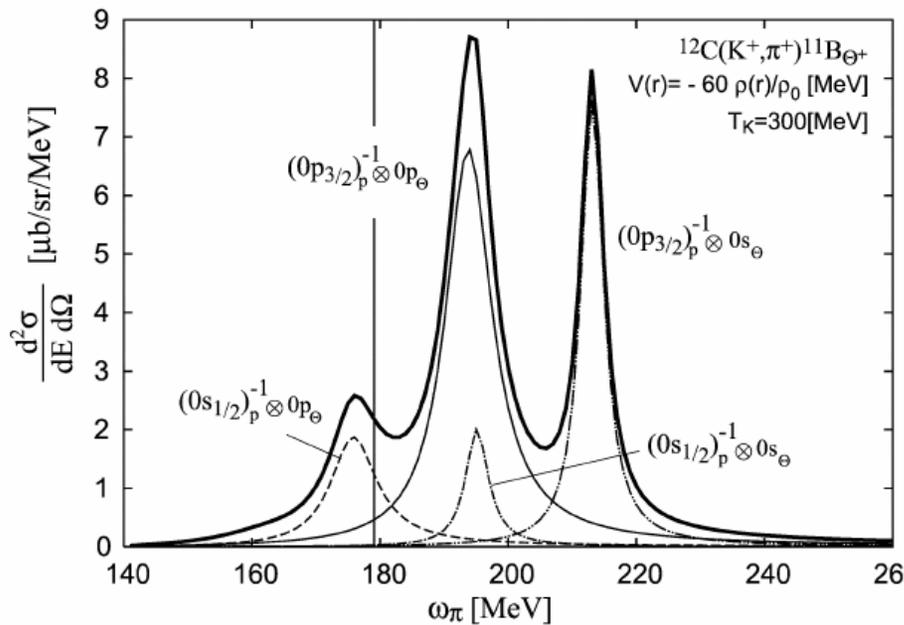
- not small  $q$
- but possible for  $\Theta^+$  bound nucleus

Use  
 $M(\Theta^+) = 1535$  MeV

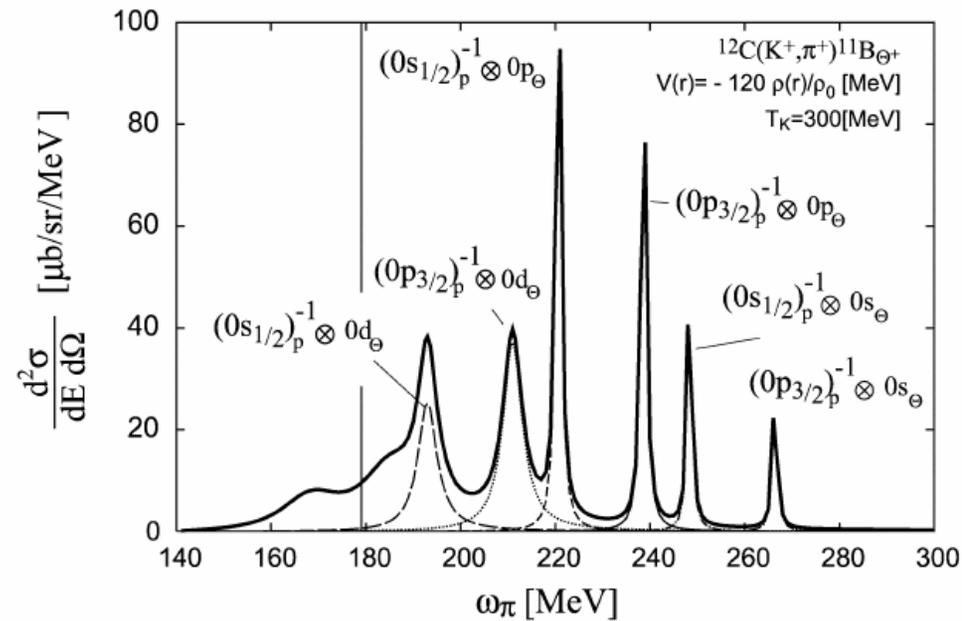
# Calculated spectra of $^{12}\text{C}(K^+, \pi^+)^{11}\text{B}_{\Theta}$ reaction

Nagahiro et al., PLB620,125(2005)

$V(r) = -60 \text{ MeV}$

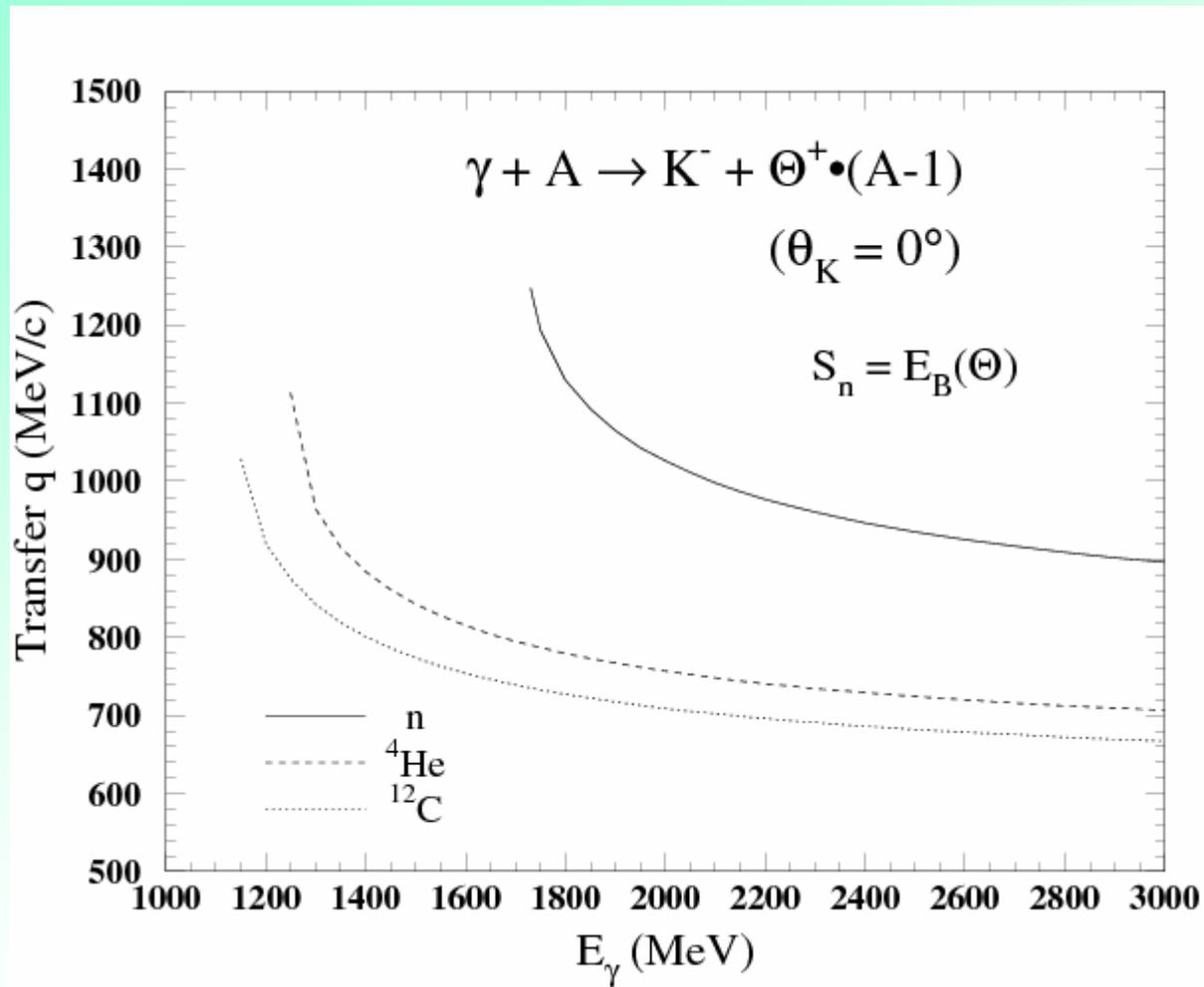


$V(r) = -120 \text{ MeV}$



# Momentum transfer in $(\gamma, K^+)$ reaction

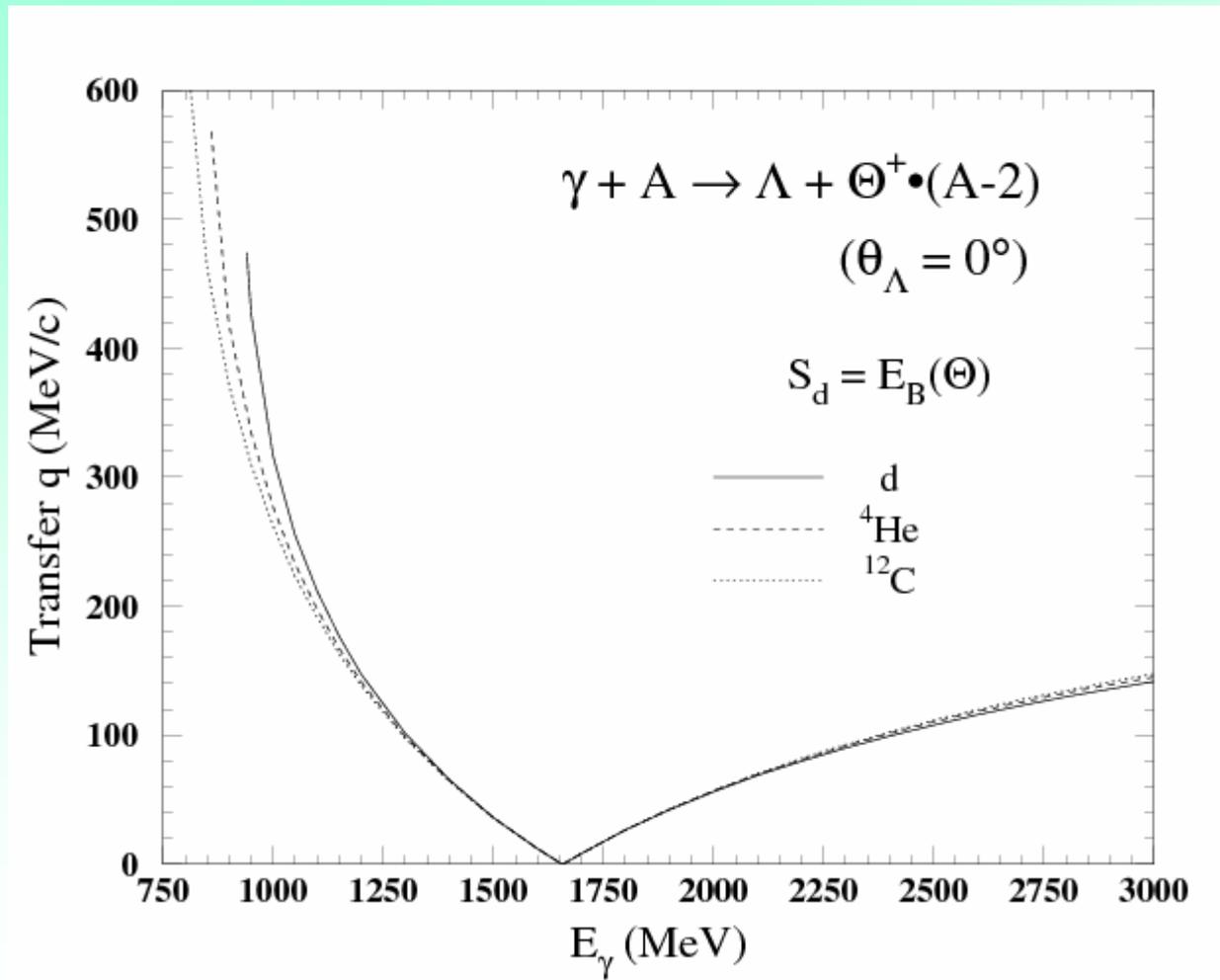
( $\Theta^+$  has been found in ' $n$ ' $(\gamma, K^+)X$  at LEPS)



- large  $q$
- not good for  $\Theta^+$  bound nucleus

# Momentum transfer in $(\gamma, \Lambda(1116))$ reaction

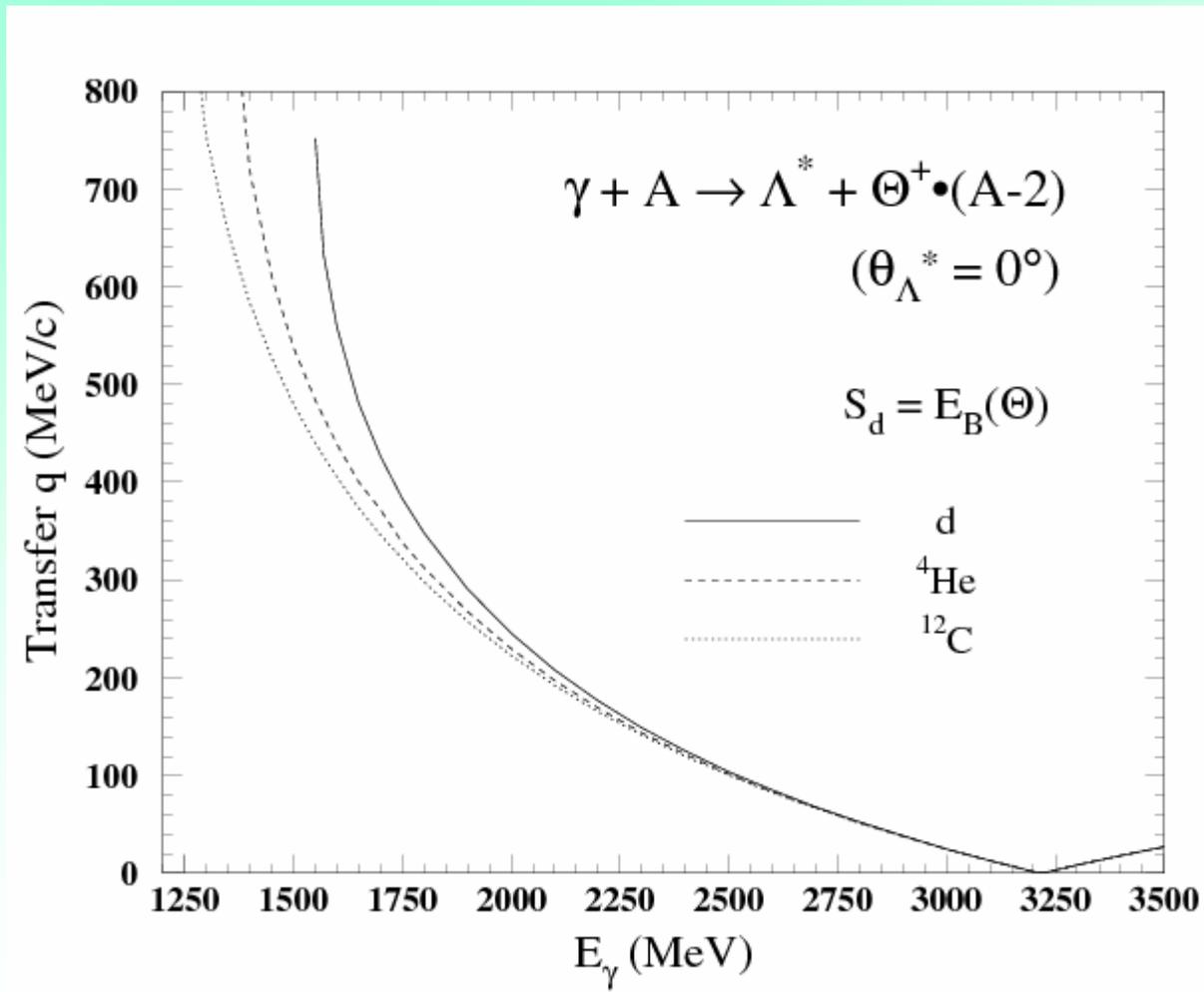
$(\Theta^+$  has still not been found in  $d(\gamma, \Lambda)X$  ( $\Lambda \rightarrow p\pi^-$ ))



- very small  $q$
- magic momentum around 1670 MeV

# Momentum transfer in $(\gamma, \Lambda^*(1520))$ reaction

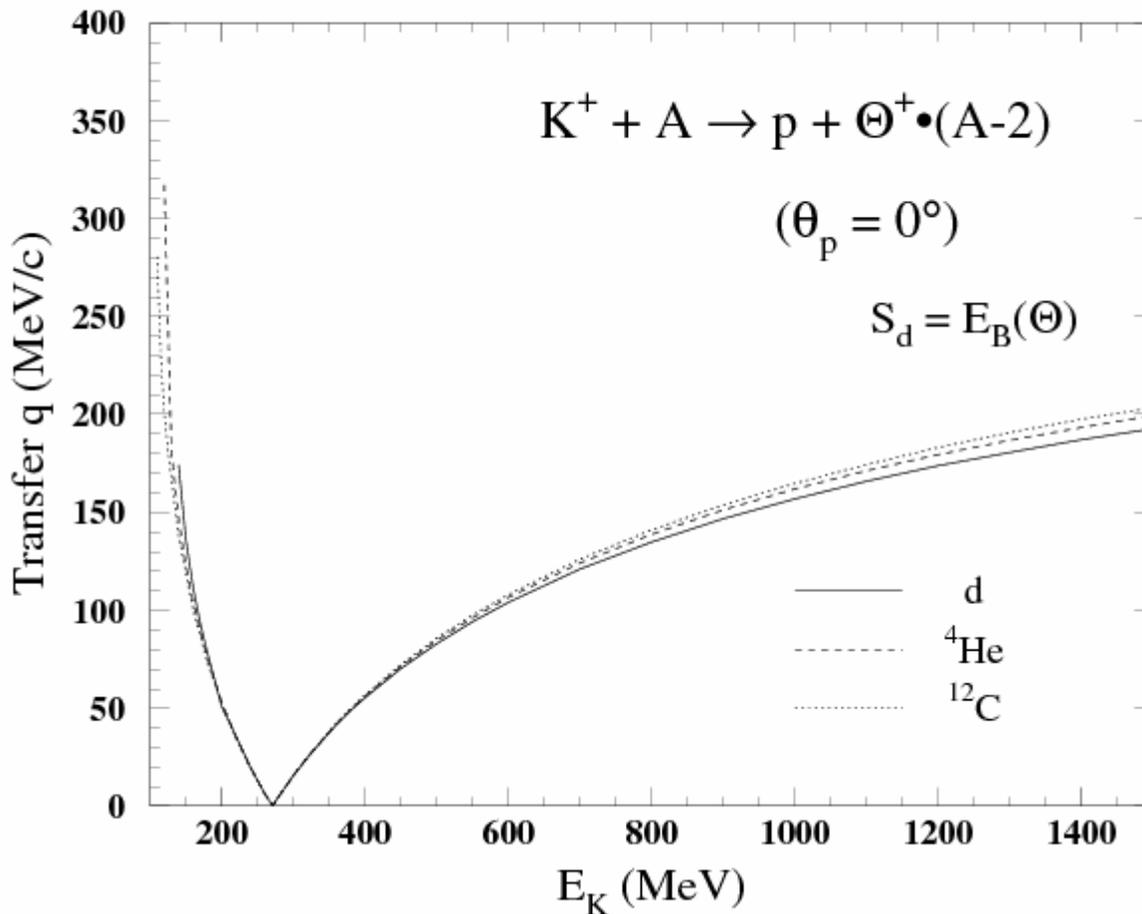
( $\Theta^+$  has been found in  $d(\gamma, \Lambda^*)X$  at LEPS ( $\Lambda^* \rightarrow pK^-$ ))



- small  $q$ , especially, above 2 GeV
- magic momentum around 3220 MeV (higher than LEPS energy)

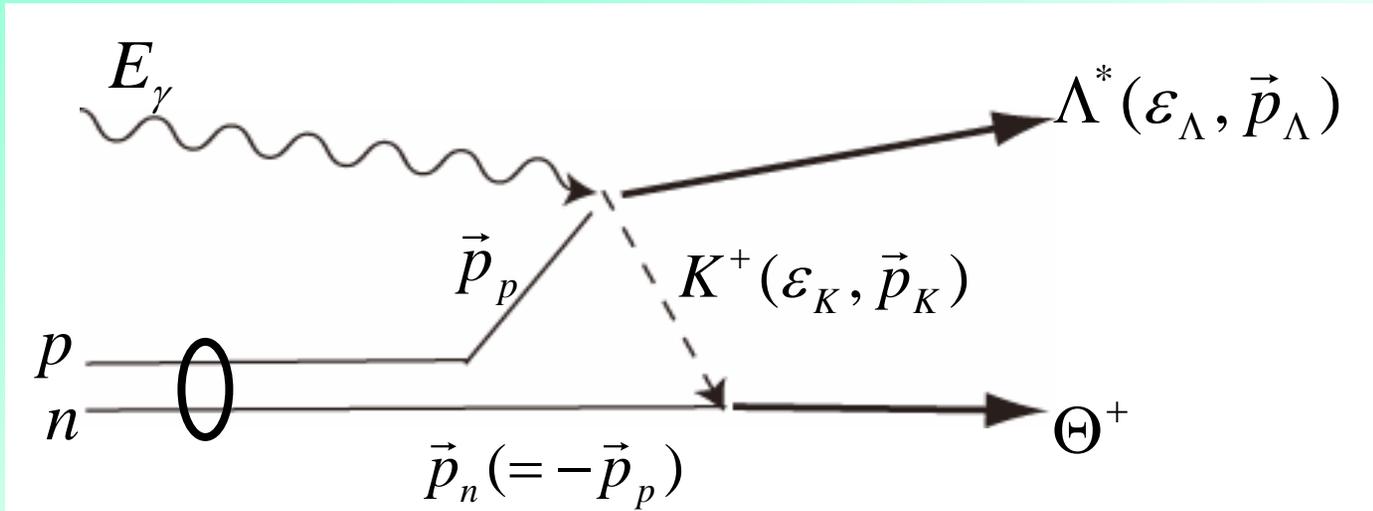
# Momentum transfer in $(K^+, p)$ reaction

$(\Theta^+$  has not been searched in  $d(K^+, p)X$ )



- small  $q$ , even at 1400 MeV (1.8 GeV/c)
- magic momentum around 270 MeV
- should be done at J-Parc !

# Comment on $\gamma d \rightarrow \Theta^+ \Lambda^* (1520)$

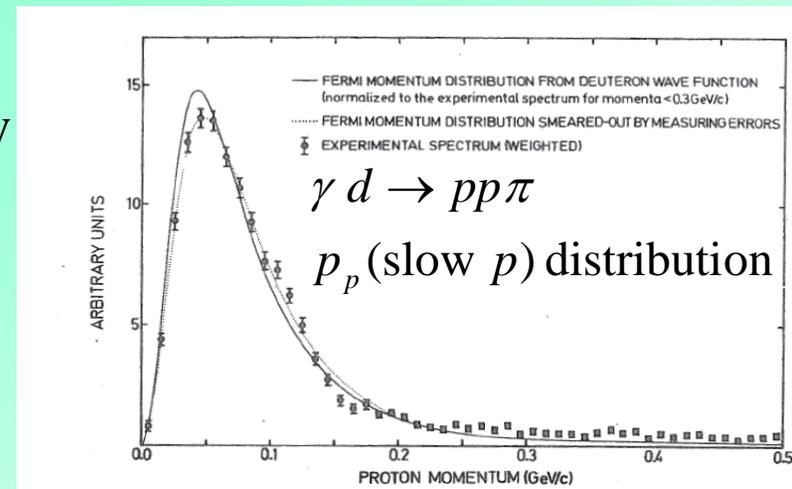


if  $K^+$  : on shell ( $m_K^2 = \epsilon_K^2 - \vec{p}_K^2$ ) and

$\Theta$  is produced only at the formation energy

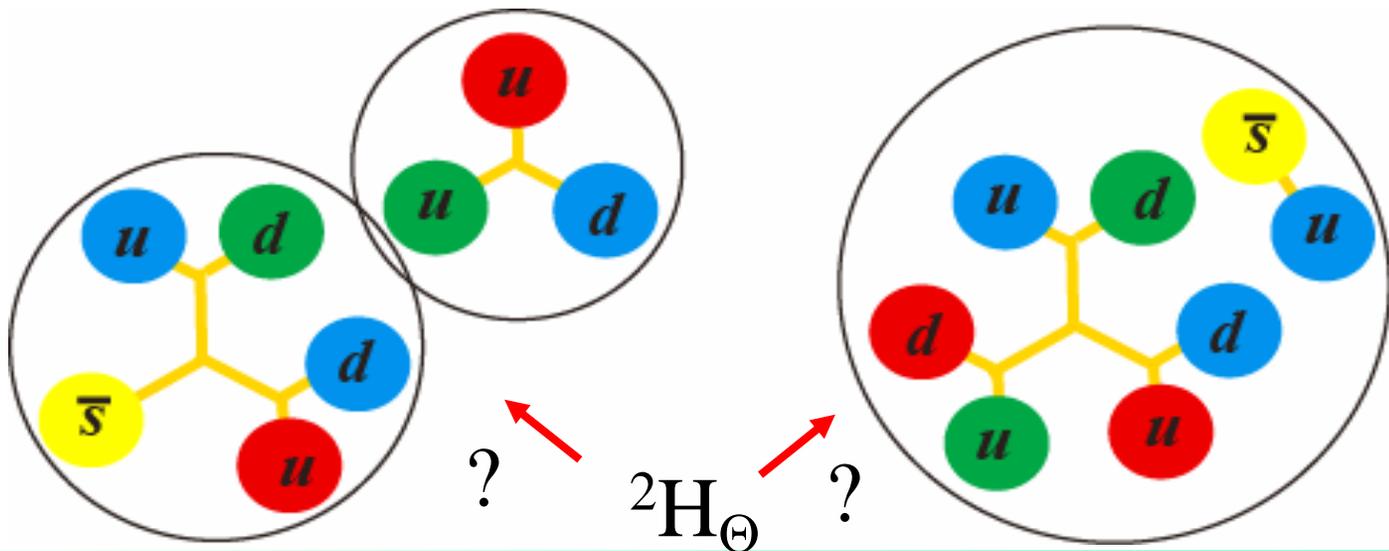
$$((\epsilon_n + \epsilon_K)^2 - (\vec{p}_n + \vec{p}_K)^2 = M_\Theta^2)$$

$\Rightarrow$  calculate  $p_n$  dependence of  
the  $\Theta^+$  production rate



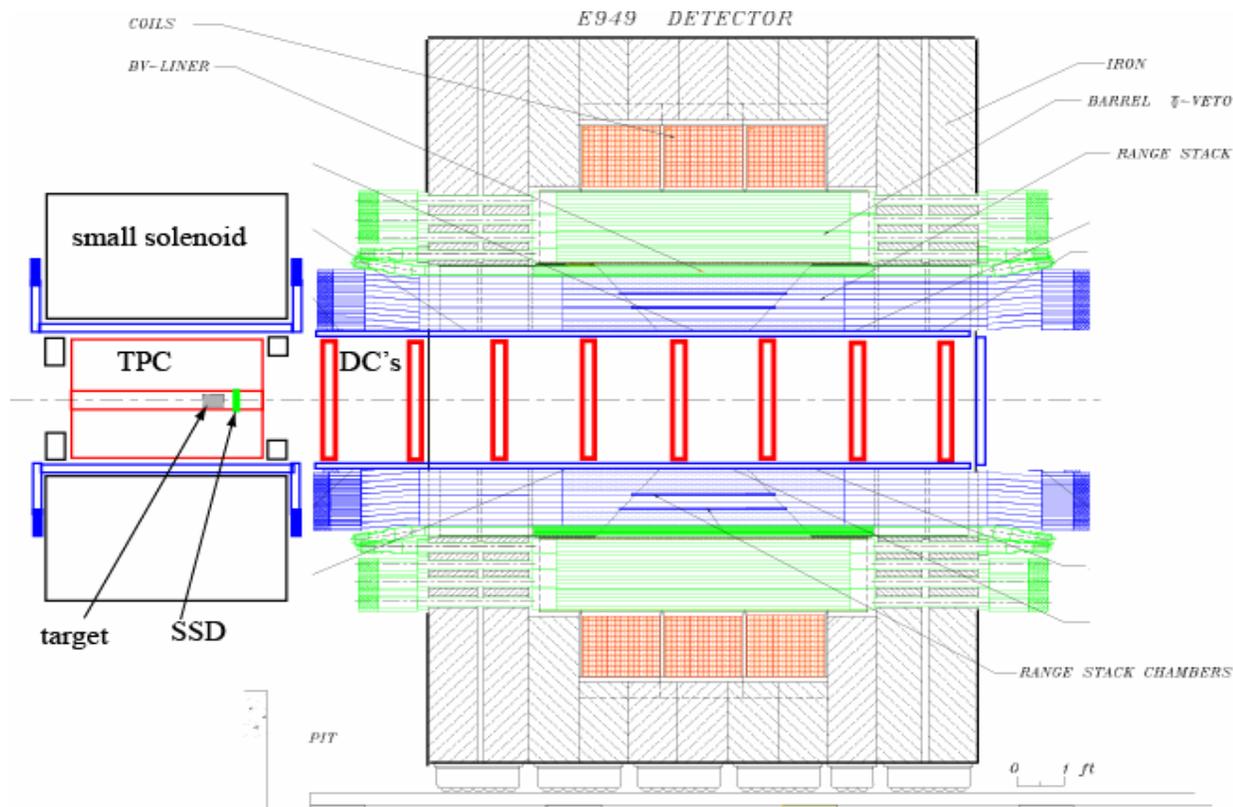
# Multi-quark state beyond 5 -- 8 quark dibaryon candidate --

- If a  $\Theta^+ N$  bound state is found, it could be a candidate of exotic 8 quark state
- e.g.)  ${}^3\text{He}(\gamma, \Lambda^*) {}^2\text{H}_{\Theta}$  or  ${}^3\text{He}(\gamma, \Sigma^+) {}^2[n\Theta]$



# Detector setup

- Good missing mass resolution and acceptance for forward going  $\Lambda(\rightarrow p\pi^-)$ ,  $\Lambda^*(\rightarrow pK^-)$  [if possible,  $\Sigma^+(\rightarrow p\pi^0, n\pi^+)$ ]
- Coincidence measurement with decay products, especially, at backward angles, which have relatively low momentum



# Summary

- Pentaquark hypernucleus is interesting and important for another confirmation of  $\Theta^+$  and the study of the  $\Theta$ N interaction.
- Several theoretical model calculations predict the existence of bound  $\Theta^+$  states, although the mutual relations between different models are not clear.
- Momentum transfer for the  $\Theta^+$  production process is small in one baryon knockout reactions at forward angles like  $(\gamma, \Lambda)$ ,  $(\gamma, \Lambda^*)$ , and  $(K^+, p)$ .
- Suggest an idea of adding a small solenoid to detect the backward decay products in addition to the E949 detector. (any detailed study has not been done yet.)